

# Sin

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## Notations

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### Traditional name

Sine

### Traditional notation

$\sin(z)$

### Mathematica StandardForm notation

`Sin[z]`

## Primary definition

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$$\sin(z) = \frac{e^{iz} - e^{-iz}}{2i}$$

## Specific values

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### Specialized values

$$\sin(\pi m) = 0 \quad ; \quad m \in \mathbb{Z}$$

$$\sin\left(\pi\left(\frac{1}{2} + m\right)\right) = (-1)^m \quad ; \quad m \in \mathbb{Z}$$

### Values at fixed points

$$\sin(0) = 0$$

$$\sin\left(\frac{\pi}{12}\right) = \frac{\sqrt{3} - 1}{2\sqrt{2}}$$

$$\sin\left(\frac{\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_3^{-1}$$

01.06.03.0006.01

$$\sin\left(\frac{\pi}{10}\right) = \frac{\sqrt{5} - 1}{4}$$

01.06.03.0007.01

$$\sin\left(\frac{\pi}{9}\right) = -\frac{i\left((-1+i\sqrt{3})^{4/3} - (-1-i\sqrt{3})^{4/3}\right)}{4\sqrt[3]{2}}$$

01.06.03.0008.01

$$\sin\left(\frac{\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_4^{-1}$$

01.06.03.0009.01

$$\sin\left(\frac{\pi}{9}\right) = -\frac{1}{2}(-1)^{7/18}(-1 + (-1)^{2/9})$$

01.06.03.0010.01

$$\sin\left(\frac{\pi}{8}\right) = \frac{\sqrt{2 - \sqrt{2}}}{2}$$

01.06.03.0011.01

$$\sin\left(\frac{\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_3^{-1}$$

01.06.03.0012.01

$$\sin\left(\frac{\pi}{8}\right) = -\frac{1}{2}(-1)^{3/8}(-1 + \sqrt[4]{-1})$$

01.06.03.0013.01

$$\sin\left(\frac{\pi}{7}\right) = -\frac{1}{24}i \left( 2(i + \sqrt{3})i \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + \frac{2\sqrt{7}(i + \sqrt{3})}{\sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}}} + \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} (2 + 2i\sqrt{3}) - 4\sqrt{7}i - \frac{2\sqrt{7}(-i + \sqrt{3})}{\sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}}} \right)$$

01.06.03.0014.01

$$\sin\left(\frac{\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_4^{-1}$$

01.06.03.0015.01

$$\sin\left(\frac{\pi}{7}\right) = -\frac{1}{2}(-1)^{5/14}(-1 + (-1)^{2/7})$$

01.06.03.0016.01

$$\sin\left(\frac{\pi}{6}\right) = \frac{1}{2}$$

01.06.03.0017.01

$$\sin\left(\frac{\pi}{5}\right) = \frac{1}{2} \sqrt{\frac{5 - \sqrt{5}}{2}}$$

01.06.03.0018.01

$$\sin\left(\frac{\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_3^{-1}$$

01.06.03.0019.01

$$\sin\left(\frac{2\pi}{9}\right) = \frac{i\left(\sqrt[3]{-1 - i\sqrt{3}} - \sqrt[3]{-1 + i\sqrt{3}}\right)}{2\sqrt[3]{2}}$$

01.06.03.0020.01

$$\sin\left(\frac{2\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_5^{-1}$$

01.06.03.0021.01

$$\sin\left(\frac{2\pi}{9}\right) = -\frac{1}{2} (-1)^{5/18} (-1 + (-1)^{4/9})$$

01.06.03.0022.01

$$\sin\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2}$$

01.06.03.0023.01

$$\begin{aligned} \sin\left(\frac{2\pi}{7}\right) = & \frac{1}{12 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}} \left( -2\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} - 2i\sqrt{21} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + \right. \\ & 4\sqrt{7} \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} + 2 \cdot 2^{2/3} \cdot 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} + \sqrt{3} \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} + \\ & \left. 2(14 + i\sqrt{7} + 3\sqrt{21})^{2/3} \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} + i \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} \right) \end{aligned}$$

01.06.03.0024.01

$$\sin\left(\frac{2\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_5^{-1}$$

01.06.03.0025.01

$$\sin\left(\frac{2\pi}{7}\right) = -\frac{1}{2} (-1)^{3/14} (-1 + (-1)^{4/7})$$

01.06.03.0026.01

$$\sin\left(\frac{3\pi}{10}\right) = \frac{\sqrt{5} + 1}{4}$$

01.06.03.0027.01

$$\sin\left(\frac{\pi}{3}\right) = \frac{\sqrt{3}}{2}$$

01.06.03.0028.01

$$\sin\left(\frac{3\pi}{8}\right) = \frac{\sqrt{2 + \sqrt{2}}}{2}$$

01.06.03.0029.01

$$\sin\left(\frac{3\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_4^{-1}$$

01.06.03.0030.01

$$\sin\left(\frac{3\pi}{8}\right) = -\frac{1}{2} \sqrt[8]{-1} (-1 + (-1)^{3/4})$$

01.06.03.0031.01

$$\sin\left(\frac{2\pi}{5}\right) = \frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2}}$$

01.06.03.0032.01

$$\sin\left(\frac{2\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_4^{-1}$$

01.06.03.0033.01

$$\sin\left(\frac{5\pi}{12}\right) = \frac{1 + \sqrt{3}}{2\sqrt{2}}$$

01.06.03.0034.01

$$\sin\left(\frac{5\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_4^{-1}$$

01.06.03.0035.01

$$\begin{aligned} \sin\left(\frac{3\pi}{7}\right) = & \frac{1}{12 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}} \left( 4\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + 2 \cdot 2^{2/3} \cdot 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} - \right. \\ & 2i(14 - i\sqrt{7} - 3\sqrt{21})^{2/3} \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} + \sqrt{3} (14 + i\sqrt{7} + 3\sqrt{21})^{2/3} \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} - \\ & \left. i \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} (14 + i\sqrt{7} + 3\sqrt{21})^{2/3} + 2\sqrt{7} \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} (i + \sqrt{3}) i \right) \end{aligned}$$

01.06.03.0036.01

$$\sin\left(\frac{3\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_6^{-1}$$

01.06.03.0037.01

$$\sin\left(\frac{3\pi}{7}\right) = -\frac{1}{2} \sqrt[14]{-1} (-1 + (-1)^{6/7})$$

01.06.03.0038.01

$$\sin\left(\frac{4\pi}{9}\right) = \frac{(-i + \sqrt{3}) \sqrt[3]{-1 + i\sqrt{3}} + (i + \sqrt{3}) \sqrt[3]{-1 - i\sqrt{3}}}{4 \sqrt[3]{2}}$$

01.06.03.0039.01

$$\sin\left(\frac{4\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_6^{-1}$$

01.06.03.0040.01

$$\sin\left(\frac{4\pi}{9}\right) = -\frac{1}{2} \sqrt[18]{-1} (-1 + (-1)^{8/9})$$

01.06.03.0041.01

$$\sin\left(\frac{\pi}{2}\right) = 1$$

01.06.03.0042.01

$$\sin\left(\frac{5\pi}{9}\right) = \frac{(-i + \sqrt{3}) \sqrt[3]{-1 + i\sqrt{3}} + (i + \sqrt{3}) \sqrt[3]{-1 - i\sqrt{3}}}{4 \sqrt[3]{2}}$$

01.06.03.0043.01

$$\sin\left(\frac{5\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_6^{-1}$$

01.06.03.0044.01

$$\sin\left(\frac{5\pi}{9}\right) = -\frac{1}{2} (-1)^{17/18} (1 + \sqrt[9]{-1})$$

01.06.03.0045.01

$$\begin{aligned} \sin\left(\frac{4\pi}{7}\right) = & \frac{1}{12 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}} \left( 4\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + 2 \cdot 2^{2/3} \cdot 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} - \right. \\ & 2i(14 - i\sqrt{7} - 3\sqrt{21})^{2/3} \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} + \sqrt{3} (14 + i\sqrt{7} + 3\sqrt{21})^{2/3} \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} - \\ & \left. i \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} (14 + i\sqrt{7} + 3\sqrt{21})^{2/3} + 2\sqrt{7} \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} (i + \sqrt{3}) i \right) \end{aligned}$$

01.06.03.0046.01

$$\sin\left(\frac{4\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_6^{-1}$$

01.06.03.0047.01

$$\sin\left(\frac{4\pi}{7}\right) = -\frac{1}{2} (-1)^{13/14} (1 + \sqrt[7]{-1})$$

01.06.03.0048.01

$$\sin\left(\frac{7\pi}{12}\right) = \frac{1 + \sqrt{3}}{2\sqrt{2}}$$

01.06.03.0049.01

$$\sin\left(\frac{7\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_4^{-1}$$

01.06.03.0050.01

$$\sin\left(\frac{3\pi}{5}\right) = \frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2}}$$

01.06.03.0051.01

$$\sin\left(\frac{3\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_4^{-1}$$

01.06.03.0052.01

$$\sin\left(\frac{5\pi}{8}\right) = \frac{\sqrt{2 + \sqrt{2}}}{2}$$

01.06.03.0053.01

$$\sin\left(\frac{5\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_4^{-1}$$

01.06.03.0054.01

$$\sin\left(\frac{5\pi}{8}\right) = -\frac{1}{2} (-1)^{7/8} (1 + \sqrt[4]{-1})$$

01.06.03.0055.01

$$\sin\left(\frac{2\pi}{3}\right) = \frac{\sqrt{3}}{2}$$

01.06.03.0056.01

$$\sin\left(\frac{7\pi}{10}\right) = \frac{\sqrt{5} + 1}{4}$$

01.06.03.0057.01

$$\sin\left(\frac{5\pi}{7}\right) = \frac{1}{12 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}} \left( -2\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} - 2i\sqrt{21} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + \right. \\ \left. 4\sqrt{7} \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} + 2 \cdot 2^{2/3} \cdot 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} + \sqrt{3} \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} + \right. \\ \left. 2(14 + i\sqrt{7} + 3\sqrt{21})^{2/3} \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} i + \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} i \right)$$

01.06.03.0058.01

$$\sin\left(\frac{5\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_5^{-1}$$

01.06.03.0059.01

$$\sin\left(\frac{5\pi}{7}\right) = -\frac{1}{2} (-1)^{11/14} (1 + (-1)^{3/7})$$

01.06.03.0060.01

$$\sin\left(\frac{3\pi}{4}\right) = \frac{\sqrt{2}}{2}$$

01.06.03.0061.01

$$\sin\left(\frac{7\pi}{9}\right) = \frac{i\left(\sqrt[3]{-1-i\sqrt{3}} - \sqrt[3]{-1+i\sqrt{3}}\right)}{2\sqrt[3]{2}}$$

01.06.03.0062.01

$$\sin\left(\frac{7\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_5^{-1}$$

01.06.03.0063.01

$$\sin\left(\frac{7\pi}{9}\right) = -\frac{1}{2}(-1)^{13/18}(1 + (-1)^{5/9})$$

01.06.03.0064.01

$$\sin\left(\frac{4\pi}{5}\right) = \frac{1}{2}\sqrt{\frac{5-\sqrt{5}}{2}}$$

01.06.03.0065.01

$$\sin\left(\frac{4\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_3^{-1}$$

01.06.03.0066.01

$$\sin\left(\frac{5\pi}{6}\right) = \frac{1}{2}$$

01.06.03.0067.01

$$\sin\left(\frac{6\pi}{7}\right) = -\frac{1}{24}i\left(2(i+\sqrt{3})i\sqrt[3]{7+\frac{i\sqrt{7}}{2}+\frac{3\sqrt{21}}{2}} + \frac{2\sqrt{7}(i+\sqrt{3})}{\sqrt[3]{7-\frac{i\sqrt{7}}{2}-\frac{3\sqrt{21}}{2}}} + \sqrt[3]{7-\frac{i\sqrt{7}}{2}-\frac{3\sqrt{21}}{2}}(2+2i\sqrt{3}) - 4\sqrt{7}i - \frac{2\sqrt{7}(-i+\sqrt{3})}{\sqrt[3]{7+\frac{i\sqrt{7}}{2}+\frac{3\sqrt{21}}{2}}}\right)$$

01.06.03.0068.01

$$\sin\left(\frac{6\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_4^{-1}$$

01.06.03.0069.01

$$\sin\left(\frac{6\pi}{7}\right) = -\frac{1}{2}(-1)^{9/14}(1 + (-1)^{5/7})$$

01.06.03.0070.01

$$\sin\left(\frac{7\pi}{8}\right) = \frac{\sqrt{2-\sqrt{2}}}{2}$$

01.06.03.0071.01

$$\sin\left(\frac{7\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_3^{-1}$$

01.06.03.0072.01

$$\sin\left(\frac{7\pi}{8}\right) = -\frac{1}{2}(-1)^{5/8}(1+(-1)^{3/4})$$

01.06.03.0073.01

$$\sin\left(\frac{8\pi}{9}\right) = -\frac{i\left((-1+i\sqrt{3})^{4/3}-(-1-i\sqrt{3})^{4/3}\right)}{4\sqrt[3]{2}}$$

01.06.03.0074.01

$$\sin\left(\frac{8\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_4^{-1}$$

01.06.03.0075.01

$$\sin\left(\frac{8\pi}{9}\right) = -\frac{1}{2}(-1)^{11/18}(1+(-1)^{7/9})$$

01.06.03.0076.01

$$\sin\left(\frac{9\pi}{10}\right) = \frac{\sqrt{5}-1}{4}$$

01.06.03.0077.01

$$\sin\left(\frac{11\pi}{12}\right) = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

01.06.03.0078.01

$$\sin\left(\frac{11\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_3^{-1}$$

01.06.03.0079.01

$$\sin(\pi) = 0$$

01.06.03.0080.01

$$\sin\left(\frac{13\pi}{12}\right) = -\frac{\sqrt{3}-1}{2\sqrt{2}}$$

01.06.03.0081.01

$$\sin\left(\frac{13\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_2^{-1}$$

01.06.03.0082.01

$$\sin\left(\frac{11\pi}{10}\right) = -\frac{\sqrt{5}-1}{4}$$

01.06.03.0083.01

$$\sin\left(\frac{10\pi}{9}\right) = -\frac{i\left((-1-i\sqrt{3})^{4/3}-(-1+i\sqrt{3})^{4/3}\right)}{4\sqrt[3]{2}}$$

01.06.03.0084.01

$$\sin\left(\frac{10\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_3^{-1}$$



01.06.03.0085.01

$$\sin\left(\frac{10\pi}{9}\right) = \frac{1}{2}(-1)^{11/18} (1 + (-1)^{7/9})$$

01.06.03.0086.01

$$\sin\left(\frac{9\pi}{8}\right) = -\frac{1}{2}\sqrt{2-\sqrt{2}}$$

01.06.03.0087.01

$$\sin\left(\frac{9\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_2^{-1}$$

01.06.03.0088.01

$$\sin\left(\frac{9\pi}{8}\right) = \frac{1}{2}(-1)^{5/8} (1 + (-1)^{3/4})$$

01.06.03.0089.01

$$\sin\left(\frac{8\pi}{7}\right) = -\frac{1}{24}i \left( 2(1-i\sqrt{3}) \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} - \right. \\ \left. (2+2i\sqrt{3}) \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} + \frac{2\sqrt{7}(-i+\sqrt{3})}{\sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}}} + 4\sqrt{7}i - \frac{2\sqrt{7}(i+\sqrt{3})}{\sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}}} \right)$$

01.06.03.0090.01

$$\sin\left(\frac{8\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_3^{-1}$$

01.06.03.0091.01

$$\sin\left(\frac{8\pi}{7}\right) = \frac{1}{2}(-1)^{9/14} (1 + (-1)^{5/7})$$

01.06.03.0092.01

$$\sin\left(\frac{7\pi}{6}\right) = -\frac{1}{2}$$

01.06.03.0093.01

$$\sin\left(\frac{6\pi}{5}\right) = -\frac{1}{2}\sqrt{\frac{5-\sqrt{5}}{2}}$$

01.06.03.0094.01

$$\sin\left(\frac{6\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_2^{-1}$$

01.06.03.0095.01

$$\sin\left(\frac{11\pi}{9}\right) = -\frac{i \left( \sqrt[3]{-1-i\sqrt{3}} - \sqrt[3]{-1+i\sqrt{3}} \right)}{2\sqrt[3]{2}}$$

01.06.03.0096.01

$$\sin\left(\frac{11\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_2^{-1}$$

01.06.03.0097.01

$$\sin\left(\frac{11\pi}{9}\right) = \frac{1}{2} (-1)^{13/18} (1 + (-1)^{5/9})$$

01.06.03.0098.01

$$\sin\left(\frac{5\pi}{4}\right) = -\frac{\sqrt{2}}{2}$$

01.06.03.0099.01

$$\begin{aligned} \sin\left(\frac{9\pi}{7}\right) = & -\left(-2\sqrt{7}\sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} - 2i\sqrt{21}\sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + 4\sqrt{7}\sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} + \right. \\ & 2 \cdot 2^{2/3} 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} + \sqrt{3} \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} + 2(14 + i\sqrt{7} + 3\sqrt{21})^{2/3} \\ & \left. \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} i + \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} i\right) / \left(12 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}\right) \end{aligned}$$

01.06.03.0100.01

$$\sin\left(\frac{9\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_2^{-1}$$

01.06.03.0101.01

$$\sin\left(\frac{9\pi}{7}\right) = \frac{1}{2} (-1)^{11/14} (1 + (-1)^{3/7})$$

01.06.03.0102.01

$$\sin\left(\frac{13\pi}{10}\right) = -\frac{\sqrt{5} + 1}{4}$$

01.06.03.0103.01

$$\sin\left(\frac{4\pi}{3}\right) = -\frac{\sqrt{3}}{2}$$

01.06.03.0104.01

$$\sin\left(\frac{11\pi}{8}\right) = -\frac{\sqrt{2 + \sqrt{2}}}{2}$$

01.06.03.0105.01

$$\sin\left(\frac{11\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_1^{-1}$$

01.06.03.0106.01

$$\sin\left(\frac{11\pi}{8}\right) = \frac{1}{2} (-1)^{7/8} (1 + \sqrt[4]{-1})$$

01.06.03.0107.01

$$\sin\left(\frac{7\pi}{5}\right) = -\frac{1}{2} \sqrt{\frac{5 + \sqrt{5}}{2}}$$

01.06.03.0108.01

$$\sin\left(\frac{7\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_1^{-1}$$

01.06.03.0109.01

$$\sin\left(\frac{17\pi}{12}\right) = -\frac{\sqrt{3} + 1}{2\sqrt{2}}$$

01.06.03.0110.01

$$\sin\left(\frac{17\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_1^{-1}$$

01.06.03.0111.01

$$\sin\left(\frac{10\pi}{7}\right) =$$

$$\frac{1}{6 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}} \left( (\sqrt{7} - i\sqrt{21}) \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} - 2^{2/3} 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} + \frac{1}{2} \left( i \sqrt[3]{14 - 42i\sqrt{3}} \right. \right. \\ \left. \left. \left( (1 + i\sqrt{3}) \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} + 2 \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} \right) - 4\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} \right) \right)$$

01.06.03.0112.01

$$\sin\left(\frac{10\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_1^{-1}$$

01.06.03.0113.01

$$\sin\left(\frac{10\pi}{7}\right) = \frac{1}{2} (-1)^{13/14} \left(1 + \sqrt[7]{-1}\right)$$

01.06.03.0114.01

$$\sin\left(\frac{13\pi}{9}\right) = -\frac{(-i + \sqrt{3}) \sqrt[3]{-1 + i\sqrt{3}} + (i + \sqrt{3}) \sqrt[3]{-1 - i\sqrt{3}}}{4 \sqrt[3]{2}}$$

01.06.03.0115.01

$$\sin\left(\frac{13\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_1^{-1}$$

01.06.03.0116.01

$$\sin\left(\frac{13\pi}{9}\right) = \frac{1}{2} (-1)^{17/18} \left(1 + \sqrt[9]{-1}\right)$$

01.06.03.0117.01

$$\sin\left(\frac{3\pi}{2}\right) = -1$$

01.06.03.0118.01

$$\sin\left(\frac{14\pi}{9}\right) = -\frac{(-i + \sqrt{3})\sqrt[3]{-1 + i\sqrt{3}} + (i + \sqrt{3})\sqrt[3]{-1 - i\sqrt{3}}}{4\sqrt[3]{2}}$$

01.06.03.0119.01

$$\sin\left(\frac{14\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_1^{-1}$$

01.06.03.0120.01

$$\sin\left(\frac{14\pi}{9}\right) = \frac{1}{2}\sqrt[18]{-1}(-1 + (-1)^{8/9})$$

01.06.03.0121.01

$$\sin\left(\frac{11\pi}{7}\right) = \frac{1}{6 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}}} \left( (\sqrt{7} - i\sqrt{21}) \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} - 2^{2/3} 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} + \frac{1}{2} \left( i \sqrt[3]{14 - 42i\sqrt{3}} \right. \right. \\ \left. \left. \left( (1 + i\sqrt{3}) \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} + 2 \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} \right) - 4\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} \right) \right)$$

01.06.03.0122.01

$$\sin\left(\frac{11\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_1^{-1}$$

01.06.03.0123.01

$$\sin\left(\frac{11\pi}{7}\right) = \frac{1}{2}\sqrt[14]{-1}(-1 + (-1)^{6/7})$$

01.06.03.0124.01

$$\sin\left(\frac{19\pi}{12}\right) = -\frac{\sqrt{3} + 1}{2\sqrt{2}}$$

01.06.03.0125.01

$$\sin\left(\frac{19\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_1^{-1}$$

01.06.03.0126.01

$$\sin\left(\frac{8\pi}{5}\right) = -\frac{1}{2}\sqrt{\frac{5 + \sqrt{5}}{2}}$$

01.06.03.0127.01

$$\sin\left(\frac{8\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_1^{-1}$$

01.06.03.0128.01

$$\sin\left(\frac{13\pi}{8}\right) = -\frac{\sqrt{2 + \sqrt{2}}}{2}$$

01.06.03.0129.01

$$\sin\left(\frac{13\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_1^{-1}$$

01.06.03.0130.01

$$\sin\left(\frac{13\pi}{8}\right) = \frac{1}{2} \sqrt[8]{-1} (-1 + (-1)^{3/4})$$

01.06.03.0131.01

$$\sin\left(\frac{5\pi}{3}\right) = -\frac{\sqrt{3}}{2}$$

01.06.03.0132.01

$$\sin\left(\frac{17\pi}{10}\right) = -\frac{\sqrt{5} + 1}{4}$$

01.06.03.0133.01

$$\begin{aligned} \sin\left(\frac{12\pi}{7}\right) = & -\left( -2\sqrt{7} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} - 2i\sqrt{21} \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} + 4\sqrt{7} \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} + \right. \\ & 2 \cdot 2^{2/3} 7^{5/6} \sqrt[3]{1 - 3i\sqrt{3}} + \sqrt{3} \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} + 2(14 + i\sqrt{7} + 3\sqrt{21})^{2/3} \\ & \left. \sqrt[3]{14 - i\sqrt{7} - 3\sqrt{21}} i + \sqrt[3]{14 + i\sqrt{7} + 3\sqrt{21}} (14 - i\sqrt{7} - 3\sqrt{21})^{2/3} i \right) / \left( 12 \cdot 2^{2/3} \sqrt[3]{7 - 21i\sqrt{3}} \right) \end{aligned}$$

01.06.03.0134.01

$$\sin\left(\frac{12\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_2^{-1}$$

01.06.03.0135.01

$$\sin\left(\frac{12\pi}{7}\right) = \frac{1}{2} (-1)^{3/14} (-1 + (-1)^{4/7})$$

01.06.03.0136.01

$$\sin\left(\frac{7\pi}{4}\right) = -\frac{\sqrt{2}}{2}$$

01.06.03.0137.01

$$\sin\left(\frac{16\pi}{9}\right) = -\frac{i \left( \sqrt[3]{-1 - i\sqrt{3}} - \sqrt[3]{-1 + i\sqrt{3}} \right)}{2 \sqrt[3]{2}}$$

01.06.03.0138.01

$$\sin\left(\frac{16\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_2^{-1}$$

01.06.03.0139.01

$$\sin\left(\frac{16\pi}{9}\right) = \frac{1}{2} (-1)^{5/18} (-1 + (-1)^{4/9})$$

01.06.03.0140.01

$$\sin\left(\frac{9\pi}{5}\right) = -\frac{1}{2} \sqrt{\frac{5-\sqrt{5}}{2}}$$

01.06.03.0141.01

$$\sin\left(\frac{9\pi}{5}\right) = (z; 16z^4 - 20z^2 + 5)_2^{-1}$$

01.06.03.0142.01

$$\sin\left(\frac{11\pi}{6}\right) = -\frac{1}{2}$$

01.06.03.0143.01

$$\sin\left(\frac{13\pi}{7}\right) = -\frac{1}{24} i \left( 2(1-i\sqrt{3}) \sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}} - \right. \\ \left. (2+2i\sqrt{3}) \sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}} + \frac{2\sqrt{7}(-i+\sqrt{3})}{\sqrt[3]{7 + \frac{i\sqrt{7}}{2} + \frac{3\sqrt{21}}{2}}} + 4\sqrt{7}i - \frac{2\sqrt{7}(i+\sqrt{3})}{\sqrt[3]{7 - \frac{i\sqrt{7}}{2} - \frac{3\sqrt{21}}{2}}} \right)$$

01.06.03.0144.01

$$\sin\left(\frac{13\pi}{7}\right) = (z; 64z^6 - 112z^4 + 56z^2 - 7)_3^{-1}$$

01.06.03.0145.01

$$\sin\left(\frac{13\pi}{7}\right) = \frac{1}{2} (-1)^{5/14} (-1 + (-1)^{2/7})$$

01.06.03.0146.01

$$\sin\left(\frac{15\pi}{8}\right) = -\frac{\sqrt{2-\sqrt{2}}}{2}$$

01.06.03.0147.01

$$\sin\left(\frac{15\pi}{8}\right) = (z; 8z^4 - 8z^2 + 1)_2^{-1}$$

01.06.03.0148.01

$$\sin\left(\frac{15\pi}{8}\right) = \frac{1}{2} (-1)^{3/8} (-1 + \sqrt[4]{-1})$$

01.06.03.0149.01

$$\sin\left(\frac{17\pi}{9}\right) = -\frac{i \left( (-1-i\sqrt{3})^{4/3} - (-1+i\sqrt{3})^{4/3} \right)}{4\sqrt[3]{2}}$$

01.06.03.0150.01

$$\sin\left(\frac{17\pi}{9}\right) = (z; 64z^6 - 96z^4 + 36z^2 - 3)_3^{-1}$$

01.06.03.0151.01

$$\sin\left(\frac{17\pi}{9}\right) = \frac{1}{2}(-1)^{7/18}(-1 + (-1)^{2/9})$$

01.06.03.0152.01

$$\sin\left(\frac{19\pi}{10}\right) = -\frac{\sqrt{5} - 1}{4}$$

01.06.03.0153.01

$$\sin\left(\frac{23\pi}{12}\right) = -\frac{\sqrt{3} - 1}{2\sqrt{2}}$$

01.06.03.0154.01

$$\sin\left(\frac{23\pi}{12}\right) = (z; 16z^4 - 16z^2 + 1)_2^{-1}$$

01.06.03.0155.01

$$\sin(2\pi) = 0$$

01.06.03.0156.01

$$\sin\left(\frac{\pi}{17}\right) = \frac{1}{4} \sqrt{\left(8 - \sqrt{\left(2 \left(\sqrt{\left(2 \left(8 \sqrt{2(\sqrt{17} + 17)} + 6\sqrt{17} + \sqrt{2(17 - \sqrt{17})} - \sqrt{34(17 - \sqrt{17}) + 34}\right)} + \sqrt{17} - \sqrt{2(17 - \sqrt{17}) + 15}\right)}\right)}\right)}$$

01.06.03.0157.01

$$\sin\left(\frac{\pi}{30}\right) = \frac{1}{4} \sqrt{\frac{3}{2}(5 - \sqrt{5})} - \frac{\sqrt{5} + 1}{8}$$

$\sin\left(\frac{n\pi}{m}\right)$  can be expressed using only square roots if  $n \in \mathbb{Z}$  and  $m$  is a product of a power of 2 and distinct Fermat primes  $\{3, 5, 17, 257, \dots\}$ .

## Values at infinities

01.06.03.0158.01

$$\sin(i\infty) = i\infty$$

01.06.03.0159.01

$$\sin(-i\infty) = -i\infty$$

01.06.03.0160.01

$$\sin(\infty) = i$$

## General characteristics

### Domain and analyticity

$\sin(z)$  is an entire analytical function of  $z$  which is defined over the whole complex  $z$ -plane.

01.06.04.0001.01

$$z \rightarrow \sin(z) :: \mathbb{C} \rightarrow \mathbb{C}$$

## Symmetries and periodicities

### Parity

$\sin(z)$  is an odd function.

01.06.04.0002.01

$$\sin(-z) = -\sin(z)$$

### Mirror symmetry

01.06.04.0003.01

$$\sin(\bar{z}) = \overline{\sin(z)}$$

### Periodicity

$\sin(z)$  is a periodic function with period  $2\pi$ .

01.06.04.0009.01

$$\sin(z + 2\pi) = \sin(z)$$

01.06.04.0004.01

$$\sin(z + 2\pi m) = \sin(z) \ ; \ m \in \mathbb{Z}$$

01.06.04.0005.01

$$\sin(z + \pi m) = (-1)^m \sin(z) \ ; \ m \in \mathbb{Z}$$

## Poles and essential singularities

The function  $\sin(z)$  has only one singular point at  $z = \infty$ . It is an essential singular point.

01.06.04.0006.01

$$\text{Sing}_z(\sin(z)) = \{\{\infty, \infty\}\}$$

## Branch points

The function  $\sin(z)$  does not have branch points.

01.06.04.0007.01

$$\mathcal{BP}_z(\sin(z)) = \{\}$$

## Branch cuts

The function  $\sin(z)$  does not have branch cuts.

01.06.04.0008.01

$$\mathcal{BC}_z(\sin(z)) = \{\}$$

## Series representations

### Generalized power series

Expansions at  $z = z_0$



### For the function itself

01.06.06.0030.01

$$\sin(z) \propto \sin(z_0) + \cos(z_0)(z - z_0) - \frac{1}{2} \sin(z_0)(z - z_0)^2 + \dots /; (z \rightarrow z_0)$$

01.06.06.0031.01

$$\sin(z) \propto \sin(z_0) + \cos(z_0)(z - z_0) - \frac{1}{2} \sin(z_0)(z - z_0)^2 + \mathcal{O}((z - z_0)^3)$$

01.06.06.0032.01

$$\sin(z) = \sum_{k=0}^{\infty} \frac{1}{k!} \sin\left(\frac{\pi k}{2} + z_0\right) (z - z_0)^k$$

01.06.06.0033.01

$$\sin(z) = \frac{1}{2} i \left( e^{-iz_0} {}_0F_0(; ; -i(z - z_0)) - e^{iz_0} {}_0F_0(; ; i(z - z_0)) \right)$$

01.06.06.0034.01

$$\sin(z) \propto \sin(z_0) (1 + \mathcal{O}(z - z_0))$$

01.06.06.0035.01

$$\sin(z) = F_{\infty}(z, z_0) /; \left( F_n(z, z_0) = \sum_{k=0}^n \frac{\sin\left(\frac{\pi k}{2} + z_0\right) (z - z_0)^k}{k!} = \frac{1}{2} i \left( e^{-iz} Q(n+1, -i(z - z_0)) - e^{iz} Q(n+1, i(z - z_0)) \right) \bigwedge n \in \mathbb{N} \right)$$

Summed form of the truncated series expansion.

### Expansions at $z = 0$

### For the function itself

01.06.06.0001.02

$$\sin(z) \propto z - \frac{z^3}{6} + \frac{z^5}{120} - \dots /; (z \rightarrow 0)$$

01.06.06.0036.01

$$\sin(z) \propto z - \frac{z^3}{6} + \frac{z^5}{120} - \mathcal{O}(z^7)$$

01.06.06.0002.01

$$\sin(z) = \sum_{k=0}^{\infty} \frac{(-1)^k z^{2k+1}}{(2k+1)!}$$

01.06.06.0003.01

$$\sin(z) = z {}_0F_1\left(\frac{3}{2}; -\frac{z^2}{4}\right)$$

01.06.06.0004.02

$$\sin(z) \propto z + \mathcal{O}(z^3)$$

01.06.06.0037.01

$$\sin(z) = F_\infty(z) /; \left( \left( F_n(z) = z \sum_{k=0}^n \frac{(-1)^k z^{2k}}{(2k+1)!} = \sin(z) + \frac{(-1)^n z^{2n+3}}{(2n+3)!} {}_1F_2 \left( 1; n+2, n+\frac{5}{2}; -\frac{z^2}{4} \right) \right) \wedge n \in \mathbb{N} \right)$$

Summed form of the truncated series expansion.

## For powers of the function

### For the second power

01.06.06.0005.02

$$\sin^2(z) \propto z^2 - \frac{z^4}{3} + \frac{2z^6}{45} - \dots /; (z \rightarrow 0)$$

01.06.06.0038.01

$$\sin^2(z) \propto z^2 - \frac{z^4}{3} + \frac{2z^6}{45} - O(z^8)$$

01.06.06.0006.01

$$\sin^2(z) = \sum_{k=1}^{\infty} \frac{(-1)^{k-1} 2^{2k-1} z^{2k}}{(2k)!}$$

01.06.06.0007.01

$$\sin^2(z) = z^2 {}_1F_2 \left( 1; 2, \frac{3}{2}; -z^2 \right)$$

01.06.06.0039.01

$$\sin^2(z) \propto z^2 + O(z^4)$$

01.06.06.0040.01

$$\sin^2(z) = F_\infty(z) /; \left( \left( F_m(z) = \frac{1}{2} z^2 \sum_{j=0}^m \frac{(-1)^j 2^{2(j+1)} z^{2j}}{\Gamma(2j+3)} = \sin^2(z) + \frac{1}{2} \sqrt{\pi} z^4 (-z^2)^m {}_1\tilde{F}_2 \left( 1; m+\frac{5}{2}, m+3; -z^2 \right) \right) \wedge m \in \mathbb{N} \right)$$

Summed form of the truncated series expansion.

### For the third power

01.06.06.0008.02

$$\sin^3(z) \propto z^3 - \frac{z^5}{2} + \frac{13z^7}{120} - \dots /; (z \rightarrow 0)$$

01.06.06.0041.01

$$\sin^3(z) \propto z^3 - \frac{z^5}{2} + \frac{13z^7}{120} - O(z^9)$$

01.06.06.0009.01

$$\sin^3(z) = \frac{1}{4} \sum_{k=1}^{\infty} \frac{(-1)^{k-1} (3^{2k+1} - 3) z^{2k+1}}{(2k+1)!}$$

01.06.06.0042.01

$$\sin^3(z) = \frac{3z}{4} \left( {}_0F_1\left(\frac{3}{2}; -\frac{z^2}{4}\right) - {}_0F_1\left(\frac{3}{2}; -\frac{9}{4}z^2\right) \right)$$

01.06.06.0043.01

$$\sin^3(z) \propto z^3 + O(z^5)$$

01.06.06.0044.01

$$\sin^3(z) = F_\infty(z) /; \left( F_m(z) = \frac{1}{4} z^3 \sum_{j=0}^m \frac{(-1)^j (-3 + 3^{2j+3}) z^{2j}}{(2j+3)!} = \right.$$

$$\left. \sin^3(z) + \frac{3(-z)^m z^{m+5}}{4\Gamma(2m+6)} \left( {}_1F_2\left(1; m+3, m+\frac{7}{2}; -\frac{9z^2}{4}\right) - {}_1F_2\left(1; m+3, m+\frac{7}{2}; -\frac{z^2}{4}\right) \right) \right) \wedge m \in \mathbb{N}$$

Summed form of the truncated series expansion.

For symbolical integer power

01.06.06.0045.01

$$\sin^n(z) \propto z^n \left( 1 - \left( \frac{2^{1-n}}{(n+2)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^{n+2} \right) z^2 + \left( \frac{2^{1-n}}{(n+4)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^{n+4} \right) z^4 + \dots \right) /; (z \rightarrow 0) \wedge n \in \mathbb{N}^+$$

01.06.06.0046.01

$$\sin^n(z) \propto z^n \left( 1 - \left( \frac{2^{1-n}}{(n+2)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^{n+2} \right) z^2 + \left( \frac{2^{1-n}}{(n+4)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^{n+4} \right) z^4 + O(z^6) \right) /; n \in \mathbb{N}^+$$

01.06.06.0047.01

$$\sin^n(z) = 2^{1-n} z^n \sum_{j=0}^{\infty} \left( \frac{(-1)^j}{(2j+n)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^{2j+n} \right) z^{2j} /; n \in \mathbb{N}^+$$

01.06.06.0048.01

$$\sin^n(z) = \frac{2^{1-n} z^n}{n!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^n {}_1F_2\left(1; \frac{n+1}{2}, \frac{n}{2}+1; -\frac{(n-2k)^2 z^2}{4}\right) /; n \in \mathbb{N}^+$$

01.06.06.0049.01

$$\sin^n(z) \propto z^n (1 + O(z^2)) /; n \in \mathbb{N}^+$$

01.06.06.0050.01

$$\begin{aligned} \sin^n(z) = F_\infty(z) /; & \left( \left( F_m(z) = 2^{1-n} z^n \sum_{j=0}^m \left( \frac{(-1)^j}{(2j+n)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^{2j+n} \right) z^{2j} = \right. \right. \\ & 2^{1-n} z^n \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{k} (n-2k)^n \left( \frac{1}{n!} {}_1F_2 \left( 1; \frac{n}{2} + \frac{1}{2}, \frac{n}{2} + 1; -\frac{(n-2k)^2 z^2}{4} \right) - \right. \\ & \left. \left. \left. \frac{(-(n-2k)^2 z^2)^{m+1}}{\Gamma(2m+n+3)} {}_1F_2 \left( 1; \frac{n+3}{2} + m, m + \frac{n}{2} + 2; -\frac{(n-2k)^2 z^2}{4} \right) \right) \right) \bigwedge m \in \mathbb{N} \bigwedge n \in \mathbb{N}^+ \end{aligned}$$

Summed form of the truncated series expansion.

For symbolical power

01.06.06.0051.01

$$\begin{aligned} \sin^a(z) = e & \left[ \frac{1}{2} - \frac{\arg\left(\frac{\sin(z)}{z}\right) - \arg(z)}{2\pi} \right] a z^a \sum_{k=0}^{\infty} \binom{k-a}{k} \sum_{j=0}^k \frac{(-1)^j}{a-j} \binom{k}{j} p_{j,k} z^k /; \\ p_{j,0} = 1 \bigwedge p_{j,k} = & \frac{1}{k} \sum_{m=1}^k \frac{(jm+m-k)(-m+2\lfloor \frac{m}{2} \rfloor + 1)(-1)^{m/2} p_{j,k-m}}{(m+1)!} \bigwedge k \in \mathbb{N}^+ \end{aligned}$$

01.06.06.0052.01

$$\begin{aligned} (z^\beta \sin(z))^a = e & \left[ \frac{1}{2} - \frac{\arg\left(\frac{\sin(z)}{z}\right) - \frac{\text{Im}((\beta+1)\log(z))}{2\pi}}{2\pi} \right] a z^{(\beta+1)a} \sum_{k=0}^{\infty} \binom{k-a}{k} \sum_{j=0}^k \frac{(-1)^j}{a-j} \binom{k}{j} p_{j,k} z^k /; \\ p_{j,0} = 1 \bigwedge p_{j,k} = & \frac{1}{k} \sum_{m=1}^k \frac{(jm+m-k)(-m+2\lfloor \frac{m}{2} \rfloor + 1)(-1)^{m/2} p_{j,k-m}}{(m+1)!} \bigwedge k \in \mathbb{N}^+ \end{aligned}$$

**Expansions at  $z = \frac{\pi}{2}$**

**For the function itself**

01.06.06.0010.02

$$\sin(z) \propto 1 - \frac{1}{2} \left( z - \frac{\pi}{2} \right)^2 + \frac{1}{24} \left( z - \frac{\pi}{2} \right)^4 - \dots /; \left( z \rightarrow \frac{\pi}{2} \right)$$

01.06.06.0053.01

$$\sin(z) \propto 1 - \frac{1}{2} \left( z - \frac{\pi}{2} \right)^2 + \frac{1}{24} \left( z - \frac{\pi}{2} \right)^4 - \mathcal{O} \left( \left( z - \frac{\pi}{2} \right)^6 \right)$$

01.06.06.0011.01

$$\sin(z) = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k)!} \left( z - \frac{\pi}{2} \right)^{2k}$$

01.06.06.0012.01

$$\sin(z) = {}_0F_1\left(\frac{1}{2}; -\frac{1}{4}\left(z - \frac{\pi}{2}\right)^2\right)$$

01.06.06.0013.02

$$\sin(z) \propto 1 + \mathcal{O}\left(\left(z - \frac{\pi}{2}\right)^2\right)$$

01.06.06.0054.01

$$\sin(z) = F_\infty(z) /;$$

$$\left(\left(F_n(z) = \sum_{k=0}^n \frac{(-1)^k}{(2k)!} \left(z - \frac{\pi}{2}\right)^{2k} = \sin(z) + \frac{(-1)^n \sqrt{\pi}}{2^{2n+2}} \left(z - \frac{\pi}{2}\right)^{2+2n} {}_1\tilde{F}_2\left(1; n + \frac{3}{2}, n + 2; -\frac{1}{4}\left(z - \frac{\pi}{2}\right)^2\right)\right) \wedge n \in \mathbb{N}\right)$$

Summed form of the truncated series expansion.

### For powers of the function

For the second power

01.06.06.0014.02

$$\sin^2(z) \propto 1 - \left(z - \frac{\pi}{2}\right)^2 + \frac{1}{3}\left(z - \frac{\pi}{2}\right)^4 - \dots /; \left(z \rightarrow \frac{\pi}{2}\right)$$

01.06.06.0055.01

$$\sin^2(z) \propto 1 - \left(z - \frac{\pi}{2}\right)^2 + \frac{1}{3}\left(z - \frac{\pi}{2}\right)^4 - \mathcal{O}\left(\left(z - \frac{\pi}{2}\right)^6\right)$$

01.06.06.0015.01

$$\sin^2(z) = 1 + \sum_{k=1}^{\infty} \frac{(-1)^k 2^{2k-1}}{(2k)!} \left(z - \frac{\pi}{2}\right)^{2k}$$

01.06.06.0016.01

$$\sin^2(z) = \frac{1}{2} {}_0F_1\left(\frac{1}{2}; -\left(z - \frac{\pi}{2}\right)^2\right) + \frac{1}{2}$$

01.06.06.0056.01

$$\sin^2(z) \propto 1 + \mathcal{O}\left(\left(z - \frac{\pi}{2}\right)^2\right)$$

01.06.06.0057.01

$$\sin^2(z) = F_\infty(z) /;$$

$$\left(\left(F_m(z) = 1 + \frac{1}{2} \sum_{j=1}^m \frac{(-1)^j 2^{2j}}{(2j)!} \left(z - \frac{\pi}{2}\right)^{2j} = \sin^2(z) + \frac{(-1)^m \sqrt{\pi}}{2} \left(z - \frac{\pi}{2}\right)^{2+2m} {}_1\tilde{F}_2\left(1; m + \frac{3}{2}, m + 2; -\left(z - \frac{\pi}{2}\right)^2\right)\right) \wedge m \in \mathbb{N}\right)$$

Summed form of the truncated series expansion.

For the third power

01.06.06.0017.02

$$\sin^3(z) \propto 1 - \frac{3}{2} \left(z - \frac{\pi}{2}\right)^2 + \frac{7}{8} \left(z - \frac{\pi}{2}\right)^4 - \dots /; \left(z \rightarrow \frac{\pi}{2}\right)$$

01.06.06.0058.01

$$\sin^3(z) \propto 1 - \frac{3}{2} \left(z - \frac{\pi}{2}\right)^2 + \frac{7}{8} \left(z - \frac{\pi}{2}\right)^4 - \mathcal{O}\left(\left(z - \frac{\pi}{2}\right)^6\right)$$

01.06.06.0018.01

$$\sin^3(z) = \frac{1}{4} \sum_{k=0}^{\infty} \frac{(-1)^k (3^{2k} + 3)}{(2k)!} \left(z - \frac{\pi}{2}\right)^{2k}$$

01.06.06.0059.01

$$\sin^3(z) = \frac{3}{4} {}_0F_1\left(\frac{1}{2}; -\frac{1}{4} \left(z - \frac{\pi}{2}\right)^2\right) + \frac{1}{4} {}_0F_1\left(\frac{1}{2}; -\frac{9}{4} \left(z - \frac{\pi}{2}\right)^2\right)$$

01.06.06.0060.01

$$\sin^3(z) \propto 1 + \mathcal{O}\left(\left(z - \frac{\pi}{2}\right)^2\right)$$

01.06.06.0061.01

$$\begin{aligned} \sin^3(z) = F_{\infty}(z) /; \left( F_m(z) = 1 + \frac{1}{4} \sum_{j=1}^m \frac{(-1)^j (3 + 3^{2j})}{(2j)!} \left(z - \frac{\pi}{2}\right)^{2j} = \sin^3(z) + (-1)^m 2^{-2m-4} \sqrt{\pi} \left(z - \frac{\pi}{2}\right)^{2+2m} \right. \\ \left. \left( {}_3F_2\left(1; m + \frac{3}{2}, m + 2; -\frac{1}{4} \left(z - \frac{\pi}{2}\right)^2\right) + 3^{2m+2} {}_1\tilde{F}_2\left(1; m + \frac{3}{2}, m + 2; -\frac{9}{4} \left(z - \frac{\pi}{2}\right)^2\right) \right) \wedge m \in \mathbb{N} \right) \end{aligned}$$

Summed form of the truncated series expansion.

For symbolical integer power

01.06.06.0062.01

$$\begin{aligned} \sin^n(z) \propto 1 + \frac{1}{2^{n+2}} \left( (1 + (-1)^n) \binom{n}{\lfloor \frac{n}{2} \rfloor} \left(n - 2 \lfloor \frac{n}{2} \rfloor\right)^2 - 2^{n+1} n \right) \left(z - \frac{\pi}{2}\right)^2 + \\ \frac{1}{3 \cdot 2^{n+4}} \left( 2^{n+1} n (3n - 2) - (1 + (-1)^n) \binom{n}{\lfloor \frac{n}{2} \rfloor} \left(n - 2 \lfloor \frac{n}{2} \rfloor\right)^4 \right) \left(z - \frac{\pi}{2}\right)^4 + \dots /; \left(z \rightarrow \frac{\pi}{2}\right) \wedge n \in \mathbb{N}^+ \end{aligned}$$

01.06.06.0063.01

$$\begin{aligned} \sin^n(z) \propto 1 + \frac{1}{2^{n+2}} \left( (1 + (-1)^n) \binom{n}{\lfloor \frac{n}{2} \rfloor} \left(n - 2 \lfloor \frac{n}{2} \rfloor\right)^2 - 2^{n+1} n \right) \left(z - \frac{\pi}{2}\right)^2 + \\ \frac{1}{3 \cdot 2^{n+4}} \left( 2^{n+1} n (3n - 2) - (1 + (-1)^n) \binom{n}{\lfloor \frac{n}{2} \rfloor} \left(n - 2 \lfloor \frac{n}{2} \rfloor\right)^4 \right) \left(z - \frac{\pi}{2}\right)^4 + \mathcal{O}\left(\left(z - \frac{\pi}{2}\right)^6\right) /; n \in \mathbb{N}^+ \end{aligned}$$

01.06.06.0064.01

$$\sin^n(z) = 1 + 2^{1-n} \sum_{j=1}^{\infty} \left( \frac{(-1)^j}{(2j)!} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n}{k} (n - 2k)^{2j} \right) \left(z - \frac{\pi}{2}\right)^{2j} /; n \in \mathbb{N}^+$$

01.06.06.0065.01

$$\sin^n(z) = 2^{-n} \binom{n}{\frac{n}{2}} (1 - n \bmod 2) + 2^{1-n} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n}{k} {}_0F_1 \left( ; \frac{1}{2}; -\frac{(n-2k)^2}{4} \left(z - \frac{\pi}{2}\right)^2 \right); n \in \mathbb{N}^+$$

01.06.06.0066.01

$$\sin^n(z) \propto 1 + O\left(\left(z - \frac{\pi}{2}\right)^2\right); n \in \mathbb{N}^+$$

01.06.06.0067.01

$$\sin^n(z) = F_\infty(z); \left( F_m(z) = 1 + 2^{1-n} \sum_{j=1}^m \frac{1}{(2j)!} \left( (-1)^j \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n}{k} (n-2k)^{2j} \right) \left(z - \frac{\pi}{2}\right)^{2j} = \sin^n(z) + \frac{(-1)^m \sqrt{\pi}}{2^{2m+n+1}} \left(z - \frac{\pi}{2}\right)^{2+2m} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n}{k} (n-2k)^{2m+2} {}_1\tilde{F}_2 \left( 1; m + \frac{3}{2}, m + 2; -\frac{(n-2k)^2}{4} \left(z - \frac{\pi}{2}\right)^2 \right) \right) \wedge m \in \mathbb{N} \wedge n \in \mathbb{N}^+$$

Summed form of the truncated series expansion.

### q-series

01.06.06.0019.01

$$\sin(z) = \frac{1}{2i} \left( q - \frac{1}{q} \right); q = e^{i\pi z}$$

### Exponential Fourier series

01.06.06.0020.01

$$\sin(ax) = -\frac{2 \sin(a\pi)}{\pi} \sum_{k=1}^{\infty} \frac{(-1)^k k \sin(kx)}{k^2 - a^2}; a \notin \mathbb{Z} \wedge -\pi < x < \pi$$

### Asymptotic series expansions

01.06.06.0021.01

$$\sin(z) \propto \sin(z); (|z| \rightarrow \infty)$$

01.06.06.0022.01

$$\sin(z) \propto \frac{i}{2} e^{-iz}; (z \rightarrow e^{i\phi} \infty) \wedge 0 < \phi < \pi$$

01.06.06.0023.01

$$\sin(z) \propto -\frac{i}{2} e^{iz}; (z \rightarrow e^{i\phi} \infty) \wedge -\pi < \phi < 0$$

01.06.06.0068.01

$$\sin(z) \propto \begin{cases} -\frac{i}{2} e^{iz} & -\pi < \arg(z) < 0 \\ \frac{1}{2} i e^{-iz} & 0 < \arg(z) < \pi \\ \sin(z) & \text{True} \end{cases}; (|z| \rightarrow \infty)$$

### Other series representations

01.06.06.0025.01

$$\sin(z) = \pi \sum_{k=0}^{\infty} (-1)^k \left( 2k + \frac{z}{\pi} \right) \left( \frac{1}{k!} \left( \frac{z}{\pi} \right)^k \right)^3$$

01.06.06.0026.01

$$\sin(z) = 2 \sum_{k=0}^{\infty} (-1)^k J_{2k+1}(z)$$

01.06.06.0027.01

$$\frac{\sin(nz)}{\sin(z)} = \sum_{j=0}^n \prod_{\substack{k=1 \\ k \neq j}}^n \frac{\sin(z + \theta_j - \theta_k)}{\sin(\theta_j - \theta_k)} ; n \in \mathbb{N} \wedge \theta_j \neq \theta_k$$

01.06.06.0028.01

$$\log\left(\frac{\sin(z)}{z}\right) = \sum_{k=1}^{\infty} \frac{(-1)^k 2^{2k-1} B_{2k} z^{2k}}{k (2k)!} ; 1.780467 < |z| \leq \pi$$

01.06.06.0029.01

$$\sin(z) = z \left( \sum_{k=n}^{\infty} (-1)^{k-n} \binom{2k}{k-n} \binom{k-n - \frac{z}{c\pi} + 1}{2k+1} - \sum_{k=n-1}^{\infty} (-1)^{k-n} \binom{2k}{k-n+1} \binom{k+n + \frac{z}{c\pi}}{2k+1} \right) ; n \in \mathbb{Z}$$

Everett series

## Residue representations

01.06.06.0024.01

$$\sin(z) = \frac{\sqrt{\pi}}{2} z \sum_{j=0}^{\infty} \operatorname{res}_s \left( \frac{\left(\frac{z^2}{4}\right)^{-s}}{\Gamma\left(\frac{3}{2} - s\right)} \Gamma(s) \right) (-j)$$

## Dual Taylor series representations

01.06.06.0069.01

$$\sin(x) \theta(x) \propto \sum_{k=0}^{\infty} (-1)^k \frac{\partial^{2k} \delta(x)}{\partial x^{2k}}$$

01.06.06.0070.01

$$\sin(\lambda x) \theta(x) \propto \sum_{k=0}^{\infty} (-1)^k \frac{\partial^{2k} \delta(x)}{\partial x^{2k}} \lambda^{-1-2k} ; (\lambda \rightarrow \infty)$$

## Integral representations

### On the real axis

#### Of the direct function

01.06.07.0001.01

$$\sin(z) = z \int_0^1 \cos(zt) dt$$



## Contour integral representations

01.06.07.0002.01

$$\sin(z) = \frac{\sqrt{\pi}}{2} \frac{z}{2\pi i} \int_{\gamma-i\infty}^{\gamma+i\infty} e^{s-\frac{z^2}{4s}} s^{-\frac{3}{2}} ds ; \gamma > 0$$

01.06.07.0003.01

$$\sin(x) = \frac{\sqrt{\pi}}{2\pi i} \int_{\gamma-i\infty}^{\gamma+i\infty} \frac{\Gamma(s)}{\Gamma(\frac{3}{2}-s)} \left(\frac{x}{2}\right)^{-2s+1} ds ; 0 < \gamma < 1 \wedge x > 0$$

01.06.07.0004.01

$$\sin(z) = \frac{\sqrt{\pi}}{4i} z \int_{\mathcal{L}} \frac{\Gamma(s)}{\Gamma(s+\frac{1}{2})\Gamma(\frac{1}{2}-s)\Gamma(\frac{3}{2}-s)} \left(-\frac{z^2}{4}\right)^{-s} ds$$

## Product representations

01.06.08.0001.01

$$\sin(z) = z \prod_{k=1}^{\infty} \left(1 - \frac{z^2}{\pi^2 k^2}\right)$$

01.06.08.0002.01

$$\sin(z) = z \prod_{\substack{k=-\infty \\ k \neq 0}}^{\infty} \left(1 - \frac{z}{\pi k}\right) e^{\frac{z}{\pi k}}$$

01.06.08.0003.01

$$\sin(z) = z \prod_{k=1}^{\infty} \cos\left(\frac{z}{2^k}\right) ; |z| < 1$$

01.06.08.0004.01

$$\sin(z) = z \prod_{k=1}^{\infty} \left(1 - \frac{4}{3} \sin^2\left(\frac{z}{3^k}\right)\right)$$

## Limit representations

01.06.09.0001.01

$$\sin(z) = \frac{\sqrt{\pi}}{2} \lim_{n \rightarrow \infty} \frac{(-1)^n}{4^n n!} H_{2n+1}\left(\frac{z}{2\sqrt{n}}\right)$$

01.06.09.0002.01

$$\sin(z) = \lim_{n \rightarrow \infty} \frac{(-1)^n \pi^{2n+1}}{4(2n)!} E_{2n}\left(\frac{z}{\pi}\right)$$

01.06.09.0003.01

$$\sin(z) = \lim_{a \rightarrow \infty} \operatorname{Se}\left(a, q, \frac{z}{\sqrt{a}}\right) ; q \in \mathbb{R}$$

01.06.09.0004.01

$$\sin(z) = -\lim_{a \rightarrow \infty} \frac{1}{\sqrt{a}} \operatorname{Ce}'\left(a, q, \frac{z}{\sqrt{a}}\right); q \in \mathbb{R}$$

01.06.09.0005.01

$$\sin(z) = -\pi \lim_{n \rightarrow \infty} \frac{1}{\log(n)} \sum_{k=1}^n \frac{\mu(k)}{k} \log\left(\frac{n}{k}\right) \operatorname{frac}\left(\frac{kz}{2\pi}\right)$$

## Differential equations

### Ordinary linear differential equations and wronskians

#### For the direct function itself

01.06.13.0001.01

$$w''(z) + w(z) = 0; w(z) = \sin(z) \wedge w(0) = 0 \wedge w'(0) = 1$$

01.06.13.0002.01

$$w''(z) + w(z) = 0; w(z) = c_1 \cos(z) + c_2 \sin(z)$$

01.06.13.0003.01

$$W_z(\cos(z), \sin(z)) = 1$$

01.06.13.0004.01

$$w''(z) + a w(z) + b = 0; w(z) = -\frac{b}{a} + c_1 \cos(\sqrt{a} z) + c_2 \sin(\sqrt{a} z)$$

01.06.13.0005.01

$$W_z(\cos(\sqrt{a} z), \sin(\sqrt{a} z)) = \sqrt{a}$$

01.06.13.0007.01

$$w''(z) - \frac{g''(z)}{g'(z)} w'(z) + g'(z)^2 w(z) = 0; w(z) = c_1 \cos(g(z)) + c_2 \sin(g(z))$$

01.06.13.0008.01

$$W_z(\cos(g(z)), \sin(g(z))) = g'(z)$$

01.06.13.0009.01

$$w''(z) - \left( \frac{2h'(z)}{h(z)} + \frac{g''(z)}{g'(z)} \right) w'(z) + \left( g'(z)^2 + \frac{2h'(z)^2}{h(z)^2} + \frac{h'(z)g''(z)}{h(z)g'(z)} - \frac{h''(z)}{h(z)} \right) w(z) = 0; w(z) = c_1 h(z) \cos(g(z)) + c_2 h(z) \sin(g(z))$$

01.06.13.0010.01

$$W_z(h(z) \cos(g(z)), h(z) \sin(g(z))) = h(z)^2 g'(z)$$

01.06.13.0011.01

$$z^2 w''(z) - (r + 2s - 1) z w'(z) + (a^2 r^2 z^{2r} + s(r + s)) w(z) = 0; w(z) = c_1 z^s \cos(a z^r) + c_2 z^s \sin(a z^r)$$

01.06.13.0012.01

$$W_z(z^s \cos(a z^r), z^s \sin(a z^r)) = a r z^{r+2s-1}$$

01.06.13.0013.01

$$w''(z) - (\log(r) + 2 \log(s)) w'(z) + (a^2 \log^2(r) r^{2z} + \log(s) (\log(r) + \log(s))) w(z) = 0; w(z) = c_1 s^z \cos(a r^z) + c_2 s^z \sin(a r^z)$$

01.06.13.0014.01

$$W_z(s^z \cos(a r^z), s^z \sin(a r^z)) = a r^z s^{2z} \log(r)$$

## Ordinary nonlinear differential equations

01.06.13.0006.02

$$w'(z) - \sqrt{1 - (w(z))^2} = 0 \ ; \ w(z) = \sin(z) \wedge w(0) = 0 \wedge |\operatorname{Re}(z)| < \frac{\pi}{2}$$

## Transformations

### Transformations and argument simplifications

#### Argument involving basic arithmetic operations

01.06.16.0001.01

$$\sin(-z) = -\sin(z)$$

01.06.16.0002.01

$$\sin(a (b z^c)^m) = \frac{(b z^c)^m}{b^m z^{m c}} \sin(a b^m z^{m c}) \ ; \ 2 m \in \mathbb{Z}$$

01.06.16.0003.01

$$\sin\left(\sqrt{z^2}\right) = \frac{\sqrt{z^2}}{z} \sin(z)$$

#### Argument involving inverse trigonometric and hyperbolic functions

### Involving $\sin^{-1}$

01.06.16.0004.01

$$\sin(\sin^{-1}(z)) = z$$

01.06.16.0017.01

$$\sin\left(\frac{1}{2} \sin^{-1}(z)\right) = \frac{z \sqrt{1 - \sqrt{1 - z^2}}}{\sqrt{2} \sqrt{z^2}}$$

01.06.16.0128.01

$$\sin(i \sin^{-1}(z)) = -\frac{1}{2} i \left( i z + \sqrt{1 - z^2} \right)^{-i} \left( \left( i z + \sqrt{1 - z^2} \right)^{2i} - 1 \right)$$

01.06.16.0129.01

$$\sin(a \sin^{-1}(z)) = -\frac{1}{2} i \left( i z + \sqrt{1 - z^2} \right)^{-a} \left( \left( i z + \sqrt{1 - z^2} \right)^{2a} - 1 \right)$$

01.06.16.0029.01

$$\sin(n \sin^{-1}(z)) = z \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} (1-z^2)^{\frac{n-1}{2}-k} \ ; \ n \in \mathbb{N}^+$$

01.06.16.0030.01

$$\sin(n \sin^{-1}(z)) = z U_{n-1}\left(\sqrt{1 - z^2}\right)$$

01.06.16.0056.01

$$\sin\left(\frac{n}{2} \sin^{-1}(z)\right) = z \left(\sqrt{1-z^2} + 1\right)^{\frac{n}{2}-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n/2-k-1} \left(\frac{1-\sqrt{1-z^2}}{z^2}\right)^k ; n \in \mathbb{N}^+$$

01.06.16.0057.01

$$\sin\left(\frac{n}{2} \sin^{-1}(z)\right) = \frac{z \sqrt{1-\sqrt{1-z^2}}}{\sqrt{2} \sqrt{z^2}} U_{n-1} \left( \frac{\sqrt{\sqrt{1-z^2} + 1}}{\sqrt{2}} \right) ; n \in \mathbb{N}^+$$

## Involving $\cos^{-1}$

01.06.16.0005.01

$$\sin(\cos^{-1}(z)) = \sqrt{1-z^2}$$

01.06.16.0018.01

$$\sin\left(\frac{1}{2} \cos^{-1}(z)\right) = \frac{\sqrt{1-z}}{\sqrt{2}}$$

01.06.16.0130.01

$$\sin(i \cos^{-1}(z)) = \frac{1}{2} i e^{-\frac{\pi}{2}} \left( i z + \sqrt{1-z^2} \right)^{-i} \left( e^{\pi} \left( i z + \sqrt{1-z^2} \right)^{2i} - 1 \right)$$

01.06.16.0131.01

$$\sin(a \cos^{-1}(z)) = -\frac{1}{2} i e^{-\frac{1}{2} i a \pi} \left( i z + \sqrt{1-z^2} \right)^a \left( e^{i a \pi} \left( i z + \sqrt{1-z^2} \right)^{-2a} - 1 \right)$$

01.06.16.0031.01

$$\sin(n \cos^{-1}(z)) = \sqrt{1-z^2} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} z^{n-2k-1} ; n \in \mathbb{N}^+$$

01.06.16.0032.01

$$\sin(n \cos^{-1}(z)) = \sqrt{1-z^2} U_{n-1}(z)$$

01.06.16.0058.01

$$\sin\left(\frac{n}{2} \cos^{-1}(z)\right) = \sqrt{1-z} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n/2-k-1} (z+1)^{\frac{n-1}{2}-k} ; n \in \mathbb{N}^+$$

01.06.16.0059.01

$$\sin\left(\frac{n}{2} \cos^{-1}(z)\right) = \frac{\sqrt{1-z}}{\sqrt{2}} U_{n-1} \left( \frac{\sqrt{z+1}}{\sqrt{2}} \right) ; n \in \mathbb{N}^+$$

## Involving $\tan^{-1}$

01.06.16.0006.01

$$\sin(\tan^{-1}(z)) = \frac{z}{\sqrt{1+z^2}}$$

01.06.16.0007.01

$$\sin(\tan^{-1}(x, y)) = \frac{y}{\sqrt{x^2+y^2}}$$

01.06.16.0019.01

$$\sin\left(\frac{1}{2} \tan^{-1}(z)\right) = \frac{z}{\sqrt{2} \sqrt{z^2}} \sqrt{1 - \frac{1}{\sqrt{z^2+1}}}$$

01.06.16.0132.01

$$\sin\left(\frac{1}{2} \tan^{-1}(x, y)\right) = \frac{i \left(1 - \frac{x+iy}{\sqrt{x^2+y^2}}\right)}{2 \sqrt{\frac{x+iy}{\sqrt{x^2+y^2}}}}$$

01.06.16.0133.01

$$\sin(i \tan^{-1}(z)) = \frac{1}{2} i \left( (1 - iz)^i - (iz + 1)^i \right) (z^2 + 1)^{-\frac{i}{2}}$$

01.06.16.0134.01

$$\sin(i \tan^{-1}(x, y)) = -\frac{1}{2} i \left( \frac{x+iy}{\sqrt{x^2+y^2}} \right)^{-i} \left( \left( \frac{x+iy}{\sqrt{x^2+y^2}} \right)^{2i} - 1 \right)$$

01.06.16.0135.01

$$\sin(a \tan^{-1}(z)) = \frac{1}{2} i \left( (1 - iz)^a - (iz + 1)^a \right) (z^2 + 1)^{-\frac{a}{2}}$$

01.06.16.0136.01

$$\sin(a \tan^{-1}(x, y)) = -\frac{1}{2} i \left( \frac{x+iy}{\sqrt{x^2+y^2}} \right)^{-a} \left( \left( \frac{x+iy}{\sqrt{x^2+y^2}} \right)^{2a} - 1 \right)$$

01.06.16.0033.01

$$\sin(n \tan^{-1}(z)) = (z^2 + 1)^{-\frac{n}{2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{2k+1} z^{2k+1} \quad ; n \in \mathbb{N}^+$$

01.06.16.0034.01

$$\sin(n \tan^{-1}(z)) = \frac{z}{\sqrt{z^2+1}} U_{n-1} \left( \frac{1}{\sqrt{z^2+1}} \right) \quad ; n \in \mathbb{N}^+$$

01.06.16.0137.01

$$\sin(i \tan^{-1}(x, y)) = -\frac{1}{2} i \left( \frac{x+iy}{\sqrt{x^2+y^2}} \right)^{-i} \left( \left( \frac{x+iy}{\sqrt{x^2+y^2}} \right)^{2i} - 1 \right)$$

01.06.16.0138.01

$$\sin(a \tan^{-1}(x, y)) = -\frac{1}{2} i \left( \frac{x + i y}{\sqrt{x^2 + y^2}} \right)^{-a} \left( \left( \frac{x + i y}{\sqrt{x^2 + y^2}} \right)^{2a} - 1 \right)$$

01.06.16.0035.01

$$\sin(n \tan^{-1}(x, y)) = \frac{x^{n-1} y}{(x^2 + y^2)^{n/2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} \left( \frac{x^2 + y^2}{x^2} \right)^k ; n \in \mathbb{N}^+$$

01.06.16.0036.01

$$\sin(n \tan^{-1}(x, y)) = \frac{y}{\sqrt{x^2 + y^2}} U_{n-1} \left( \frac{x}{\sqrt{x^2 + y^2}} \right)$$

01.06.16.0060.01

$$\sin\left(\frac{n}{2} \tan^{-1}(z)\right) = \frac{z}{\sqrt{z^2 + 1}} \left( 1 + \frac{1}{\sqrt{z^2 + 1}} \right)^{\frac{n}{2}-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left( \frac{\sqrt{z^2 + 1}}{\sqrt{z^2 + 1} + 1} \right)^k ; n \in \mathbb{N}^+$$

01.06.16.0061.01

$$\sin\left(\frac{n}{2} \tan^{-1}(z)\right) = \frac{z}{\sqrt{2} \sqrt{z^2}} \sqrt{1 - \frac{1}{\sqrt{z^2 + 1}}} U_{n-1} \left( \frac{1}{\sqrt{2}} \sqrt{1 + \frac{1}{\sqrt{z^2 + 1}}} \right) ; n \in \mathbb{N}^+$$

## Involving $\cot^{-1}$

01.06.16.0008.01

$$\sin(\cot^{-1}(z)) = \frac{\sqrt{-z}}{\sqrt{z} \sqrt{-1 - z^2}}$$

01.06.16.0020.01

$$\sin\left(\frac{1}{2} \cot^{-1}(z)\right) = \frac{z}{\sqrt{2}} \sqrt{\frac{1}{z^2}} \sqrt{1 - \frac{1}{\sqrt{1 + \frac{1}{z^2}}}}$$

01.06.16.0139.01

$$\sin(i \cot^{-1}(z)) = \frac{1}{2} i \left( 1 + \frac{1}{z^2} \right)^{-\frac{i}{2}} \left( \left( \frac{-i + z}{z} \right)^i - \left( \frac{i + z}{z} \right)^i \right)$$

01.06.16.0140.01

$$\sin(a \cot^{-1}(z)) = \frac{1}{2} i \left( 1 + \frac{1}{z^2} \right)^{-\frac{a}{2}} \left( \left( \frac{-i + z}{z} \right)^a - \left( \frac{i + z}{z} \right)^a \right)$$

01.06.16.0037.01

$$\sin(n \cot^{-1}(z)) = \left( 1 + \frac{1}{z^2} \right)^{-\frac{n}{2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{2k+1} z^{-2k-1} ; n \in \mathbb{N}^+$$

01.06.16.0038.01

$$\sin(n \cot^{-1}(z)) = \frac{\sqrt{-z}}{\sqrt{z} \sqrt{-z^2 - 1}} U_{n-1} \left( \frac{\sqrt{-z^2}}{\sqrt{-z^2 - 1}} \right); n \in \mathbb{N}^+$$

01.06.16.0062.01

$$\sin\left(\frac{n}{2} \cot^{-1}(z)\right) = \frac{1}{z \sqrt{1 + \frac{1}{z^2}}} \left( \frac{\sqrt{-z^2}}{\sqrt{-z^2 - 1}} + 1 \right)^{\frac{n}{2}-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left( 1 - \left( \sqrt{1 + \frac{1}{z^2}} - 1 \right) z^2 \right)^k; n \in \mathbb{N}^+$$

01.06.16.0063.01

$$\sin\left(\frac{n}{2} \cot^{-1}(z)\right) = \frac{z}{\sqrt{2}} \sqrt{\frac{1}{z^2}} \sqrt{1 - \frac{\sqrt{-z^2}}{\sqrt{-z^2 - 1}}} U_{n-1} \left( \frac{1}{\sqrt{2}} \sqrt{\frac{\sqrt{-z^2}}{\sqrt{-z^2 - 1}} + 1} \right); n \in \mathbb{N}^+$$

### Involving $\csc^{-1}$

01.06.16.0009.01

$$\sin(\csc^{-1}(z)) = \frac{1}{z}$$

01.06.16.0021.01

$$\sin\left(\frac{1}{2} \csc^{-1}(z)\right) = \frac{z}{\sqrt{2}} \sqrt{\frac{1}{z^2}} \sqrt{1 - \sqrt{1 - \frac{1}{z^2}}}$$

01.06.16.0141.01

$$\sin(i \csc^{-1}(z)) = -\frac{1}{2} i \left( \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{2i} - 1 \right) \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{-i}$$

01.06.16.0142.01

$$\sin(a \csc^{-1}(z)) = -\frac{1}{2} i \left( \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{2a} - 1 \right) \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{-a}$$

01.06.16.0039.01

$$\sin(n \csc^{-1}(z)) = \frac{1}{z} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} \left( 1 - \frac{1}{z^2} \right)^{\frac{n-1}{2}-k}; n \in \mathbb{N}^+$$

01.06.16.0040.01

$$\sin(n \csc^{-1}(z)) = \frac{1}{z} U_{n-1} \left( \sqrt{1 - \frac{1}{z^2}} \right); n \in \mathbb{N}^+$$

01.06.16.0064.01

$$\sin\left(\frac{n}{2} \csc^{-1}(z)\right) = \frac{1}{z} \left( \frac{\sqrt{z^2-1}}{\sqrt{z^2}} + 1 \right)^{\frac{n}{2}-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left( z^2 - \sqrt{z^2} \sqrt{z^2-1} \right)^k ; n \in \mathbb{N}^+$$

01.06.16.0065.01

$$\sin\left(\frac{n}{2} \csc^{-1}(z)\right) = \frac{z}{\sqrt{2}} \sqrt{\frac{1}{z^2}} \sqrt{1 - \sqrt{1 - \frac{1}{z^2}}} U_{n-1} \left( \frac{1}{\sqrt{2}} \sqrt{\sqrt{1 - \frac{1}{z^2}} + 1} \right) ; n \in \mathbb{N}^+$$

### Involving $\sec^{-1}$

01.06.16.0010.01

$$\sin(\sec^{-1}(z)) = \sqrt{1 - \frac{1}{z^2}}$$

01.06.16.0022.01

$$\sin\left(\frac{1}{2} \sec^{-1}(z)\right) = \frac{\sqrt{z-1}}{\sqrt{2z}}$$

01.06.16.0143.01

$$\sin(i \sec^{-1}(z)) = \frac{1}{2} i e^{-\frac{\pi}{2}} \left( e^{\pi} \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{2i} - 1 \right) \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{-i}$$

01.06.16.0144.01

$$\sin(a \sec^{-1}(z)) = -\frac{1}{2} e^{-\frac{1}{2} i a \pi} i \left( e^{i a \pi} - \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{2a} \right) \left( \sqrt{1 - \frac{1}{z^2}} + \frac{i}{z} \right)^{-a}$$

01.06.16.0041.01

$$\sin(n \sec^{-1}(z)) = \sqrt{1 - \frac{1}{z^2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} z^{2k-n+1} ; n \in \mathbb{N}^+$$

01.06.16.0042.01

$$\sin(n \sec^{-1}(z)) = \sqrt{1 - \frac{1}{z^2}} U_{n-1}\left(\frac{1}{z}\right)$$

01.06.16.0066.01

$$\sin\left(\frac{n}{2} \sec^{-1}(z)\right) = \left(\frac{z+1}{z}\right)^{\frac{n-1}{2}} \sqrt{\frac{z-1}{z}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left(\frac{z}{z+1}\right)^k ; n \in \mathbb{N}^+$$

01.06.16.0067.01

$$\sin\left(\frac{n}{2} \sec^{-1}(z)\right) = \frac{1}{\sqrt{2}} \sqrt{\frac{z-1}{z}} U_{n-1}\left(\frac{1}{\sqrt{2}} \sqrt{\frac{z+1}{z}}\right) ; n \in \mathbb{N}^+$$



### Involving $\sinh^{-1}$

01.06.16.0145.01

$$\sin(\sinh^{-1}(z)) = -\frac{1}{2} i \left( z + \sqrt{z^2 + 1} \right)^{-i} \left( \left( z + \sqrt{z^2 + 1} \right)^{2i} - 1 \right)$$

01.06.16.0011.01

$$\sin(i \sinh^{-1}(z)) = i z$$

01.06.16.0023.01

$$\sin\left(\frac{i}{2} \sinh^{-1}(z)\right) = \frac{i z}{\sqrt{2} \sqrt{z^2}} \sqrt{\sqrt{1+z^2} - 1}$$

01.06.16.0146.01

$$\sin(a \sinh^{-1}(z)) = -\frac{1}{2} i \left( z + \sqrt{z^2 + 1} \right)^{-ia} \left( \left( z + \sqrt{z^2 + 1} \right)^{2ia} - 1 \right)$$

01.06.16.0043.01

$$\sin(in \sinh^{-1}(z)) = i z \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} (z^2 + 1)^{\frac{n-1}{2}-k} ; n \in \mathbb{N}^+$$

01.06.16.0044.01

$$\sin(in \sinh^{-1}(z)) = i z U_{n-1}\left(\sqrt{z^2 + 1}\right) ; n \in \mathbb{N}^+$$

01.06.16.0068.01

$$\sin\left(\frac{in}{2} \sinh^{-1}(z)\right) = i z \left( \sqrt{z^2 + 1} + 1 \right)^{\frac{n}{2}-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left( \frac{\sqrt{z^2 + 1} - 1}{z^2} \right)^k ; n \in \mathbb{N}^+$$

01.06.16.0069.01

$$\sin\left(\frac{in}{2} \sinh^{-1}(z)\right) = \frac{i z}{\sqrt{2} \sqrt{\sqrt{z^2 + 1} + 1}} U_{n-1}\left(\frac{\sqrt{\sqrt{z^2 + 1} + 1}}{\sqrt{2}}\right) ; n \in \mathbb{N}^+$$

### Involving $\cosh^{-1}$

01.06.16.0147.01

$$\sin(\cosh^{-1}(z)) = -\frac{1}{2} i \left( z + \sqrt{z-1} \sqrt{z+1} \right)^{-i} \left( \left( z + \sqrt{z-1} \sqrt{z+1} \right)^{2i} - 1 \right)$$

01.06.16.0012.01

$$\sin(i \cosh^{-1}(z)) = i \sqrt{z-1} \sqrt{z+1}$$

01.06.16.0024.01

$$\sin\left(\frac{i}{2} \cosh^{-1}(z)\right) = \frac{i \sqrt{z-1}}{\sqrt{2}}$$

01.06.16.0148.01

$$\sin(a \cosh^{-1}(z)) = -\frac{1}{2} i (z + \sqrt{z-1} \sqrt{z+1})^{-ia} \left( (z + \sqrt{z-1} \sqrt{z+1})^{2ia} - 1 \right)$$

01.06.16.0045.01

$$\sin(in \cosh^{-1}(z)) = i \sqrt{z-1} \sqrt{z+1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} z^{n-2k-1} ; n \in \mathbb{N}^+$$

01.06.16.0046.01

$$\sin(in \cosh^{-1}(z)) = i \sqrt{z-1} \sqrt{z+1} U_{n-1}(z) ; n \in \mathbb{N}^+$$

01.06.16.0070.01

$$\sin\left(\frac{in}{2} \cosh^{-1}(z)\right) = i \sqrt{z-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} (z+1)^{\frac{n-1}{2}-k} ; n \in \mathbb{N}^+$$

01.06.16.0071.01

$$\sin\left(\frac{in}{2} \cosh^{-1}(z)\right) = \frac{i \sqrt{z-1}}{\sqrt{2}} U_{n-1}\left(\frac{\sqrt{z+1}}{\sqrt{2}}\right) ; n \in \mathbb{N}^+$$

## Involving $\tanh^{-1}$

01.06.16.0149.01

$$\sin(\tanh^{-1}(z)) = \frac{1}{2} i (1-z^2)^{-\frac{i}{2}} \left( (1-z)^i - (z+1)^i \right)$$

01.06.16.0013.01

$$\sin(i \tanh^{-1}(z)) = \frac{iz}{\sqrt{1-z^2}}$$

01.06.16.0025.01

$$\sin\left(\frac{i}{2} \tanh^{-1}(z)\right) = \frac{iz}{\sqrt{2} \sqrt{z^2}} \sqrt{\frac{1}{\sqrt{1-z^2}} - 1}$$

01.06.16.0150.01

$$\sin(a \tanh^{-1}(z)) = \frac{1}{2} i (1-z^2)^{-\frac{1}{2}(ia)} \left( (1-z)^{ia} - (z+1)^{ia} \right)$$

01.06.16.0047.01

$$\sin(in \tanh^{-1}(z)) = i (1-z^2)^{-\frac{n}{2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n}{2k+1} z^{2k+1} ; n \in \mathbb{N}^+$$

01.06.16.0048.01

$$\sin(in \tanh^{-1}(z)) = \frac{iz}{\sqrt{1-z^2}} U_{n-1}\left(\frac{1}{\sqrt{1-z^2}}\right) ; n \in \mathbb{N}^+$$

01.06.16.0072.01

$$\sin\left(\frac{in}{2} \tanh^{-1}(z)\right) = \frac{iz}{\sqrt{1-z^2}} \left(1 + \frac{1}{\sqrt{1-z^2}}\right)^{\frac{n-1}{2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n/2-k-1} \left(\frac{\sqrt{1-z^2}}{\sqrt{1-z^2}+1}\right)^k; n \in \mathbb{N}^+$$

01.06.16.0073.01

$$\sin\left(\frac{in}{2} \tanh^{-1}(z)\right) = \frac{iz}{\sqrt{2}\sqrt{-z^2}} \sqrt{1 - \frac{1}{\sqrt{1-z^2}}} U_{n-1}\left(\frac{1}{\sqrt{2}} \sqrt{1 + \frac{1}{\sqrt{1-z^2}}}\right); n \in \mathbb{N}^+$$

### Involving $\coth^{-1}$

01.06.16.0151.01

$$\sin(\coth^{-1}(z)) = \frac{1}{2} i \left( \left(1 - \frac{1}{z}\right)^i - \left(1 + \frac{1}{z}\right)^i \right) \left(1 - \frac{1}{z^2}\right)^{-\frac{i}{2}}$$

01.06.16.0014.01

$$\sin(i \coth^{-1}(z)) = \frac{i \sqrt{z^2}}{z \sqrt{z^2 - 1}}$$

01.06.16.0026.01

$$\sin\left(\frac{i}{2} \coth^{-1}(z)\right) = \frac{iz}{\sqrt{2}} \sqrt{\frac{1}{z^2}} \sqrt{\frac{1}{\sqrt{1 - \frac{1}{z^2}}} - 1}$$

01.06.16.0152.01

$$\sin(a \coth^{-1}(z)) = \frac{1}{2} i \left(1 - \frac{1}{z^2}\right)^{-\frac{1}{2}(ia)} \left( \left(1 - \frac{1}{z}\right)^{ia} - \left(1 + \frac{1}{z}\right)^{ia} \right)$$

01.06.16.0049.01

$$\sin(in \coth^{-1}(z)) = i \left(1 - \frac{1}{z^2}\right)^{\frac{n}{2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n}{2k+1} z^{-2k-1}; n \in \mathbb{N}^+$$

01.06.16.0051.01

$$\sin(in \coth^{-1}(z)) = \frac{i \sqrt{z^2}}{z \sqrt{z^2 - 1}} U_{n-1}\left(\frac{\sqrt{z^2}}{\sqrt{z^2 - 1}}\right); n \in \mathbb{N}^+$$

01.06.16.0074.01

$$\sin\left(\frac{in}{2} \coth^{-1}(z)\right) = \frac{i}{z \sqrt{1 - \frac{1}{z^2}}} \left(\frac{\sqrt{z^2}}{\sqrt{z^2 - 1}} + 1\right)^{\frac{n-1}{2}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left(\left(\sqrt{1 - \frac{1}{z^2}} - 1\right) z^2 + 1\right)^k; n \in \mathbb{N}^+$$

01.06.16.0075.01

$$\sin\left(\frac{in}{2} \coth^{-1}(z)\right) = -\frac{iz}{\sqrt{2}} \sqrt{-\frac{1}{z^2}} \sqrt{1 - \frac{\sqrt{z^2}}{\sqrt{z^2-1}}} U_{n-1}\left(\frac{1}{\sqrt{2}} \sqrt{\frac{\sqrt{z^2}}{\sqrt{z^2-1}} + 1}\right); n \in \mathbb{N}^+$$

### Involving $\operatorname{csch}^{-1}$

01.06.16.0153.01

$$\sin(\operatorname{csch}^{-1}(z)) = \frac{1}{2} i \left( \sqrt{1 + \frac{1}{z^2} + \frac{1}{z}} \right)^{-i} - \frac{1}{2} i \left( \sqrt{1 + \frac{1}{z^2} + \frac{1}{z}} \right)^i$$

01.06.16.0015.01

$$\sin(i \operatorname{csch}^{-1}(z)) = \frac{i}{z}$$

01.06.16.0027.01

$$\sin\left(\frac{i}{2} \operatorname{csch}^{-1}(z)\right) = \frac{iz}{\sqrt{2}} \sqrt{\frac{1}{z^2}} \sqrt{\sqrt{1 + \frac{1}{z^2}} - 1}$$

01.06.16.0154.01

$$\sin(a \operatorname{csch}^{-1}(z)) = \frac{1}{2} i \left( \sqrt{1 + \frac{1}{z^2} + \frac{1}{z}} \right)^{-ia} - \frac{1}{2} i \left( \sqrt{1 + \frac{1}{z^2} + \frac{1}{z}} \right)^{ia}$$

01.06.16.0052.01

$$\sin(in \operatorname{csch}^{-1}(z)) = \frac{i}{z} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} \left(1 + \frac{1}{z^2}\right)^{\frac{n-1}{2}-k}; n \in \mathbb{N}^+$$

01.06.16.0053.01

$$\sin(in \operatorname{csch}^{-1}(z)) = \frac{i}{z} U_{n-1}\left(\sqrt{1 + \frac{1}{z^2}}\right); n \in \mathbb{N}^+$$

01.06.16.0076.01

$$\sin\left(\frac{in}{2} \operatorname{csch}^{-1}(z)\right) = \frac{i}{z} \left( \sqrt{1 + \frac{1}{z^2} + 1} \right)^{\frac{n}{2}-1} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left( z^2 + \sqrt{-z^2} \sqrt{-z^2-1} \right)^k; n \in \mathbb{N}^+$$

01.06.16.0077.01

$$\sin\left(\frac{in}{2} \operatorname{csch}^{-1}(z)\right) = -\frac{iz}{\sqrt{2}} \sqrt{-\frac{1}{z^2}} \sqrt{1 - \sqrt{1 + \frac{1}{z^2}}} U_{n-1}\left(\frac{1}{\sqrt{2}} \sqrt{\sqrt{1 + \frac{1}{z^2}} + 1}\right); n \in \mathbb{N}^+$$

### Involving $\operatorname{sech}^{-1}$

01.06.16.0155.01

$$\sin(\operatorname{sech}^{-1}(z)) = \frac{1}{2} i \left( \sqrt{\frac{1}{z}-1} \sqrt{1+\frac{1}{z}+\frac{1}{z}} \right)^{-i} - \frac{1}{2} i \left( \sqrt{\frac{1}{z}-1} \sqrt{1+\frac{1}{z}+\frac{1}{z}} \right)^i$$

01.06.16.0016.01

$$\sin(i \operatorname{sech}^{-1}(z)) = \frac{i}{z} \sqrt{\frac{1-z}{1+z}} (1+z)$$

01.06.16.0028.01

$$\sin\left(\frac{i}{2} \operatorname{sech}^{-1}(z)\right) = \frac{i \sqrt{1-z}}{\sqrt{2}} \sqrt{\frac{1}{z}}$$

01.06.16.0156.01

$$\sin(a \operatorname{sech}^{-1}(z)) = \frac{1}{2} i \left( \sqrt{\frac{1}{z}-1} \sqrt{1+\frac{1}{z}+\frac{1}{z}} \right)^{-ia} - \frac{1}{2} i \left( \sqrt{\frac{1}{z}-1} \sqrt{1+\frac{1}{z}+\frac{1}{z}} \right)^{ia}$$

01.06.16.0054.01

$$\sin(in \operatorname{sech}^{-1}(z)) = i \sqrt{\frac{1-z}{1+z}} (1+z) \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} z^{2k-n} /; n \in \mathbb{N}^+$$

01.06.16.0055.01

$$\sin(in \operatorname{sech}^{-1}(z)) = \frac{i}{z} \sqrt{\frac{1-z}{1+z}} (1+z) U_{n-1}\left(\frac{1}{z}\right) /; n \in \mathbb{N}^+$$

01.06.16.0078.01

$$\sin\left(\frac{in}{2} \operatorname{sech}^{-1}(z)\right) = i \sqrt{\frac{1-z}{z}} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{\frac{n}{2}-k-1} \left(\frac{z+1}{z}\right)^{\frac{n-1}{2}-k} /; n \in \mathbb{N}^+$$

01.06.16.0079.01

$$\sin\left(\frac{in}{2} \operatorname{sech}^{-1}(z)\right) = \frac{i}{\sqrt{2}} \sqrt{\frac{1-z}{z}} U_{n-1}\left(\frac{1}{\sqrt{2}} \sqrt{\frac{z+1}{z}}\right) /; n \in \mathbb{N}^+$$

## Argument involving complex components

01.06.16.0080.01

$$\sin(\arg(z)) = \frac{\operatorname{Im}(z)}{|z|}$$

01.06.16.0081.01

$$\sin(\arg(z)) + i \cos(\arg(z)) = \frac{i \bar{z}}{|z|}$$

01.06.16.0082.01

$$\sin(a \arg(z)) = \frac{\operatorname{Re}(z) |z|^{-a}}{2 \operatorname{Im}(z)} \sqrt{-\frac{\operatorname{Im}(z)^2}{\operatorname{Re}(z)^2}} \left( \left( \operatorname{Re}(z) - \operatorname{Re}(z) \sqrt{-\frac{\operatorname{Im}(z)^2}{\operatorname{Re}(z)^2}} \right)^a - \left( \operatorname{Re}(z) + \operatorname{Re}(z) \sqrt{-\frac{\operatorname{Im}(z)^2}{\operatorname{Re}(z)^2}} \right)^a \right)$$

01.06.16.0083.01

$$\sin(a \arg(z)) = \frac{i |z|^{-a} |\operatorname{Im}(z)| |\operatorname{Re}(z)|}{2 \operatorname{Im}(z) \operatorname{Re}(z)} \left( \left( \operatorname{Re}(z) - \frac{i |\operatorname{Im}(z)| |\operatorname{Re}(z)|}{\operatorname{Re}(z)} \right)^a - \left( \operatorname{Re}(z) + \frac{i |\operatorname{Im}(z)| |\operatorname{Re}(z)|}{\operatorname{Re}(z)} \right)^a \right)$$

## Addition formulas

01.06.16.0084.01

$$\sin(a + b) = \sin(a) \cos(b) + \cos(a) \sin(b)$$

01.06.16.0085.01

$$\sin(a - b) = \sin(a) \cos(b) - \cos(a) \sin(b)$$

01.06.16.0086.01

$$\sin(a + i b) = \sin(a) \cosh(b) + i \cos(a) \sinh(b)$$

01.06.16.0087.01

$$\sin(a - i b) = \sin(a) \cosh(b) - i \cos(a) \sinh(b)$$

## Half-angle formulas

01.06.16.0088.02

$$\sin\left(\frac{z}{2}\right) = \sqrt{\frac{1 - \cos(z)}{2}} \quad ; 0 < \operatorname{Re}(z) < 2\pi \vee \operatorname{Re}(z) = 0 \wedge \operatorname{Im}(z) \geq 0 \vee \operatorname{Re}(z) = 2\pi \wedge \operatorname{Im}(z) \leq 0$$

01.06.16.0089.01

$$\sin\left(\frac{z}{2}\right) = (-1)^{\lfloor \frac{\operatorname{Re}(z)}{2\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{2\pi} \rfloor + \lfloor -\frac{\operatorname{Re}(z)}{2\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right) \sqrt{\frac{1 - \cos(z)}{2}}$$

## Multiple arguments

### Argument involving numeric multiples of variable

01.06.16.0090.01

$$\sin(2z) = 2 \sin(z) \cos(z)$$

01.06.16.0091.01

$$\sin(3z) = 3 \sin(z) - 4 \sin^3(z)$$

01.06.16.0092.01

$$\sin(3z) = 3 \cos^2(z) \sin(z) - \sin^3(z)$$

### Argument involving symbolic multiples of variable

01.06.16.0093.01

$$\sin(nz) = \sin(z) \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n-k-1}{k} 2^{n-2k-1} \cos^{n-2k-1}(z) \quad ; n \in \mathbb{N}^+$$

01.06.16.0094.01

$$\sin(nz) = \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^k \binom{n}{2k+1} \sin^{2k+1}(z) \cos^{-2k+n-1}(z) \quad ; n \in \mathbb{N}^+$$

01.06.16.0095.01

$$\sin(nz) = 2^{n-1} \prod_{k=0}^{n-1} \sin\left(\frac{\pi k}{n} + z\right) \quad ; n \in \mathbb{N}^+$$

01.06.16.0096.01

$$\sin(nz) = \sin(z) U_{n-1}(\cos(z))$$

01.06.16.0157.01

$$\sin(az) = \frac{1}{2i} \left( (\cos(z) + i \sin(z))^a e^{-2i\pi a \left[ \frac{\pi - \operatorname{Re}(z)}{2\pi} \right]} - (\cos(z) - i \sin(z))^a e^{-2i\pi a \left[ \frac{\operatorname{Re}(z) + \pi}{2\pi} \right]} \right)$$

## Some functions of arguments

01.06.16.0158.01

$$\sin(a(bz^c)^m) = \sin(ab^m z^{mc}) /; -\pi < \arg(b) + \operatorname{Im}(c \log(z)) \leq \pi$$

01.06.16.0159.01

$$\sin\left(\sqrt{z^2}\right) = \sin(z) /; -\frac{\pi}{2} < \arg(z) \leq \frac{\pi}{2}$$

01.06.16.0160.01

$$\sin\left(\sqrt{z^2}\right) = -\sin(z) /; -\pi < \arg(z) \leq -\frac{\pi}{2} \vee \frac{\pi}{2} < \arg(z) \leq \pi$$

01.06.16.0161.01

$$\sin\left(\sqrt{z^2}\right) = \frac{\sqrt{z^2}}{z} \sin(z)$$

01.06.16.0162.01

$$\sin\left(a\sqrt{bz^2}\right) = \frac{\sqrt{bz^2}}{\sqrt{b}z} \sin\left(a\sqrt{b}z\right)$$

01.06.16.0163.01

$$\begin{aligned} \sin\left(a\sqrt[3]{bz^3}\right) = & -\frac{i e^{-ia\sqrt[3]{bz^3}}}{6b^{2/3}z^2} \left( (-1 + e^{2ia\sqrt[3]{bz^3}}) \left( \sqrt[3]{bz^3} z \sqrt[3]{bz^3} + (bz^3)^{2/3} + b^{2/3}z^2 \right) + e^{\frac{1}{2}ia\sqrt[3]{bz^3}z} \left( \sqrt[3]{bz^3} - \sqrt[3]{bz^3}z \right) \right) \\ & \left( (-1 + e^{ia\sqrt[3]{bz^3}z}) \left( 2z\sqrt[3]{bz^3} + \sqrt[3]{bz^3}z \right) \cosh\left(\frac{1}{2}\sqrt{3}a\sqrt[3]{bz^3}z\right) - i\sqrt{3} \left( 1 + e^{ia\sqrt[3]{bz^3}z} \right) \sqrt[3]{bz^3} \sinh\left(\frac{1}{2}\sqrt{3}a\sqrt[3]{bz^3}z\right) \right) \end{aligned}$$

01.06.16.0164.01

$$\sin\left(a\sqrt[4]{bz^4}\right) = \frac{\sqrt[4]{bz^4}}{2(bz^4)^{3/4}} \left( \left( \sqrt{bz^2} + \sqrt{bz^4} \right) \sin\left(a\sqrt[4]{bz^4}z\right) + \left( \sqrt{bz^2} - \sqrt{bz^4} \right) \sinh\left(a\sqrt[4]{bz^4}z\right) \right)$$

01.06.16.0165.01

$$\begin{aligned} \sin\left(a(bz^n)^{1/n}\right) = & \frac{1}{2} i \sum_{i=0}^{n-1} \left( \frac{(-ia(bz^n)^{1/n})^i}{i!} {}_1F_n\left(1; \frac{i+1}{n}, \frac{i+2}{n}, \dots, \frac{i+n}{n}; \frac{(-i)^n a^n b z^n}{n^n}\right) - \right. \\ & \left. \frac{(ia(bz^n)^{1/n})^i}{i!} {}_1F_n\left(1; \frac{i+1}{n}, \frac{i+2}{n}, \dots, \frac{i+n}{n}; \frac{i^n a^n b z^n}{n^n}\right) \right) /; n \in \mathbb{N}^+ \end{aligned}$$

## Products, sums, and powers of the direct function

### Products of the direct function

01.06.16.0097.01

$$\sin(a) \sin(b) = \frac{1}{2} (\cos(a-b) - \cos(a+b))$$

**Products involving the direct function**

01.06.16.0098.01

$$\sin(a) \cos(b) = \frac{1}{2} (\sin(a-b) + \sin(a+b))$$

01.06.16.0113.01

$$\prod_{k=1}^n \sin(z_k) = (-2)^{-n} \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \cos\left(\sum_{j=1}^n k_j \left(z_j + \frac{\pi}{2}\right)\right)$$

**Sums of the direct function**

01.06.16.0099.01

$$\sin(a) + \sin(b) = 2 \cos\left(\frac{a-b}{2}\right) \sin\left(\frac{a+b}{2}\right)$$

01.06.16.0100.01

$$\sin(a) - \sin(b) = 2 \cos\left(\frac{a+b}{2}\right) \sin\left(\frac{a-b}{2}\right)$$

**Sums involving the direct function****Involving other trigonometric functions****Involving cos**

01.06.16.0114.01

$$\sin(z) + \cos(z) = \sqrt{2} \cos\left(z - \frac{\pi}{4}\right)$$

01.06.16.0115.01

$$\sin(z) - \cos(z) = -\sqrt{2} \cos\left(z + \frac{\pi}{4}\right)$$

01.06.16.0116.01

$$\sin(a) + \cos(b) = 2 \cos\left(\frac{a-b}{2} - \frac{\pi}{4}\right) \cos\left(\frac{a+b}{2} - \frac{\pi}{4}\right)$$

01.06.16.0117.01

$$\sin(a) - \cos(b) = -2 \cos\left(\frac{a+b}{2} + \frac{\pi}{4}\right) \cos\left(\frac{a-b}{2} + \frac{\pi}{4}\right)$$

01.06.16.0118.01

$$a \sin(z) + b \cos(z) = a \sqrt{1 + \frac{b^2}{a^2}} \sin\left(z + \tan^{-1}\left(\frac{b}{a}\right)\right)$$

**Involving hyperbolic functions****Involving sinh**



01.06.16.0119.01

$$\sin(z) + i \sinh(z) = 2 \cos\left(\frac{z e^{-\frac{1}{4}(i\pi)}}{\sqrt{2}}\right) \sin\left(\frac{z e^{\frac{i\pi}{4}}}{\sqrt{2}}\right)$$

01.06.16.0120.01

$$\sin(z) - i \sinh(z) = 2 \cos\left(\frac{z e^{\frac{i\pi}{4}}}{\sqrt{2}}\right) \sin\left(\frac{z e^{-\frac{1}{4}(i\pi)}}{\sqrt{2}}\right)$$

01.06.16.0121.01

$$\sin(a) + i \sinh(b) = 2 \cos\left(\frac{1}{2}(a - i b)\right) \sin\left(\frac{1}{2}(a + b i)\right)$$

01.06.16.0122.01

$$\sin(a) - i \sinh(b) = 2 \cos\left(\frac{1}{2}(a + b i)\right) \sin\left(\frac{1}{2}(a - i b)\right)$$

### Involving cosh

01.06.16.0123.01

$$\sin(z) + \cosh(z) = 2 \cos\left(\frac{z e^{-\frac{1}{4}(i\pi)}}{\sqrt{2}} - \frac{\pi}{4}\right) \cos\left(\frac{z e^{\frac{i\pi}{4}}}{\sqrt{2}} - \frac{\pi}{4}\right)$$

01.06.16.0124.01

$$\sin(z) - \cosh(z) = -2 \cos\left(\frac{e^{\frac{i\pi}{4}} z}{\sqrt{2}} + \frac{\pi}{4}\right) \cos\left(\frac{e^{-\frac{1}{4}(i\pi)} z}{\sqrt{2}} + \frac{\pi}{4}\right)$$

01.06.16.0125.01

$$\sin(a) + \cosh(b) = 2 \cos\left(\frac{1}{2}(a - i b) - \frac{\pi}{4}\right) \cos\left(\frac{1}{2}(a + b i) - \frac{\pi}{4}\right)$$

01.06.16.0126.01

$$\sin(a) - \cosh(b) = -2 \cos\left(\frac{1}{2}(a + b i) + \frac{\pi}{4}\right) \cos\left(\frac{1}{2}(a - i b) + \frac{\pi}{4}\right)$$

### Powers of the direct function

01.06.16.0101.01

$$\sin^2(z) = \frac{1}{2}(1 - \cos(2z))$$

01.06.16.0102.01

$$\sin^3(z) = \frac{1}{4}(3 \sin(z) - \sin(3z))$$

01.06.16.0103.01

$$\sin^{2n}(z) = 2^{-2n} \binom{2n}{n} + 2^{1-2n} \sum_{k=0}^{n-1} (-1)^{n-k} \binom{2n}{k} \cos(2(n-k)z) ; n \in \mathbb{N}^+$$

01.06.16.0127.01

$$\sin^{2n}(z) = 2^{1-2n} \sum_{k=0}^{n-1} (-1)^{n-k} \binom{2n}{k} (\cos(2(n-k)z) - 1) ; n \in \mathbb{N}^+$$

01.06.16.0104.01

$$\sin^{2n-1}(z) = 2^{2-2n} \sum_{k=0}^{n-1} (-1)^{n-k-1} \binom{2n-1}{k} \sin((2n-2k-1)z); n \in \mathbb{N}^+$$

01.06.16.0105.01

$$\sin^n(z) = 2^{-n} \binom{n}{\frac{n}{2}} (1 - n \bmod 2) - 2^{1-n} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^{k+n-1} \binom{n}{k} \cos\left(\frac{\pi n}{2} + (n-2k)z\right); n \in \mathbb{N}^+$$

### Powers involving the direct function

01.06.16.0106.01

$$(\cos(z) + i \sin(z))^n = \cos(nz) + i \sin(nz); n \in \mathbb{N}^+$$

De Moivre's theorem

01.06.16.0107.01

$$(\cos(z) + i \sin(z))^n = e^{inz}; n \in \mathbb{N}^+$$

01.06.16.0108.01

$$(\cos(z) - i \sin(z))^n = \cos(nz) - i \sin(nz); n \in \mathbb{N}^+$$

01.06.16.0109.01

$$(\cos(z) - i \sin(z))^n = e^{-inz}; n \in \mathbb{N}^+$$

### Sums of powers involving the direct function

01.06.16.0110.01

$$\sin^2(a) - \sin^2(b) = \sin(a-b) \sin(a+b)$$

01.06.16.0111.01

$$\sin^2(a) - \cos^2(b) = -\cos(a-b) \cos(a+b)$$

### Related transformations

01.06.16.0112.01

$$\sin(a \sin^{-1}(z)) = \frac{\sqrt{z^2}}{z} \sin\left(\frac{1}{2} a \cos^{-1}(1 - 2z^2)\right)$$

## Identities

### Functional identities

#### Univariate functional identities

01.06.17.0001.01

$$\sin^2(2z) = 4(1 - \sin^2(z)) \sin^2(z)$$

01.06.17.0002.01

$$\sin^4(z_1 + z_2) - 2(-2 \sin^2(z_2) \sin^2(z_1) + \sin^2(z_1) + \sin^2(z_2)) \sin^2(z_1 + z_2) + (\sin^2(z_1) - \sin^2(z_2))^2 = 0$$

01.06.17.0003.01

$$\sin(z) = n \sin\left(\frac{z}{n}\right) \prod_{k=1}^{\lfloor \frac{n}{2} \rfloor} \left(1 - \frac{\sin^2\left(\frac{z}{n}\right)}{\sin^2\left(\frac{4k\pi}{2n}\right)}\right); \frac{n-1}{2} \in \mathbb{N}^+$$

**Biivariate functional identities**

01.06.17.0004.01

$$|g(x + iy)| = |g(x) + g(iy)|; g(z) = c \sin(dz) \wedge d \in \mathbb{R} \wedge x \in \mathbb{R} \wedge y \in \mathbb{R}$$

01.06.17.0005.01

$$g(x+y)g(x-y) = g(x)^2 - g(y)^2; g(z) = \sin(cz) \wedge x \in \mathbb{R} \wedge y \in \mathbb{R}$$

**Complex characteristics****Real part**

01.06.19.0001.01

$$\operatorname{Re}(\sin(x + iy)) = \cosh(y) \sin(x)$$

**Imaginary part**

01.06.19.0002.01

$$\operatorname{Im}(\sin(x + iy)) = \cos(x) \sinh(y)$$

**Absolute value**

01.06.19.0003.01

$$|\sin(x + iy)| = \sqrt{\frac{\cosh(2y) - \cos(2x)}{2}}$$

01.06.19.0004.01

$$|\sin(x + iy)| = \sqrt{\cosh^2(y) \sin^2(x) + \cos^2(x) \sinh^2(y)}$$

01.06.19.0008.01

$$|\sin(x + iy)| = |\sin(x) + \sin(iy)|; x \in \mathbb{R} \wedge y \in \mathbb{R}$$

**Argument**

01.06.19.0005.01

$$\arg(\sin(x + iy)) = \tan^{-1}(\cot(x) \tanh(y)) + \frac{\pi}{2} \operatorname{sgn}\left(\operatorname{sgn}(\cos(x) \sinh(y)) + \frac{1}{2}\right) \left(1 - \operatorname{sgn}(\cosh(y) \sin(x))\right)$$

01.06.19.0006.01

$$\arg(\sin(x + iy)) = \tan^{-1}(\cosh(y) \sin(x), \cos(x) \sinh(y))$$

**Conjugate value**

01.06.19.0007.01

$$\overline{\sin(x + iy)} = \cosh(y) \sin(x) - i \cos(x) \sinh(y)$$

**Differentiation**

## Low-order differentiation

01.06.20.0001.01

$$\frac{\partial \sin(z)}{\partial z} = \cos(z)$$

01.06.20.0002.01

$$\frac{\partial^2 \sin(z)}{\partial z^2} = -\sin(z)$$

## Symbolic differentiation

01.06.20.0003.02

$$\frac{\partial^n \sin(z)}{\partial z^n} = \sin\left(z + \frac{\pi n}{2}\right); n \in \mathbb{N}$$

01.06.20.0004.01

$$\frac{\partial^n f(\sin(z))}{\partial z^n} = \sum_{m=1}^n \frac{1}{m!} \left( \sum_{j=0}^{m-1} \binom{m}{j} \sum_{l=0}^{m-j} (-1)^j 2^{j-m} \sin^j(z) (j+2l-m)^n \exp\left(-\frac{i}{2}(n\pi - (j+2l-m)(\pi-2z))\right) \binom{m-j}{l} f^{(m)}(\sin(z)) \right); n \in \mathbb{N}^+$$

01.06.20.0005.02

$$\frac{\partial^n f(\sin(z))}{\partial z^n} = \sum_{m=0}^n \frac{f^{(m)}(\sin(z))}{m!} \left( \frac{\partial^n (\sin(y) - \sin(z))^m}{\partial y^n} / \{y \rightarrow z\} \right); n \in \mathbb{N}$$

01.06.20.0007.02

$$\frac{\partial^n \sin(az+b)}{\partial z^n} = a^n \sin\left(az+b + \frac{n\pi}{2}\right); n \in \mathbb{N}$$

01.06.20.0011.01

$$\frac{\partial^n \sin^m(z)}{\partial z^n} = i^{m+n} 2^{-m} \sum_{k=0}^m (-1)^k \binom{m}{k} (2k-m)^n e^{(2k-m)iz}; m \in \mathbb{N} \wedge n \in \mathbb{N}^+$$

01.06.20.0012.01

$$\frac{\partial^n \sin^m(z)}{\partial z^n} = 2^{-m} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^n (i^{n-m} e^{(m-2k)iz} + i^{m-n} e^{-(m-2k)iz}); m \in \mathbb{N} \wedge n \in \mathbb{N}^+$$

01.06.20.0008.02

$$\frac{\partial^n \sin^m(z)}{\partial z^n} = 2^{1-m} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} (m-2k)^n \cos\left(\frac{1}{2}\pi(m+n) + (m-2k)z\right); m \in \mathbb{N} \wedge n \in \mathbb{N}^+$$

01.06.20.0013.01

$$\frac{\partial^n \sin^m(z)}{\partial z^n} = 2^{-m} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^n ((i^{n-m} + i^{m-n}) \cos((m-2k)z) + i(i^{n-m} - i^{m-n}) \sin((m-2k)z)); m \in \mathbb{N} \wedge n \in \mathbb{N}^+$$

01.06.20.0014.01

$$\frac{\partial^n \sin^m(z)}{\partial z^n} = 2^{-m} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^n \left( i (i^{n-m} - i^{m-n}) \sum_{j=0}^{\lfloor \frac{m-1}{2} \rfloor - k} (-1)^j \binom{m-2k}{2j+1} \sin^{2j+1}(z) \cos^{-2j-2k+m-1}(z) + (i^{n-m} + i^{m-n}) \sum_{j=0}^{\lfloor \frac{m}{2} \rfloor - k} (-1)^j \binom{m-2k}{2j} \sin^{2j}(z) \cos^{-2j-2k+m}(z) \right) /; m \in \mathbb{N} \wedge n \in \mathbb{N}^+$$

### Fractional integro-differentiation

01.06.20.0006.01

$$\frac{\partial^\alpha \sin(z)}{\partial z^\alpha} = 2^{\alpha-1} \sqrt{\pi} z^{1-\alpha} {}_1\tilde{F}_2\left(1; 1 - \frac{\alpha}{2}, \frac{3}{2} - \frac{\alpha}{2}; -\frac{z^2}{4}\right)$$

01.06.20.0009.01

$$\frac{\partial^\alpha \sin(az + b)}{\partial z^\alpha} = 2^{\alpha-1} \sqrt{\pi} z^{-\alpha} \left( a z \cos(b) {}_1\tilde{F}_2\left(1; 1 - \frac{\alpha}{2}, \frac{3}{2} - \frac{\alpha}{2}; -\frac{1}{4} a^2 z^2\right) + 2 {}_1\tilde{F}_2\left(1; \frac{1}{2} - \frac{\alpha}{2}, 1 - \frac{\alpha}{2}; -\frac{1}{4} a^2 z^2\right) \sin(b) \right)$$

01.06.20.0010.01

$$\frac{\partial^\alpha \sin^n(z)}{\partial z^\alpha} = \frac{2^{-n} (1 - n \bmod 2) z^{-\alpha}}{\Gamma(1 - \alpha)} \binom{n}{\frac{n}{2}} - 2^{\alpha-n} \sqrt{\pi} z^{-\alpha} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^{k+n-1} \binom{n}{k} \left( 2 \cos\left(\frac{n\pi}{2}\right) {}_1\tilde{F}_2\left(1; \frac{1}{2} - \frac{\alpha}{2}, 1 - \frac{\alpha}{2}; -\frac{1}{4} (n-2k)^2 z^2\right) - (n-2k) z {}_1\tilde{F}_2\left(1; 1 - \frac{\alpha}{2}, \frac{3}{2} - \frac{\alpha}{2}; -\frac{1}{4} (n-2k)^2 z^2\right) \sin\left(\frac{n\pi}{2}\right) \right) /; n \in \mathbb{N}^+$$

01.06.20.0015.01

$$\frac{\partial^\alpha (z^\beta \sin(z))^a}{\partial z^\alpha} = e^{2i a \pi \left[ \frac{1}{2} - \frac{\arg\left(\frac{\sin(z)}{z}\right)}{2\pi} - \frac{\text{Im}((\beta+1)\log(z))}{2\pi} \right]} a z^{(\beta+1)a-\alpha} \sum_{k=0}^{\infty} \binom{k-a}{k} \sum_{j=0}^k \frac{(-1)^j}{a-j} \binom{k}{j} p_{j,k} \mathcal{FC}_{\exp}^{(\alpha)}(z, (\beta+1)a+k) z^k /;$$

$$p_{j,0} = 1 \wedge p_{j,k} = \frac{1}{k} \sum_{m=1}^k \frac{(jm+m-k)(-m+2\lfloor \frac{m}{2} \rfloor+1)(-1)^{m/2}}{(m+1)!} p_{j,k-m} \wedge k \in \mathbb{N}^+$$

## Integration

### Indefinite integration

#### Involving only one direct function

01.06.21.0024.01

$$\int \sin(b + az) dz = -\frac{\cos(b + az)}{a}$$

01.06.21.0025.01

$$\int \sin(az) dz = -\frac{\cos(az)}{a}$$

01.06.21.0026.01

$$\int \sin(z) dz = -\cos(z)$$

**Involving one direct function and elementary functions**

## Involving power function

Involving power

### Power arguments

01.06.21.0027.01

$$\int \sin(a z^r) dz = -\frac{iz}{2r} \left( (i a z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i a z^r\right) - (-i a z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i a z^r\right) \right)$$

01.06.21.0028.01

$$\int \sin(a z^2) dz = \frac{1}{\sqrt{a}} \sqrt{\frac{\pi}{2}} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right)$$

01.06.21.0029.01

$$\int \sin(a \sqrt{z}) dz = \frac{2 \sin(a \sqrt{z}) - 2 a \sqrt{z} \cos(a \sqrt{z})}{a^2}$$

01.06.21.0030.01

$$\int \sin(a (z^r)^p) dz = \frac{iz}{2pr} \left( (-i a (z^r)^p)^{-\frac{1}{pr}} \Gamma\left(\frac{1}{pr}, -i a (z^r)^p\right) - (i a (z^r)^p)^{-\frac{1}{pr}} \Gamma\left(\frac{1}{pr}, i a (z^r)^p\right) \right)$$

01.06.21.0031.01

$$\int \sin(a (z^r)^{1/r}) dz = -\frac{z (z^r)^{-1/r} \cos(a (z^r)^{1/r})}{a}$$

01.06.21.0032.01

$$\int \sin(a \sqrt{z^2}) dz = -\frac{\sqrt{z^2} \cos(a \sqrt{z^2})}{a z}$$

## Involving $z^{\alpha-1}$ and arguments $a z$

01.06.21.0033.01

$$\int z^{\alpha-1} \sin(a z) dz = \frac{1}{2} i z^\alpha (E_{1-\alpha}(-i a z) - E_{1-\alpha}(i a z))$$

01.06.21.0034.01

$$\int z^{\alpha-1} \sin(z) dz = \frac{1}{2} i z^\alpha (z^2)^{-\alpha} ((i z)^\alpha \Gamma(\alpha, -i z) - (-i z)^\alpha \Gamma(\alpha, i z))$$

01.06.21.0035.01

$$\int z^n \sin(a z) dz = -\frac{i^n (\Gamma(n+1, -i a z) + (-1)^n \Gamma(n+1, i a z))}{2 a^{n+1}} ; n \in \mathbb{Z}$$

01.06.21.0036.01

$$\int z^n \sin(az) dz = \frac{1}{2} i (-ia)^{-n-1} \left( \frac{\text{Ei}(-ia z) + (-1)^n \text{Ei}(ia z)}{(-n-1)!} + e^{ia z} \left( \sum_{k=0}^n \frac{(-ia z)^k}{(n+1)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(-ia z)^k}{(n+1)_{k-n}} \right) + (-1)^n e^{-ia z} \left( \sum_{k=0}^n \frac{(ia z)^k}{(n+1)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(ia z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0037.01

$$\int z \sin(az) dz = \frac{\sin(az) - az \cos(az)}{a^2}$$

01.06.21.0038.01

$$\int z^2 \sin(az) dz = \frac{(2 - a^2 z^2) \cos(az) + 2az \sin(az)}{a^3}$$

01.06.21.0039.01

$$\int z^3 \sin(az) dz = \frac{3(a^2 z^2 - 2) \sin(az) - az(a^2 z^2 - 6) \cos(az)}{a^4}$$

01.06.21.0040.01

$$\int z^4 \sin(az) dz = \frac{4az(a^2 z^2 - 6) \sin(az) - (a^4 z^4 - 12a^2 z^2 + 24) \cos(az)}{a^5}$$

01.06.21.0041.01

$$\int z^5 \sin(az) dz = \frac{5(a^4 z^4 - 12a^2 z^2 + 24) \sin(az) - az(a^4 z^4 - 20a^2 z^2 + 120) \cos(az)}{a^6}$$

01.06.21.0042.01

$$\int z^6 \sin(az) dz = \frac{(-a^6 z^6 + 30a^4 z^4 - 360a^2 z^2 + 720) \cos(az) + 6az(a^4 z^4 - 20a^2 z^2 + 120) \sin(az)}{a^7}$$

01.06.21.0043.01

$$\int z^7 \sin(az) dz = \frac{1}{a^8} (7(a^6 z^6 - 30a^4 z^4 + 360a^2 z^2 - 720) \sin(az) - az(a^6 z^6 - 42a^4 z^4 + 840a^2 z^2 - 5040) \cos(az))$$

01.06.21.0044.01

$$\int z^8 \sin(az) dz = \frac{1}{a^9} (8az(a^6 z^6 - 42a^4 z^4 + 840a^2 z^2 - 5040) \sin(az) - (a^8 z^8 - 56a^6 z^6 + 1680a^4 z^4 - 20160a^2 z^2 + 40320) \cos(az))$$

01.06.21.0045.01

$$\int \frac{\sin(az)}{z} dz = \text{Si}(az)$$

01.06.21.0046.01

$$\int \frac{\sin(az)}{z^2} dz = a \text{Ci}(az) - \frac{\sin(az)}{z}$$

01.06.21.0047.01

$$\int \frac{\sin(az)}{z^3} dz = -\frac{a^2 \text{Si}(az) z^2 + a \cos(az) z + \sin(az)}{2z^2}$$

01.06.21.0048.01

$$\int \frac{\sin(az)}{z^4} dz = -\frac{a^3 \operatorname{Ci}(az) z^3 + a \cos(az) z + (2 - a^2 z^2) \sin(az)}{6 z^3}$$

01.06.21.0049.01

$$\int \frac{\sin(az)}{z^5} dz = \frac{a^4 \operatorname{Si}(az) z^4 + a(a^2 z^2 - 2) \cos(az) z + (a^2 z^2 - 6) \sin(az)}{24 z^4}$$

01.06.21.0050.01

$$\int z^{n+\frac{1}{2}} \sin(az) dz = -\frac{i^n a^{-n-1} \sqrt{z}}{2 \sqrt{a^2 z^2}} \left( \sqrt{iaz} \Gamma\left(n + \frac{3}{2}, -iaz\right) + (-1)^n \sqrt{-iaz} \Gamma\left(n + \frac{3}{2}, iaz\right) \right); n \in \mathbb{Z}$$

01.06.21.0051.01

$$\int z^{n+\frac{1}{2}} \sin(az) dz = -\frac{i(-1)^n (ia)^{-n-1} \sqrt{z}}{2 \sqrt{a^2 z^2}} \left( \left( \sqrt{iaz} \operatorname{erfc}(\sqrt{-iaz}) + (-1)^n \sqrt{-iaz} \operatorname{erfc}(\sqrt{iaz}) \right) \Gamma\left(n + \frac{3}{2}\right) + e^{iaz} \sqrt{iaz} \left( \sum_{k=0}^n \frac{(-iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(-iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) + (-1)^n e^{-iaz} \sqrt{-iaz} \left( \sum_{k=0}^n \frac{(iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0052.01

$$\int \sqrt{z} \sin(az) dz = \frac{1}{a^{3/2}} \sqrt{\frac{\pi}{2}} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) - \frac{\sqrt{z} \cos(az)}{a}$$

01.06.21.0053.01

$$\int z^{3/2} \sin(az) dz = \frac{1}{4 a^{5/2}} \left( 2 \sqrt{a} \sqrt{z} (3 \sin(az) - 2 a z \cos(az)) - 3 \sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \right)$$

01.06.21.0054.01

$$\int z^{5/2} \sin(az) dz = \frac{1}{8 a^{7/2}} \left( 2 \sqrt{a} \sqrt{z} ((15 - 4 a^2 z^2) \cos(az) + 10 a z \sin(az)) - 15 \sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \right)$$

01.06.21.0055.01

$$\int z^{7/2} \sin(az) dz = \frac{1}{16 a^{9/2}} \left( 105 \sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) + 2 \sqrt{a} \sqrt{z} ((70 a z - 8 a^3 z^3) \cos(az) + 7(4 a^2 z^2 - 15) \sin(az)) \right)$$

01.06.21.0056.01

$$\int z^{9/2} \sin(az) dz = \frac{1}{32 a^{11/2}} \left( 945 \sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) - 2 \sqrt{a} \sqrt{z} ((16 a^4 z^4 - 252 a^2 z^2 + 945) \cos(az) + 18 a z (35 - 4 a^2 z^2) \sin(az)) \right)$$

01.06.21.0057.01

$$\int \frac{\sin(az)}{\sqrt{z}} dz = \frac{\sqrt{2\pi}}{\sqrt{a}} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right)$$

01.06.21.0058.01

$$\int \frac{\sin(az)}{z^{3/2}} dz = 2 \sqrt{a} \sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) - \frac{2 \sin(az)}{\sqrt{z}}$$



01.06.21.0059.01

$$\int \frac{\sin(az)}{z^{5/2}} dz = -\frac{2}{3 z^{3/2}} \left( 2 a^{3/2} \sqrt{2\pi} S \left( \sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z} \right) z^{3/2} + 2 a \cos(az) z + \sin(az) \right)$$

01.06.21.0060.01

$$\int \frac{\sin(az)}{z^{7/2}} dz = \frac{1}{15 z^{5/2}} \left( -8 a^{5/2} \sqrt{2\pi} C \left( \sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z} \right) z^{5/2} - 4 a \cos(az) z + 2 (4 a^2 z^2 - 3) \sin(az) \right)$$

01.06.21.0061.01

$$\int \frac{\sin(az)}{z^{9/2}} dz = \frac{2}{105 z^{7/2}} \left( 8 a^{7/2} \sqrt{2\pi} S \left( \sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z} \right) z^{7/2} + 2 a (4 a^2 z^2 - 3) \cos(az) z + (4 a^2 z^2 - 15) \sin(az) \right)$$

### Involving $z^{\alpha-1}$ and arguments $az + b$

01.06.21.0062.01

$$\int z^{\alpha-1} \sin(b + az) dz = \frac{1}{2} i e^{-ib} z^\alpha (e^{2ib} E_{1-\alpha}(-iaz) - E_{1-\alpha}(iaz))$$

01.06.21.0063.01

$$\int z^n \sin(b + az) dz = -\frac{1}{2} i^n a^{-n-1} (e^{ib} \Gamma(n+1, -iaz) + (-1)^n e^{-ib} \Gamma(n+1, iaz)); n \in \mathbb{Z}$$

01.06.21.0064.01

$$\int z^n \sin(b + az) dz = \frac{1}{2} i (-ia)^{-n-1} \left( \frac{e^{-ib} \text{Ei}(-iaz) + (-1)^n e^{ib} \text{Ei}(iaz)}{(-n-1)!} + e^{ib+iaz} \left( \sum_{k=0}^n \frac{(-iaz)^k}{(n+1)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(-iaz)^k}{(n+1)_{k-n}} \right) + (-1)^n e^{-ib-iaz} \left( \sum_{k=0}^n \frac{(iaz)^k}{(n+1)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(iaz)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0065.01

$$\int z \sin(b + az) dz = \frac{\sin(b + az) - az \cos(b + az)}{a^2}$$

01.06.21.0066.01

$$\int z^2 \sin(b + az) dz = \frac{(2 - a^2 z^2) \cos(b + az) + 2 az \sin(b + az)}{a^3}$$

01.06.21.0067.01

$$\int z^3 \sin(b + az) dz = \frac{3(a^2 z^2 - 2) \sin(b + az) - az(a^2 z^2 - 6) \cos(b + az)}{a^4}$$

01.06.21.0068.01

$$\int z^4 \sin(b + az) dz = \frac{4az(a^2 z^2 - 6) \sin(b + az) - (a^4 z^4 - 12 a^2 z^2 + 24) \cos(b + az)}{a^5}$$

01.06.21.0069.01

$$\int z^5 \sin(b + az) dz = \frac{5(a^4 z^4 - 12 a^2 z^2 + 24) \sin(b + az) - az(a^4 z^4 - 20 a^2 z^2 + 120) \cos(b + az)}{a^6}$$

01.06.21.0070.01

$$\int \frac{\sin(b + az)}{z} dz = \text{Ci}(az) \sin(b) + \cos(b) \text{Si}(az)$$

01.06.21.0071.01

$$\int \frac{\sin(b + az)}{z^2} dz = a \cos(b) \text{Ci}(az) - \frac{\sin(b + az) + az \sin(b) \text{Si}(az)}{z}$$

01.06.21.0072.01

$$\int \frac{\sin(b + az)}{z^3} dz = -\frac{a^2 \text{Ci}(az) \sin(b) z^2 + a^2 \cos(b) \text{Si}(az) z^2 + a \cos(b + az) z + \sin(b + az)}{2 z^2}$$

01.06.21.0073.01

$$\int \frac{\sin(b + az)}{z^4} dz = -\frac{1}{6 z^3} (a^3 \cos(b) \text{Ci}(az) z^3 - a^3 \sin(b) \text{Si}(az) z^3 - a^2 \sin(b + az) z^2 + a \cos(b + az) z + 2 \sin(b + az))$$

01.06.21.0074.01

$$\int \frac{\sin(b + az)}{z^5} dz = \frac{1}{24 z^4} (a^4 \text{Ci}(az) \sin(b) z^4 + a^4 \cos(b) \text{Si}(az) z^4 + a^3 \cos(b + az) z^3 + a^2 \sin(b + az) z^2 - 2 a \cos(b + az) z - 6 \sin(b + az))$$

01.06.21.0075.01

$$\int z^{n+\frac{1}{2}} \sin(b + az) dz = -\frac{i}{2 \sqrt{a^2 z^2}} \left( (ia)^{-n-1} \sqrt{z} \left( (-1)^n e^{ib} \sqrt{iaz} \Gamma\left(n + \frac{3}{2}, -iaz\right) + e^{-ib} \sqrt{-iaz} \Gamma\left(n + \frac{3}{2}, iaz\right) \right) \right); n \in \mathbf{Z}$$

01.06.21.0076.01

$$\int z^{n+\frac{1}{2}} \sin(b + az) dz = -\frac{i (-1)^n (ia)^{-n-1} e^{-ib} \sqrt{z}}{2 \sqrt{a^2 z^2}} \left( \left( e^{2ib} \sqrt{iaz} \operatorname{erfc}(\sqrt{-iaz}) + (-1)^n \sqrt{-iaz} \operatorname{erfc}(\sqrt{iaz}) \right) \Gamma\left(n + \frac{3}{2}\right) + e^{2ib+iaz} \sqrt{iaz} \left( \sum_{k=0}^n \frac{(-iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(-iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) + (-1)^n e^{-iaz} \sqrt{-iaz} \left( \sum_{k=0}^n \frac{(iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(iaz)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) \right); n \in \mathbf{Z}$$

01.06.21.0077.01

$$\int \sqrt{z} \sin(b + az) dz = -\frac{1}{2 a^{3/2}} \left( 2 \sqrt{a} \sqrt{z} \cos(b + az) - \sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) + \sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) \right)$$

01.06.21.0078.01

$$\int z^{3/2} \sin(b + az) dz = \frac{1}{4 a^{5/2}} \left( -3 \sqrt{2\pi} \cos(b) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) - 3 \sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) + 2 \sqrt{a} \sqrt{z} (3 \sin(b + az) - 2 a z \cos(b + az)) \right)$$

01.06.21.0079.01

$$\int z^{5/2} \sin(b + az) dz = \frac{1}{8a^{7/2}} \left( -15\sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) + 15\sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) + 2\sqrt{a} \sqrt{z} \left( (15 - 4a^2 z^2) \cos(b + az) + 10az \sin(b + az) \right) \right)$$

01.06.21.0080.01

$$\int z^{7/2} \sin(b + az) dz = \frac{1}{16a^{9/2}} \left( 105\sqrt{2\pi} \cos(b) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) + 105\sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) + 2\sqrt{a} \sqrt{z} \left( (70az - 8a^3 z^3) \cos(b + az) + 7(4a^2 z^2 - 15) \sin(b + az) \right) \right)$$

01.06.21.0081.01

$$\int z^{9/2} \sin(b + az) dz = \frac{1}{32a^{11/2}} \left( 945\sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) - 945\sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) - 2\sqrt{a} \sqrt{z} \left( (16a^4 z^4 - 252a^2 z^2 + 945) \cos(b + az) + 18az(35 - 4a^2 z^2) \sin(b + az) \right) \right)$$

01.06.21.0082.01

$$\int \frac{\sin(b + az)}{\sqrt{z}} dz = \frac{\sqrt{2\pi}}{\sqrt{a}} \left( \cos(b) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) + C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) \right)$$

01.06.21.0083.01

$$\int \frac{\sin(b + az)}{z^{3/2}} dz = 2\sqrt{a} \sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) - 2\sqrt{a} \sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) - \frac{2\sin(b + az)}{\sqrt{z}}$$

01.06.21.0084.01

$$\int \frac{\sin(b + az)}{z^{5/2}} dz = -\frac{1}{3z^{3/2}} \left( 2 \left( 2a^{3/2} \sqrt{2\pi} \cos(b) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) z^{3/2} + 2a^{3/2} \sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) z^{3/2} + 2a \cos(b + az) z + \sin(b + az) \right) \right)$$

01.06.21.0085.01

$$\int \frac{\sin(b + az)}{z^{7/2}} dz = -\frac{1}{15z^{5/2}} \left( 2 \left( 4a^{5/2} \sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) z^{5/2} - 4a^{5/2} \sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z}\right) \sin(b) z^{5/2} - 4a^2 \sin(b + az) z^2 + 2a \cos(b + az) z + 3 \sin(b + az) \right) \right)$$

01.06.21.0086.01

$$\int \frac{\sin(b + a z)}{z^{9/2}} dz = \frac{1}{105 z^{7/2}} \left( 2 \left( 8 a^{7/2} \sqrt{2\pi} \cos(b) S \left( \sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z} \right) z^{7/2} + 8 a^{7/2} \sqrt{2\pi} C \left( \sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{z} \right) \sin(b) z^{7/2} + 8 a^3 \cos(b + a z) z^3 + 4 a^2 \sin(b + a z) z^2 - 6 a \cos(b + a z) z - 15 \sin(b + a z) \right) \right)$$

**Involving  $z^{\alpha-1}$  and arguments  $a z^r$**

01.06.21.0087.01

$$\int z^{\alpha-1} \sin(a z^r) dz = -\frac{i z^\alpha}{2r} \left( (i a z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, i a z^r\right) - (-i a z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -i a z^r\right) \right)$$

01.06.21.0088.01

$$\int \frac{\sin(a z^r)}{z} dz = \frac{\text{Si}(a z^r)}{r}$$

01.06.21.0089.01

$$\int z^{2n} \sin(a z^2) dz = \frac{i z}{4} \left( \frac{(-i a)^{-n}}{\sqrt{-i a z^2}} \left( \text{erfc}\left(\sqrt{-i a z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{i a z^2} \sum_{k=0}^{n-1} \frac{(-i a z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{i a z^2} \sum_{k=n}^{-1} \frac{(-i a z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) - \frac{(i a)^{-n}}{\sqrt{i a z^2}} \left( \text{erfc}\left(\sqrt{i a z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{-i a z^2} \sum_{k=0}^{n-1} \frac{(i a z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{-i a z^2} \sum_{k=n}^{-1} \frac{(i a z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0090.01

$$\int z^{2n-1} \sin(a z^2) dz = \frac{1}{4} i \left( (-i a)^{-n} \left( \frac{(-1)^{n-1} \text{Ei}(i a z^2)}{(-n)!} + e^{i a z^2} \sum_{k=0}^{n-1} \frac{(-i a z^2)^k}{(n)_{k-n+1}} - e^{i a z^2} \sum_{k=n}^{-1} \frac{(-i a z^2)^k}{(n)_{k-n+1}} \right) - (i a)^{-n} \left( \frac{(-1)^{n-1} \text{Ei}(-i a z^2)}{(-n)!} + e^{-i a z^2} \sum_{k=0}^{n-1} \frac{(i a z^2)^k}{(n)_{k-n+1}} - e^{-i a z^2} \sum_{k=n}^{-1} \frac{(i a z^2)^k}{(n)_{k-n+1}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0091.01

$$\int z \sin(a z^2) dz = -\frac{\cos(a z^2)}{2a}$$

01.06.21.0092.01

$$\int z^2 \sin(a z^2) dz = \frac{1}{4} \left( \frac{\sqrt{2\pi}}{a^{3/2}} C \left( \sqrt{a} \sqrt{\frac{2}{\pi}} z \right) - \frac{2 z \cos(a z^2)}{a} \right)$$

01.06.21.0093.01

$$\int z^3 \sin(a z^2) dz = \frac{\sin(a z^2) - a z^2 \cos(a z^2)}{2 a^2}$$

01.06.21.0094.01

$$\int z^4 \sin(a z^2) dz = \frac{1}{8} \left( \frac{6 z \sin(a z^2) - 4 a z^3 \cos(a z^2)}{a^2} - \frac{3 \sqrt{2 \pi}}{a^{5/2}} S \left( \sqrt{a} \sqrt{\frac{2}{\pi}} z \right) \right)$$

01.06.21.0095.01

$$\int z^5 \sin(a z^2) dz = \frac{2 a \sin(a z^2) z^2 + (2 - a^2 z^4) \cos(a z^2)}{2 a^3}$$

01.06.21.0096.01

$$\int \frac{\sin(a z^2)}{z} dz = \frac{1}{2} \text{Si}(a z^2)$$

01.06.21.0097.01

$$\int \frac{\sin(a z^2)}{z^2} dz = \sqrt{a} \sqrt{2 \pi} C \left( \sqrt{a} \sqrt{\frac{2}{\pi}} z \right) - \frac{\sin(a z^2)}{z}$$

01.06.21.0098.01

$$\int \frac{\sin(a z^2)}{z^3} dz = \frac{1}{2} \left( a \text{Ci}(a z^2) - \frac{\sin(a z^2)}{z^2} \right)$$

01.06.21.0099.01

$$\int \frac{\sin(a z^2)}{z^4} dz = -\frac{1}{3 z^3} \left( 2 \sqrt{2 \pi} z^3 S \left( \sqrt{a} \sqrt{\frac{2}{\pi}} z \right) a^{3/2} + 2 z^2 \cos(a z^2) a + \sin(a z^2) \right)$$

01.06.21.0100.01

$$\int \frac{\sin(a z^2)}{z^5} dz = -\frac{a^2 \text{Si}(a z^2) z^4 + a \cos(a z^2) z^2 + \sin(a z^2)}{4 z^4}$$

01.06.21.0101.01

$$\int z^n \sin(a \sqrt{z}) dz = i a^{-2(n+1)} (-1)^{n-1} \left( \frac{\text{Ei}(-i a \sqrt{z})}{(-2n-2)!} + e^{i a \sqrt{z}} \sum_{k=0}^{2n+1} \frac{(-i a \sqrt{z})^k}{(2n+2)_{k-2n-1}} - e^{i a \sqrt{z}} \sum_{k=2n+2}^{-1} \frac{(-i a \sqrt{z})^k}{(2n+2)_{k-2n-1}} - e^{-i a \sqrt{z}} \sum_{k=0}^{2n+1} \frac{(i a \sqrt{z})^k}{(2n+2)_{k-2n-1}} + e^{-i a \sqrt{z}} \sum_{k=2n+2}^{-1} \frac{(i a \sqrt{z})^k}{(2n+2)_{k-2n-1}} - \frac{\text{Ei}(i a \sqrt{z})}{(-2n-2)!} \right); n \in \mathbb{Z}$$

01.06.21.0102.01

$$\int z \sin(a \sqrt{z}) dz = -\frac{2 \left( a \sqrt{z} (a^2 z - 6) \cos(a \sqrt{z}) - 3 (a^2 z - 2) \sin(a \sqrt{z}) \right)}{a^4}$$

01.06.21.0103.01

$$\int z^2 \sin(a \sqrt{z}) dz = -\frac{2 \left( a \sqrt{z} (z^2 a^4 - 20 z a^2 + 120) \cos(a \sqrt{z}) - 5 (z^2 a^4 - 12 z a^2 + 24) \sin(a \sqrt{z}) \right)}{a^6}$$

01.06.21.0104.01

$$\int z^3 \sin(a \sqrt{z}) dz = -\frac{1}{a^8} \left( 2 \left( a \sqrt{z} (z^3 a^6 - 42 z^2 a^4 + 840 z a^2 - 5040) \cos(a \sqrt{z}) - 7 (z^3 a^6 - 30 z^2 a^4 + 360 z a^2 - 720) \sin(a \sqrt{z}) \right) \right)$$

01.06.21.0105.01

$$\int z^4 \sin(a \sqrt{z}) dz = -\frac{1}{a^{10}} \left( 2 \left( a \sqrt{z} \left( z^4 a^8 - 72 z^3 a^6 + 3024 z^2 a^4 - 60480 z a^2 + 362880 \right) \cos(a \sqrt{z}) - 9 \left( z^4 a^8 - 56 z^3 a^6 + 1680 z^2 a^4 - 20160 z a^2 + 40320 \right) \sin(a \sqrt{z}) \right) \right)$$

01.06.21.0106.01

$$\int z^5 \sin(a \sqrt{z}) dz = -\frac{1}{a^{12}} \left( 2 \left( a \sqrt{z} \left( z^5 a^{10} - 110 z^4 a^8 + 7920 z^3 a^6 - 332640 z^2 a^4 + 6652800 z a^2 - 39916800 \right) \cos(a \sqrt{z}) - 11 \left( z^5 a^{10} - 90 z^4 a^8 + 5040 z^3 a^6 - 151200 z^2 a^4 + 1814400 z a^2 - 3628800 \right) \sin(a \sqrt{z}) \right) \right)$$

01.06.21.0107.01

$$\int \frac{\sin(a \sqrt{z})}{z} dz = 2 \operatorname{Si}(a \sqrt{z})$$

01.06.21.0108.01

$$\int \frac{\sin(a \sqrt{z})}{z^2} dz = -\frac{z \operatorname{Si}(a \sqrt{z}) a^2 + \sqrt{z} \cos(a \sqrt{z}) a + \sin(a \sqrt{z})}{z}$$

01.06.21.0109.01

$$\int \frac{\sin(a \sqrt{z})}{z^3} dz = \frac{z^2 \operatorname{Si}(a \sqrt{z}) a^4 + \sqrt{z} (a^2 z - 2) \cos(a \sqrt{z}) a + (a^2 z - 6) \sin(a \sqrt{z})}{12 z^2}$$

01.06.21.0110.01

$$\int \frac{\sin(a \sqrt{z})}{z^4} dz = -\frac{1}{360 z^3} \left( z^3 \operatorname{Si}(a \sqrt{z}) a^6 + \sqrt{z} (z^2 a^4 - 2 z a^2 + 24) \cos(a \sqrt{z}) a + (z^2 a^4 - 6 z a^2 + 120) \sin(a \sqrt{z}) \right)$$

01.06.21.0111.01

$$\int \frac{\sin(a \sqrt{z})}{z^5} dz = \frac{1}{20160 z^4} \left( z^4 \operatorname{Si}(a \sqrt{z}) a^8 + \sqrt{z} (z^3 a^6 - 2 z^2 a^4 + 24 z a^2 - 720) \cos(a \sqrt{z}) a + (z^3 a^6 - 6 z^2 a^4 + 120 z a^2 - 5040) \sin(a \sqrt{z}) \right)$$

### Involving $z^{\alpha-1}$ and arguments $a z^r + b$

01.06.21.0112.01

$$\int z^{\alpha-1} \sin(a z^r + b) dz = \frac{i z^\alpha}{2r} \left( e^{ib} (-i a z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -i a z^r\right) - e^{-ib} (i a z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, i a z^r\right) \right)$$

01.06.21.0113.01

$$\int \frac{\sin(a z^r + b)}{z} dz = \frac{\operatorname{Ci}(a z^r) \sin(b) + \cos(b) \operatorname{Si}(a z^r)}{r}$$

01.06.21.0114.01

$$\int z^n \sin(a z^2 + b) dz = \frac{1}{4} i z^{n+1} \left( e^{ib} (-i a z^2)^{-\frac{n+1}{2}} \Gamma\left(\frac{n+1}{2}, -i a z^2\right) - e^{-ib} (i a z^2)^{-\frac{n+1}{2}} \Gamma\left(\frac{n+1}{2}, i a z^2\right) \right); n \in \mathbb{Z}$$

01.06.21.0115.01

$$\int z^{2n} \sin(az^2 + b) dz = \frac{1}{4} iz \left( e^{ib} (-ia z^2)^{-\frac{1}{2}} (-ia)^{-n} \left( \operatorname{erfc}(\sqrt{-ia z^2}) \Gamma\left(n + \frac{1}{2}\right) + e^{ia z^2} \sum_{k=0}^{n-1} \frac{(-ia z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{ia z^2} \sum_{k=n}^{-1} \frac{(-ia z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) - e^{-ib} (ia z^2)^{-\frac{1}{2}} (ia)^{-n} \left( \operatorname{erfc}(\sqrt{ia z^2}) \Gamma\left(n + \frac{1}{2}\right) + e^{-ia z^2} \sum_{k=0}^{n-1} \frac{(ia z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{-ia z^2} \sum_{k=n}^{-1} \frac{(ia z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0116.01

$$\int z^{2n-1} \sin(az^2 + b) dz = \frac{1}{4} i \left( e^{ib} (-ia)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(ia z^2)}{(-n)!} + e^{ia z^2} \operatorname{Sum}\left(\frac{(-ia z^2)^k}{(n)_{k-n+1}}, \{k, 0, n-1\}\right) - e^{ia z^2} \operatorname{Sum}\left(\frac{(-ia z^2)^k}{(n)_{k-n+1}}, \{k, n, -1\}\right) \right) - e^{-ib} (ia)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(-ia z^2)}{(-n)!} + e^{-ia z^2} \operatorname{Sum}\left(\frac{(ia z^2)^k}{(n)_{k-n+1}}, \{k, 0, n-1\}\right) - e^{-ia z^2} \operatorname{Sum}\left(\frac{(ia z^2)^k}{(n)_{k-n+1}}, \{k, n, -1\}\right) \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0117.01

$$\int z \sin(az^2 + b) dz = -\frac{\cos(az^2 + b)}{2a}$$

01.06.21.0118.01

$$\int z^2 \sin(az^2 + b) dz = -\frac{2\sqrt{a} z \cos(az^2 + b) - \sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) + \sqrt{2\pi} S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) \sin(b)}{4a^{3/2}}$$

01.06.21.0119.01

$$\int z^3 \sin(az^2 + b) dz = \frac{\sin(az^2 + b) - az^2 \cos(az^2 + b)}{2a^2}$$

01.06.21.0120.01

$$\int z^4 \sin(az^2 + b) dz = -\frac{1}{8a^{5/2}} \left( 3\sqrt{2\pi} \cos(b) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) + 3\sqrt{2\pi} C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) \sin(b) + 2\sqrt{a} z (2az^2 \cos(az^2 + b) - 3 \sin(az^2 + b)) \right)$$

01.06.21.0121.01

$$\int z^5 \sin(az^2 + b) dz = \frac{2a \sin(az^2 + b) z^2 + (2 - a^2 z^4) \cos(az^2 + b)}{2a^3}$$

01.06.21.0122.01

$$\int \frac{\sin(az^2 + b)}{z} dz = \frac{1}{2} (\operatorname{Ci}(az^2) \sin(b) + \cos(b) \operatorname{Si}(az^2))$$

01.06.21.0123.01

$$\int \frac{\sin(az^2 + b)}{z^2} dz = \sqrt{a} \sqrt{2\pi} \cos(b) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) - \frac{\sqrt{a} \sqrt{2\pi} z S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) \sin(b) + \sin(az^2 + b)}{z}$$

01.06.21.0124.01

$$\int \frac{\sin(az^2 + b)}{z^3} dz = \frac{1}{2} \left( a \cos(b) \operatorname{Ci}(az^2) - a \sin(b) \operatorname{Si}(az^2) - \frac{\sin(az^2 + b)}{z^2} \right)$$

01.06.21.0125.01

$$\int \frac{\sin(az^2 + b)}{z^4} dz = -\frac{1}{3z^3} \left( 2\sqrt{2\pi} z^3 \cos(b) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) a^{3/2} + 2\sqrt{2\pi} z^3 C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) \sin(b) a^{3/2} + 2z^2 \cos(az^2 + b) a + \sin(az^2 + b) \right)$$

01.06.21.0126.01

$$\int \frac{\sin(az^2 + b)}{z^5} dz = -\frac{a^2 \operatorname{Ci}(az^2) \sin(b) z^4 + a^2 \cos(b) \operatorname{Si}(az^2) z^4 + a \cos(az^2 + b) z^2 + \sin(az^2 + b)}{4z^4}$$

01.06.21.0127.01

$$\int z^{\alpha-1} \sin(\sqrt{z} a + b) dz = i z^\alpha \left( e^{ib} (-ia\sqrt{z})^{-2\alpha} \Gamma(2\alpha, -ia\sqrt{z}) - e^{-ib} (ia\sqrt{z})^{-2\alpha} \Gamma(2\alpha, ia\sqrt{z}) \right)$$

01.06.21.0128.01

$$\int z^n \sin(\sqrt{z} a + b) dz = i z^{n+1} \left( e^{ib} (-ia\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), -ia\sqrt{z}) - e^{-ib} (ia\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), ia\sqrt{z}) \right); n \in \mathbf{Z}$$

01.06.21.0129.01

$$\int z^n \sin(\sqrt{z} a + b) dz = (-1)^{n-1} i a^{-2(n+1)} \left( e^{ib} \left( -\frac{\operatorname{Ei}(ia\sqrt{z})}{(-2(n+1))!} + e^{ia\sqrt{z}} \sum_{k=0}^{2(n+1)-1} \frac{(-ia\sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} - e^{ia\sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{(-ia\sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} \right) - e^{-ib} \left( -\frac{\operatorname{Ei}(-ia\sqrt{z})}{(-2(n+1))!} + e^{-ia\sqrt{z}} \sum_{k=0}^{2(n+1)-1} \frac{(ia\sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} - e^{-ia\sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{(ia\sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} \right) \right); n \in \mathbf{Z}$$

01.06.21.0130.01

$$\int z \sin(\sqrt{z} a + b) dz = \frac{6(a^2 z - 2) \sin(\sqrt{z} a + b) - 2a\sqrt{z} (a^2 z - 6) \cos(\sqrt{z} a + b)}{a^4}$$

01.06.21.0131.01

$$\int z^2 \sin(\sqrt{z} a + b) dz = \frac{1}{a^6} \left( 10(z(a^2 z - 12)a^2 + 24) \sin(\sqrt{z} a + b) - 2a\sqrt{z} (z(a^2 z - 20)a^2 + 120) \cos(\sqrt{z} a + b) \right)$$

01.06.21.0132.01

$$\int z^3 \sin(\sqrt{z} a + b) dz = \frac{1}{a^8} \left( 14(a^2 z (z(a^2 z - 30)a^2 + 360) - 720) \sin(\sqrt{z} a + b) - 2a\sqrt{z} (a^2 z (z(a^2 z - 42)a^2 + 840) - 5040) \cos(\sqrt{z} a + b) \right)$$



01.06.21.0133.01

$$\int z^4 \sin(\sqrt{z} a + b) dz = \frac{1}{a^{10}} \left( 18 (z (a^2 z (z (a^2 z - 56) a^2 + 1680) - 20 160) a^2 + 40 320) \sin(\sqrt{z} a + b) - \right. \\ \left. 2 a \sqrt{z} (z (a^2 z (z (a^2 z - 72) a^2 + 3024) - 60 480) a^2 + 362 880) \cos(\sqrt{z} a + b) \right)$$

01.06.21.0134.01

$$\int z^5 \sin(\sqrt{z} a + b) dz = \\ - \frac{1}{a^{12}} \left( 2 (a \sqrt{z} (z^5 a^{10} - 110 z^4 a^8 + 7920 z^3 a^6 - 332 640 z^2 a^4 + 6 652 800 z a^2 - 39 916 800) \cos(\sqrt{z} a + b) - \right. \\ \left. 11 (z^5 a^{10} - 90 z^4 a^8 + 5040 z^3 a^6 - 151 200 z^2 a^4 + 1 814 400 z a^2 - 3 628 800) \sin(\sqrt{z} a + b) \right)$$

01.06.21.0135.01

$$\int \frac{\sin(\sqrt{z} a + b)}{z} dz = 2 \left( \text{Ci}(a \sqrt{z}) \sin(b) + \cos(b) \text{Si}(a \sqrt{z}) \right)$$

01.06.21.0136.01

$$\int \frac{\sin(\sqrt{z} a + b)}{z^2} dz = - \frac{z \left( \text{Ci}(a \sqrt{z}) \sin(b) + \cos(b) \text{Si}(a \sqrt{z}) \right) a^2 + \sqrt{z} \cos(\sqrt{z} a + b) a + \sin(\sqrt{z} a + b)}{z}$$

01.06.21.0137.01

$$\int \frac{\sin(\sqrt{z} a + b)}{z^3} dz = \\ \frac{1}{12 z^2} \left( z^2 \text{Ci}(a \sqrt{z}) \sin(b) a^4 + z^2 \cos(b) \text{Si}(a \sqrt{z}) a^4 + \sqrt{z} (a^2 z - 2) \cos(\sqrt{z} a + b) a + (a^2 z - 6) \sin(\sqrt{z} a + b) \right)$$

01.06.21.0138.01

$$\int \frac{\sin(\sqrt{z} a + b)}{z^4} dz = - \frac{1}{360 z^3} \left( z^3 \text{Ci}(a \sqrt{z}) \sin(b) a^6 + z^3 \cos(b) \text{Si}(a \sqrt{z}) a^6 + \right. \\ \left. \sqrt{z} (z (a^2 z - 2) a^2 + 24) \cos(\sqrt{z} a + b) a + (z (a^2 z - 6) a^2 + 120) \sin(\sqrt{z} a + b) \right)$$

01.06.21.0139.01

$$\int \frac{\sin(\sqrt{z} a + b)}{z^5} dz = \frac{1}{20 160 z^4} \\ \left( 24 a^3 \cos(\sqrt{z} a + b) z^{3/2} - 2 a^5 \cos(\sqrt{z} a + b) z^{5/2} + a^7 \cos(\sqrt{z} a + b) z^{7/2} + a^8 \text{Ci}(a \sqrt{z}) \sin(b) z^4 + a^8 \cos(b) \text{Si}(a \sqrt{z}) z^4 + \right. \\ \left. a^6 \sin(\sqrt{z} a + b) z^3 - 6 a^4 \sin(\sqrt{z} a + b) z^2 + 120 a^2 \sin(\sqrt{z} a + b) z - 720 a \cos(\sqrt{z} a + b) \sqrt{z} - 5040 \sin(\sqrt{z} a + b) \right)$$

## Involving rational functions

### Involving $(a z + b)^{-n}$

01.06.21.0140.01

$$\int \frac{\sin(c z)}{b + a z} dz = \frac{1}{a} \left( \cos\left(\frac{b c}{a}\right) \text{Si}\left(c \left(\frac{b}{a} + z\right)\right) - \text{Ci}\left(c \left(\frac{b}{a} + z\right)\right) \sin\left(\frac{b c}{a}\right) \right)$$

01.06.21.0141.01

$$\int \frac{\sin(cz)}{(b+az)^2} dz = \frac{1}{a^2} \left( c \cos\left(\frac{bc}{a}\right) \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) + c \sin\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) - \frac{a \sin(cz)}{b+az} \right)$$

01.06.21.0142.01

$$\int \frac{\sin(cz)}{(b+az)^3} dz = -\frac{1}{2a^3} \left( \cos\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) c^2 - c^2 \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \sin\left(\frac{bc}{a}\right) + \frac{a(c(b+az)\cos(cz) + a \sin(cz))}{(b+az)^2} \right)$$

01.06.21.0143.01

$$\int \frac{\sin(cz)}{(b+az)^4} dz = -\frac{1}{6a^4} \left( \left( \cos\left(\frac{bc}{a}\right) \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) + \sin\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) \right) c^3 + \frac{a^2 \cos(cz)c}{(b+az)^2} - \frac{a((c^2 z^2 - 2)a^2 + 2bc^2 za + b^2 c^2) \sin(cz)}{(b+az)^3} \right)$$

01.06.21.0144.01

$$\int \frac{\sin(cz)}{(b+az)^5} dz = \frac{1}{24a^5} \left( -\left( \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \sin\left(\frac{bc}{a}\right) - \cos\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) \right) c^4 + \frac{a((c^2 z^2 - 2)a^2 + 2bc^2 za + b^2 c^2) \cos(cz)c}{(b+az)^3} + \frac{a^2((c^2 z^2 - 6)a^2 + 2bc^2 za + b^2 c^2) \sin(cz)}{(b+az)^4} \right)$$

01.06.21.0145.01

$$\int \frac{\sin(cz)}{(b+az)^6} dz = \frac{1}{120a^6} \left( \left( \cos\left(\frac{bc}{a}\right) \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) + \sin\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) \right) c^5 + \frac{a^2((c^2 z^2 - 6)a^2 + 2bc^2 za + b^2 c^2) \cos(cz)c}{(b+az)^4} - \frac{1}{(b+az)^5} \left( a((c^4 z^4 - 2c^2 z^2 + 24)a^4 + 4bc^2 z(c^2 z^2 - 1)a^3 + 2b^2 c^2(3c^2 z^2 - 1)a^2 + 4b^3 c^4 za + b^4 c^4) \sin(cz) \right) \right)$$

01.06.21.0146.01

$$\int \frac{z \sin(cz)}{b+az} dz = -\frac{a \cos(cz) - bc \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \sin\left(\frac{bc}{a}\right) + bc \cos\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right)}{a^2 c}$$

01.06.21.0147.01

$$\int \frac{z^2 \sin(cz)}{b+az} dz = \frac{1}{a^3 c^2} \left( -b^2 \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \sin\left(\frac{bc}{a}\right) c^2 + b^2 \cos\left(\frac{bc}{a}\right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) c^2 + a(c(b-az)\cos(cz) + a \sin(cz)) \right)$$

01.06.21.0148.01

$$\int \frac{z \sin(cz)}{(b+az)^2} dz = \frac{1}{a^3 (b+az)} \left( -(b+az) \text{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \left( bc \cos\left(\frac{bc}{a}\right) + a \sin\left(\frac{bc}{a}\right) \right) + ab \sin(cz) + (b+az) \left( a \cos\left(\frac{bc}{a}\right) - bc \sin\left(\frac{bc}{a}\right) \right) \text{Si}\left(c\left(\frac{b}{a}+z\right)\right) \right)$$

01.06.21.0149.01

$$\int \frac{z^2 \sin(cz)}{(b+az)^2} dz = \frac{1}{a^4 c (b+az)} \left( bc(b+az) \operatorname{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \left( bc \cos\left(\frac{bc}{a}\right) + 2a \sin\left(\frac{bc}{a}\right) \right) - \right. \\ \left. a(c \sin(cz) b^2 + a(b+az) \cos(cz)) + bc(b+az) \left( bc \sin\left(\frac{bc}{a}\right) - 2a \cos\left(\frac{bc}{a}\right) \right) \operatorname{Si}\left(c\left(\frac{b}{a}+z\right)\right) \right)$$

01.06.21.0150.01

$$\int \frac{z^3 \sin(cz)}{(b+az)^2} dz = \frac{1}{a^5} \left( -\frac{(az-2b) \cos(cz) a^2}{c} + \frac{(z a^3 + b a^2 + b^3 c^2) \sin(cz) a}{c^2 (b+az)} - \right. \\ \left. b^2 \left( \operatorname{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \left( bc \cos\left(\frac{bc}{a}\right) + 3a \sin\left(\frac{bc}{a}\right) \right) + \left( bc \sin\left(\frac{bc}{a}\right) - 3a \cos\left(\frac{bc}{a}\right) \right) \operatorname{Si}\left(c\left(\frac{b}{a}+z\right)\right) \right) \right)$$

01.06.21.0151.01

$$\int \frac{z^4 \sin(cz)}{(b+az)^2} dz = \frac{1}{a^6 c^3 (b+az)} \\ \left( b^3 (b+az) \operatorname{Ci}\left(c\left(\frac{b}{a}+z\right)\right) \left( bc \cos\left(\frac{bc}{a}\right) + 4a \sin\left(\frac{bc}{a}\right) \right) c^3 + b^3 (b+az) \left( bc \sin\left(\frac{bc}{a}\right) - 4a \cos\left(\frac{bc}{a}\right) \right) \operatorname{Si}\left(c\left(\frac{b}{a}+z\right)\right) c^3 - \right. \\ \left. a(a(b+az))((c^2 z^2 - 2) a^2 - 2bc^2 z a + 3b^2 c^2) \cos(cz) + c(-2z^2 a^4 + 2b^2 a^2 + b^4 c^2) \sin(cz) \right)$$

### Involving $(az^2 + b)^{-n}$

01.06.21.0152.01

$$\int \frac{\sin(cz)}{az^2 + b} dz = \frac{1}{2\sqrt{a}\sqrt{b}} \left( \operatorname{Ci}\left(c\left(\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) \sinh\left(\frac{\sqrt{b}c}{\sqrt{a}}\right) + \right. \\ \left. \operatorname{Ci}\left(c\left(-\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) \sinh\left(\frac{\sqrt{b}c}{\sqrt{a}}\right) + i \cosh\left(\frac{\sqrt{b}c}{\sqrt{a}}\right) \left( \operatorname{Si}\left(c\left(\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) + \operatorname{Si}\left(\frac{i\sqrt{b}c}{\sqrt{a}} - cz\right) \right) \right)$$

01.06.21.0153.01

$$\int \frac{\sin(z)}{z^2 - 1} dz = \frac{1}{2} (\sin(1) \operatorname{Ci}(1-z) - \cos(1) (\operatorname{Si}(1-z) + \operatorname{Si}(z+1)) + \operatorname{Ci}(z+1) \sin(1))$$

01.06.21.0154.01

$$\int \frac{z \sin(cz)}{az^2 + b} dz = \frac{1}{2a} \left( -i \operatorname{Ci}\left(c\left(\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) \sinh\left(\frac{\sqrt{b}c}{\sqrt{a}}\right) + \right. \\ \left. i \operatorname{Ci}\left(c\left(-\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) \sinh\left(\frac{\sqrt{b}c}{\sqrt{a}}\right) + \cosh\left(\frac{\sqrt{b}c}{\sqrt{a}}\right) \left( \operatorname{Si}\left(c\left(\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) + \operatorname{Si}\left(c\left(-\frac{i\sqrt{b}}{\sqrt{a}}+z\right)\right) \right) \right)$$

01.06.21.0155.01

$$\int \frac{\sin(cz)}{(az^2+b)^2} dz = \frac{1}{4ab^{3/2}(az^2+b)} \left( -(az^2+b) \operatorname{Ci} \left( c \left( \frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) \left( \sqrt{b} c \cosh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) - \sqrt{a} \sinh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \right) - \right. \\ \left. (az^2+b) \operatorname{Ci} \left( c \left( -\frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) \left( \sqrt{b} c \cosh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) - \sqrt{a} \sinh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \right) - \right. \\ \left. i \left( (az^2+b) \left( \sqrt{b} c \sinh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) - \sqrt{a} \cosh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \right) \operatorname{Si} \left( c \left( \frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) + \sqrt{a} (az^2+b) \cosh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \right. \right. \\ \left. \left. \operatorname{Si} \left( c \left( -\frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) + \sqrt{b} \left( 2aiz \sin(cz) + c(az^2+b) \sinh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \operatorname{Si} \left( \frac{i\sqrt{b} c}{\sqrt{a}} - cz \right) \right) \right) \right)$$

01.06.21.0156.01

$$\int \frac{z \sin(cz)}{(az^2+b)^2} dz = \frac{1}{4a^{3/2}} \left( -\frac{2\sqrt{a} \sin(cz)}{az^2+b} + \frac{c \left( i \cosh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \operatorname{Ci} \left( c \left( \frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) - \sinh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \operatorname{Si} \left( c \left( \frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) \right)}{\sqrt{b}} + \right. \\ \left. \frac{c \left( \sinh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \operatorname{Si} \left( \frac{i\sqrt{b} c}{\sqrt{a}} - cz \right) - i \cosh \left( \frac{\sqrt{b} c}{\sqrt{a}} \right) \operatorname{Ci} \left( c \left( -\frac{i\sqrt{b}}{\sqrt{a}} + z \right) \right) \right)}{\sqrt{b}} \right)$$

Involving  $(az^2 + bz + c)^{-n}$

01.06.21.0157.01

$$\int \frac{\sin(dz)}{az^2+bz+c} dz = \frac{1}{\sqrt{b^2-4ac}} \left( -\operatorname{Ci} \left( \frac{d(b+2az-\sqrt{b^2-4ac})}{2a} \right) \sin \left( \frac{(b-\sqrt{b^2-4ac})d}{2a} \right) + \operatorname{Ci} \left( \frac{d(b+2az+\sqrt{b^2-4ac})}{2a} \right) \right. \\ \left. \sin \left( \frac{(b+\sqrt{b^2-4ac})d}{2a} \right) + \cos \left( \frac{(b-\sqrt{b^2-4ac})d}{2a} \right) \operatorname{Si} \left( \frac{d(b+2az-\sqrt{b^2-4ac})}{2a} \right) - \right. \\ \left. \cos \left( \frac{(b+\sqrt{b^2-4ac})d}{2a} \right) \operatorname{Si} \left( \frac{d(b+2az+\sqrt{b^2-4ac})}{2a} \right) \right)$$

01.06.21.0158.01

$$\int \frac{z \sin(dz)}{az^2 + bz + c} dz = \frac{1}{2a\sqrt{b^2 - 4ac}}$$

$$\left( -\left(\sqrt{b^2 - 4ac} - b\right) \left( \text{Ci} \left( \frac{d(b + 2az - \sqrt{b^2 - 4ac})}{2a} \right) \sin \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) - \cos \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) \right. \right.$$

$$\left. \text{Si} \left( \frac{d(b + 2az - \sqrt{b^2 - 4ac})}{2a} \right) - (b + \sqrt{b^2 - 4ac}) \left( \text{Ci} \left( \frac{d(b + 2az + \sqrt{b^2 - 4ac})}{2a} \right) \right. \right.$$

$$\left. \left. \sin \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) - \cos \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) \text{Si} \left( \frac{d(b + 2az + \sqrt{b^2 - 4ac})}{2a} \right) \right) \right)$$

01.06.21.0159.01

$$\int \frac{\sin(dz)}{(az^2 + bz + c)^2} dz = \frac{1}{(c + z(b + az)) \sqrt{b^2 - 4ac}}$$

$$\left( \left( \text{Ci} \left( \frac{d(b + 2az - \sqrt{b^2 - 4ac})}{2a} \right) \left( \sqrt{b^2 - 4ac} d \cos \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) + 2a \sin \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) \right) \right. \right.$$

$$\left. \left. \text{Ci} \left( \frac{d(b + 2az + \sqrt{b^2 - 4ac})}{2a} \right) \left( \sqrt{b^2 - 4ac} d \cos \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) - 2a \sin \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) \right) \right) \right)$$

$$\left. \left. \sqrt{b^2 - 4ac} (b + 2az) \sin(dz) \right) / \left( (b^2 - 4ac)^{3/2} (c + z(b + az)) \right) + \frac{1}{(b^2 - 4ac)^{3/2}} \right.$$

$$\left( \left( \sqrt{b^2 - 4ac} d \sin \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) - 2a \cos \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) \right) \text{Si} \left( \frac{d(b + 2az - \sqrt{b^2 - 4ac})}{2a} \right) \right. \right.$$

$$\left. \left. \left( 2a \cos \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) + \sqrt{b^2 - 4ac} d \sin \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) \right) \text{Si} \left( \frac{d(b + 2az + \sqrt{b^2 - 4ac})}{2a} \right) \right) \right)$$

01.06.21.0160.01

$$\int \frac{z \sin(dz)}{(az^2 + bz + c)^2} dz =$$

$$\frac{1}{2a(b^2 - 4ac)^{3/2}} \left( \left( -b^2 + \sqrt{b^2 - 4ac} \right) d \cos \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) - 2ab \sin \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) \right)$$

$$\operatorname{Ci} \left( \frac{d(b + 2az - \sqrt{b^2 - 4ac})}{2a} \right) +$$

$$\frac{1}{2a(b^2 - 4ac)^{3/2}} \left( \left( 2ab \sin \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) - (b^2 + \sqrt{b^2 - 4ac} - b - 4ac) d \cos \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) \right) \right)$$

$$\operatorname{Ci} \left( \frac{d(b + 2az + \sqrt{b^2 - 4ac})}{2a} \right) + \frac{(2c + bz) \sin(dz)}{(b^2 - 4ac)(c + z(b + az))} +$$

$$\frac{1}{2a(b^2 - 4ac)^{3/2}} \left( \left( 2ab \cos \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) + (b^2 - \sqrt{b^2 - 4ac} - b - 4ac) d \sin \left( \frac{(b - \sqrt{b^2 - 4ac})d}{2a} \right) \right) \right)$$

$$\operatorname{Si} \left( \frac{d(b + 2az - \sqrt{b^2 - 4ac})}{2a} \right) +$$

$$\frac{1}{2a(b^2 - 4ac)^{3/2}} \left( \left( -2ab \cos \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) - (b^2 + \sqrt{b^2 - 4ac} - b - 4ac) d \sin \left( \frac{(b + \sqrt{b^2 - 4ac})d}{2a} \right) \right) \right)$$

$$\operatorname{Si} \left( \frac{d(b + 2az + \sqrt{b^2 - 4ac})}{2a} \right)$$

### Involving algebraic functions

Involving  $(az + b)^\beta$

01.06.21.0161.01

$$\int (b+az)^\beta \sin(d+cz) dz = -\frac{1}{2c} \left( (b+az)^\beta \left( \frac{c^2(b+az)^2}{a^2} \right)^{-\beta} \left( \Gamma\left(\beta+1, -\frac{ic(b+az)}{a}\right) \left( \cos\left(\frac{bc}{a}-d\right) - i \sin\left(\frac{bc}{a}-d\right) \right) \left( \frac{ic(b+az)}{a} \right)^\beta + \left( -\frac{ic(b+az)}{a} \right)^\beta \Gamma\left(\beta+1, \frac{ic(b+az)}{a}\right) \left( \cos\left(\frac{bc}{a}-d\right) + i \sin\left(\frac{bc}{a}-d\right) \right) \right) \right)$$

01.06.21.0162.01

$$\int (b+az)^\beta \sin(cz) dz = -\frac{1}{2c} \left( (b+az)^\beta \left( \frac{c^2(b+az)^2}{a^2} \right)^{-\beta} \left( \Gamma\left(\beta+1, -\frac{ic(b+az)}{a}\right) \left( \cos\left(\frac{bc}{a}\right) - i \sin\left(\frac{bc}{a}\right) \right) \left( \frac{ic(b+az)}{a} \right)^\beta + \left( -\frac{ic(b+az)}{a} \right)^\beta \Gamma\left(\beta+1, \frac{ic(b+az)}{a}\right) \left( \cos\left(\frac{bc}{a}\right) + i \sin\left(\frac{bc}{a}\right) \right) \right) \right)$$

01.06.21.0163.01

$$\int (b+az)^{3/2} \sin(cz) dz = \frac{1}{4a^2 \left(\frac{c}{a}\right)^{5/2}} \left( -3a\sqrt{2\pi} \cos\left(\frac{bc}{a}\right) S\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) + 3a\sqrt{2\pi} C\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) \sin\left(\frac{bc}{a}\right) - 2\sqrt{\frac{c}{a}} \sqrt{b+az} (2c(b+az)\cos(cz) - 3a\sin(cz)) \right)$$

01.06.21.0164.01

$$\int \sqrt{az+b} \sin(cz) dz = \frac{1}{2c\sqrt{\frac{c}{a}}} \left( -2\sqrt{\frac{c}{a}} \sqrt{b+az} \cos(cz) + \sqrt{2\pi} \cos\left(\frac{bc}{a}\right) C\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) + \sqrt{2\pi} S\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) \sin\left(\frac{bc}{a}\right) \right)$$

01.06.21.0165.01

$$\int \frac{\sin(cz)}{\sqrt{az+b}} dz = \frac{1}{c\sqrt{\frac{c}{a}}} \sqrt{2\pi} \left( \cos\left(\frac{bc}{a}\right) S\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) - C\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) \sin\left(\frac{bc}{a}\right) \right)$$

01.06.21.0166.01

$$\int \frac{\sin(cz)}{(b+az)^{3/2}} dz = \frac{2}{a} \left( \sqrt{\frac{c}{a}} \sqrt{2\pi} \cos\left(\frac{bc}{a}\right) C\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) + \sqrt{\frac{c}{a}} \sqrt{2\pi} S\left(\sqrt{\frac{c}{a}} \sqrt{\frac{2}{\pi}} \sqrt{b+az}\right) \sin\left(\frac{bc}{a}\right) - \frac{\sin(cz)}{\sqrt{b+az}} \right)$$

**Involving exponential function**

## Involving exp

Involving  $a^{bz} \sin(cz)$ 

01.06.21.0167.01

$$\int a^{bz} \sin(cz) dz = \frac{a^{bz} (b \log(a) \sin(cz) - c \cos(cz))}{c^2 + b^2 \log^2(a)}$$

01.06.21.0168.01

$$\int e^{bz} \sin(cz) dz = \frac{e^{bz} (b \sin(cz) - c \cos(cz))}{b^2 + c^2}$$

01.06.21.0169.01

$$\int e^{iaz} \sin(az) dz = -\frac{e^{2iaz} - 2iaz}{4a}$$

01.06.21.0170.01

$$\int e^{-iaz} \sin(az) dz = -\frac{2iaz + e^{-2iaz}}{4a}$$

01.06.21.0171.01

$$\int e^{-az} \sin(az) dz = -\frac{e^{-az} (\cos(az) + \sin(az))}{2a}$$

Involving  $a^{bz+e} \sin(cz)$ 

01.06.21.0172.01

$$\int a^{bz+e} \sin(cz) dz = \frac{a^{bz+e} (b \log(a) \sin(cz) - c \cos(cz))}{c^2 + b^2 \log^2(a)}$$

01.06.21.0173.01

$$\int e^{e+bz} \sin(cz) dz = \frac{e^{e+bz} (b \sin(cz) - c \cos(cz))}{b^2 + c^2}$$

01.06.21.0174.01

$$\int e^{e-iaz} \sin(az) dz = -\frac{2ae^e iz + e^{e-2iaz}}{4a}$$

01.06.21.0175.01

$$\int e^{e+iaz} \sin(az) dz = \frac{e^e (2iaz - e^{2iaz})}{4a}$$

Involving  $a^{bz} \sin(cz + d)$ 

01.06.21.0176.01

$$\int a^{bz} \sin(d + cz) dz = \frac{a^{bz} (b \log(a) \sin(d + cz) - c \cos(d + cz))}{c^2 + b^2 \log^2(a)}$$



01.06.21.01777.01

$$\int e^{bz} \sin(d + cz) dz = \frac{e^{bz} (b \sin(d + cz) - c \cos(d + cz))}{b^2 + c^2}$$

01.06.21.0178.01

$$\int e^{-iaz} \sin(d + az) dz = -\frac{2a e^{id} iz + e^{-id-2iaz}}{4a}$$

01.06.21.0179.01

$$\int e^{iaz} \sin(d + az) dz = \frac{e^{-id} (2iaz - e^{2i(d+az)})}{4a}$$

### Involving $a^{bz+e} \sin(cz + d)$

01.06.21.0180.01

$$\int a^{bz+e} \sin(d + cz) dz = \frac{a^{bz+e} (b \log(a) \sin(d + cz) - c \cos(d + cz))}{c^2 + b^2 \log^2(a)}$$

01.06.21.0181.01

$$\int e^{e+bz} \sin(d + cz) dz = \frac{e^{e+bz} (b \sin(d + cz) - c \cos(d + cz))}{b^2 + c^2}$$

01.06.21.0182.01

$$\int e^{-iaz} \sin(d + az) dz = -\frac{2a e^{e+id} iz + e^{e-id-2iaz}}{4a}$$

01.06.21.0183.01

$$\int e^{e+iaz} \sin(d + az) dz = \frac{e^{e-id} (2iaz - e^{2i(d+az)})}{4a}$$

### Involving $a^{bz^f} \sin(cz)$

01.06.21.0184.01

$$\int a^{bz^2} \sin(cz) dz = \frac{i\sqrt{\pi}}{4\sqrt{b} \log^{\frac{1}{2}}(a)} e^{\frac{c^2}{4b \log(a)}} \left( \operatorname{erfi} \left( \frac{-ic + 2bz \log(a)}{2\sqrt{b} \log^{\frac{1}{2}}(a)} \right) - \operatorname{erfi} \left( \frac{ic + 2bz \log(a)}{2\sqrt{b} \log^{\frac{1}{2}}(a)} \right) \right)$$

01.06.21.0185.01

$$\int e^{bz^2} \sin(cz) dz = \frac{\sqrt{\pi}}{4\sqrt{b}} e^{\frac{c^2}{4b}} \left( \operatorname{erf} \left( \frac{c + 2ibz}{2\sqrt{b}} \right) + \operatorname{erf} \left( \frac{c - 2ibz}{2\sqrt{b}} \right) \right)$$

01.06.21.0186.01

$$\int e^{z^2} \sin(z) dz = \frac{1}{4} \sqrt[4]{e} \sqrt{\pi} \left( \operatorname{erf} \left( \frac{1}{2} - iz \right) + \operatorname{erf} \left( iz + \frac{1}{2} \right) \right)$$

01.06.21.0187.01

$$\int a^{b\sqrt{z}} \sin(cz) dz = \frac{ib\sqrt{\pi}}{4(ic)^{3/2}} e^{\frac{ib^2 \log^2(a)}{4c}} \log(a) \left( e^{-\frac{ib^2 \log^2(a)}{2c}} \operatorname{erf} \left( \frac{2ic\sqrt{z} - b \log(a)}{2\sqrt{ic}} \right) + \operatorname{erfi} \left( \frac{2ic\sqrt{z} + b \log(a)}{2\sqrt{ic}} \right) \right) - \frac{a^{b\sqrt{z}} \cos(cz)}{c}$$

01.06.21.0188.01

$$\int e^{b\sqrt{z}} \sin(cz) dz = \frac{ib\sqrt{\pi}}{4(ic)^{3/2}} e^{\frac{ib^2}{4c}} \left( e^{-\frac{ib^2}{2c}} \operatorname{erf}\left(\frac{2ic\sqrt{z}-b}{2\sqrt{ic}}\right) + \operatorname{erfi}\left(\frac{b+2ic\sqrt{z}}{2\sqrt{ic}}\right) \right) - \frac{e^{b\sqrt{z}} \cos(cz)}{c}$$

### Involving $a^{bz^f+e} \sin(cz)$

01.06.21.0189.01

$$\int a^{bz^2+e} \sin(cz) dz = \frac{i\sqrt{\pi}}{4\sqrt{b} \log^{\frac{1}{2}}(a)} a^e e^{\frac{c^2}{4b \log(a)}} \left( \operatorname{erfi}\left(\frac{-ic+2bz \log(a)}{2\sqrt{b} \log^{\frac{1}{2}}(a)}\right) - \operatorname{erfi}\left(\frac{ic+2bz \log(a)}{2\sqrt{b} \log^{\frac{1}{2}}(a)}\right) \right)$$

01.06.21.0190.01

$$\int e^{bz^2+e} \sin(cz) dz = \frac{\sqrt{\pi}}{4\sqrt{b}} e^{\frac{c^2}{4b+e}} \left( \operatorname{erf}\left(\frac{c+2ibz}{2\sqrt{b}}\right) + \operatorname{erf}\left(\frac{c-2ibz}{2\sqrt{b}}\right) \right)$$

01.06.21.0191.01

$$\int a^{b\sqrt{z}+e} \sin(cz) dz = \frac{ib\sqrt{\pi}}{4(ic)^{3/2}} a^e e^{\frac{ib^2 \log^2(a)}{4c}} \log(a) \left( e^{-\frac{ib^2 \log^2(a)}{2c}} \operatorname{erf}\left(\frac{2ic\sqrt{z}-b \log(a)}{2\sqrt{ic}}\right) + \operatorname{erfi}\left(\frac{2ic\sqrt{z}+b \log(a)}{2\sqrt{ic}}\right) \right) - \frac{a^{b\sqrt{z}+e} \cos(cz)}{c}$$

01.06.21.0192.01

$$\int e^{b\sqrt{z}+e} \sin(cz) dz = \frac{ib\sqrt{\pi}}{4(ic)^{3/2}} e^{\frac{ib^2}{4c}+e} \left( e^{-\frac{ib^2}{2c}} \operatorname{erf}\left(\frac{2ic\sqrt{z}-b}{2\sqrt{ic}}\right) + \operatorname{erfi}\left(\frac{b+2ic\sqrt{z}}{2\sqrt{ic}}\right) \right) - \frac{e^{b\sqrt{z}+e} \cos(cz)}{c}$$

### Involving $a^{bz^f+dz} \sin(cz)$

01.06.21.0193.01

$$\int a^{bz^2+dz} \sin(cz) dz = \frac{i\sqrt{\pi}}{4\sqrt{b} \log^{\frac{1}{2}}(a)} a^{-\frac{d^2}{4b}} e^{\frac{c(-2id \log(a))}{4b \log(a)}} \left( e^{\frac{icd}{b}} \operatorname{erfi}\left(\frac{-ic+(d+2bz) \log(a)}{2\sqrt{b} \log^{\frac{1}{2}}(a)}\right) - \operatorname{erfi}\left(\frac{ic+(d+2bz) \log(a)}{2\sqrt{b} \log^{\frac{1}{2}}(a)}\right) \right)$$

01.06.21.0194.01

$$\int e^{bz^2+dz} \sin(cz) dz = \frac{i\sqrt{\pi}}{4\sqrt{b}} e^{\frac{(c-id)^2}{4b}} \left( e^{\frac{icd}{b}} \operatorname{erfi}\left(\frac{d-ic+2bz}{2\sqrt{b}}\right) - \operatorname{erfi}\left(\frac{d+ic+2bz}{2\sqrt{b}}\right) \right)$$

01.06.21.0195.01

$$\int a^{\sqrt{z} b+dz} \sin(cz) dz = -\frac{1}{2} \left( \frac{e^{-icz} a^{\sqrt{z} b+dz}}{c+di \log(a)} + \frac{e^{icz} a^{\sqrt{z} b+dz}}{c-id \log(a)} + b\sqrt{\pi} \log(a) \left( \frac{i e^{\frac{b^2 \log^2(a)}{4(-ic-d \log(a))}} \operatorname{erf}\left(\frac{-2ic\sqrt{z}-b \log(a)-2d\sqrt{z} \log(a)}{2\sqrt{-ic-d \log(a)}}\right)}{2(-ic-d \log(a))^{3/2}} - \frac{i e^{\frac{b^2 \log^2(a)}{4(ic-d \log(a))}} \operatorname{erf}\left(\frac{2ic\sqrt{z}-b \log(a)-2d\sqrt{z} \log(a)}{2\sqrt{ic-d \log(a)}}\right)}{2(ic-d \log(a))^{3/2}} \right) \right)$$

01.06.21.0196.01

$$\int e^{\sqrt{z} b+dz} \sin(cz) dz = \frac{1}{2} \left( -b \sqrt{\pi} \left( \frac{i e^{\frac{b^2}{4(-d-i)c}} \operatorname{erf}\left(\frac{-b-2ic\sqrt{z}-2d\sqrt{z}}{2\sqrt{-d-ic}}\right)}{2(-d-ic)^{3/2}} - \frac{i e^{\frac{b^2}{4(ic-d)}} \operatorname{erf}\left(\frac{-b-2d\sqrt{z}+2ic\sqrt{z}}{2\sqrt{ic-d}}\right)}{2(ic-d)^{3/2}} \right) - \frac{e^{\sqrt{z} b-icz+dz}}{c+id} - \frac{e^{\sqrt{z} b+dz+icz}}{c-id} \right)$$

### Involving $a^{bz^r+dz+e} \sin(cz)$

01.06.21.0197.01

$$\int a^{bz^2+dz+e} \sin(cz) dz = \frac{i \sqrt{\pi}}{4 \sqrt{b} \log^{\frac{1}{2}}(a)} a^{\frac{d^2}{4b}} e^{\frac{c(c-2id \log(a))}{4b \log(a)}} \left( e^{\frac{icd}{b}} \operatorname{erfi}\left(\frac{-ic+(d+2bz) \log(a)}{2 \sqrt{b} \log^{\frac{1}{2}}(a)}\right) + \operatorname{erfi}\left(\frac{-ic-(d+2bz) \log(a)}{2 \sqrt{b} \log^{\frac{1}{2}}(a)}\right) \right)$$

01.06.21.0198.01

$$\int e^{bz^2+dz+e} \sin(cz) dz = \frac{i \sqrt{\pi}}{4 \sqrt{b}} e^{\frac{(c-id)^2}{4b}+e} \left( e^{\frac{icd}{b}} \operatorname{erfi}\left(\frac{d-ic+2bz}{2 \sqrt{b}}\right) - \operatorname{erfi}\left(\frac{d+ic+2bz}{2 \sqrt{b}}\right) \right)$$

01.06.21.0199.01

$$\int a^{\sqrt{z} b+e+dz} \sin(cz) dz = -\frac{1}{2} a^e \left( \frac{e^{-icz} a^{\sqrt{z} b+dz}}{c+di \log(a)} + \frac{e^{icz} a^{\sqrt{z} b+dz}}{c-id \log(a)} + b i \sqrt{\pi} \log(a) \left( \frac{e^{\frac{b^2 \log^2(a)}{4(-ic-d \log(a))}} \operatorname{erf}\left(\frac{-2ic\sqrt{z}-b \log(a)-2d\sqrt{z} \log(a)}{2\sqrt{-ic-d \log(a)}}\right)}{2(-ic-d \log(a))^{3/2}} - \frac{e^{\frac{b^2 \log^2(a)}{4(ic-d \log(a))}} \operatorname{erf}\left(\frac{2ic\sqrt{z}-b \log(a)-2d\sqrt{z} \log(a)}{2\sqrt{ic-d \log(a)}}\right)}{2(ic-d \log(a))^{3/2}} \right) \right)$$

01.06.21.0200.01

$$\int e^{\sqrt{z} b+e+dz} \sin(cz) dz = -\frac{1}{2} e^e \left( \frac{e^{\sqrt{z} b-icz+dz}}{c+id} + \frac{e^{\sqrt{z} b+dz+icz}}{c-id} + i b \sqrt{\pi} \left( \frac{e^{\frac{b^2}{4(-d-ic)}} \operatorname{erf}\left(\frac{-b-2ic\sqrt{z}-2d\sqrt{z}}{2\sqrt{-d-ic}}\right)}{2(-d-ic)^{3/2}} - \frac{e^{\frac{b^2}{4(ic-d)}} \operatorname{erf}\left(\frac{-b-2d\sqrt{z}+2ic\sqrt{z}}{2\sqrt{ic-d}}\right)}{2(ic-d)^{3/2}} \right) \right)$$

### Involving $a^{bz^r} \sin(fz+g)$

01.06.21.0201.01

$$\int a^{bz^2} \sin(fz+g) dz = \frac{i e^{\frac{f^2}{4b \log(a)}-ig} \sqrt{\pi} \left( \operatorname{erfi}\left(\frac{-if+2bz \log(a)}{2 \sqrt{b \log(a)}}\right) - e^{2ig} \operatorname{erfi}\left(\frac{if+2bz \log(a)}{2 \sqrt{b \log(a)}}\right) \right)}{4 \sqrt{b \log(a)}}$$

01.06.21.0202.01

$$\int e^{bz^2} \sin(fz + g) dz = \frac{e^{\frac{f^2}{4b} - ig} \sqrt{\pi} \left( \operatorname{erf}\left(\frac{f+2ibz}{2\sqrt{b}}\right) + e^{2ig} \operatorname{erf}\left(\frac{f-2ibz}{2\sqrt{b}}\right) \right)}{4\sqrt{b}}$$

01.06.21.0203.01

$$\int a^{\sqrt{z}} b \sin(fz + g) dz = \frac{1}{4f\sqrt{f^2}} \left( e^{-\frac{i(b^2 \log^2(a) + 4f(g+fz))}{4f}} \left( b e^{ifz} \sqrt{if} \sqrt{\pi} \operatorname{erfi}\left(\frac{-2if\sqrt{z} + b \log(a)}{2\sqrt{-if}}\right) \log(a) + e^{\frac{ib^2 \log^2(a)}{4f}} \left( b e^{\frac{1}{4}i\left(\frac{b^2 \log^2(a)}{f} + 8g + 4fz\right)} \sqrt{-if} \sqrt{\pi} \operatorname{erfi}\left(\frac{2if\sqrt{z} + b \log(a)}{2\sqrt{if}}\right) \log(a) - 2a^{b\sqrt{z}} (1 + e^{2i(g+fz)}) \sqrt{f^2} \right) \right) \right)$$

01.06.21.0204.01

$$\int e^{\sqrt{z}} b \sin(fz + g) dz = \frac{1}{4} e^{-ig} \left( -\frac{2e^{b\sqrt{z} - ifz} (1 + e^{2i(g+fz)})}{f} + \frac{b e^{\frac{i(b^2 + 8fz)}{4f}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2if\sqrt{z}}{2\sqrt{if}}\right)}{(if)^{3/2}} - \frac{b e^{-\frac{ib^2}{4f}} f \sqrt{\pi} \operatorname{erfi}\left(\frac{b-2if\sqrt{z}}{2\sqrt{-if}}\right)}{(-if)^{5/2}} \right)$$

### Involving $a^{bz^e} \sin(fz + g)$

01.06.21.0205.01

$$\int a^{bz^2+e} \sin(fz + g) dz = \frac{ia^e e^{\frac{f^2}{4b \log(a)} - ig} \sqrt{\pi} \left( \operatorname{erfi}\left(\frac{-if+2bz \log(a)}{2\sqrt{b \log(a)}}\right) - e^{2ig} \operatorname{erfi}\left(\frac{if+2bz \log(a)}{2\sqrt{b \log(a)}}\right) \right)}{4\sqrt{b \log(a)}}$$

01.06.21.0206.01

$$\int e^{bz^2+e} \sin(fz + g) dz = \frac{e^{\frac{f^2}{4b} + e - ig} \sqrt{\pi} \left( \operatorname{erf}\left(\frac{f+2ibz}{2\sqrt{b}}\right) + e^{2ig} \operatorname{erf}\left(\frac{f-2ibz}{2\sqrt{b}}\right) \right)}{4\sqrt{b}}$$

01.06.21.0207.01

$$\int a^{\sqrt{z}} b^{+e} \sin(fz + g) dz = \frac{1}{4f\sqrt{f^2}} \left( a^e e^{-\frac{i(b^2 \log^2(a) + 4f(g+fz))}{4f}} \left( b e^{ifz} \sqrt{if} \sqrt{\pi} \operatorname{erfi}\left(\frac{-2if\sqrt{z} + b \log(a)}{2\sqrt{-if}}\right) \log(a) + e^{\frac{ib^2 \log^2(a)}{4f}} \left( b e^{\frac{1}{4}i\left(\frac{b^2 \log^2(a)}{f} + 8g + 4fz\right)} \sqrt{-if} \sqrt{\pi} \operatorname{erfi}\left(\frac{2if\sqrt{z} + b \log(a)}{2\sqrt{if}}\right) \log(a) - 2a^{b\sqrt{z}} (1 + e^{2i(g+fz)}) \sqrt{f^2} \right) \right) \right)$$

01.06.21.0208.01

$$\int e^{\sqrt{z} b+e} \sin(f z+g) d z = \frac{1}{4} e^{-i g} \left( \frac{2 e^{b \sqrt{z}-i f z} \left(1+e^{2 i(g+f z)}\right)}{f} + \frac{b e^{\frac{i\left(b^2+8 f g\right)}{4 f}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 i f \sqrt{z}}{2 \sqrt{i f}}\right)}{(i f)^{3 / 2}} - \frac{b e^{-\frac{i b^2}{4 f}} f \sqrt{\pi} \operatorname{erfi}\left(\frac{b-2 i f \sqrt{z}}{2 \sqrt{-i f}}\right)}{(-i f)^{5 / 2}} \right)$$

### Involving $a^{b z^f+d z} \sin(f z+g)$

01.06.21.0209.01

$$\int a^{b z^2+d z} \sin(f z+g) d z = \frac{1}{4 \sqrt{b \log (a)}} \left( i a^{-\frac{d^2}{4 b}} e^{\frac{f^2-2 i(d f+2 b g) \log (a)}{4 b \log (a)}} \sqrt{\pi} \left( e^{\frac{i d f}{b}} \operatorname{erfi}\left(\frac{-i f+(d+2 b z) \log (a)}{2 \sqrt{b \log (a)}}\right) - e^{2 i g} \operatorname{erfi}\left(\frac{i f+(d+2 b z) \log (a)}{2 \sqrt{b \log (a)}}\right) \right) \right)$$

01.06.21.0210.01

$$\int e^{b z^2+d z} \sin(f z+g) d z = \frac{i e^{-\frac{d^2+2 i f d-f^2+4 i b g}{4 b}} \sqrt{\pi} \left( e^{\frac{i d f}{b}} \operatorname{erfi}\left(\frac{d-i f+2 b z}{2 \sqrt{b}}\right) - e^{2 i g} \operatorname{erfi}\left(\frac{d+i f+2 b z}{2 \sqrt{b}}\right) \right)}{4 \sqrt{b}}$$

01.06.21.0211.01

$$\int a^{\sqrt{z} b+d z} \sin(f z+g) d z = \frac{e^{-i(g+f z)} a^{\sqrt{z} b+d z}}{2(f+d i \log (a))} - \frac{e^{i(g+f z)} a^{\sqrt{z} b+d z}}{2(f-i d \log (a))} - \frac{i b e^{-\frac{-i b^2 \log ^2(a)+4 d g \log (a)-4 i f g}{4(f+d i \log (a))}} \sqrt{\pi} \operatorname{erfi}\left(\frac{-2 i f \sqrt{z}+(b+2 d \sqrt{z}) \log (a)}{2 \sqrt{-i f+d \log (a)}}\right) \log (a)}{4(-i f+d \log (a))^{3 / 2}} + \frac{i b e^{-\frac{b^2 \log ^2(a)-4 i d g \log (a)+4 f g}{4(i f+d \log (a))}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b \log (a)+2 \sqrt{z}(i f+d \log (a))}{2 \sqrt{i f+d \log (a)}}\right) \log (a)}{4(i f+d \log (a))^{3 / 2}}$$

01.06.21.0212.01

$$\int e^{\sqrt{z} b+d z} \sin(f z+g) d z = \frac{1}{4} e^{-i g} \left( 2 e^{\sqrt{z} b+d z-i f z} \left( -\frac{1}{f+i d} - \frac{e^{2 i(g+f z)}}{f-i d} \right) + \frac{b e^{\frac{b^2}{-4 d-4 i f}+2 i g} i \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d+i f) \sqrt{z}}{2 \sqrt{d+i f}}\right)}{(d+i f)^{3 / 2}} - \frac{i b e^{\frac{b^2}{4 i f-4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d-i f) \sqrt{z}}{2 \sqrt{d-i f}}\right)}{(d-i f)^{3 / 2}} \right)$$

### Involving $a^{b z^f+d z+e} \sin(f z+g)$

01.06.21.0213.01

$$\int a^{bz^2+dz+e} \sin(fz+g) dz = \frac{1}{4\sqrt{b \log(a)}} \left( i a^{-\frac{d^2}{4b}} e^{\frac{f^2-2i(df+2bg)\log(a)}{4b \log(a)}} \sqrt{\pi} \left( e^{\frac{idf}{b}} \operatorname{erfi} \left( \frac{-if+(d+2bz)\log(a)}{2\sqrt{b \log(a)}} \right) - e^{2ig} \operatorname{erfi} \left( \frac{if+(d+2bz)\log(a)}{2\sqrt{b \log(a)}} \right) \right) \right)$$

01.06.21.0214.01

$$\int e^{bz^2+dz+e} \sin(fz+g) dz = \frac{i e^{-\frac{d^2+2idf-f^2-4be+4ibg}{4b}} \sqrt{\pi} \left( e^{\frac{idf}{b}} \operatorname{erfi} \left( \frac{d-if+2bz}{2\sqrt{b}} \right) - e^{2ig} \operatorname{erfi} \left( \frac{d+if+2bz}{2\sqrt{b}} \right) \right)}{4\sqrt{b}}$$

01.06.21.0215.01

$$\int a^{\sqrt{z}bz+dz+e} \sin(fz+g) dz = -\frac{e^{-i(g+fz)} a^{\sqrt{z}bz+dz}}{2(f+di \log(a))} - \frac{e^{i(g+fz)} a^{\sqrt{z}bz+dz}}{2(f-id \log(a))} - \frac{\left( i b e^{-\frac{(b^2-4d)\log^2(a)+4(e f+d g)\log(a)-4ifg}{4(f+d \log(a))}} \sqrt{\pi} \operatorname{erfi} \left( \frac{-2if\sqrt{z}+(b+2d\sqrt{z})\log(a)}{2\sqrt{-if+d \log(a)}} \right) \log(a) \right)}{(4(-if+d \log(a))^{3/2})} + \frac{i b e^{-\frac{(b^2-4d)\log^2(a)-4i(e f+d g)\log(a)+4fg}{4(if+d \log(a))}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b \log(a)+2\sqrt{z}(if+d \log(a))}{2\sqrt{if+d \log(a)}} \right) \log(a)}{4(if+d \log(a))^{3/2}}$$

01.06.21.0216.01

$$\int e^{\sqrt{z}bz+dz+e} \sin(fz+g) dz = \frac{1}{4} e^{-ig} \left( 2 e^{\sqrt{z}bz+dz-ifz} \left( -\frac{1}{f+id} - \frac{e^{2i(g+fz)}}{f-id} \right) + \frac{b e^{-\frac{b^2}{-4d-4if}+2ig} i \sqrt{\pi} \operatorname{erfi} \left( \frac{b+2(d+if)\sqrt{z}}{2\sqrt{d+if}} \right)}{(d+if)^{3/2}} - \frac{i b e^{\frac{b^2}{4if-4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+2(d-if)\sqrt{z}}{2\sqrt{d-if}} \right)}{(d-if)^{3/2}} \right)$$

### Involving $a^{bz} \sin(cz^r)$

01.06.21.0217.01

$$\int a^{bz} \sin(cz^2) dz = \frac{i\sqrt{\pi}}{4\sqrt{ic}} \left( e^{-\frac{ib^2 \log^2(a)}{4c}} \operatorname{erf} \left( \frac{2icz-b \log(a)}{2\sqrt{ic}} \right) - e^{\frac{ib^2 \log^2(a)}{4c}} \operatorname{erfi} \left( \frac{2icz+b \log(a)}{2\sqrt{ic}} \right) \right)$$

01.06.21.0218.01

$$\int e^{bz} \sin(cz^2) dz = \frac{i\sqrt{\pi}}{4\sqrt{ic}} \left( e^{-\frac{ib^2}{4c}} \operatorname{erf} \left( \frac{2icz-b}{2\sqrt{ic}} \right) - e^{\frac{ib^2}{4c}} \operatorname{erfi} \left( \frac{b+2icz}{2\sqrt{ic}} \right) \right)$$

01.06.21.0219.01

$$\int a^{bz} \sin(c\sqrt{z}) dz = \frac{\sin(c\sqrt{z}) a^{bz}}{b \log(a)} - \frac{c e^{\frac{c^2}{4b \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+2b\sqrt{z} \log(a)}{2\sqrt{b \log(a)}} \right)}{4(b \log(a))^{3/2}} + \frac{c e^{\frac{c^2}{4b \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic-2b\sqrt{z} \log(a)}{2\sqrt{b \log(a)}} \right)}{4(b \log(a))^{3/2}}$$

01.06.21.0220.01

$$\int e^{bz} \sin(c\sqrt{z}) dz = -\frac{c e^{\frac{c^2}{4b}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2\sqrt{z} b+ic}{2\sqrt{b}}\right)}{4 b^{3/2}} + \frac{c e^{\frac{c^2}{4b}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic-2b\sqrt{z}}{2\sqrt{b}}\right)}{4 b^{3/2}} + \frac{e^{bz} \sin(c\sqrt{z})}{b}$$

### Involving $a^{bz+e} \sin(cz^r)$

01.06.21.0221.01

$$\int a^{bz+e} \sin(cz^2) dz = \frac{i\sqrt{\pi}}{4\sqrt{ic}} a^e \left( e^{-\frac{ib^2 \log^2(a)}{4c}} \operatorname{erf}\left(\frac{2icz-b \log(a)}{2\sqrt{ic}}\right) - e^{\frac{ib^2 \log^2(a)}{4c}} \operatorname{erfi}\left(\frac{2icz+b \log(a)}{2\sqrt{ic}}\right) \right)$$

01.06.21.0222.01

$$\int e^{bz+e} \sin(cz^2) dz = \frac{i\sqrt{\pi}}{4\sqrt{ic}} \left( e^{-\frac{ib^2}{4c}} \operatorname{erf}\left(\frac{2icz-b}{2\sqrt{ic}}\right) - e^{e+\frac{ib^2}{4c}} \operatorname{erfi}\left(\frac{b+2icz}{2\sqrt{ic}}\right) \right)$$

01.06.21.0223.01

$$\int a^{bz+e} \sin(c\sqrt{z}) dz = \frac{\sin(c\sqrt{z}) a^{bz+e}}{b \log(a)} - \frac{c a^e e^{\frac{c^2}{4b \log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic+2b\sqrt{z} \log(a)}{2\sqrt{b \log(a)}}\right)}{4 (b \log(a))^{3/2}} + \frac{c a^e e^{\frac{c^2}{4b \log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic-2b\sqrt{z} \log(a)}{2\sqrt{b \log(a)}}\right)}{4 (b \log(a))^{3/2}}$$

01.06.21.0224.01

$$\int e^{bz+e} \sin(c\sqrt{z}) dz = -\frac{c e^{\frac{c^2}{4b+e}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2\sqrt{z} b+ic}{2\sqrt{b}}\right)}{4 b^{3/2}} + \frac{c e^{\frac{c^2}{4b+e}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic-2b\sqrt{z}}{2\sqrt{b}}\right)}{4 b^{3/2}} + \frac{e^{bz+e} \sin(c\sqrt{z})}{b}$$

### Involving $a^{bz^r} \sin(cz^r)$

01.06.21.0225.01

$$\int a^{bz^r} \sin(cz^r) dz = -\frac{iz}{2r} \left( \Gamma\left(\frac{1}{r}, iz^r(c+bi \log(a))\right) (iz^r(c+bi \log(a)))^{-1/r} - \Gamma\left(\frac{1}{r}, -z^r(ic+bi \log(a))\right) (-z^r(ic+bi \log(a)))^{-1/r} \right)$$

01.06.21.0226.01

$$\int e^{bz^r} \sin(cz^r) dz = -\frac{iz}{2r} \left( (-b-ic)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -(b-ic)z^r\right) - (-b+ic)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -(b+ic)z^r\right) \right)$$

01.06.21.0227.01

$$\int a^{bz^2} \sin(cz^2) dz = -\frac{1}{4(c^2+b^2 \log^2(a))} \left( \sqrt{\pi} \left( \operatorname{erfi}\left(z\sqrt{ic+b \log(a)}\right) \sqrt{ic+b \log(a)} (c+bi \log(a)) + \operatorname{erfi}\left(z\sqrt{-ic+b \log(a)}\right) \sqrt{-ic+b \log(a)} (c-bi \log(a)) \right) \right)$$

01.06.21.0228.01

$$\int e^{bz^2} \sin(cz^2) dz = \frac{i\sqrt{\pi} \left( \sqrt{b-ic} (b+ic) \operatorname{erfi}\left(\sqrt{b-ic} z\right) - (b-ic) \sqrt{b+ic} \operatorname{erfi}\left(\sqrt{b+ic} z\right) \right)}{4(b^2+c^2)}$$

01.06.21.0229.01

$$\int a^{b\sqrt{z}} \sin(c\sqrt{z}) dz = \frac{1}{(c^2 + b^2 \log^2(a))^2} \left( 2 a^{b\sqrt{z}} \left( (c^2 + b \log(a) (\sqrt{z} c^2 + b \log(a) (b \sqrt{z} \log(a) - 1))) \sin(c\sqrt{z}) - c \cos(c\sqrt{z}) (\sqrt{z} c^2 + b \log(a) (b \sqrt{z} \log(a) - 2)) \right) \right)$$

01.06.21.0230.01

$$\int e^{b\sqrt{z}} \sin(c\sqrt{z}) dz = \frac{1}{(b^2 + c^2)^2} \left( 2 e^{b\sqrt{z}} \left( (c^2 + b (\sqrt{z} c^2 + b (b \sqrt{z} - 1))) \sin(c\sqrt{z}) - c (\sqrt{z} c^2 + b (b \sqrt{z} - 2)) \cos(c\sqrt{z}) \right) \right)$$

### Involving $a^{bz^r+e} \sin(cz^r)$

01.06.21.0231.01

$$\int a^{bz^r+e} \sin(cz^r) dz = -\frac{iz a^e}{2r} \left( \Gamma\left(\frac{1}{r}, iz^r(c + b i \log(a))\right) (iz^r(c + b i \log(a)))^{-1/r} - \Gamma\left(\frac{1}{r}, -z^r(i c + b \log(a))\right) (-iz^r(c - i b \log(a)))^{-1/r} \right)$$

01.06.21.0232.01

$$\int e^{bz^r+e} \sin(cz^r) dz = -\frac{iz e^e}{2r} \left( (-(b - ic) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -(b - ic) z^r\right) - (-(b + ic) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -(b + ic) z^r\right) \right)$$

01.06.21.0233.01

$$\int a^{bz^2+e} \sin(cz^2) dz = -\frac{1}{4(c^2 + b^2 \log^2(a))} \sqrt{\pi} a^e \left( \operatorname{erfi}\left(z \sqrt{ic + b \log(a)}\right) \sqrt{ic + b \log(a)} (c + b i \log(a)) + \operatorname{erfi}\left(z \sqrt{-ic + b \log(a)}\right) \sqrt{-ic + b \log(a)} (c - i b \log(a)) \right)$$

01.06.21.0234.01

$$\int e^{bz^2+e} \sin(cz^2) dz = \frac{i \sqrt{\pi} e^e \left( \sqrt{b - ic} (b + ic) \operatorname{erfi}\left(\sqrt{b - ic} z\right) - (b - ic) \sqrt{b + ic} \operatorname{erfi}\left(\sqrt{b + ic} z\right) \right)}{4(b^2 + c^2)}$$

01.06.21.0235.01

$$\int a^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz = \frac{1}{(c^2 + b^2 \log^2(a))^2} \left( 2 a^{b\sqrt{z}+e} \left( (c^2 + b \log(a) (\sqrt{z} c^2 + b \log(a) (b \sqrt{z} \log(a) - 1))) \sin(c\sqrt{z}) - c \cos(c\sqrt{z}) (\sqrt{z} c^2 + b \log(a) (b \sqrt{z} \log(a) - 2)) \right) \right)$$

01.06.21.0236.01

$$\int e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz = \frac{1}{(b^2 + c^2)^2} \left( 2 e^{b\sqrt{z}+e} \left( (c^2 + b (\sqrt{z} c^2 + b (b \sqrt{z} - 1))) \sin(c\sqrt{z}) - c (\sqrt{z} c^2 + b (b \sqrt{z} - 2)) \cos(c\sqrt{z}) \right) \right)$$

### Involving $a^{bz^r+d z} \sin(cz^r)$



01.06.21.0237.01

$$\int a^{bz^2+dz} \sin(cz^2) dz = \frac{1}{4(c^2 + b^2 \log^2(a))} \left( i \sqrt{\pi} e^{-\frac{bd^2 \log^3(a)}{-2c^2 - 2b^2 \log^2(a)}} \left( e^{\frac{d^2 \log^2(a)}{4(ic+b \log(a))}} \operatorname{erfi} \left( \frac{(d+2bz) \log(a) - 2icz}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) + e^{-\frac{d^2 \log^2(a)}{-4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{2icz + (d+2bz) \log(a)}{2\sqrt{ic+b \log(a)}} \right) (ic-b \log(a)) \sqrt{ic+b \log(a)} \right) \right)$$

01.06.21.0238.01

$$\int e^{bz^2+dz} \sin(cz^2) dz = \frac{i \sqrt{\pi}}{4(b^2 + c^2)} e^{-\frac{bd^2}{-2b^2-2c^2}} \left( (ic-b) \sqrt{b+ic} e^{\frac{d^2}{4b-4ic}} \operatorname{erfi} \left( \frac{d+2bz+2icz}{2\sqrt{b+ic}} \right) + (b+ic) \sqrt{b-ic} e^{\frac{d^2}{4(b+ic)}} \operatorname{erfi} \left( \frac{d+2bz-2icz}{2\sqrt{b-ic}} \right) \right)$$

01.06.21.0239.01

$$\int a^{\sqrt{z}bz+dz} \sin(c\sqrt{z}) dz = \frac{\sin(c\sqrt{z}) a^{\sqrt{z}bz+dz}}{d \log(a)} + \frac{e^{-\frac{(ic-b \log(a))^2}{4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic-b \log(a)-2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}} \right) (c+bi \log(a)) - e^{-\frac{(ic+b \log(a))^2}{4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+b \log(a)+2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}} \right) (c-ib \log(a))}{4(d \log(a))^{3/2}}$$

01.06.21.0240.01

$$\int e^{\sqrt{z}bz+dz} \sin(c\sqrt{z}) dz = -\frac{(c-ib) e^{-\frac{(b+ic)^2}{4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+ic+2d\sqrt{z}}{2\sqrt{d}} \right)}{4d^{3/2}} + \frac{(c+ib) e^{-\frac{(ic-b)^2}{4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{-b+ic-2d\sqrt{z}}{2\sqrt{d}} \right)}{4d^{3/2}} + \frac{e^{\sqrt{z}bz+dz} \sin(c\sqrt{z})}{d}$$

### Involving $a^{bz^r+dz+e} \sin(cz^r)$

01.06.21.0241.01

$$\int a^{bz^2+dz+e} \sin(cz^2) dz = \frac{ia^e \sqrt{\pi}}{4(c^2 + b^2 \log^2(a))} e^{-\frac{bd^2 \log^3(a)}{-2c^2 - 2b^2 \log^2(a)}} \left( e^{\frac{d^2 \log^2(a)}{4(ic+b \log(a))}} \operatorname{erfi} \left( \frac{(d+2bz) \log(a) - 2icz}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) + e^{-\frac{d^2 \log^2(a)}{-4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{2icz + (d+2bz) \log(a)}{2\sqrt{ic+b \log(a)}} \right) (ic-b \log(a)) \sqrt{ic+b \log(a)} \right)$$

01.06.21.0242.01

$$\int e^{bz^2+dz+e} \sin(cz^2) dz = \frac{i\sqrt{\pi}}{4(b^2+c^2)} e^{\frac{bd^2}{-2b^2-2c^2}+e} \left( (i c - b) \sqrt{b+ic} e^{\frac{d^2}{4b-4ic}} \operatorname{erfi}\left(\frac{d+2bz+2icz}{2\sqrt{b+ic}}\right) + (b+ic) \sqrt{b-ic} e^{\frac{d^2}{4(b+ic)}} \operatorname{erfi}\left(\frac{d+2bz-2icz}{2\sqrt{b-ic}}\right) \right)$$

01.06.21.0243.01

$$\int a^{\sqrt{z} b+e+dz} \sin(c\sqrt{z}) dz = \frac{\sin(c\sqrt{z}) a^{\sqrt{z} b+e+dz} e^{\frac{e \log(a) - \frac{(ic-b \log(a))^2}{4d \log(a)}}{4d \log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic-b \log(a) - 2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}}\right) (c + b i \log(a))}{d \log(a)} + \frac{e^{\frac{e \log(a) - \frac{(ic+b \log(a))^2}{4d \log(a)}}{4d \log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic+b \log(a) + 2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}}\right) (c - i b \log(a))}{4 (d \log(a))^{3/2}}$$

01.06.21.0244.01

$$\int e^{\sqrt{z} b+e+dz} \sin(c\sqrt{z}) dz = \frac{(c - ib) e^{-\frac{(b+ic)^2}{4d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+ic+2d\sqrt{z}}{2\sqrt{d}}\right) + (c + ib) e^{-\frac{(ic-b)^2}{4d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{-b+ic-2d\sqrt{z}}{2\sqrt{d}}\right) + e^{\sqrt{z} b+e+dz} \sin(c\sqrt{z})}{4d^{3/2}} + \frac{e^{\sqrt{z} b+e+dz} \sin(c\sqrt{z})}{d}$$

### Involving $a^{dz} \sin(cz^r + g)$

01.06.21.0245.01

$$\int a^{dz} \sin(cz^2 + g) dz = -\frac{1}{4c} \left( e^{-\frac{1}{4}i\left(\frac{d^2 \log^2(a)}{c} + 4g\right)} \sqrt{\pi} \left( \sqrt{-ic} \operatorname{erfi}\left(\frac{d \log(a) - 2icz}{2\sqrt{-ic}}\right) + \sqrt{ic} e^{\frac{1}{2}i\left(\frac{d^2 \log^2(a)}{c} + 4g\right)} \operatorname{erfi}\left(\frac{2icz + d \log(a)}{2\sqrt{ic}}\right) \right) \right)$$

01.06.21.0246.01

$$\int e^{dz} \sin(cz^2 + g) dz = -\frac{\sqrt{\pi}}{4c} e^{-\frac{id^2}{4c} - ig} \left( \sqrt{-ic} \operatorname{erfi}\left(\frac{d - 2icz}{2\sqrt{-ic}}\right) + \sqrt{ic} e^{\frac{i(d^2+4cg)}{2c}} \operatorname{erfi}\left(\frac{d + 2icz}{2\sqrt{ic}}\right) \right)$$

01.06.21.0247.01

$$\int a^{dz} \sin(\sqrt{z} c + g) dz = -\frac{1}{4 (d \log(a))^{3/2}} \left( i e^{-i(\sqrt{z} c + g)} \left( 2 \left( -1 + e^{2i(\sqrt{z} c + g)} \right) \sqrt{d \log(a)} a^{dz} - ic e^{\frac{1}{4}c\left(\frac{c}{d \log(a)} + 4i\sqrt{z}\right)} \sqrt{\pi} \operatorname{erfi}\left(\frac{-ic + 2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}}\right) - ic e^{\frac{c^2}{4d \log(a)} + i\sqrt{z} c + 2ig} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic + 2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}}\right) \right) \right)$$

01.06.21.0248.01

$$\int e^{dz} \sin(\sqrt{z} c + g) dz = -\frac{1}{4d^{3/2}} \left( i e^{-i(\sqrt{z} c + g)} \right. \\ \left. \left( 2\sqrt{d} e^{dz} \left( -1 + e^{2i(\sqrt{z} c + g)} \right) - c e^{\frac{c(c+4id\sqrt{z})}{4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{c+2id\sqrt{z}}{2\sqrt{d}} \right) + c e^{\frac{c^2}{4d} + i\sqrt{z} c + 2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{c-2id\sqrt{z}}{2\sqrt{d}} \right) \right) \right)$$

### Involving $a^{dz+e} \sin(cz^r + g)$

01.06.21.0249.01

$$\int a^{dz+e} \sin(cz^2 + g) dz = \\ -\frac{1}{4c} \left( a^e e^{-\frac{1}{4}i \left( \frac{d^2 \log^2(a)}{c} + 4g \right)} \sqrt{\pi} \left( \sqrt{-ic} \operatorname{erfi} \left( \frac{d \log(a) - 2icz}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{1}{2}i \left( \frac{d^2 \log^2(a)}{c} + 4g \right)} \operatorname{erfi} \left( \frac{2icz + d \log(a)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0250.01

$$\int e^{dz+e} \sin(cz^2 + g) dz = -\frac{\sqrt{\pi}}{4c} e^{-\frac{id^2}{4c} + e - ig} \left( \sqrt{-ic} \operatorname{erfi} \left( \frac{d-2icz}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{i(d^2+4cg)}{2c}} \operatorname{erfi} \left( \frac{d+2icz}{2\sqrt{ic}} \right) \right)$$

01.06.21.0251.01

$$\int a^{dz+e} \sin(\sqrt{z} c + g) dz = \\ -\frac{1}{4(d \log(a))^{3/2}} \left( i a^e e^{-i(\sqrt{z} c + g)} \left( 2 \left( -1 + e^{2i(\sqrt{z} c + g)} \right) \sqrt{d \log(a)} a^{dz} - i c e^{\frac{1}{4}c \left( \frac{c}{d \log(a)} + 4i\sqrt{z} \right)} \sqrt{\pi} \operatorname{erfi} \left( \frac{-ic + 2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}} \right) - \right. \right. \\ \left. \left. i c e^{\frac{c^2}{4d \log(a)} + i\sqrt{z} c + 2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic + 2d\sqrt{z} \log(a)}{2\sqrt{d \log(a)}} \right) \right) \right)$$

01.06.21.0252.01

$$\int e^{dz+e} \sin(\sqrt{z} c + g) dz = -\frac{1}{4d^{3/2}} \left( i e^{e-i(\sqrt{z} c + g)} \right. \\ \left. \left( 2\sqrt{d} e^{dz} \left( -1 + e^{2i(\sqrt{z} c + g)} \right) - c e^{\frac{c(c+4id\sqrt{z})}{4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{c+2id\sqrt{z}}{2\sqrt{d}} \right) + c e^{\frac{c^2}{4d} + i\sqrt{z} c + 2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{c-2id\sqrt{z}}{2\sqrt{d}} \right) \right) \right)$$

### Involving $a^{bz^r} \sin(cz^r + g)$

01.06.21.0253.01

$$\int a^{bz^r} \sin(cz^r + g) dz = \\ -\frac{1}{2r} i z \left( e^{-ig} \Gamma \left( \frac{1}{r}, i z^r (c + b i \log(a)) \right) (i z^r (c + b i \log(a)))^{-1/r} - e^{ig} \Gamma \left( \frac{1}{r}, -z^r (i c + b \log(a)) \right) (-z^r (i c + b \log(a)))^{-1/r} \right)$$

01.06.21.0254.01

$$\int e^{bz^r} \sin(cz^r + g) dz = \frac{iz}{2r} \left( e^{ig} (-b + ic) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, -(b + ic) z^r \right) - e^{-ig} (i(c + ib) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, i(c + ib) z^r \right) \right)$$

01.06.21.0255.01

$$\int a^{bz^2} \sin(cz^2 + g) dz = \frac{1}{4} i \sqrt{\pi} \left( \frac{e^{-ig} \operatorname{erfi}\left(z \sqrt{-ic + b \log(a)}\right)}{\sqrt{-ic + b \log(a)}} - \frac{e^{ig} \operatorname{erfi}\left(z \sqrt{ic + b \log(a)}\right)}{\sqrt{ic + b \log(a)}} \right)$$

01.06.21.0256.01

$$\int e^{bz^2} \sin(cz^2 + g) dz = \frac{1}{4} i \sqrt{\pi} \left( \frac{e^{-ig} \operatorname{erfi}\left(\sqrt{b-ic} z\right)}{\sqrt{b-ic}} - \frac{e^{ig} \operatorname{erfi}\left(\sqrt{b+ic} z\right)}{\sqrt{b+ic}} \right)$$

01.06.21.0257.01

$$\int a^{b\sqrt{z}} \sin(\sqrt{z} c + g) dz = -\frac{1}{(c^2 + b^2 \log^2(a))^2} \left( 2 a^{b\sqrt{z}} \left( c \cos(\sqrt{z} c + g) (\sqrt{z} c^2 + b^2 \sqrt{z} \log^2(a) - 2 b \log(a)) - (b^3 \sqrt{z} \log^3(a) - b^2 \log^2(a) + b c^2 \sqrt{z} \log(a) + c^2) \sin(\sqrt{z} c + g) \right) \right)$$

01.06.21.0258.01

$$\int e^{b\sqrt{z}} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^2} \left( 2 e^{b\sqrt{z}} \left( (\sqrt{z} b^3 - b^2 + c^2 \sqrt{z} b + c^2) \sin(\sqrt{z} c + g) - c (\sqrt{z} b^2 - 2 b + c^2 \sqrt{z}) \cos(\sqrt{z} c + g) \right) \right)$$

### Involving $a^{bz^r+e} \sin(cz^r + g)$

01.06.21.0259.01

$$\int a^{bz^r+e} \sin(cz^r + g) dz = \frac{1}{2r} \left( i a^e e^{-ig} z \left( e^{2ig} \Gamma\left(\frac{1}{r}, z^r(-ic - b \log(a))\right) (z^r(-ic - b \log(a)))^{-1/r} - \Gamma\left(\frac{1}{r}, i z^r(c + b i \log(a))\right) (i z^r(c + b i \log(a)))^{-1/r} \right) \right)$$

01.06.21.0260.01

$$\int e^{bz^r+e} \sin(cz^r + g) dz = \frac{iz}{2r} \left( e^{e+ig} (-b + ic) z^r \Gamma\left(\frac{1}{r}, -(b + ic) z^r\right) - e^{-ig} (ic + ib) z^r \Gamma\left(\frac{1}{r}, i(c + ib) z^r\right) \right)$$

01.06.21.0261.01

$$\int a^{bz^2+e} \sin(cz^2 + g) dz = \frac{1}{4} i a^e e^{-ig} \sqrt{\pi} \left( \frac{\operatorname{erfi}\left(z \sqrt{-ic + b \log(a)}\right)}{\sqrt{-ic + b \log(a)}} - \frac{e^{2ig} \operatorname{erfi}\left(z \sqrt{ic + b \log(a)}\right)}{\sqrt{ic + b \log(a)}} \right)$$

01.06.21.0262.01

$$\int e^{bz^2+e} \sin(cz^2 + g) dz = \frac{1}{4} i \sqrt{\pi} \left( \frac{e^{-ig} \operatorname{erfi}\left(\sqrt{b-ic} z\right)}{\sqrt{b-ic}} - \frac{e^{e+ig} \operatorname{erfi}\left(\sqrt{b+ic} z\right)}{\sqrt{b+ic}} \right)$$

01.06.21.0263.01

$$\int a^{\sqrt{z} b+e} \sin(\sqrt{z} c + g) dz = \frac{1}{(c^2 + b^2 \log^2(a))^2} \left( 2 a^{\sqrt{z} b+e} \left( (b^3 \sqrt{z} \log^3(a) - b^2 \log^2(a) + b c^2 \sqrt{z} \log(a) + c^2) \sin(\sqrt{z} c + g) - c \cos(\sqrt{z} c + g) (\sqrt{z} c^2 + b^2 \sqrt{z} \log^2(a) - 2 b \log(a)) \right) \right)$$

01.06.21.0264.01

$$\int e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^2} (2 e^{b\sqrt{z}+e} ((\sqrt{z} b^3 - b^2 + c^2 \sqrt{z} b + c^2) \sin(\sqrt{z} c + g) - c(\sqrt{z} b^2 - 2b + c^2 \sqrt{z}) \cos(\sqrt{z} c + g)))$$

**Involving  $a^{bz^r+dz} \sin(cz^r + g)$**

01.06.21.0265.01

$$\int a^{bz^2+dz} \sin(cz^2 + g) dz = \frac{1}{4(c^2 + b^2 \log^2(a))} \left( i a^{-\frac{bd^2 \log^2(a)}{2(c^2+b^2 \log^2(a))}} \sqrt{\pi} \left( e^{\frac{d^2 \log^2(a)}{4ic+4b \log(a)} - ig} \operatorname{erfi} \left( \frac{(d+2bz) \log(a) - 2icz}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) + e^{\frac{d^2 \log^2(a)}{4ic+4b \log(a)} + ig} i \operatorname{erfi} \left( \frac{2icz + (d+2bz) \log(a)}{2\sqrt{ic+b \log(a)}} \right) (c+bi \log(a)) \sqrt{ic+b \log(a)} \right) \right)$$

01.06.21.0266.01

$$\int e^{bz^2+dz} \sin(cz^2 + g) dz = \frac{1}{4(b^2 + c^2)} \left( i e^{-\frac{bd^2}{2(b^2+c^2)} - ig} \sqrt{\pi} \left( \sqrt{b-ic} (b+ic) e^{\frac{d^2}{4b+4ic}} \operatorname{erfi} \left( \frac{d+2(b-ic)z}{2\sqrt{b-ic}} \right) - (b-ic) \sqrt{b+ic} e^{\frac{d^2}{4b-4ic} + 2ig} \operatorname{erfi} \left( \frac{d+2(b+ic)z}{2\sqrt{b+ic}} \right) \right) \right)$$

01.06.21.0267.01

$$\int a^{\sqrt{z} b+dz} \sin(\sqrt{z} c + g) dz = -\frac{1}{4(d \log(a))^{3/2}} \left( i a^{-\frac{b^2}{4d}} e^{-\frac{i(b c+2d(\sqrt{z} c+g))}{2d}} \left( 2 e^{\frac{ibc}{2d}} (-1 + e^{2i(\sqrt{z} c+g)}) \sqrt{d \log(a)} a^{\frac{(b+2d\sqrt{z})^2}{4d}} + e^{\frac{c(c+4i(b+d\sqrt{z}) \log(a))}{4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{-ic + (b+2d\sqrt{z}) \log(a)}{2\sqrt{d \log(a)}} \right) (-ic+b \log(a)) - i e^{\frac{c^2}{4d \log(a)} + i\sqrt{z} c+2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic + (b+2d\sqrt{z}) \log(a)}{2\sqrt{d \log(a)}} \right) (c-ib \log(a)) \right) \right)$$

01.06.21.0268.01

$$\int e^{\sqrt{z} b+dz} \sin(\sqrt{z} c + g) dz = -\frac{1}{4d^{3/2}} \left( i e^{-\frac{b^2+2icb+4di(\sqrt{z} c+g)}{4d}} \left( 2\sqrt{d} e^{\frac{b^2+2icb+4d\sqrt{z} b+4d^2z}{4d}} (-1 + e^{2i(\sqrt{z} c+g)}) - (b+ic) e^{\frac{c^2}{4d} + i\sqrt{z} c+2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+ic+2d\sqrt{z}}{2\sqrt{d}} \right) + (b-ic) e^{\frac{c(c+4ib+4id\sqrt{z})}{4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b-ic+2d\sqrt{z}}{2\sqrt{d}} \right) \right) \right)$$

**Involving  $a^{bz^r+dz+e} \sin(cz^r + g)$**

01.06.21.0269.01

$$\int a^{bz^2+dz+e} \sin(cz^2+g) dz = \frac{1}{4(c^2+b^2 \log^2(a))} \left( i a^{-\frac{bd^2 \log^2(a)}{2(c^2+b^2 \log^2(a))}} \sqrt{\pi} \left( e^{\frac{d^2 \log^2(a)}{4ic+4b \log(a)}-ig} \operatorname{erfi} \left( \frac{(d+2bz) \log(a) - 2icz}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) + e^{-\frac{d^2 \log^2(a)}{4ic+4b \log(a)}+ig} i \operatorname{erfi} \left( \frac{2icz+(d+2bz) \log(a)}{2\sqrt{ic+b \log(a)}} \right) (c+bi \log(a)) \sqrt{ic+b \log(a)} \right) \right)$$

01.06.21.0270.01

$$\int e^{bz^2+dz+e} \sin(cz^2+g) dz = \frac{1}{4(b^2+c^2)} \left( i e^{-\frac{bd^2}{2(b^2+c^2)}+e-ig} \sqrt{\pi} \left( \sqrt{b-ic} (b+ic) e^{\frac{d^2}{4b+4ic}} \operatorname{erfi} \left( \frac{d+2(b-ic)z}{2\sqrt{b-ic}} \right) - (b-ic) \sqrt{b+ic} e^{\frac{d^2}{4b-4ic}+2ig} \operatorname{erfi} \left( \frac{d+2(b+ic)z}{2\sqrt{b+ic}} \right) \right) \right)$$

01.06.21.0271.01

$$\int a^{\sqrt{z}bz+dz+e} \sin(\sqrt{z}c+g) dz = -\frac{1}{4(d \log(a))^{3/2}} \left( i a^{-\frac{bd^2}{4d}} e^{-\frac{i(b+c+2d(\sqrt{z}c+g))}{2d}} \left( 2 e^{\frac{ibc}{2d}} (-1 + e^{2i(\sqrt{z}c+g)}) \sqrt{d \log(a)} a^{\frac{(b+2d\sqrt{z})^2}{4d}} + e^{\frac{c(c+4i(b+d\sqrt{z}) \log(a))}{4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{-ic+(b+2d\sqrt{z}) \log(a)}{2\sqrt{d \log(a)}} \right) (-ic+b \log(a)) - i e^{\frac{c^2}{4d \log(a)}+i\sqrt{z}c+2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+(b+2d\sqrt{z}) \log(a)}{2\sqrt{d \log(a)}} \right) (c-ib \log(a)) \right) \right)$$

01.06.21.0272.01

$$\int e^{\sqrt{z}bz+dz+e} \sin(\sqrt{z}c+g) dz = -\frac{1}{4d^{3/2}} \left( i e^{-\frac{b^2+2icb-4d(e-i(\sqrt{z}c+g))}{4d}} \left( 2\sqrt{d} e^{\frac{b^2+2icb+4d\sqrt{z}b+4d^2z}{4d}} (-1 + e^{2i(\sqrt{z}c+g)}) - (b+ic) e^{\frac{c^2}{4d}+i\sqrt{z}c+2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+ic+2d\sqrt{z}}{2\sqrt{d}} \right) + (b-ic) e^{\frac{c(c+4ib+4id\sqrt{z})}{4d}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b-ic+2d\sqrt{z}}{2\sqrt{d}} \right) \right) \right)$$

Involving rational functions of exp

Involving  $(a + b e^{dz})^{-n} \sin(cz + e)$

01.06.21.0273.01

$$\int \frac{\sin(cz)}{(a + b e^{dz})^n} dz = -\frac{a^{-n}}{2c} \left( e^{icz} {}_2F_1 \left( \frac{ic}{d}, n; \frac{d+ic}{d}; -\frac{b e^{dz}}{a} \right) + e^{-icz} {}_2F_1 \left( -\frac{ic}{d}, n; \frac{d-ic}{d}; -\frac{b e^{dz}}{a} \right) \right) /; n \in \mathbb{N}^+$$

01.06.21.0274.01

$$\int \frac{\sin(e+cz)}{(a+be^{dz})^n} dz = -\frac{a^{-n}}{2c} \left( e^{ie+ic z} {}_2F_1\left(\frac{ic}{d}, n; \frac{d+ic}{d}; -\frac{be^{dz}}{a}\right) + e^{-ie-ic z} {}_2F_1\left(-\frac{ic}{d}, n; \frac{d-ic}{d}; -\frac{be^{dz}}{a}\right) \right); n \in \mathbb{N}^+$$

**Involving  $e^{pz}(a+be^{dz})^{-n} \sin(cz+e)$**

01.06.21.0275.01

$$\int \frac{e^{pz} \sin(cz)}{(a+be^{dz})^n} dz = -\frac{1}{2(c+ip)(c-ip)} \left( a^{-n} \left( e^{(-ic+p)z} (c-ip) {}_2F_1\left(\frac{-ic+p}{d}, n; \frac{d-ic+p}{d}; -\frac{be^{dz}}{a}\right) + e^{(ic+p)z} (c+ip) {}_2F_1\left(\frac{ic+p}{d}, n; \frac{d+ic+p}{d}; -\frac{be^{dz}}{a}\right) \right) \right); n \in \mathbb{N}^+$$

01.06.21.0276.01

$$\int \frac{e^{pz} \sin(e+cz)}{(a+be^{dz})^n} dz = -\frac{1}{2(c+ip)(c-ip)} \left( a^{-n} e^{-ie} \left( e^{(-ic+p)z} (c-ip) {}_2F_1\left(\frac{-ic+p}{d}, n; \frac{d-ic+p}{d}; -\frac{be^{dz}}{a}\right) + e^{2ie+(ic+p)z} (c+ip) {}_2F_1\left(\frac{ic+p}{d}, n; \frac{d+ic+p}{d}; -\frac{be^{dz}}{a}\right) \right) \right); n \in \mathbb{N}^+$$

**Involving algebraic functions of exp**

**Involving  $(a+be^{dz})^\beta \sin(c+ez)$**

01.06.21.0277.01

$$\int (a+be^{dz})^\beta \sin(cz) dz = -\frac{e^{-icz} (a+be^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta}}{2c} \left( e^{2icz} {}_2F_1\left(\frac{ic}{d}, -\beta; 1 + \frac{ic}{d}; -\frac{be^{dz}}{a}\right) + {}_2F_1\left(-\frac{ic}{d}, -\beta; 1 - \frac{ic}{d}; -\frac{be^{dz}}{a}\right) \right)$$

01.06.21.0278.01

$$\int (a+be^{dz})^\beta \sin(e+cz) dz = -\frac{1}{2c} e^{-i(e+cz)} (a+be^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \left( e^{2i(e+cz)} {}_2F_1\left(\frac{ic}{d}, -\beta; 1 + \frac{ic}{d}; -\frac{be^{dz}}{a}\right) + {}_2F_1\left(-\frac{ic}{d}, -\beta; 1 - \frac{ic}{d}; -\frac{be^{dz}}{a}\right) \right)$$

**Involving  $e^{pz}(a+be^{dz})^\beta \sin(cz+e)$**

01.06.21.0279.01

$$\int e^{pz} (a+be^{dz})^\beta \sin(cz) dz = -\frac{1}{2(c+ip)(c-ip)} (a+be^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \left( e^{(-ic+p)z} (c-ip) {}_2F_1\left(\frac{-ic+p}{d}, -\beta; \frac{d-ic+p}{d}; -\frac{be^{dz}}{a}\right) + e^{(ic+p)z} (c+ip) {}_2F_1\left(\frac{ic+p}{d}, -\beta; \frac{d+ic+p}{d}; -\frac{be^{dz}}{a}\right) \right)$$

01.06.21.0280.01

$$\int e^{pz} (a + b e^{dz})^\beta \sin(e + cz) dz =$$

$$-\frac{1}{2(c + ip)(c - ip)} \left( e^{-ie} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \left( e^{(-ic+p)z} (c - ip) {}_2F_1 \left( \frac{-ic+p}{d}, -\beta; \frac{d-ic+p}{d}; -\frac{b e^{dz}}{a} \right) + \right.$$

$$\left. e^{2ie+(ic+p)z} (c + ip) {}_2F_1 \left( \frac{ic+p}{d}, -\beta; \frac{d+ic+p}{d}; -\frac{b e^{dz}}{a} \right) \right)$$

### Involving exponential function and a power function

Involving exp and power

### Involving $z^{\alpha-1} e^{bz} \sin(cz)$

01.06.21.0281.01

$$\int z^{\alpha-1} e^{bz} \sin(cz) dz = -\frac{1}{2} i z^\alpha \left( (-b - ic) z^{-\alpha} \Gamma(\alpha, -(b - ic)z) - (-b + ic) z^{-\alpha} \Gamma(\alpha, -(b + ic)z) \right)$$

01.06.21.0282.01

$$\int z^{\alpha-1} e^{icz} \sin(cz) dz = \frac{1}{2} i z^\alpha \left( 2^{-\alpha} \Gamma(\alpha, -2icz) (-icz)^{-\alpha} + \frac{1}{\alpha} \right)$$

01.06.21.0283.01

$$\int z^{\alpha-1} e^{-icz} \sin(cz) dz = -\frac{1}{2} i z^\alpha \left( 2^{-\alpha} \Gamma(\alpha, 2icz) (icz)^{-\alpha} + \frac{1}{\alpha} \right)$$

01.06.21.0284.01

$$\int z^n e^{bz} \sin(cz) dz =$$

$$\frac{1}{2} i z^{n+1} \left( (-ic - b) z^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}((ic + b)z)}{(-n-1)!} + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic - b)z)^k}{(n+1)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic - b)z)^k}{(n+1)_{k-n}} \right) - \right.$$

$$\left. ((ic - b)z)^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}((-ic + b)z)}{(-n-1)!} + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic - b)z)^k}{(n+1)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic - b)z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0285.01

$$\int z^n e^{bz} \sin(cz) dz = -\frac{i}{2} n! \left( (ic - b)^{-n-1} e^{(b-ic)z} \sum_{k=0}^n \frac{((ic - b)z)^k}{k!} - (-b - ic)^{-n-1} e^{(b+ic)z} \sum_{k=0}^n \frac{(-b + ic)z)^k}{k!} \right); n \in \mathbb{N}$$

01.06.21.0286.01

$$\int z e^{bz} \sin(cz) dz = \frac{e^{bz} \left( (zb^3 - b^2 + c^2 z b + c^2) \sin(cz) - c(zb^2 - 2b + c^2 z) \cos(cz) \right)}{(b^2 + c^2)^2}$$

01.06.21.0287.01

$$\int z e^{icz} \sin(cz) dz = \frac{2ic^2 z^2 - e^{2icz} (i + 2cz)}{8c^2}$$



01.06.21.0288.01

$$\int z e^{-ic z} \sin(c z) dz = \frac{1}{8} \left( \frac{e^{-2ic z} (i - 2c z)}{c^2} - 2i z^2 \right)$$

01.06.21.0289.01

$$\int z^2 e^{bz} \sin(c z) dz = \frac{1}{(b^2 + c^2)^3} (e^{bz} ((z^2 b^5 - 2z b^4 + 2(c^2 z^2 + 1)b^3 + c^2(c^2 z^2 - 6)b + 2c^4 z) \sin(c z) - c(z^2 b^4 - 4z b^3 + 2(c^2 z^2 + 3)b^2 - 4c^2 z b + c^2(c^2 z^2 - 2)) \cos(c z)))$$

01.06.21.0290.01

$$\int z^2 e^{ic z} \sin(c z) dz = \frac{4c^3 i z^3 + e^{2ic z} (-6c^2 z^2 - 6ic z + 3)}{24c^3}$$

01.06.21.0291.01

$$\int z^2 e^{-ic z} \sin(c z) dz = \frac{e^{-2ic z} (-2c^2 z^2 + 2ic z + 1)}{8c^3} - \frac{iz^3}{6}$$

01.06.21.0292.01

$$\int z^3 e^{bz} \sin(c z) dz = \frac{1}{(b^2 + c^2)^4} e^{bz} ((z^3 b^7 - 3z^2 b^6 + 3z(c^2 z^2 + 2)b^5 - 3(c^2 z^2 + 2)b^4 + 3c^2 z(c^2 z^2 - 4)b^3 + 3c^2(c^2 z^2 + 12)b^2 + c^4 z(c^2 z^2 - 18)b + 3c^4(c^2 z^2 - 2)) \sin(c z) - c(z^3 b^6 - 6z^2 b^5 + 3z(c^2 z^2 + 6)b^4 - 12(c^2 z^2 + 2)b^3 + 3c^2 z(c^2 z^2 + 4)b^2 - 6c^2(c^2 z^2 - 4)b + c^4 z(c^2 z^2 - 6)) \cos(c z))$$

01.06.21.0293.01

$$\int z^4 e^{bz} \sin(c z) dz = \frac{1}{(b^2 + c^2)^5} e^{bz} ((z^4 b^9 - 4z^3 b^8 + 4z^2(c^2 z^2 + 3)b^7 - 8z(c^2 z^2 + 3)b^6 + 6(c^4 z^4 - 2c^2 z^2 + 4)b^5 + 120c^2 z b^4 + 4c^2(c^4 z^4 - 15c^2 z^2 - 60)b^3 + 8c^4 z(c^2 z^2 + 15)b^2 + c^4(c^4 z^4 - 36c^2 z^2 + 120)b + 4c^6 z(c^2 z^2 - 6)) \sin(c z) - c(z^4 b^8 - 8z^3 b^7 + 4z^2(c^2 z^2 + 9)b^6 - 24z(c^2 z^2 + 4)b^5 + 6(c^4 z^4 + 10c^2 z^2 + 20)b^4 - 24c^4 z^3 b^3 + 4c^2(c^4 z^4 + 3c^2 z^2 - 60)b^2 + (96c^4 z - 8c^6 z^3)b + c^4(c^4 z^4 - 12c^2 z^2 + 24)) \cos(c z))$$

01.06.21.0294.01

$$\int z^5 e^{bz} \sin(c z) dz = \frac{1}{(b^2 + c^2)^6} (e^{bz} ((z^5 b^{11} - 5z^4 b^{10} + 5z^3(c^2 z^2 + 4)b^9 - 15z^2(c^2 z^2 + 4)b^8 + 10z(c^4 z^4 + 12)b^7 - 10(c^4 z^4 - 24c^2 z^2 + 12)b^6 + 10c^2 z(c^4 z^4 - 12c^2 z^2 - 108)b^5 + 10c^2(c^4 z^4 + 60c^2 z^2 + 180)b^4 + 5c^4 z(c^4 z^4 - 32c^2 z^2 - 120)b^3 + 15c^4(c^4 z^4 + 16c^2 z^2 - 120)b^2 + c^6 z(c^4 z^4 - 60c^2 z^2 + 600)b + 5c^6(c^4 z^4 - 12c^2 z^2 + 24)) \sin(c z) - c(z^5 b^{10} - 10z^4 b^9 + 5z^3(c^2 z^2 + 12)b^8 - 40z^2(c^2 z^2 + 6)b^7 + 10z(c^4 z^4 + 16c^2 z^2 + 60)b^6 - 60(c^4 z^4 + 4c^2 z^2 + 12)b^5 + 10c^2 z(c^4 z^4 + 12c^2 z^2 - 60)b^4 - 40c^2(c^4 z^4 - 6c^2 z^2 - 60)b^3 + 5c^4 z(c^4 z^4 - 216)b^2 - 10c^4(c^4 z^4 - 24c^2 z^2 + 72)b + c^6 z(c^4 z^4 - 20c^2 z^2 + 120)) \cos(c z)))$$

01.06.21.0295.01

$$\int z^{-n} e^{bz} \sin(cz) dz = \frac{i e^{(-b-i)c} z}{2(b^2 + c^2)(n-1)!} \left( -(i c - b)^n (b + i c) e^{2bz} (n-1)! \sum_{k=1}^{n-1} \frac{(i c - b)^{k-n} z^{k-n}}{(1-n)_k} - (-b - i c)^n (i c - b) e^{2(b+i c)z} (n-1)! \sum_{k=1}^{n-1} \frac{(-b - i c)^{k-n} z^{k-n}}{(1-n)_k} + (-1)^n e^{(b+i c)z} ((b + i c) \operatorname{Ei}((b - i c) z) (i c - b)^n + (-b - i c)^n \operatorname{Ei}((b + i c) z) (i c - b)) \right) /; n \in \mathbb{N}^+$$

01.06.21.0296.01

$$\int \frac{e^{bz} \sin(cz)}{z} dz = \frac{1}{2} i (\operatorname{Ei}((b - i c) z) - \operatorname{Ei}((b + i c) z))$$

01.06.21.0297.01

$$\int \frac{e^{icz} \sin(cz)}{z} dz = -\frac{1}{2} i (\operatorname{Ei}(2 i c z) - \log(z))$$

01.06.21.0298.01

$$\int \frac{e^{-icz} \sin(cz)}{z} dz = \frac{1}{2} i (\operatorname{Ei}(-2 i c z) - \log(z))$$

01.06.21.0299.01

$$\int \frac{e^{bz} \sin(cz)}{z^2} dz = \frac{i e^{(b-i)c} z (-1 + e^{2icz}) + (c + i b) z \operatorname{Ei}((b - i c) z) + (c - i b) z \operatorname{Ei}((b + i c) z)}{2 z}$$

01.06.21.0300.01

$$\int \frac{e^{icz} \sin(cz)}{z^2} dz = \frac{i (-1 + e^{2icz}) + 2 c z \operatorname{Ei}(2 i c z)}{2 z}$$

01.06.21.0301.01

$$\int \frac{e^{-icz} \sin(cz)}{z^2} dz = \frac{i - i e^{-2icz} + 2 c z \operatorname{Ei}(-2 i c z)}{2 z}$$

01.06.21.0302.01

$$\int \frac{e^{bz} \sin(cz)}{z^3} dz = \frac{1}{4 z^2} i \left( -(b + i c)^2 \operatorname{Ei}((b + i c) z) z^2 + (b - i c)^2 \operatorname{Ei}((b - i c) z) z^2 + e^{(b-i)c} z (-b z + i c z + e^{2icz} (b z + i c z + 1) - 1) \right)$$

01.06.21.0303.01

$$\int \frac{e^{bz} \sin(cz)}{z^4} dz = -\frac{1}{12} i \left( \operatorname{Ei}((b + i c) z) (b + i c)^3 + \frac{e^{(b-i)c} z ((b - i c)^2 z^2 + (b - i c) z + 2)}{z^3} - (b - i c)^3 \operatorname{Ei}((b - i c) z) - \frac{e^{(b+i)c} z ((b + i c)^2 z^2 + (b + i c) z + 2)}{z^3} \right)$$

01.06.21.0304.01

$$\int \frac{e^{bz} \sin(cz)}{z^5} dz = -\frac{1}{48} i \left( \text{Ei}((b+ic)z) (b+ic)^4 + \frac{e^{(b-ic)z} ((b-ic)^3 z^3 + (b-ic)^2 z^2 + 2(b-ic)z + 6)}{z^4} - \right. \\ \left. (b-ic)^4 \text{Ei}((b-ic)z) - \frac{e^{(b+ic)z} ((b+ic)^3 z^3 + (b+ic)^2 z^2 + 2(b+ic)z + 6)}{z^4} \right)$$

01.06.21.0305.01

$$\int z^{n+\frac{1}{2}} e^{bz} \sin(cz) dz = \\ \frac{1}{2} i z^{n+\frac{3}{2}} \left( (-ic-b)z^{-n-\frac{3}{2}} \left( \text{erfc}(\sqrt{-ic-b}z) \Gamma\left(n+\frac{3}{2}\right) + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) - \right. \\ \left. ((ic-b)z)^{-n-\frac{3}{2}} \left( \text{erfc}(\sqrt{ic-b}z) \Gamma\left(n+\frac{3}{2}\right) + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0306.01

$$\int \sqrt{z} e^{bz} \sin(cz) dz = -\frac{1}{2} i z^{3/2} \\ \left( \frac{\frac{1}{2} \sqrt{\pi} \left( \text{erf}(\sqrt{-(b+ic)z}) - 1 \right) - e^{(b+ic)z} \sqrt{-(b+ic)z}}{(-(b+ic)z)^{3/2}} + \frac{e^{(b-ic)z} \sqrt{-(b-ic)z} - \frac{1}{2} \sqrt{\pi} \left( \text{erf}(\sqrt{-(b-ic)z}) - 1 \right)}{(-(b-ic)z)^{3/2}} \right)$$

01.06.21.0307.01

$$\int z^{3/2} e^{bz} \sin(cz) dz = -\frac{1}{8} i z^{5/2} \left( \frac{2 e^{(b+ic)z} \sqrt{-(b+ic)z} (2bz + 2icz - 3) + 3 \sqrt{\pi} \text{erf}(\sqrt{-(b+ic)z}) - 3 \sqrt{\pi}}{(-(b+ic)z)^{5/2}} + \right. \\ \left. \frac{1}{(-(b-ic)z)^{5/2}} \left( e^{-icz} \left( 3 e^{icz} \sqrt{\pi} - 2 e^{bz} \sqrt{-(b-ic)z} (2bz - 2icz - 3) \right) - 3 \sqrt{\pi} \text{erf}(\sqrt{-(b-ic)z}) \right) \right)$$

01.06.21.0308.01

$$\int z^{5/2} e^{bz} \sin(cz) dz = -\frac{1}{2} i z^{7/2} \\ \left( \left( 2 e^{(b+ic)z} \sqrt{-(b+ic)z} (4b^2 z^2 - 4c^2 z^2 - 10icz + 2b(4icz - 5)z + 15) - 15 \sqrt{\pi} \text{erf}(\sqrt{-(b+ic)z}) + 15 \sqrt{\pi} \right) / \right. \\ \left. \left( 8(b+ic)^3 z^3 \sqrt{-(b+ic)z} \right) + \frac{1}{(-(b-ic)z)^{7/2}} \left( e^{(b-ic)z} (-(b-ic)z)^{5/2} - \right. \right. \\ \left. \left. \frac{5}{8} \left( e^{-icz} \left( 2 e^{bz} \sqrt{-(b-ic)z} (2bz - 2icz - 3) - 3 e^{icz} \sqrt{\pi} \right) + 3 \sqrt{\pi} \text{erf}(\sqrt{-(b-ic)z}) \right) \right) \right)$$

01.06.21.0309.01

$$\int z^{7/2} e^{bz} \sin(cz) dz =$$

$$-\frac{1}{2} i z^{9/2} \left( \frac{1}{(-b-i c) z^{9/2}} \left( e^{(b-i c) z} (-b-i c) z^{7/2} + \frac{7}{16} e^{-i c z} \left( 2 e^{b z} \sqrt{-(b-i c) z} (4 b^2 z^2 - 4 c^2 z^2 + 10 i c z + \right. \right. \right.$$

$$\left. \left. \left. 2 b(-4 i c z - 5) z + 15 \right) - 15 e^{i c z} \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-i c) z}\right) + 15 e^{i c z} \sqrt{\pi} \right) \right) - \frac{1}{(-b+i c) z^{9/2}}$$

$$\left( e^{(b+i c) z} (-b+i c) z^{7/2} + \frac{7}{16} \left( 2 e^{(b+i c) z} \sqrt{-(b+i c) z} (4 b^2 z^2 - 4 c^2 z^2 - 10 i c z + 2 b(4 i c z - 5) z + 15) - \right. \right.$$

$$\left. \left. \left. 15 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z}\right) + 15 \sqrt{\pi} \right) \right) \right)$$

01.06.21.0310.01

$$\int z^{9/2} e^{bz} \sin(cz) dz =$$

$$-\frac{1}{2} i z^{11/2} \left( \frac{1}{(-b-i c) z^{11/2}} \left( e^{(b-i c) z} (-b-i c) z^{9/2} + \frac{9}{2} \left( e^{(b-i c) z} (-b-i c) z^{7/2} + \frac{7}{16} e^{-i c z} \left( 2 e^{b z} \sqrt{-(b-i c) z} (4 b^2 z^2 - \right. \right. \right.$$

$$\left. \left. \left. 4 c^2 z^2 + 10 i c z + 2 b(-4 i c z - 5) z + 15 \right) - 15 e^{i c z} \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-i c) z}\right) + 15 e^{i c z} \sqrt{\pi} \right) \right) \right) -$$

$$\frac{1}{(-b+i c) z^{11/2}} \left( e^{(b+i c) z} (-b+i c) z^{9/2} + \frac{9}{2} \left( e^{(b+i c) z} (-b+i c) z^{7/2} + \frac{7}{16} \left( 2 e^{(b+i c) z} \sqrt{-(b+i c) z} \right. \right. \right.$$

$$\left. \left. \left. (4 b^2 z^2 - 4 c^2 z^2 - 10 i c z + 2 b(4 i c z - 5) z + 15) - 15 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z}\right) + 15 \sqrt{\pi} \right) \right) \right)$$

01.06.21.0311.01

$$\int \frac{e^{bz} \sin(cz)}{\sqrt{z}} dz = \frac{1}{2(b^2 + c^2)} \left( i \sqrt{\pi} \left( \sqrt{b-i c} (b+i c) \operatorname{erfi}\left(\sqrt{b-i c} \sqrt{z}\right) - (b-i c) \sqrt{b+i c} \operatorname{erfi}\left(\sqrt{b+i c} \sqrt{z}\right) \right) \right)$$

01.06.21.0312.01

$$\int \frac{e^{bz} \sin(cz)}{z^{3/2}} dz =$$

$$-\frac{1}{\sqrt{z}} \left( i \left( -\sqrt{\pi} \sqrt{-(b+i c) z} \operatorname{erf}\left(\sqrt{-(b+i c) z}\right) - e^{(b+i c) z} + e^{(b-i c) z} + \sqrt{\pi} \sqrt{-(b-i c) z} \operatorname{erf}\left(\sqrt{-(b-i c) z}\right) + \right. \right.$$

$$\left. \left. \sqrt{\pi} \sqrt{-(b+i c) z} - \sqrt{\pi} \sqrt{-(b-i c) z} \right) \right)$$

01.06.21.0313.01

$$\int \frac{e^{bz} \sin(cz)}{z^{5/2}} dz =$$

$$\frac{1}{3 z^{3/2}} \left( i \left( -2 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z}\right) (-b+i c) z^{3/2} + 2 \sqrt{\pi} (-b+i c) z^{3/2} - 2 \sqrt{\pi} (-b-i c) z^{3/2} + e^{(b+i c) z} - \right. \right.$$

$$\left. \left. e^{(b-i c) z} + 2(b+i c) e^{(b+i c) z} z - 2(b-i c) e^{(b-i c) z} z + 2 \sqrt{\pi} (-b-i c) z^{3/2} \operatorname{erf}\left(\sqrt{-(b-i c) z}\right) \right) \right)$$

01.06.21.0314.01

$$\int \frac{e^{bz} \sin(cz)}{z^{7/2}} dz = -\frac{1}{15 z^{5/2}} \left( i \left( -4 \sqrt{\pi} \operatorname{erf} \left( \sqrt{-(b+ic)z} \right) (-b+ic) z^{5/2} + 4 \sqrt{\pi} (-b+ic) z^{5/2} - 4 \sqrt{\pi} (-b-ic) z^{5/2} - 3 e^{(b+ic)z} + 3 e^{(b-ic)z} - 4 (b+ic)^2 e^{(b+ic)z} z^2 + 4 (b-ic)^2 e^{(b-ic)z} z^2 - 2 (b+ic) e^{(b+ic)z} z + 2 (b-ic) e^{(b-ic)z} z + 4 \sqrt{\pi} (-b-ic) z^{5/2} \operatorname{erf} \left( \sqrt{-(b-ic)z} \right) \right) \right)$$

01.06.21.0315.01

$$\int \frac{e^{bz} \sin(cz)}{z^{9/2}} dz = \frac{1}{105 z^{7/2}} \left( i \left( -8 \sqrt{\pi} \operatorname{erf} \left( \sqrt{-(b+ic)z} \right) (-b+ic) z^{7/2} + 8 \sqrt{\pi} (-b+ic) z^{7/2} - 8 \sqrt{\pi} (-b-ic) z^{7/2} + 15 e^{(b+ic)z} - 15 e^{(b-ic)z} + 8 (b+ic)^3 e^{(b+ic)z} z^3 - 8 (b-ic)^3 e^{(b-ic)z} z^3 + 4 (b+ic)^2 e^{(b+ic)z} z^2 - 4 (b-ic)^2 e^{(b-ic)z} z^2 + 6 (b+ic) e^{(b+ic)z} z - 6 (b-ic) e^{(b-ic)z} z + 8 \sqrt{\pi} (-b-ic) z^{7/2} \operatorname{erf} \left( \sqrt{-(b-ic)z} \right) \right) \right)$$

### Involving $z^{\alpha-1} e^{bz+e} \sin(cz)$

01.06.21.0316.01

$$\int z^{\alpha-1} e^{bz+e} \sin(cz) dz = -\frac{1}{2} i z^\alpha e^e \left( (-b-ic) z^{-\alpha} \Gamma(\alpha, -(b-ic)z) - (-b+ic) z^{-\alpha} \Gamma(\alpha, -(b+ic)z) \right)$$

01.06.21.0317.01

$$\int z^{\alpha-1} e^{ic+e} \sin(cz) dz = \frac{1}{2} i z^\alpha e^e \left( 2^{-\alpha} \Gamma(\alpha, -2ic) (-ic) z^{-\alpha} + \frac{1}{\alpha} \right)$$

01.06.21.0318.01

$$\int z^{\alpha-1} e^{-ic+e} \sin(cz) dz = -\frac{1}{2} i z^\alpha e^e \left( 2^{-\alpha} \Gamma(\alpha, 2ic) (ic) z^{-\alpha} + \frac{1}{\alpha} \right)$$

01.06.21.0319.01

$$\int z^n e^{bz+e} \sin(cz) dz = \frac{1}{2} i z^{n+1} e^e \left( (-ic-b) z^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}((ic+b)z)}{(-n-1)!} + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^k}{(n+1)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^k}{(n+1)_{k-n}} \right) - ((ic-b)z)^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}((-ic+b)z)}{(-n-1)!} + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^k}{(n+1)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0320.01

$$\int z^n e^{bz+e} \sin(cz) dz = -\frac{ie^e}{2} n! \left( (ic-b)^{-n-1} e^{(b-ic)z} \sum_{k=0}^n \frac{((ic-b)z)^k}{k!} - (-b-ic)^{-n-1} e^{(b+ic)z} \sum_{k=0}^n \frac{(-b+ic)z)^k}{k!} \right); n \in \mathbb{N}$$

01.06.21.0321.01

$$\int z e^{bz+e} \sin(cz) dz = \frac{e^{bz+e} \left( (zb^3 - b^2 + c^2 zb + c^2) \sin(cz) - c(zb^2 - 2b + c^2 z) \cos(cz) \right)}{(b^2 + c^2)^2}$$

01.06.21.0322.01

$$\int z e^{c z+e} \sin(c z) dz = \frac{e^{c z+e} ((1-c z) \cos(c z) + c z \sin(c z))}{2 c^2}$$

01.06.21.0323.01

$$\int z e^{e-c z} \sin(c z) dz = -\frac{e^{e-c z} ((c z+1) \cos(c z) + c z \sin(c z))}{2 c^2}$$

01.06.21.0324.01

$$\int z^2 e^{b z+e} \sin(c z) dz = \frac{1}{(b^2+c^2)^3} e^{b z+e} ((z^2 b^5 - 2 z b^4 + 2(c^2 z^2 + 1) b^3 + c^2(c^2 z^2 - 6) b + 2 c^4 z) \sin(c z) - c(z^2 b^4 - 4 z b^3 + 2(c^2 z^2 + 3) b^2 - 4 c^2 z b + c^2(c^2 z^2 - 2)) \cos(c z))$$

01.06.21.0325.01

$$\int z^2 e^{c z+e} \sin(c z) dz = -\frac{e^{c z+e} (c z-1) ((c z-1) \cos(c z) - (c z+1) \sin(c z))}{2 c^3}$$

01.06.21.0326.01

$$\int z^2 e^{e-c z} \sin(c z) dz = -\frac{e^{e-c z} (c z+1) ((c z+1) \cos(c z) + (c z-1) \sin(c z))}{2 c^3}$$

01.06.21.0327.01

$$\int z^3 e^{b z+e} \sin(c z) dz = \frac{1}{(b^2+c^2)^4} e^{b z+e} ((z^3 b^7 - 3 z^2 b^6 + 3 z(c^2 z^2 + 2) b^5 - 3(c^2 z^2 + 2) b^4 + 3 c^2 z(c^2 z^2 - 4) b^3 + 3 c^2(c^2 z^2 + 12) b^2 + c^4 z(c^2 z^2 - 18) b + 3 c^4(c^2 z^2 - 2)) \sin(c z) - c(z^3 b^6 - 6 z^2 b^5 + 3 z(c^2 z^2 + 6) b^4 - 12(c^2 z^2 + 2) b^3 + 3 c^2 z(c^2 z^2 + 4) b^2 - 6 c^2(c^2 z^2 - 4) b + c^4 z(c^2 z^2 - 6)) \cos(c z))$$

01.06.21.0328.01

$$\int z^4 e^{b z+e} \sin(c z) dz = \frac{1}{(b^2+c^2)^5} e^{b z+e} ((z^4 b^9 - 4 z^3 b^8 + 4 z^2(c^2 z^2 + 3) b^7 - 8 z(c^2 z^2 + 3) b^6 + 6(c^4 z^4 - 2 c^2 z^2 + 4) b^5 + 120 c^2 z b^4 + 4 c^2(c^4 z^4 - 15 c^2 z^2 - 60) b^3 + 8 c^4 z(c^2 z^2 + 15) b^2 + c^4(c^4 z^4 - 36 c^2 z^2 + 120) b + 4 c^6 z(c^2 z^2 - 6)) \sin(c z) - c(z^4 b^8 - 8 z^3 b^7 + 4 z^2(c^2 z^2 + 9) b^6 - 24 z(c^2 z^2 + 4) b^5 + 6(c^4 z^4 + 10 c^2 z^2 + 20) b^4 - 24 c^4 z^3 b^3 + 4 c^2(c^4 z^4 + 3 c^2 z^2 - 60) b^2 + (96 c^4 z - 8 c^6 z^3) b + c^4(c^4 z^4 - 12 c^2 z^2 + 24)) \cos(c z))$$

01.06.21.0329.01

$$\int z^5 e^{b z+e} \sin(c z) dz = \frac{1}{(b^2+c^2)^6} e^{b z+e} ((z^5 b^{11} - 5 z^4 b^{10} + 5 z^3(c^2 z^2 + 4) b^9 - 15 z^2(c^2 z^2 + 4) b^8 + 10 z(c^4 z^4 + 12) b^7 - 10(c^4 z^4 - 24 c^2 z^2 + 12) b^6 + 10 c^2 z(c^4 z^4 - 12 c^2 z^2 - 108) b^5 + 10 c^2(c^4 z^4 + 60 c^2 z^2 + 180) b^4 + 5 c^4 z(c^4 z^4 - 32 c^2 z^2 - 120) b^3 + 15 c^4(c^4 z^4 + 16 c^2 z^2 - 120) b^2 + c^6 z(c^4 z^4 - 60 c^2 z^2 + 600) b + 5 c^6(c^4 z^4 - 12 c^2 z^2 + 24)) \sin(c z) - c(z^5 b^{10} - 10 z^4 b^9 + 5 z^3(c^2 z^2 + 12) b^8 - 40 z^2(c^2 z^2 + 6) b^7 + 10 z(c^4 z^4 + 16 c^2 z^2 + 60) b^6 - 60(c^4 z^4 + 4 c^2 z^2 + 12) b^5 + 10 c^2 z(c^4 z^4 + 12 c^2 z^2 - 60) b^4 - 40 c^2(c^4 z^4 - 6 c^2 z^2 - 60) b^3 + 5 c^4 z(c^4 z^4 - 216) b^2 - 10 c^4(c^4 z^4 - 24 c^2 z^2 + 72) b + c^6 z(c^4 z^4 - 20 c^2 z^2 + 120)) \cos(c z))$$

01.06.21.0330.01

$$\int z^{-n} e^{bz+e} \sin(cz) dz = \frac{i e^{(-b-i c)z+e}}{2(b^2+c^2)(n-1)!} \left( -(i c-b)^n (b+i c) e^{2bz} (n-1)! \sum_{k=1}^{n-1} \frac{(i c-b)^{k-n} z^{k-n}}{(1-n)_k} - (-b-i c)^n (i c-b) e^{2(b+i c)z} (n-1)! \sum_{k=1}^{n-1} \frac{(-b-i c)^{k-n} z^{k-n}}{(1-n)_k} + (-1)^n e^{(b+i c)z} ((b+i c) \operatorname{Ei}((b-i c)z) (i c-b)^n + (-b-i c)^n \operatorname{Ei}((b+i c)z) (i c-b)) \right); n \in \mathbb{N}^+$$

01.06.21.0331.01

$$\int \frac{e^{e+bz} \sin(cz)}{z} dz = \frac{1}{2} i e^e (\operatorname{Ei}((b-i c)z) - \operatorname{Ei}((b+i c)z))$$

01.06.21.0332.01

$$\int \frac{e^{icze} \sin(cz)}{z} dz = -\frac{1}{2} i e^e (\operatorname{Ei}(2icze) - \log(z))$$

01.06.21.0333.01

$$\int \frac{e^{-icz} \sin(cz)}{z} dz = \frac{1}{2} i e^e (\operatorname{Ei}(-2icz) - \log(z))$$

01.06.21.0334.01

$$\int \frac{e^{bz+e} \sin(cz)}{z^2} dz = e^e \frac{i e^{(b-i c)z} (-1 + e^{2icze}) + (c+i b) z \operatorname{Ei}((b-i c)z) + (c-i b) z \operatorname{Ei}((b+i c)z)}{2z}$$

01.06.21.0335.01

$$\int \frac{e^{icze} \sin(cz)}{z^2} dz = e^e \frac{i (-1 + e^{2icze}) + 2c z \operatorname{Ei}(2icze)}{2z}$$

01.06.21.0336.01

$$\int \frac{e^{-icz} \sin(cz)}{z^2} dz = e^e \frac{i - i e^{-2icze} + 2c z \operatorname{Ei}(-2icze)}{2z}$$

01.06.21.0337.01

$$\int \frac{e^{bz+e} \sin(cz)}{z^3} dz = \frac{1}{4z^2} i e^e \left( -(b+i c)^2 \operatorname{Ei}((b+i c)z) z^2 + (b-i c)^2 \operatorname{Ei}((b-i c)z) z^2 + e^{(b-i c)z} (-bz + icz + e^{2icze} (bz + icz + 1) - 1) \right)$$

01.06.21.0338.01

$$\int \frac{e^{bz+e} \sin(cz)}{z^4} dz = -\frac{1}{12} i e^e \left( \operatorname{Ei}((b+i c)z) (b+i c)^3 + \frac{e^{(b-i c)z} ((b-i c)^2 z^2 + (b-i c)z + 2)}{z^3} - (b-i c)^3 \operatorname{Ei}((b-i c)z) - \frac{e^{(b+i c)z} ((b+i c)^2 z^2 + (b+i c)z + 2)}{z^3} \right)$$

01.06.21.0339.01

$$\int \frac{e^{bz+e} \sin(cz)}{z^5} dz = -\frac{1}{48} i e^e \left( \text{Ei}((b+ic)z) (b+ic)^4 + \frac{e^{(b-ic)z} ((b-ic)^3 z^3 + (b-ic)^2 z^2 + 2(b-ic)z + 6)}{z^4} - \frac{e^{(b+ic)z} ((b+ic)^3 z^3 + (b+ic)^2 z^2 + 2(b+ic)z + 6)}{z^4} \right)$$

01.06.21.0340.01

$$\int z^{n+\frac{1}{2}} e^{bz+e} \sin(cz) dz = \frac{1}{2} i z^{n+\frac{3}{2}} e^e \left( ((-ic-b)z)^{-n-\frac{3}{2}} \left( \text{erfc}(\sqrt{-ic-b}z) \Gamma\left(n+\frac{3}{2}\right) + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) - ((ic-b)z)^{-n-\frac{3}{2}} \left( \text{erfc}(\sqrt{ic-b}z) \Gamma\left(n+\frac{3}{2}\right) + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0341.01

$$\int \sqrt{z} e^{bz+e} \sin(cz) dz = -\frac{1}{2} i z^{3/2} e^e \left( \frac{\frac{1}{2} \sqrt{\pi} (\text{erf}(\sqrt{-(b+ic)z}) - 1) - e^{(b+ic)z} \sqrt{-(b+ic)z}}{(-(b+ic)z)^{3/2}} + \frac{e^{(b-ic)z} \sqrt{-(b-ic)z} - \frac{1}{2} \sqrt{\pi} (\text{erf}(\sqrt{-(b-ic)z}) - 1)}{(-(b-ic)z)^{3/2}} \right)$$

01.06.21.0342.01

$$\int z^{3/2} e^{bz+e} \sin(cz) dz = -\frac{1}{8} i z^{5/2} e^e \left( \frac{2 e^{(b+ic)z} \sqrt{-(b+ic)z} (2bz + 2icz - 3) + 3 \sqrt{\pi} \text{erf}(\sqrt{-(b+ic)z}) - 3 \sqrt{\pi}}{(-(b+ic)z)^{5/2}} + \frac{1}{(-(b-ic)z)^{5/2}} \left( e^{-icz} (3 e^{icz} \sqrt{\pi} - 2 e^{bz} \sqrt{-(b-ic)z} (2bz - 2icz - 3)) - 3 \sqrt{\pi} \text{erf}(\sqrt{-(b-ic)z}) \right) \right)$$

01.06.21.0343.01

$$\int z^{5/2} e^{bz+e} \sin(cz) dz = -\frac{1}{2} i z^{7/2} e^e \left( \left( 2 e^{(b+ic)z} \sqrt{-(b+ic)z} (4b^2 z^2 - 4c^2 z^2 - 10icz + 2b(4icz - 5)z + 15) - 15 \sqrt{\pi} \text{erf}(\sqrt{-(b+ic)z}) + 15 \sqrt{\pi} \right) / \left( 8(b+ic)^3 z^3 \sqrt{-(b+ic)z} \right) + \frac{1}{(-(b-ic)z)^{7/2}} \left( e^{(b-ic)z} (-(b-ic)z)^{5/2} - \frac{5}{8} \left( e^{-icz} (2 e^{bz} \sqrt{-(b-ic)z} (2bz - 2icz - 3) - 3 e^{icz} \sqrt{\pi}) + 3 \sqrt{\pi} \text{erf}(\sqrt{-(b-ic)z}) \right) \right) \right)$$



01.06.21.0344.01

$$\int z^{7/2} e^{b z+e} \sin(c z) dz =$$

$$-\frac{1}{2} i z^{9/2} e^e \left( \frac{1}{(-b-i c) z^{9/2}} \left( e^{(b-i c) z} (-b-i c) z^{7/2} + \frac{7}{16} e^{-i c z} \left( 2 e^{b z} \sqrt{-b-i c} z (4 b^2 z^2 - 4 c^2 z^2 + 10 i c z + 2 b(-4 i c z - 5) z + 15) - 15 e^{i c z} \sqrt{\pi} \operatorname{erf}\left(\sqrt{-b-i c} z\right) + 15 e^{i c z} \sqrt{\pi} \right) \right) - \frac{1}{(-b+i c) z^{9/2}} \left( e^{(b+i c) z} (-b+i c) z^{7/2} + \frac{7}{16} \left( 2 e^{(b+i c) z} \sqrt{-b+i c} z (4 b^2 z^2 - 4 c^2 z^2 - 10 i c z + 2 b(4 i c z - 5) z + 15) - 15 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-b+i c} z\right) + 15 \sqrt{\pi} \right) \right) \right)$$

01.06.21.0345.01

$$\int z^{9/2} e^{b z+e} \sin(c z) dz =$$

$$-\frac{1}{2} i z^{11/2} e^e \left( \frac{1}{(-b-i c) z^{11/2}} \left( e^{(b-i c) z} (-b-i c) z^{9/2} + \frac{9}{2} \left( e^{(b-i c) z} (-b-i c) z^{7/2} + \frac{7}{16} e^{-i c z} \left( 2 e^{b z} \sqrt{-b-i c} z (4 b^2 z^2 - 4 c^2 z^2 + 10 i c z + 2 b(-4 i c z - 5) z + 15) - 15 e^{i c z} \sqrt{\pi} \operatorname{erf}\left(\sqrt{-b-i c} z\right) + 15 e^{i c z} \sqrt{\pi} \right) \right) \right) - \frac{1}{(-b+i c) z^{11/2}} \left( e^{(b+i c) z} (-b+i c) z^{9/2} + \frac{9}{2} \left( e^{(b+i c) z} (-b+i c) z^{7/2} + \frac{7}{16} \left( 2 e^{(b+i c) z} \sqrt{-b+i c} z (4 b^2 z^2 - 4 c^2 z^2 - 10 i c z + 2 b(4 i c z - 5) z + 15) - 15 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-b+i c} z\right) + 15 \sqrt{\pi} \right) \right) \right) \right)$$

01.06.21.0346.01

$$\int \frac{e^{b z+e} \sin(c z)}{\sqrt{z}} dz = e^e \frac{1}{2(b^2 + c^2)} \left( i \sqrt{\pi} \left( \sqrt{b-i c} (b+i c) \operatorname{erfi}\left(\sqrt{b-i c} \sqrt{z}\right) - (b-i c) \sqrt{b+i c} \operatorname{erfi}\left(\sqrt{b+i c} \sqrt{z}\right) \right) \right)$$

01.06.21.0347.01

$$\int \frac{e^{e+b z} \sin(c z)}{z^{3/2}} dz =$$

$$-\frac{1}{\sqrt{z}} \left( i e^e \left( -\sqrt{\pi} \sqrt{-b+i c} z \operatorname{erf}\left(\sqrt{-b+i c} z\right) - e^{(b+i c) z} + e^{(b-i c) z} + \sqrt{\pi} \sqrt{-b-i c} z \operatorname{erf}\left(\sqrt{-b-i c} z\right) + \sqrt{\pi} \sqrt{-b+i c} z - \sqrt{\pi} \sqrt{-b-i c} z \right) \right)$$

01.06.21.0348.01

$$\int \frac{e^{b z+e} \sin(c z)}{z^{5/2}} dz =$$

$$\frac{1}{3 z^{3/2}} i e^e \left( -2 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-b+i c} z\right) (-b+i c) z^{3/2} + 2 \sqrt{\pi} (-b+i c) z^{3/2} - 2 \sqrt{\pi} (-b-i c) z^{3/2} + e^{(b+i c) z} - e^{(b-i c) z} + 2(b+i c) e^{(b+i c) z} z - 2(b-i c) e^{(b-i c) z} z + 2 \sqrt{\pi} (-b-i c) z^{3/2} \operatorname{erf}\left(\sqrt{-b-i c} z\right) \right)$$

01.06.21.0349.01

$$\int \frac{e^{bz+e} \sin(cz)}{z^{7/2}} dz = -\frac{1}{15 z^{5/2}} i e^e \left( -4 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+ic)z}\right) (-b+ic)z^{5/2} + 4 \sqrt{\pi} (-b+ic)z^{5/2} - 4 \sqrt{\pi} (-b-ic)z^{5/2} - 3 e^{(b+ic)z} + 3 e^{(b-ic)z} - 4 (b+ic)^2 e^{(b+ic)z} z^2 + 4 (b-ic)^2 e^{(b-ic)z} z^2 - 2 (b+ic) e^{(b+ic)z} z + 2 (b-ic) e^{(b-ic)z} z + 4 \sqrt{\pi} (-b-ic)z^{5/2} \operatorname{erf}\left(\sqrt{-(b-ic)z}\right) \right)$$

01.06.21.0350.01

$$\int \frac{e^{bz+e} \sin(cz)}{z^{9/2}} dz = \frac{1}{105 z^{7/2}} i e^e \left( -8 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+ic)z}\right) (-b+ic)z^{7/2} + 8 \sqrt{\pi} (-b+ic)z^{7/2} - 8 \sqrt{\pi} (-b-ic)z^{7/2} + 15 e^{(b+ic)z} - 15 e^{(b-ic)z} + 8 (b+ic)^3 e^{(b+ic)z} z^3 - 8 (b-ic)^3 e^{(b-ic)z} z^3 + 4 (b+ic)^2 e^{(b+ic)z} z^2 - 4 (b-ic)^2 e^{(b-ic)z} z^2 + 6 (b+ic) e^{(b+ic)z} z - 6 (b-ic) e^{(b-ic)z} z + 8 \sqrt{\pi} (-b-ic)z^{7/2} \operatorname{erf}\left(\sqrt{-(b-ic)z}\right) \right)$$

### Involving $z^{\alpha-1} e^{bz} \sin(cz+d)$

01.06.21.0351.01

$$\int z^{\alpha-1} e^{bz} \sin(cz+d) dz = \frac{1}{2} i e^{-id} z^\alpha \left( e^{2id} E_{1-\alpha}(-b+ic)z - E_{1-\alpha}(-b-ic)z \right)$$

01.06.21.0352.01

$$\int z^n e^{bz} \sin(d+cz) dz = \frac{1}{2} i e^{-id} z^{n+1} \left( e^{2id} ((-ic-b)z)^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}((ic+b)z)}{(-n-1)!} + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^k}{(n+1)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^k}{(n+1)_{k-n}} \right) - ((ic-b)z)^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}((-ic+b)z)}{(-n-1)!} + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^k}{(n+1)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0353.01

$$\int z^{n+\frac{1}{2}} e^{bz} \sin(cz+d) dz = \frac{1}{2} i e^{-id} z^{n+\frac{3}{2}} \left( e^{2id} ((-ic-b)z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}\left(\sqrt{(-ic-b)z}\right) \Gamma\left(n+\frac{3}{2}\right) + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) - ((ic-b)z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}\left(\sqrt{(ic-b)z}\right) \Gamma\left(n+\frac{3}{2}\right) + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0354.01

$$\int z e^{bz} \sin(cz+d) dz = \frac{e^{bz} \left( (-b^2 + (b^2 + c^2)zb + c^2) \sin(d+cz) - c \left( (b^2 + c^2)z - 2b \right) \cos(d+cz) \right)}{(b^2 + c^2)^2}$$

### Involving $z^{\alpha-1} e^{bz+e} \sin(cz+d)$

01.06.21.0355.01

$$\int z^{\alpha-1} e^{bz+e} \sin(cz+d) dz = \frac{1}{2} i e^{-id+e} z^{\alpha} (e^{2id} E_{1-\alpha}(-(b+ic)z) - E_{1-\alpha}(-(b-ic)z))$$

01.06.21.0356.01

$$\int z^n e^{bz+e} \sin(d+cz) dz = \frac{1}{2} i e^{e-id} z^{n+1} \left( e^{2id} ((-ic-b)z)^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}((ic+b)z)}{(-n-1)!} + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^k}{(n+1)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^k}{(n+1)_{k-n}} \right) - ((ic-b)z)^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}((-ic+b)z)}{(-n-1)!} + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^k}{(n+1)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0357.01

$$\int z^{n+\frac{1}{2}} e^{bz+e} \sin(cz+d) dz = \frac{1}{2} i e^{e-id} z^{n+\frac{3}{2}} \left( e^{2id} ((-ic-b)z)^{-n-\frac{3}{2}} \left( \text{erfc}(\sqrt{(-ic-b)z}) \Gamma\left(n+\frac{3}{2}\right) + e^{(ic+b)z} \sum_{k=0}^n \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(ic+b)z} \sum_{k=n+1}^{-1} \frac{((-ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) - ((ic-b)z)^{-n-\frac{3}{2}} \left( \text{erfc}(\sqrt{(ic-b)z}) \Gamma\left(n+\frac{3}{2}\right) + e^{(-ic+b)z} \sum_{k=0}^n \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{(-ic+b)z} \sum_{k=n+1}^{-1} \frac{((ic-b)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0358.01

$$\int z e^{bz+e} \sin(cz+d) dz = \frac{e^{bz+e} ((-b^2 + (b^2 + c^2)zb + c^2) \sin(d+cz) - c((b^2 + c^2)z - 2b) \cos(d+cz))}{(b^2 + c^2)^2}$$

### Involving $z^n e^{bz^r} \sin(cz)$

01.06.21.0359.01

$$\int z^n e^{bz^r} \sin(cz) dz = \frac{i}{4\sqrt{b}} e^{\frac{c^2}{4b}} \left( \sum_{k=0}^n 2^{k-n} b^{-n-\frac{1}{2}} (-ic)^{n-k} (ic+2bz)^{k+1} \left( -\frac{(ic+2bz)^2}{b} \right)^{\frac{1}{2}(-k-1)} \binom{n}{k} \Gamma\left(\frac{k+1}{2}, -\frac{(ic+2bz)^2}{4b}\right) - \sum_{k=0}^n 2^{k-n} b^{-n-\frac{1}{2}} (ic)^{n-k} \left( -\frac{(ic-2bz)^2}{b} \right)^{\frac{1}{2}(-k-1)} (-ic+2bz)^{k+1} \binom{n}{k} \Gamma\left(\frac{k+1}{2}, -\frac{(ic-2bz)^2}{4b}\right) \right); n \in \mathbb{N}$$

01.06.21.0360.01

$$\int z^n e^{b\sqrt{z}} \sin(cz) dz =$$

$$i 2^{-2(n+1)} (ic)^{-2n-2} e^{\frac{ib^2}{4c}} \left( e^{-\frac{ib^2}{2c} \sum_{k=0}^n \sum_{m=0}^k (-1)^{k-m} 4^k b^{-k-m+2n} (b-2ic\sqrt{z})^{k+m} \left( -\frac{i(b-2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-k-m-1)}} \right.$$

$$\left. \binom{k}{m} \binom{n}{k} \left( b(b-2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(k+m+1), -\frac{i(b-2ic\sqrt{z})^2}{4c} \right) - \right.$$

$$\left. \left. 2ic \sqrt{-\frac{i(b-2ic\sqrt{z})^2}{c}} \Gamma \left( \frac{1}{2}(k+m+2), -\frac{i(b-2ic\sqrt{z})^2}{4c} \right) \right) \right)$$

$$\sum_{k=0}^n \sum_{m=0}^k (-1)^{k-m} 4^k b^{-k-m+2n} (b+2ic\sqrt{z})^{k+m} \left( \frac{i(b+2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-k-m-1)} \binom{k}{m} \binom{n}{k}$$

$$\left( b(b+2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(k+m+1), \frac{i(b+2ic\sqrt{z})^2}{4c} \right) + \right.$$

$$\left. \left. 2 \sqrt{\frac{i(b+2ic\sqrt{z})^2}{c}} ci \Gamma \left( \frac{1}{2}(k+m+2), \frac{i(b+2ic\sqrt{z})^2}{4c} \right) \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+e} \sin(cz)$

01.06.21.0361.01

$$\int z^n e^{bz^2+e} \sin(cz) dz =$$

$$\frac{i}{4\sqrt{b}} e^{\frac{c^2}{4b}+e} \left( \sum_{k=0}^n 2^{k-n} b^{-n-\frac{1}{2}} (-ic)^{n-k} (ic+2bz)^{k+1} \left( -\frac{(ic+2bz)^2}{b} \right)^{\frac{1}{2}(-k-1)} \binom{n}{k} \Gamma \left( \frac{k+1}{2}, -\frac{(ic+2bz)^2}{4b} \right) - \right.$$

$$\left. \sum_{k=0}^n 2^{k-n} b^{-n-\frac{1}{2}} (ic)^{n-k} \left( -\frac{(ic-2bz)^2}{b} \right)^{\frac{1}{2}(-k-1)} (-ic+2bz)^{k+1} \binom{n}{k} \Gamma \left( \frac{k+1}{2}, -\frac{(ic-2bz)^2}{4b} \right) \right) /; n \in \mathbb{N}$$

01.06.21.0362.01

$$\int z^n e^{b\sqrt{z}+e} \sin(cz) dz =$$

$$i 2^{-2(n+1)} (ic)^{-2n-2} e^{\frac{ib^2}{4c}+e} \left( e^{-\frac{ib^2}{2c}} \sum_{k=0}^n \sum_{m=0}^k (-1)^{k-m} 4^k b^{-k-m+2n} (b-2ic\sqrt{z})^{k+m} \left( -\frac{i(b-2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-k-m-1)} \right.$$

$$\left. \binom{k}{m} \binom{n}{k} \left( b(b-2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(k+m+1), -\frac{i(b-2ic\sqrt{z})^2}{4c} \right) - \right.$$

$$\left. 2ic \sqrt{-\frac{i(b-2ic\sqrt{z})^2}{c}} \Gamma \left( \frac{1}{2}(k+m+2), -\frac{i(b-2ic\sqrt{z})^2}{4c} \right) \right) -$$

$$\sum_{k=0}^n \sum_{m=0}^k (-1)^{k-m} 4^k b^{-k-m+2n} (b+2ic\sqrt{z})^{k+m} \left( \frac{i(b+2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-k-m-1)} \binom{k}{m} \binom{n}{k}$$

$$\left( b(b+2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(k+m+1), \frac{i(b+2ic\sqrt{z})^2}{4c} \right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+2ic\sqrt{z})^2}{c}} ci \Gamma \left( \frac{1}{2}(k+m+2), \frac{i(b+2ic\sqrt{z})^2}{4c} \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+dz} \sin(cz)$

01.06.21.0363.01

$$\int z^n e^{bz^2+dz} \sin(cz) dz =$$

$$\frac{1}{4} i b^{-n-1} \left( e^{-\frac{(d+ic)^2}{4b}} \sum_{q=0}^n 2^{q-n} (-d-ic)^{n-q} (d+ic+2bz)^{q+1} \left( -\frac{(d+ic+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d+ic+2bz)^2}{4b} \right) - \right.$$

$$\left. e^{-\frac{(d-ic)^2}{4b}} \sum_{q=0}^n 2^{q-n} (ic-d)^{n-q} (d-ic+2bz)^{q+1} \left( -\frac{(d-ic+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d-ic+2bz)^2}{4b} \right) \right) /; n \in \mathbb{N}$$

01.06.21.0364.01

$$\int z^n e^{\sqrt{z} b+dz} \sin(c z) dz =$$

$$i 2^{-2n-2} \left( (d-i c)^{-2(n+1)} e^{\frac{b^2}{4ic-4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d-i c)\sqrt{z})^{h+k} \left( -\frac{(b+2(d-i c)\sqrt{z})^2}{d-i c} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2(d-i c)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d-i c)\sqrt{z})^2}{4(d-i c)} \right) \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d-i c)\sqrt{z})^2}{d-i c}} (d-i c) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d-i c)\sqrt{z})^2}{4(d-i c)} \right) \right) -$$

$$(d+i c)^{-2(n+1)} e^{-\frac{b^2}{4(d+i c)}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d+i c)\sqrt{z})^{h+k} \left( -\frac{(b+2(d+i c)\sqrt{z})^2}{d+i c} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2(d+i c)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d+i c)\sqrt{z})^2}{4(d+i c)} \right) \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d+i c)\sqrt{z})^2}{d+i c}} (d+i c) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d+i c)\sqrt{z})^2}{4(d+i c)} \right) \right) \Bigg) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+dz+e} \sin(c z)$

01.06.21.0365.01

$$\int z^n e^{bz^2+dz+e} \sin(c z) dz = \frac{i e^e}{4 \sqrt{b}}$$

$$\left( e^{-\frac{(d+i c)^2}{4b}} \sum_{q=0}^n 2^{q-n} b^{-n-\frac{1}{2}} (-d-i c)^{n-q} (d+i c+2bz)^{q+1} \left( -\frac{(d+i c+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d+i c+2bz)^2}{4b} \right) \right) -$$

$$e^{-\frac{(i c-d)^2}{4b}}$$

$$\sum_{q=0}^n 2^{q-n} b^{-n-\frac{1}{2}} (i c-d)^{n-q} (d-i c+2bz)^{q+1} \left( -\frac{(d-i c+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d-i c+2bz)^2}{4b} \right) \Bigg) /; n \in \mathbb{N}$$

01.06.21.0366.01

$$\int z^n e^{\sqrt{z} b+e+dz} \sin(cz) dz =$$

$$i 2^{-2(n+1)} e^e \left( (d-i c)^{-2(n+1)} e^{\frac{b^2}{4ic-4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d-i c)\sqrt{z})^{h+k} \left( \frac{(b+2(d-i c)\sqrt{z})^2}{ic-d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2(d-i c)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{(b+2(d-i c)\sqrt{z})^2}{4(ic-d)} \right) + \right.$$

$$\left. 2 \sqrt{\frac{(b+2(d-i c)\sqrt{z})^2}{ic-d}} (d-i c) \Gamma \left( \frac{1}{2}(h+k+2), \frac{(b+2(d-i c)\sqrt{z})^2}{4(ic-d)} \right) \right) -$$

$$(d+i c)^{-2(n+1)} e^{-\frac{b^2}{4(d+i c)}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d+i c)\sqrt{z})^{h+k} \left( -\frac{(b+2(d+i c)\sqrt{z})^2}{d+i c} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2(d+i c)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d+i c)\sqrt{z})^2}{4(d+i c)} \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d+i c)\sqrt{z})^2}{d+i c}} (d+i c) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d+i c)\sqrt{z})^2}{4(d+i c)} \right) \right) \Bigg| ; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r} \sin(fz+g)$

01.06.21.0367.01

$$\int z^n e^{bz^2} \sin(fz+g) dz =$$

$$\frac{1}{4} i b^{-n-1} \left( e^{\frac{f^2}{4b}+ig} \sum_{q=0}^n 2^{q-n} (-if)^{n-q} (if+2bz)^{q+1} \left( -\frac{(if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(if+2bz)^2}{4b} \right) - \right.$$

$$\left. e^{\frac{f^2}{4b}-ig} \sum_{q=0}^n 2^{q-n} (if)^{n-q} (-if+2bz)^{q+1} \left( -\frac{(-if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(-if+2bz)^2}{4b} \right) \right) \Bigg| ; n \in \mathbb{N}$$

01.06.21.0368.01

$$\int z^n e^{\sqrt{z} b} \sin(f z + g) dz =$$

$$i 2^{-2(n+1)} e^{-ig} \left( e^{-\frac{ib^2}{4f}} (-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b-2if\sqrt{z})^{h+k} \left( -\frac{i(b-2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right)$$

$$\binom{k}{h} \binom{n}{k} \left( b(b-2if\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{i(b-2if\sqrt{z})^2}{4f}\right) - \right.$$

$$\left. 2if \sqrt{-\frac{i(b-2if\sqrt{z})^2}{f}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{i(b-2if\sqrt{z})^2}{4f}\right) \right)$$

$$e^{\frac{ib^2}{4f}+2ig} (if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2if\sqrt{z})^{h+k} \left( \frac{i(b+2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( b(b+2if\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+2if\sqrt{z})^2}{4f}\right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+2if\sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+2if\sqrt{z})^2}{4f}\right) \right) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+e} \sin(fz+g)$

01.06.21.0369.01

$$\int z^n e^{bz^2+e} \sin(fz+g) dz =$$

$$\frac{1}{4} i b^{-n-1} \left( e^{\frac{f^2}{4b}+e+ig} \sum_{q=0}^n 2^{q-n} (-if)^{n-q} (if+2bz)^{q+1} \left( -\frac{(if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(if+2bz)^2}{4b}\right) - \right.$$

$$\left. e^{\frac{f^2}{4b}+e-ig} \sum_{q=0}^n 2^{q-n} (if)^{n-q} (-if+2bz)^{q+1} \left( -\frac{(-if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(-if+2bz)^2}{4b}\right) \right) /; n \in \mathbb{N}$$



01.06.21.0370.01

$$\int z^n e^{\sqrt{z}} b^{+e} \sin(f z + g) dz =$$

$$i 2^{-2(n+1)} e^{e-ig} \left( e^{-\frac{ib^2}{4f}} (-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b-2if\sqrt{z})^{h+k} \left( -\frac{i(b-2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right)$$

$$\binom{k}{h} \binom{n}{k} \left( b(b-2if\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(b-2if\sqrt{z})^2}{4f} \right) - \right.$$

$$\left. 2if \sqrt{-\frac{i(b-2if\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(b-2if\sqrt{z})^2}{4f} \right) \right)$$

$$e^{\frac{ib^2}{4f}+2ig} (if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2if\sqrt{z})^{h+k} \left( \frac{i(b+2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( b(b+2if\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{i(b+2if\sqrt{z})^2}{4f} \right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+2if\sqrt{z})^2}{f}} f i \Gamma \left( \frac{1}{2}(h+k+2), \frac{i(b+2if\sqrt{z})^2}{4f} \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+dz} \sin(fz+g)$

01.06.21.0371.01

$$\int z^n e^{bz^2+dz} \sin(fz+g) dz = \frac{1}{4} i b^{-n-1}$$

$$\left( e^{-\frac{(d+if)^2}{4b}+ig} \sum_{q=0}^n 2^{q-n} (-d-if)^{n-q} (d+if+2bz)^{q+1} \left( -\frac{(d+if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d+if+2bz)^2}{4b} \right) - \right.$$

$$e^{-\frac{(d-if)^2}{4b}-ig}$$

$$\left. \sum_{q=0}^n 2^{q-n} (if-d)^{n-q} (d-if+2bz)^{q+1} \left( -\frac{(d-if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d-if+2bz)^2}{4b} \right) \right) /; n \in \mathbb{N}$$

01.06.21.0372.01

$$\int z^n e^{\sqrt{z} b+dz} \sin(g+fz) dz =$$

$$i 2^{-2(n+1)} e^{-ig} \left( e^{-\frac{b^2}{4(d-if)}} (d-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d-if)\sqrt{z})^{h+k} \left( -\frac{(b+2(d-if)\sqrt{z})^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2(d-if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d-if)\sqrt{z})^2}{4(d-if)} \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d-if)\sqrt{z})^2}{d-if}} (d-if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) -$$

$$e^{2ig-\frac{b^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d+if)\sqrt{z})^{h+k} \left( -\frac{(b+2(d+if)\sqrt{z})^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2(d+if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d+if)\sqrt{z})^2}{4(d+if)} \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d+if)\sqrt{z})^2}{d+if}} (d+if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) \Bigg| ; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+dz+e} \sin(fz+g)$

01.06.21.0373.01

$$\int z^n e^{bz^2+dz+e} \sin(fz+g) dz = \frac{1}{4} i b^{-n-1}$$

$$\left( e^{-\frac{(d+if)^2}{4b}+e+ig} \sum_{q=0}^n 2^{q-n} (-d-if)^{n-q} (d+if+2bz)^{q+1} \left( -\frac{(d+if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d+if+2bz)^2}{4b} \right) - \right.$$

$$e^{-\frac{(d-if)^2}{4b}+e-ig}$$

$$\left. \sum_{q=0}^n 2^{q-n} (if-d)^{n-q} (d-if+2bz)^{q+1} \left( -\frac{(d-if+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d-if+2bz)^2}{4b} \right) \right) \Bigg| ; n \in \mathbb{N}$$

01.06.21.0374.01

$$\int z^n e^{\sqrt{z}} b+dz+e \sin(g+fz) dz =$$

$$i 2^{-2(n+1)} e^{e-ig} \left( e^{-\frac{b^2}{4(d-if)}} (d-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d-if)\sqrt{z})^{h+k} \left( -\frac{(b+2(d-if)\sqrt{z})^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \right)$$

$$\binom{k}{h} \binom{n}{k} \left( b(b+2(d-if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d-if)\sqrt{z})^2}{4(d-if)} \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d-if)\sqrt{z})^2}{d-if}} (d-if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) -$$

$$e^{2ig-\frac{b^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d+if)\sqrt{z})^{h+k} \left( -\frac{(b+2(d+if)\sqrt{z})^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( b(b+2(d+if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+2(d+if)\sqrt{z})^2}{4(d+if)} \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+2(d+if)\sqrt{z})^2}{d+if}} (d+if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz} \sin(cz^r)$

01.06.21.0375.01

$$\int z^n e^{bz} \sin(cz^2) dz = \frac{1}{4} i (ic)^{-n-1} e^{\frac{ib^2}{4c}} \sum_{k=0}^n 2^{k-n} (-b)^{n-k} (b+2icz)^{k+1} \left( \frac{i(b+2icz)^2}{c} \right)^{\frac{1}{2}(-k-1)} \binom{n}{k} \Gamma \left( \frac{k+1}{2}, \frac{i(b+2icz)^2}{4c} \right) -$$

$$\frac{1}{4} i (-ic)^{-n-1} e^{-\frac{ib^2}{4c}} \sum_{k=0}^n 2^{k-n} (-b)^{n-k} (b-2icz)^{k+1} \left( -\frac{i(b-2icz)^2}{c} \right)^{\frac{1}{2}(-k-1)} \binom{n}{k} \Gamma \left( \frac{k+1}{2}, -\frac{i(b-2icz)^2}{4c} \right) /; n \in \mathbb{N}$$

01.06.21.0376.01

$$\int z^n e^{bz} \sin(c \sqrt{z}) dz = i 4^{-n-1} b^{-2(n+1)} e^{\frac{c^2}{4b}}$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} \left( -\frac{(ic-2b\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-k-1)} (2b\sqrt{z}-ic)^{h+k} \binom{k}{h} \binom{n}{k} \left( ci(ic-2b\sqrt{z}) \right. \right. \\ \left. \left. \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(ic-2b\sqrt{z})^2}{4b} \right) + 2\sqrt{-\frac{(ic-2b\sqrt{z})^2}{b}} b \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(ic-2b\sqrt{z})^2}{4b} \right) \right) \right) - \\ \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z}b+ic)^{h+k} \left( -\frac{(2\sqrt{z}b+ic)^2}{b} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \\ \left( ci(2\sqrt{z}b+ic) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}b+ic)^2}{4b} \right) + \right. \\ \left. 2\sqrt{-\frac{(2\sqrt{z}b+ic)^2}{b}} b \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}b+ic)^2}{4b} \right) \right) \Bigg) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz+e} \sin(cz^r)$

01.06.21.0377.01

$$\int z^n e^{bz+e} \sin(cz^2) dz =$$

$$\frac{1}{4} i (ic)^{-n-1} e^{\frac{ib^2}{4c}+e} \sum_{k=0}^n 2^{k-n} (-b)^{n-k} (b+2icz)^{k+1} \left( \frac{i(b+2icz)^2}{c} \right)^{\frac{1}{2}(-k-1)} \binom{n}{k} \Gamma \left( \frac{k+1}{2}, \frac{i(b+2icz)^2}{4c} \right) - \\ \frac{1}{4} i (-ic)^{-n-1} e^{\frac{-ib^2}{4c}+e} \sum_{k=0}^n 2^{k-n} (-b)^{n-k} (b-2icz)^{k+1} \left( -\frac{i(b-2icz)^2}{c} \right)^{\frac{1}{2}(-k-1)} \binom{n}{k} \Gamma \left( \frac{k+1}{2}, -\frac{i(b-2icz)^2}{4c} \right) /; n \in \mathbb{N}$$

01.06.21.0378.01

$$\int z^n e^{bz+e} \sin(c\sqrt{z}) dz = i 4^{-n-1} b^{-2(n+1)} e^{\frac{c^2}{4b}+e}$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} \left( -\frac{(ic-2b\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-k-1)} (2b\sqrt{z}-ic)^{h+k} \binom{k}{h} \binom{n}{k} \left( ci(ic-2b\sqrt{z}) \right) \right. \\ \left. \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(ic-2b\sqrt{z})^2}{4b} \right) + 2 \sqrt{-\frac{(ic-2b\sqrt{z})^2}{b}} b \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(ic-2b\sqrt{z})^2}{4b} \right) \right) - \\ \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z}b+ic)^{h+k} \left( -\frac{(2\sqrt{z}b+ic)^2}{b} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \\ \left( ci(2\sqrt{z}b+ic) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}b+ic)^2}{4b} \right) + \right. \\ \left. 2 \sqrt{-\frac{(2\sqrt{z}b+ic)^2}{b}} b \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}b+ic)^2}{4b} \right) \right) \Bigg) /; n \in \mathbb{N}$$

**Involving  $z^{\alpha-1} e^{bz^r} \sin(cz^r)$**

01.06.21.0379.01

$$\int z^{\alpha-1} e^{bz^r} \sin(cz^r) dz = \frac{iz^\alpha}{2r} \left( ((-b-ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ic)z^r\right) - ((ic-b)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ic-b)z^r\right) \right)$$

01.06.21.0380.01

$$\int \frac{e^{bz^r} \sin(cz^r)}{z} dz = \frac{i(\text{Ei}((b-ic)z^r) - \text{Ei}((b+ic)z^r))}{2r}$$

01.06.21.0381.01

$$\int z^{2n} e^{b z^2} \sin(c z^2) dz =$$

$$\frac{1}{4} i z \left( \frac{1}{\sqrt{(-b-i c) z^2}} \left( (-b-i c)^{-n} \left( \operatorname{erfc}\left(\sqrt{(-b-i c) z^2}\right) \Gamma\left(n+\frac{1}{2}\right) + e^{(b+i c) z^2} \sum_{k=0}^{n-1} \frac{((-b-i c) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} - e^{(b+i c) z^2} \sum_{k=n}^{-1} \frac{((-b-i c) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} \right) \right) - \frac{1}{\sqrt{(i c-b) z^2}} \left( (i c-b)^{-n} \left( \operatorname{erfc}\left(\sqrt{(i c-b) z^2}\right) \Gamma\left(n+\frac{1}{2}\right) + e^{(b-i c) z^2} \sum_{k=0}^{n-1} \frac{((i c-b) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} - e^{(b-i c) z^2} \sum_{k=n}^{-1} \frac{((i c-b) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} \right) \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0382.01

$$\int z^{2n-1} e^{b z^2} \sin(c z^2) dz =$$

$$\frac{1}{4} i \left( (-b-i c)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}((b+i c) z^2)}{(-n)!} + e^{(b+i c) z^2} \sum_{k=0}^{n-1} \frac{((-b-i c) z^2)^k}{(n)_{k-n+1}} - e^{(b+i c) z^2} \sum_{k=n}^{-1} \frac{((-b-i c) z^2)^k}{(n)_{k-n+1}} \right) - (i c-b)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}((b-i c) z^2)}{(-n)!} + e^{(b-i c) z^2} \sum_{k=0}^{n-1} \frac{((i c-b) z^2)^k}{(n)_{k-n+1}} - e^{(b-i c) z^2} \sum_{k=n}^{-1} \frac{((i c-b) z^2)^k}{(n)_{k-n+1}} \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0383.01

$$\int z e^{b z^2} \sin(c z^2) dz = \frac{e^{b z^2} (b \sin(c z^2) - c \cos(c z^2))}{2(b^2 + c^2)}$$

01.06.21.0384.01

$$\int z^2 e^{b z^2} \sin(c z^2) dz = -\frac{1}{4} i z^3 \left( \frac{\frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right) - 1 \right) - e^{(b+i c) z^2} \sqrt{-(b+i c) z^2}}{(-b+i c) z^2}{}^{3/2}} + \frac{e^{(b-i c) z^2} \sqrt{-(b-i c) z^2} - \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right) - 1 \right)}{(-b-i c) z^2}{}^{3/2}} \right)$$

01.06.21.0385.01

$$\int z^3 e^{b z^2} \sin(c z^2) dz = \frac{e^{b z^2} ((z^2 b^3 - b^2 + c^2 z^2 b + c^2) \sin(c z^2) - c (b^2 z^2 + c^2 z^2 - 2 b) \cos(c z^2))}{2(b^2 + c^2)^2}$$

01.06.21.0386.01

$$\int z^4 e^{b z^2} \sin(c z^2) dz = -\frac{1}{16} i z^5 \left( \frac{1}{(-b+i c) z^2} \left( 2 e^{(b+i c) z^2} \sqrt{-(b+i c) z^2} (2 b z^2 + 2 c i z^2 - 3) + 3 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right) - 3 \sqrt{\pi} \right) + \frac{1}{(-b-i c) z^2} \left( -2 e^{(b-i c) z^2} \sqrt{-(b-i c) z^2} (2 b z^2 - 2 i c z^2 - 3) - 3 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right) + 3 \sqrt{\pi} \right) \right)$$

01.06.21.0387.01

$$\int z^5 e^{b z^2} \sin(c z^2) dz = \frac{1}{2(b^2 + c^2)^3} \left( e^{b z^2} \left( (z^4 b^5 - 2 z^2 b^4 + 2(c^2 z^4 + 1) b^3 + c^2(c^2 z^4 - 6) b + 2 c^4 z^2) \sin(c z^2) - c(b^4 z^4 - 4 b^3 z^2 - 4 b c^2 z^2 + c^2(c^2 z^4 - 2) + 2 b^2(c^2 z^4 + 3)) \cos(c z^2) \right) \right)$$

01.06.21.0388.01

$$\int \frac{e^{b z^2} \sin(c z^2)}{z} dz = \frac{1}{4} i \left( \operatorname{Ei}((b-i c) z^2) - \operatorname{Ei}((b+i c) z^2) \right)$$

01.06.21.0389.01

$$\int \frac{e^{b z^2} \sin(c z^2)}{z^2} dz = -\frac{1}{2 z} \left( i \left( -\sqrt{\pi} \sqrt{-(b+i c) z^2} \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right) - e^{(b+i c) z^2} + e^{(b-i c) z^2} + \sqrt{\pi} \sqrt{-(b-i c) z^2} \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right) + \sqrt{\pi} \sqrt{-(b+i c) z^2} - \sqrt{\pi} \sqrt{-(b-i c) z^2} \right) \right)$$

01.06.21.0390.01

$$\int \frac{e^{b z^2} \sin(c z^2)}{z^3} dz = \frac{(c-i b) \operatorname{Ei}((b+i c) z^2) z^2 + (c+i b) \operatorname{Ei}((b-i c) z^2) z^2 + e^{(b-i c) z^2} (-1 + e^{2 i c z^2}) i}{4 z^2}$$

01.06.21.0391.01

$$\int \frac{e^{b z^2} \sin(c z^2)}{z^4} dz = \frac{1}{6 z^3} \left( i \left( -2 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right) (-b+i c) z^2 \right)^{3/2} + 2 \sqrt{\pi} (-b+i c) z^2 \right)^{3/2} - 2 \sqrt{\pi} (-b-i c) z^2 \right)^{3/2} + e^{(b+i c) z^2} - e^{(b-i c) z^2} + 2(b+i c) e^{(b+i c) z^2} z^2 - 2(b-i c) e^{(b-i c) z^2} z^2 + 2 \sqrt{\pi} (-b-i c) z^2 \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right) \right)$$

01.06.21.0392.01

$$\int \frac{e^{b z^2} \sin(c z^2)}{z^5} dz = \frac{1}{8 z^4} \left( i \left( -(b+i c)^2 \operatorname{Ei}((b+i c) z^2) z^4 + (b-i c)^2 \operatorname{Ei}((b-i c) z^2) z^4 + e^{(b-i c) z^2} (-b z^2 + c i z^2 + e^{2 i c z^2} (b z^2 + c i z^2 + 1) - 1) \right) \right)$$

01.06.21.0393.01

$$\int z^n e^{b\sqrt{z}} \sin(c\sqrt{z}) dz =$$

$$i \left( (b+ic)^{-2(n+1)} \left( \frac{(-1)^{2n+1} \operatorname{Ei}((b+ic)\sqrt{z})}{(-2n-2)!} + e^{(b+ic)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((-b-ic)\sqrt{z})^k}{(2n+2)_{k-2n-1}} - e^{(b+ic)\sqrt{z}} \sum_{k=2n+2}^{-1} \frac{((-b-ic)\sqrt{z})^k}{(2n+2)_{k-2n-1}} \right) - \right.$$

$$\left. \frac{(-1)^{2n+1} \operatorname{Ei}((b-ic)\sqrt{z})}{(-2n-2)!} + e^{(b-ic)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((b-ic)\sqrt{z})^k}{(2n+2)_{k-2n-1}} - e^{(b-ic)\sqrt{z}} \sum_{k=2n+2}^{-1} \frac{((b-ic)\sqrt{z})^k}{(2n+2)_{k-2n-1}} \right) /; n \in \mathbb{Z}$$

01.06.21.0394.01

$$\int z e^{b\sqrt{z}} \sin(c\sqrt{z}) dz =$$

$$\frac{2}{(b^2+c^2)^4} e^{b\sqrt{z}} \left( (b^7 z^{3/2} - 3b^6 z + b c^4 (c^2 z - 18) \sqrt{z} + 3b^3 c^2 (c^2 z - 4) \sqrt{z} + 3b^5 (z c^2 + 2) \sqrt{z} + 3c^4 (c^2 z - 2) - \right.$$

$$3b^4 (z c^2 + 2) + 3b^2 c^2 (z c^2 + 12) \left. \right) \sin(c\sqrt{z}) - c (b^6 z^{3/2} - 6b^5 z + c^4 (c^2 z - 6) \sqrt{z} +$$

$$3b^2 c^2 (z c^2 + 4) \sqrt{z} + 3b^4 (z c^2 + 6) \sqrt{z} - 6b c^2 (c^2 z - 4) - 12b^3 (z c^2 + 2) \left. \right) \cos(c\sqrt{z})$$

01.06.21.0395.01

$$\int z^2 e^{b\sqrt{z}} \sin(c\sqrt{z}) dz = \frac{2}{(b^2+c^2)^6} e^{b\sqrt{z}}$$

$$\left( (20b(b^2+c^2)^3 (b^2-3c^2) z^{3/2} + b(b^2+c^2)^5 z^{5/2} - 5(b-c)(b+c)(b^2+c^2)^4 z^2 - 60(b^2+c^2)^2 (b^4-6c^2 b^2+c^4) z + \right.$$

$$120b(b^2+c^2)(b^4-10c^2 b^2+5c^4) \sqrt{z} - 120(b^6-15c^2 b^4+15c^4 b^2-c^6) \left. \right) \sin(c\sqrt{z}) -$$

$$c \left( 20(3b^2-c^2)(b^2+c^2)^3 z^{3/2} + (b^2+c^2)^5 z^{5/2} - 10b(b^2+c^2)^4 z^2 - 240b(b-c)(b+c)(b^2+c^2)^2 z + \right.$$

$$120(b^2+c^2)(5b^4-10c^2 b^2+c^4) \sqrt{z} - 240b(3b^4-10c^2 b^2+3c^4) \left. \right) \cos(c\sqrt{z})$$

01.06.21.0396.01

$$\int z^3 e^{b\sqrt{z}} \sin(c\sqrt{z}) dz = \frac{2}{(b^2+c^2)^8} e^{b\sqrt{z}}$$

$$\left( (840b(b^2+c^2)^3 (b^4-10c^2 b^2+5c^4) z^{3/2} + 42b(b^2+c^2)^5 (b^2-3c^2) z^{5/2} + b(b^2+c^2)^7 z^{7/2} - 7(b-c)(b+c)(b^2+c^2)^6 z^3 - \right.$$

$$210(b^2+c^2)^4 (b^4-6c^2 b^2+c^4) z^2 - 2520(b^2+c^2)^2 (b^6-15c^2 b^4+15c^4 b^2-c^6) z +$$

$$5040b(b^2+c^2)(b^6-21c^2 b^4+35c^4 b^2-7c^6) \sqrt{z} - 5040(b^8-28c^2 b^6+70c^4 b^4-28c^6 b^2+c^8) \left. \right) \sin(c\sqrt{z}) -$$

$$c \left( 840(b^2+c^2)^3 (5b^4-10c^2 b^2+c^4) z^{3/2} + 42(3b^2-c^2)(b^2+c^2)^5 z^{5/2} + (b^2+c^2)^7 z^{7/2} - 14b(b^2+c^2)^6 z^3 - \right.$$

$$840b(b-c)(b+c)(b^2+c^2)^4 z^2 - 5040b(b^2+c^2)^2 (3b^4-10c^2 b^2+3c^4) z +$$

$$5040(b^2+c^2)(7b^6-35c^2 b^4+21c^4 b^2-c^6) \sqrt{z} - 40320b(b^6-7c^2 b^4+7c^4 b^2-c^6) \left. \right) \cos(c\sqrt{z})$$



01.06.21.0397.01

$$\int z^4 e^{b\sqrt{z}} \sin(c\sqrt{z}) dz =$$

$$\frac{2}{(b^2 + c^2)^{10}} e^{b\sqrt{z}} \left( (60480 b (b^2 + c^2)^3 (b^6 - 21 c^2 b^4 + 35 c^4 b^2 - 7 c^6) z^{3/2} + 3024 b (b^2 + c^2)^5 (b^4 - 10 c^2 b^2 + 5 c^4) z^{5/2} + \right. \\ \left. 72 b (b^2 + c^2)^7 (b^2 - 3 c^2) z^{7/2} + b (b^2 + c^2)^9 z^{9/2} - 9 (b - c) (b + c) (b^2 + c^2)^8 z^4 - \right. \\ \left. 504 (b^2 + c^2)^6 (b^4 - 6 c^2 b^2 + c^4) z^3 - 15120 (b^2 + c^2)^4 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) z^2 - 181440 (b^2 + c^2)^2 \right. \\ \left. (b^8 - 28 c^2 b^6 + 70 c^4 b^4 - 28 c^6 b^2 + c^8) z + 362880 b (b^2 + c^2) (b^2 - 3 c^2) (b^6 - 33 c^2 b^4 + 27 c^4 b^2 - 3 c^6) \sqrt{z} - \right. \\ \left. 362880 (b^{10} - 45 c^2 b^8 + 210 c^4 b^6 - 210 c^6 b^4 + 45 c^8 b^2 - c^{10}) \right) \sin(c\sqrt{z}) - \\ c \left( 60480 (b^2 + c^2)^3 (7 b^6 - 35 c^2 b^4 + 21 c^4 b^2 - c^6) z^{3/2} + 3024 (b^2 + c^2)^5 (5 b^4 - 10 c^2 b^2 + c^4) z^{5/2} + \right. \\ \left. 72 (3 b^2 - c^2) (b^2 + c^2)^7 z^{7/2} + (b^2 + c^2)^9 z^{9/2} - 18 b (b^2 + c^2)^8 z^4 - 2016 b (b - c) (b + c) (b^2 + c^2)^6 z^3 - \right. \\ \left. 30240 b (b^2 + c^2)^4 (3 b^4 - 10 c^2 b^2 + 3 c^4) z^2 - 1451520 b (b^2 + c^2)^2 (b^6 - 7 c^2 b^4 + 7 c^4 b^2 - c^6) z + \right. \\ \left. 362880 (9 b^{10} - 75 c^2 b^8 + 42 c^4 b^6 + 90 c^6 b^4 - 35 c^8 b^2 + c^{10}) \sqrt{z} - \right. \\ \left. 725760 b (5 b^4 - 10 c^2 b^2 + c^4) (b^4 - 10 c^2 b^2 + 5 c^4) \right) \cos(c\sqrt{z}) \Bigg)$$

01.06.21.0398.01

$$\int z^5 e^{b\sqrt{z}} \sin(c\sqrt{z}) dz = \frac{1}{(b^2 + c^2)^{12}}$$

$$\begin{aligned} & \left( 2 e^{b\sqrt{z}} \left( (330 b^{15} (z^4 c^8 - 8 z^3 c^6 - 1056 z^2 c^4 - 16128 z c^2 + 20160) z^{3/2} + 165 b^{17} (z^3 c^6 + 6 z^2 c^4 - 144 z c^2 + 2016) z^{5/2} + \right. \right. \\ & 55 b^{19} (z^2 c^4 + 12 z c^2 + 144) z^{7/2} + 11 b^{21} (z c^2 + 10) z^{9/2} + b^{23} z^{11/2} - 11 b^{22} z^5 - 99 b^{20} (z c^2 + 10) z^4 - \\ & 55 b^{18} (7 z^2 c^4 + 36 z c^2 + 1008) z^3 - 165 b^{16} (5 z^3 c^6 - 114 z^2 c^4 - 3024 z c^2 + 10080) z^2 - \\ & 990 b^{14} (z^4 c^8 - 104 z^3 c^6 - 3360 z^2 c^4 - 40320 z c^2 + 20160) z + \\ & 462 b^{13} (z^5 c^{10} - 30 z^4 c^8 - 2400 z^3 c^6 - 43200 z^2 c^4 - 475200 z c^2 + 86400) \sqrt{z} + \\ & 462 b^{11} c^2 (z^5 c^{10} - 60 z^4 c^8 - 3600 z^3 c^6 - 23040 z^2 c^4 + 302400 z c^2 - 4665600) \sqrt{z} + \\ & 330 b^9 c^4 (z^5 c^{10} - 98 z^4 c^8 - 3696 z^3 c^6 + 110880 z^2 c^4 + 3769920 z c^2 + 33264000) \sqrt{z} + \\ & 165 b^7 c^6 (z^5 c^{10} - 144 z^4 c^8 - 1344 z^3 c^6 + 354816 z^2 c^4 + 3991680 z c^2 - 31933440) \sqrt{z} + \\ & 55 b^5 c^8 (z^5 c^{10} - 198 z^4 c^8 + 5184 z^3 c^6 + 508032 z^2 c^4 - 11975040 z c^2 - 215550720) \sqrt{z} + \\ & 11 b^3 c^{10} (z^5 c^{10} - 260 z^4 c^8 + 18000 z^3 c^6 - 34473600 z c^2 + 558835200) \sqrt{z} + \\ & b c^{12} (z^5 c^{10} - 330 z^4 c^8 + 39600 z^3 c^6 - 2328480 z^2 c^4 + 59875200 z c^2 - 439084800) \sqrt{z} + \\ & 990 b^8 c^4 (z^5 c^{10} + 238 z^4 c^8 - 3696 z^3 c^6 - 332640 z^2 c^4 - 3326400 z c^2 - 19958400) + \\ & 462 b^{10} c^2 (z^5 c^{10} + 660 z^4 c^8 + 7920 z^3 c^6 - 316800 z^2 c^4 - 5227200 z c^2 + 5702400) + \\ & 99 b^2 c^{10} (z^5 c^{10} - 20 z^4 c^8 - 5040 z^3 c^6 + 403200 z^2 c^4 - 8668800 z c^2 + 26611200) + \\ & 11 c^{12} (z^5 c^{10} - 90 z^4 c^8 + 5040 z^3 c^6 - 151200 z^2 c^4 + 1814400 z c^2 - 3628800) - \\ & 462 b^{12} (z^5 c^{10} - 510 z^4 c^8 - 13920 z^3 c^6 - 129600 z^2 c^4 - 1857600 z c^2 + 86400) + \\ & 165 b^6 c^6 (5 z^5 c^{10} + 624 z^4 c^8 - 38976 z^3 c^6 - 887040 z^2 c^4 + 19958400 z c^2 + 223534080) + \\ & 55 b^4 c^8 (7 z^5 c^{10} + 342 z^4 c^8 - 60480 z^3 c^6 + 1088640 z^2 c^4 + 43908480 z c^2 - 359251200) \Big) \sin(c\sqrt{z}) - \\ & c (330 b^{14} (z^4 c^8 + 72 z^3 c^6 + 864 z^2 c^4 + 181440) z^{3/2} + 165 b^{16} (z^3 c^6 + 66 z^2 c^4 + 1200 z c^2 + 14112) z^{5/2} + \\ & 55 b^{18} (z^2 c^4 + 52 z c^2 + 720) z^{7/2} + 11 b^{20} (z c^2 + 30) z^{9/2} + b^{22} z^{11/2} - 22 b^{21} z^5 - 220 b^{19} (z c^2 + 18) z^4 - \\ & 990 b^{17} (z^2 c^4 + 28 z c^2 + 336) z^3 - 2640 b^{15} (z^3 c^6 + 30 z^2 c^4 + 336 z c^2 + 5040) z^2 - \\ & 4620 b^{13} (z^4 c^8 + 24 z^3 c^6 - 288 z^2 c^4 - 8640 z c^2 + 43200) z + \\ & 165 b^6 c^6 (z^5 c^{10} + 16 z^4 c^8 - 6720 z^3 c^6 + 64512 z^2 c^4 + 7539840 z c^2 + 31933440) \sqrt{z} + \\ & 330 b^8 c^4 (z^5 c^{10} + 42 z^4 c^8 - 5040 z^3 c^6 - 110880 z^2 c^4 + 1995840 z c^2 + 35925120) \sqrt{z} + \\ & 462 b^{10} c^2 (z^5 c^{10} + 60 z^4 c^8 - 2640 z^3 c^6 - 126720 z^2 c^4 - 1425600 z c^2 - 13305600) \sqrt{z} + \\ & 462 b^{12} (z^5 c^{10} + 70 z^4 c^8 - 480 z^3 c^6 - 60480 z^2 c^4 - 820800 z c^2 + 950400) \sqrt{z} + \\ & 55 b^4 c^8 (z^5 c^{10} - 18 z^4 c^8 - 6336 z^3 c^6 + 362880 z^2 c^4 + 2540160 z c^2 - 199584000) \sqrt{z} + \\ & 11 b^2 c^{10} (z^5 c^{10} - 60 z^4 c^8 - 2160 z^3 c^6 + 483840 z^2 c^4 - 19958400 z c^2 + 195955200) \sqrt{z} + \\ & c^{12} (z^5 c^{10} - 110 z^4 c^8 + 7920 z^3 c^6 - 332640 z^2 c^4 + 6652800 z c^2 - 39916800) \sqrt{z} - \\ & 5544 b^{11} (z^5 c^{10} + 10 z^4 c^8 - 1440 z^3 c^6 - 36000 z^2 c^4 - 360000 z c^2 + 86400) - \\ & 4620 b^9 c^2 (z^5 c^{10} - 12 z^4 c^8 - 2640 z^3 c^6 - 31680 z^2 c^4 + 95040 z c^2 - 1900800) - \\ & 2640 b^7 c^4 (z^5 c^{10} - 42 z^4 c^8 - 3024 z^3 c^6 + 55440 z^2 c^4 + 1995840 z c^2 + 11975040) - \\ & 990 b^5 c^6 (z^5 c^{10} - 80 z^4 c^8 - 1344 z^3 c^6 + 201600 z^2 c^4 + 443520 z c^2 - 31933440) - \\ & 220 b^3 c^8 (z^5 c^{10} - 126 z^4 c^8 + 4032 z^3 c^6 + 181440 z^2 c^4 - 9072000 z c^2 + 39916800) - \\ & 22 b c^{10} (z^5 c^{10} - 180 z^4 c^8 + 15120 z^3 c^6 - 604800 z^2 c^4 + 9072000 z c^2 - 21772800) \Big) \cos(c\sqrt{z}) \Big) \end{aligned}$$

$$\int \frac{e^{b\sqrt{z}} \sin(c\sqrt{z})}{z} dz = i \left( \text{Ei}((b-ic)\sqrt{z}) - \text{Ei}((b+ic)\sqrt{z}) \right)$$

$$\int \frac{e^{b\sqrt{z}} \sin(c\sqrt{z})}{z^2} dz = \frac{1}{2z} \left( i \left( -z \text{Ei}((b+ic)\sqrt{z}) (b+ic)^2 + e^{(b-ic)\sqrt{z}} \left( -\sqrt{z} b + e^{2ic\sqrt{z}} (\sqrt{z} b + ic\sqrt{z} + 1) + ic\sqrt{z} - 1 \right) + (b-ic)^2 z \text{Ei}((b-ic)\sqrt{z}) \right) \right)$$

$$\int \frac{e^{b\sqrt{z}} \sin(c\sqrt{z})}{z^3} dz = -\frac{1}{24} i \left( \text{Ei}((b+ic)\sqrt{z}) (b+ic)^4 + \frac{e^{(b-ic)\sqrt{z}} \left( (b-ic)^3 z^{3/2} + (b-ic)^2 z + 2(b-ic)\sqrt{z} + 6 \right)}{z^2} - (b-ic)^4 \text{Ei}((b-ic)\sqrt{z}) - \frac{e^{(b+ic)\sqrt{z}} \left( (b+ic)^3 z^{3/2} + (b+ic)^2 z + 2(b+ic)\sqrt{z} + 6 \right)}{z^2} \right)$$

$$\int \frac{e^{b\sqrt{z}} \sin(c\sqrt{z})}{z^4} dz = -\frac{1}{720} i \left( \text{Ei}((b+ic)\sqrt{z}) (b+ic)^6 - \frac{1}{z^3} \left( e^{(b+ic)\sqrt{z}} \left( 2(b+ic)^3 z^{3/2} + (b+ic)^5 z^{5/2} + (b+ic)^4 z^2 + 6(b+ic)^2 z + 24(b+ic)\sqrt{z} + 120 \right) \right) + \frac{1}{z^3} \left( e^{(b-ic)\sqrt{z}} \left( 2(b-ic)^3 z^{3/2} + (b-ic)^5 z^{5/2} + (b-ic)^4 z^2 + 6(b-ic)^2 z + 24(b-ic)\sqrt{z} + 120 \right) \right) - (b-ic)^6 \text{Ei}((b-ic)\sqrt{z}) \right)$$

$$\int \frac{e^{b\sqrt{z}} \sin(c\sqrt{z})}{z^5} dz = -\frac{1}{40320} \left( i \left( \text{Ei}((b+ic)\sqrt{z}) (b+ic)^8 - \frac{1}{z^4} \left( e^{(b+ic)\sqrt{z}} \left( 24(b+ic)^3 z^{3/2} + 2(b+ic)^5 z^{5/2} + (b+ic)^7 z^{7/2} + (b+ic)^6 z^3 + 6(b+ic)^4 z^2 + 120(b+ic)^2 z + 720(b+ic)\sqrt{z} + 5040 \right) \right) + \frac{1}{z^4} \left( e^{(b-ic)\sqrt{z}} \left( 24(b-ic)^3 z^{3/2} + 2(b-ic)^5 z^{5/2} + (b-ic)^7 z^{7/2} + (b-ic)^6 z^3 + 6(b-ic)^4 z^2 + 120(b-ic)^2 z + 720(b-ic)\sqrt{z} + 5040 \right) \right) - (b-ic)^8 \text{Ei}((b-ic)\sqrt{z}) \right) \right)$$

Involving  $z^{\alpha-1} e^{bz^r} \sin(cz^r)$

01.06.21.0404.01

$$\int z^{\alpha-1} e^{b z^r + e} \sin(c z^r) dz = \frac{i z^\alpha}{2r} e^e \left( ((-b - ic) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b - ic) z^r\right) - ((ic - b) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ic - b) z^r\right) \right)$$

01.06.21.0405.01

$$\int \frac{e^{b z^r + e} \sin(c z^r)}{z} dz = \frac{i e^e (\text{Ei}((b - ic) z^r) - \text{Ei}((b + ic) z^r))}{2r}$$

01.06.21.0406.01

$$\int z^{2n} e^{b z^2 + e} \sin(c z^2) dz =$$

$$\frac{1}{4} i z e^e \left( \frac{1}{\sqrt{(-b - ic) z^2}} \left( (-b - ic)^{-n} \left( \text{erfc}\left(\sqrt{(-b - ic) z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{(b+ic) z^2} \sum_{k=0}^{n-1} \frac{((-b - ic) z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{(b+ic) z^2} \sum_{k=n}^{-1} \frac{((-b - ic) z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) \right) - \frac{1}{\sqrt{(ic - b) z^2}} \left( (ic - b)^{-n} \left( \text{erfc}\left(\sqrt{(ic - b) z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{(b-ic) z^2} \sum_{k=0}^{n-1} \frac{((ic - b) z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{(b-ic) z^2} \sum_{k=n}^{-1} \frac{((ic - b) z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0407.01

$$\int z^{2n-1} e^{b z^2 + e} \sin(c z^2) dz =$$

$$\frac{1}{4} i e^e \left( (-b - ic)^{-n} \left( \frac{(-1)^{n-1} \text{Ei}((b + ic) z^2)}{(-n)!} + e^{(b+ic) z^2} \sum_{k=0}^{n-1} \frac{((-b - ic) z^2)^k}{(n)_{k-n+1}} - e^{(b+ic) z^2} \sum_{k=n}^{-1} \frac{((-b - ic) z^2)^k}{(n)_{k-n+1}} \right) - (ic - b)^{-n} \left( \frac{(-1)^{n-1} \text{Ei}((b - ic) z^2)}{(-n)!} + e^{(b-ic) z^2} \sum_{k=0}^{n-1} \frac{((ic - b) z^2)^k}{(n)_{k-n+1}} - e^{(b-ic) z^2} \sum_{k=n}^{-1} \frac{((ic - b) z^2)^k}{(n)_{k-n+1}} \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0408.01

$$\int z e^{b z^2 + e} \sin(c z^2) dz = \frac{e^{b z^2 + e} (b \sin(c z^2) - c \cos(c z^2))}{2(b^2 + c^2)}$$

01.06.21.0409.01

$$\int z^2 e^{b z^2 + e} \sin(c z^2) dz = -\frac{1}{4} i z^3 e^e \left( \frac{\frac{1}{2} \sqrt{\pi} \left( \text{erf}\left(\sqrt{-(b + ic) z^2}\right) - 1 \right) - e^{(b+ic) z^2} \sqrt{-(b + ic) z^2}}{(-(b + ic) z^2)^{3/2}} + \frac{e^{(b-ic) z^2} \sqrt{-(b - ic) z^2} - \frac{1}{2} \sqrt{\pi} \left( \text{erf}\left(\sqrt{-(b - ic) z^2}\right) - 1 \right)}{(-(b - ic) z^2)^{3/2}} \right)$$

01.06.21.0410.01

$$\int z^3 e^{b z^2 + e} \sin(c z^2) dz = \frac{e^{b z^2 + e} ((z^2 b^3 - b^2 + c^2 z^2 b + c^2) \sin(c z^2) - c (b^2 z^2 + c^2 z^2 - 2b) \cos(c z^2))}{2(b^2 + c^2)^2}$$

01.06.21.0411.01

$$\int z^4 e^{b z^2+e} \sin(c z^2) dz = -\frac{1}{16} i z^5 e^e \left( \frac{1}{(-b+i c) z^2} \left( 2 e^{(b+i c) z^2} \sqrt{-(b+i c) z^2} (2 b z^2+2 c i z^2-3)+3 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right)-3 \sqrt{\pi}\right) + \frac{1}{(-b-i c) z^2} \left( -2 e^{(b-i c) z^2} \sqrt{-(b-i c) z^2} (2 b z^2-2 i c z^2-3)-3 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right)+3 \sqrt{\pi}\right) \right)$$

01.06.21.0412.01

$$\int z^5 e^{b z^2+e} \sin(c z^2) dz = \frac{1}{2(b^2+c^2)^3} e^{b z^2+e} ((z^4 b^5-2 z^2 b^4+2(c^2 z^4+1) b^3+c^2(c^2 z^4-6) b+2 c^4 z^2) \sin(c z^2)-c(b^4 z^4-4 b^3 z^2-4 b c^2 z^2+c^2(c^2 z^4-2)+2 b^2(c^2 z^4+3)) \cos(c z^2))$$

01.06.21.0413.01

$$\int \frac{e^{b z^2+e} \sin(c z^2)}{z} dz = \frac{1}{4} i e^e (\operatorname{Ei}((b-i c) z^2)-\operatorname{Ei}((b+i c) z^2))$$

01.06.21.0414.01

$$\int \frac{e^{b z^2+e} \sin(c z^2)}{z^2} dz = -\frac{1}{2 z} i e^e \left( -\sqrt{\pi} \sqrt{-(b+i c) z^2} \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right)-e^{(b+i c) z^2} + e^{(b-i c) z^2} + \sqrt{\pi} \sqrt{-(b-i c) z^2} \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right) + \sqrt{\pi} \sqrt{-(b+i c) z^2} - \sqrt{\pi} \sqrt{-(b-i c) z^2} \right)$$

01.06.21.0415.01

$$\int \frac{e^{b z^2+e} \sin(c z^2)}{z^3} dz = e^e \frac{(c-i b) \operatorname{Ei}((b+i c) z^2) z^2+(c+i b) \operatorname{Ei}((b-i c) z^2) z^2+e^{(b-i c) z^2}(-1+e^{2 i c z^2}) i}{4 z^2}$$

01.06.21.0416.01

$$\int \frac{e^{b z^2+e} \sin(c z^2)}{z^4} dz = \frac{1}{6 z^3} i e^e \left( -2 \sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+i c) z^2}\right) (-b+i c) z^2)^{3/2}+2 \sqrt{\pi} (-b+i c) z^2)^{3/2}-2 \sqrt{\pi} (-b-i c) z^2)^{3/2}+e^{(b+i c) z^2}-e^{(b-i c) z^2}+2(b+i c) e^{(b+i c) z^2} z^2-2(b-i c) e^{(b-i c) z^2} z^2+2 \sqrt{\pi} (-b-i c) z^2)^{3/2} \operatorname{erf}\left(\sqrt{-(b-i c) z^2}\right) \right)$$

01.06.21.0417.01

$$\int \frac{e^{b z^2+e} \sin(c z^2)}{z^5} dz = \frac{1}{8 z^4} \left( i e^e \left( -(b+i c)^2 \operatorname{Ei}((b+i c) z^2) z^4+(b-i c)^2 \operatorname{Ei}((b-i c) z^2) z^4+e^{(b-i c) z^2} \left( -b z^2+c i z^2+e^{2 i c z^2} (b z^2+c i z^2+1)-1 \right) \right) \right)$$

01.06.21.0418.01

$$\int z^n e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz =$$

$$i e^e \left( (b+ic)^{-2(n+1)} \left( \frac{(-1)^{2n+1} \operatorname{Ei}((b+ic)\sqrt{z})}{(-2n-2)!} + e^{(b+ic)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((-b-ic)\sqrt{z})^k}{(2n+2)_{k-2n-1}} - e^{(b+ic)\sqrt{z}} \sum_{k=2n+2}^{-1} \frac{((-b-ic)\sqrt{z})^k}{(2n+2)_{k-2n-1}} \right) \right. \\ \left. (b-ic)^{-2(n+1)} \left( \frac{(-1)^{2n+1} \operatorname{Ei}((b-ic)\sqrt{z})}{(-2n-2)!} + e^{(b-ic)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((ic-b)\sqrt{z})^k}{(2n+2)_{k-2n-1}} - e^{(b-ic)\sqrt{z}} \sum_{k=2n+2}^{-1} \frac{((ic-b)\sqrt{z})^k}{(2n+2)_{k-2n-1}} \right) \right) /; n \in \mathbb{Z}$$

01.06.21.0419.01

$$\int z e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz =$$

$$\frac{2}{(b^2+c^2)^4} e^{b\sqrt{z}+e} \left( (b^7 z^{3/2} - 3b^6 z + b^4 c^2 (c^2 z - 18) \sqrt{z} + 3b^3 c^2 (c^2 z - 4) \sqrt{z} + 3b^5 (z c^2 + 2) \sqrt{z} + \right. \\ \left. 3c^4 (c^2 z - 2) - 3b^4 (z c^2 + 2) + 3b^2 c^2 (z c^2 + 12) \right) \sin(c\sqrt{z}) - c (b^6 z^{3/2} - 6b^5 z + c^4 (c^2 z - 6) \sqrt{z} + \\ \left. 3b^2 c^2 (z c^2 + 4) \sqrt{z} + 3b^4 (z c^2 + 6) \sqrt{z} - 6b c^2 (c^2 z - 4) - 12b^3 (z c^2 + 2) \right) \cos(c\sqrt{z})$$

01.06.21.0420.01

$$\int z^2 e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz = \frac{2}{(b^2+c^2)^6} e^{b\sqrt{z}+e}$$

$$\left( (20b(b^2+c^2)^3 (b^2-3c^2) z^{3/2} + b(b^2+c^2)^5 z^{5/2} - 5(b-c)(b+c)(b^2+c^2)^4 z^2 - 60(b^2+c^2)^2 (b^4-6c^2 b^2+c^4) z + \right. \\ \left. 120b(b^2+c^2)(b^4-10c^2 b^2+5c^4) \sqrt{z} - 120(b^6-15c^2 b^4+15c^4 b^2-c^6) \right) \sin(c\sqrt{z}) - \\ c \left( 20(3b^2-c^2)(b^2+c^2)^3 z^{3/2} + (b^2+c^2)^5 z^{5/2} - 10b(b^2+c^2)^4 z^2 - 240b(b-c)(b+c)(b^2+c^2)^2 z + \right. \\ \left. 120(b^2+c^2)(5b^4-10c^2 b^2+c^4) \sqrt{z} - 240b(3b^4-10c^2 b^2+3c^4) \right) \cos(c\sqrt{z})$$

01.06.21.0421.01

$$\int z^3 e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz = \frac{2}{(b^2+c^2)^8} e^{b\sqrt{z}+e}$$

$$\left( (840b(b^2+c^2)^3 (b^4-10c^2 b^2+5c^4) z^{3/2} + 42b(b^2+c^2)^5 (b^2-3c^2) z^{5/2} + b(b^2+c^2)^7 z^{7/2} - 7(b-c)(b+c)(b^2+c^2)^6 z^3 - \right. \\ \left. 210(b^2+c^2)^4 (b^4-6c^2 b^2+c^4) z^2 - 2520(b^2+c^2)^2 (b^6-15c^2 b^4+15c^4 b^2-c^6) z + \right. \\ \left. 5040b(b^2+c^2)(b^6-21c^2 b^4+35c^4 b^2-7c^6) \sqrt{z} - 5040(b^8-28c^2 b^6+70c^4 b^4-28c^6 b^2+c^8) \right) \sin(c\sqrt{z}) - \\ c \left( 840(b^2+c^2)^3 (5b^4-10c^2 b^2+c^4) z^{3/2} + 42(3b^2-c^2)(b^2+c^2)^5 z^{5/2} + (b^2+c^2)^7 z^{7/2} - 14b(b^2+c^2)^6 z^3 - \right. \\ \left. 840b(b-c)(b+c)(b^2+c^2)^4 z^2 - 5040b(b^2+c^2)^2 (3b^4-10c^2 b^2+3c^4) z + \right. \\ \left. 5040(b^2+c^2)(7b^6-35c^2 b^4+21c^4 b^2-c^6) \sqrt{z} - 40320b(b^6-7c^2 b^4+7c^4 b^2-c^6) \right) \cos(c\sqrt{z})$$

01.06.21.0422.01

$$\int z^4 e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz =$$

$$\frac{2}{(b^2+c^2)^{10}} e^{b\sqrt{z}+e} \left( (60480 b (b^2+c^2)^3 (b^6-21 c^2 b^4+35 c^4 b^2-7 c^6) z^{3/2} + 3024 b (b^2+c^2)^5 (b^4-10 c^2 b^2+5 c^4) z^{5/2} + \right. \\ \left. 72 b (b^2+c^2)^7 (b^2-3 c^2) z^{7/2} + b (b^2+c^2)^9 z^{9/2} - 9 (b-c)(b+c)(b^2+c^2)^8 z^4 - \right. \\ \left. 504 (b^2+c^2)^6 (b^4-6 c^2 b^2+c^4) z^3 - 15120 (b^2+c^2)^4 (b^6-15 c^2 b^4+15 c^4 b^2-c^6) z^2 - 181440 (b^2+c^2)^2 \right. \\ \left. (b^8-28 c^2 b^6+70 c^4 b^4-28 c^6 b^2+c^8) z + 362880 b (b^2+c^2)(b^2-3 c^2)(b^6-33 c^2 b^4+27 c^4 b^2-3 c^6) \sqrt{z} - \right. \\ \left. 362880 (b^{10}-45 c^2 b^8+210 c^4 b^6-210 c^6 b^4+45 c^8 b^2-c^{10}) \right) \sin(c\sqrt{z}) - \\ c \left( 60480 (b^2+c^2)^3 (7 b^6-35 c^2 b^4+21 c^4 b^2-c^6) z^{3/2} + 3024 (b^2+c^2)^5 (5 b^4-10 c^2 b^2+c^4) z^{5/2} + \right. \\ \left. 72 (3 b^2-c^2)(b^2+c^2)^7 z^{7/2} + (b^2+c^2)^9 z^{9/2} - 18 b (b^2+c^2)^8 z^4 - 2016 b (b-c)(b+c)(b^2+c^2)^6 z^3 - \right. \\ \left. 30240 b (b^2+c^2)^4 (3 b^4-10 c^2 b^2+3 c^4) z^2 - 1451520 b (b^2+c^2)^2 (b^6-7 c^2 b^4+7 c^4 b^2-c^6) z + \right. \\ \left. 362880 (9 b^{10}-75 c^2 b^8+42 c^4 b^6+90 c^6 b^4-35 c^8 b^2+c^{10}) \sqrt{z} - \right. \\ \left. 725760 b (5 b^4-10 c^2 b^2+c^4)(b^4-10 c^2 b^2+5 c^4) \right) \cos(c\sqrt{z}) \Bigg)$$

01.06.21.0423.01

$$\int z^5 e^{b\sqrt{z}+e} \sin(c\sqrt{z}) dz = \frac{1}{(b^2+c^2)^{12}}$$

$$\begin{aligned} & \left( 2 e^{b\sqrt{z}+e} \left( (330 b^{15} (z^4 c^8 - 8 z^3 c^6 - 1056 z^2 c^4 - 16128 z c^2 + 20160) z^{3/2} + 165 b^{17} (z^3 c^6 + 6 z^2 c^4 - 144 z c^2 + 2016) z^{5/2} + \right. \right. \\ & \quad 55 b^{19} (z^2 c^4 + 12 z c^2 + 144) z^{7/2} + 11 b^{21} (z c^2 + 10) z^{9/2} + b^{23} z^{11/2} - 11 b^{22} z^5 - 99 b^{20} (z c^2 + 10) z^4 - \\ & \quad 55 b^{18} (7 z^2 c^4 + 36 z c^2 + 1008) z^3 - 165 b^{16} (5 z^3 c^6 - 114 z^2 c^4 - 3024 z c^2 + 10080) z^2 - \\ & \quad 990 b^{14} (z^4 c^8 - 104 z^3 c^6 - 3360 z^2 c^4 - 40320 z c^2 + 20160) z + \\ & \quad 462 b^{13} (z^5 c^{10} - 30 z^4 c^8 - 2400 z^3 c^6 - 43200 z^2 c^4 - 475200 z c^2 + 86400) \sqrt{z} + \\ & \quad 462 b^{11} c^2 (z^5 c^{10} - 60 z^4 c^8 - 3600 z^3 c^6 - 23040 z^2 c^4 + 302400 z c^2 - 4665600) \sqrt{z} + \\ & \quad 330 b^9 c^4 (z^5 c^{10} - 98 z^4 c^8 - 3696 z^3 c^6 + 110880 z^2 c^4 + 3769920 z c^2 + 33264000) \sqrt{z} + \\ & \quad 165 b^7 c^6 (z^5 c^{10} - 144 z^4 c^8 - 1344 z^3 c^6 + 354816 z^2 c^4 + 3991680 z c^2 - 31933440) \sqrt{z} + \\ & \quad 55 b^5 c^8 (z^5 c^{10} - 198 z^4 c^8 + 5184 z^3 c^6 + 508032 z^2 c^4 - 11975040 z c^2 - 215550720) \sqrt{z} + \\ & \quad 11 b^3 c^{10} (z^5 c^{10} - 260 z^4 c^8 + 18000 z^3 c^6 - 34473600 z c^2 + 558835200) \sqrt{z} + \\ & \quad b c^{12} (z^5 c^{10} - 330 z^4 c^8 + 39600 z^3 c^6 - 2328480 z^2 c^4 + 59875200 z c^2 - 439084800) \sqrt{z} + \\ & \quad 990 b^8 c^4 (z^5 c^{10} + 238 z^4 c^8 - 3696 z^3 c^6 - 332640 z^2 c^4 - 3326400 z c^2 - 19958400) + \\ & \quad 462 b^{10} c^2 (z^5 c^{10} + 660 z^4 c^8 + 7920 z^3 c^6 - 316800 z^2 c^4 - 5227200 z c^2 + 5702400) + \\ & \quad 99 b^2 c^{10} (z^5 c^{10} - 20 z^4 c^8 - 5040 z^3 c^6 + 403200 z^2 c^4 - 8668800 z c^2 + 26611200) + \\ & \quad 11 c^{12} (z^5 c^{10} - 90 z^4 c^8 + 5040 z^3 c^6 - 151200 z^2 c^4 + 1814400 z c^2 - 3628800) - \\ & \quad 462 b^{12} (z^5 c^{10} - 510 z^4 c^8 - 13920 z^3 c^6 - 129600 z^2 c^4 - 1857600 z c^2 + 86400) + \\ & \quad 165 b^6 c^6 (5 z^5 c^{10} + 624 z^4 c^8 - 38976 z^3 c^6 - 887040 z^2 c^4 + 19958400 z c^2 + 223534080) + \\ & \quad \left. 55 b^4 c^8 (7 z^5 c^{10} + 342 z^4 c^8 - 60480 z^3 c^6 + 1088640 z^2 c^4 + 43908480 z c^2 - 359251200) \right) \sin(c\sqrt{z}) - \\ & c \left( 330 b^{14} (z^4 c^8 + 72 z^3 c^6 + 864 z^2 c^4 + 181440) z^{3/2} + 165 b^{16} (z^3 c^6 + 66 z^2 c^4 + 1200 z c^2 + 14112) z^{5/2} + \right. \\ & \quad 55 b^{18} (z^2 c^4 + 52 z c^2 + 720) z^{7/2} + 11 b^{20} (z c^2 + 30) z^{9/2} + b^{22} z^{11/2} - 22 b^{21} z^5 - 220 b^{19} (z c^2 + 18) z^4 - \\ & \quad 990 b^{17} (z^2 c^4 + 28 z c^2 + 336) z^3 - 2640 b^{15} (z^3 c^6 + 30 z^2 c^4 + 336 z c^2 + 5040) z^2 - \\ & \quad 4620 b^{13} (z^4 c^8 + 24 z^3 c^6 - 288 z^2 c^4 - 8640 z c^2 + 43200) z + \\ & \quad 165 b^6 c^6 (z^5 c^{10} + 16 z^4 c^8 - 6720 z^3 c^6 + 64512 z^2 c^4 + 7539840 z c^2 + 31933440) \sqrt{z} + \\ & \quad 330 b^8 c^4 (z^5 c^{10} + 42 z^4 c^8 - 5040 z^3 c^6 - 110880 z^2 c^4 + 1995840 z c^2 + 35925120) \sqrt{z} + \\ & \quad 462 b^{10} c^2 (z^5 c^{10} + 60 z^4 c^8 - 2640 z^3 c^6 - 126720 z^2 c^4 - 1425600 z c^2 - 13305600) \sqrt{z} + \\ & \quad 462 b^{12} (z^5 c^{10} + 70 z^4 c^8 - 480 z^3 c^6 - 60480 z^2 c^4 - 820800 z c^2 + 950400) \sqrt{z} + \\ & \quad 55 b^4 c^8 (z^5 c^{10} - 18 z^4 c^8 - 6336 z^3 c^6 + 362880 z^2 c^4 + 2540160 z c^2 - 199584000) \sqrt{z} + \\ & \quad 11 b^2 c^{10} (z^5 c^{10} - 60 z^4 c^8 - 2160 z^3 c^6 + 483840 z^2 c^4 - 19958400 z c^2 + 195955200) \sqrt{z} + \\ & \quad c^{12} (z^5 c^{10} - 110 z^4 c^8 + 7920 z^3 c^6 - 332640 z^2 c^4 + 6652800 z c^2 - 39916800) \sqrt{z} - \\ & \quad 5544 b^{11} (z^5 c^{10} + 10 z^4 c^8 - 1440 z^3 c^6 - 36000 z^2 c^4 - 360000 z c^2 + 86400) - \\ & \quad 4620 b^9 c^2 (z^5 c^{10} - 12 z^4 c^8 - 2640 z^3 c^6 - 31680 z^2 c^4 + 95040 z c^2 - 1900800) - \\ & \quad 2640 b^7 c^4 (z^5 c^{10} - 42 z^4 c^8 - 3024 z^3 c^6 + 55440 z^2 c^4 + 1995840 z c^2 + 11975040) - \\ & \quad 990 b^5 c^6 (z^5 c^{10} - 80 z^4 c^8 - 1344 z^3 c^6 + 201600 z^2 c^4 + 443520 z c^2 - 31933440) - \\ & \quad 220 b^3 c^8 (z^5 c^{10} - 126 z^4 c^8 + 4032 z^3 c^6 + 181440 z^2 c^4 - 9072000 z c^2 + 39916800) - \\ & \quad \left. 22 b c^{10} (z^5 c^{10} - 180 z^4 c^8 + 15120 z^3 c^6 - 604800 z^2 c^4 + 9072000 z c^2 - 21772800) \right) \cos(c\sqrt{z}) \end{aligned}$$



$$01.06.21.0424.01 \int \frac{e^{b\sqrt{z}+e} \sin(c\sqrt{z})}{z} dz = i e^e \left( \text{Ei}((b-ic)\sqrt{z}) - \text{Ei}((b+ic)\sqrt{z}) \right)$$

$$01.06.21.0425.01 \int \frac{e^{b\sqrt{z}+e} \sin(c\sqrt{z})}{z^2} dz = \frac{1}{2z} i e^e \left( -z \text{Ei}((b+ic)\sqrt{z}) (b+ic)^2 + e^{(b-ic)\sqrt{z}} \left( -\sqrt{z} b + e^{2ic\sqrt{z}} (\sqrt{z} b + ic\sqrt{z} + 1) + ic\sqrt{z} - 1 \right) + (b-ic)^2 z \text{Ei}((b-ic)\sqrt{z}) \right)$$

$$01.06.21.0426.01 \int \frac{e^{b\sqrt{z}+e} \sin(c\sqrt{z})}{z^3} dz = -\frac{1}{24} i e^e \left( \text{Ei}((b+ic)\sqrt{z}) (b+ic)^4 + \frac{e^{(b-ic)\sqrt{z}} \left( (b-ic)^3 z^{3/2} + (b-ic)^2 z + 2(b-ic)\sqrt{z} + 6 \right)}{z^2} - (b-ic)^4 \text{Ei}((b-ic)\sqrt{z}) - \frac{e^{(b+ic)\sqrt{z}} \left( (b+ic)^3 z^{3/2} + (b+ic)^2 z + 2(b+ic)\sqrt{z} + 6 \right)}{z^2} \right)$$

$$01.06.21.0427.01 \int \frac{e^{b\sqrt{z}+e} \sin(c\sqrt{z})}{z^4} dz = -\frac{1}{720} i e^e \left( \text{Ei}((b+ic)\sqrt{z}) (b+ic)^6 - \frac{1}{z^3} \left( e^{(b+ic)\sqrt{z}} \left( 2(b+ic)^3 z^{3/2} + (b+ic)^5 z^{5/2} + (b+ic)^4 z^2 + 6(b+ic)^2 z + 24(b+ic)\sqrt{z} + 120 \right) \right) + \frac{1}{z^3} \left( e^{(b-ic)\sqrt{z}} \left( 2(b-ic)^3 z^{3/2} + (b-ic)^5 z^{5/2} + (b-ic)^4 z^2 + 6(b-ic)^2 z + 24(b-ic)\sqrt{z} + 120 \right) \right) - (b-ic)^6 \text{Ei}((b-ic)\sqrt{z}) \right)$$

$$01.06.21.0428.01 \int \frac{e^{b\sqrt{z}+e} \sin(c\sqrt{z})}{z^5} dz = -\frac{1}{40320} i e^e \left( \text{Ei}((b+ic)\sqrt{z}) (b+ic)^8 - \frac{1}{z^4} \left( e^{(b+ic)\sqrt{z}} \left( 24(b+ic)^3 z^{3/2} + 2(b+ic)^5 z^{5/2} + (b+ic)^7 z^{7/2} + (b+ic)^6 z^3 + 6(b+ic)^4 z^2 + 120(b+ic)^2 z + 720(b+ic)\sqrt{z} + 5040 \right) \right) + \frac{1}{z^4} \left( e^{(b-ic)\sqrt{z}} \left( 24(b-ic)^3 z^{3/2} + 2(b-ic)^5 z^{5/2} + (b-ic)^7 z^{7/2} + (b-ic)^6 z^3 + 6(b-ic)^4 z^2 + 120(b-ic)^2 z + 720(b-ic)\sqrt{z} + 5040 \right) \right) - (b-ic)^8 \text{Ei}((b-ic)\sqrt{z}) \right)$$

Involving  $z^n e^{bz^r+dz} \sin(cz^r)$

01.06.21.0429.01

$$\int z^n e^{bz^2+dz} \sin(cz^2) dz = \frac{i}{4\sqrt{b+ic}} e^{-\frac{d^2}{4(b+ic)}}$$

$$\sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d+2(b+ic)z)^{q+1} \left( -\frac{(d+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b+ic)z)^2}{4(b+ic)}\right) -$$

$$\frac{i}{4\sqrt{b-ic}} e^{\frac{d^2}{4(b-ic)}} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d+2(b-ic)z)^{q+1}$$

$$\left( -\frac{(d+2(b-ic)z)^2}{b-ic} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b-ic)z)^2}{4(b-ic)}\right); n \in \mathbb{N}$$

01.06.21.0430.01

$$\int z^n e^{\sqrt{z}bz+dz} \sin(c\sqrt{z}) dz =$$

$$i 2^{-2(n+1)} d^{-2(n+1)} e^{-\frac{b^2-c^2}{2d}} \left( e^{\frac{(b+ic)^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2d\sqrt{z})^{h+k} \left( -\frac{(b-ic+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b-ic+2d\sqrt{z})^2}{4d}\right) \right) + \right.$$

$$\left. 2\sqrt{-\frac{(b-ic+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b-ic+2d\sqrt{z})^2}{4d}\right) \right) -$$

$$e^{\frac{(b-ic)^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2d\sqrt{z})^{h+k} \left( -\frac{(b+ic+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b+ic)(b+ic+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ic+2d\sqrt{z})^2}{4d}\right) \right) + \right.$$

$$\left. 2\sqrt{-\frac{(b+ic+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ic+2d\sqrt{z})^2}{4d}\right) \right) ; n \in \mathbb{N}$$

Involving  $z^n e^{bz^r+dz+e} \sin(cz^r)$

01.06.21.0431.01

$$\int z^n e^{b z^2 + d z + e} \sin(c z^2) dz =$$

$$\frac{1}{4} i e^e \left( \frac{1}{\sqrt{b+ic}} e^{-\frac{d^2}{4(b+ic)}} \sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d+2(b+ic)z)^{q+1} \left( -\frac{(d+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b+ic)z)^2}{4(b+ic)}\right) - \frac{1}{\sqrt{b-ic}} e^{\frac{d^2}{4ic-4b}} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (-d)^{n-q} \right. \\ \left. (d+2(b-ic)z)^{q+1} \left( \frac{(d+2(b-ic)z)^2}{ic-b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{(d+2(b-ic)z)^2}{4(ic-b)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0432.01

$$\int z^n e^{\sqrt{z} b + d z + e} \sin(c \sqrt{z}) dz =$$

$$i 2^{-2(n+1)} d^{-2(n+1)} e^{-\frac{b^2-c^2-2de}{2d}} \left( e^{\frac{(b+ic)^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2d\sqrt{z})^{h+k} \left( -\frac{(b-ic+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right. \\ \left. \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b-ic+2d\sqrt{z})^2}{4d}\right) + \right. \right. \\ \left. \left. 2 \sqrt{-\frac{(b-ic+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b-ic+2d\sqrt{z})^2}{4d}\right) \right) \right) - \\ e^{\frac{(ic-b)^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2d\sqrt{z})^{h+k} \left( -\frac{(b+ic+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \\ \left. \binom{k}{h} \binom{n}{k} \left( (b+ic)(b+ic+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ic+2d\sqrt{z})^2}{4d}\right) + \right. \right. \\ \left. \left. 2 \sqrt{-\frac{(b+ic+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ic+2d\sqrt{z})^2}{4d}\right) \right) \right) /; n \in \mathbb{N}$$

Involving  $z^n e^{dz} \sin(cz^r + g)$

01.06.21.0433.01

$$\int z^n e^{dz} \sin(cz^2 + g) dz = \frac{1}{4\sqrt{ic}}$$

$$\left( i e^{\frac{id^2}{4c} + ig} \sum_{q=0}^n 2^{q-n} (ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d+2icz)^{q+1} \left( \frac{i(d+2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+2icz)^2}{4c}\right) \right) - \frac{1}{4\sqrt{-ic}}$$

$$\left( i e^{-\frac{id^2}{4c} - ig} \sum_{q=0}^n 2^{q-n} (-ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d-2icz)^{q+1} \left( -\frac{i(d-2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-2icz)^2}{4c}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0434.01

$$\int z^n e^{dz} \sin(\sqrt{z} c + g) dz =$$

$$i 2^{-2(n+1)} e^{-ig} \left( d^{-2(n+1)} e^{\frac{c^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} (2d\sqrt{z} - ic)^{h+k} \left( -\frac{(2d\sqrt{z} - ic)^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\binom{k}{h} \binom{n}{k} \left( 2d \sqrt{-\frac{(2d\sqrt{z} - ic)^2}{d}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2d\sqrt{z} - ic)^2}{4d}\right) - \right.$$

$$\left. ic(2d\sqrt{z} - ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2d\sqrt{z} - ic)^2}{4d}\right) \right) -$$

$$d^{-2(n+1)} e^{\frac{c^2}{4d} + 2ig} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z}d + ic)^{h+k} \left( -\frac{(2\sqrt{z}d + ic)^2}{d} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( ci(2\sqrt{z}d + ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}d + ic)^2}{4d}\right) + \right.$$

$$\left. 2 \sqrt{-\frac{(2\sqrt{z}d + ic)^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}d + ic)^2}{4d}\right) \right) /; n \in \mathbb{N}$$

Involving  $z^n e^{dz+e} \sin(cz^r + g)$

01.06.21.0435.01

$$\int z^n e^{dz+e} \sin(cz^2 + g) dz = \frac{1}{4\sqrt{ic}}$$

$$\left( i e^{\frac{id^2}{4c} + e + ig} \sum_{q=0}^n 2^{q-n} (ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d+2icz)^{q+1} \left( \frac{i(d+2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+2icz)^2}{4c}\right) \right) - \frac{1}{4\sqrt{-ic}}$$

$$\left( i e^{-\frac{id^2}{4c} + e - ig} \sum_{q=0}^n 2^{q-n} (-ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d-2icz)^{q+1} \left( -\frac{i(d-2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-2icz)^2}{4c}\right) \right); n \in \mathbb{N}$$

01.06.21.0436.01

$$\int z^n e^{dz+e} \sin(\sqrt{z} c + g) dz =$$

$$i 2^{-2(n+1)} e^{e-ig} \left( d^{-2(n+1)} e^{\frac{c^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} (2d\sqrt{z} - ic)^{h+k} \left( -\frac{(2d\sqrt{z} - ic)^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( 2d \sqrt{-\frac{(2d\sqrt{z} - ic)^2}{d}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2d\sqrt{z} - ic)^2}{4d}\right) - \right.$$

$$\left. ic(2d\sqrt{z} - ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2d\sqrt{z} - ic)^2}{4d}\right) \right) \right) -$$

$$d^{-2(n+1)} e^{\frac{c^2}{4d} + 2ig} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z} d + ic)^{h+k} \left( -\frac{(2\sqrt{z} d + ic)^2}{d} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left( \binom{k}{h} \binom{n}{k} \left( ci(2\sqrt{z} d + ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} d + ic)^2}{4d}\right) \right. \right.$$

$$\left. \left. + 2 \sqrt{-\frac{(2\sqrt{z} d + ic)^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} d + ic)^2}{4d}\right) \right) \right); n \in \mathbb{N}$$

Involving  $z^{\alpha-1} e^{bz^r} \sin(cz^r + g)$

01.06.21.0437.01

$$\int z^{\alpha-1} e^{bz^r} \sin(cz^r + g) dz = -\frac{i z^\alpha}{2r} \left( e^{-ig} ((ic-b)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ic-b)z^r\right) - e^{ig} (-(b+ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -(b+ic)z^r\right) \right)$$

01.06.21.0438.01

$$\int \frac{e^{bz^r} \sin(cz^r + g)}{z} dz = \frac{\text{Ei}((b+ic)z^r) (\sin(g) - i \cos(g)) + \text{Ei}((b-ic)z^r) (i \cos(g) + \sin(g))}{2r}$$

01.06.21.0439.01

$$\int z^{2n} e^{bz^2} \sin(cz^2 + g) dz = \frac{1}{4} i z \left( e^{ig} ((-b-ic)z^2)^{-\frac{1}{2}} (-b-ic)^{-n} \left( \text{erfc}\left(\sqrt{(-b-ic)z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{-(b-ic)z^2} \sum_{k=0}^{n-1} \frac{((-b-ic)z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{-(b-ic)z^2} \sum_{k=n}^{-1} \frac{((-b-ic)z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) - e^{-ig} ((ic-b)z^2)^{-\frac{1}{2}} (ic-b)^{-n} \left( \text{erfc}\left(\sqrt{(ic-b)z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{-(ic-b)z^2} \sum_{k=0}^{n-1} \frac{((ic-b)z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} - e^{-(ic-b)z^2} \sum_{k=n}^{-1} \frac{((ic-b)z^2)^{k+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{k-n+1}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0440.01

$$\int z^{2n-1} e^{bz^2} \sin(cz^2 + g) dz = \frac{1}{4} i \left( e^{ig} (-b-ic)^{-n} \left( \frac{(-1)^{n-1} \text{Ei}(-(-b-ic)z^2)}{(-n)!} + e^{-(b-ic)z^2} \sum_{k=0}^{n-1} \frac{((-b-ic)z^2)^k}{(n)_{k-n+1}} - e^{-(b-ic)z^2} \sum_{k=n}^{-1} \frac{((-b-ic)z^2)^k}{(n)_{k-n+1}} \right) - e^{-ig} (ic-b)^{-n} \left( \frac{(-1)^{n-1} \text{Ei}(-(ic-b)z^2)}{(-n)!} + e^{-(ic-b)z^2} \sum_{k=0}^{n-1} \frac{((ic-b)z^2)^k}{(n)_{k-n+1}} - e^{-(ic-b)z^2} \sum_{k=n}^{-1} \frac{((ic-b)z^2)^k}{(n)_{k-n+1}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0441.01

$$\int z e^{bz^2} \sin(cz^2 + g) dz = \frac{e^{bz^2} (b \sin(cz^2 + g) - c \cos(cz^2 + g))}{2(b^2 + c^2)}$$

01.06.21.0442.01

$$\int z^2 e^{bz^2} \sin(cz^2 + g) dz = \frac{1}{4} z^3 \left( \frac{\frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 1\right) - e^{(b+ic)z^2} \sqrt{-(b+ic)z^2}}{(-b+ic)z^2} + \frac{\frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 1\right) - e^{(b-ic)z^2} \sqrt{-(b-ic)z^2}}{(-b-ic)z^2} \right) \sin(g) - i \cos(g) \left( \frac{\frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 1\right) - e^{(b+ic)z^2} \sqrt{-(b+ic)z^2}}{(-b+ic)z^2} + \frac{e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} - \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 1\right)}{(-b-ic)z^2} \right) \right)$$

01.06.21.0443.01

$$\int z^3 e^{bz^2} \sin(cz^2 + g) dz = \frac{e^{bz^2} ((z^2 b^3 - b^2 + c^2 z^2 b + c^2) \sin(cz^2 + g) - c(b^2 z^2 + c^2 z^2 - 2b) \cos(cz^2 + g))}{2(b^2 + c^2)^2}$$

01.06.21.0444.01

$$\int z^4 e^{bz^2} \sin(cz^2 + g) dz = \frac{1}{16} z^5 \left( \frac{1}{(-b+ic)z^2} \left( 2 e^{(b+ic)z^2} \sqrt{-(b+ic)z^2} (2bz^2 + 2ciz^2 - 3) + 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 3\sqrt{\pi} \right) + \frac{1}{(-b-ic)z^2} \left( 2 e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} (2bz^2 - 2iciz^2 - 3) + 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 3\sqrt{\pi} \right) \right) \sin(g) - i \cos(g) \left( \frac{1}{(-b+ic)z^2} \left( 2 e^{(b+ic)z^2} \sqrt{-(b+ic)z^2} (2bz^2 + 2ciz^2 - 3) + 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 3\sqrt{\pi} \right) + \frac{1}{(-b-ic)z^2} \left( -2 e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} (2bz^2 - 2iciz^2 - 3) - 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) + 3\sqrt{\pi} \right) \right) \right)$$

01.06.21.0445.01

$$\int z^5 e^{bz^2} \sin(cz^2 + g) dz = \frac{1}{2(b^2 + c^2)^3} \left( e^{bz^2} ((z^4 b^5 - 2z^2 b^4 + 2(c^2 z^4 + 1)b^3 + c^2(c^2 z^4 - 6)b + 2c^4 z^2) \sin(cz^2 + g) - c(b^4 z^4 - 4b^3 z^2 - 4bc^2 z^2 + c^2(c^2 z^4 - 2) + 2b^2(c^2 z^4 + 3)) \cos(cz^2 + g)) \right)$$

01.06.21.0446.01

$$\int \frac{e^{bz^2} \sin(cz^2 + g)}{z} dz = \frac{1}{4} i e^{-ig} (\operatorname{Ei}((b-ic)z^2) - e^{2ig} \operatorname{Ei}((b+ic)z^2))$$

01.06.21.0447.01

$$\int \frac{e^{bz^2} \sin(cz^2 + g)}{z^2} dz = \frac{1}{2z} \left( i\sqrt{\pi} e^{-ig} \left( \sqrt{-(b-ic)z^2} \operatorname{erfc} \left( \sqrt{-(b-ic)z^2} \right) - e^{2ig} \sqrt{-(b+ic)z^2} \operatorname{erfc} \left( \sqrt{-(b+ic)z^2} \right) \right) - 2e^{bz^2} \sin(cz^2 + g) \right)$$

01.06.21.0448.01

$$\int \frac{e^{bz^2} \sin(cz^2 + g)}{z^3} dz = \frac{1}{4} \left( (c-ib) e^{ig} \operatorname{Ei}((b+ic)z^2) + (c+ib) e^{-ig} \operatorname{Ei}((b-ic)z^2) - \frac{2e^{bz^2} \sin(cz^2 + g)}{z^2} \right)$$

01.06.21.0449.01

$$\int \frac{e^{bz^2} \sin(cz^2 + g)}{z^4} dz = -\frac{1}{6z^3} \left( -2i\sqrt{\pi} \cos(g) \left( (b-ic)^{3/2} \operatorname{erfi}(\sqrt{b-ic}z) - (b+ic)^{3/2} \operatorname{erfi}(\sqrt{b+ic}z) \right) z^3 - \right. \\ \left. 2\sqrt{\pi} \left( \operatorname{erfi}(\sqrt{b+ic}z) (b+ic)^{3/2} + (b-ic)^{3/2} \operatorname{erfi}(\sqrt{b-ic}z) \right) \sin(g) z^3 + \right. \\ \left. (-2i\sqrt{\pi} (-(b+ic)z^2)^{3/2} + 2i\sqrt{\pi} (-(b-ic)z^2)^{3/2} + e^{(b+ic)z^2} (2(c-ib)z^2 - i) + e^{(b-ic)z^2} (2(c+ib)z^2 + i)) \cos(g) + \right. \\ \left. (2\sqrt{\pi} (-(b+ic)z^2)^{3/2} + 2\sqrt{\pi} (-(b-ic)z^2)^{3/2} + e^{(b+ic)z^2} (2(b+ic)z^2 + 1) + e^{(b-ic)z^2} (2(b-ic)z^2 + 1)) \sin(g) \right)$$

01.06.21.0450.01

$$\int \frac{e^{bz^2} \sin(cz^2 + g)}{z^5} dz = \frac{1}{8z^4} \left( (b+ic)^2 \operatorname{Ei}((b+ic)z^2) (\sin(g) - i \cos(g)) z^4 + (b-ic)^2 \operatorname{Ei}((b-ic)z^2) (i \cos(g) + \sin(g)) z^4 + \right. \\ \left. e^{(b-ic)z^2} i \left( (-bz^2 + ciz^2 + e^{2ic}z^2 (bz^2 + ciz^2 + 1) - 1) \cos(g) - (e^{2ic}z^2 (-ibz^2 + cz^2 - i) - i(bz^2 - icz^2 + 1)) \sin(g) \right) \right)$$

01.06.21.0451.01

$$\int z^n e^{b\sqrt{z}} \sin(\sqrt{z}c + g) dz = i e^{ig} (-b-ic)^{-2(n+1)} \\ \left( -\frac{\operatorname{Ei}(-(-b-ic)\sqrt{z})}{(-2(n+1))!} + e^{-(-b-ic)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((-b-ic)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} - e^{-(-b-ic)\sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{((-b-ic)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} \right) - i e^{-ig} \\ (ic-b)^{-2(n+1)} \left( -\frac{\operatorname{Ei}(-(ic-b)\sqrt{z})}{(-2(n+1))!} + e^{-(ic-b)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((ic-b)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} - e^{-(ic-b)\sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{((ic-b)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} \right) /; n \in \mathbb{Z}$$

01.06.21.0452.01

$$\int z e^{b\sqrt{z}} \sin(\sqrt{z}c + g) dz = \frac{1}{(b^2 + c^2)^4} 2 e^{b\sqrt{z}} \\ \left( (b(b^2 + c^2)^3 z^{3/2} - 3(b-c)(b+c)(b^2 + c^2)^2 z + 6b(b^2 + c^2)(b^2 - 3c^2)\sqrt{z} - 6(b^4 - 6c^2b^2 + c^4)) \sin(\sqrt{z}c + g) - \right. \\ \left. c((b^2 + c^2)^3 z^{3/2} - 6b(b^2 + c^2)^2 z + 6(3b^2 - c^2)(b^2 + c^2)\sqrt{z} - 24b(b-c)(b+c)) \cos(\sqrt{z}c + g) \right)$$



01.06.21.0453.01

$$\int z^2 e^{b\sqrt{z}} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^6} 2 e^{b\sqrt{z}} \left( (20 b (b^2 + c^2)^3 (b^2 - 3 c^2) z^{3/2} + b (b^2 + c^2)^5 z^{5/2} - 5 (b - c) (b + c) (b^2 + c^2)^4 z^2 - 60 (b^2 + c^2)^2 (b^4 - 6 c^2 b^2 + c^4) z + 120 b (b^2 + c^2) (b^4 - 10 c^2 b^2 + 5 c^4) \sqrt{z} - 120 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) \right) \sin(\sqrt{z} c + g) - c \left( 20 (3 b^2 - c^2) (b^2 + c^2)^3 z^{3/2} + (b^2 + c^2)^5 z^{5/2} - 10 b (b^2 + c^2)^4 z^2 - 240 b (b - c) (b + c) (b^2 + c^2)^2 z + 120 (b^2 + c^2) (5 b^4 - 10 c^2 b^2 + c^4) \sqrt{z} - 240 b (3 b^4 - 10 c^2 b^2 + 3 c^4) \right) \cos(\sqrt{z} c + g) \right)$$

01.06.21.0454.01

$$\int z^3 e^{b\sqrt{z}} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^8} 2 e^{b\sqrt{z}} \left( (840 b (b^2 + c^2)^3 (b^4 - 10 c^2 b^2 + 5 c^4) z^{3/2} + 42 b (b^2 + c^2)^5 (b^2 - 3 c^2) z^{5/2} + b (b^2 + c^2)^7 z^{7/2} - 7 (b - c) (b + c) (b^2 + c^2)^6 z^3 - 210 (b^2 + c^2)^4 (b^4 - 6 c^2 b^2 + c^4) z^2 - 2520 (b^2 + c^2)^2 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) z + 5040 b (b^2 + c^2) (b^6 - 21 c^2 b^4 + 35 c^4 b^2 - 7 c^6) \sqrt{z} - 5040 (b^8 - 28 c^2 b^6 + 70 c^4 b^4 - 28 c^6 b^2 + c^8) \right) \sin(\sqrt{z} c + g) - c \left( 840 (b^2 + c^2)^3 (5 b^4 - 10 c^2 b^2 + c^4) z^{3/2} + 42 (3 b^2 - c^2) (b^2 + c^2)^5 z^{5/2} + (b^2 + c^2)^7 z^{7/2} - 14 b (b^2 + c^2)^6 z^3 - 840 b (b - c) (b + c) (b^2 + c^2)^4 z^2 - 5040 b (b^2 + c^2)^2 (3 b^4 - 10 c^2 b^2 + 3 c^4) z + 5040 (b^2 + c^2) (7 b^6 - 35 c^2 b^4 + 21 c^4 b^2 - c^6) \sqrt{z} - 40320 b (b^6 - 7 c^2 b^4 + 7 c^4 b^2 - c^6) \right) \cos(\sqrt{z} c + g) \right)$$

01.06.21.0455.01

$$\int z^4 e^{b\sqrt{z}} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^{10}} 2 e^{b\sqrt{z}} \left( (60480 b (b^2 + c^2)^3 (b^6 - 21 c^2 b^4 + 35 c^4 b^2 - 7 c^6) z^{3/2} + 3024 b (b^2 + c^2)^5 (b^4 - 10 c^2 b^2 + 5 c^4) z^{5/2} + 72 b (b^2 + c^2)^7 (b^2 - 3 c^2) z^{7/2} + b (b^2 + c^2)^9 z^{9/2} - 9 (b - c) (b + c) (b^2 + c^2)^8 z^4 - 504 (b^2 + c^2)^6 (b^4 - 6 c^2 b^2 + c^4) z^3 - 15120 (b^2 + c^2)^4 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) z^2 - 181440 (b^2 + c^2)^2 (b^8 - 28 c^2 b^6 + 70 c^4 b^4 - 28 c^6 b^2 + c^8) z + 362880 b (b^2 + c^2) (b^2 - 3 c^2) (b^6 - 33 c^2 b^4 + 27 c^4 b^2 - 3 c^6) \sqrt{z} - 362880 (b^{10} - 45 c^2 b^8 + 210 c^4 b^6 - 210 c^6 b^4 + 45 c^8 b^2 - c^{10}) \right) \sin(\sqrt{z} c + g) - c \left( 60480 (b^2 + c^2)^3 (7 b^6 - 35 c^2 b^4 + 21 c^4 b^2 - c^6) z^{3/2} + 3024 (b^2 + c^2)^5 (5 b^4 - 10 c^2 b^2 + c^4) z^{5/2} + 72 (3 b^2 - c^2) (b^2 + c^2)^7 z^{7/2} + (b^2 + c^2)^9 z^{9/2} - 18 b (b^2 + c^2)^8 z^4 - 2016 b (b - c) (b + c) (b^2 + c^2)^6 z^3 - 30240 b (b^2 + c^2)^4 (3 b^4 - 10 c^2 b^2 + 3 c^4) z^2 - 1451520 b (b^2 + c^2)^2 (b^6 - 7 c^2 b^4 + 7 c^4 b^2 - c^6) z + 362880 (9 b^{10} - 75 c^2 b^8 + 42 c^4 b^6 + 90 c^6 b^4 - 35 c^8 b^2 + c^{10}) \sqrt{z} - 725760 b (5 b^4 - 10 c^2 b^2 + c^4) (b^4 - 10 c^2 b^2 + 5 c^4) \right) \cos(\sqrt{z} c + g) \right)$$

01.06.21.0456.01

$$\int z^5 e^{b\sqrt{z}} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^{12}}$$

$$\begin{aligned} & \left( 2 e^{b\sqrt{z}} \left( (330 b^{15} (z^4 c^8 - 8 z^3 c^6 - 1056 z^2 c^4 - 16128 z c^2 + 20160) z^{3/2} + 165 b^{17} (z^3 c^6 + 6 z^2 c^4 - 144 z c^2 + 2016) z^{5/2} + \right. \right. \\ & 55 b^{19} (z^2 c^4 + 12 z c^2 + 144) z^{7/2} + 11 b^{21} (z c^2 + 10) z^{9/2} + b^{23} z^{11/2} - 11 b^{22} z^5 - 99 b^{20} (z c^2 + 10) z^4 - \\ & 55 b^{18} (7 z^2 c^4 + 36 z c^2 + 1008) z^3 - 165 b^{16} (5 z^3 c^6 - 114 z^2 c^4 - 3024 z c^2 + 10080) z^2 - \\ & 990 b^{14} (z^4 c^8 - 104 z^3 c^6 - 3360 z^2 c^4 - 40320 z c^2 + 20160) z + \\ & 462 b^{13} (z^5 c^{10} - 30 z^4 c^8 - 2400 z^3 c^6 - 43200 z^2 c^4 - 475200 z c^2 + 86400) \sqrt{z} + \\ & 462 b^{11} c^2 (z^5 c^{10} - 60 z^4 c^8 - 3600 z^3 c^6 - 23040 z^2 c^4 + 302400 z c^2 - 4665600) \sqrt{z} + \\ & 330 b^9 c^4 (z^5 c^{10} - 98 z^4 c^8 - 3696 z^3 c^6 + 110880 z^2 c^4 + 3769920 z c^2 + 33264000) \sqrt{z} + \\ & 165 b^7 c^6 (z^5 c^{10} - 144 z^4 c^8 - 1344 z^3 c^6 + 354816 z^2 c^4 + 3991680 z c^2 - 31933440) \sqrt{z} + \\ & 55 b^5 c^8 (z^5 c^{10} - 198 z^4 c^8 + 5184 z^3 c^6 + 508032 z^2 c^4 - 11975040 z c^2 - 215550720) \sqrt{z} + \\ & 11 b^3 c^{10} (z^5 c^{10} - 260 z^4 c^8 + 18000 z^3 c^6 - 34473600 z c^2 + 558835200) \sqrt{z} + \\ & b c^{12} (z^5 c^{10} - 330 z^4 c^8 + 39600 z^3 c^6 - 2328480 z^2 c^4 + 59875200 z c^2 - 439084800) \sqrt{z} + \\ & 990 b^8 c^4 (z^5 c^{10} + 238 z^4 c^8 - 3696 z^3 c^6 - 332640 z^2 c^4 - 3326400 z c^2 - 19958400) + \\ & 462 b^{10} c^2 (z^5 c^{10} + 660 z^4 c^8 + 7920 z^3 c^6 - 316800 z^2 c^4 - 5227200 z c^2 + 5702400) + \\ & 99 b^2 c^{10} (z^5 c^{10} - 20 z^4 c^8 - 5040 z^3 c^6 + 403200 z^2 c^4 - 8668800 z c^2 + 26611200) + \\ & 11 c^{12} (z^5 c^{10} - 90 z^4 c^8 + 5040 z^3 c^6 - 151200 z^2 c^4 + 1814400 z c^2 - 3628800) - \\ & 462 b^{12} (z^5 c^{10} - 510 z^4 c^8 - 13920 z^3 c^6 - 129600 z^2 c^4 - 1857600 z c^2 + 86400) + \\ & 165 b^6 c^6 (5 z^5 c^{10} + 624 z^4 c^8 - 38976 z^3 c^6 - 887040 z^2 c^4 + 19958400 z c^2 + 223534080) + \\ & 55 b^4 c^8 (7 z^5 c^{10} + 342 z^4 c^8 - 60480 z^3 c^6 + 1088640 z^2 c^4 + 43908480 z c^2 - 359251200) \Big) \sin(\sqrt{z} c + g) - \\ & c (330 b^{14} (z^4 c^8 + 72 z^3 c^6 + 864 z^2 c^4 + 181440) z^{3/2} + 165 b^{16} (z^3 c^6 + 66 z^2 c^4 + 1200 z c^2 + 14112) z^{5/2} + \\ & 55 b^{18} (z^2 c^4 + 52 z c^2 + 720) z^{7/2} + 11 b^{20} (z c^2 + 30) z^{9/2} + b^{22} z^{11/2} - 22 b^{21} z^5 - 220 b^{19} (z c^2 + 18) z^4 - \\ & 990 b^{17} (z^2 c^4 + 28 z c^2 + 336) z^3 - 2640 b^{15} (z^3 c^6 + 30 z^2 c^4 + 336 z c^2 + 5040) z^2 - \\ & 4620 b^{13} (z^4 c^8 + 24 z^3 c^6 - 288 z^2 c^4 - 8640 z c^2 + 43200) z + \\ & 165 b^6 c^6 (z^5 c^{10} + 16 z^4 c^8 - 6720 z^3 c^6 + 64512 z^2 c^4 + 7539840 z c^2 + 31933440) \sqrt{z} + \\ & 330 b^8 c^4 (z^5 c^{10} + 42 z^4 c^8 - 5040 z^3 c^6 - 110880 z^2 c^4 + 1995840 z c^2 + 35925120) \sqrt{z} + \\ & 462 b^{10} c^2 (z^5 c^{10} + 60 z^4 c^8 - 2640 z^3 c^6 - 126720 z^2 c^4 - 1425600 z c^2 - 13305600) \sqrt{z} + \\ & 462 b^{12} (z^5 c^{10} + 70 z^4 c^8 - 480 z^3 c^6 - 60480 z^2 c^4 - 820800 z c^2 + 950400) \sqrt{z} + \\ & 55 b^4 c^8 (z^5 c^{10} - 18 z^4 c^8 - 6336 z^3 c^6 + 362880 z^2 c^4 + 2540160 z c^2 - 199584000) \sqrt{z} + \\ & 11 b^2 c^{10} (z^5 c^{10} - 60 z^4 c^8 - 2160 z^3 c^6 + 483840 z^2 c^4 - 19958400 z c^2 + 195955200) \sqrt{z} + \\ & c^{12} (z^5 c^{10} - 110 z^4 c^8 + 7920 z^3 c^6 - 332640 z^2 c^4 + 6652800 z c^2 - 39916800) \sqrt{z} - \\ & 5544 b^{11} (z^5 c^{10} + 10 z^4 c^8 - 1440 z^3 c^6 - 36000 z^2 c^4 - 360000 z c^2 + 86400) - \\ & 4620 b^9 c^2 (z^5 c^{10} - 12 z^4 c^8 - 2640 z^3 c^6 - 31680 z^2 c^4 + 95040 z c^2 - 1900800) - \\ & 2640 b^7 c^4 (z^5 c^{10} - 42 z^4 c^8 - 3024 z^3 c^6 + 55440 z^2 c^4 + 1995840 z c^2 + 11975040) - \\ & 990 b^5 c^6 (z^5 c^{10} - 80 z^4 c^8 - 1344 z^3 c^6 + 201600 z^2 c^4 + 443520 z c^2 - 31933440) - \\ & 220 b^3 c^8 (z^5 c^{10} - 126 z^4 c^8 + 4032 z^3 c^6 + 181440 z^2 c^4 - 9072000 z c^2 + 39916800) - \\ & 22 b c^{10} (z^5 c^{10} - 180 z^4 c^8 + 15120 z^3 c^6 - 604800 z^2 c^4 + 9072000 z c^2 - 21772800) \Big) \cos(\sqrt{z} c + g) \Big) \end{aligned}$$

$$01.06.21.0457.01 \int \frac{e^{b\sqrt{z}} \sin(\sqrt{z} c + g)}{z} dz = i e^{-ig} \left( \text{Ei}((b - ic)\sqrt{z}) - e^{2ig} \text{Ei}((b + ic)\sqrt{z}) \right)$$

$$01.06.21.0458.01 \int \frac{e^{b\sqrt{z}} \sin(\sqrt{z} c + g)}{z^2} dz = \frac{1}{2z} i e^{-ig} \left( -e^{2ig} z \text{Ei}((b + ic)\sqrt{z}) (b + ic)^2 + e^{(b-ic)\sqrt{z}} \left( -\sqrt{z} b + e^{2i(\sqrt{z} c + g)} (\sqrt{z} b + ic\sqrt{z} + 1) + ic\sqrt{z} - 1 \right) + (b - ic)^2 z \text{Ei}((b - ic)\sqrt{z}) \right)$$

$$01.06.21.0459.01 \int \frac{e^{b\sqrt{z}} \sin(\sqrt{z} c + g)}{z^3} dz = \frac{1}{24} i e^{-ig} \left( -e^{2ig} \text{Ei}((b + ic)\sqrt{z}) (b + ic)^4 + \frac{1}{z^2} \left( e^{(b-ic)\sqrt{z}} \left( -b^3 z^{3/2} - ic^3 z^{3/2} + c^2 z + 2ic\sqrt{z} + b(3z c^2 + 2i\sqrt{z} c - 2) \sqrt{z} + b^2(3ic z^{3/2} - z) - 6 \right) + \frac{1}{z^2} \left( e^{\sqrt{z}(b+ic)+2ig} \left( b^3 z^{3/2} - ic^3 z^{3/2} - c^2 z + 2ic\sqrt{z} + b^2(3ic z^{3/2} + z) + b(-3c^2 z^{3/2} + 2icz + 2\sqrt{z}) + 6 \right) + (b - ic)^4 \text{Ei}((b - ic)\sqrt{z}) \right) \right)$$

$$01.06.21.0460.01 \int \frac{e^{b\sqrt{z}} \sin(\sqrt{z} c + g)}{z^4} dz = \frac{1}{720} i e^{-ig} \left( -e^{2ig} \text{Ei}((b + ic)\sqrt{z}) (b + ic)^6 - \frac{1}{z^3} \left( e^{\sqrt{z}(b+ic)+2ig} \left( -2(b + ic)^3 z^{3/2} - (b + ic)^5 z^{5/2} - (b + ic)^4 z^2 - 6(b + ic)^2 z - 24(b + ic)\sqrt{z} - 120 \right) + \frac{1}{z^3} \left( e^{(b-ic)\sqrt{z}} \left( -2(b - ic)^3 z^{3/2} - (b - ic)^5 z^{5/2} - (b - ic)^4 z^2 - 6(b - ic)^2 z - 24(b - ic)\sqrt{z} - 120 \right) + (b - ic)^6 \text{Ei}((b - ic)\sqrt{z}) \right) \right)$$

$$01.06.21.0461.01 \int \frac{e^{b\sqrt{z}} \sin(\sqrt{z} c + g)}{z^5} dz = \frac{1}{40320} \left( i e^{-ig} \left( -e^{2ig} \text{Ei}((b + ic)\sqrt{z}) (b + ic)^8 - \frac{1}{z^4} \left( e^{\sqrt{z}(b+ic)+2ig} \left( -24(b + ic)^3 z^{3/2} - 2(b + ic)^5 z^{5/2} - (b + ic)^7 z^{7/2} - (b + ic)^6 z^3 - 6(b + ic)^4 z^2 - 120(b + ic)^2 z - 720(b + ic)\sqrt{z} - 5040 \right) + \frac{1}{z^4} \left( e^{(b-ic)\sqrt{z}} \left( -24(b - ic)^3 z^{3/2} - 2(b - ic)^5 z^{5/2} - (b - ic)^7 z^{7/2} - (b - ic)^6 z^3 - 6(b - ic)^4 z^2 - 120(b - ic)^2 z - 720(b - ic)\sqrt{z} - 5040 \right) + (b - ic)^8 \text{Ei}((b - ic)\sqrt{z}) \right) \right) \right)$$

Involving  $z^{\alpha-1} e^{bz^r+e} \sin(cz^r + g)$

01.06.21.0462.01

$$\int z^{\alpha-1} e^{b z^r+e} \sin(c z^r+g) dz = -\frac{i z^\alpha}{2 r} \left( e^{-i g} ((i c-b) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (i c-b) z^r\right) - e^{e+i g} (-(b+i c) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -(b+i c) z^r\right) \right)$$

01.06.21.0463.01

$$\int \frac{e^{b z^r+e} \sin(c z^r+g)}{z} dz = e^e \frac{\operatorname{Ei}((b+i c) z^r) (\sin(g)-i \cos(g)) + \operatorname{Ei}((b-i c) z^r) (i \cos(g)+\sin(g))}{2 r}$$

01.06.21.0464.01

$$\int z^{2 n} e^{b z^2+e} \sin(c z^2+g) dz =$$

$$\frac{1}{4} i z e^e \left( e^{i g} ((-b-i c) z^2)^{-\frac{1}{2}} (-b-i c)^{-n} \left( \operatorname{erfc}\left(\sqrt{(-b-i c) z^2}\right) \Gamma\left(n+\frac{1}{2}\right) + e^{-(-b-i c) z^2} \sum_{k=0}^{n-1} \frac{((-b-i c) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} - e^{-(-b-i c) z^2} \sum_{k=n}^{-1} \frac{((-b-i c) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} \right) - e^{-i g} ((i c-b) z^2)^{-\frac{1}{2}} (i c-b)^{-n} \left( \operatorname{erfc}\left(\sqrt{(i c-b) z^2}\right) \Gamma\left(n+\frac{1}{2}\right) + e^{-(-i c-b) z^2} \sum_{k=0}^{n-1} \frac{((i c-b) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} - e^{-(-i c-b) z^2} \sum_{k=n}^{-1} \frac{((i c-b) z^2)^{k+\frac{1}{2}}}{\left(n+\frac{1}{2}\right)_{k-n+1}} \right) \right) / ; n \in \mathbb{Z}$$

01.06.21.0465.01

$$\int z^{2 n-1} e^{b z^2+e} \sin(c z^2+g) dz =$$

$$\frac{1}{4} i e^e \left( e^{i g} (-b-i c)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(-(-b-i c) z^2)}{(-n)!} + e^{-(-b-i c) z^2} \sum_{k=0}^{n-1} \frac{((-b-i c) z^2)^k}{(n)_{k-n+1}} - e^{-(-b-i c) z^2} \sum_{k=n}^{-1} \frac{((-b-i c) z^2)^k}{(n)_{k-n+1}} \right) - e^{-i g} (i c-b)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(-(i c-b) z^2)}{(-n)!} + e^{-(-i c-b) z^2} \sum_{k=0}^{n-1} \frac{((i c-b) z^2)^k}{(n)_{k-n+1}} - e^{-(-i c-b) z^2} \sum_{k=n}^{-1} \frac{((i c-b) z^2)^k}{(n)_{k-n+1}} \right) \right) / ; n \in \mathbb{Z}$$

01.06.21.0466.01

$$\int z e^{b z^2+e} \sin(c z^2+g) dz = \frac{e^{b z^2+e} (b \sin(c z^2+g) - c \cos(c z^2+g))}{2 (b^2+c^2)}$$

01.06.21.0467.01

$$\int z^2 e^{bz^2+e} \sin(cz^2+g) dz = \frac{1}{4} z^3 e^e \left( \frac{\left( \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 1\right) - e^{(b+ic)z^2} \sqrt{-(b+ic)z^2} \right)}{(-b+ic)z^2} + \frac{\left( \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 1\right) - e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} \right)}{(-b-ic)z^2} \right) \sin(g) - i \cos(g) \left( \frac{\left( \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 1\right) - e^{(b+ic)z^2} \sqrt{-(b+ic)z^2} \right)}{(-b+ic)z^2} + \frac{\left( \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 1\right) - e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} - \frac{1}{2} \sqrt{\pi} \left( \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 1\right) \right)}{(-b-ic)z^2} \right) \right)$$

01.06.21.0468.01

$$\int z^3 e^{bz^2+e} \sin(cz^2+g) dz = \frac{1}{2(b^2+c^2)^2} e^{bz^2+e} ((z^2 b^3 - b^2 + c^2 z^2 b + c^2) \sin(cz^2+g) - c(b^2 z^2 + c^2 z^2 - 2b) \cos(cz^2+g))$$

01.06.21.0469.01

$$\int z^4 e^{bz^2+e} \sin(cz^2+g) dz = \frac{1}{16} z^5 e^e \left( \frac{1}{(-b+ic)z^2} \left( 2 e^{(b+ic)z^2} \sqrt{-(b+ic)z^2} (2bz^2 + 2ci z^2 - 3) + 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 3\sqrt{\pi} \right) + \frac{1}{(-b-ic)z^2} \left( 2 e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} (2bz^2 - 2ic z^2 - 3) + 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) - 3\sqrt{\pi} \right) \right) \sin(g) - i \cos(g) \left( \frac{1}{(-b+ic)z^2} \left( 2 e^{(b+ic)z^2} \sqrt{-(b+ic)z^2} (2bz^2 + 2ci z^2 - 3) + 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b+ic)z^2}\right) - 3\sqrt{\pi} \right) + \frac{1}{(-b-ic)z^2} \left( -2 e^{(b-ic)z^2} \sqrt{-(b-ic)z^2} (2bz^2 - 2ic z^2 - 3) - 3\sqrt{\pi} \operatorname{erf}\left(\sqrt{-(b-ic)z^2}\right) + 3\sqrt{\pi} \right) \right) \right)$$

01.06.21.0470.01

$$\int z^5 e^{bz^2+e} \sin(cz^2+g) dz = \frac{1}{2(b^2+c^2)^3} e^{bz^2+e} ((z^4 b^5 - 2z^2 b^4 + 2(c^2 z^4 + 1) b^3 + c^2 (c^2 z^4 - 6) b + 2c^4 z^2) \sin(cz^2+g) - c(b^4 z^4 - 4b^3 z^2 - 4b c^2 z^2 + c^2 (c^2 z^4 - 2) + 2b^2 (c^2 z^4 + 3)) \cos(cz^2+g))$$

01.06.21.0471.01

$$\int \frac{e^{bz^2+e} \sin(cz^2+g)}{z} dz = \frac{1}{4} i e^{e-ig} (\operatorname{Ei}((b-ic)z^2) - e^{2ig} \operatorname{Ei}((b+ic)z^2))$$

01.06.21.0472.01

$$\int \frac{e^{bz^2+e} \sin(cz^2+g)}{z^2} dz = \frac{1}{2z} e^e \left( i\sqrt{\pi} e^{-ig} \left( \sqrt{-(b-ic)z^2} \operatorname{erfc}\left(\sqrt{-(b-ic)z^2}\right) - e^{2ig} \sqrt{-(b+ic)z^2} \operatorname{erfc}\left(\sqrt{-(b+ic)z^2}\right) \right) - 2e^{bz^2} \sin(cz^2+g) \right)$$

01.06.21.0473.01

$$\int \frac{e^{bz^2+e} \sin(cz^2+g)}{z^3} dz = \frac{1}{4} e^e \left( (c-ib) e^{ig} \operatorname{Ei}((b+ic)z^2) + (c+ib) e^{-ig} \operatorname{Ei}((b-ic)z^2) - \frac{2e^{bz^2} \sin(cz^2+g)}{z^2} \right)$$

01.06.21.0474.01

$$\int \frac{e^{bz^2+e} \sin(cz^2+g)}{z^4} dz = -\frac{1}{6z^3} e^e \left( -2i\sqrt{\pi} \cos(g) \left( (b-ic)^{3/2} \operatorname{erfi}\left(\sqrt{b-ic}z\right) - (b+ic)^{3/2} \operatorname{erfi}\left(\sqrt{b+ic}z\right) \right) z^3 - 2\sqrt{\pi} \left( \operatorname{erfi}\left(\sqrt{b+ic}z\right) (b+ic)^{3/2} + (b-ic)^{3/2} \operatorname{erfi}\left(\sqrt{b-ic}z\right) \right) \sin(g) z^3 + (-2i\sqrt{\pi} (-(b+ic)z^2)^{3/2} + 2i\sqrt{\pi} (-(b-ic)z^2)^{3/2} + e^{(b+ic)z^2} (2(c-ib)z^2-i) + e^{(b-ic)z^2} (2(c+ib)z^2+i)) \cos(g) + (2\sqrt{\pi} (-(b+ic)z^2)^{3/2} + 2\sqrt{\pi} (-(b-ic)z^2)^{3/2} + e^{(b+ic)z^2} (2(b+ic)z^2+1) + e^{(b-ic)z^2} (2(b-ic)z^2+1)) \sin(g) \right)$$

01.06.21.0475.01

$$\int \frac{e^{bz^2+e} \sin(cz^2+g)}{z^5} dz = \frac{1}{8z^4} e^e \left( (b+ic)^2 \operatorname{Ei}((b+ic)z^2) (\sin(g) - i \cos(g)) z^4 + (b-ic)^2 \operatorname{Ei}((b-ic)z^2) (i \cos(g) + \sin(g)) z^4 + e^{(b-ic)z^2} i \left( (-bz^2 + ciz^2 + e^{2ic}z^2 (bz^2 + ciz^2 + 1) - 1 \right) \cos(g) - \left( e^{2ic}z^2 (-ibz^2 + cz^2 - i) - i(bz^2 - icz^2 + 1) \right) \sin(g) \right)$$

01.06.21.0476.01

$$\int z^n e^{b\sqrt{z}+e} \sin(\sqrt{z}c+g) dz = i e^{e+ig} (-b-ic)^{-2(n+1)} \left( -\frac{\operatorname{Ei}(-(-b-ic)\sqrt{z})}{(-2(n+1))!} + e^{-(-b-ic)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((-b-ic)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} - e^{-(-b-ic)\sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{((-b-ic)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} \right) - i e^{e-ig} \left( (ic-b)^{-2(n+1)} \left( -\frac{\operatorname{Ei}(-(ic-b)\sqrt{z})}{(-2(n+1))!} + e^{-(ic-b)\sqrt{z}} \sum_{k=0}^{2n+1} \frac{((ic-b)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} - e^{-(ic-b)\sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{((ic-b)\sqrt{z})^k}{(2(n+1))_{k-2n-1}} \right) \right); n \in \mathbb{Z}$$

01.06.21.0477.01

$$\int z e^{b\sqrt{z}+e} \sin(\sqrt{z}c+g) dz = \frac{1}{(b^2+c^2)^4} 2e^{b\sqrt{z}+e} \left( (b(b^2+c^2)^3 z^{3/2} - 3(b-c)(b+c)(b^2+c^2)^2 z + 6b(b^2+c^2)(b^2-3c^2)\sqrt{z} - 6(b^4-6c^2b^2+c^4)) \sin(\sqrt{z}c+g) - c((b^2+c^2)^3 z^{3/2} - 6b(b^2+c^2)^2 z + 6(3b^2-c^2)(b^2+c^2)\sqrt{z} - 24b(b-c)(b+c)) \cos(\sqrt{z}c+g) \right)$$

01.06.21.0478.01

$$\int z^2 e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^6} 2 e^{b\sqrt{z}+e} \left( (20 b (b^2 + c^2)^3 (b^2 - 3 c^2) z^{3/2} + b (b^2 + c^2)^5 z^{5/2} - 5 (b - c) (b + c) (b^2 + c^2)^4 z^2 - 60 (b^2 + c^2)^2 (b^4 - 6 c^2 b^2 + c^4) z + 120 b (b^2 + c^2) (b^4 - 10 c^2 b^2 + 5 c^4) \sqrt{z} - 120 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) \right) \sin(\sqrt{z} c + g) - c \left( 20 (3 b^2 - c^2) (b^2 + c^2)^3 z^{3/2} + (b^2 + c^2)^5 z^{5/2} - 10 b (b^2 + c^2)^4 z^2 - 240 b (b - c) (b + c) (b^2 + c^2)^2 z + 120 (b^2 + c^2) (5 b^4 - 10 c^2 b^2 + c^4) \sqrt{z} - 240 b (3 b^4 - 10 c^2 b^2 + 3 c^4) \right) \cos(\sqrt{z} c + g) \right)$$

01.06.21.0479.01

$$\int z^3 e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^8} 2 e^{b\sqrt{z}+e} \left( (840 b (b^2 + c^2)^3 (b^4 - 10 c^2 b^2 + 5 c^4) z^{3/2} + 42 b (b^2 + c^2)^5 (b^2 - 3 c^2) z^{5/2} + b (b^2 + c^2)^7 z^{7/2} - 7 (b - c) (b + c) (b^2 + c^2)^6 z^3 - 210 (b^2 + c^2)^4 (b^4 - 6 c^2 b^2 + c^4) z^2 - 2520 (b^2 + c^2)^2 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) z + 5040 b (b^2 + c^2) (b^6 - 21 c^2 b^4 + 35 c^4 b^2 - 7 c^6) \sqrt{z} - 5040 (b^8 - 28 c^2 b^6 + 70 c^4 b^4 - 28 c^6 b^2 + c^8) \right) \sin(\sqrt{z} c + g) - c \left( 840 (b^2 + c^2)^3 (5 b^4 - 10 c^2 b^2 + c^4) z^{3/2} + 42 (3 b^2 - c^2) (b^2 + c^2)^5 z^{5/2} + (b^2 + c^2)^7 z^{7/2} - 14 b (b^2 + c^2)^6 z^3 - 840 b (b - c) (b + c) (b^2 + c^2)^4 z^2 - 5040 b (b^2 + c^2)^2 (3 b^4 - 10 c^2 b^2 + 3 c^4) z + 5040 (b^2 + c^2) (7 b^6 - 35 c^2 b^4 + 21 c^4 b^2 - c^6) \sqrt{z} - 40320 b (b^6 - 7 c^2 b^4 + 7 c^4 b^2 - c^6) \right) \cos(\sqrt{z} c + g) \right)$$

01.06.21.0480.01

$$\int z^4 e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^{10}} 2 e^{b\sqrt{z}+e} \left( (60480 b (b^2 + c^2)^3 (b^6 - 21 c^2 b^4 + 35 c^4 b^2 - 7 c^6) z^{3/2} + 3024 b (b^2 + c^2)^5 (b^4 - 10 c^2 b^2 + 5 c^4) z^{5/2} + 72 b (b^2 + c^2)^7 (b^2 - 3 c^2) z^{7/2} + b (b^2 + c^2)^9 z^{9/2} - 9 (b - c) (b + c) (b^2 + c^2)^8 z^4 - 504 (b^2 + c^2)^6 (b^4 - 6 c^2 b^2 + c^4) z^3 - 15120 (b^2 + c^2)^4 (b^6 - 15 c^2 b^4 + 15 c^4 b^2 - c^6) z^2 - 181440 (b^2 + c^2)^2 (b^8 - 28 c^2 b^6 + 70 c^4 b^4 - 28 c^6 b^2 + c^8) z + 362880 b (b^2 + c^2) (b^2 - 3 c^2) (b^6 - 33 c^2 b^4 + 27 c^4 b^2 - 3 c^6) \sqrt{z} - 362880 (b^{10} - 45 c^2 b^8 + 210 c^4 b^6 - 210 c^6 b^4 + 45 c^8 b^2 - c^{10}) \right) \sin(\sqrt{z} c + g) - c \left( 60480 (b^2 + c^2)^3 (7 b^6 - 35 c^2 b^4 + 21 c^4 b^2 - c^6) z^{3/2} + 3024 (b^2 + c^2)^5 (5 b^4 - 10 c^2 b^2 + c^4) z^{5/2} + 72 (3 b^2 - c^2) (b^2 + c^2)^7 z^{7/2} + (b^2 + c^2)^9 z^{9/2} - 18 b (b^2 + c^2)^8 z^4 - 2016 b (b - c) (b + c) (b^2 + c^2)^6 z^3 - 30240 b (b^2 + c^2)^4 (3 b^4 - 10 c^2 b^2 + 3 c^4) z^2 - 1451520 b (b^2 + c^2)^2 (b^6 - 7 c^2 b^4 + 7 c^4 b^2 - c^6) z + 362880 (9 b^{10} - 75 c^2 b^8 + 42 c^4 b^6 + 90 c^6 b^4 - 35 c^8 b^2 + c^{10}) \sqrt{z} - 725760 b (5 b^4 - 10 c^2 b^2 + c^4) (b^4 - 10 c^2 b^2 + 5 c^4) \right) \cos(\sqrt{z} c + g) \right)$$

01.06.21.0481.01

$$\int z^5 e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g) dz = \frac{1}{(b^2 + c^2)^{12}}$$

$$\begin{aligned} & \left( 2 e^{b\sqrt{z}+e} \left( (330 b^{15} (z^4 c^8 - 8 z^3 c^6 - 1056 z^2 c^4 - 16128 z c^2 + 20160) z^{3/2} + 165 b^{17} (z^3 c^6 + 6 z^2 c^4 - 144 z c^2 + 2016) z^{5/2} + \right. \right. \\ & \quad 55 b^{19} (z^2 c^4 + 12 z c^2 + 144) z^{7/2} + 11 b^{21} (z c^2 + 10) z^{9/2} + b^{23} z^{11/2} - 11 b^{22} z^5 - 99 b^{20} (z c^2 + 10) z^4 - \\ & \quad 55 b^{18} (7 z^2 c^4 + 36 z c^2 + 1008) z^3 - 165 b^{16} (5 z^3 c^6 - 114 z^2 c^4 - 3024 z c^2 + 10080) z^2 - \\ & \quad 990 b^{14} (z^4 c^8 - 104 z^3 c^6 - 3360 z^2 c^4 - 40320 z c^2 + 20160) z + \\ & \quad 462 b^{13} (z^5 c^{10} - 30 z^4 c^8 - 2400 z^3 c^6 - 43200 z^2 c^4 - 475200 z c^2 + 86400) \sqrt{z} + \\ & \quad 462 b^{11} c^2 (z^5 c^{10} - 60 z^4 c^8 - 3600 z^3 c^6 - 23040 z^2 c^4 + 302400 z c^2 - 4665600) \sqrt{z} + \\ & \quad 330 b^9 c^4 (z^5 c^{10} - 98 z^4 c^8 - 3696 z^3 c^6 + 110880 z^2 c^4 + 3769920 z c^2 + 33264000) \sqrt{z} + \\ & \quad 165 b^7 c^6 (z^5 c^{10} - 144 z^4 c^8 - 1344 z^3 c^6 + 354816 z^2 c^4 + 3991680 z c^2 - 31933440) \sqrt{z} + \\ & \quad 55 b^5 c^8 (z^5 c^{10} - 198 z^4 c^8 + 5184 z^3 c^6 + 508032 z^2 c^4 - 11975040 z c^2 - 215550720) \sqrt{z} + \\ & \quad 11 b^3 c^{10} (z^5 c^{10} - 260 z^4 c^8 + 18000 z^3 c^6 - 34473600 z c^2 + 558835200) \sqrt{z} + \\ & \quad b c^{12} (z^5 c^{10} - 330 z^4 c^8 + 39600 z^3 c^6 - 2328480 z^2 c^4 + 59875200 z c^2 - 439084800) \sqrt{z} + \\ & \quad 990 b^8 c^4 (z^5 c^{10} + 238 z^4 c^8 - 3696 z^3 c^6 - 332640 z^2 c^4 - 3326400 z c^2 - 19958400) + \\ & \quad 462 b^{10} c^2 (z^5 c^{10} + 660 z^4 c^8 + 7920 z^3 c^6 - 316800 z^2 c^4 - 5227200 z c^2 + 5702400) + \\ & \quad 99 b^2 c^{10} (z^5 c^{10} - 20 z^4 c^8 - 5040 z^3 c^6 + 403200 z^2 c^4 - 8668800 z c^2 + 26611200) + \\ & \quad 11 c^{12} (z^5 c^{10} - 90 z^4 c^8 + 5040 z^3 c^6 - 151200 z^2 c^4 + 1814400 z c^2 - 3628800) - \\ & \quad 462 b^{12} (z^5 c^{10} - 510 z^4 c^8 - 13920 z^3 c^6 - 129600 z^2 c^4 - 1857600 z c^2 + 86400) + \\ & \quad 165 b^6 c^6 (5 z^5 c^{10} + 624 z^4 c^8 - 38976 z^3 c^6 - 887040 z^2 c^4 + 19958400 z c^2 + 223534080) + \\ & \quad \left. 55 b^4 c^8 (7 z^5 c^{10} + 342 z^4 c^8 - 60480 z^3 c^6 + 1088640 z^2 c^4 + 43908480 z c^2 - 359251200) \right) \sin(\sqrt{z} c + g) - \\ & c \left( 330 b^{14} (z^4 c^8 + 72 z^3 c^6 + 864 z^2 c^4 + 181440) z^{3/2} + 165 b^{16} (z^3 c^6 + 66 z^2 c^4 + 1200 z c^2 + 14112) z^{5/2} + \right. \\ & \quad 55 b^{18} (z^2 c^4 + 52 z c^2 + 720) z^{7/2} + 11 b^{20} (z c^2 + 30) z^{9/2} + b^{22} z^{11/2} - 22 b^{21} z^5 - 220 b^{19} (z c^2 + 18) z^4 - \\ & \quad 990 b^{17} (z^2 c^4 + 28 z c^2 + 336) z^3 - 2640 b^{15} (z^3 c^6 + 30 z^2 c^4 + 336 z c^2 + 5040) z^2 - \\ & \quad 4620 b^{13} (z^4 c^8 + 24 z^3 c^6 - 288 z^2 c^4 - 8640 z c^2 + 43200) z + \\ & \quad 165 b^6 c^6 (z^5 c^{10} + 16 z^4 c^8 - 6720 z^3 c^6 + 64512 z^2 c^4 + 7539840 z c^2 + 31933440) \sqrt{z} + \\ & \quad 330 b^8 c^4 (z^5 c^{10} + 42 z^4 c^8 - 5040 z^3 c^6 - 110880 z^2 c^4 + 1995840 z c^2 + 35925120) \sqrt{z} + \\ & \quad 462 b^{10} c^2 (z^5 c^{10} + 60 z^4 c^8 - 2640 z^3 c^6 - 126720 z^2 c^4 - 1425600 z c^2 - 13305600) \sqrt{z} + \\ & \quad 462 b^{12} (z^5 c^{10} + 70 z^4 c^8 - 480 z^3 c^6 - 60480 z^2 c^4 - 820800 z c^2 + 950400) \sqrt{z} + \\ & \quad 55 b^4 c^8 (z^5 c^{10} - 18 z^4 c^8 - 6336 z^3 c^6 + 362880 z^2 c^4 + 2540160 z c^2 - 199584000) \sqrt{z} + \\ & \quad 11 b^2 c^{10} (z^5 c^{10} - 60 z^4 c^8 - 2160 z^3 c^6 + 483840 z^2 c^4 - 19958400 z c^2 + 195955200) \sqrt{z} + \\ & \quad c^{12} (z^5 c^{10} - 110 z^4 c^8 + 7920 z^3 c^6 - 332640 z^2 c^4 + 6652800 z c^2 - 39916800) \sqrt{z} - \\ & \quad 5544 b^{11} (z^5 c^{10} + 10 z^4 c^8 - 1440 z^3 c^6 - 36000 z^2 c^4 - 360000 z c^2 + 86400) - \\ & \quad 4620 b^9 c^2 (z^5 c^{10} - 12 z^4 c^8 - 2640 z^3 c^6 - 31680 z^2 c^4 + 95040 z c^2 - 1900800) - \\ & \quad 2640 b^7 c^4 (z^5 c^{10} - 42 z^4 c^8 - 3024 z^3 c^6 + 55440 z^2 c^4 + 1995840 z c^2 + 11975040) - \\ & \quad 990 b^5 c^6 (z^5 c^{10} - 80 z^4 c^8 - 1344 z^3 c^6 + 201600 z^2 c^4 + 443520 z c^2 - 31933440) - \\ & \quad 220 b^3 c^8 (z^5 c^{10} - 126 z^4 c^8 + 4032 z^3 c^6 + 181440 z^2 c^4 - 9072000 z c^2 + 39916800) - \\ & \quad \left. 22 b c^{10} (z^5 c^{10} - 180 z^4 c^8 + 15120 z^3 c^6 - 604800 z^2 c^4 + 9072000 z c^2 - 21772800) \right) \cos(\sqrt{z} c + g) \end{aligned}$$



$$\int \frac{e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g)}{z} dz = i e^{e-ig} \left( \text{Ei}((b-ic)\sqrt{z}) - e^{2ig} \text{Ei}((b+ic)\sqrt{z}) \right)$$

$$\int \frac{e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g)}{z^2} dz = \frac{1}{2z} i e^{e-ig} \left( -e^{2ig} z \text{Ei}((b+ic)\sqrt{z}) (b+ic)^2 + e^{(b-ic)\sqrt{z}} \left( -\sqrt{z} b + e^{2i(\sqrt{z} c+g)} (\sqrt{z} b + ic\sqrt{z} + 1) + ic\sqrt{z} - 1 \right) + (b-ic)^2 z \text{Ei}((b-ic)\sqrt{z}) \right)$$

$$\int \frac{e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g)}{z^3} dz = \frac{1}{24} i e^{e-ig} \left( -e^{2ig} \text{Ei}((b+ic)\sqrt{z}) (b+ic)^4 + \frac{1}{z^2} \left( e^{(b-ic)\sqrt{z}} \left( -b^3 z^{3/2} - ic^3 z^{3/2} + c^2 z + 2ic\sqrt{z} + b(3zc^2 + 2i\sqrt{z}c - 2) \sqrt{z} + b^2(3ic z^{3/2} - z) - 6 \right) + \frac{1}{z^2} \left( e^{\sqrt{z}(b+ic)+2ig} \left( b^3 z^{3/2} - ic^3 z^{3/2} - c^2 z + 2ic\sqrt{z} + b^2(3ic z^{3/2} + z) + b(-3c^2 z^{3/2} + 2icz + 2\sqrt{z}) + 6 \right) + (b-ic)^4 \text{Ei}((b-ic)\sqrt{z}) \right) \right)$$

$$\int \frac{e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g)}{z^4} dz = \frac{1}{720} i e^{e-ig} \left( -e^{2ig} \text{Ei}((b+ic)\sqrt{z}) (b+ic)^6 - \frac{1}{z^3} \left( e^{\sqrt{z}(b+ic)+2ig} \left( -2(b+ic)^3 z^{3/2} - (b+ic)^5 z^{5/2} - (b+ic)^4 z^2 - 6(b+ic)^2 z - 24(b+ic)\sqrt{z} - 120 \right) + \frac{1}{z^3} \left( e^{(b-ic)\sqrt{z}} \left( -2(b-ic)^3 z^{3/2} - (b-ic)^5 z^{5/2} - (b-ic)^4 z^2 - 6(b-ic)^2 z - 24(b-ic)\sqrt{z} - 120 \right) + (b-ic)^6 \text{Ei}((b-ic)\sqrt{z}) \right) \right)$$

$$\int \frac{e^{b\sqrt{z}+e} \sin(\sqrt{z} c + g)}{z^5} dz = \frac{1}{40320} \left( i e^{e-ig} \left( -e^{2ig} \text{Ei}((b+ic)\sqrt{z}) (b+ic)^8 - \frac{1}{z^4} \left( e^{\sqrt{z}(b+ic)+2ig} \left( -24(b+ic)^3 z^{3/2} - 2(b+ic)^5 z^{5/2} - (b+ic)^7 z^{7/2} - (b+ic)^6 z^3 - 6(b+ic)^4 z^2 - 120(b+ic)^2 z - 720(b+ic)\sqrt{z} - 5040 \right) + \frac{1}{z^4} \left( e^{(b-ic)\sqrt{z}} \left( -24(b-ic)^3 z^{3/2} - 2(b-ic)^5 z^{5/2} - (b-ic)^7 z^{7/2} - (b-ic)^6 z^3 - 6(b-ic)^4 z^2 - 120(b-ic)^2 z - 720(b-ic)\sqrt{z} - 5040 \right) + (b-ic)^8 \text{Ei}((b-ic)\sqrt{z}) \right) \right) \right)$$

Involving  $z^n e^{bz^r+dz} \sin(cz^r + g)$

01.06.21.0487.01

$$\int z^n e^{b z^2 + d z} \sin(c z^2 + g) dz =$$

$$\frac{1}{4 \sqrt{b + i c}} \left( i e^{-\frac{d^2}{4(b+i c)} + i g} \sum_{q=0}^n 2^{q-n} (b + i c)^{-n-\frac{1}{2}} (-d)^{n-q} (d + 2(b + i c) z)^{q+1} \left( -\frac{(d + 2(b + i c) z)^2}{b + i c} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2(b + i c) z)^2}{4(b + i c)}\right) - \frac{1}{4 \sqrt{b - i c}} \left( i e^{-\frac{d^2}{4(b-i c)} - i g} \sum_{q=0}^n 2^{q-n} (b - i c)^{-n-\frac{1}{2}} (-d)^{n-q} \right.$$

$$\left. (d + 2 b z - 2 i c z)^{q+1} \left( -\frac{(d + 2 b z - 2 i c z)^2}{b - i c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 b z - 2 i c z)^2}{4(b - i c)}\right) \right) / ; n \in \mathbb{N}$$

01.06.21.0488.01

$$\int z^n e^{\sqrt{z} b + d z} \sin(\sqrt{z} c + g) dz =$$

$$i 2^{-2(n+1)} e^{-i g} \left( d^{-2(n+1)} e^{-\frac{(b-i c)^2}{4 d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b - i c)^{-h-k+2n} (b - i c + 2 d \sqrt{z})^{h+k} \left( -\frac{(b - i c + 2 d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b - i c)(b - i c + 2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b - i c + 2 d \sqrt{z})^2}{4 d}\right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b - i c + 2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b - i c + 2 d \sqrt{z})^2}{4 d}\right) \right) -$$

$$d^{-2(n+1)} e^{2 i g - \frac{(b+i c)^2}{4 d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b + i c)^{-h-k+2n} (b + i c + 2 d \sqrt{z})^{h+k} \left( -\frac{(b + i c + 2 d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b + i c)(b + i c + 2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + i c + 2 d \sqrt{z})^2}{4 d}\right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b + i c + 2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b + i c + 2 d \sqrt{z})^2}{4 d}\right) \right) / ; n \in \mathbb{N}$$

### Involving $z^n e^{bz^r+dz+e} \sin(cz^r + g)$

01.06.21.0489.01

$$\int z^n e^{bz^2+dz+e} \sin(cz^2 + g) dz =$$

$$\frac{1}{4\sqrt{b+ic}} \left( i e^{-\frac{d^2}{4(b+ic)}+e+ig} \sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-d)^{n-q} (d+2(b+ic)z)^{q+1} \left( -\frac{(d+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b+ic)z)^2}{4(b+ic)}\right) \right) - \frac{1}{4\sqrt{b-ic}} \left( i e^{-\frac{d^2}{4(b-ic)}+e-ig} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (-d)^{n-q} \right. \\ \left. (d+2bz-2icz)^{q+1} \left( -\frac{(d+2bz-2icz)^2}{b-ic} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz-2icz)^2}{4(b-ic)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0490.01

$$\int z^n e^{\sqrt{z}} b+dz+e \sin(\sqrt{z} c+g) dz =$$

$$i 2^{-2(n+1)} e^{e-ig} \left( d^{-2(n+1)} e^{-\frac{(b-ic)^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2d\sqrt{z})^{h+k} \left( -\frac{(b-ic+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b-ic+2d\sqrt{z})^2}{4d}\right) \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b-ic+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b-ic+2d\sqrt{z})^2}{4d}\right) \right) -$$

$$d^{-2(n+1)} e^{2ig-\frac{(b+ic)^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2d\sqrt{z})^{h+k} \left( -\frac{(b+ic+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b+ic)(b+ic+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ic+2d\sqrt{z})^2}{4d}\right) \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b+ic+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ic+2d\sqrt{z})^2}{4d}\right) \right) \Bigg) ; n \in \mathbb{N}$$

### Involving exponential and algebraic functions

Involving exp and algebraic functions

### Involving $(az+b)^\beta dz$

01.06.21.0491.01

$$\int (az+b)^\beta dz \sin(cz+e) dz =$$

$$\frac{1}{2a} i d^{-\frac{b}{a}} e^{-\frac{i(bc+ae)}{a}} (b+az)^{\beta+1} \left( e^{2ie} E_{-\beta} \left( -\frac{i(b+az)(c-i \log(d))}{a} \right) - e^{\frac{2ibc}{a}} E_{-\beta} \left( \frac{i(b+az)(c+i \log(d))}{a} \right) \right)$$

01.06.21.0492.01

$$\int (az+b)^\beta e^{pz} \sin(cz+e) dz = \frac{i e^{-\frac{i(bc+ae)+bp}{a}} (b+az)^{\beta+1}}{2a} \left( e^{2ie} E_{-\beta} \left( -\frac{i(c-ip)(b+az)}{a} \right) - e^{\frac{2ibc}{a}} E_{-\beta} \left( \frac{i(c+ip)(b+az)}{a} \right) \right)$$

01.06.21.0493.01

$$\int (az + b)^\beta d^z \sin(cz) dz = \frac{id^{-\frac{b}{a}}}{2a} e^{-\frac{ibc}{a}} (b + az)^{\beta+1} \left( E_{-\beta} \left( -\frac{i(b+az)(c-i \log(d))}{a} \right) - e^{\frac{2ibc}{a}} E_{-\beta} \left( \frac{i(b+az)(c+i \log(d))}{a} \right) \right)$$

01.06.21.0494.01

$$\int (az + b)^\beta e^{pz} \sin(cz) dz = \frac{i}{2a} e^{-\frac{b(i+c+p)}{a}} (b + az)^{\beta+1} \left( E_{-\beta} \left( -\frac{i(c-ip)(b+az)}{a} \right) - e^{\frac{2ibc}{a}} E_{-\beta} \left( \frac{i(c+ip)(b+az)}{a} \right) \right)$$

01.06.21.0495.01

$$\int \frac{e^{pz} \sin(cz)}{\sqrt{az+b}} dz = \frac{1}{2(c^2+p^2)\sqrt{b+az}} e^{-\frac{b(i+c+p)}{a}} \sqrt{\pi} \left( -e^{\frac{2ibc}{a}} (c-ip) \sqrt{\frac{i(c+ip)(b+az)}{a}} \operatorname{erfc} \left( \sqrt{\frac{i(c+ip)(b+az)}{a}} \right) + \sqrt{-\frac{i(c-ip)(b+az)}{a}} (-c+ip) \operatorname{erfc} \left( \sqrt{-\frac{i(c-ip)(b+az)}{a}} \right) \right)$$

### Arguments involving polynomials

#### Involving $az^2 + bz + c$

01.06.21.0496.01

$$\int \sin(az^2 + bz + c) dz = \frac{1}{\sqrt{a}} \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{b^2}{4a} - c\right) S\left(\frac{b+2az}{\sqrt{a}\sqrt{2\pi}}\right) - C\left(\frac{b+2az}{\sqrt{a}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4a} - c\right) \right)$$

#### Involving $az^2 + bz$

01.06.21.0497.01

$$\int \sin(az^2 + bz) dz = \frac{1}{\sqrt{a}} \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{b^2}{4a}\right) S\left(\frac{b+2az}{\sqrt{a}\sqrt{2\pi}}\right) - C\left(\frac{b+2az}{\sqrt{a}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4a}\right) \right)$$

#### Involving $az^2 + c$

01.06.21.0498.01

$$\int \sin(az^2 + c) dz = \frac{1}{\sqrt{a}} \sqrt{\frac{\pi}{2}} \left( \cos(c) S\left(\sqrt{a}\sqrt{\frac{2}{\pi}}z\right) + C\left(\sqrt{a}\sqrt{\frac{2}{\pi}}z\right) \sin(c) \right)$$

### Arguments involving rational functions

#### Involving $az^2 + \frac{b}{z^2}$

01.06.21.0499.01

$$\int \sin\left(az^2 + \frac{b}{z^2}\right) dz =$$

$$-\frac{1}{8} i \sqrt{\pi} \left[ \frac{1}{\sqrt{-ia}} \left( e^{-2\sqrt{-ia}\sqrt{-ib}} \left( e^{4\sqrt{-ia}\sqrt{-ib}} \left( \operatorname{erf}\left(\sqrt{-ia}z + \frac{\sqrt{-ib}}{z}\right) - 1 \right) - \operatorname{erf}\left(\frac{\sqrt{-ib}}{z} - \sqrt{-ia}z\right) + 1 \right) \right) + \right.$$

$$\left. \frac{e^{-2\sqrt{ia}\sqrt{ib}} \left( -e^{4\sqrt{ia}\sqrt{ib}} \left( \operatorname{erf}\left(\sqrt{ia}z + \frac{\sqrt{ib}}{z}\right) - 1 \right) + \operatorname{erf}\left(\frac{\sqrt{ib}}{z} - \sqrt{ia}z\right) - 1 \right) \right)}{\sqrt{ia}} \right]$$

Involving  $az^2 + \frac{b}{z^2} + c$

01.06.21.0500.01

$$\int \sin\left(az^2 + \frac{b}{z^2} + c\right) dz =$$

$$-\frac{1}{8} i e^{-ic} \sqrt{\pi} \left[ \frac{1}{\sqrt{-ia}} \left( e^{-2\sqrt{-ia}\sqrt{-ib} + 2ic} \left( e^{4\sqrt{-ia}\sqrt{-ib}} \left( \operatorname{erf}\left(\sqrt{-ia}z + \frac{\sqrt{-ib}}{z}\right) - 1 \right) - \operatorname{erf}\left(\frac{\sqrt{-ib}}{z} - \sqrt{-ia}z\right) + 1 \right) \right) + \right.$$

$$\left. \frac{e^{-2\sqrt{ia}\sqrt{ib}} \left( -e^{4\sqrt{ia}\sqrt{ib}} \left( \operatorname{erf}\left(\sqrt{ia}z + \frac{\sqrt{ib}}{z}\right) - 1 \right) + \operatorname{erf}\left(\frac{\sqrt{ib}}{z} - \sqrt{ia}z\right) - 1 \right) \right)}{\sqrt{ia}} \right]$$

### Arguments involving algebraic functions

Involving  $az + b\sqrt{z} + c$

01.06.21.0501.01

$$\int \sin(az + \sqrt{z}b + c) dz =$$

$$-\frac{1}{2a^{3/2}} \left( 2\sqrt{a} \cos(\sqrt{z}b + c + az) + b\sqrt{2\pi} \cos\left(\frac{b^2}{4a} - c\right) S\left(\frac{2\sqrt{z}a + b}{\sqrt{a}\sqrt{2\pi}}\right) - b\sqrt{2\pi} C\left(\frac{2\sqrt{z}a + b}{\sqrt{a}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4a} - c\right) \right)$$

Involving  $az + b\sqrt{z}$

01.06.21.0502.01

$$\int \sin(\sqrt{z}b + az) dz = -\frac{\cos(\sqrt{z}b + az)}{a} - \frac{b}{a^{3/2}} \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{b^2}{4a}\right) S\left(\frac{2\sqrt{z}a + b}{\sqrt{a}\sqrt{2\pi}}\right) - C\left(\frac{2\sqrt{z}a + b}{\sqrt{a}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4a}\right) \right)$$

### Involving $az^r + c$

01.06.21.0503.01

$$\int \sin(az^r + c) dz = \frac{i}{2r} \left( e^{ic} z (-ia z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -ia z^r\right) - e^{-ic} z (ia z^r)^{-1/r} \Gamma\left(\frac{1}{r}, ia z^r\right) \right)$$

01.06.21.0504.01

$$\int \sin(az^2 + c) dz = \frac{1}{\sqrt{a}} \sqrt{\frac{\pi}{2}} \left( \cos(c) S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) + C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} z\right) \sin(c) \right)$$

01.06.21.0505.01

$$\int \sin(\sqrt{z} a + c) dz = \frac{2 \sin(\sqrt{z} a + c) - 2 a \sqrt{z} \cos(\sqrt{z} a + c)}{a^2}$$

### Arguments involving exponential functions

01.06.21.0506.01

$$\int \sin(a^z) dz = \frac{\text{Si}(a^z)}{\log(a)}$$

01.06.21.0507.01

$$\int \sin(e^z) dz = \text{Si}(e^z)$$

### Arguments involving trigonometric functions

#### Involving tan

01.06.21.0508.01

$$\int \sin(\tan(z)) dz = \frac{1}{4e} \left( (-1 + e^2) \text{Ci}(i - \tan(z)) + (-1 + e^2) \text{Ci}(i + \tan(z)) + (1 + e^2) i (\text{Si}(i - \tan(z)) + \text{Si}(i + \tan(z))) \right)$$

01.06.21.0509.01

$$\int \sin(a \tan(z)) dz = \frac{1}{2} \left( \text{Ci}(-a(-i + \tan(z))) \sinh(a) + \text{Ci}(a(i + \tan(z))) \sinh(a) + i \cosh(a) (\text{Si}(a(i + \tan(z))) + \text{Si}(i a - a \tan(z))) \right)$$

#### Involving cot

01.06.21.0510.01

$$\int \sin(\cot(z)) dz = -\frac{1}{4e} \left( (-1 + e^2) \text{Ci}(i - \cot(z)) + (-1 + e^2) \text{Ci}(i + \cot(z)) + (1 + e^2) i (\text{Si}(i - \cot(z)) + \text{Si}(i + \cot(z))) \right)$$

01.06.21.0511.01

$$\int \sin(a \cot(z)) dz = \frac{1}{2} \left( -\text{Ci}(-a(-i + \cot(z))) \sinh(a) - \text{Ci}(a(i + \cot(z))) \sinh(a) - i \cosh(a) (\text{Si}(a(i + \cot(z))) + \text{Si}(i a - a \cot(z))) \right)$$

### Arguments involving hyperbolic functions

#### Involving tanh

$$\int \sin(\tanh(z)) dz = \frac{1}{2} (-\text{Ci}(1 - \tanh(z)) \sin(1) - \text{Ci}(\tanh(z) + 1) \sin(1) + \cos(1) (\text{Si}(1 - \tanh(z)) + \text{Si}(\tanh(z) + 1)))$$

$$\int \sin(a \tanh(z)) dz = \frac{1}{2} (-\text{Ci}(\tanh(z) a + a) \sin(a) - \text{Ci}(a - a \tanh(z)) \sin(a) + \cos(a) (\text{Si}(\tanh(z) a + a) + \text{Si}(a - a \tanh(z))))$$

### Involving coth

$$\int \sin(\coth(z)) dz = \frac{1}{2} (-\text{Ci}(1 - \coth(z)) \sin(1) - \text{Ci}(\coth(z) + 1) \sin(1) + \cos(1) (\text{Si}(1 - \coth(z)) + \text{Si}(\coth(z) + 1)))$$

$$\int \sin(a \coth(z)) dz = \frac{1}{2} (-\text{Ci}(\coth(z) a + a) \sin(a) - \text{Ci}(a - a \coth(z)) \sin(a) + \cos(a) (\text{Si}(\coth(z) a + a) + \text{Si}(a - a \coth(z))))$$

## Arguments involving inverse trigonometric functions

### Involving $\sin^{-1}$

$$\int \sin(\sin^{-1}(z)) dz = \frac{z^2}{2}$$

$$\int \sin(a \sin^{-1}(z)) dz = \frac{\cos((a-1) \sin^{-1}(z))}{2-2a} - \frac{\cos((a+1) \sin^{-1}(z))}{2(a+1)}$$

### Involving $\cos^{-1}$

$$\int \sin(\cos^{-1}(z)) dz = \frac{1}{2} (\sqrt{1-z^2} z + \sin^{-1}(z))$$

$$\int \sin(a \cos^{-1}(z)) dz = \frac{1}{2} \left( \frac{\sin((a+1) \cos^{-1}(z))}{a+1} + \frac{\sin(\cos^{-1}(z) - a \cos^{-1}(z))}{a-1} \right)$$

### Involving $\tan^{-1}$

$$\int \sin(\tan^{-1}(z)) dz = \sqrt{z^2 + 1}$$



01.06.21.0521.01

$$\int \sin(a \tan^{-1}(z)) dz = \frac{1}{2(a^2 - 4)} e^{-ia \tan^{-1}(z)} \left( (a-2) \left( (a+2) \left( -i \left( -1 + e^{2ia \tan^{-1}(z)} \right) z - e^{2ia \tan^{-1}(z)} {}_2F_1 \left( \frac{a}{2}, 1; \frac{a}{2} + 1; -e^{2ia \tan^{-1}(z)} \right) + {}_2F_1 \left( -\frac{a}{2}, 1; 1 - \frac{a}{2}; -e^{2ia \tan^{-1}(z)} \right) \right) + a e^{2i(a+1) \tan^{-1}(z)} {}_2F_1 \left( \frac{a}{2} + 1, 1; \frac{a}{2} + 2; -e^{2ia \tan^{-1}(z)} \right) \right) - a(a+2) e^{2ia \tan^{-1}(z)} {}_2F_1 \left( 1 - \frac{a}{2}, 1; 2 - \frac{a}{2}; -e^{2ia \tan^{-1}(z)} \right) \right)$$

### Involving $\cot^{-1}$

01.06.21.0522.01

$$\int \sin(\cot^{-1}(z)) dz = \frac{\sqrt{1 + \frac{1}{z^2}} z \sinh^{-1}(z)}{\sqrt{z^2 + 1}}$$

01.06.21.0523.01

$$\int \sin(a \cot^{-1}(z)) dz = \frac{1}{2(a^2 - 4)} e^{-ia \cot^{-1}(z)} \left( (a-2) \left( (a+2) \left( -i \left( -1 + e^{2ia \cot^{-1}(z)} \right) z + e^{2ia \cot^{-1}(z)} {}_2F_1 \left( \frac{a}{2}, 1; \frac{a}{2} + 1; e^{2ia \cot^{-1}(z)} \right) - {}_2F_1 \left( -\frac{a}{2}, 1; 1 - \frac{a}{2}; e^{2ia \cot^{-1}(z)} \right) \right) + a e^{2i(a+1) \cot^{-1}(z)} {}_2F_1 \left( \frac{a}{2} + 1, 1; \frac{a}{2} + 2; e^{2ia \cot^{-1}(z)} \right) \right) - a(a+2) e^{2ia \cot^{-1}(z)} {}_2F_1 \left( 1 - \frac{a}{2}, 1; 2 - \frac{a}{2}; e^{2ia \cot^{-1}(z)} \right) \right)$$

### Involving $\csc^{-1}$

01.06.21.0524.01

$$\int \sin(\csc^{-1}(z)) dz = \log(z)$$

01.06.21.0525.01

$$\int \sin(a \csc^{-1}(z)) dz = \frac{1}{a^2 - 1} \left( e^{-ia \csc^{-1}(z)} \left( (a-1) e^{ia \csc^{-1}(z)} \left( a e^{i(a+1) \csc^{-1}(z)} {}_2F_1 \left( \frac{a+1}{2}, 1; \frac{a+3}{2}; e^{2i \csc^{-1}(z)} \right) + (a+1) z \sin(a \csc^{-1}(z)) \right) - a(a+1) e^{i \csc^{-1}(z)} {}_2F_1 \left( \frac{1}{2} - \frac{a}{2}, 1; \frac{3}{2} - \frac{a}{2}; e^{2i \csc^{-1}(z)} \right) \right) \right)$$

### Involving $\sec^{-1}$

01.06.21.0526.01

$$\int \sin(\sec^{-1}(z)) dz = \frac{\sqrt{z^2} \left( \cot^{-1} \left( \sqrt{z^2 - 1} \right) + \sqrt{z^2 - 1} \right)}{z}$$

01.06.21.0527.01

$$\int \sin(a \sec^{-1}(z)) dz = -\frac{1}{2(a^2-1)} \left( i e^{-i a \sec^{-1}(z)} \left( (a-1) \left( (a+1) (-1 + e^{2i a \sec^{-1}(z)}) z - 2 a e^{i(2a+1) \sec^{-1}(z)} {}_2F_1\left(\frac{a+1}{2}, 1; \frac{a+3}{2}; -e^{2i \sec^{-1}(z)}\right) \right) + 2 a (a+1) e^{i \sec^{-1}(z)} {}_2F_1\left(\frac{1}{2} - \frac{a}{2}, 1; \frac{3}{2} - \frac{a}{2}; -e^{2i \sec^{-1}(z)}\right) \right) \right)$$

### Arguments involving inverse hyperbolic functions

#### Involving $\sinh^{-1}$

01.06.21.0528.01

$$\int \sin(\sinh^{-1}(z)) dz = \frac{1}{2} \left( z \sin(\sinh^{-1}(z)) - \sqrt{z^2+1} \cos(\sinh^{-1}(z)) \right)$$

01.06.21.0529.01

$$\int \sin(a \sinh^{-1}(z)) dz = \frac{z \sin(a \sinh^{-1}(z)) - a \sqrt{z^2+1} \cos(a \sinh^{-1}(z))}{a^2+1}$$

#### Involving $\cosh^{-1}$

01.06.21.0530.01

$$\int \sin(\cosh^{-1}(z)) dz = \frac{1}{2} \left( z \sin(\cosh^{-1}(z)) - \sqrt{\frac{z-1}{z+1}} (z+1) \cos(\cosh^{-1}(z)) \right)$$

01.06.21.0531.01

$$\int \sin(a \cosh^{-1}(z)) dz = \frac{z \sin(a \cosh^{-1}(z)) - a \sqrt{\frac{z-1}{z+1}} (z+1) \cos(a \cosh^{-1}(z))}{a^2+1}$$

#### Involving $\tanh^{-1}$

01.06.21.0532.01

$$\int \sin(\tanh^{-1}(z)) dz = \frac{1}{10} i e^{-i \tanh^{-1}(z)} \left( -5 e^{2i \tanh^{-1}(z)} z + 5 z - 5 e^{2i \tanh^{-1}(z)} {}_2F_1\left(\frac{i}{2}, 1; 1 + \frac{i}{2}; -e^{2 \tanh^{-1}(z)}\right) + 5 {}_2F_1\left(-\frac{i}{2}, 1; 1 - \frac{i}{2}; -e^{2 \tanh^{-1}(z)}\right) + e^{(2+2i) \tanh^{-1}(z)} (1+2i) {}_2F_1\left(1 + \frac{i}{2}, 1; 2 + \frac{i}{2}; -e^{2 \tanh^{-1}(z)}\right) - (1-2i) e^{2 \tanh^{-1}(z)} {}_2F_1\left(1 - \frac{i}{2}, 1; 2 - \frac{i}{2}; -e^{2 \tanh^{-1}(z)}\right) \right)$$

01.06.21.0533.01

$$\int \sin(a \tanh^{-1}(z)) dz = -\frac{1}{2(a^2+4)} i e^{-i a \tanh^{-1}(z)} \left( (a+2i) \left( (a-2i) \left( (-1+e^{2i a \tanh^{-1}(z)}) z + e^{2i a \tanh^{-1}(z)} {}_2F_1\left(\frac{ia}{2}, 1; 1+\frac{ia}{2}; -e^{2 \tanh^{-1}(z)}\right) - {}_2F_1\left(-\frac{1}{2}(ia), 1; 1-\frac{ia}{2}; -e^{2 \tanh^{-1}(z)}\right) \right) - a e^{2(1+ia) \tanh^{-1}(z)} {}_2F_1\left(1+\frac{ia}{2}, 1; 2+\frac{ia}{2}; -e^{2 \tanh^{-1}(z)}\right) \right) + a(a-2i) e^{2 \tanh^{-1}(z)} {}_2F_1\left(1-\frac{ia}{2}, 1; 2-\frac{ia}{2}; -e^{2 \tanh^{-1}(z)}\right) \right)$$

Involving  $\coth^{-1}$

01.06.21.0534.01

$$\int \sin(\coth^{-1}(z)) dz = -\frac{1}{10} i e^{-i \coth^{-1}(z)} \left( 5 e^{2i \coth^{-1}(z)} z - 5z + 5 e^{2i \coth^{-1}(z)} {}_2F_1\left(\frac{i}{2}, 1; 1+\frac{i}{2}; e^{2 \coth^{-1}(z)}\right) - 5 {}_2F_1\left(-\frac{i}{2}, 1; 1-\frac{i}{2}; e^{2 \coth^{-1}(z)}\right) + e^{(2+2i) \coth^{-1}(z)} (1+2i) {}_2F_1\left(1+\frac{i}{2}, 1; 2+\frac{i}{2}; e^{2 \coth^{-1}(z)}\right) - (1-2i) e^{2 \coth^{-1}(z)} {}_2F_1\left(1-\frac{i}{2}, 1; 2-\frac{i}{2}; e^{2 \coth^{-1}(z)}\right) \right)$$

01.06.21.0535.01

$$\int \sin(a \coth^{-1}(z)) dz = -\frac{1}{2(a^2+4)} i e^{-i a \coth^{-1}(z)} \left( (a+2i) \left( (a-2i) \left( (-1+e^{2i a \coth^{-1}(z)}) z + e^{2i a \coth^{-1}(z)} {}_2F_1\left(\frac{ia}{2}, 1; 1+\frac{ia}{2}; e^{2 \coth^{-1}(z)}\right) - {}_2F_1\left(-\frac{1}{2}(ia), 1; 1-\frac{ia}{2}; e^{2 \coth^{-1}(z)}\right) \right) + a e^{2(1+ia) \coth^{-1}(z)} {}_2F_1\left(1+\frac{ia}{2}, 1; 2+\frac{ia}{2}; e^{2 \coth^{-1}(z)}\right) \right) - a(a-2i) e^{2 \coth^{-1}(z)} {}_2F_1\left(1-\frac{ia}{2}, 1; 2-\frac{ia}{2}; e^{2 \coth^{-1}(z)}\right) \right)$$

Involving  $\operatorname{csch}^{-1}$

01.06.21.0536.01

$$\int \sin(\operatorname{csch}^{-1}(z)) dz = \left(\frac{1}{2} - \frac{i}{2}\right) e^{(1+i) \operatorname{csch}^{-1}(z)} {}_2F_1\left(\frac{1}{2} + \frac{i}{2}, 1; \frac{3}{2} + \frac{i}{2}; e^{2 \operatorname{csch}^{-1}(z)}\right) + \left(\frac{1}{2} + \frac{i}{2}\right) e^{(1-i) \operatorname{csch}^{-1}(z)} {}_2F_1\left(\frac{1}{2} - \frac{i}{2}, 1; \frac{3}{2} - \frac{i}{2}; e^{2 \operatorname{csch}^{-1}(z)}\right) + z \sin(\operatorname{csch}^{-1}(z))$$

01.06.21.0537.01

$$\int \sin(a \operatorname{csch}^{-1}(z)) dz = \frac{1}{2(a^2+1)} i e^{-i a \operatorname{csch}^{-1}(z)} \left( 2a(a-i) e^{\operatorname{csch}^{-1}(z)} {}_2F_1\left(\frac{1}{2} - \frac{ia}{2}, 1; \frac{3}{2} - \frac{ia}{2}; e^{2 \operatorname{csch}^{-1}(z)}\right) - (a+i) \left( (a-i) \left( (-1+e^{2i a \operatorname{csch}^{-1}(z)}) z + 2a e^{2i a \operatorname{csch}^{-1}(z)} e^{\operatorname{csch}^{-1}(z)} {}_2F_1\left(\frac{1}{2} + \frac{ia}{2}, 1; \frac{3}{2} + \frac{ia}{2}; e^{2 \operatorname{csch}^{-1}(z)}\right) \right) \right) \right)$$

Involving  $\operatorname{sech}^{-1}$

01.06.21.0538.01

$$\int \sin(\operatorname{sech}^{-1}(z)) dz = -\left(\frac{1}{2} - \frac{i}{2}\right) e^{(1+i)\operatorname{sech}^{-1}(z)} {}_2F_1\left(\frac{1}{2} + \frac{i}{2}, 1; \frac{3}{2} + \frac{i}{2}; -e^{2\operatorname{sech}^{-1}(z)}\right) + \left(-\frac{1}{2} - \frac{i}{2}\right) e^{(1-i)\operatorname{sech}^{-1}(z)} {}_2F_1\left(\frac{1}{2} - \frac{i}{2}, 1; \frac{3}{2} - \frac{i}{2}; -e^{2\operatorname{sech}^{-1}(z)}\right) + z \sin(\operatorname{sech}^{-1}(z))$$

01.06.21.0539.01

$$\int \sin(a \operatorname{sech}^{-1}(z)) dz = -\frac{1}{2(a^2 + 1)} i e^{-ia \operatorname{sech}^{-1}(z)} \left( (a+i) \left( (a-i) \left( -1 + e^{2ia \operatorname{sech}^{-1}(z)} \right) z - 2a e^{2ia \operatorname{sech}^{-1}(z) + \operatorname{sech}^{-1}(z)} {}_2F_1\left(\frac{1}{2} + \frac{ia}{2}, 1; \frac{3}{2} + \frac{ia}{2}; -e^{2\operatorname{sech}^{-1}(z)}\right) \right) + 2a(a-i) e^{\operatorname{sech}^{-1}(z)} {}_2F_1\left(\frac{1}{2} - \frac{ia}{2}, 1; \frac{3}{2} - \frac{ia}{2}; -e^{2\operatorname{sech}^{-1}(z)}\right) \right)$$

### Arguments involving polynomials or algebraic functions and power factors

Involving power

Involving  $z^n \sin(cz^r + fz)$

01.06.21.0540.01

$$\int z^n \sin(az^2 + bz) dz = \frac{1}{2^{n+2} a^{n+1}} \left( i(-b)^n (b+2az) e^{-\frac{ib^2}{4a}} \left( \sum_{j=0}^n \left( -\frac{2b+4az}{b} \right)^j \left( -\frac{i(b+2az)^2}{a} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(b+2az)^2}{4a}\right) - e^{\frac{ib^2}{2a}} \sum_{j=0}^n \left( -\frac{2b+4az}{b} \right)^j \left( \frac{i(b+2az)^2}{a} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(b+2az)^2}{4a}\right) \right) \right); n \in \mathbb{N}$$

01.06.21.0541.01

$$\int z^n \sin(\sqrt{z} a + b z) dz = i 4^{-n-1} a^{2n} b^{-2n-2} e^{-\frac{ia^2}{4b}}$$

$$\left( e^{\frac{ia^2}{2b}} \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{a+2b\sqrt{z}}{a} \right)^{h+j} \left( \frac{i(a+2b\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( a(a+2b\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(a+2b\sqrt{z})^2}{4b} \right) + 2\sqrt{\frac{i(a+2b\sqrt{z})^2}{b}} b i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(a+2b\sqrt{z})^2}{4b} \right) \right) - \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{a+2b\sqrt{z}}{a} \right)^{h+j} \left( -\frac{i(a+2b\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( a(a+2b\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(a+2b\sqrt{z})^2}{4b} \right) - 2ib\sqrt{-\frac{i(a+2b\sqrt{z})^2}{b}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(a+2b\sqrt{z})^2}{4b} \right) \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n \sin(az' + bz + c)$

01.06.21.0542.01

$$\int z^n \sin(az^2 + bz + c) dz =$$

$$\frac{1}{2^{n+2} a^{n+1}} \left( (i(-b)^n (b+2az)) e^{-\frac{i(b^2+4ac)}{4a}} \left( e^{2ic} \sum_{j=0}^n \left( -\frac{2b+4az}{b} \right)^j \left( -\frac{i(b+2az)^2}{a} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(b+2az)^2}{4a} \right) - e^{\frac{ib^2}{2a}} \sum_{j=0}^n \left( -\frac{2b+4az}{b} \right)^j \left( \frac{i(b+2az)^2}{a} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(b+2az)^2}{4a} \right) \right) \right) /; n \in \mathbb{N}$$

01.06.21.0543.01

$$\int z^n \sin(\sqrt{z} a + c + b z) dz = i 4^{-n-1} a^{2n} b^{-2n-2} e^{-\frac{ia^2}{4b} - ic}$$

$$\left( e^{\frac{ia^2}{2b}} \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{a+2b\sqrt{z}}{a} \right)^{h+j} \left( \frac{i(a+2b\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( a(a+2b\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(a+2b\sqrt{z})^2}{4b} \right) + 2 \sqrt{\frac{i(a+2b\sqrt{z})^2}{b}} b i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(a+2b\sqrt{z})^2}{4b} \right) \right) - e^{2ic} \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{a+2b\sqrt{z}}{a} \right)^{h+j} \left( -\frac{i(a+2b\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( a(a+2b\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(a+2b\sqrt{z})^2}{4b} \right) - 2ib \sqrt{-\frac{i(a+2b\sqrt{z})^2}{b}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(a+2b\sqrt{z})^2}{4b} \right) \right) \right) /; n \in \mathbb{N}$$

**Arguments involving polynomials or algebraic functions and factors involving exponential functions**

Involving exp

**Involving  $a^{dz} \sin(cz^r + fz)$**

01.06.21.0544.01

$$\int a^{dz} \sin(cz^2 + fz) dz = -\frac{1}{4c} \left( a^{\frac{df}{2c}} e^{-\frac{i(f^2+d^2 \log^2(a))}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi} \left( \frac{d \log(a) - i(f+2cz)}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{id^2 \log^2(a)}{2c}} \operatorname{erfi} \left( \frac{i(f+2cz) + d \log(a)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0545.01

$$\int e^{dz} \sin(cz^2 + fz) dz = -\frac{1}{4c} \left( e^{-\frac{i(d^2-2ifd+f^2)}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi} \left( \frac{d-i(f+2cz)}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{id^2}{2c}} \operatorname{erfi} \left( \frac{d+i(f+2cz)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0546.01

$$\int a^{dz} \sin(\sqrt{z} c + fz) dz = \frac{1}{4} i \left( 2 i e^{-i(\sqrt{z} c + fz)} \left( \frac{e^{2i(\sqrt{z} c + fz)}}{f - i d \log(a)} + \frac{1}{f + d i \log(a)} \right) a^{dz} + \frac{i c e^{-\frac{c^2}{-4if+4d\log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2d\sqrt{z} \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if+d\log(a)}}\right)}{(-if+d\log(a))^{3/2}} + \frac{i c e^{\frac{c^2}{4if+4d\log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic+2\sqrt{z}(if+d\log(a))}{2\sqrt{if+d\log(a)}}\right)}{(if+d\log(a))^{3/2}} \right)$$

01.06.21.0547.01

$$\int e^{dz} \sin(\sqrt{z} c + fz) dz = e^{dz - ifz - ic\sqrt{z}} \left( \frac{e^{2i(\sqrt{z} c + fz)}}{2id - 2f} + \frac{1}{-2f - 2id} \right) + \frac{c e^{\frac{c^2}{4d-4if}} i \sqrt{\pi} \operatorname{erf}\left(\frac{c+2(f+id)\sqrt{z}}{2\sqrt{d-if}}\right)}{4(d-if)^{3/2}} - \frac{c e^{\frac{c^2}{4d+4if}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2\sqrt{z}(d+if)+ic}{2\sqrt{d+if}}\right)}{4(d+if)^{3/2}}$$

**Involving  $a^{dz+e} \sin(cz^f + fz)$**

01.06.21.0548.01

$$\int a^{dz+e} \sin(cz^2 + fz) dz = -\frac{1}{4c} \left( a^{-\frac{df}{2c}} e^{-\frac{i(f^2+d^2\log^2(a))}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi}\left(\frac{d\log(a) - i(f+2cz)}{2\sqrt{-ic}}\right) + \sqrt{ic} e^{\frac{id^2\log^2(a)}{2c}} \operatorname{erfi}\left(\frac{i(f+2cz) + d\log(a)}{2\sqrt{ic}}\right) \right) \right)$$

01.06.21.0549.01

$$\int e^{dz+e} \sin(cz^2 + fz) dz = -\frac{1}{4c} \left( e^{-\frac{i(d^2-2ifd+f^2+4ice)}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi}\left(\frac{d-i(f+2cz)}{2\sqrt{-ic}}\right) + \sqrt{ic} e^{\frac{id^2}{2c}} \operatorname{erfi}\left(\frac{d+i(f+2cz)}{2\sqrt{ic}}\right) \right) \right)$$

01.06.21.0550.01

$$\int a^{e+dz} \sin(\sqrt{z} c + fz) dz = \frac{1}{4} i a^e \left( 2 e^{-i(\sqrt{z} c + fz)} i \left( \frac{e^{2i(\sqrt{z} c + fz)}}{f - i d \log(a)} + \frac{1}{f + d i \log(a)} \right) a^{dz} + \frac{c e^{-\frac{c^2}{-4if+4d\log(a)}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{2d\sqrt{z} \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if+d\log(a)}}\right)}{(-if+d\log(a))^{3/2}} + \frac{c e^{\frac{c^2}{4if+4d\log(a)}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{ic+2\sqrt{z}(if+d\log(a))}{2\sqrt{if+d\log(a)}}\right)}{(if+d\log(a))^{3/2}} \right)$$

01.06.21.0551.01

$$\int e^{dz+e} \sin(\sqrt{z} c + fz) dz = e^{e+dz-iz-ic\sqrt{z}} \left( \frac{e^{2i(\sqrt{z} c+fz)}}{2id-2f} + \frac{1}{-2f-2id} \right) + \frac{c e^{\frac{c^2+4de-4ief}{4d-4if}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{c+2(f+id)\sqrt{z}}{2\sqrt{d-if}}\right)}{4(d-if)^{3/2}} - \frac{c e^{\frac{c^2+4de+4ief}{4d+4if}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2\sqrt{z}(d+if)+ic}{2\sqrt{d+if}}\right)}{4(d+if)^{3/2}}$$

**Involving  $a^{bz^r} \sin(cz^r + fz)$**

01.06.21.0552.01

$$\int a^{bz^2} \sin(cz^2 + fz) dz = \frac{1}{4(c^2 + b^2 \log^2(a))} \left( i a^{\frac{bf^2}{2(c^2+b^2 \log^2(a))}} \sqrt{\pi} \left( e^{-\frac{f^2}{4ic+4b \log(a)}} \operatorname{erfi}\left(\frac{2bz \log(a) - i(f+2cz)}{2\sqrt{-ic+b \log(a)}}\right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) + e^{-\frac{f^2}{-4ic+4b \log(a)}} \operatorname{erfi}\left(\frac{i(f+2cz) + 2bz \log(a)}{2\sqrt{ic+b \log(a)}}\right) (ic-b \log(a)) \sqrt{ic+b \log(a)} \right) \right)$$

01.06.21.0553.01

$$\int e^{bz^2} \sin(cz^2 + fz) dz = \frac{1}{4(b^2 + c^2)} \left( i e^{\frac{bf^2}{2(b^2+c^2)}} \sqrt{\pi} \left( (ic-b) \sqrt{b+ic} e^{-\frac{f^2}{4b-4ic}} \operatorname{erfi}\left(\frac{2bz+i(f+2cz)}{2\sqrt{b+ic}}\right) + (b+ic) \sqrt{b-ic} e^{-\frac{f^2}{4b+4ic}} \operatorname{erfi}\left(\frac{2bz-i(f+2cz)}{2\sqrt{b-ic}}\right) \right) \right)$$

01.06.21.0554.01

$$\int a^{b\sqrt{z}} \sin(\sqrt{z} c + fz) dz = -\frac{a^{b\sqrt{z}} \cos(\sqrt{z} c + fz)}{f} - \frac{e^{\frac{ic^2-2b \log(a)c-i b^2 \log^2(a)}{4f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b \log(a)-i(c+2f\sqrt{z})}{2\sqrt{-if}}\right) (c+b i \log(a))}{4(-if)^{3/2}} - \frac{e^{\frac{i(-c^2+2b i \log(a)c+b^2 \log^2(a))}{4f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic+2if\sqrt{z}+b \log(a)}{2\sqrt{if}}\right) (c-i b \log(a))}{4(if)^{3/2}}$$

01.06.21.0555.01

$$\int e^{b\sqrt{z}} \sin(\sqrt{z} c + fz) dz = \frac{(c+ib) e^{\frac{-ib^2-2cb+c^2i}{4f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b-i(c+2f\sqrt{z})}{2\sqrt{-if}}\right)}{4(-if)^{3/2}} - \frac{(c-ib) e^{\frac{i(b^2+2icb-c^2)}{4f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+ic+2if\sqrt{z}}{2\sqrt{if}}\right)}{4(if)^{3/2}} - \frac{e^{b\sqrt{z}} \cos(\sqrt{z} c + fz)}{f}$$

**Involving  $a^{bz^r+e} \sin(cz^r + fz)$**



01.06.21.0556.01

$$\int a^{bz^2+e} \sin(cz^2 + fz) dz = \frac{1}{4(c^2 + b^2 \log^2(a))} \left( i a^{\frac{bf^2}{c^2+b^2 \log^2(a)}+e} \sqrt{\pi} \left( e^{-\frac{f^2}{4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{2bz \log(a) - i(f+2cz)}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) + e^{-\frac{f^2}{-4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{i(f+2cz) + 2bz \log(a)}{2\sqrt{ic+b \log(a)}} \right) (ic-b \log(a)) \sqrt{ic+b \log(a)} \right) \right)$$

01.06.21.0557.01

$$\int e^{bz^2+e} \sin(cz^2 + fz) dz = \frac{1}{4(b^2 + c^2)} \left( i e^{\frac{bf^2}{b^2+c^2}+e} \sqrt{\pi} \left( (ic-b) \sqrt{b+ic} e^{-\frac{f^2}{4b-4ic}} \operatorname{erfi} \left( \frac{2bz+i(f+2cz)}{2\sqrt{b+ic}} \right) + (b+ic) \sqrt{b-ic} e^{-\frac{f^2}{4b+4ic}} \operatorname{erfi} \left( \frac{2bz-i(f+2cz)}{2\sqrt{b-ic}} \right) \right) \right)$$

01.06.21.0558.01

$$\int a^{\sqrt{z} b+e} \sin(\sqrt{z} c + fz) dz = \frac{a^{\sqrt{z} b+e} \cos(\sqrt{z} c + fz) e^{\frac{ic^2-i b^2 \log^2(a)+(4ef-2bc) \log(a)}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if}} \right) (c + b i \log(a))}{f} - \frac{e^{\frac{i(-c^2+b^2 \log^2(a)+2(bc-2ef) i \log(a))}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+2if\sqrt{z} + b \log(a)}{2\sqrt{if}} \right) (c - i b \log(a))}{4(i f)^{3/2}}$$

01.06.21.0559.01

$$\int e^{\sqrt{z} b+e} \sin(\sqrt{z} c + fz) dz = - \frac{(c + i b) e^{\frac{-ib^2-2cb+4ef+c^2 i}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b-i(c+2f\sqrt{z})}{2\sqrt{-if}} \right)}{4(-if)^{3/2}} - \frac{(c - i b) e^{\frac{i(b^2-c^2+2(bc-2ef) i)}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+ic+2if\sqrt{z}}{2\sqrt{if}} \right)}{4(i f)^{3/2}} - \frac{e^{\sqrt{z} b+e} \cos(\sqrt{z} c + fz)}{f}$$

Involving  $a^{bz^r+dz} \sin(cz^r + fz)$

01.06.21.0560.01

$$\int a^{bz^2+dz} \sin(cz^2 + fz) dz = \frac{1}{4(c^2 + b^2 \log^2(a))} \left( i a^{\frac{b(f^2-d^2 \log^2(a))}{2(c^2+b^2 \log^2(a))} + \frac{df}{2ib \log(a)-2c}} \sqrt{\pi} \left( e^{\frac{d^2 \log^2(a)-f^2}{4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{(d+2bz) \log(a) - i(f+2cz)}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} (ic+b \log(a)) a^{\frac{ibdf \log(a)}{c^2+b^2 \log^2(a)}} + e^{\frac{d^2 \log^2(a)-f^2}{-4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{i(f+2cz) + (d+2bz) \log(a)}{2\sqrt{ic+b \log(a)}} \right) \sqrt{ic+b \log(a)} (ic-b \log(a)) \right) \right)$$

01.06.21.0561.01

$$\int e^{bz^2+dz} \sin(cz^2 + fz) dz = \frac{1}{4(b+ic)(c+ib)} \left( e^{-\frac{ci(d-i)^2+2bd(d+if)}{4(b^2+c^2)}} \sqrt{\pi} \left( (b-ic) \sqrt{b+ic} e^{\frac{b(d^2+f^2)+2c(d^2-f^2)i}{4(b^2+c^2)}} \operatorname{erfi} \left( \frac{d+if+2(b+ic)z}{2\sqrt{b+ic}} \right) - \sqrt{b-ic} (b+ic) e^{\frac{b(d^2+4ifd+f^2)}{4(b^2+c^2)}} \operatorname{erfi} \left( \frac{d-i(f+2(c+ib)z)}{2\sqrt{b-ic}} \right) \right) \right)$$

01.06.21.0562.01

$$\int a^{\sqrt{z}bz+dz} \sin(\sqrt{z}c + fz) dz = - \left( \frac{e^{-i(\sqrt{z}c+fz)} a^{\sqrt{z}bz+dz}}{2(f+di \log(a))} + \frac{e^{i(\sqrt{z}c+fz)} a^{\sqrt{z}bz+dz}}{2(f-id \log(a))} + \frac{1}{4(if+d \log(a))^{3/2}} \left( e^{-\frac{-c^2+2bi \log(a)c+b^2 \log^2(a)}{4(if+d \log(a))}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+b \log(a) + 2\sqrt{z}(if+d \log(a))}{2\sqrt{if+d \log(a)}} \right) (c-ib \log(a)) \right) + \frac{e^{\frac{ic^2-2b \log(a)c-i b^2 \log^2(a)}{4(f+di \log(a))}} \sqrt{\pi} \operatorname{erfi} \left( \frac{(b+2d\sqrt{z}) \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if+d \log(a)}} \right) (c+bi \log(a)) \right) \right)$$

01.06.21.0563.01

$$\int e^{\sqrt{z}bz+dz} \sin(\sqrt{z}c + fz) dz = - \frac{(c-ib) e^{-\frac{b^2+2icb-c^2}{4(d+if)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+ic+2(d+if)\sqrt{z}}{2\sqrt{d+if}} \right)}{4(d+if)^{3/2}} - \frac{e^{\sqrt{z}bz+dz+i(\sqrt{z}c+fz)}}{2(f-id)} - \frac{e^{\sqrt{z}bz+dz-i(\sqrt{z}c+fz)}}{2(f+id)} - \frac{(c+ib) e^{-\frac{-ib^2-2cb+c^2i}{4(f+id)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b-i(c+2f\sqrt{z})+2d\sqrt{z}}{2\sqrt{d-if}} \right)}{4(d-if)^{3/2}}$$

Involving  $a^{bz^r+dz+e} \sin(cz^r + fz)$

01.06.21.0564.01

$$\int a^{bz^2+dz+e} \sin(cz^2+fz) dz = \frac{1}{4(c^2+b^2 \log^2(a))} \left( i a^{\frac{b(f^2-d^2 \log^2(a))}{2(c^2+b^2 \log^2(a))} + \frac{df}{2ib \log(a)-2c}} \sqrt{\pi} \left( e^{\frac{d^2 \log^2(a)-f^2}{4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{(d+2bz) \log(a) - i(f+2cz)}{2\sqrt{-ic+b \log(a)}} \right) \sqrt{-ic+b \log(a)} \right. \right. \\ \left. \left. + (ic+b \log(a)) a^{\frac{ibdf \log(a)}{c^2+b^2 \log^2(a)} + \frac{d^2 \log^2(a)-f^2}{-4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{i(f+2cz) + (d+2bz) \log(a)}{2\sqrt{ic+b \log(a)}} \right) \sqrt{ic+b \log(a)} (ic-b \log(a)) \right) \right)$$

01.06.21.0565.01

$$\int e^{bz^2+dz+e} \sin(cz^2+fz) dz = \frac{1}{4(b^2+c^2)} \left( i e^{\frac{4eb^2-2d(d+if)b+c(-i d^2-2fd+4ce+f^2i)}{4(b^2+c^2)}} \sqrt{\pi} \left( \sqrt{b+ic} (b-ic) e^{\frac{b(d^2+f^2)+2c(d^2-f^2)i}{4(b^2+c^2)}} \operatorname{erfi} \left( \frac{-d-if-2bz-2icz}{2\sqrt{b+ic}} \right) + \right. \right. \\ \left. \left. (b+ic) \sqrt{b-ic} e^{\frac{b(d^2+4ifd+f^2)}{4(b^2+c^2)}} \operatorname{erfi} \left( \frac{d-i(f+2(c+ib)z)}{2\sqrt{b-ic}} \right) \right) \right)$$

01.06.21.0566.01

$$\int a^{\sqrt{z} b+e+dz} \sin(\sqrt{z} c+fz) dz = -i \frac{1}{4} a^e \left( -i 2 e^{-i(\sqrt{z} c+fz)} \left( \frac{e^{2i(\sqrt{z} c+fz)}}{f-i d \log(a)} + \frac{1}{f+d i \log(a)} \right) a^{\sqrt{z} b+dz} + \right. \\ \left. \frac{e^{\frac{(c+bi \log(a))^2}{-4if+4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{(b+2d\sqrt{z}) \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if+d \log(a)}} \right) (-ic+b \log(a))}{(-if+d \log(a))^{3/2}} - \right. \\ \left. \frac{e^{\frac{(c-i b \log(a))^2}{4if+4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+b \log(a)+2\sqrt{z}(if+d \log(a))}{2\sqrt{if+d \log(a)}} \right) (ic+b \log(a))}{(if+d \log(a))^{3/2}} \right)$$

01.06.21.0567.01

$$\int e^{\sqrt{z} b+dz+e} \sin(\sqrt{z} c+fz) dz = - \frac{(c-ib) e^{-\frac{b^2-e^2-4de+2(bc-2ef)i}{4(d+if)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b+ic+2(d+if)\sqrt{z}}{2\sqrt{d+if}} \right)}{4(d+if)^{3/2}} - \\ \frac{e^{\sqrt{z} b+e+dz+i(\sqrt{z} c+fz)}}{2(f-id)} - \frac{e^{\sqrt{z} b+e+dz-i(\sqrt{z} c+fz)}}{2(f+id)} - \frac{(c+ib) e^{\frac{ic^2-2bc-i(b^2-4de)+4ef}{4(f+id)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b-i(c+2f\sqrt{z})+2d\sqrt{z}}{2\sqrt{d-if}} \right)}{4(d-if)^{3/2}}$$

**Involving  $a^{dz} \sin(cz^r + fz + g)$**

01.06.21.0568.01

$$\int a^{dz} \sin(cz^2 + fz + g) dz = -\frac{1}{4c} \left( a^{-\frac{df}{2c}} e^{-\frac{i(f^2+d^2 \log^2(a)+4cg)}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi} \left( \frac{d \log(a) - i(f+2cz)}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{1}{2}i \left( \frac{d^2 \log^2(a)}{c} + 4g \right)} \operatorname{erfi} \left( \frac{i(f+2cz) + d \log(a)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0569.01

$$\int e^{dz} \sin(cz^2 + fz + g) dz = -\frac{1}{4c} \left( e^{-\frac{i(d^2-2idf+f^2+4cg)}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi} \left( \frac{d-i(f+2cz)}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{i(d^2+4cg)}{2c}} \operatorname{erfi} \left( \frac{d+i(f+2cz)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0570.01

$$\int a^{dz} \sin(\sqrt{z}c + fz + g) dz = -\frac{1}{4} i e^{-ig} \left( -2i e^{-i(\sqrt{z}c+fz)} \left( \frac{e^{2i(\sqrt{z}c+fz)}}{f-id \log(a)} + \frac{1}{f+di \log(a)} \right) a^{dz} - \frac{ic e^{-\frac{c^2}{-4if+4d \log(a)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{2d\sqrt{z} \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if+d \log(a)}} \right) - ic e^{\frac{c^2}{4if+4d \log(a)}+2ig} \sqrt{\pi} \operatorname{erfi} \left( \frac{ic+2\sqrt{z}(if+d \log(a))}{2\sqrt{if+d \log(a)}} \right)}{(-if+d \log(a))^{3/2} - (if+d \log(a))^{3/2}} \right)$$

01.06.21.0571.01

$$\int e^{dz} \sin(\sqrt{z}c + fz + g) dz = \frac{c e^{-\frac{-c^2-4idg+4fg}{4(d+if)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{2\sqrt{z}(d+if)+ic}{2\sqrt{d+if}} \right) - e^{dz+i(\sqrt{z}c+fz)} - e^{dz-i(\sqrt{z}c+fz)} - c e^{\frac{4dg+(c^2-4fg)i}{4(f+id)}} \sqrt{\pi} \operatorname{erfi} \left( \frac{2d\sqrt{z}-i(c+2f\sqrt{z})}{2\sqrt{d-if}} \right)}{4(d+if)^{3/2} - 2(f-id) - 2(f+id) - 4(d-if)^{3/2}}$$

### Involving $a^{dz+e} \sin(cz^r + fz + g)$

01.06.21.0572.01

$$\int a^{dz+e} \sin(cz^2 + fz + g) dz = -\frac{1}{4c} \left( a^{-\frac{df}{2c}} e^{-\frac{i(f^2+d^2 \log^2(a)+4cg)}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi} \left( \frac{d \log(a) - i(f+2cz)}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{1}{2}i \left( \frac{d^2 \log^2(a)}{c} + 4g \right)} \operatorname{erfi} \left( \frac{i(f+2cz) + d \log(a)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0573.01

$$\int e^{dz+e} \sin(cz^2 + fz + g) dz = -\frac{1}{4c} \left( e^{-\frac{i(d^2-2idf+f^2+4c(g+ie))}{4c}} \sqrt{\pi} \left( \sqrt{-ic} e^{\frac{if^2}{2c}} \operatorname{erfi} \left( \frac{d-i(f+2cz)}{2\sqrt{-ic}} \right) + \sqrt{ic} e^{\frac{i(d^2+4cg)}{2c}} \operatorname{erfi} \left( \frac{d+i(f+2cz)}{2\sqrt{ic}} \right) \right) \right)$$

01.06.21.0574.01

$$\int a^{dz+e} \sin(\sqrt{z} c + f z + g) dz =$$

$$\frac{e^{-i(\sqrt{z} c + g + f z)} a^{e+dz}}{2(f + di \log(a))} - \frac{e^{i(\sqrt{z} c + g + f z)} a^{e+dz}}{2(f - id \log(a))} - \frac{c e^{\frac{4dei \log^2(a) + (4ef + 4dg) \log(a) + (c^2 - 4fg)i}{4(f+di \log(a))}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2d\sqrt{z} \log(a) - i(c + 2f\sqrt{z})}{2\sqrt{-if + d \log(a)}}\right)}{4(-if + d \log(a))^{3/2}}$$

$$\frac{c e^{\frac{-c^2 - 4de \log^2(a) + 4fg - 4i(ef + dg) \log(a)}{4(if + d \log(a))}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic + 2\sqrt{z}(if + d \log(a))}{2\sqrt{if + d \log(a)}}\right)}{4(if + d \log(a))^{3/2}}$$

01.06.21.0575.01

$$\int a^{dz+e} \sin(\sqrt{z} c + f z + g) dz = -\frac{1}{4} i a^e e^{-ig} \left( -2i e^{-i(\sqrt{z} c + f z)} \left( \frac{e^{2i(\sqrt{z} c + g + f z)}}{f - id \log(a)} + \frac{1}{f + di \log(a)} \right) a^{dz} - \right.$$

$$\left. \frac{ic e^{\frac{c^2}{-4if + 4d \log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2d\sqrt{z} \log(a) - i(c + 2f\sqrt{z})}{2\sqrt{-if + d \log(a)}}\right)}{(-if + d \log(a))^{3/2}} - \frac{ic e^{\frac{c^2}{4if + 4d \log(a)} + 2ig} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic + 2\sqrt{z}(if + d \log(a))}{2\sqrt{if + d \log(a)}}\right)}{(if + d \log(a))^{3/2}} \right)$$

01.06.21.0576.01

$$\int e^{e+dz} \sin(\sqrt{z} c + g + f z) dz = -\frac{c e^{\frac{-c^2 - 4de + 4fg - 4i(ef + dg)}{4(d+if)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2\sqrt{z}(d+if) + ic}{2\sqrt{d+if}}\right)}{4(d+if)^{3/2}} -$$

$$\frac{e^{e+dz+i(\sqrt{z} c + g + f z)}}{2(f - id)} - \frac{e^{e+dz-i(\sqrt{z} c + g + f z)}}{2(f + id)} - \frac{c e^{\frac{4ef + 4dg + 4ide + (c^2 - 4fg)i}{4(f+id)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{2d\sqrt{z} - i(c + 2f\sqrt{z})}{2\sqrt{d-if}}\right)}{4(d-if)^{3/2}}$$

### Involving $a^{bz^r} \sin(cz^r + fz + g)$

01.06.21.0577.01

$$\int a^{bz^2} \sin(cz^2 + fz + g) dz =$$

$$\frac{1}{4(c^2 + b^2 \log^2(a))} \left( \frac{bf^2}{ia^{2(c^2 + b^2 \log^2(a))}} \sqrt{\pi} \left( e^{-\frac{f^2}{4ic + 4b \log(a)} - ig} \operatorname{erfi}\left(\frac{2bz \log(a) - i(f + 2cz)}{2\sqrt{-ic + b \log(a)}}\right) \sqrt{-ic + b \log(a)} (ic + b \log(a)) + \right.$$

$$\left. e^{ig - \frac{f^2}{-4ic + 4b \log(a)}} \operatorname{erfi}\left(\frac{i(f + 2cz) + 2bz \log(a)}{2\sqrt{ic + b \log(a)}}\right) (ic - b \log(a)) \sqrt{ic + b \log(a)} \right)$$

01.06.21.0578.01

$$\int e^{bz^2} \sin(cz^2 + fz + g) dz = \frac{1}{4(b^2 + c^2)} \left( i e^{\frac{bf^2}{2(b^2+c^2)}} \sqrt{\pi} \left( (ic - b) \sqrt{b+ic} e^{ig - \frac{f^2}{4b-4ic}} \operatorname{erfi} \left( \frac{2bz + i(f+2cz)}{2\sqrt{b+ic}} \right) + (b+ic) \sqrt{b-ic} e^{-\frac{f^2}{4b+4ic} - ig} \operatorname{erfi} \left( \frac{2bz - i(f+2cz)}{2\sqrt{b-ic}} \right) \right) \right)$$

01.06.21.0579.01

$$\int a^{\sqrt{z}} b \sin(\sqrt{z} c + fz + g) dz = \frac{\cos(\sqrt{z} c + g + fz) a^{b\sqrt{z}} e^{\frac{-ib^2 \log^2(a) - 2bc \log(a) + (c^2 - 4fg)i}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b \log(a) - i(c+2f\sqrt{z})}{2\sqrt{-if}} \right) (c + b i \log(a))}{f} - \frac{e^{\frac{i(-c^2 + 2bi \log(a)c + b^2 \log^2(a) + 4fg)}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{i(c+2f\sqrt{z}) + b \log(a)}{2\sqrt{if}} \right) (c - ib \log(a))}{4(i f)^{3/2}}$$

01.06.21.0580.01

$$\int e^{b\sqrt{z}} \sin(\sqrt{z} c + fz + g) dz = - \frac{(c + ib) e^{\frac{-ib^2 - 2cb + (c^2 - 4fg)i}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b - i(c+2f\sqrt{z})}{2\sqrt{-if}} \right)}{4(-if)^{3/2}} - \frac{(c - ib) e^{\frac{i(b^2 + 2icb - c^2 + 4fg)}{4f}} \sqrt{\pi} \operatorname{erfi} \left( \frac{b + ic + 2if\sqrt{z}}{2\sqrt{if}} \right) e^{b\sqrt{z}} \cos(\sqrt{z} c + g + fz)}{4(i f)^{3/2} f}$$

### Involving $a^{bz^f+e} \sin(cz^r + fz + g)$

01.06.21.0581.01

$$\int a^{bz^2+e} \sin(cz^2 + fz + g) dz = \frac{1}{4(c^2 + b^2 \log^2(a))} \left( i a^{\frac{bf^2}{2(c^2+b^2 \log^2(a))} + e} \sqrt{\pi} \left( e^{-\frac{f^2}{4ic+4b \log(a)} - ig} \operatorname{erfi} \left( \frac{2bz \log(a) - i(f+2cz)}{2\sqrt{-ic + b \log(a)}} \right) \sqrt{-ic + b \log(a)} + e^{ig - \frac{f^2}{-4ic+4b \log(a)}} \operatorname{erfi} \left( \frac{i(f+2cz) + 2bz \log(a)}{2\sqrt{ic + b \log(a)}} \right) (ic - b \log(a)) \sqrt{ic + b \log(a)} \right) \right)$$

01.06.21.0582.01

$$\int e^{bz^2+e} \sin(cz^2 + fz + g) dz = \frac{1}{4(b^2 + c^2)} \left( i e^{\frac{bf^2}{2(b^2+c^2)} + e} \sqrt{\pi} \left( (ic - b) \sqrt{b+ic} e^{ig - \frac{f^2}{4b-4ic}} \operatorname{erfi} \left( \frac{2bz + i(f+2cz)}{2\sqrt{b+ic}} \right) + (b+ic) \sqrt{b-ic} e^{-\frac{f^2}{4b+4ic} - ig} \operatorname{erfi} \left( \frac{2bz - i(f+2cz)}{2\sqrt{b-ic}} \right) \right) \right)$$

01.06.21.0583.01

$$\int a^{\sqrt{z} b+e} \sin(\sqrt{z} c+f z+g) dz =$$

$$\frac{\cos(\sqrt{z} c+g+f z) a^{\sqrt{z} b+e} e^{\frac{-i b^2 \log^2(a)+(4 e f-2 b c) \log(a)+(c^2-4 f g) i}{4 f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b \log(a)-i(c+2 f \sqrt{z})}{2 \sqrt{-i f}}\right)(c+b i \log(a))}{f} - \frac{4(-i f)^{3/2}}{4(i f)^{3/2}}$$

$$\frac{e^{\frac{i(-c^2+b^2 \log^2(a)+4 f g+2(b c-2 e f) i \log(a))}{4 f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{i(c+2 f \sqrt{z})+b \log(a)}{2 \sqrt{i f}}\right)(c-i b \log(a))}{4(i f)^{3/2}}$$

01.06.21.0584.01

$$\int e^{\sqrt{z} b+e} \sin(\sqrt{z} c+f z+g) dz = - \frac{(c+i b) e^{\frac{-i b^2-2 c b+4 e f+(c^2-4 f g) i}{4 f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b-i(c+2 f \sqrt{z})}{2 \sqrt{-i f}}\right)}{4(-i f)^{3/2}}$$

$$\frac{(c-i b) e^{\frac{i(b^2-c^2+4 f g+2(b c-2 e f) i)}{4 f}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+i c+2 i f \sqrt{z}}{2 \sqrt{i f}}\right)}{4(i f)^{3/2}} - \frac{e^{\sqrt{z} b+e} \cos(\sqrt{z} c+g+f z)}{f}$$

### Involving $a^{bz^r+dz} \sin(cz^r+fz+g)$

01.06.21.0585.01

$$\int a^{bz^2+dz} \sin(cz^2+fz+g) dz =$$

$$\frac{1}{4(c^2+b^2 \log^2(a))} \left( i a^{\frac{b(f^2-d^2 \log^2(a))}{2(c^2+b^2 \log^2(a))} + \frac{df}{2ib \log(a)-2c}} \sqrt{\pi} \left( e^{\frac{d^2 \log^2(a)-f^2}{4ic+4b \log(a)} - ig} \operatorname{erfi}\left(\frac{(d+2bz) \log(a) - i(f+2cz)}{2 \sqrt{-ic+b \log(a)}}\right) \sqrt{-ic+b \log(a)} \right. \right.$$

$$\left. \left. (ic+b \log(a)) a^{\frac{ibdf \log(a)}{c^2+b^2 \log^2(a)} + e^{\frac{d^2 \log^2(a)-f^2}{-4ic+4b \log(a)} + ig} \operatorname{erfi}\left(\frac{i(f+2cz) + (d+2bz) \log(a)}{2 \sqrt{ic+b \log(a)}}\right) \sqrt{ic+b \log(a)} (ic-b \log(a)) \right) \right)$$

01.06.21.0586.01

$$\int e^{bz^2+dz} \sin(cz^2+fz+g) dz = \frac{1}{4(b+ic)(c+ib)}$$

$$\left( e^{\frac{-ci(d-if)^2+2bd(d+if)}{4(b^2+c^2)}} \sqrt{\pi} \left( (b-ic) \sqrt{b+ic} e^{\frac{b(d^2+f^2)+2c(d^2-f^2)i}{4(b^2+c^2)}} \operatorname{erfi}\left(\frac{d+if+2(b+ic)z}{2 \sqrt{b+ic}}\right) (\cos(g)+i \sin(g)) - \right. \right.$$

$$\left. \left. \sqrt{b-ic} (b+ic) e^{\frac{b(d^2+4ifd+f^2)}{4(b^2+c^2)}} \operatorname{erfi}\left(\frac{d-i(f+2(c+ib)z)}{2 \sqrt{b-ic}}\right) (\cos(g)-i \sin(g)) \right) \right)$$

01.06.21.0587.01

$$\int a^{\sqrt{z} b+d z} \sin(\sqrt{z} c+f z+g) d z=-i \frac{1}{4} e^{-i g}\left(-i 2 e^{-i(\sqrt{z} c+f z)}\left(\frac{e^{2 i(\sqrt{z} c+g+f z)}}{f-i d \log (a)}+\frac{1}{f+d i \log (a)}\right) a^{\sqrt{z} b+d z}+\frac{e^{\frac{(c+b i \log (a))^2}{-4 i f+4 d \log (a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2 d \sqrt{z}) \log (a)-i(c+2 f \sqrt{z})}{2 \sqrt{-i f+d \log (a)}}\right)(-i c+b \log (a))}{(-i f+d \log (a))^{3 / 2}}-\frac{e^{\frac{(c-i b \log (a))^2}{4 i f+4 d \log (a)}}+2 i g \sqrt{\pi} \operatorname{erfi}\left(\frac{i c+b \log (a)+2 \sqrt{z}(i f+d \log (a))}{2 \sqrt{i f+d \log (a)}}\right)(i c+b \log (a))}{(i f+d \log (a))^{3 / 2}}\right)$$

01.06.21.0588.01

$$\int e^{\sqrt{z} b+d z} \sin(\sqrt{z} c+f z+g) d z=-\frac{(c-i b) e^{-\frac{b^2-c^2+4 f g+2(b c-2 d g) i}{4(d+i f)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+i c+2(d+i f) \sqrt{z}}{2 \sqrt{d+i f}}\right)}{4(d+i f)^{3 / 2}}-\frac{(c+i b) e^{-\frac{-i b^2-2 c b+4 d g+(c^2-4 f g) i}{4(f+i d)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b-i(c+2 f \sqrt{z})+2 d \sqrt{z}}{2 \sqrt{d-i f}}\right)}{4(d-i f)^{3 / 2}}-\frac{e^{\sqrt{z} b+d z+i(\sqrt{z} c+g+f z)}}{2(f-i d)}-\frac{e^{\sqrt{z} b+d z-i(\sqrt{z} c+g+f z)}}{2(f+i d)}$$

### Involving $a^{b z^2+d z+e} \sin(c z^r+f z+g)$

01.06.21.0589.01

$$\int a^{b z^2+d z+e} \sin(c z^2+f z+g) d z==\frac{1}{4\left(c^2+b^2 \log ^2(a)\right)}\left(i a^{\frac{e+\frac{b\left(f^2-d^2 \log ^2(a)\right)}{2\left(c^2+b^2 \log ^2(a)\right)}+\frac{d f}{2 i b \log (a)-2 c}} \sqrt{\pi}\left(e^{\frac{d^2 \log ^2(a)-f^2}{4 i c+4 b \log (a)}}-i g \operatorname{erfi}\left(\frac{(d+2 b z) \log (a)-i(f+2 c z)}{2 \sqrt{-i c+b \log (a)}}\right)\right) \sqrt{-i c+b \log (a)}+\left(i c+b \log (a)\right) a^{\frac{i b d f \log (a)}{c^2+b^2 \log ^2(a)}}+e^{\frac{d^2 \log ^2(a)-f^2}{-4 i c+4 b \log (a)}}+i g \operatorname{erfi}\left(\frac{i(f+2 c z)+(d+2 b z) \log (a)}{2 \sqrt{i c+b \log (a)}}\right)\right) \sqrt{i c+b \log (a)}(i c-b \log (a))\right)$$



01.06.21.0590.01

$$\int e^{bz^2+dz+e} \sin(cz^2+fz+g) dz = \frac{1}{4(b-ic)(c-ib)} \left( e^{\frac{4eb^2-2d(d+if)b+c(-id^2-2fd+4ce+f^2i)}{4(b^2+c^2)}} \sqrt{\pi} \left( \sqrt{b+ic} (b-ic) e^{\frac{b(d^2+f^2)+2c(d^2-f^2)i}{4(b^2+c^2)}} \operatorname{erfi}\left(\frac{-d-if-2bz-2icz}{2\sqrt{b+ic}}\right) (\cos(g)+i\sin(g)) + (b+ic) \sqrt{b-ic} e^{\frac{b(d^2+4ifd+f^2)}{4(b^2+c^2)}} \operatorname{erfi}\left(\frac{d-i(f+2(c+ib)z)}{2\sqrt{b-ic}}\right) (\cos(g)-i\sin(g)) \right) \right)$$

01.06.21.0591.01

$$\int a^{\sqrt{z}} b^{bz+e} \sin(\sqrt{z}c+fz+g) dz = -\frac{1}{4} a^e e^{-ig} \left( -i2 e^{-i(\sqrt{z}c+fz)} \left( \frac{e^{2i(\sqrt{z}c+g+fz)}}{f-id\log(a)} + \frac{1}{f+d\log(a)} \right) a^{\sqrt{z}bz+e} + \frac{e^{\frac{(c+bi\log(a))^2}{-4if+4d\log(a)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2d\sqrt{z})\log(a)-i(c+2f\sqrt{z})}{2\sqrt{-if+d\log(a)}}\right) (-ic+b\log(a))}{(-if+d\log(a))^{3/2}} - \frac{e^{\frac{(c-bi\log(a))^2}{4if+4d\log(a)}+2ig} \sqrt{\pi} \operatorname{erfi}\left(\frac{ic+b\log(a)+2\sqrt{z}(if+d\log(a))}{2\sqrt{if+d\log(a)}}\right) (ic+b\log(a))}{(if+d\log(a))^{3/2}} \right)$$

01.06.21.0592.01

$$\int e^{\sqrt{z}} b^{bz+e} \sin(\sqrt{z}c+fz+g) dz = -\frac{(c-ib) e^{-\frac{b^2-c^2-4de+4fg+2(bc-2(e+f+d)g)i}{4(d+if)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+ic+2(d+if)\sqrt{z}}{2\sqrt{d+if}}\right)}{4(d+if)^{3/2}} - \frac{(c+ib) e^{-\frac{-2bc-i(b^2-4de)+4ef+4dg+(c^2-4fg)i}{4(f+id)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b-i(c+2f\sqrt{z})+2d\sqrt{z}}{2\sqrt{d-if}}\right)}{4(d-if)^{3/2}} - \frac{e^{\sqrt{z}b+e+dz+i(\sqrt{z}c+g+fz)}}{2(f-id)} - \frac{e^{\sqrt{z}b+e+dz-i(\sqrt{z}c+g+fz)}}{2(f+id)}$$

**Arguments involving polynomials or algebraic functions and factors involving exponential function and a power function**

Involving exp and power

Involving  $z^n e^{dz} \sin(cz^r + fz)$

01.06.21.0593.01

$$\int z^n e^{dz} \sin(cz^2 + fz) dz =$$

$$\frac{1}{4\sqrt{ic}} \left( i e^{\frac{i(d+if)^2}{4c}} \sum_{q=0}^n 2^{q-n} (ic)^{-n-\frac{1}{2}} (-d-if)^{n-q} (d+if+2icz)^{q+1} \left( \frac{i(d+if+2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \right.$$

$$\left. \Gamma\left(\frac{q+1}{2}, \frac{i(d+if+2icz)^2}{4c}\right) - \frac{1}{4\sqrt{-ic}} \left( i e^{-\frac{i(d-if)^2}{4c}} \sum_{q=0}^n 2^{q-n} (-ic)^{-n-\frac{1}{2}} (if-d)^{n-q} \right.$$

$$\left. (d-if-2icz)^{q+1} \left( -\frac{i(d-if-2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-if-2icz)^2}{4c}\right) \right) ; n \in \mathbb{N}$$

01.06.21.0594.01

$$\int z^n e^{dz} \sin(\sqrt{z} c + fz) dz =$$

$$i 2^{-2(n+1)} \left( e^{\frac{c^2}{4(d-if)}} (d-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} (2(d-if)\sqrt{z}-ic)^{h+k} \left( -\frac{(2(d-if)\sqrt{z}-ic)^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( 2(d-if) \sqrt{-\frac{(2(d-if)\sqrt{z}-ic)^2}{d-if}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2(d-if)\sqrt{z}-ic)^2}{4(d-if)}\right) - \right.$$

$$\left. ic(2(d-if)\sqrt{z}-ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2(d-if)\sqrt{z}-ic)^2}{4(d-if)}\right) \right) -$$

$$e^{\frac{c^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z}(d+if)+ic)^{h+k} \left( -\frac{(2\sqrt{z}(d+if)+ic)^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( ci(2\sqrt{z}(d+if)+ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}(d+if)+ic)^2}{4(d+if)}\right) + \right.$$

$$\left. 2\sqrt{-\frac{(2\sqrt{z}(d+if)+ic)^2}{d+if}} (d+if) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}(d+if)+ic)^2}{4(d+if)}\right) \right) \right) ; n \in \mathbb{N}$$

Involving  $z^n e^{dz+e} \sin(cz^r + fz)$

01.06.21.0595.01

$$\int z^n e^{dz+e} \sin(cz^2 + fz) dz =$$

$$\frac{1}{4\sqrt{ic}} \left( i e^{\frac{i(d+if)^2}{4c} + e} \sum_{q=0}^n 2^{q-n} (ic)^{-n-\frac{1}{2}} (-d-if)^{n-q} (d+if+2icz)^{q+1} \left( \frac{i(d+if+2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+if+2icz)^2}{4c}\right) - \frac{1}{4\sqrt{-ic}} \left( i e^{-\frac{i(d-if)^2}{4c}} \sum_{q=0}^n 2^{q-n} (-ic)^{-n-\frac{1}{2}} (if-d)^{n-q} \right.$$

$$\left. (d-if-2icz)^{q+1} \left( -\frac{i(d-if-2icz)^2}{c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-if-2icz)^2}{4c}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0596.01

$$\int z^n e^{dz+e} \sin(\sqrt{z} c + fz) dz = i 2^{-2(n+1)} e^e$$

$$\left( e^{\frac{c^2}{4(d-if)}} (d-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} (2(d-if)\sqrt{z} - ic)^{h+k} \left( -\frac{(2(d-if)\sqrt{z} - ic)^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( 2(d-if) \sqrt{-\frac{(2(d-if)\sqrt{z} - ic)^2}{d-if}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2(d-if)\sqrt{z} - ic)^2}{4(d-if)}\right) - \right.$$

$$\left. ic(2(d-if)\sqrt{z} - ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2(d-if)\sqrt{z} - ic)^2}{4(d-if)}\right) \right) -$$

$$\left. e^{\frac{c^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z}(d+if) + ic)^{h+k} \left( -\frac{(2\sqrt{z}(d+if) + ic)^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( ci(2\sqrt{z}(d+if) + ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}(d+if) + ic)^2}{4(d+if)}\right) + \right.$$

$$\left. 2\sqrt{-\frac{(2\sqrt{z}(d+if) + ic)^2}{d+if}} (d+if) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}(d+if) + ic)^2}{4(d+if)}\right) \right) /; n \in \mathbb{N}$$

Involving  $z^n e^{bz'} \sin(cz' + fz)$

01.06.21.0597.01

$$\int z^n e^{b z^2} \sin(c z^2 + f z) dz =$$

$$\frac{1}{4\sqrt{b+ic}} \left( i e^{\frac{f^2}{4(b+ic)}} \sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-if)^{n-q} (if+2(b+ic)z)^{q+1} \left( -\frac{(if+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(if+2(b+ic)z)^2}{4(b+ic)}\right) \right) - \\ \frac{1}{4\sqrt{b-ic}} \left( i e^{\frac{f^2}{4(b-ic)}} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (if)^{n-q} (-if+2bz-2icz)^{q+1} \left( -\frac{(-if+2bz-2icz)^2}{b-ic} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(-if+2bz-2icz)^2}{4(b-ic)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0598.01

$$\int z^n e^{\sqrt{z} b} \sin(\sqrt{z} c + f z) dz =$$

$$i 2^{-2(n+1)} \left( e^{-\frac{i(b-ic)^2}{4f}} (-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic-2if\sqrt{z})^{h+k} \left( -\frac{i(b-ic-2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic-2if\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(b-ic-2if\sqrt{z})^2}{4f} \right) - \right.$$

$$\left. 2if \sqrt{-\frac{i(b-ic-2if\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(b-ic-2if\sqrt{z})^2}{4f} \right) \right) -$$

$$e^{\frac{i(b+ic)^2}{4f}} (if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2if\sqrt{z})^{h+k} \left( \frac{i(b+ic+2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b+ic)(b+ic+2if\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{i(b+ic+2if\sqrt{z})^2}{4f} \right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+ic+2if\sqrt{z})^2}{f}} f i \Gamma \left( \frac{1}{2}(h+k+2), \frac{i(b+ic+2if\sqrt{z})^2}{4f} \right) \right) \Bigg) ; n \in \mathbb{N}$$

Involving  $z^n e^{bz^r+e} \sin(cz^r + fz)$

01.06.21.0599.01

$$\int z^n e^{b z^2 + e} \sin(c z^2 + f z) dz =$$

$$\frac{1}{4\sqrt{b+ic}} \left( i e^{\frac{f^2}{4(b+ic)} + e} \sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-if)^{n-q} (if+2(b+ic)z)^{q+1} \left( -\frac{(if+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(if+2(b+ic)z)^2}{4(b+ic)}\right) \right) - \\ \frac{1}{4\sqrt{b-ic}} \left( i e^{\frac{f^2}{4(b-ic)} + e} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (if)^{n-q} (-if+2bz-2icz)^{q+1} \left( -\frac{(-if+2bz-2icz)^2}{b-ic} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(-if+2bz-2icz)^2}{4(b-ic)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0600.01

$$\int z^n e^{\sqrt{z} b+e} \sin(\sqrt{z} c+fz) dz = i 2^{-2(n+1)} e^e$$

$$\left( e^{-\frac{i(b-i c)^2}{4 f}} (-i f)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-i c)^{-h-k+2 n}(b-i c-2 i f \sqrt{z})^{h+k} \left( -\frac{i(b-i c-2 i f \sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b-i c)(b-i c-2 i f \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1),-\frac{i(b-i c-2 i f \sqrt{z})^2}{4 f}\right) - \right.$$

$$\left. 2 i f \sqrt{-\frac{i(b-i c-2 i f \sqrt{z})^2}{f}} \Gamma\left(\frac{1}{2}(h+k+2),-\frac{i(b-i c-2 i f \sqrt{z})^2}{4 f}\right) \right) -$$

$$\left. e^{\frac{i(b+i c)^2}{4 f}} (i f)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+i c)^{-h-k+2 n}(b+i c+2 i f \sqrt{z})^{h+k} \left( \frac{i(b+i c+2 i f \sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b+i c)(b+i c+2 i f \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1),\frac{i(b+i c+2 i f \sqrt{z})^2}{4 f}\right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+i c+2 i f \sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+k+2),\frac{i(b+i c+2 i f \sqrt{z})^2}{4 f}\right) \right) \Bigg) ; n \in \mathbb{N}$$

### Involving $z^n e^{b z^r+d z} \sin(c z^r+f z)$

01.06.21.0601.01

$$\int z^n e^{b z^2+d z} \sin(c z^2+f z) dz =$$

$$\frac{i}{4 \sqrt{b+i c}} e^{-\frac{(d+i f)^2}{4(b+i c)}} \sum_{q=0}^n 2^{q-n} (b+i c)^{-n-\frac{1}{2}} (-d-i f)^{n-q} (d+i f+2(b+i c) z)^{q+1} \left( -\frac{(d+i f+2(b+i c) z)^2}{b+i c} \right)^{\frac{1}{2}(-q-1)}$$

$$\binom{n}{q} \Gamma\left(\frac{q+1}{2},-\frac{(d+i f+2(b+i c) z)^2}{4(b+i c)}\right) - \frac{i}{4 \sqrt{b-i c}} e^{-\frac{(d-i f)^2}{4(b-i c)}} \sum_{q=0}^n 2^{q-n} (b-i c)^{-n-\frac{1}{2}} (i f-d)^{n-q}$$

$$(d-i f+2 b z-2 i c z)^{q+1} \left( -\frac{(d-i f+2 b z-2 i c z)^2}{b-i c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2},-\frac{(d-i f+2 b z-2 i c z)^2}{4(b-i c)}\right) ; n \in \mathbb{N}$$

01.06.21.0602.01

$$\int z^n e^{\sqrt{z} b+dz} \sin(\sqrt{z} c+fz) dz = i 2^{-2(n+1)} \left( e^{-\frac{(b-ic)^2}{4(d-if)}} (d-if)^{-2(n+1)} \right. \\ \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2(d-if)\sqrt{z})^{h+k} \left( -\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \\ \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic+2(d-if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) + \right. \\ \left. 2 \sqrt{-\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if}} (d-if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) - \\ e^{-\frac{(b+ic)^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2(d+if)\sqrt{z})^{h+k} \\ \left( -\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \\ \left( (b+ic)(b+ic+2(d+if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) + \right. \\ \left. 2 \sqrt{-\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if}} (d+if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) \Bigg) ; n \in \mathbb{N}$$

Involving  $z^n e^{bz^r+dz+e} \sin(cz^r+fz)$



01.06.21.0603.01

$$\int z^n e^{b z^2 + d z + e} \sin(c z^2 + f z) dz =$$

$$\frac{i}{4 \sqrt{b + i c}} e^{-\frac{(d + i f)^2}{4(b + i c)} + e} \sum_{q=0}^n 2^{q-n} (b + i c)^{-n - \frac{1}{2}} (-d - i f)^{n-q} (d + i f + 2(b + i c) z)^{q+1} \left( -\frac{(d + i f + 2(b + i c) z)^2}{b + i c} \right)^{\frac{1}{2}(-q-1)}$$

$$\binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + i f + 2(b + i c) z)^2}{4(b + i c)}\right) - \frac{i}{4 \sqrt{b - i c}} e^{-\frac{(d - i f)^2}{4(b - i c)} + e} \sum_{q=0}^n 2^{q-n} (b - i c)^{-n - \frac{1}{2}} (i f - d)^{n-q}$$

$$(d - i f + 2 b z - 2 i c z)^{q+1} \left( -\frac{(d - i f + 2 b z - 2 i c z)^2}{b - i c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d - i f + 2 b z - 2 i c z)^2}{4(b - i c)}\right); n \in \mathbb{N}$$

01.06.21.0604.01

$$\int z^n e^{\sqrt{z} b + dz + e} \sin(\sqrt{z} c + fz) dz = i 2^{-2(n+1)} e^e \left( e^{-\frac{(b-ic)^2}{4(d-if)}} (d-if)^{-2(n+1)} \right.$$

$$\sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2(d-if)\sqrt{z})^{h+k} \left( -\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left( \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic+2(d-if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) + \right.$$

$$\left. 2 \sqrt{-\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if}} (d-if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) \Bigg) -$$

$$e^{-\frac{(b+ic)^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2(d+if)\sqrt{z})^{h+k}$$

$$\left( -\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k}$$

$$\left( (b+ic)(b+ic+2(d+if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) +$$

$$\left. 2 \sqrt{-\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if}} (d+if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) \Bigg) \Bigg) ; n \in \mathbb{N}$$

Involving  $z^n e^{dz} \sin(cz^2 + fz + g)$

01.06.21.0605.01

$$\int z^n e^{dz} \sin(cz^2 + fz + g) dz = \frac{i}{4\sqrt{ic}} e^{\frac{i(d+if)^2}{4c} + ig} \sum_{q=0}^n 2^{q-n} (ic)^{-n-\frac{1}{2}} (-d-if)^{n-q} (d+if+2icz)^{q+1} \left(\frac{i(d+if+2icz)^2}{c}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+if+2icz)^2}{4c}\right) - \frac{i}{4\sqrt{-ic}} e^{-\frac{i(d-if)^2}{4c} - ig} \sum_{q=0}^n 2^{q-n} (-ic)^{-n-\frac{1}{2}} (if-d)^{n-q} (d-if-2icz)^{q+1} \left(-\frac{i(d-if-2icz)^2}{c}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-if-2icz)^2}{4c}\right); n \in \mathbb{N}$$

01.06.21.0606.01

$$\int z e^{dz} \sin(cz^2 + fz + g) dz = \frac{1}{8c^{3/2}} \left( e^{-\frac{i(3d^2-2ifd+f^2+4c^2z^2)}{4c}} \left( -\sqrt[4]{-1} e^{\frac{i(d^2+f^2+2c^2z^2)}{2c}} (d-if)\sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(f+id+2cz)}{2\sqrt{c}}\right) (i\cos(g) + \sin(g)) - 2\sqrt{c} e^{\frac{(d-if)(-f+3id+4cz)}{4c}} ((1+e^{2iz(f+cz)})\cos(g) + (-1+e^{2iz(f+cz)})i\sin(g)) + \sqrt[4]{-1} e^{\frac{i(d^2+c^2z^2)}{c}} (f-id)\sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(f-id+2cz)}{2\sqrt{c}}\right) (\cos(g) + i\sin(g)) \right) \right)$$

### Involving $z^n e^{dz+e} \sin(cz^r + fz + g)$

01.06.21.0607.01

$$\int z^n e^{dz+e} \sin(cz^2 + fz + g) dz = \frac{1}{4\sqrt{ic}} \left( i e^{\frac{i(d+if)^2}{4c} + e+ig} \sum_{q=0}^n 2^{q-n} (ic)^{-n-\frac{1}{2}} (-d-if)^{n-q} (d+if+2icz)^{q+1} \left(\frac{i(d+if+2icz)^2}{c}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+if+2icz)^2}{4c}\right) - \frac{1}{4\sqrt{-ic}} \left( i e^{-\frac{i(d-if)^2}{4c} + e-ig} \sum_{q=0}^n 2^{q-n} (-ic)^{-n-\frac{1}{2}} (if-d)^{n-q} (d-if-2icz)^{q+1} \left(-\frac{i(d-if-2icz)^2}{c}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-if-2icz)^2}{4c}\right) \right) \right); n \in \mathbb{N}$$

01.06.21.0608.01

$$\int z^n e^{dz+e} \sin(\sqrt{z} c + f z + g) dz = i 2^{-2(n+1)} e^{e-ig}$$

$$\left( e^{\frac{c^2}{4(d-if)}} (d-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic)^{-h-k+2n} (2(d-if)\sqrt{z} - ic)^{h+k} \left( -\frac{(2(d-if)\sqrt{z} - ic)^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( 2(d-if) \sqrt{-\frac{(2(d-if)\sqrt{z} - ic)^2}{d-if}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2(d-if)\sqrt{z} - ic)^2}{4(d-if)}\right) - \right.$$

$$\left. ic(2(d-if)\sqrt{z} - ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2(d-if)\sqrt{z} - ic)^2}{4(d-if)}\right) \right) -$$

$$e^{\frac{c^2}{4(d+if)}+2ig} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic)^{-h-k+2n} (2\sqrt{z}(d+if) + ic)^{h+k} \left( -\frac{(2\sqrt{z}(d+if) + ic)^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( ci(2\sqrt{z}(d+if) + ic) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}(d+if) + ic)^2}{4(d+if)}\right) + \right.$$

$$\left. 2\sqrt{-\frac{(2\sqrt{z}(d+if) + ic)^2}{d+if}} (d+if) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}(d+if) + ic)^2}{4(d+if)}\right) \right) /; n \in \mathbb{N}$$

### Involving $z^n e^{bz'} \sin(cz' + fz + g)$

01.06.21.0609.01

$$\int z^n e^{bz^2} \sin(cz^2 + fz + g) dz =$$

$$\frac{1}{4\sqrt{b+ic}} \left( i e^{\frac{f^2}{4(b+ic)}+ig} \sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-if)^{n-q} (if+2(b+ic)z)^{q+1} \left( -\frac{(if+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(if+2(b+ic)z)^2}{4(b+ic)}\right) \right) - \frac{1}{4\sqrt{b-ic}} \left( i e^{\frac{f^2}{4(b-ic)}-ig} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (if)^{n-q} \right.$$

$$\left. (-if+2bz-2icz)^{q+1} \left( -\frac{(-if+2bz-2icz)^2}{b-ic} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(-if+2bz-2icz)^2}{4(b-ic)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0610.01

$$\int z^n e^{\sqrt{z} b} \sin(\sqrt{z} c + f z + g) dz = i 2^{-2(n+1)} e^{-ig}$$

$$\left( e^{-\frac{i(b-ic)^2}{4f}} (-if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic-2if\sqrt{z})^{h+k} \left( -\frac{i(b-ic-2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right)$$

$$\binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic-2if\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(b-ic-2if\sqrt{z})^2}{4f} \right) - \right.$$

$$\left. 2if \sqrt{-\frac{i(b-ic-2if\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(b-ic-2if\sqrt{z})^2}{4f} \right) \right)$$

$$e^{\frac{i(b+ic)^2}{4f} + 2ig} (if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2if\sqrt{z})^{h+k} \left( \frac{i(b+ic+2if\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( (b+ic)(b+ic+2if\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{i(b+ic+2if\sqrt{z})^2}{4f} \right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+ic+2if\sqrt{z})^2}{f}} f i \Gamma \left( \frac{1}{2}(h+k+2), \frac{i(b+ic+2if\sqrt{z})^2}{4f} \right) \right) ; n \in \mathbb{N}$$

Involving  $z^n e^{bz^r+e} \sin(cz^r + fz + g)$

01.06.21.0611.01

$$\int z^n e^{b z^2 + e} \sin(c z^2 + f z + g) dz =$$

$$\frac{1}{4 \sqrt{b + i c}} \left( i e^{\frac{f^2}{4(b+i c)} + e + i g} \sum_{q=0}^n 2^{q-n} (b + i c)^{-n - \frac{1}{2}} (-i f)^{n-q} (i f + 2(b + i c) z)^{q+1} \left( -\frac{(i f + 2(b + i c) z)^2}{b + i c} \right)^{\frac{1}{2}(-q-1)} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(i f + 2(b + i c) z)^2}{4(b + i c)}\right) \right) -$$

$$\frac{1}{4 \sqrt{b - i c}} \left( i e^{\frac{f^2}{4(b-i c)} + e - i g} \sum_{q=0}^n 2^{q-n} (b - i c)^{-n - \frac{1}{2}} (i f)^{n-q} (-i f + 2 b z - 2 i c z)^{q+1} \right. \\ \left. \left( -\frac{(-i f + 2 b z - 2 i c z)^2}{b - i c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(-i f + 2 b z - 2 i c z)^2}{4(b - i c)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.0612.01

$$\int z^n e^{\sqrt{z} b+e} \sin(\sqrt{z} c+fz+g) dz = i 2^{-2(n+1)} e^{e-ig}$$

$$\left( e^{-\frac{i(b-i c)^2}{4f}} (-i f)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-i c)^{-h-k+2n} (b-i c-2 i f \sqrt{z})^{h+k} \left( -\frac{i(b-i c-2 i f \sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( (b-i c)(b-i c-2 i f \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{i(b-i c-2 i f \sqrt{z})^2}{4f}\right) - \right.$$

$$\left. 2 i f \sqrt{-\frac{i(b-i c-2 i f \sqrt{z})^2}{f}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{i(b-i c-2 i f \sqrt{z})^2}{4f}\right) \right) \left. \right)$$

$$e^{\frac{i(b+i c)^2}{4f}+2ig} (i f)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+i c)^{-h-k+2n} (b+i c+2 i f \sqrt{z})^{h+k} \left( \frac{i(b+i c+2 i f \sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left( \binom{k}{h} \binom{n}{k} \left( (b+i c)(b+i c+2 i f \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+i c+2 i f \sqrt{z})^2}{4f}\right) + \right.$$

$$\left. 2 \sqrt{\frac{i(b+i c+2 i f \sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+i c+2 i f \sqrt{z})^2}{4f}\right) \right) \right) ; n \in \mathbb{N}$$

**Involving  $z^n e^{bz^r+dz} \sin(cz^r+fz+g)$**

01.06.21.0613.01

$$\int z^n e^{bz^2+dz} \sin(cz^2+fz+g) dz =$$

$$\frac{i}{4 \sqrt{b+i c}} e^{-\frac{(d+if)^2}{4(b+i c)}+ig} \sum_{q=0}^n 2^{q-n} (b+i c)^{-n-\frac{1}{2}} (-d-i f)^{n-q} (d+i f+2(b+i c)z)^{q+1} \left( -\frac{(d+i f+2(b+i c)z)^2}{b+i c} \right)^{\frac{1}{2}(-q-1)}$$

$$\binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+i f+2(b+i c)z)^2}{4(b+i c)}\right) - \frac{i}{4 \sqrt{b-i c}} e^{-\frac{(d-if)^2}{4(b-i c)}-ig} \sum_{q=0}^n 2^{q-n} (b-i c)^{-n-\frac{1}{2}} (i f-d)^{n-q}$$

$$(d-i f+2bz-2icz)^{q+1} \left( -\frac{(d-i f+2bz-2icz)^2}{b-i c} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d-i f+2bz-2icz)^2}{4(b-i c)}\right) ; n \in \mathbb{N}$$

01.06.21.0614.01

$$\int z^n e^{\sqrt{z} b+dz} \sin(\sqrt{z} c+fz+g) dz = i 2^{-2(n+1)} e^{-ig} \left( e^{-\frac{(b-ic)^2}{4(d-if)}} (d-if)^{-2(n+1)} \right. \\ \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2(d-if)\sqrt{z})^{h+k} \left( -\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \\ \left( \begin{matrix} k \\ h \end{matrix} \right) \binom{n}{k} \left( (b-ic)(b-ic+2(d-if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right. \\ \left. \left. 2 \sqrt{-\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if}} (d-if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) \right) - \\ e^{2ig-\frac{(b+ic)^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2(d+if)\sqrt{z})^{h+k} \\ \left( -\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \\ \left( (b+ic)(b+ic+2(d+if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right. \\ \left. \left. 2 \sqrt{-\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if}} (d+if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) \right) \Bigg) /; n \in \mathbb{N}$$

Involving  $z^n e^{bz^r+dz+e} \sin(cz^r+fz+g)$



01.06.21.0615.01

$$\int z^n e^{b z^2 + d z + e} \sin(c z^2 + f z + g) dz =$$

$$\frac{i}{4\sqrt{b+ic}} e^{-\frac{(d+if)^2}{4(b+ic)} + e + ig} \sum_{q=0}^n 2^{q-n} (b+ic)^{-n-\frac{1}{2}} (-d-if)^{n-q} (d+if+2(b+ic)z)^{q+1} \left( -\frac{(d+if+2(b+ic)z)^2}{b+ic} \right)^{\frac{1}{2}(-q-1)}$$

$$\binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+if+2(b+ic)z)^2}{4(b+ic)}\right) - \frac{i}{4\sqrt{b-ic}} e^{-\frac{(d-if)^2}{4(b-ic)} + e - ig} \sum_{q=0}^n 2^{q-n} (b-ic)^{-n-\frac{1}{2}} (if-d)^{n-q}$$

$$(d-if+2bz-2icz)^{q+1} \left( -\frac{(d-if+2bz-2icz)^2}{b-ic} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d-if+2bz-2icz)^2}{4(b-ic)}\right); n \in \mathbb{N}$$

01.06.21.0616.01

$$\int z^n e^{\sqrt{z} b+dz+e} \sin(\sqrt{z} c+fz+g) dz = i 2^{-2(n+1)} e^{e-ig} \left( e^{-\frac{(b-ic)^2}{4(d-if)}} (d-if)^{-2(n+1)} \right. \\ \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b-ic)^{-h-k+2n} (b-ic+2(d-if)\sqrt{z})^{h+k} \left( -\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if} \right)^{\frac{1}{2}(-h-k-1)} \\ \binom{k}{h} \binom{n}{k} \left( (b-ic)(b-ic+2(d-if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) + \right. \\ \left. 2 \sqrt{-\frac{(b-ic+2(d-if)\sqrt{z})^2}{d-if}} (d-if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b-ic+2(d-if)\sqrt{z})^2}{4(d-if)} \right) \right) \\ e^{2ig-\frac{(b+ic)^2}{4(d+if)}} (d+if)^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ic)^{-h-k+2n} (b+ic+2(d+if)\sqrt{z})^{h+k} \\ \left( -\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \\ \left( (b+ic)(b+ic+2(d+if)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) + \right. \\ \left. 2 \sqrt{-\frac{(b+ic+2(d+if)\sqrt{z})^2}{d+if}} (d+if) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+ic+2(d+if)\sqrt{z})^2}{4(d+if)} \right) \right) \Bigg) ; n \in \mathbb{N}$$

**Involving functions of the direct function**

**Involving powers of the direct function**

Involving powers of sin

**Involving  $\sin^v(az)$**

01.06.21.0617.01

$$\int \sin^{\nu}(a z) dz = -\frac{\cos(a z) \sin^{\nu+1}(a z) \sin^2(a z)^{\frac{1}{2}(-\nu-1)}}{a} {}_2F_1\left(\frac{1}{2}, \frac{1-\nu}{2}; \frac{3}{2}; \cos^2(a z)\right)$$

01.06.21.0618.01

$$\int \sin^2(a z) dz = \frac{z}{2} - \frac{\sin(2 a z)}{4 a}$$

01.06.21.0619.01

$$\int \sin^3(a z) dz = \frac{\cos(3 a z) - 9 \cos(a z)}{12 a}$$

01.06.21.0620.01

$$\int \sin^4(a z) dz = \frac{12 a z - 8 \sin(2 a z) + \sin(4 a z)}{32 a}$$

01.06.21.0621.01

$$\int \sin^5(a z) dz = -\frac{150 \cos(a z) - 25 \cos(3 a z) + 3 \cos(5 a z)}{240 a}$$

01.06.21.0622.01

$$\int \sin^6(a z) dz = -\frac{-60 a z + 45 \sin(2 a z) - 9 \sin(4 a z) + \sin(6 a z)}{192 a}$$

01.06.21.0623.01

$$\int \sin^7(a z) dz = \frac{-1225 \cos(a z) + 245 \cos(3 a z) - 49 \cos(5 a z) + 5 \cos(7 a z)}{2240 a}$$

01.06.21.0624.01

$$\int \sin^8(a z) dz = \frac{840 a z - 672 \sin(2 a z) + 168 \sin(4 a z) - 32 \sin(6 a z) + 3 \sin(8 a z)}{3072 a}$$

01.06.21.1614.01

$$\int \sin^{2n}(a z) dz = \frac{\left(\frac{1}{2}\right)_n}{2 a n!} \left( 2 a z - \cot(a z) \sum_{k=1}^n \frac{(k-1)! \sin^{2k}(a z)}{\left(\frac{1}{2}\right)_k} \right) /; n \in \mathbb{N}$$

01.06.21.1615.01

$$\int \sin^{2n+1}(a z) dz = -\frac{n! \cos^{2n+1}(a z)}{a} \sum_{k=0}^n \frac{\tan^{2k}(a z)}{k! \left(\frac{3}{2}\right)_{n-k}} /; n \in \mathbb{N}$$

01.06.21.1616.01

$$\int \sin^{2n}(a z) dz = \frac{\cos(a z) \sin^{2n+1}(a z)}{a(2n+1)} {}_2F_1\left(1, n+1; n+\frac{3}{2}; \sin^2(a z)\right) + \frac{a z \left(\frac{1}{2}\right)_n}{a n!} - \frac{\left(\frac{1}{2}\right)_n \sin^{-1}(\sin(a z)) \cos(a z)}{a n! \sqrt{\cos^2(a z)}} /; n \in \mathbb{N}$$

01.06.21.1617.01

$$\int \sin^{2n+1}(a z) dz = \frac{\sec(a z) \sin^{2n+2}(a z)}{2 a(n+1)} {}_2F_1\left(\frac{1}{2}, 1; n+2; -\tan^2(a z)\right) - \frac{\cos(a z) n! \sqrt{\sec^2(a z)}}{a \left(\frac{3}{2}\right)_n} /; n \in \mathbb{N}$$

01.06.21.0625.01

$$\int \sin^{\frac{3}{2}}(a z) dz = -\frac{2}{3 a} \left( \sin^{\frac{1}{2}}(a z) \cos(a z) + F\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right) \right)$$

01.06.21.0626.01

$$\int \sin^{\frac{1}{2}}(a z) dz = -\frac{2}{a} E\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right)$$

01.06.21.0627.01

$$\int \frac{1}{\sin^{\frac{1}{2}}(a z)} dz = -\frac{2}{a} F\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right)$$

01.06.21.0628.01

$$\int \frac{1}{\sin^{\frac{3}{2}}(a z)} dz = \frac{2}{a} \left( E\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right) - \frac{\cos(a z)}{\sin^{\frac{1}{2}}(a z)} \right)$$

01.06.21.0629.01

$$\int \frac{1}{\sqrt{\sin^3(a z)}} dz = -\frac{1}{a \sqrt{\sin^3(a z)}} \left( \sin(2 a z) - 2 E\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right) \sin^{\frac{3}{2}}(a z) \right)$$

01.06.21.0630.01

$$\int \frac{1}{\sin^{\frac{5}{2}}(a z)} dz = -\frac{1}{3 a} \left( \frac{2 \cos(a z)}{\sin^{\frac{3}{2}}(a z)} + 2 F\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right) \right)$$

01.06.21.0631.01

$$\int \frac{1}{\sqrt{\sin^5(a z)}} dz = -\frac{1}{3 a \sqrt{\sin^5(a z)}} \left( 2 F\left(\frac{1}{4}(\pi - 2 a z) \mid 2\right) \sin^{\frac{5}{2}}(a z) + \sin(2 a z) \right)$$

### Involving $\sin^v(a z + b)$

01.06.21.0632.01

$$\int \sin^v(b + a z) dz = -\frac{\cos(b + a z) \sin^{v+1}(b + a z) \sin^2(b + a z)^{\frac{1}{2}(-v-1)}}{a} {}_2F_1\left(\frac{1}{2}, \frac{1-v}{2}; \frac{3}{2}; \cos^2(b + a z)\right)$$

### Involving $\sin^v\left(a z^2 + \frac{b}{z^2}\right)$

01.06.21.0633.01

$$\int \sin^v \left( a z^2 + \frac{b}{z^2} \right) dz = 2^{-v} z^{\left( \frac{v}{2} \right)} (1 - v \bmod 2) + 2^{-v-2} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{-i a (2k-v)}} i^v e^{-2\sqrt{-i a (2k-v)} \sqrt{-i b (2k-v)}} \left( e^{4\sqrt{-i a (2k-v)} \sqrt{-i b (2k-v)}} \right. \right. \\ \left. \left. \left( \operatorname{erf} \left( \sqrt{-i a (2k-v)} z + \frac{\sqrt{-i b (2k-v)}}{z} \right) - 1 \right) - \operatorname{erf} \left( \frac{\sqrt{-i b (2k-v)}}{z} - \sqrt{-i a (2k-v)} z \right) + 1 \right) + \frac{1}{\sqrt{i a (2k-v)}} i^{-v} e^{-2\sqrt{i a (2k-v)} \sqrt{i b (2k-v)}} \left( e^{4\sqrt{i a (2k-v)} \sqrt{i b (2k-v)}} \right. \right. \\ \left. \left. \left( \operatorname{erf} \left( \sqrt{i a (2k-v)} z + \frac{\sqrt{i b (2k-v)}}{z} \right) - 1 \right) - \operatorname{erf} \left( \frac{\sqrt{i b (2k-v)}}{z} - \sqrt{i a (2k-v)} z \right) + 1 \right) \right) /; v \in \mathbb{N}^+$$

### Involving $\sin^v \left( a z^2 + \frac{b}{z^2} + c \right)$

01.06.21.0634.01

$$\int \sin^v \left( a z^2 + \frac{b}{z^2} + c \right) dz = 2^{-v} z^{\left( \frac{v}{2} \right)} (1 - v \bmod 2) + 2^{-v-2} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{-i \left( \frac{\pi v}{2} - c (v-2k) \right)} \left( \frac{1}{\sqrt{-i a (2k-v)}} \left( e^{2i \left( \frac{\pi v}{2} - c (v-2k) \right) - 2\sqrt{-i a (2k-v)} \sqrt{-i b (2k-v)}} \left( e^{4\sqrt{-i a (2k-v)} \sqrt{-i b (2k-v)}} \right. \right. \right. \\ \left. \left. \left( \operatorname{erf} \left( \sqrt{-i a (2k-v)} z + \frac{\sqrt{-i b (2k-v)}}{z} \right) - 1 \right) - \operatorname{erf} \left( \frac{\sqrt{-i b (2k-v)}}{z} - \sqrt{-i a (2k-v)} z \right) + 1 \right) + \frac{1}{\sqrt{i a (2k-v)}} \left( e^{-2\sqrt{i a (2k-v)} \sqrt{i b (2k-v)}} \left( e^{4\sqrt{i a (2k-v)} \sqrt{i b (2k-v)}} \right. \right. \right. \\ \left. \left. \left( \operatorname{erf} \left( \sqrt{i a (2k-v)} z + \frac{\sqrt{i b (2k-v)}}{z} \right) - 1 \right) - \operatorname{erf} \left( \frac{\sqrt{i b (2k-v)}}{z} - \sqrt{i a (2k-v)} z \right) + 1 \right) \right) \right) /; v \in \mathbb{N}^+$$

### Involving $\sin^v (a z^r)$

01.06.21.0635.01

$$\int \sin^v (a z^r) dz = 2^{-v} z^{\left( \frac{v}{2} \right)} (1 - v \bmod 2) - \frac{2^{-v} z}{r} \sum_{i=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^i \binom{v}{i} \left( e^{-\frac{1}{2} i \pi v} \Gamma \left( \frac{1}{r}, -i a (v-2i) z^r \right) (-i a (v-2i) z^r)^{-1/r} + e^{\frac{i \pi v}{2}} (i a (v-2i) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, i a (v-2i) z^r \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0636.01

$$\int \sin^v(a z^2) dz = 2^{-v} z \binom{v}{\frac{v}{2}} (1 - v \bmod 2) + \frac{2^{\frac{1}{2}-v} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \cos\left(\frac{\pi v}{2}\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{a(v-2k)} z\right) + S\left(\sqrt{\frac{2}{\pi}} \sqrt{a(v-2k)} z\right) \sin\left(\frac{\pi v}{2}\right) \right)}{\sqrt{a(v-2k)}}; v \in \mathbb{N}^+$$

01.06.21.0637.01

$$\int \sin^v(a \sqrt{z}) dz = 2^{-v} z \binom{v}{\frac{v}{2}} (1 - v \bmod 2) + \frac{2^{2-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} - a(v-2k)\sqrt{z}\right) - a(v-2k)\sqrt{z} \sin\left(\frac{\pi v}{2} - a(v-2k)\sqrt{z}\right) \right)}{a^2 (v-2k)^2}; v \in \mathbb{N}^+$$

### Involving $\sin^v(a(z^r)^p)$

01.06.21.0638.01

$$\int \sin^v(a(z^r)^p) dz = 2^{-v} z \binom{v}{\frac{v}{2}} (1 - v \bmod 2) - \frac{2^{-v} z^{\frac{v-1}{2}}}{pr} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( i^{-v} \Gamma\left(\frac{1}{pr}, -ia(v-2k)(z^r)^p\right) (-ia(v-2k)(z^r)^p)^{-\frac{1}{pr}} + i^v (ia(v-2k)(z^r)^p)^{-\frac{1}{pr}} \Gamma\left(\frac{1}{pr}, ia(v-2k)(z^r)^p\right) \right); v \in \mathbb{N}^+$$

01.06.21.0639.01

$$\int \sin^v(a(z^r)^{1/r}) dz = 2^{-v} z \binom{v}{\frac{v}{2}} (1 - v \bmod 2) + \frac{2(z^r)^{-1/r}}{a} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{e^{ik\pi}}{2k-v} \binom{v}{k} \sin\left(a(2k-v)(z^r)^{1/r} + \frac{\pi v}{2}\right); v \in \mathbb{N}^+$$

01.06.21.0640.01

$$\int \sin^v(a\sqrt{z^2}) dz = 2^{-v} z \binom{v}{\frac{v}{2}} (1 - v \bmod 2) + \frac{2}{a\sqrt{z^2}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{e^{ik\pi}}{2k-v} \binom{v}{k} \sin\left(a\sqrt{z^2}(2k-v) + \frac{\pi v}{2}\right); v \in \mathbb{N}^+$$

### Involving $\sin^v(a z^r + b)$

01.06.21.0641.01

$$\int \sin^v(a z^r + b) dz = 2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) z - \frac{2^{-v} z^{\frac{v-1}{2}}}{r} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{ib(v-2k) - \frac{i\pi v}{2}} \Gamma\left(\frac{1}{r}, -ia(v-2k)z^r\right) (-ia(v-2k)z^r)^{-\frac{1}{r}} + e^{\frac{i\pi v}{2} - ib(v-2k)} (ia(v-2k)z^r)^{-\frac{1}{r}} \Gamma\left(\frac{1}{r}, ia(v-2k)z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.0642.01

$$\int \sin^{\nu}(a z^2 + b) dz = 2^{-\nu} z \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) + \frac{2^{\frac{1}{2}-\nu} \sqrt{\pi}}{\sqrt{a}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{1}{\sqrt{\nu-2k}} (-1)^k \binom{\nu}{k} \left( \cos\left(2bk - b\nu + \frac{\pi\nu}{2}\right) C\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{\nu-2k} z\right) + S\left(\sqrt{a} \sqrt{\frac{2}{\pi}} \sqrt{\nu-2k} z\right) \sin\left(2bk - b\nu + \frac{\pi\nu}{2}\right) \right); \nu \in \mathbb{N}^+$$

01.06.21.0643.01

$$\int \sin^{\nu}(\sqrt{z} a + b) dz = 2^{-\nu} z \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) + \frac{2^{2-\nu}}{a^2} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{1}{(\nu-2k)^2} (-1)^k \binom{\nu}{k} \left( \cos\left(2bk - b\nu + \frac{\pi\nu}{2} + a(2k-\nu)\sqrt{z}\right) + a(2k-\nu)\sqrt{z} \sin\left(2bk - b\nu + \frac{\pi\nu}{2} + a(2k-\nu)\sqrt{z}\right) \right); \nu \in \mathbb{N}^+$$

### Involving $\sin^{\nu}(a z^r + b z)$

01.06.21.0644.01

$$\int \sin^{\nu}(a z^2 + b z) dz = 2^{-\nu} z \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) + \frac{2^{\frac{1}{2}-\nu} \sqrt{\pi}}{\sqrt{a}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{(-1)^k}{\sqrt{\nu-2k}} \binom{\nu}{k} \left( \cos\left(\frac{1}{4} \left( \frac{(\nu-2k)b^2}{a} + 2\pi\nu \right)\right) C\left(\frac{\sqrt{\nu-2k}(b+2az)}{\sqrt{a}\sqrt{2\pi}}\right) + S\left(\frac{\sqrt{\nu-2k}(b+2az)}{\sqrt{a}\sqrt{2\pi}}\right) \sin\left(\frac{1}{4} \left( \frac{(\nu-2k)b^2}{a} + 2\pi\nu \right)\right) \right); \nu \in \mathbb{N}^+$$

01.06.21.0645.01

$$\int \sin^{\nu}(\sqrt{z} a + b z) dz = 2^{-\nu} z \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) + \frac{2^{-\nu}}{b^{3/2}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{1}{(\nu-2k)^{3/2}} \left( (-1)^k \binom{\nu}{k} \left( a \sqrt{2\pi} (2k-\nu) \cos\left(\frac{1}{4} \left( \frac{(\nu-2k)a^2}{b} + 2\pi\nu \right)\right) C\left(\frac{\sqrt{\nu-2k}(a+2b\sqrt{z})}{\sqrt{b}\sqrt{2\pi}}\right) + a \sqrt{2\pi} (2k-\nu) S\left(\frac{\sqrt{\nu-2k}(a+2b\sqrt{z})}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{1}{4} \left( \frac{(\nu-2k)a^2}{b} + 2\pi\nu \right)\right) - 2\sqrt{b}\sqrt{\nu-2k} \sin\left((a+b\sqrt{z})\sqrt{z}(2k-\nu) + \frac{\pi\nu}{2}\right) \right) \right); \nu \in \mathbb{N}^+$$

### Involving $\sin^{\nu}(a z^r + b z + c)$

01.06.21.0646.01

$$\int \sin^{\nu}(a z^2 + b z + c) dz = 2^{-\nu} z \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) + \frac{1}{\sqrt{a}} \left[ \left( 2^{\frac{1}{2}-\nu} \sqrt{\pi} \right) \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{1}{\sqrt{\nu-2k}} \left( (-1)^k \binom{\nu}{k} \cos \left( \frac{1}{4} \left( \frac{(\nu-2k)b^2}{a} + 8ck - 4c\nu + 2\pi\nu \right) \right) C \left( \frac{\sqrt{\nu-2k}(b+2az)}{\sqrt{a}\sqrt{2\pi}} \right) + S \left( \frac{\sqrt{\nu-2k}(b+2az)}{\sqrt{a}\sqrt{2\pi}} \right) \sin \left( \frac{1}{4} \left( \frac{(\nu-2k)b^2}{a} + 8ck - 4c\nu + 2\pi\nu \right) \right) \right] /; \nu \in \mathbb{N}^+$$

01.06.21.0647.01

$$\int \sin^{\nu}(\sqrt{z} a + b z + c) dz = 2^{-\nu} z \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) + \frac{2^{-\nu}}{b^{3/2}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{1}{(\nu-2k)^{3/2}} (-1)^k \binom{\nu}{k} \left[ a \sqrt{2\pi} (2k-\nu) \cos \left( \frac{1}{4} \left( \frac{(\nu-2k)a^2}{b} + 8ck - 4c\nu + 2\pi\nu \right) \right) C \left( \frac{\sqrt{\nu-2k}(a+2b\sqrt{z})}{\sqrt{b}\sqrt{2\pi}} \right) + a \sqrt{2\pi} (2k-\nu) S \left( \frac{\sqrt{\nu-2k}(a+2b\sqrt{z})}{\sqrt{b}\sqrt{2\pi}} \right) \sin \left( \frac{1}{4} \left( \frac{(\nu-2k)a^2}{b} + 8ck - 4c\nu + 2\pi\nu \right) \right) - 2\sqrt{b}\sqrt{\nu-2k} \sin \left( c(2k-\nu) + (a+b\sqrt{z})\sqrt{z} (2k-\nu) + \frac{\pi\nu}{2} \right) \right] /; \nu \in \mathbb{N}^+$$

### Involving products of the direct function

Involving products of two direct functions

#### Involving $\sin(cz)\sin(az)$

01.06.21.0648.01

$$\int \sin(cz)\sin(az) dz = \frac{c \cos(cz)\sin(az) - a \cos(az)\sin(cz)}{a^2 - c^2}$$

#### Involving $\sin(cz)\sin(az+b)$

01.06.21.0649.01

$$\int \sin(cz)\sin(az+b) dz = \frac{(a+c)\sin(b+(a-c)z) + (c-a)\sin(b+(a+c)z)}{2(a-c)(a+c)}$$

#### Involving $\sin(cz+d)\sin(az+b)$

01.06.21.0650.01

$$\int \sin(cz+d)\sin(az+b) dz = \frac{(c-a)\sin(b+d+(a+c)z) + (a+c)\sin(b-d+az-cz)}{2(a-c)(a+c)}$$



### Involving $\sin(dz) \sin(cz^r)$

01.06.21.0651.01

$$\int \sin(dz) \sin(cz^2) dz = \frac{1}{2\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{d^2}{4c}\right) C\left(\frac{2cz-d}{\sqrt{c}\sqrt{2\pi}}\right) - \cos\left(\frac{d^2}{4c}\right) C\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) + S\left(\frac{2cz-d}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c}\right) - S\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c}\right) \right) \right)$$

01.06.21.0652.01

$$\int \sin(dz) \sin(c\sqrt{z}) dz = \frac{1}{4d^{3/2}} \left( c\sqrt{2\pi} \left( \cos\left(\frac{c^2}{4d}\right) \left( C\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) + C\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \right) + \left( S\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) + S\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \right) \sin\left(\frac{c^2}{4d}\right) \right) - 4\sqrt{d} \cos(dz) \sin(c\sqrt{z}) \right)$$

### Involving $\sin(dz + e) \sin(cz^r)$

01.06.21.0653.01

$$\int \sin(e + dz) \sin(cz^2) dz = \frac{1}{2\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{d^2}{4c} + e\right) C\left(\frac{2cz-d}{\sqrt{c}\sqrt{2\pi}}\right) - \cos\left(\frac{d^2}{4c} - e\right) C\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - S\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c} - e\right) + S\left(\frac{2cz-d}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c} + e\right) \right) \right)$$

01.06.21.0654.01

$$\int \sin(e + dz) \sin(c\sqrt{z}) dz = \frac{1}{4d^{3/2}} \left( c\sqrt{2\pi} \left( \cos\left(\frac{c^2}{4d} - e\right) \left( C\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) + C\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \right) + \left( S\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) + S\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \right) \sin\left(\frac{c^2}{4d} - e\right) \right) - 4\sqrt{d} \cos(e + dz) \sin(c\sqrt{z}) \right)$$

### Involving $\sin(bz^r) \sin(cz^r)$

01.06.21.0655.01

$$\int \sin(bz^r) \sin(cz^r) dz = -\frac{z}{4r} \left( \Gamma\left(\frac{1}{r}, (-ib + ic)z^r\right) ((-ib + ic)z^r)^{-1/r} - ((ib + ic)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib + ic)z^r\right) - ((-ib - ic)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-ib - ic)z^r\right) + ((ib - ic)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib - ic)z^r\right) \right)$$

01.06.21.0656.01

$$\int \sin(bz^2) \sin(cz^2) dz = \frac{1}{2} \sqrt{\frac{\pi}{2}} \left( \frac{1}{\sqrt{b-c}} C\left(\sqrt{b-c} \sqrt{\frac{2}{\pi}} z\right) - \frac{1}{\sqrt{b+c}} C\left(\sqrt{b+c} \sqrt{\frac{2}{\pi}} z\right) \right)$$

01.06.21.0657.01

$$\int \sin(b\sqrt{z}) \sin(c\sqrt{z}) dz = \sqrt{z} \left( \frac{\sin((b-c)\sqrt{z})}{b-c} - \frac{\sin((b+c)\sqrt{z})}{b+c} \right) + \frac{\cos((b-c)\sqrt{z})}{(b-c)^2} - \frac{\cos((b+c)\sqrt{z})}{(b+c)^2}$$

### Involving $\sin(dz) \sin(cz^f + g)$

01.06.21.0658.01

$$\int \sin(dz) \sin(cz^2 + g) dz = \frac{1}{2\sqrt{-c}\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{c} \cos\left(\frac{d^2}{4c} - g\right) C\left(\frac{d-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) - \sqrt{-c} \cos\left(\frac{d^2}{4c} - g\right) C\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - \sqrt{c} S\left(\frac{d-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c} - g\right) - \sqrt{-c} S\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c} - g\right) \right) \right)$$

01.06.21.0659.01

$$\int \sin(dz) \sin(\sqrt{z}c + g) dz = \frac{1}{2} \left( \frac{1}{d^{3/2}} \left( c \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{c^2}{4d} + g\right) C\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) + \cos\left(\frac{c^2-4dg}{4d}\right) C\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + S\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{c^2-4dg}{4d}\right) + S\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{c^2}{4d} + g\right) \right) \right) - \frac{2\cos(dz) \sin(\sqrt{z}c + g)}{d} \right)$$

### Involving $\sin(dz + e) \sin(cz^f + g)$

01.06.21.0660.01

$$\int \sin(dz + e) \sin(cz^2 + g) dz = \frac{1}{2\sqrt{-c}\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{c} \cos\left(\frac{d^2}{4c} + e - g\right) C\left(\frac{d-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) - \sqrt{-c} \cos\left(\frac{d^2}{4c} - e - g\right) C\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - \sqrt{-c} S\left(\frac{d+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c} - e - g\right) - \sqrt{c} S\left(\frac{d-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4c} + e - g\right) \right) \right)$$

01.06.21.0661.01

$$\int \sin(dz + e) \sin(\sqrt{z}c + g) dz = \frac{1}{2} \left( \frac{1}{d^{3/2}} \left( c \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{c^2}{4d} - e + g\right) C\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) + \cos\left(\frac{c^2-4d(e+g)}{4d}\right) C\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + S\left(\frac{c+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{c^2-4d(e+g)}{4d}\right) + S\left(\frac{2d\sqrt{z}-c}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{c^2}{4d} - e + g\right) \right) \right) - \frac{2\cos(e+dz) \sin(\sqrt{z}c + g)}{d} \right)$$

### Involving $\sin(b z^r) \sin(c z^r + g)$

01.06.21.0662.01

$$\int \sin(b z^r) \sin(c z^r + g) dz = \frac{1}{4r} \left( e^{-ig} z \left( -(-i(b-c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(b-c)z^r\right) - e^{2ig} (i(b-c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i(b-c)z^r\right) + e^{2ig} (-i(b+c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(b+c)z^r\right) + (i(b+c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i(b+c)z^r\right) \right) \right)$$

01.06.21.0663.01

$$\int \sin(b z^2) \sin(c z^2 + g) dz = \frac{1}{2} \sqrt{\frac{\pi}{2}} \left( \frac{\cos(g) C\left(\sqrt{b-c} \sqrt{\frac{2}{\pi}} z\right) + S\left(\sqrt{b-c} \sqrt{\frac{2}{\pi}} z\right) \sin(g)}{\sqrt{b-c}} + \frac{S\left(\sqrt{b+c} \sqrt{\frac{2}{\pi}} z\right) \sin(g) - \cos(g) C\left(\sqrt{b+c} \sqrt{\frac{2}{\pi}} z\right)}{\sqrt{b+c}} \right)$$

01.06.21.0664.01

$$\int \sin(b \sqrt{z}) \sin(\sqrt{z} c + g) dz = \frac{1}{2} \left( \frac{2 \cos((b-c)\sqrt{z}) (\cos(g) + (c-b)\sqrt{z} \sin(g))}{(b-c)^2} + \frac{2((b-c)\sqrt{z} \cos(g) + \sin(g)) \sin((b-c)\sqrt{z})}{(b-c)^2} - \frac{2 \cos((b+c)\sqrt{z}) (\cos(g) + (b+c)\sqrt{z} \sin(g))}{(b+c)^2} - \frac{2((b+c)\sqrt{z} \cos(g) - \sin(g)) \sin((b+c)\sqrt{z})}{(b+c)^2} \right)$$

### Involving $\sin(b z^r + e) \sin(c z^r + g)$

01.06.21.0665.01

$$\int \sin(b z^r + e) \sin(c z^r + g) dz = \frac{1}{4r} e^{-i(e+g)} z \left( -e^{2ie} \Gamma\left(\frac{1}{r}, -i(b-c)z^r\right) (-i(b-c)z^r)^{-1/r} - e^{2ig} (i(b-c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i(b-c)z^r\right) + e^{2i(e+g)} (-i(b+c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(b+c)z^r\right) + (i(b+c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i(b+c)z^r\right) \right)$$

01.06.21.0666.01

$$\int \sin(bz^2 + e) \sin(cz^2 + g) dz = \frac{1}{2} \sqrt{\frac{\pi}{2}} \left( \frac{\cos(e-g) C\left(\sqrt{b-c} \sqrt{\frac{2}{\pi}} z\right) - S\left(\sqrt{b-c} \sqrt{\frac{2}{\pi}} z\right) \sin(e-g)}{\sqrt{b-c}} + \frac{S\left(\sqrt{b+c} \sqrt{\frac{2}{\pi}} z\right) \sin(e+g) - \cos(e+g) C\left(\sqrt{b+c} \sqrt{\frac{2}{\pi}} z\right)}{\sqrt{b+c}} \right)$$

01.06.21.0667.01

$$\int \sin(\sqrt{z} b + e) \sin(\sqrt{z} c + g) dz = \frac{1}{2} \left( \frac{2 \cos((b-c)\sqrt{z}) (\cos(e-g) + (b-c)\sqrt{z} \sin(e-g))}{(b-c)^2} + \frac{2((b-c)\sqrt{z} \cos(e-g) - \sin(e-g)) \sin((b-c)\sqrt{z})}{(b-c)^2} - \frac{2 \cos((b+c)\sqrt{z}) (\cos(e+g) + (b+c)\sqrt{z} \sin(e+g))}{(b+c)^2} - \frac{2((b+c)\sqrt{z} \cos(e+g) - \sin(e+g)) \sin((b+c)\sqrt{z})}{(b+c)^2} \right)$$

### Involving $\sin(dz) \sin(cz^r + fz)$

01.06.21.0668.01

$$\int \sin(dz) \sin(cz^2 + fz) dz = \frac{1}{2\sqrt{-c}\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{c} \cos\left(\frac{(d-f)^2}{4c}\right) C\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) - \sqrt{-c} \cos\left(\frac{(d+f)^2}{4c}\right) C\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - \sqrt{c} S\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) \sin\left(\frac{(d-f)^2}{4c}\right) - \sqrt{-c} S\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{(d+f)^2}{4c}\right) \right) \right)$$

01.06.21.0669.01

$$\int \sin(dz) \sin(\sqrt{z} c + fz) dz = \frac{1}{2} \left( \frac{c \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{c^2}{4(d-f)}\right) C\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) + S\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) \sin\left(\frac{c^2}{4(d-f)}\right) \right)}{(d-f)^{3/2}} + \frac{c \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{c^2}{4(d+f)}\right) C\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) + S\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \sin\left(\frac{c^2}{4(d+f)}\right) \right)}{(d+f)^{3/2}} - \frac{\sin(c\sqrt{z} - (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}c + (d+f)z)}{d+f} \right)$$

### Involving $\sin(dz + e) \sin(cz^r + fz)$

01.06.21.0670.01

$$\int \sin(dz + e) \sin(cz^2 + fz) dz =$$

$$\frac{1}{2\sqrt{-c}\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{c} \cos\left(\frac{(d-f)^2}{4c} + e\right) C\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) - \sqrt{-c} \cos\left(e - \frac{(d+f)^2}{4c}\right) C\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - \sqrt{c} S\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) \sin\left(\frac{(d-f)^2}{4c} + e\right) + \sqrt{-c} S\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(e - \frac{(d+f)^2}{4c}\right) \right) \right)$$

01.06.21.0671.01

$$\int \sin(dz + e) \sin(\sqrt{z}c + fz) dz = \frac{1}{2} \left( \frac{c\sqrt{\frac{\pi}{2}} \left( \cos\left(e - \frac{c^2}{4(d-f)}\right) C\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) - S\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) \sin\left(e - \frac{c^2}{4(d-f)}\right) \right)}{(d-f)^{3/2}} + \frac{c\sqrt{\frac{\pi}{2}} \left( \cos\left(e - \frac{c^2}{4(d+f)}\right) C\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) - S\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \sin\left(e - \frac{c^2}{4(d+f)}\right) \right)}{(d+f)^{3/2}} + \frac{\sin(-\sqrt{z}c + e + (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}c + e + (d+f)z)}{d+f} \right)$$

### Involving $\sin(bz^r) \sin(cz^r + fz)$

01.06.21.0672.01

$$\int \sin(bz^2) \sin(cz^2 + fz) dz =$$

$$\frac{1}{2\sqrt{b-c}\sqrt{b+c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(\frac{f^2}{4(b-c)}\right) C\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(\frac{f^2}{4(b+c)}\right) C\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) + \sqrt{b+c} S\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(\frac{f^2}{4(b-c)}\right) - \sqrt{b-c} S\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(\frac{f^2}{4(b+c)}\right) \right) \right)$$

01.06.21.0673.01

$$\int \sin(b\sqrt{z}) \sin(\sqrt{z}c + fz) dz = \frac{1}{2} \left( -\frac{(b-c)\sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b-c)^2}{4f}\right) C\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) - S\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) \sin\left(\frac{(b-c)^2}{4f}\right) \right)}{(-f)^{3/2}} + \frac{(b+c)\sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b+c)^2}{4f}\right) C\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) + S\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) \sin\left(\frac{(b+c)^2}{4f}\right) \right)}{f^{3/2}} - \frac{\sin(\sqrt{z}(b+c) + fz)}{f} - \frac{\sin((b-c)\sqrt{z} - fz)}{f} \right)$$

**Involving  $\sin(bz' + e) \sin(cz' + fz)$**

01.06.21.0674.01

$$\int \sin(bz^2 + e) \sin(cz^2 + fz) dz = \frac{1}{2\sqrt{b-c}\sqrt{b+c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(e - \frac{f^2}{4(b-c)}\right) C\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(e - \frac{f^2}{4(b+c)}\right) C\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) - \sqrt{b+c} S\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(e - \frac{f^2}{4(b-c)}\right) + \sqrt{b-c} S\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(e - \frac{f^2}{4(b+c)}\right) \right) \right)$$

01.06.21.0675.01

$$\int \sin(\sqrt{z} b + e) \sin(\sqrt{z} c + fz) dz = \frac{1}{2} \left( \frac{(b-c)\sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b-c)^2}{4f} + e\right) C\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) - S\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) \sin\left(\frac{(b-c)^2}{4f} + e\right) \right)}{(-f)^{3/2}} + \frac{(b+c)\sqrt{\frac{\pi}{2}} \left( \cos\left(e - \frac{(b+c)^2}{4f}\right) C\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) - S\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) \sin\left(e - \frac{(b+c)^2}{4f}\right) \right)}{f^{3/2}} - \left( \frac{\sin(\sqrt{z}(b+c) + e + fz)}{f} - \frac{\sin(\sqrt{z}(b-c) + e - fz)}{f} \right) \right)$$

**Involving  $\sin(bz' + dz) \sin(cz' + fz)$**

01.06.21.0676.01

$$\int \sin(bz^2 + dz) \sin(cz^2 + fz) dz = \frac{1}{2\sqrt{b-c}\sqrt{b+c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(\frac{(d-f)^2}{4(b-c)}\right) C\left(\frac{d-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(\frac{(d+f)^2}{4(b+c)}\right) C\left(\frac{d+f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) + \sqrt{b+c} S\left(\frac{d-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(\frac{(d-f)^2}{4(b-c)}\right) - \sqrt{b-c} S\left(\frac{d+f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(\frac{(d+f)^2}{4(b+c)}\right) \right) \right)$$

01.06.21.0677.01

$$\int \sin(\sqrt{z} b + d z) \sin(\sqrt{z} c + f z) dz = \frac{1}{2} \left( - \frac{(b-c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b-c)^2}{4(d-f)}\right) C\left(\frac{b-c+2(d-f)\sqrt{z}}{\sqrt{d-f}\sqrt{2\pi}}\right) + S\left(\frac{b-c+2(d-f)\sqrt{z}}{\sqrt{d-f}\sqrt{2\pi}}\right) \right) \sin\left(\frac{(b-c)^2}{4(d-f)}\right)}{(d-f)^{3/2}} + \frac{(b+c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b+c)^2}{4(d+f)}\right) C\left(\frac{b+c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) + S\left(\frac{b+c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \right) \sin\left(\frac{(b+c)^2}{4(d+f)}\right)}{(d+f)^{3/2}} + \left. \frac{\sin(\sqrt{z}(b-c) + (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}(b+c) + (d+f)z)}{d+f} \right)$$

**Involving  $\sin(d z) \sin(c z^f + f z + g)$**

01.06.21.0678.01

$$\int \sin(d z) \sin(c z^2 + f z + g) dz = \frac{1}{2\sqrt{-c}\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{c} \cos\left(\frac{(d-f)^2}{4c} - g\right) C\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) - \sqrt{-c} \cos\left(\frac{(d+f)^2}{4c} - g\right) C\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - \sqrt{c} S\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) \sin\left(\frac{(d-f)^2}{4c} - g\right) - \sqrt{-c} S\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(\frac{(d+f)^2}{4c} - g\right) \right) \right)$$

01.06.21.0679.01

$$\int \sin(d z) \sin(\sqrt{z} c + f z + g) dz = \frac{1}{2} \left( \frac{c \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{c^2}{4(d+f)} - g\right) C\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) + S\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \right) \sin\left(\frac{c^2}{4(d+f)} - g\right)}{(d+f)^{3/2}} + \frac{c \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{c^2}{4(d-f)} + g\right) C\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) + S\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) \right) \sin\left(\frac{c^2}{4(d-f)} + g\right)}{(d-f)^{3/2}} - \left. \frac{\sin(\sqrt{z}c + g - (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}c + g + (d+f)z)}{d+f} \right)$$

**Involving  $\sin(d z + e) \sin(c z^f + f z + g)$**

01.06.21.0680.01

$$\int \sin(dz + e) \sin(cz^2 + fz + g) dz =$$

$$\frac{1}{2\sqrt{-c}\sqrt{c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{c} \cos\left(\frac{(d-f)^2}{4c} + e - g\right) C\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) - \sqrt{-c} \cos\left(-\frac{(d+f)^2}{4c} + e + g\right) C\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) - \sqrt{c} S\left(\frac{d-f-2cz}{\sqrt{-c}\sqrt{2\pi}}\right) \sin\left(\frac{(d-f)^2}{4c} + e - g\right) + \sqrt{-c} S\left(\frac{d+f+2cz}{\sqrt{c}\sqrt{2\pi}}\right) \sin\left(-\frac{(d+f)^2}{4c} + e + g\right) \right) \right)$$

01.06.21.0681.01

$$\int \sin(dz + e) \sin(\sqrt{z}c + fz + g) dz =$$

$$\frac{1}{2} \left( \frac{1}{(d-f)^{3/2}} \left( c \sqrt{\frac{\pi}{2}} \left( \cos\left(-\frac{c^2}{4(d-f)} + e - g\right) C\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) - S\left(\frac{2(d-f)\sqrt{z}-c}{\sqrt{d-f}\sqrt{2\pi}}\right) \sin\left(-\frac{c^2}{4(d-f)} + e - g\right) \right) \right) + \frac{1}{(d+f)^{3/2}} \left( c \sqrt{\frac{\pi}{2}} \left( \cos\left(-\frac{c^2}{4(d+f)} + e + g\right) C\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) - S\left(\frac{c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \sin\left(-\frac{c^2}{4(d+f)} + e + g\right) \right) \right) + \frac{\sin(-\sqrt{z}c + e - g + (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}c + e + g + (d+f)z)}{d+f} \right)$$

### Involving $\sin(bz^r) \sin(cz^r + fz + g)$

01.06.21.0682.01

$$\int \sin(bz^2) \sin(cz^2 + fz + g) dz = \frac{1}{2\sqrt{b-c}\sqrt{b+c}}$$

$$\left( \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(\frac{f^2}{4(b-c)} + g\right) C\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(\frac{f^2}{4(b+c)} - g\right) C\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) - \sqrt{b-c} S\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(\frac{f^2}{4(b-c)} - g\right) + \sqrt{b+c} S\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(\frac{f^2}{4(b+c)} + g\right) \right) \right)$$



01.06.21.0683.01

$$\int \sin(b\sqrt{z}) \sin(\sqrt{z} c + fz + g) dz = \frac{1}{2} \left( - \frac{(b-c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b-c)^2}{4f} - g\right) C\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) - S\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) \sin\left(\frac{(b-c)^2}{4f} - g\right) \right)}{(-f)^{3/2}} + \frac{(b+c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b+c)^2}{4f} - g\right) C\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) + S\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) \sin\left(\frac{(b+c)^2}{4f} - g\right) \right)}{f^{3/2}} + \frac{\sin(-\sqrt{z}(b-c) + g + fz)}{f} - \frac{\sin(\sqrt{z}(b+c) + g + fz)}{f} \right)$$

**Involving  $\sin(bz^r + e) \sin(cz^r + fz + g)$**

01.06.21.0684.01

$$\int \sin(bz^2 + e) \sin(cz^2 + fz + g) dz = \frac{1}{2\sqrt{b-c}\sqrt{b+c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(-\frac{f^2}{4(b-c)} + e - g\right) C\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(-\frac{f^2}{4(b+c)} + e + g\right) C\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) - \sqrt{b+c} S\left(\frac{-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(-\frac{f^2}{4(b-c)} + e - g\right) + \sqrt{b-c} S\left(\frac{f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(-\frac{f^2}{4(b+c)} + e + g\right) \right)$$

01.06.21.0685.01

$$\int \sin(\sqrt{z} b + e) \sin(\sqrt{z} c + fz + g) dz = \frac{1}{2} \left( - \frac{1}{(-f)^{3/2}} \left( (b-c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b-c)^2}{4f} + e - g\right) C\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) - S\left(\frac{b-c-2f\sqrt{z}}{\sqrt{-f}\sqrt{2\pi}}\right) \sin\left(\frac{(b-c)^2}{4f} + e - g\right) \right) \right) + \frac{1}{f^{3/2}} \left( (b+c) \sqrt{\frac{\pi}{2}} \left( \cos\left(-\frac{(b+c)^2}{4f} + e + g\right) C\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) - S\left(\frac{b+c+2f\sqrt{z}}{\sqrt{f}\sqrt{2\pi}}\right) \sin\left(-\frac{(b+c)^2}{4f} + e + g\right) \right) \right) - \frac{\sin(\sqrt{z}(b+c) + e + g + fz)}{f} - \frac{\sin(\sqrt{z}(b-c) + e - g - fz)}{f} \right)$$

**Involving  $\sin(bz^r + dz) \sin(cz^r + fz + g)$**

01.06.21.0686.01

$$\int \sin(bz^2 + dz) \sin(cz^2 + fz + g) dz = \frac{1}{2\sqrt{b-c}\sqrt{b+c}} \left( \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(\frac{(d-f)^2}{4(b-c)} + g\right) C\left(\frac{d-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(\frac{(d+f)^2}{4(b+c)} - g\right) C\left(\frac{d+f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) - \sqrt{b-c} S\left(\frac{d+f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(\frac{(d-f)^2}{4(b-c)} + g\right) + \sqrt{b+c} S\left(\frac{d-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(\frac{(d+f)^2}{4(b+c)} - g\right) \right) \right)$$

01.06.21.0687.01

$$\int \sin(\sqrt{z}bz + dz) \sin(\sqrt{z}cz + fz + g) dz = \frac{1}{2} \left( \frac{1}{(d+f)^{3/2}} \left( (b+c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b+c)^2}{4(d+f)} - g\right) C\left(\frac{b+c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) + S\left(\frac{b+c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \sin\left(\frac{(b+c)^2}{4(d+f)} - g\right) \right) - \frac{1}{(d-f)^{3/2}} \left( (b-c) \sqrt{\frac{\pi}{2}} \left( \cos\left(\frac{(b-c)^2}{4(d-f)} + g\right) C\left(\frac{b-c+2(d-f)\sqrt{z}}{\sqrt{d-f}\sqrt{2\pi}}\right) + S\left(\frac{b-c+2(d-f)\sqrt{z}}{\sqrt{d-f}\sqrt{2\pi}}\right) \sin\left(\frac{(b-c)^2}{4(d-f)} + g\right) \right) \right) - \frac{\sin(-\sqrt{z}(b-c) + g - (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}(b+c) + g + (d+f)z)}{d+f} \right)$$

**Involving  $\sin(bz' + dz + e) \sin(cz' + fz + g)$**

01.06.21.0688.01

$$\int \sin(bz^2 + dz + e) \sin(cz^2 + fz + g) dz = \frac{1}{2\sqrt{b-c}\sqrt{b+c}} \sqrt{\frac{\pi}{2}} \left( \sqrt{b+c} \cos\left(-\frac{(d-f)^2}{4(b-c)} + e - g\right) C\left(\frac{d-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) - \sqrt{b-c} \cos\left(-\frac{(d+f)^2}{4(b+c)} + e + g\right) C\left(\frac{d+f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) - \sqrt{b+c} S\left(\frac{d-f+2bz-2cz}{\sqrt{b-c}\sqrt{2\pi}}\right) \sin\left(-\frac{(d-f)^2}{4(b-c)} + e - g\right) + \sqrt{b-c} S\left(\frac{d+f+2(b+c)z}{\sqrt{b+c}\sqrt{2\pi}}\right) \sin\left(-\frac{(d+f)^2}{4(b+c)} + e + g\right) \right)$$

01.06.21.0689.01

$$\int \sin(\sqrt{z} b + d z + e) \sin(\sqrt{z} c + f z + g) dz = \frac{1}{2} \left( \frac{1}{(d-f)^{3/2}} \sqrt{\frac{\pi}{2}} (b-c)(-1) \right. \\ \left. \left( \cos\left(-\frac{(b-c)^2}{4(d-f)} + e-g\right) C\left(\frac{b-c+2(d-f)\sqrt{z}}{\sqrt{d-f}\sqrt{2\pi}}\right) - S\left(\frac{b-c+2(d-f)\sqrt{z}}{\sqrt{d-f}\sqrt{2\pi}}\right) \sin\left(-\frac{(b-c)^2}{4(d-f)} + e-g\right) \right) + \frac{1}{(d+f)^{3/2}} \right. \\ \left. (b+c) \sqrt{\frac{\pi}{2}} \left( \cos\left(-\frac{(b+c)^2}{4(d+f)} + e+g\right) C\left(\frac{b+c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) - S\left(\frac{b+c+2(d+f)\sqrt{z}}{\sqrt{d+f}\sqrt{2\pi}}\right) \sin\left(-\frac{(b+c)^2}{4(d+f)} + e+g\right) \right) \right. \\ \left. \frac{\sin(\sqrt{z}(b-c) + e-g + (d-f)z)}{d-f} - \frac{\sin(\sqrt{z}(b+c) + e+g + (d+f)z)}{d+f} \right)$$

Involving products of several direct functions

**Involving  $\sin(az + \alpha) \sin(bz + \beta) \sin(cz + \gamma)$**

01.06.21.0690.01

$$\int \sin(az) \sin(bz) \sin(cz) dz = \frac{1}{4} \left( \frac{\cos((a-b-c)z)}{a-b-c} + \frac{\cos((a+b+c)z)}{a+b+c} - \frac{\cos((a+b-c)z)}{a+b-c} - \frac{\cos((a-b+c)z)}{a-b+c} \right)$$

01.06.21.0691.01

$$\int \sin(az + \alpha) \sin(bz + \beta) \sin(cz + \gamma) dz = \\ \frac{1}{4} \left( \frac{\cos((a-b-c)z) \cos(\alpha - \beta - \gamma)}{a-b-c} + \frac{\cos((a+b+c)z) \cos(\alpha + \beta + \gamma)}{a+b+c} + \frac{\sin((a+b-c)z) \sin(\alpha + \beta - \gamma)}{a+b-c} + \right. \\ \left. \frac{\sin((a-b+c)z) \sin(\alpha - \beta + \gamma)}{a-b+c} - \frac{\sin((a-b-c)z) \sin(\alpha - \beta - \gamma)}{a-b-c} - \right. \\ \left. \frac{\cos((a+b-c)z) \cos(\alpha + \beta - \gamma)}{a+b-c} - \frac{\cos((a-b+c)z) \cos(\alpha - \beta + \gamma)}{a-b+c} - \frac{\sin((a+b+c)z) \sin(\alpha + \beta + \gamma)}{a+b+c} \right)$$

01.06.21.0692.01

$$\int \sin(z) \sin(a+z) \sin(b+z) dz = \frac{1}{12} (-3 \cos(a-b-z) - 3 \cos(a-b+z) - 3 \cos(a+b+z) + \cos(a+b+3z))$$

**Involving  $\prod_{k=1}^n \sin(a_k z)$**

01.06.21.0693.01

$$\int \prod_{k=1}^n \sin(a_k z) dz = (-2)^{-n} \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \left( \frac{1}{\sum_{j=1}^n (k_j a_j)} \sin\left(\sum_{j=1}^n k_j \left(a_j z + \frac{\pi}{2}\right)\right) \right)$$

Involving products of powers of the direct function

Involving product of power of the direct function and the direct function

Involving  $\sin(c z) \sin^v(a z)$

01.06.21.0694.01

$$\int \sin(c z) \sin^v(a z) dz = -\frac{1}{2(c^2 - a^2 v^2)} e^{-icz} (1 - e^{2iaz})^{-v} \sin^v(a z) \\ \left( e^{2icz} (c + av) {}_2F_1\left(\frac{c - av}{2a}, -v; \frac{c}{2} - v + 2; e^{2iaz}\right) + (c - av) {}_2F_1\left(-\frac{c + av}{2a}, -v; -\frac{c + a(v - 2)}{2a}; e^{2iaz}\right) \right)$$

01.06.21.0695.01

$$\int \sin(c z) \sin^v(a z) dz = -\frac{1}{c} 2^{-v-1} \left( 2 \binom{v}{\frac{v}{2}} \cos(c z) (1 - v \bmod 2) + \right. \\ \left. c i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \left( \frac{e^{-i(c+2ak-av)z}}{c+2ak-av} + \frac{e^{i(\pi v+(c+2ak-av)z)}}{c+2ak-av} + \frac{e^{i(c-2ak+av)z}}{c-2ak+av} + \frac{e^{i(\pi v-(c-2ak+av)z)}}{c-2ak+av} \right) \binom{v}{k} \right); v \in \mathbb{N}^+$$

01.06.21.0696.01

$$\int \sin(c z) \sin^{\frac{1}{2}}(a z) dz = \frac{1}{(a^2 - 4c^2) \sqrt{1 - e^{2iaz}}} e^{-icz} \sin^{\frac{1}{2}}(a z) \\ \left( (a + 2c) e^{2icz} {}_2F_1\left(\frac{c}{2a} - \frac{1}{4}, -\frac{1}{2}; \frac{c}{2a} + \frac{3}{4}; e^{2iaz}\right) - (a - 2c) {}_2F_1\left(-\frac{a + 2c}{4a}, -\frac{1}{2}; \frac{3}{4} - \frac{c}{2a}; e^{2iaz}\right) \right)$$

01.06.21.0697.01

$$\int \frac{\sin(c z)}{\sin^{\frac{1}{2}}(a z)} dz = \frac{1}{(a^2 - 4c^2) \sin^{\frac{1}{2}}(a z)} \\ \left( e^{-icz} \sqrt{1 - e^{2iaz}} \left( (a + 2c) {}_2F_1\left(\frac{a - 2c}{4a}, \frac{1}{2}; \frac{5}{4} - \frac{c}{2a}; e^{2iaz}\right) - (a - 2c) e^{2icz} {}_2F_1\left(\frac{a + 2c}{4a}, \frac{1}{2}; \frac{c}{2a} + \frac{5}{4}; e^{2iaz}\right) \right) \right)$$

01.06.21.0698.01

$$\int \sin((v + 2) z) \sin^v(z) dz = \frac{\sin^{v+1}(z) \sin(z(v + 1))}{v + 1}$$

01.06.21.0699.01

$$\int \sin(a z) \sin^{\frac{1}{2}}(2 a z) dz = -\frac{\sin^{\frac{1}{2}}(2 a z) \cos(a z)}{2 a} - \frac{\cos(a z)}{6 a \sqrt{\sin^2(a z)}} {}_2F_1\left(\frac{3}{4}, \frac{3}{4}; \frac{7}{4}; \cos^2(a z)\right) \sin^{\frac{1}{2}}(2 a z)$$

01.06.21.0700.01

$$\int \frac{\sin(a z)}{\sin^{\frac{1}{2}}(2 a z)} dz = -\frac{\csc(a z)}{a} {}_2F_1\left(\frac{1}{4}, \frac{1}{4}; \frac{5}{4}; \cos^2(a z)\right) \sqrt[4]{\sin^2(a z)} \sin^{\frac{1}{2}}(2 a z)$$

01.06.21.0701.01

$$\int \sin(2 a z) \sin^v(a z) dz = \frac{2 \sin^{v+2}(a z)}{a(v + 2)}$$

### Involving $\sin(cz + d) \sin^v(az)$

01.06.21.0702.01

$$\int \sin(d + cz) \sin^v(az) dz = \frac{1}{(av - c)(c + av)} \left( 2^{-v-1} e^{-icz} (1 - e^{2iaz})^{-v} (-i e^{-iaz} (-1 + e^{2iaz}))^v \left( e^{2icz} (c + av) {}_2F_1\left(\frac{c - av}{2a}, -v; \frac{1}{2}\left(\frac{c}{a} - v + 2\right); e^{2iaz}\right) (\cos(d) + i \sin(d)) + (c - av) {}_2F_1\left(-\frac{c + av}{2a}, -v; -\frac{c + a(v - 2)}{2a}; e^{2iaz}\right) (\cos(d) - i \sin(d)) \right) \right)$$

01.06.21.0703.01

$$\int \sin(cz + d) \sin^v(az) dz = -\frac{1}{c} 2^{-v-1} \left( 2 \left(\frac{v}{2}\right) \cos(d + cz) (1 - v \bmod 2) + c i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{id} \left( \frac{e^{-i(2d+(c+2ak-av)z)}}{c+2ak-av} + \frac{e^{i(\pi v+(c+2ak-av)z)}}{c+2ak-av} + \frac{e^{i(c-2ak+av)z}}{c-2ak+av} + \frac{e^{i(-2d+\pi v-cz+2akz-avz)}}{c-2ak+av} \right) \binom{v}{k} \right); v \in \mathbb{N}^+$$

### Involving $\sin(cz) \sin^v(az + b)$

01.06.21.0704.01

$$\int \sin(cz) \sin^v(az + b) dz = -\frac{1}{2(c^2 - a^2 v^2)} e^{-icz} (1 - e^{2i(b+az)})^{-v} \sin^v(b + az) \left( e^{2icz} (c + av) {}_2F_1\left(\frac{c - av}{2a}, -v; \frac{1}{2}\left(\frac{c}{a} - v + 2\right); e^{2i(b+az)}\right) + (c - av) {}_2F_1\left(-\frac{c + av}{2a}, -v; -\frac{c + a(v - 2)}{2a}; e^{2i(b+az)}\right) \right)$$

01.06.21.0705.01

$$\int \sin(cz) \sin^v(az + b) dz = -\frac{1}{c} 2^{-v-1} \left( 2 \left(\frac{v}{2}\right) \cos(cz) (1 - v \bmod 2) + i^{-v} c \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-ib(2k+v)} \left( \frac{e^{-i((c+2ak-av)z-2bv)}}{c+2ak-av} + \frac{e^{i(4bk+\pi v+(c+2ak-av)z)}}{c+2ak-av} + \frac{e^{i(2bv+(c-2ak+av)z)}}{c-2ak+av} + \frac{e^{i(4bk+2azk+\pi v-cz-avz)}}{c-2ak+av} \right) \binom{v}{k} \right); v \in \mathbb{N}^+$$

### Involving $\sin(cz + d) \sin^v(az + b)$

01.06.21.0706.01

$$\int \sin(d + cz) \sin^v(az + b) dz = -\frac{1}{2(c^2 - a^2 v^2)} \left( e^{-i(d+cz)} (1 - e^{2i(b+az)})^{-v} \left( e^{2i(d+cz)} (c + av) {}_2F_1\left(\frac{c - av}{2a}, -v; \frac{1}{2}\left(\frac{c}{a} - v + 2\right); e^{2i(b+az)}\right) + (c - av) {}_2F_1\left(-\frac{c + av}{2a}, -v; -\frac{c + a(v - 2)}{2a}; e^{2i(b+az)}\right) \right) \sin^v(b + az) \right)$$

01.06.21.0707.01

$$\int \sin(d + cz) \sin^v(b + az) dz = -\frac{1}{c} 2^{-v-1} \left( 2 \binom{v}{\frac{v}{2}} \cos(d + cz) (1 - v \bmod 2) + c i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{i(d-b(2k+v))} \left( \frac{e^{i(4bk+\pi v+(c+2ak-av)z)}}{c+2ak-av} + \frac{e^{-i(2d-2bv+(c+2ak-av)z)}}{c+2ak-av} + \frac{e^{i(2bv+(c-2ak+av)z)}}{c-2ak+av} + \frac{e^{i(-2d+4bk+\pi v-cz+2akz-avz)}}{c-2ak+av} \right) \binom{v}{k} \right) /; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r) \sin^v(cz)$

01.06.21.0708.01

$$\int \sin(bz^2) \sin^v(cz) dz = \frac{2^{-v-\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) (1 - v \bmod 2)}{\sqrt{b}} - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b}} \left( \cos\left(\frac{1}{2} \pi (1-v) - \frac{(cv-2cs)^2}{4b}\right) C\left(\frac{-2cs+cv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) + S\left(\frac{-2cs+cv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) \sin\left(\frac{1}{2} \pi (1-v) - \frac{(cv-2cs)^2}{4b}\right) \right) + \frac{1}{\sqrt{-b}} \left( \cos\left(\frac{1}{2} \pi (v+1) - \frac{(2cs-cv)^2}{4b}\right) C\left(\frac{2cs-cv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) + S\left(\frac{2cs-cv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) \sin\left(\frac{1}{2} \pi (v+1) - \frac{(2cs-cv)^2}{4b}\right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0709.01

$$\int \sin(b\sqrt{z}) \sin^v(cz) dz = \frac{2^{1-v} \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) (b\sqrt{z} \cos(b\sqrt{z}) - \sin(b\sqrt{z}))}{b^2} - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(cv-2cs)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{1}{2} \pi (v-1) - \frac{b^2}{4(cv-2cs)}\right) C\left(\frac{2(cv-2cs)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) - b\sqrt{2\pi} S\left(\frac{2(cv-2cs)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) \sin\left(\frac{1}{2} \pi (v-1) - \frac{b^2}{4(cv-2cs)}\right) + 2\sqrt{cv-2cs} \sin\left(-\sqrt{z} b + \frac{1}{2} \pi (v-1) + (cv-2cs)z\right) \right) + \frac{1}{(2cs-cv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(2cs-cv)} + \frac{1}{2} \pi (v+1)\right) C\left(\frac{2(2cs-cv)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) + b\sqrt{2\pi} S\left(\frac{2(2cs-cv)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) \sin\left(\frac{b^2}{4(2cs-cv)} + \frac{1}{2} \pi (v+1)\right) - 2\sqrt{2cs-cv} \sin\left(\sqrt{z} b + \frac{1}{2} \pi (v+1) - (2cs-cv)z\right) \right) \right) /; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + e) \sin^v(cz)$

01.06.21.0710.01

$$\int \sin(bz^2 + e) \sin^v(cz) dz = -\frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \left(\frac{v}{\frac{v}{2}}\right) (1 - v \bmod 2) \left( -\cos(e) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) - C\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) \sin(e) \right) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(cv-2cs)^2}{4b} + e + \frac{1}{2}\pi(1-v)\right) C\left(\frac{-2cs+cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + S\left(\frac{-2cs+cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \right.$$

$$\left. \sin\left(-\frac{(cv-2cs)^2}{4b} + e + \frac{1}{2}\pi(1-v)\right) \right) + \frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(2cs-cv)^2}{4b} + e + \frac{1}{2}\pi(v+1)\right) \right.$$

$$\left. C\left(\frac{2cs-cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + S\left(\frac{2cs-cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(2cs-cv)^2}{4b} + e + \frac{1}{2}\pi(v+1)\right) \right) \Bigg/; v \in \mathbb{N}^+$$

01.06.21.0711.01

$$\int \sin(\sqrt{z} b + e) \sin^v(cz) dz =$$

$$\frac{2^{1-v} \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) (b\sqrt{z} \cos(\sqrt{z} b + e) - \sin(\sqrt{z} b + e))}{b^2} - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(cv-2cs)^{3/2}} \right.$$

$$\left. \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(cv-2cs)} + e - \frac{1}{2}\pi(v-1)\right) C\left(\frac{2(cv-2cs)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) + b\sqrt{2\pi} S\left(\frac{2(cv-2cs)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \right.$$

$$\left. \sin\left(\frac{b^2}{4(cv-2cs)} + e - \frac{1}{2}\pi(v-1)\right) - 2\sqrt{cv-2cs} \sin\left(\sqrt{z} b + e - \frac{1}{2}\pi(v-1) - (cv-2cs)z\right) \right) \Bigg) +$$

$$\frac{1}{(2cs-cv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(2cs-cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) + \right.$$

$$\left. b\sqrt{2\pi} S\left(\frac{2(2cs-cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(\frac{b^2}{4(2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) - \right.$$

$$\left. 2\sqrt{2cs-cv} \sin\left(\sqrt{z} b + e + \frac{1}{2}\pi(v+1) - (2cs-cv)z\right) \right) \Bigg/; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + dz) \sin^v(cz)$

01.06.21.0712.01

$$\int \sin(bz^2 + dz) \sin^v(cz) dz =$$

$$\frac{2^{-v-\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b}\right) - \cos\left(\frac{d^2}{4b}\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right)}{\sqrt{b}} - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{-b}} \left( \cos\left(\frac{1}{2}\pi(1-v) - \frac{(-d-2cs+cv)^2}{4b}\right) C\left(\frac{-d-2cs+cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + S\left(\frac{-d-2cs+cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(\frac{1}{2}\pi(1-v) - \frac{(-d-2cs+cv)^2}{4b}\right) \right) \right.$$

$$\left. + \frac{1}{\sqrt{-b}} \left( \cos\left(\frac{1}{2}\pi(v+1) - \frac{(-d+2cs-cv)^2}{4b}\right) C\left(\frac{-d+2cs-cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + S\left(\frac{-d+2cs-cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(\frac{1}{2}\pi(v+1) - \frac{(-d+2cs-cv)^2}{4b}\right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0713.01

$$\int \sin(\sqrt{z} b + dz) \sin^v(cz) dz = \frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right.$$

$$\left. \left( -2\sqrt{d} \cos(\sqrt{z} b + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d}\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d}\right) \right) \right) - 2^{-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d-2cs+cv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{1}{2}\pi(v-1) - \frac{b^2}{4(-d-2cs+cv)}\right) C\left(\frac{2(-d-2cs+cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d-2cs+cv}}\right) - \right.$$

$$\left. b\sqrt{2\pi} S\left(\frac{2(-d-2cs+cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d-2cs+cv}}\right) \sin\left(\frac{1}{2}\pi(v-1) - \frac{b^2}{4(-d-2cs+cv)}\right) \right) +$$

$$\left. 2\sqrt{-d-2cs+cv} \sin\left(-\sqrt{z} b + \frac{1}{2}\pi(v-1) + (-d-2cs+cv)z\right) \right) +$$

$$\frac{1}{(-d+2cs-cv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(-d+2cs-cv)} + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(-d+2cs-cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d+2cs-cv}}\right) + \right.$$

$$\left. b\sqrt{2\pi} S\left(\frac{2(-d+2cs-cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d+2cs-cv}}\right) \sin\left(\frac{b^2}{4(-d+2cs-cv)} + \frac{1}{2}\pi(v+1)\right) - \right.$$

$$\left. 2\sqrt{-d+2cs-cv} \sin\left(\sqrt{z} b + \frac{1}{2}\pi(v+1) - (-d+2cs-cv)z\right) \right) /; v \in \mathbb{N}^+$$

**Involving  $\sin(bz^r + dz + e) \sin^v(cz)$**



01.06.21.0714.01

$$\int \sin(bz^2 + dz + e) \sin^v(cz) dz =$$

$$-\frac{1}{\sqrt{b}} \left( 2^{-v-\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b} - e\right) - \cos\left(\frac{d^2}{4b} - e\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right) - \right.$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(-d-2cs+cv)^2}{4b} + e + \frac{1}{2}\pi(1-v)\right) C\left(\frac{-d-2cs+cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + \right.$$

$$S\left(\frac{-d-2cs+cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(-d-2cs+cv)^2}{4b} + e + \frac{1}{2}\pi(1-v)\right) \right) +$$

$$\frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(-d+2cs-cv)^2}{4b} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2cs-cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + \right.$$

$$S\left(\frac{-d+2cs-cv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(-d+2cs-cv)^2}{4b} + e + \frac{1}{2}\pi(v+1)\right) \left. \right) /; v \in \mathbb{N}^+$$

01.06.21.0715.01

$$\int \sin(\sqrt{z}bz + dz + e) \sin^v(cz) dz =$$

$$\frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( -2\sqrt{d} \cos(\sqrt{z}bz + e + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d} - e\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + \right.$$

$$b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d} - e\right) \left. \right) - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{(-d-2cs+cv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(-d-2cs+cv)} + e - \frac{1}{2}\pi(v-1)\right) C\left(\frac{2(-d-2cs+cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d-2cs+cv}}\right) + \right.$$

$$b\sqrt{2\pi} S\left(\frac{2(-d-2cs+cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d-2cs+cv}}\right) \sin\left(\frac{b^2}{4(-d-2cs+cv)} + e - \frac{1}{2}\pi(v-1)\right) -$$

$$2\sqrt{-d-2cs+cv} \sin\left(\sqrt{z}bz + e - \frac{1}{2}\pi(v-1) - (-d-2cs+cv)z\right) \left. \right) +$$

$$\frac{1}{(-d+2cs-cv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(-d+2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(-d+2cs-cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d+2cs-cv}}\right) + \right.$$

$$b\sqrt{2\pi} S\left(\frac{2(-d+2cs-cv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{-d+2cs-cv}}\right) \sin\left(\frac{b^2}{4(-d+2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) -$$

$$2\sqrt{-d+2cs-cv} \sin\left(\sqrt{z}bz + e + \frac{1}{2}\pi(v+1) - (-d+2cs-cv)z\right) \left. \right) /; v \in \mathbb{N}^+$$

Involving  $\sin(bz^f) \sin^v(fz + g)$

01.06.21.0716.01

$$\int \sin(bz^2) \sin^v(fz + g) dz = \frac{2^{-v-\frac{1}{2}} (1 - v \bmod 2)}{\sqrt{b}} \sqrt{\pi} \left(\frac{v}{2}\right) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b}} \left( \cos\left(\frac{(2fs-fv)^2}{4b} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) C\left(\frac{2fs-fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) - \right.$$

$$S\left(\frac{2fs-fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(\frac{(2fs-fv)^2}{4b} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) \right) +$$

$$\frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(fv-2fs)^2}{4b} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{-2fs+fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + \right.$$

$$\left. S\left(\frac{-2fs+fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(fv-2fs)^2}{4b} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) \Bigg) ; v \in \mathbb{N}^+$$

01.06.21.0717.01

$$\int \sin(b\sqrt{z}) \sin^v(fz + g) dz = \frac{2^{1-v} \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) (b\sqrt{z} \cos(b\sqrt{z}) - \sin(b\sqrt{z}))}{b^2} - 2^{-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(2fs-fv)^{3/2}} \left( b\sqrt{2\pi} \cos\left(-\frac{b^2}{4(2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(2fs-fv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) - \right.$$

$$b\sqrt{2\pi} S\left(\frac{2(2fs-fv)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) \sin\left(-\frac{b^2}{4(2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1)\right) +$$

$$2\sqrt{2fs-fv} \sin\left(-\sqrt{z}b + 2gs-gv - \frac{1}{2}\pi(v+1) + (2fs-fv)z\right) \right) +$$

$$\frac{1}{(fv-2fs)^{3/2}} \left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(fv-2fs)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{2(fv-2fs)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) + \right.$$

$$b\sqrt{2\pi} S\left(\frac{2(fv-2fs)\sqrt{z}-b}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) \sin\left(\frac{b^2}{4(fv-2fs)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) -$$

$$2\sqrt{fv-2fs} \sin\left(\sqrt{z}b + 2gs - \frac{1}{2}\pi(v-1) - gv - (fv-2fs)z\right) \right) \Bigg) ; v \in \mathbb{N}^+$$

**Involving  $\sin(bz^r + e) \sin^v(fz + g)$**

01.06.21.0718.01

$$\int \sin(bz^2 + e) \sin^v(fz + g) dz = - \frac{2^{-v-\frac{1}{2}} \sqrt{\pi} \left(\frac{v}{\frac{v}{2}}\right) (1 - v \bmod 2) \left(-\cos(e) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) - C\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) \sin(e)\right)}{\sqrt{b}} -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left(\frac{1}{\sqrt{-b}} \left(\cos\left(-\frac{(fv-2fs)^2}{4b} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{-2fs+fv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) +\right.\right.$$

$$S\left(\frac{-2fs+fv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) \sin\left(-\frac{(fv-2fs)^2}{4b} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \Bigg) +$$

$$\frac{1}{\sqrt{-b}} \left(\cos\left(-\frac{(2fs-fv)^2}{4b} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2fs-fv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) +\right.$$

$$\left. S\left(\frac{2fs-fv-2bz}{\sqrt{-b} \sqrt{2\pi}}\right) \sin\left(-\frac{(2fs-fv)^2}{4b} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \Bigg) \Bigg) /; v \in \mathbb{N}^+$$

01.06.21.0719.01

$$\int \sin(\sqrt{z} b + e) \sin^v(fz + g) dz = \frac{2^{1-v} \left(\frac{v}{\frac{v}{2}}\right) (v \bmod 2 - 1) (b\sqrt{z} \cos(\sqrt{z} b + e) - \sin(\sqrt{z} b + e))}{b^2} - 2^{-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left(\frac{1}{(fv-2fs)^{3/2}} \left(b\sqrt{2\pi} \cos\left(\frac{b^2}{4(fv-2fs)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{2(fv-2fs)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{fv-2fs}}\right) +\right.\right.$$

$$b\sqrt{2\pi} S\left(\frac{2(fv-2fs)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{fv-2fs}}\right) \sin\left(\frac{b^2}{4(fv-2fs)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) -$$

$$\left. 2\sqrt{fv-2fs} \sin\left(\sqrt{z} b + e + 2gs - \frac{1}{2}\pi(v-1) - gv - (fv-2fs)z\right) \Bigg) +$$

$$\frac{1}{(2fs-fv)^{3/2}} \left(b\sqrt{2\pi} \cos\left(\frac{b^2}{4(2fs-fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(2fs-fv)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{2fs-fv}}\right) +\right.$$

$$b\sqrt{2\pi} S\left(\frac{2(2fs-fv)\sqrt{z}-b}{\sqrt{2\pi} \sqrt{2fs-fv}}\right) \sin\left(\frac{b^2}{4(2fs-fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) -$$

$$\left. 2\sqrt{2fs-fv} \sin\left(\sqrt{z} b + e - 2gs + gv + \frac{1}{2}\pi(v+1) - (2fs-fv)z\right) \Bigg) \Bigg) /; v \in \mathbb{N}^+$$

**Involving  $\sin(bz' + dz) \sin^v(fz + g)$**

01.06.21.0720.01

$$\int \sin(bz^2 + dz) \sin^v(g + fz) dz = - \frac{2^{-v-\frac{1}{2}} \sqrt{\pi} \left(\frac{v}{2}\right) (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b}\right) - \cos\left(\frac{d^2}{4b}\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right)}{\sqrt{b}} -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b}} \left( \cos\left(\frac{(-d+2fs-fv)^2}{4b} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) - \right.$$

$$S\left(\frac{-d+2fs-fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(\frac{(-d+2fs-fv)^2}{4b} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) \Bigg) +$$

$$\frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(-d-2fs+fv)^2}{4b} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{-d-2fs+fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + \right.$$

$$\left. S\left(\frac{-d-2fs+fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(-d-2fs+fv)^2}{4b} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) \Bigg) ; v \in \mathbb{N}^+$$

01.06.21.0721.01

$$\int \sin(\sqrt{z} b + dz) \sin^v(g + fz) dz =$$

$$\frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -2\sqrt{d} \cos(\sqrt{z} b + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d}\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + \right.$$

$$\left. b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d}\right) \right) - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d+2fs-fv)^{3/2}} \right.$$

$$\left( b\sqrt{2\pi} \cos\left(-\frac{b^2}{4(-d+2fs-fv)} + 2gs - gv - \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(-d+2fs-fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) - \right.$$

$$b\sqrt{2\pi} S\left(\frac{2(-d+2fs-fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) \sin\left(-\frac{b^2}{4(-d+2fs-fv)} + 2gs - gv - \frac{1}{2}\pi(v+1)\right) +$$

$$\left. 2\sqrt{-d+2fs-fv} \sin\left(-\sqrt{z} b + 2gs - gv - \frac{1}{2}\pi(v+1) + (-d+2fs-fv)z\right) \right) + \frac{1}{(-d-2fs+fv)^{3/2}}$$

$$\left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(-d-2fs+fv)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{2(-d-2fs+fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) + \right.$$

$$b\sqrt{2\pi} S\left(\frac{2(-d-2fs+fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{b^2}{4(-d-2fs+fv)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) -$$

$$\left. 2\sqrt{-d-2fs+fv} \sin\left(\sqrt{z} b + 2gs - \frac{1}{2}\pi(v-1) - gv - (-d-2fs+fv)z\right) \right) \Bigg) ; v \in \mathbb{N}^+$$

**Involving  $\sin(bz^r + dz + e) \sin^v(fz + g)$**

01.06.21.0722.01

$$\int \sin(bz^2 + dz + e) \sin^v(fz + g) dz =$$

$$-\frac{1}{\sqrt{b}} \left( 2^{-v-\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b} - e\right) - \cos\left(\frac{d^2}{4b} - e\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right) \right) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(-d-2fs+fv)^2}{4b} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{-d-2fs+fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + \right.$$

$$S\left(\frac{-d-2fs+fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(-d-2fs+fv)^2}{4b} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{-b}} \left( \cos\left(-\frac{(-d+2fs-fv)^2}{4b} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) + \right.$$

$$S\left(\frac{-d+2fs-fv-2bz}{\sqrt{-b}\sqrt{2\pi}}\right) \sin\left(-\frac{(-d+2fs-fv)^2}{4b} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \left. \right) \Bigg) /; v \in \mathbb{N}^+$$

01.06.21.0723.01

$$\int \sin(\sqrt{z} b + dz + e) \sin^v(fz + g) dz =$$

$$\frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -2\sqrt{d} \cos(\sqrt{z} b + e + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d} - e\right) S\left(\frac{b + 2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + \right.$$

$$\left. b\sqrt{2\pi} C\left(\frac{b + 2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d} - e\right) \right) - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d - 2fs + fv)^{3/2}} \right.$$

$$\left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(-d - 2fs + fv)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{2(-d - 2fs + fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d - 2fs + fv}}\right) + \right.$$

$$\left. b\sqrt{2\pi} S\left(\frac{2(-d - 2fs + fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d - 2fs + fv}}\right) \sin\left(\frac{b^2}{4(-d - 2fs + fv)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) - \right.$$

$$\left. 2\sqrt{-d - 2fs + fv} \sin\left(\sqrt{z} b + e + 2gs - \frac{1}{2}\pi(v-1) - gv - (-d - 2fs + fv)z\right) \right) + \frac{1}{(-d + 2fs - fv)^{3/2}}$$

$$\left( b\sqrt{2\pi} \cos\left(\frac{b^2}{4(-d + 2fs - fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(-d + 2fs - fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d + 2fs - fv}}\right) + \right.$$

$$\left. b\sqrt{2\pi} S\left(\frac{2(-d + 2fs - fv)\sqrt{z} - b}{\sqrt{2\pi}\sqrt{-d + 2fs - fv}}\right) \sin\left(\frac{b^2}{4(-d + 2fs - fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) - \right.$$

$$\left. 2\sqrt{-d + 2fs - fv} \sin\left(\sqrt{z} b + e - 2gs + gv + \frac{1}{2}\pi(v+1) - (-d + 2fs - fv)z\right) \right) \Bigg/ ; v \in \mathbb{N}^+$$

### Involving $\sin(bz) \sin^v(cz^2)$

01.06.21.0724.01

$$\int \sin(bz) \sin^v(cz^2) dz = -\frac{2^{-v}(1 - v \bmod 2)}{b} \binom{v}{\frac{v}{2}} \cos(bz) - 2^{-v-\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{2ck - cv}} \left( (-1)^{k+v} \binom{v}{k} \left( \left( S\left(\frac{2(2ck - cv)z - b}{\sqrt{2\pi}\sqrt{2ck - cv}}\right) - S\left(\frac{b + 2(2ck - cv)z}{\sqrt{2\pi}\sqrt{2ck - cv}}\right) \right) \cos\left(\frac{b^2}{4(2ck - cv)} + \frac{\pi v}{2}\right) - \right.$$

$$\left. \sin\left(\frac{b^2}{4(2ck - cv)} + \frac{\pi v}{2}\right) \left( C\left(\frac{2(2ck - cv)z - b}{\sqrt{2\pi}\sqrt{2ck - cv}}\right) - C\left(\frac{b + 2(2ck - cv)z}{\sqrt{2\pi}\sqrt{2ck - cv}}\right) \right) \right) \Bigg/ ; v \in \mathbb{N}^+$$

01.06.21.0725.01

$$\int \sin(bz) \sin^v(c\sqrt{z}) dz = -\frac{2^{-v} \cos(bz) (1 - v \bmod 2)}{b} \left(\frac{v}{2}\right) -$$

$$\frac{1}{(-b)^{3/2}} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left[ c \sqrt{2\pi} (2s-v) \left( \cos\left(\frac{1}{4} \left( \frac{c^2 (v-2s)^2}{b} + 2\pi v \right)\right) S\left(\frac{c(v-2s) - 2b\sqrt{z}}{\sqrt{-b} \sqrt{2\pi}}\right) - \right.$$

$$\left. \cos\left(\frac{\pi v}{2} - \frac{c^2 (v-2s)^2}{4b}\right) S\left(\frac{b(2\sqrt{z}b - 2cs + cv)}{(-b)^{3/2} \sqrt{2\pi}}\right) + C\left(\frac{-2\sqrt{z}b - 2cs + cv}{\sqrt{-b} \sqrt{2\pi}}\right) \right.$$

$$\left. \sin\left(\frac{1}{4} \left( \frac{c^2 (v-2s)^2}{b} + 2\pi v \right)\right) + C\left(\frac{b(2\sqrt{z}b - 2cs + cv)}{(-b)^{3/2} \sqrt{2\pi}}\right) \sin\left(\frac{\pi v}{2} - \frac{c^2 (v-2s)^2}{4b}\right) \right] -$$

$$4\sqrt{-b} \cos\left(\frac{\pi v}{2} + c(v-2s)\sqrt{z}\right) \cos(bz) \Bigg]; v \in \mathbb{N}^+$$

### Involving $\sin(dz + e) \sin^v(cz^r)$

01.06.21.0726.01

$$\int \sin(e + dz) \sin^v(cz^2) dz = -\frac{2^{-v} (1 - v \bmod 2)}{d} \left(\frac{v}{2}\right) \cos(e + dz) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{d^2}{4(cv-2cs)} + e + \frac{1}{2}\pi(1-v)\right) C\left(\frac{2(cv-2cs)z-d}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) + \right.$$

$$\left. S\left(\frac{2(cv-2cs)z-d}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) \sin\left(\frac{d^2}{4(cv-2cs)} + e + \frac{1}{2}\pi(1-v)\right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(\frac{d^2}{4(2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(2cs-cv)z-d}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) + \right.$$

$$\left. S\left(\frac{2(2cs-cv)z-d}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) \sin\left(\frac{d^2}{4(2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) \right) \Bigg]; v \in \mathbb{N}^+$$

01.06.21.0727.01

$$\int \sin(e + dz) \sin^v(c\sqrt{z}) dz = -\frac{2^{-v}(1-v \bmod 2)}{d} \left(\frac{v}{\frac{1}{2}}\right) \cos(e + dz) -$$

$$\frac{2^{-v-1}}{(-d)^{3/2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( c\sqrt{2\pi} (2s-v) \left( \cos\left( e - \frac{c^2(v-2s)^2 + 2d\pi v}{4d} \right) S\left( \frac{c(v-2s) - 2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}} \right) - \right.$$

$$\left. \cos\left( -\frac{c^2(v-2s)^2}{4d} + e + \frac{\pi v}{2} \right) S\left( \frac{d(2\sqrt{z}d - 2cs + cv)}{(-d)^{3/2}\sqrt{2\pi}} \right) + C\left( \frac{d(2\sqrt{z}d - 2cs + cv)}{(-d)^{3/2}\sqrt{2\pi}} \right) \right)$$

$$\left. \sin\left( -\frac{c^2(v-2s)^2}{4d} + e + \frac{\pi v}{2} \right) - C\left( \frac{-2\sqrt{z}d - 2cs + cv}{\sqrt{-d}\sqrt{2\pi}} \right) \sin\left( -\frac{c^2(v-2s)^2}{4d} + e - \frac{\pi v}{2} \right) \right) -$$

$$4\sqrt{-d} \cos\left( \frac{\pi v}{2} + c(v-2s)\sqrt{z} \right) \cos(e + dz) \Bigg/; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r) \sin^v(cz^r)$

01.06.21.0728.01

$$\int \sin(bz^r) \sin^v(cz^r) dz = \frac{i2^{-v-1}(1-v \bmod 2)}{r} z \left(\frac{v}{\frac{1}{2}}\right) \left( (-ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, -ibz^r\right) - (ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, ibz^r\right) \right) -$$

$$\frac{(2i)^{-v-1} z^{\lfloor \frac{v-1}{2} \rfloor}}{r} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \Gamma\left(\frac{1}{r}, (-ib - 2ics + icv)z^r\right) \left( (-ib - 2ics + icv)z^r \right)^{-1/r} + \right.$$

$$\left. (-1)^{v+1} \left( (ib - 2ics + icv)z^r \right)^{-1/r} \Gamma\left(\frac{1}{r}, (ib - 2ics + icv)z^r\right) + \left( (-ib + 2ics - icv)z^r \right)^{-1/r} \right.$$

$$\left. \Gamma\left(\frac{1}{r}, (-ib + 2ics - icv)z^r\right) - \left( (ib + 2ics - icv)z^r \right)^{-1/r} \Gamma\left(\frac{1}{r}, (ib + 2ics - icv)z^r\right) \right) \Bigg/; v \in \mathbb{N}^+$$

01.06.21.0729.01

$$\int \sin(bz^2) \sin^v(cz^2) dz = \frac{2^{-v-\frac{1}{2}}\sqrt{\pi}(1-v \bmod 2)}{\sqrt{b}} \left(\frac{v}{\frac{1}{2}}\right) S\left(\sqrt{b}\sqrt{\frac{2}{\pi}}z\right) -$$

$$2^{-v-\frac{1}{2}}\sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{1}{2}\pi(1-v)\right) C\left(\sqrt{\frac{2}{\pi}}\sqrt{-b-2cs+cv}z\right) + \right.$$

$$\left. S\left(\sqrt{\frac{2}{\pi}}\sqrt{-b-2cs+cv}z\right) \sin\left(\frac{1}{2}\pi(1-v)\right) \right) + \frac{1}{\sqrt{-b+2cs-cv}}$$

$$\left( \cos\left(\frac{1}{2}\pi(v+1)\right) C\left(\sqrt{\frac{2}{\pi}}\sqrt{-b+2cs-cv}z\right) + S\left(\sqrt{\frac{2}{\pi}}\sqrt{-b+2cs-cv}z\right) \sin\left(\frac{1}{2}\pi(v+1)\right) \right) \Bigg/; v \in \mathbb{N}^+$$



01.06.21.0730.01

$$\int \sin(b \sqrt{z}) \sin^v(c \sqrt{z}) dz =$$

$$\frac{2^{1-v}}{b^2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) (\sin(b \sqrt{z}) - b \sqrt{z} \cos(b \sqrt{z})) - 2^{1-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-b - 2cs + cv)^2} \right.$$

$$\left. \left( \cos\left(\frac{1}{2} \pi (v - 1) + (-b - 2cs + cv) \sqrt{z}\right) + (-b - 2cs + cv) \sqrt{z} \sin\left(\frac{1}{2} \pi (v - 1) + (-b - 2cs + cv) \sqrt{z}\right) \right) + \right.$$

$$\left. \frac{1}{(-b + 2cs - cv)^2} \left( \cos\left(\frac{1}{2} \pi (v + 1) - (-b + 2cs - cv) \sqrt{z}\right) - (-b + 2cs - cv) \sqrt{z} \sin\left(\frac{1}{2} \pi (v + 1) - (-b + 2cs - cv) \sqrt{z}\right) \right) \right); v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + e) \sin^v(cz^r)$

01.06.21.0731.01

$$\int \sin(bz^r + e) \sin^v(cz^r) dz = \frac{1}{r} \left( i 2^{-v-1} z^{\frac{v}{2}} \left( e^{ie} (-ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, -ibz^r\right) - e^{-ie} (ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, ibz^r\right) \right) (1 - v \bmod 2) \right) -$$

$$\frac{(2i)^{-v-1}}{r} z^{\frac{v-1}{2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{ie} \Gamma\left(\frac{1}{r}, (-ib - 2ics + icv) z^r\right) ((-ib - 2ics + icv) z^r)^{-1/r} + \right.$$

$$\left. (-1)^{v+1} e^{-ie} ((ib - 2ics + icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib - 2ics + icv) z^r\right) + e^{ie} ((-ib + 2ics - icv) z^r)^{-1/r} \right.$$

$$\left. \Gamma\left(\frac{1}{r}, (-ib + 2ics - icv) z^r\right) - e^{-ie} ((ib + 2ics - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib + 2ics - icv) z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.0732.01

$$\int \sin(bz^2 + e) \sin^v(cz^2) dz = -\frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -\cos(e) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) - C\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) \sin(e) \right) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b - 2cs + cv}} \left( \cos\left(e + \frac{1}{2} \pi (1 - v)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{-b - 2cs + cv} z\right) + \right.$$

$$\left. S\left(\sqrt{\frac{2}{\pi}} \sqrt{-b - 2cs + cv} z\right) \sin\left(e + \frac{1}{2} \pi (1 - v)\right) \right) + \frac{1}{\sqrt{-b + 2cs - cv}} \left( \cos\left(e + \frac{1}{2} \pi (v + 1)\right) \right.$$

$$\left. C\left(\sqrt{\frac{2}{\pi}} \sqrt{-b + 2cs - cv} z\right) + S\left(\sqrt{\frac{2}{\pi}} \sqrt{-b + 2cs - cv} z\right) \sin\left(e + \frac{1}{2} \pi (v + 1)\right) \right); v \in \mathbb{N}^+$$

01.06.21.0733.01

$$\int \sin(\sqrt{z} b + e) \sin^v(c \sqrt{z}) dz = \frac{2^{1-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) (\sin(\sqrt{z} b + e) - b \sqrt{z} \cos(\sqrt{z} b + e))}{b^2} +$$

$$2^{1-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \sin\left(e + \frac{\pi v}{2} + (b + c(2k - v)) \sqrt{z}\right) (b - c(2k - v))^2 + \right.$$

$$(b + c(2k - v)) \left( (b - c(2k - v)) \sqrt{z} \left( (c(2k - v) - b) \cos\left(e + \frac{\pi v}{2} + (b + c(2k - v)) \sqrt{z}\right) + \right. \right.$$

$$\left. \left. (-b - c(2k - v)) \cos\left(e + (b - c(2k - v)) \sqrt{z} - \frac{\pi v}{2}\right) \right) + \right.$$

$$\left. \left. (b + c(2k - v)) \sin\left(e + (b - c(2k - v)) \sqrt{z} - \frac{\pi v}{2}\right) \right) \right) / ((b - c(2k - v))^2 (b + c(2k - v))^2) ; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + dz) \sin^v(cz^r)$

01.06.21.0734.01

$$\int \sin(bz^2 + dz) \sin^v(cz^2) dz = -\frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b} \sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b}\right) - \cos\left(\frac{d^2}{4b}\right) S\left(\frac{d+2bz}{\sqrt{b} \sqrt{2\pi}}\right) \right) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{d^2}{4(-b-2cs+cv)} + \frac{1}{2} \pi(1-v)\right) C\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) + \right. \right.$$

$$\left. \left. S\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) \sin\left(\frac{d^2}{4(-b-2cs+cv)} + \frac{1}{2} \pi(1-v)\right) \right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{d^2}{4(-b+2cs-cv)} + \frac{1}{2} \pi(v+1)\right) C\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) + \right.$$

$$\left. \left. S\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) \sin\left(\frac{d^2}{4(-b+2cs-cv)} + \frac{1}{2} \pi(v+1)\right) \right) \right) ; v \in \mathbb{N}^+$$

01.06.21.0735.01

$$\int \sin(\sqrt{z} b + dz) \sin^v(c \sqrt{z}) dz = \frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right. \\ \left. \left( -2 \sqrt{d} \cos(\sqrt{z} b + dz) - b \sqrt{2\pi} \cos\left(\frac{b^2}{4d}\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d} \sqrt{2\pi}}\right) + b \sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d} \sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d}\right) \right) \right) - 2^{-v-1} \\ \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(\frac{1}{2} \pi(v+1) - \frac{(-b+2cs-cv)^2}{4d}\right) C\left(\frac{-b+2cs-cv-2d\sqrt{z}}{\sqrt{-d} \sqrt{2\pi}}\right) - \right. \right. \\ \left. \left. \sqrt{2\pi} (-b+2cs-cv) S\left(\frac{-b+2cs-cv-2d\sqrt{z}}{\sqrt{-d} \sqrt{2\pi}}\right) \sin\left(\frac{1}{2} \pi(v+1) - \frac{(-b+2cs-cv)^2}{4d}\right) - \right. \right. \\ \left. \left. 2 \sqrt{-d} \sin\left(\frac{1}{2} \pi(v+1) + dz - (-b+2cs-cv) \sqrt{z}\right) \right) + \right. \\ \left. \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(\frac{(-b-2cs+cv)^2}{4d} + \frac{1}{2} \pi(v-1)\right) C\left(\frac{-b-2cs+cv-2d\sqrt{z}}{\sqrt{-d} \sqrt{2\pi}}\right) + \right. \right. \\ \left. \left. \sqrt{2\pi} (-b-2cs+cv) S\left(\frac{-b-2cs+cv-2d\sqrt{z}}{\sqrt{-d} \sqrt{2\pi}}\right) \sin\left(\frac{(-b-2cs+cv)^2}{4d} + \frac{1}{2} \pi(v-1)\right) + \right. \right. \\ \left. \left. 2 \sqrt{-d} \sin\left(\frac{1}{2} \pi(v-1) - dz + (-b-2cs+cv) \sqrt{z}\right) \right) \right) \Bigg) /; v \in \mathbb{N}^+$$

### Involving $\sin(bz' + dz + e) \sin^v(cz')$

01.06.21.0736.01

$$\int \sin(bz^2 + dz + e) \sin^v(cz^2) dz = \\ - \frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b} \sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b} - e\right) - \cos\left(\frac{d^2}{4b} - e\right) S\left(\frac{d+2bz}{\sqrt{b} \sqrt{2\pi}}\right) \right) - \\ 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{d^2}{4(-b-2cs+cv)} + e + \frac{1}{2} \pi(1-v)\right) C\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) + \right. \right. \\ \left. \left. S\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) \sin\left(\frac{d^2}{4(-b-2cs+cv)} + e + \frac{1}{2} \pi(1-v)\right) \right) + \right. \\ \left. \frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{d^2}{4(-b+2cs-cv)} + e + \frac{1}{2} \pi(v+1)\right) C\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) + \right. \right. \\ \left. \left. S\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) \sin\left(\frac{d^2}{4(-b+2cs-cv)} + e + \frac{1}{2} \pi(v+1)\right) \right) \right) \Bigg) /; v \in \mathbb{N}^+$$

01.06.21.0737.01

$$\int \sin(\sqrt{z} b + dz + e) \sin^v(c \sqrt{z}) dz =$$

$$\frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -2\sqrt{d} \cos(\sqrt{z} b + e + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d} - e\right) S\left(\frac{b + 2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + \right.$$

$$\left. b\sqrt{2\pi} C\left(\frac{b + 2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d} - e\right) \right) - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b + 2cs - cv) \cos\left(-\frac{(-b - 2cs + cv)^2}{4d} + e - \frac{1}{2}\pi(v-1)\right) C\left(\frac{-b - 2cs + cv - 2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) - \right.$$

$$\left. \sqrt{2\pi} (-b - 2cs + cv) S\left(\frac{-b - 2cs + cv - 2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(-\frac{(-b - 2cs + cv)^2}{4d} + e - \frac{1}{2}\pi(v-1)\right) - \right.$$

$$\left. 2\sqrt{-d} \sin\left(e - \frac{1}{2}\pi(v-1) + dz - (-b - 2cs + cv)\sqrt{z}\right) \right) +$$

$$\frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b - 2cs + cv) \cos\left(-\frac{(-b + 2cs - cv)^2}{4d} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-b + 2cs - cv - 2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) - \right.$$

$$\left. \sqrt{2\pi} (-b + 2cs - cv) S\left(\frac{-b + 2cs - cv - 2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(-\frac{(-b + 2cs - cv)^2}{4d} + e + \frac{1}{2}\pi(v+1)\right) - \right.$$

$$\left. 2\sqrt{-d} \sin\left(e + \frac{1}{2}\pi(v+1) + dz - (-b + 2cs - cv)\sqrt{z}\right) \right) \Bigg/; v \in \mathbb{N}^+$$

### Involving $\sin(dz) \sin^v(cz^r + g)$

01.06.21.0738.01

$$\int \sin(dz) \sin^v(cz^2 + g) dz = \frac{2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sin\left(\frac{1}{2}(-2dz - \pi)\right)}{d} -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{d^2}{4(cv-2cs)} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{2(cv-2cs)z-d}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) + \right.$$

$$\left. S\left(\frac{2(cv-2cs)z-d}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \sin\left(\frac{d^2}{4(cv-2cs)} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(-\frac{d^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(2cs-cv)z-d}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) - \right.$$

$$\left. S\left(\frac{2(2cs-cv)z-d}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(-\frac{d^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) \right) \Bigg/; v \in \mathbb{N}^+$$

01.06.21.0739.01

$$\int \sin(dz) \sin^v(\sqrt{z}c + g) dz = -\frac{2^{-v} \binom{v}{\frac{v}{2}} \cos(dz) (1 - v \bmod 2)}{d} - 2^{-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (2cs - cv) \cos\left(-\frac{(cv - 2cs)^2}{4d} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{-2\sqrt{z}d - 2cs + cv}{\sqrt{-d}\sqrt{2\pi}}\right) - \sqrt{2\pi} (cv - 2cs) S\left(\frac{-2\sqrt{z}d - 2cs + cv}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(-\frac{(cv - 2cs)^2}{4d} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) - 2\sqrt{-d} \sin\left(2gs - \frac{1}{2}\pi(v-1) - gv + dz - (cv - 2cs)\sqrt{z}\right) \right) + \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (cv - 2cs) \cos\left(\frac{(2cs - cv)^2}{4d} + 2gs - gv - \frac{1}{2}\pi(v+1)\right) C\left(\frac{-2\sqrt{z}d + 2cs - cv}{\sqrt{-d}\sqrt{2\pi}}\right) + \sqrt{2\pi} (2cs - cv) S\left(\frac{-2\sqrt{z}d + 2cs - cv}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(\frac{(2cs - cv)^2}{4d} + 2gs - gv - \frac{1}{2}\pi(v+1)\right) + 2\sqrt{-d} \sin\left(2gs - gv - \frac{1}{2}\pi(v+1) - dz + (2cs - cv)\sqrt{z}\right) \right) \right) /; v \in \mathbb{N}^+$$

### Involving $\sin(dz + e) \sin^v(cz^r + g)$

01.06.21.0740.01

$$\int \sin(e + dz) \sin^v(cz^2 + g) dz = -\frac{2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sin\left(e + \frac{1}{2}(2dz + \pi)\right)}{d} -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv - 2cs}} \left( \cos\left(\frac{d^2}{4(cv - 2cs)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{2(cv - 2cs)z - d}{\sqrt{2\pi}\sqrt{cv - 2cs}}\right) + S\left(\frac{2(cv - 2cs)z - d}{\sqrt{2\pi}\sqrt{cv - 2cs}}\right) \sin\left(\frac{d^2}{4(cv - 2cs)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) + \frac{1}{\sqrt{2cs - cv}} \left( \cos\left(\frac{d^2}{4(2cs - cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(2cs - cv)z - d}{\sqrt{2\pi}\sqrt{2cs - cv}}\right) + S\left(\frac{2(2cs - cv)z - d}{\sqrt{2\pi}\sqrt{2cs - cv}}\right) \sin\left(\frac{d^2}{4(2cs - cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0741.01

$$\int \sin(e + dz) \sin^v(\sqrt{z} c + g) dz = -\frac{2^{-v} \binom{v}{\frac{v}{2}} \cos(e + dz) (1 - v \bmod 2)}{d} - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (2cs - cv) \cos\left(-\frac{(cv - 2cs)^2}{4d} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{-2\sqrt{z} d - 2cs + cv}{\sqrt{-d} \sqrt{2\pi}}\right) - \sqrt{2\pi} (cv - 2cs) S\left(\frac{-2\sqrt{z} d - 2cs + cv}{\sqrt{-d} \sqrt{2\pi}}\right) \sin\left(-\frac{(cv - 2cs)^2}{4d} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) - 2\sqrt{-d} \sin\left(e + 2gs - \frac{1}{2}\pi(v-1) - gv + dz - (cv - 2cs)\sqrt{z}\right) \right) + \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (cv - 2cs) \cos\left(-\frac{(2cs - cv)^2}{4d} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-2\sqrt{z} d + 2cs - cv}{\sqrt{-d} \sqrt{2\pi}}\right) - \sqrt{2\pi} (2cs - cv) S\left(\frac{-2\sqrt{z} d + 2cs - cv}{\sqrt{-d} \sqrt{2\pi}}\right) \sin\left(-\frac{(2cs - cv)^2}{4d} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) - 2\sqrt{-d} \sin\left(e - 2gs + gv + \frac{1}{2}\pi(v+1) + dz - (2cs - cv)\sqrt{z}\right) \right) \right) /; v \in \mathbb{N}^+$$

**Involving  $\sin(bz^r) \sin^v(cz^r + g)$**

01.06.21.0742.01

$$\int \sin(bz^r) \sin^v(cz^r + g) dz = \frac{i 2^{-v-1} (1 - v \bmod 2)}{r} z^{\binom{v}{\frac{v}{2}}} \left( (-ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, -ibz^r\right) - (ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, ibz^r\right) \right) - \frac{(2i)^{-v-1} z^{\lfloor \frac{v-1}{2} \rfloor}}{r} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{2igs - igv} \Gamma\left(\frac{1}{r}, (-ib - 2ics + icv)z^r\right) ((-ib - 2ics + icv)z^r)^{-1/r} + (-1)^{v+1} e^{2igs - igv} ((ib - 2ics + icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib - 2ics + icv)z^r\right) + e^{igs - 2igs} ((-ib + 2ics - icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-ib + 2ics - icv)z^r\right) - e^{igs - 2igs} ((ib + 2ics - icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib + 2ics - icv)z^r\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0743.01

$$\int \sin(bz^2) \sin^v(cz^2 + g) dz = \frac{2^{-v-\frac{1}{2}} \sqrt{\pi} (1-v \bmod 2)}{\sqrt{b}} \left(\frac{v}{2}\right) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) -$$

$$2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{-b-2cs+cv} z\right) + \right.$$

$$\left. S\left(\sqrt{\frac{2}{\pi}} \sqrt{-b-2cs+cv} z\right) \sin\left(\frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(g(2s-v) - \frac{1}{2}\pi(v+1)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{-b+2cs-cv} z\right) - \right.$$

$$\left. S\left(\sqrt{\frac{2}{\pi}} \sqrt{-b+2cs-cv} z\right) \sin\left(g(2s-v) - \frac{1}{2}\pi(v+1)\right) \right) \Bigg/; v \in \mathbb{N}^+$$

01.06.21.0744.01

$$\int \sin(b\sqrt{z}) \sin^v(\sqrt{z}c + g) dz = \frac{2^{1-v}}{b^2} \left(\frac{v}{2}\right) (1-v \bmod 2) (\sin(b\sqrt{z}) - b\sqrt{z} \cos(b\sqrt{z})) +$$

$$2^{1-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{1}{(c(v-2s)-b)^2} \left( \cos\left(\frac{1}{2}\pi(1-v) + g(v-2s) + (c(v-2s)-b)\sqrt{z}\right) + \right.$$

$$\left. (c(v-2s)-b)\sqrt{z} \sin\left(\frac{1}{2}\pi(1-v) + g(v-2s) + (c(v-2s)-b)\sqrt{z}\right) \right) +$$

$$\frac{1}{(-b-c(v-2s))^2} \left( \cos\left(\frac{1}{2}\pi(v+1) - g(v-2s) + (-b-c(v-2s))\sqrt{z}\right) + \right.$$

$$\left. (-b-c(v-2s))\sqrt{z} \sin\left(\frac{1}{2}\pi(v+1) - g(v-2s) + (-b-c(v-2s))\sqrt{z}\right) \right) \Bigg/; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + e) \sin^v(cz^r + g)$

01.06.21.0745.01

$$\int \sin(bz^r + e) \sin^v(cz^r + g) dz =$$

$$\frac{i 2^{-v-1} (1-v \bmod 2)}{r} z \left(\frac{v}{2}\right) \left( e^{ie} (-ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, -ibz^r\right) - e^{-ie} (ibz^r)^{-1/r} \Gamma\left(\frac{1}{r}, ibz^r\right) \right) - \frac{(2i)^{-v-1} z}{r}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{ie+2igs-igv} \Gamma\left(\frac{1}{r}, (-ib-2ics+icv)z^r\right) ((-ib-2ics+icv)z^r)^{-1/r} + (-1)^{v+1} e^{-ie+2igs-igv} \right.$$

$$\left. ((ib-2ics+icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib-2ics+icv)z^r\right) + e^{ie-2igs+igv} ((-ib+2ics-icv)z^r)^{-1/r} \right.$$

$$\left. \Gamma\left(\frac{1}{r}, (-ib+2ics-icv)z^r\right) - e^{-ie-2igs+igv} ((ib+2ics-icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ib+2ics-icv)z^r\right) \right) \Bigg/; v \in \mathbb{N}^+$$

01.06.21.0746.01

$$\int \sin(bz^2 + e) \sin^v(cz^2 + g) dz =$$

$$-\frac{2^{-v-\frac{1}{2}} \sqrt{\pi} (1-v \bmod 2)}{\sqrt{b}} \binom{v}{\frac{v}{2}} \left( -\cos(e) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) - C\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) \sin(e) \right) - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(e + \frac{1}{2} \pi(1-v) + g(2s-v)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{-b-2cs+cv} z\right) + S\left(\sqrt{\frac{2}{\pi}} \sqrt{-b-2cs+cv} z\right) \right. \right.$$

$$\left. \sin\left(e + \frac{1}{2} \pi(1-v) + g(2s-v)\right) \right) + \frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(e - g(2s-v) + \frac{1}{2} \pi(v+1)\right) \right.$$

$$\left. C\left(\sqrt{\frac{2}{\pi}} \sqrt{-b+2cs-cv} z\right) + S\left(\sqrt{\frac{2}{\pi}} \sqrt{-b+2cs-cv} z\right) \sin\left(e - g(2s-v) + \frac{1}{2} \pi(v+1)\right) \right) \Bigg) /; v \in \mathbb{N}^+$$

01.06.21.0747.01

$$\int \sin(\sqrt{z} b + e) \sin^v(\sqrt{z} c + g) dz = \frac{2^{1-v} (1-v \bmod 2) (\sin(\sqrt{z} b + e) - b \sqrt{z} \cos(\sqrt{z} b + e))}{b^2} \binom{v}{\frac{v}{2}} +$$

$$2^{1-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \left( (-1)^k \binom{v}{k} \left( \sin\left(e + \frac{\pi v}{2} - g(v-2k) + (b+c(2k-v)) \sqrt{z}\right) (b-c(2k-v))^2 + \right. \right.$$

$$(b+c(2k-v)) \left( (b-c(2k-v)) \sqrt{z} \left( (c(2k-v)-b) \cos\left(e + \frac{\pi v}{2} - g(v-2k) + (b+c(2k-v)) \sqrt{z}\right) - \right. \right.$$

$$\left. \left. (b+c(2k-v)) \cos\left(e + g(v-2k) + (b-c(2k-v)) \sqrt{z} - \frac{\pi v}{2}\right) \right) + (b+c(2k-v)) \right.$$

$$\left. \left. \sin\left(e + g(v-2k) + (b-c(2k-v)) \sqrt{z} - \frac{\pi v}{2}\right) \right) \right) / ((b-c(2k-v))^2 (b+c(2k-v))^2) /; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + dz) \sin^v(cz^r + g)$

01.06.21.0748.01

$$\int \sin(bz^2 + dz + e) \sin^v(cz^2 + g) dz =$$

$$-\frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b} \sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b} - e\right) - \cos\left(\frac{d^2}{4b} - e\right) S\left(\frac{d+2bz}{\sqrt{b} \sqrt{2\pi}}\right) \right) - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{d^2}{4(-b-2cs+cv)} + e + \frac{1}{2} \pi(1-v) + g(2s-v)\right) C\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) + \right. \right.$$

$$\left. S\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) \sin\left(\frac{d^2}{4(-b-2cs+cv)} + e + \frac{1}{2} \pi(1-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{d^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2} \pi(v+1)\right) C\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) + \right.$$

$$\left. S\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) \sin\left(\frac{d^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2} \pi(v+1)\right) \right) \Bigg) /; v \in \mathbb{N}^+$$



01.06.21.0749.01

$$\int \sin(\sqrt{z} b + d z) \sin^v(\sqrt{z} c + g) dz =$$

$$\frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -2\sqrt{d} \cos(\sqrt{z} b + d z) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d}\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + \right. \right.$$

$$\left. b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d}\right) \right) - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(-\frac{(-b-2cs+cv)^2}{4d} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) C\left(\frac{-b-2cs+cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) - \right. \right.$$

$$\left. \sqrt{2\pi} (-b-2cs+cv) S\left(\frac{-b-2cs+cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(-\frac{(-b-2cs+cv)^2}{4d} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) - \right.$$

$$\left. 2\sqrt{-d} \sin\left(2gs - \frac{1}{2}\pi(v-1) - gv + dz - (-b-2cs+cv)\sqrt{z}\right) \right) +$$

$$\frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(\frac{(-b+2cs-cv)^2}{4d} + 2gs - gv - \frac{1}{2}\pi(v+1)\right) C\left(\frac{-b+2cs-cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) + \right.$$

$$\left. \sqrt{2\pi} (-b+2cs-cv) S\left(\frac{-b+2cs-cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(\frac{(-b+2cs-cv)^2}{4d} + 2gs - gv - \frac{1}{2}\pi(v+1)\right) + \right.$$

$$\left. 2\sqrt{-d} \sin\left(2gs - gv - \frac{1}{2}\pi(v+1) - dz + (-b+2cs-cv)\sqrt{z}\right) \right) \Bigg/ ; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r + dz + e) \sin^v(cz^r + g)$

01.06.21.0750.01

$$\int \sin(bz^2 + dz + e) \sin^v(cz^2 + g) dz =$$

$$-\frac{2^{-v-\frac{1}{2}}\sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b} - e\right) - \cos\left(\frac{d^2}{4b} - e\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right) - 2^{-v-\frac{1}{2}}\sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{d^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi}\sqrt{-b-2cs+cv}}\right) + \right. \right.$$

$$\left. S\left(\frac{2(-b-2cs+cv)z-d}{\sqrt{2\pi}\sqrt{-b-2cs+cv}}\right) \sin\left(\frac{d^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{d^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi}\sqrt{-b+2cs-cv}}\right) + \right.$$

$$\left. S\left(\frac{2(-b+2cs-cv)z-d}{\sqrt{2\pi}\sqrt{-b+2cs-cv}}\right) \sin\left(\frac{d^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \right) \Bigg/ ; v \in \mathbb{N}^+$$

01.06.21.0751.01

$$\int \sin(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + g) dz = \frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right. \\ \left. \left( -2\sqrt{d} \cos(\sqrt{z} b + e + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d} - e\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d} - e\right) \right) \right) - \\ 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(-\frac{(-b-2cs+cv)^2}{4d} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) \right. \right. \\ \left. \left. C\left(\frac{-b-2cs+cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) - \sqrt{2\pi} (-b-2cs+cv) S\left(\frac{-b-2cs+cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) \right. \right. \\ \left. \left. \sin\left(-\frac{(-b-2cs+cv)^2}{4d} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) - \right. \right. \\ \left. \left. 2\sqrt{-d} \sin\left(e + 2gs - \frac{1}{2}\pi(v-1) - gv + dz - (-b-2cs+cv)\sqrt{z}\right) \right) \right) + \frac{1}{(-d)^{3/2}} \\ \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(-\frac{(-b+2cs-cv)^2}{4d} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-b+2cs-cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) - \right. \\ \left. \sqrt{2\pi} (-b+2cs-cv) S\left(\frac{-b+2cs-cv-2d\sqrt{z}}{\sqrt{-d}\sqrt{2\pi}}\right) \sin\left(-\frac{(-b+2cs-cv)^2}{4d} + e - 2gs + gv + \right. \right. \\ \left. \left. \frac{1}{2}\pi(v+1)\right) - 2\sqrt{-d} \sin\left(e - 2gs + gv + \frac{1}{2}\pi(v+1) + dz - (-b+2cs-cv)\sqrt{z}\right) \right) \Bigg) /; v \in \mathbb{N}^+$$

### Involving $\sin(dz) \sin^v(cz^r + fz)$

01.06.21.0752.01

$$\int \sin(dz) \sin^v(cz^2 + fz) dz = \frac{2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sin\left(\frac{1}{2}(-2dz - \pi)\right)}{d} - \\ 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{(-d-2fs+fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(1-v)\right) C\left(\frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \right. \right. \\ \left. \left. S\left(\frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \sin\left(\frac{(-d-2fs+fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(1-v)\right) \right) \right) + \\ \frac{1}{\sqrt{2cs-cv}} \left( \cos\left(\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \right. \\ \left. S\left(\frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + \frac{1}{2}\pi(v+1)\right) \right) \Bigg) /; v \in \mathbb{N}^+$$

01.06.21.0753.01

$$\int \sin(dz) \sin^v(\sqrt{z}c + fz) dz =$$

$$-\frac{2^{-v} \binom{v}{\frac{v}{2}} \cos(dz) (1 - v \bmod 2)}{d} - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d-2fs+fv)^{3/2}} \left( \sqrt{2\pi} (2cs-cv) \right. \right.$$

$$\left. \left. \cos\left(\frac{1}{2}\pi(v-1) - \frac{(cv-2cs)^2}{4(-d-2fs+fv)}\right) C\left(\frac{-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) + \sqrt{2\pi} (cv-2cs) \right. \right.$$

$$\left. \left. S\left(\frac{-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{1}{2}\pi(v-1) - \frac{(cv-2cs)^2}{4(-d-2fs+fv)}\right) + \right. \right.$$

$$\left. \left. 2\sqrt{-d-2fs+fv} \sin\left(\frac{1}{2}\pi(v-1) + (-d-2fs+fv)z + (cv-2cs)\sqrt{z}\right) \right) + \frac{1}{(-d+2fs-fv)^{3/2}}$$

$$\left( \sqrt{2\pi} (cv-2cs) \cos\left(\frac{(2cs-cv)^2}{4(-d+2fs-fv)} + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) - \right.$$

$$\left. \sqrt{2\pi} (2cs-cv) S\left(\frac{2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) \sin\left(\frac{(2cs-cv)^2}{4(-d+2fs-fv)} + \frac{1}{2}\pi(v+1)\right) - \right.$$

$$\left. \left. 2\sqrt{-d+2fs-fv} \sin\left(\frac{1}{2}\pi(v+1) - (-d+2fs-fv)z - (2cs-cv)\sqrt{z}\right) \right) \right); v \in \mathbb{N}^+$$

### Involving $\sin(dz + e) \sin^v(cz^r + fz)$

01.06.21.0754.01

$$\int \sin(dz + e) \sin^v(cz^2 + fz) dz = -\frac{2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sin\left(e + \frac{1}{2}(2dz + \pi)\right)}{d} - 2^{-v-\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{(-d-2fs+fv)^2}{4(cv-2cs)} + e + \frac{1}{2}\pi(1-v)\right) C\left(\frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) + \right. \right.$$

$$\left. \left. S\left(\frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \sin\left(\frac{(-d-2fs+fv)^2}{4(cv-2cs)} + e + \frac{1}{2}\pi(1-v)\right) \right) + \right.$$

$$\left. \frac{1}{\sqrt{2cs-cv}} \left( \cos\left(\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) + \right. \right.$$

$$\left. \left. S\left(\frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) \right) \right); v \in \mathbb{N}^+$$

01.06.21.0755.01

$$\int \sin(dz + e) \sin^v(\sqrt{z}c + fz) dz =$$

$$\frac{2^{-v} \binom{v}{\frac{v}{2}} \cos(e + dz) (1 - v \bmod 2)}{d} - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d-2fs+fv)^{3/2}} \left( \sqrt{2\pi} (2cs-cv) \right. \right.$$

$$\left. \left. \cos\left( \frac{(cv-2cs)^2}{4(-d-2fs+fv)} + e - \frac{1}{2}\pi(v-1) \right) C\left( \frac{-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}} \right) - \sqrt{2\pi} \right. \right.$$

$$\left. \left. (cv-2cs) S\left( \frac{-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}} \right) \sin\left( \frac{(cv-2cs)^2}{4(-d-2fs+fv)} + e - \frac{1}{2}\pi(v-1) \right) - \right.$$

$$\left. \left. 2\sqrt{-d-2fs+fv} \sin\left( e - \frac{1}{2}\pi(v-1) - (-d-2fs+fv)z - (cv-2cs)\sqrt{z} \right) \right) + \frac{1}{(-d+2fs-fv)^{3/2}} \right.$$

$$\left. \left( \sqrt{2\pi} (cv-2cs) \cos\left( \frac{(2cs-cv)^2}{4(-d+2fs-fv)} + e + \frac{1}{2}\pi(v+1) \right) C\left( \frac{2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}} \right) - \right.$$

$$\left. \left. \sqrt{2\pi} (2cs-cv) S\left( \frac{2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}} \right) \sin\left( \frac{(2cs-cv)^2}{4(-d+2fs-fv)} + e + \frac{1}{2}\pi(v+1) \right) - \right.$$

$$\left. \left. 2\sqrt{-d+2fs-fv} \sin\left( e + \frac{1}{2}\pi(v+1) - (-d+2fs-fv)z - (2cs-cv)\sqrt{z} \right) \right) \right) /; v \in \mathbb{N}^+$$

### Involving $\sin(bz^r) \sin^v(cz^r + fz)$

01.06.21.0756.01

$$\int \sin(bz^2) \sin^v(cz^2 + fz) dz = \frac{2^{-v-\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) (1 - v \bmod 2)}{\sqrt{b}} - 2^{-v-\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left( \frac{(fv-2fs)^2}{4(-b-2cs+cv)} + \frac{1}{2}\pi(1-v) \right) C\left( \frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi}\sqrt{-b-2cs+cv}} \right) + \right.$$

$$\left. S\left( \frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi}\sqrt{-b-2cs+cv}} \right) \sin\left( \frac{(fv-2fs)^2}{4(-b-2cs+cv)} + \frac{1}{2}\pi(1-v) \right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left( \frac{(2fs-fv)^2}{4(-b+2cs-cv)} + \frac{1}{2}\pi(v+1) \right) C\left( \frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi}\sqrt{-b+2cs-cv}} \right) + \right.$$

$$\left. S\left( \frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi}\sqrt{-b+2cs-cv}} \right) \sin\left( \frac{(2fs-fv)^2}{4(-b+2cs-cv)} + \frac{1}{2}\pi(v+1) \right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0757.01

$$\int \sin(b \sqrt{z}) \sin^v(\sqrt{z} c + f z) dz =$$

$$\frac{2^{1-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) (\sin(b \sqrt{z}) - b \sqrt{z} \cos(b \sqrt{z}))}{b^2} - 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(f v - 2 f s)^{3/2}} \right.$$

$$\left. \left( \sqrt{2\pi} (b + 2 c s - c v) \cos \left( \frac{1}{2} \pi (v-1) - \frac{(-b - 2 c s + c v)^2}{4 (f v - 2 f s)} \right) C \left( \frac{-b - 2 c s + c v + 2 (f v - 2 f s) \sqrt{z}}{\sqrt{2\pi} \sqrt{f v - 2 f s}} \right) + \right.$$

$$\left. \sqrt{2\pi} (-b - 2 c s + c v) S \left( \frac{-b - 2 c s + c v + 2 (f v - 2 f s) \sqrt{z}}{\sqrt{2\pi} \sqrt{f v - 2 f s}} \right) \sin \left( \frac{1}{2} \pi (v-1) - \frac{(-b - 2 c s + c v)^2}{4 (f v - 2 f s)} \right) \right) +$$

$$\left. 2 \sqrt{f v - 2 f s} \sin \left( \frac{1}{2} \pi (v-1) + (f v - 2 f s) z + (-b - 2 c s + c v) \sqrt{z} \right) \right) + \frac{1}{(2 f s - f v)^{3/2}}$$

$$\left( \sqrt{2\pi} (b - 2 c s + c v) \cos \left( \frac{(-b + 2 c s - c v)^2}{4 (2 f s - f v)} + \frac{1}{2} \pi (v+1) \right) C \left( \frac{-b + 2 c s - c v + 2 (2 f s - f v) \sqrt{z}}{\sqrt{2\pi} \sqrt{2 f s - f v}} \right) - \right.$$

$$\left. \sqrt{2\pi} (-b + 2 c s - c v) S \left( \frac{-b + 2 c s - c v + 2 (2 f s - f v) \sqrt{z}}{\sqrt{2\pi} \sqrt{2 f s - f v}} \right) \sin \left( \frac{(-b + 2 c s - c v)^2}{4 (2 f s - f v)} + \frac{1}{2} \pi (v+1) \right) - \right.$$

$$\left. \left. 2 \sqrt{2 f s - f v} \sin \left( \frac{1}{2} \pi (v+1) - (2 f s - f v) z - (-b + 2 c s - c v) \sqrt{z} \right) \right) \right) /; v \in \mathbb{N}^+$$

**Involving  $\sin(b z^r + e) \sin^v(c z^r + f z)$**

01.06.21.0758.01

$$\int \sin(bz^2 + e) \sin^v(cz^2 + fz) dz =$$

$$\frac{2^{-v-\frac{1}{2}}}{\sqrt{b}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( \cos(e) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) + C\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) \sin(e) \right) - 2^{-v-\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{(fv-2fs)^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v)\right) C\left(\frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) + \right.$$

$$\left. S\left(\frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) \sin\left(\frac{(fv-2fs)^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v)\right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{(2fs-fv)^2}{4(-b+2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) + \right.$$

$$\left. S\left(\frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) \sin\left(\frac{(2fs-fv)^2}{4(-b+2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) \right) \Bigg/; v \in \mathbb{N}^+$$

01.06.21.0759.01

$$\int \sin^m(\sqrt{z} b + e) \sin^v(\sqrt{z} c + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi} (v-2k) \cos\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) C\left(\frac{c(v-2k)+2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}}\right) + \right.$$

$$c\sqrt{2\pi} (v-2k) S\left(\frac{c(v-2k)+2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) +$$

$$\left. \left. 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + f(v-2k)z + c(v-2k)\sqrt{z}\right) \right) \right) +$$

$$\frac{1}{b^2} \left( 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(m-2k)^2} \left( (-1)^{k+m} \binom{m}{k} \left( \cos\left(2ek - em + b(2k-m)\sqrt{z} - \frac{m\pi}{2}\right) + \right.$$

$$\left. \left. b(2k-m)\sqrt{z} \sin\left(2ek - em + b(2k-m)\sqrt{z} - \frac{m\pi}{2}\right) \right) \right) + 2^{-m-v}$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(fv-2fs)^{3/2}} \left( \sqrt{2\pi} (-2bk+bm+2cs-cv) \cos\left(-\frac{(2bk-bm-2cs+cv)^2}{4(fv-2fs)} + \right.$$

$$\left. \left. 2ek - em + \frac{1}{2}\pi(v-m) \right) C\left(\frac{2bk-bm-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi} \sqrt{fv-2fs}}\right) + \right.$$

$$\begin{aligned}
 & \sqrt{2\pi} (2bk - bm - 2cs + cv) S \left( \frac{2bk - bm - 2cs + cv + 2(fv - 2fs)\sqrt{z}}{\sqrt{2\pi} \sqrt{fv - 2fs}} \right) \\
 & \sin \left( -\frac{(2bk - bm - 2cs + cv)^2}{4(fv - 2fs)} + 2ek - em + \frac{1}{2}\pi(v - m) \right) + \\
 & \left. 2\sqrt{fv - 2fs} \sin \left( 2ek - em + \frac{1}{2}\pi(v - m) + (fv - 2fs)z + (2bk - bm - 2cs + cv)\sqrt{z} \right) \right) + \\
 & \frac{1}{(2fs - fv)^{3/2}} \left( \sqrt{2\pi} (-2bk + bm - 2cs + cv) \cos \left( -\frac{(2bk - bm + 2cs - cv)^2}{4(2fs - fv)} + 2ek - \right. \right. \\
 & \left. \left. em - \frac{1}{2}\pi(m + v) \right) C \left( \frac{2bk - bm + 2cs - cv + 2(2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2fs - fv}} \right) + \right. \\
 & \left. \sqrt{2\pi} (2bk - bm + 2cs - cv) S \left( \frac{2bk - bm + 2cs - cv + 2(2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2fs - fv}} \right) \right. \\
 & \left. \sin \left( -\frac{(2bk - bm + 2cs - cv)^2}{4(2fs - fv)} + 2ek - em - \frac{1}{2}\pi(m + v) \right) + 2\sqrt{2fs - fv} \right. \\
 & \left. \sin \left( 2ek - em - \frac{1}{2}\pi(m + v) + (2fs - fv)z + (2bk - bm + 2cs - cv)\sqrt{z} \right) \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $\sin(bz^r + dz) \sin^v(cz^r + fz)$

01.06.21.0760.01

$$\int \sin(bz^2 + dz) \sin^v(cz^2 + fz) dz =$$

$$\frac{2^{-v-\frac{1}{2}}}{\sqrt{b}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( \cos \left( \frac{d^2}{4b} \right) S \left( \frac{d + 2bz}{\sqrt{b} \sqrt{2\pi}} \right) - C \left( \frac{d + 2bz}{\sqrt{b} \sqrt{2\pi}} \right) \sin \left( \frac{d^2}{4b} \right) \right) - 2^{-v-\frac{1}{2}} \sqrt{\pi}$$

$$\begin{aligned}
 & \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b - 2cs + cv}} \left( \cos \left( \frac{(-d - 2fs + fv)^2}{4(-b - 2cs + cv)} + \frac{1}{2}\pi(1 - v) \right) C \left( \frac{-d - 2fs + fv + 2(-b - 2cs + cv)z}{\sqrt{2\pi} \sqrt{-b - 2cs + cv}} \right) + \right. \right. \\
 & \left. \left. S \left( \frac{-d - 2fs + fv + 2(-b - 2cs + cv)z}{\sqrt{2\pi} \sqrt{-b - 2cs + cv}} \right) \sin \left( \frac{(-d - 2fs + fv)^2}{4(-b - 2cs + cv)} + \frac{1}{2}\pi(1 - v) \right) \right) \right) + \\
 & \frac{1}{\sqrt{-b + 2cs - cv}} \left( \cos \left( \frac{(-d + 2fs - fv)^2}{4(-b + 2cs - cv)} + \frac{1}{2}\pi(v + 1) \right) C \left( \frac{-d + 2fs - fv + 2(-b + 2cs - cv)z}{\sqrt{2\pi} \sqrt{-b + 2cs - cv}} \right) + \right. \\
 & \left. \left. S \left( \frac{-d + 2fs - fv + 2(-b + 2cs - cv)z}{\sqrt{2\pi} \sqrt{-b + 2cs - cv}} \right) \sin \left( \frac{(-d + 2fs - fv)^2}{4(-b + 2cs - cv)} + \frac{1}{2}\pi(v + 1) \right) \right) \right) \Bigg) /; v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0761.01

$$\int \sin(\sqrt{z} b + dz) \sin^v(\sqrt{z} c + fz) dz = \frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right. \\ \left. \left( -2\sqrt{d} \cos(\sqrt{z} b + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d}\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d}\right) \right) \right) - \\ 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d-2fs+fv)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(\frac{1}{2}\pi(v-1) - \frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)}\right) \right. \right. \\ \left. \left. C\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) + \sqrt{2\pi} (-b-2cs+cv) \right. \right. \\ \left. \left. S\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{1}{2}\pi(v-1) - \frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)}\right) \right) + \right. \\ \left. 2\sqrt{-d-2fs+fv} \sin\left(\frac{1}{2}\pi(v-1) + (-d-2fs+fv)z + (-b-2cs+cv)\sqrt{z}\right) \right) + \\ \frac{1}{(-d+2fs-fv)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + \frac{1}{2}\pi(v+1)\right) \right. \\ \left. C\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) - \sqrt{2\pi} (-b+2cs-cv) \right. \\ \left. S\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) \sin\left(\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + \frac{1}{2}\pi(v+1)\right) \right) - \\ \left. 2\sqrt{-d+2fs-fv} \sin\left(\frac{1}{2}\pi(v+1) - (-d+2fs-fv)z - (-b+2cs-cv)\sqrt{z}\right) \right) \Bigg) ; v \in \mathbb{N}^+$$

Involving  $\sin(bz' + dz + e) \sin^v(cz' + fz)$



01.06.21.0762.01

$$\int \sin(bz^2 + dz + e) \sin^v(cz^2 + fz) dz =$$

$$\begin{aligned}
 & -\frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b} - e\right) - \cos\left(\frac{d^2}{4b} - e\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right) - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \\
 & \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{(-d-2fs+fv)^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v)\right) C\left(\frac{-d-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi}\sqrt{-b-2cs+cv}}\right) + \right. \right. \\
 & \quad \left. \left. S\left(\frac{-d-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi}\sqrt{-b-2cs+cv}}\right) \sin\left(\frac{(-d-2fs+fv)^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v)\right) \right) \right) + \\
 & \frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{(-d+2fs-fv)^2}{4(-b+2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi}\sqrt{-b+2cs-cv}}\right) + \right. \\
 & \quad \left. \left. S\left(\frac{-d+2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi}\sqrt{-b+2cs-cv}}\right) \sin\left(\frac{(-d+2fs-fv)^2}{4(-b+2cs-cv)} + e + \frac{1}{2}\pi(v+1)\right) \right) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0763.01

$$\int \sin(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + fz) dz = \frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right. \\ \left. \left( -2\sqrt{d} \cos(\sqrt{z} b + e + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d} - e\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d} - e\right) \right) - \right. \\ \left. 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d-2fs+fv)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(\frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)} + e - \frac{1}{2}\pi(v-1)\right) \right. \right. \right. \\ \left. \left. C\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) - \sqrt{2\pi} (-b-2cs+cv) \right. \right. \\ \left. \left. S\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)} + e - \frac{1}{2}\pi(v-1)\right) \right) - \right. \\ \left. \left. 2\sqrt{-d-2fs+fv} \sin\left(e - \frac{1}{2}\pi(v-1) - (-d-2fs+fv)z - (-b-2cs+cv)\sqrt{z}\right) \right) \right) + \\ \frac{1}{(-d+2fs-fv)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + e + \frac{1}{2}\pi(v+1)\right) \right. \\ \left. C\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) - \sqrt{2\pi} (-b+2cs-cv) \right. \\ \left. S\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) \sin\left(\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + e + \frac{1}{2}\pi(v+1)\right) \right) - \\ \left. \left. 2\sqrt{-d+2fs-fv} \sin\left(e + \frac{1}{2}\pi(v+1) - (-d+2fs-fv)z - (-b+2cs-cv)\sqrt{z}\right) \right) \right) /; v \in \mathbb{N}^+$$

Involving  $\sin(dz) \sin^v(cz^r + fz + g)$

01.06.21.0764.01

$$\int \sin(dz) \sin^v(cz^2 + fz + g) dz = \frac{2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sin\left(\frac{1}{2}(-2dz - \pi)\right)}{d} - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left( \frac{(-d-2fs+fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(1-v) + g(2s-v) \right) C\left( \frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}} \right) + S\left( \frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}} \right) \sin\left( \frac{(-d-2fs+fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(1-v) + g(2s-v) \right) \right) + \frac{1}{\sqrt{2cs-cv}} \left( \cos\left( -\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(v+1) \right) C\left( \frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}} \right) - S\left( \frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}} \right) \sin\left( -\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(v+1) \right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0765.01

$$\int \sin(dz) \sin^v(\sqrt{z}c + fz + g) dz = - \frac{2^{-v} \binom{v}{\frac{v}{2}} \cos(dz) (1 - v \bmod 2)}{d} -$$

$$2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d+2fs-fv)^{3/2}} \left[ \sqrt{2\pi} (cv-2cs) \cos\left(-\frac{(2cs-cv)^2}{4(-d+2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1)\right) \right. \right.$$

$$C\left(\frac{2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) + \sqrt{2\pi} (2cs-cv)$$

$$S\left(\frac{2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) \sin\left(-\frac{(2cs-cv)^2}{4(-d+2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1)\right) +$$

$$\left. \left. 2\sqrt{-d+2fs-fv} \sin\left(2gs-gv - \frac{1}{2}\pi(v+1) + (-d+2fs-fv)z + (2cs-cv)\sqrt{z}\right) \right] \right) +$$

$$\frac{1}{(-d-2fs+fv)^{3/2}} \left[ \sqrt{2\pi} (2cs-cv) \cos\left(\frac{(cv-2cs)^2}{4(-d-2fs+fv)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) \right.$$

$$C\left(\frac{-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) - \sqrt{2\pi} (cv-2cs)$$

$$S\left(\frac{-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{(cv-2cs)^2}{4(-d-2fs+fv)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) -$$

$$\left. \left. 2\sqrt{-d-2fs+fv} \sin\left(2gs - \frac{1}{2}\pi(v-1) - gv - (-d-2fs+fv)z - (cv-2cs)\sqrt{z}\right) \right] \right) /; v \in \mathbb{N}^+$$

Involving  $\sin(dz + e) \sin^v(cz^r + fz + g)$

01.06.21.0766.01

$$\int \sin(dz + e) \sin^v(cz^2 + fz + g) dz = -\frac{2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sin\left(e + \frac{1}{2}(2dz + \pi)\right)}{d} - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left[ \cos\left(\frac{(-d-2fs+fv)^2}{4(cv-2cs)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) + S\left(\frac{-d-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \sin\left(\frac{(-d-2fs+fv)^2}{4(cv-2cs)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right] + \frac{1}{\sqrt{2cs-cv}} \left[ \cos\left(\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) + S\left(\frac{-d+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(\frac{(-d+2fs-fv)^2}{4(2cs-cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \right] \right) /; v \in \mathbb{N}^+$$

01.06.21.0767.01

$$\int \sin^m(dz + e) \sin^v(\sqrt{z}c + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + e(m-2k) + d(m-2k)z\right)}{m-2k} + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left[ -c\sqrt{2\pi}(v-2k) \cos\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) + c\sqrt{2\pi}(v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) \sin\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) + 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + g(v-2k) + f(v-2k)z + c(v-2k)\sqrt{z}\right) \right] \right) + 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left[ \sqrt{2\pi}(2cs-cv) \cos\left(-\frac{(cv-2cs)^2}{4(2dk-dm-2fs+fv)} + 2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m)\right) C\left(\frac{-2cs+cv+2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right) + \sqrt{2\pi}(cv-2cs) S\left(\frac{-2cs+cv+2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right) \sin\left(-\frac{(cv-2cs)^2}{4(2dk-dm-2fs+fv)} + 2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m)\right) + 2\sqrt{2dk-dm-2fs+fv} \sin\left(2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m)\right) \right] \right)$$

$$\left. \frac{1}{2} \pi (v - m) + (2dk - dm - 2fs + fv)z + (cv - 2cs)\sqrt{z} \right) \Big/ (2dk - dm - 2fs + fv)^{3/2} +$$

$$\left( \sqrt{2\pi} (cv - 2cs) \cos \left( -\frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + 2ek - em + 2gs - gv - \frac{1}{2} \pi (m + v) \right) \right.$$

$$\left. C \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) + \sqrt{2\pi} (2cs - cv) \right.$$

$$\left. S \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) \sin \left( -\frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + 2ek - em + 2g \right.$$

$$\left. s - gv - \frac{1}{2} \pi (m + v) \right) + 2\sqrt{2dk - dm + 2fs - fv} \sin \left( 2ek - em + 2gs - gv - \frac{1}{2} \pi (m + v) + \right.$$

$$\left. (2dk - dm + 2fs - fv)z + (2cs - cv)\sqrt{z} \right) \Big/ (2dk - dm + 2fs - fv)^{3/2} \Big/ ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $\sin(bz^r) \sin^v(cz^r + fz + g)$

01.06.21.0768.01

$$\int \sin(bz^2) \sin^v(cz^2 + fz + g) dz = \frac{2^{-v-\frac{1}{2}} \sqrt{\pi} \left( \frac{v}{\frac{v}{2}} \right) S \left( \sqrt{b} \sqrt{\frac{2}{\pi}} z \right) (1 - v \bmod 2)}{\sqrt{b}} - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos \left( \frac{(fv-2fs)^2}{4(-b-2cs+cv)} + \frac{1}{2} \pi (1-v) + g(2s-v) \right) C \left( \frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}} \right) + \right.$$

$$\left. S \left( \frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}} \right) \sin \left( \frac{(fv-2fs)^2}{4(-b-2cs+cv)} + \frac{1}{2} \pi (1-v) + g(2s-v) \right) \right) +$$

$$\frac{1}{\sqrt{-b+2cs-cv}} \left( \cos \left( -\frac{(2fs-fv)^2}{4(-b+2cs-cv)} + g(2s-v) - \frac{1}{2} \pi (v+1) \right) C \left( \frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}} \right) - \right.$$

$$\left. S \left( \frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}} \right) \sin \left( -\frac{(2fs-fv)^2}{4(-b+2cs-cv)} + g(2s-v) - \frac{1}{2} \pi (v+1) \right) \right) \Big/ ; v \in \mathbb{N}^+$$

01.06.21.0769.01

$$\int \sin(\sqrt{z} b) \sin^v(\sqrt{z} c + f z + g) dz = \frac{2^{1-v} \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) (b \sqrt{z} \cos(b \sqrt{z}) - \sin(b \sqrt{z}))}{b^2} -$$

$$2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(2fs-fv)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left( -\frac{(-b+2cs-cv)^2}{4(2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1) \right) \right. \right.$$

$$C\left( \frac{-b+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}} \right) + \sqrt{2\pi} (-b+2cs-cv)$$

$$S\left( \frac{-b+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}} \right) \sin\left( -\frac{(-b+2cs-cv)^2}{4(2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1) \right) +$$

$$\left. \left. 2\sqrt{2fs-fv} \sin\left( 2gs-gv - \frac{1}{2}\pi(v+1) + (2fs-fv)z + (-b+2cs-cv)\sqrt{z} \right) \right) \right) +$$

$$\frac{1}{(fv-2fs)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left( \frac{(-b-2cs+cv)^2}{4(fv-2fs)} + 2gs - \frac{1}{2}\pi(v-1) - gv \right) \right.$$

$$C\left( \frac{-b-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}} \right) - \sqrt{2\pi} (-b-2cs+cv)$$

$$S\left( \frac{-b-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}} \right) \sin\left( \frac{(-b-2cs+cv)^2}{4(fv-2fs)} + 2gs - \frac{1}{2}\pi(v-1) - gv \right) -$$

$$\left. \left. 2\sqrt{fv-2fs} \sin\left( 2gs - \frac{1}{2}\pi(v-1) - gv - (fv-2fs)z - (-b-2cs+cv)\sqrt{z} \right) \right) \right) /; v \in \mathbb{N}^+$$

Involving  $\sin(bz' + e) \sin^v(cz' + fz + g)$

01.06.21.0770.01

$$\int \sin(bz^2 + e) \sin^v(cz^2 + fz + g) dz =$$

$$\begin{aligned}
 & -\frac{2^{-v-\frac{1}{2}}}{\sqrt{b}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -\cos(e) S\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) - C\left(\sqrt{b} \sqrt{\frac{2}{\pi}} z\right) \sin(e) \right) - 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \\
 & \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{(fv-2fs)^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) C\left(\frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) + \right. \right. \\
 & \left. \left. S\left(\frac{-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}}\right) \sin\left(\frac{(fv-2fs)^2}{4(-b-2cs+cv)} + e + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) \right) + \\
 & \frac{1}{\sqrt{-b+2cs-cv}} \left( \cos\left(\frac{(2fs-fv)^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \right. \\
 & \left. C\left(\frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) + S\left(\frac{2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}}\right) \right. \\
 & \left. \left. \sin\left(\frac{(2fs-fv)^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2}\pi(v+1)\right) \right) \right) \Bigg/ ; v \in \mathbb{N}^+
 \end{aligned}$$



01.06.21.0771.01

$$\int \sin(\sqrt{z} b + e) \sin^v(\sqrt{z} c + f z + g) dz = \frac{2^{1-v} \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) (b \sqrt{z} \cos(\sqrt{z} b + e) - \sin(\sqrt{z} b + e))}{b^2} -$$

$$2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(fv-2fs)^{3/2}} \left[ \sqrt{2\pi} (b+2cs-cv) \cos\left(\frac{(-b-2cs+cv)^2}{4(fv-2fs)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) \right. \right.$$

$$C\left(\frac{-b-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) - \sqrt{2\pi} (-b-2cs+cv)$$

$$S\left(\frac{-b-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) \sin\left(\frac{(-b-2cs+cv)^2}{4(fv-2fs)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) -$$

$$\left. \left. 2\sqrt{fv-2fs} \sin\left(e + 2gs - \frac{1}{2}\pi(v-1) - gv - (fv-2fs)z - (-b-2cs+cv)\sqrt{z}\right) \right] \right) +$$

$$\frac{1}{(2fs-fv)^{3/2}} \left[ \sqrt{2\pi} (b-2cs+cv) \cos\left(\frac{(-b+2cs-cv)^2}{4(2fs-fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) \right.$$

$$C\left(\frac{-b+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) - \sqrt{2\pi} (-b+2cs-cv)$$

$$S\left(\frac{-b+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) \sin\left(\frac{(-b+2cs-cv)^2}{4(2fs-fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1)\right) -$$

$$\left. \left. 2\sqrt{2fs-fv} \sin\left(e - 2gs + gv + \frac{1}{2}\pi(v+1) - (2fs-fv)z - (-b+2cs-cv)\sqrt{z}\right) \right] \right) ; v \in \mathbb{N}^+$$

Involving  $\sin(bz' + dz) \sin^v(cz' + fz + g)$

01.06.21.0772.01

$$\begin{aligned}
 & \int \sin(bz^2 + dz) \sin^v(cz^2 + fz + g) dz = \\
 & -\frac{2^{-v-\frac{1}{2}}}{\sqrt{b}} \sqrt{\pi} \left(\frac{v}{2}\right) (1-v \bmod 2) \left( C\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \sin\left(\frac{d^2}{4b}\right) - \cos\left(\frac{d^2}{4b}\right) S\left(\frac{d+2bz}{\sqrt{b}\sqrt{2\pi}}\right) \right) - \\
 & 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos\left(\frac{(-d-2fs+fv)^2}{4(-b-2cs+cv)} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right. \right. \\
 & \quad \left. \left. C\left(\frac{-d-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi}\sqrt{-b-2cs+cv}}\right) + S\left(\frac{-d-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi}\sqrt{-b-2cs+cv}}\right) \right. \right. \\
 & \quad \left. \left. \sin\left(\frac{(-d-2fs+fv)^2}{4(-b-2cs+cv)} + \frac{1}{2}\pi(1-v) + g(2s-v)\right) \right) + \frac{1}{\sqrt{-b+2cs-cv}} \right. \\
 & \quad \left. \left( \cos\left(-\frac{(-d+2fs-fv)^2}{4(-b+2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) C\left(\frac{-d+2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi}\sqrt{-b+2cs-cv}}\right) - \right. \right. \\
 & \quad \left. \left. S\left(\frac{-d+2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi}\sqrt{-b+2cs-cv}}\right) \sin\left(-\frac{(-d+2fs-fv)^2}{4(-b+2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(v+1)\right) \right) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0773.01

$$\int \sin(\sqrt{z} b + dz) \sin^v(\sqrt{z} c + fz + g) dz = \frac{1}{d^{3/2}} \left( 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right. \\
 \left. \left( -2\sqrt{d} \cos(\sqrt{z} b + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d}\right) S\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + b\sqrt{2\pi} C\left(\frac{b+2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d}\right) \right) \right) - \\
 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d+2fs-fv)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(-\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1)\right) \right. \right. \\
 \left. \left. C\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) + \sqrt{2\pi} (-b+2cs-cv) \right. \right. \\
 \left. \left. S\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) \sin\left(-\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(v+1)\right) \right) + \right. \\
 \left. 2\sqrt{-d+2fs-fv} \sin\left(2gs-gv - \frac{1}{2}\pi(v+1) + (-d+2fs-fv)z + (-b+2cs-cv)\sqrt{z}\right) \right) + \\
 \frac{1}{(-d-2fs+fv)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(\frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) \right. \\
 \left. C\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) - \sqrt{2\pi} (-b-2cs+cv) \right. \\
 \left. S\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)} + 2gs - \frac{1}{2}\pi(v-1) - gv\right) \right) - \\
 \left. 2\sqrt{-d-2fs+fv} \sin\left(2gs - \frac{1}{2}\pi(v-1) - gv - (-d-2fs+fv)z - (-b-2cs+cv)\sqrt{z}\right) \right) \Bigg) /; v \in \mathbb{N}^+$$

Involving  $\sin(bz' + dz + e) \sin^v(cz' + fz + g)$

01.06.21.0774.01

$$\begin{aligned}
 & \int \sin(bz^2 + dz + e) \sin^v(cz^2 + fz + g) dz = \\
 & -\frac{2^{-v-\frac{1}{2}} \sqrt{\pi}}{\sqrt{b}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( C \left( \frac{d+2bz}{\sqrt{b} \sqrt{2\pi}} \right) \sin \left( \frac{d^2}{4b} - e \right) - \cos \left( \frac{d^2}{4b} - e \right) S \left( \frac{d+2bz}{\sqrt{b} \sqrt{2\pi}} \right) \right) - \\
 & 2^{-v-\frac{1}{2}} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{-b-2cs+cv}} \left( \cos \left( \frac{(-d-2fs+fv)^2}{4(-b-2cs+cv)} + e + \frac{1}{2} \pi(1-v) + g(2s-v) \right) \right. \right. \\
 & \quad C \left( \frac{-d-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}} \right) + S \left( \frac{-d-2fs+fv+2(-b-2cs+cv)z}{\sqrt{2\pi} \sqrt{-b-2cs+cv}} \right) \\
 & \quad \left. \left. \sin \left( \frac{(-d-2fs+fv)^2}{4(-b-2cs+cv)} + e + \frac{1}{2} \pi(1-v) + g(2s-v) \right) \right) + \frac{1}{\sqrt{-b+2cs-cv}} \right. \\
 & \quad \left( \cos \left( \frac{(-d+2fs-fv)^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2} \pi(v+1) \right) C \left( \frac{-d+2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}} \right) + \right. \\
 & \quad \left. \left. S \left( \frac{-d+2fs-fv+2(-b+2cs-cv)z}{\sqrt{2\pi} \sqrt{-b+2cs-cv}} \right) \sin \left( \frac{(-d+2fs-fv)^2}{4(-b+2cs-cv)} + e - g(2s-v) + \frac{1}{2} \pi(v+1) \right) \right) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0775.01

$$\int \sin(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + fz + g) dz = \frac{1}{d^{3/2}} 2^{-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( -2\sqrt{d} \cos(\sqrt{z} b + e + dz) - b\sqrt{2\pi} \cos\left(\frac{b^2}{4d} - e\right) S\left(\frac{b + 2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) + b\sqrt{2\pi} C\left(\frac{b + 2d\sqrt{z}}{\sqrt{d}\sqrt{2\pi}}\right) \sin\left(\frac{b^2}{4d} - e\right) \right) -$$

$$2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(-d-2fs+fv)^{3/2}} \left( \sqrt{2\pi} (b+2cs-cv) \cos\left(\frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) \right. \right.$$

$$C\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) - \sqrt{2\pi} (-b-2cs+cv)$$

$$S\left(\frac{-b-2cs+cv+2(-d-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d-2fs+fv}}\right) \sin\left(\frac{(-b-2cs+cv)^2}{4(-d-2fs+fv)} + e + 2gs - \frac{1}{2}\pi(v-1) - gv\right) -$$

$$\left. \left. 2\sqrt{-d-2fs+fv} \sin\left(e + 2gs - \frac{1}{2}\pi(v-1) - gv - (-d-2fs+fv)z - (-b-2cs+cv)\sqrt{z}\right) \right) \right) +$$

$$\frac{1}{(-d+2fs-fv)^{3/2}} \left( \sqrt{2\pi} (b-2cs+cv) \cos\left(\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1) \right) \right.$$

$$C\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right) -$$

$$\sqrt{2\pi} (-b+2cs-cv) S\left(\frac{-b+2cs-cv+2(-d+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{-d+2fs-fv}}\right)$$

$$\sin\left(\frac{(-b+2cs-cv)^2}{4(-d+2fs-fv)} + e - 2gs + gv + \frac{1}{2}\pi(v+1) \right) - 2\sqrt{-d+2fs-fv}$$

$$\left. \left. \sin\left(e - 2gs + gv + \frac{1}{2}\pi(v+1) - (-d+2fs-fv)z - (-b+2cs-cv)\sqrt{z}\right) \right) \right) /; v \in \mathbb{N}^+$$

Involving product of powers of two direct functions

Involving  $\sin^\mu(cz) \sin^v(az)$

01.06.21.0776.01

$$\int \sin^\mu(cz) \sin^\nu(az) dz = \frac{i 2^{-\nu} (1 - e^{2icz})^{-\mu} \sin^\mu(cz)}{c\mu} \left( \left(\frac{\nu}{2}\right) {}_2F_1\left(-\frac{\mu}{2}, -\mu; 1 - \frac{\mu}{2}; e^{2icz}\right) (1 - \nu \bmod 2) + \right. \\ \left. c\mu i^{-\nu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{i(-az\nu + \pi\nu + 2akz)}}{-2ak + av + c\mu} {}_2F_1\left(-\frac{2ak + av + c\mu}{2c}, -\mu; \frac{1}{2}\left(\frac{a(2k - \nu)}{c} - \mu + 2\right); e^{2icz}\right) + \right. \right. \\ \left. \left. \frac{e^{ia(v-2k)z}}{2ak - av + c\mu} {}_2F_1\left(-\frac{2ak - av + c\mu}{2c}, -\mu; \frac{1}{2}\left(\frac{a(v-2k)}{c} - \mu + 2\right); e^{2icz}\right) \right) \right); \nu \in \mathbb{N}^+$$

01.06.21.0777.01

$$\int \sin^m(cz) \sin^\nu(az) dz = 2^{-m-\nu} \left( (-1)^m z \binom{m}{\frac{m}{2}} \binom{\nu}{\frac{\nu}{2}} (m \bmod 2 - 1) (\nu \bmod 2 - 1) - \right. \\ \left. \frac{i^{1-m}}{c} \binom{\nu}{\frac{\nu}{2}} (\nu \bmod 2 - 1) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \frac{(-1)^k e^{-ic(m-2k)z} (-(-1)^m + e^{2ic(m-2k)z})}{2k - m} - \right. \\ \left. \frac{(-1)^m i^{1-\nu}}{a} \binom{m}{\frac{m}{2}} (m \bmod 2 - 1) \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \binom{\nu}{s} \frac{(-1)^s e^{-ia(v-2s)z} (-(-1)^\nu + e^{2ia(v-2s)z})}{2s - \nu} - \right. \\ \left. i^{-m-\nu+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^{m+s} \binom{\nu}{s} \left( \frac{e^{i(\pi\nu - (2ck - 2as + a\nu)z + m(cz + \pi))}}{-2ck + cm + 2as - a\nu} + \frac{e^{i(\pi\nu + (2ck - cm + 2as - a\nu)z)}}{2ck - cm + 2as - a\nu} + \right. \right. \\ \left. \left. \frac{e^{i((a(v-2s) - 2ck)z + m(cz + \pi))}}{c(m-2k) + a(v-2s)} + \frac{e^{i(2ck - cm - 2as + a\nu)z}}{2ck - cm - 2as + a\nu} \right) \right); m \in \mathbb{N}^+ \wedge \nu \in \mathbb{N}^+$$

01.06.21.0778.01

$$\int \sin^\mu(cz) \sin^\nu(2cz) dz = -\frac{1}{c(\nu+1)} \cos(cz) {}_2F_1\left(\frac{\nu+1}{2}, \frac{1}{2}(-\mu-\nu+1); \frac{\nu+3}{2}; \cos^2(cz)\right) \sin^{\mu+1}(cz) \sin^2(cz)^{\frac{1}{2}(-\mu-\nu-1)} \sin^\nu(2cz)$$

01.06.21.0779.01

$$\int \sin^2(cz) \sin^{\frac{1}{2}}(az) dz = \left( -4(a^2 - 16c^2) \sqrt{1 - e^{2iaz}} E\left(\frac{1}{4}(\pi - 2az) \middle| 2\right) - i\sqrt{2} a e^{-2icz} \sqrt{-i e^{-iaz} (-1 + e^{2iaz})} \left( (a+4c) e^{4icz} \right. \right. \\ \left. \left. {}_2F_1\left(\frac{c}{a} - \frac{1}{4}, -\frac{1}{2}; \frac{c}{a} + \frac{3}{4}; e^{2iaz}\right) + (a-4c) {}_2F_1\left(-\frac{c}{a} - \frac{1}{4}, -\frac{1}{2}; \frac{3}{4} - \frac{c}{a}; e^{2iaz}\right) \right) \right) / \left( 4(a^3 - 16ac^2) \sqrt{1 - e^{2iaz}} \right)$$

01.06.21.0780.01

$$\int \sin^2(cz) \sin^{\frac{1}{2}}(2cz) dz = -\frac{\sin^{\frac{3}{2}}(2cz) + 3E\left(\frac{\pi}{4} - cz \middle| 2\right)}{6c}$$

01.06.21.0781.01

$$\int \frac{\sin^2(cz)}{\sin^{\frac{1}{2}}(az)} dz = \left( e^{-\frac{1}{2}iaz} \left( ia \sqrt{2-2e^{2iaz}} \right. \right. \\ \left. \left. \left( (a-4c) e^{\frac{1}{2}i(a+4c)z} {}_2F_1\left(\frac{c}{a} + \frac{1}{4}, \frac{1}{2}; \frac{c}{a} + \frac{5}{4}; e^{2iaz}\right) + (a+4c) e^{\frac{1}{2}i(a-4c)z} {}_2F_1\left(\frac{1}{4} - \frac{c}{a}, \frac{1}{2}; \frac{5}{4} - \frac{c}{a}; e^{2iaz}\right) \right) - \right. \\ \left. \left. 2(a^2 - 16c^2) e^{\frac{iaz}{2}} \sqrt{-i e^{-iaz}(-1 + e^{2iaz})} F\left(\frac{1}{4}(\pi - 2az) \mid 2\right) \right) \right) / \left( 2(a^3 - 16ac^2) \sqrt{-i e^{-iaz}(-1 + e^{2iaz})} \right)$$

01.06.21.0782.01

$$\int \frac{\sin^2(cz)}{\sin^{\frac{1}{2}}(2cz)} dz = \\ \frac{1}{4c \sqrt{\sin(2cz) + 1}} \left( -\sqrt{2} F\left(\sin^{-1}(\cos(cz) - \sin(cz)) \mid \frac{1}{2}\right) (\cos(cz) + \sin(cz)) - 2 \sin^{\frac{1}{2}}(2cz) \sqrt{\sin(2cz) + 1} \right)$$

01.06.21.0783.01

$$\int \frac{\sin^7(cz)}{\sqrt{\sin^7(2cz)}} dz = \\ \frac{\sin^4(2cz)}{120c \sqrt[4]{\sin^2(cz)} \sqrt{\sin^7(2cz)}} \left( 3 \sec(cz) (\sec^2(cz) - 6) \sqrt[4]{\sin^2(cz)} - 5 \cos(cz) {}_2F_1\left(\frac{3}{4}, \frac{3}{4}; \frac{7}{4}; \cos^2(cz)\right) \right)$$

### Involving $\sin^\mu(cz) \sin^\nu(az + b)$

01.06.21.0784.01

$$\int \sin^\mu(cz) \sin^\nu(az + b) dz = \frac{i 2^{-\nu} (1 - e^{2icz})^{-\mu} \sin^\mu(cz)}{c \mu} \left( \left( \frac{\nu}{\frac{\nu}{2}} \right) {}_2F_1\left(-\frac{\mu}{2}, -\mu; 1 - \frac{\mu}{2}; e^{2icz}\right) (1 - \nu \bmod 2) + i^{-\nu} c \mu \right. \\ \left. \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k e^{ib(v-2k)} \binom{\nu}{k} \left( \frac{e^{i(4bk+2azk-2bv+\pi v-avz)}}{-2ak+av+c\mu} {}_2F_1\left(-\frac{2ak+av+c\mu}{2c}, -\mu; \frac{1}{2}\left(\frac{a(2k-\nu)}{c} - \mu + 2\right); e^{2icz}\right) + \right. \right. \\ \left. \left. \frac{e^{ia(v-2k)z}}{2ak-av+c\mu} {}_2F_1\left(-\frac{2ak-av+c\mu}{2c}, -\mu; \frac{1}{2}\left(\frac{a(v-2k)}{c} - \mu + 2\right); e^{2icz}\right) \right) \right) /; \nu \in \mathbb{N}^+$$

01.06.21.0785.01

$$\int \sin^m(cz) \sin^v(az+b) dz = \frac{i 2^{-m} (1 - e^{2i(b+az)})^{-v} \sin^v(b+az)}{av} \left( \binom{m}{\frac{m}{2}} {}_2F_1\left(-\frac{v}{2}, -v; 1 - \frac{v}{2}; e^{2i(b+az)}\right) (1 - m \bmod 2) + \right.$$

$$i^{-m} a v \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( \frac{e^{i(-cm+\pi m+2ckz)}}{-2ck+cm+av} {}_2F_1\left(-\frac{2ck+cm+av}{2a}, -v; \frac{1}{2}\left(\frac{c(2k-m)}{a} - v + 2\right); e^{2i(b+az)}\right) + \right.$$

$$\left. \left. \frac{e^{ic(m-2k)z}}{2ck-cm+av} {}_2F_1\left(-\frac{2ck-cm+av}{2a}, -v; \frac{1}{2}\left(\frac{c(m-2k)}{a} - v + 2\right); e^{2i(b+az)}\right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.0786.01

$$\int \sin^m(cz) \sin^v(az+b) dz = i 2^{-m-v} \left( i (-1)^{m-1} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (m \bmod 2 - 1) (v \bmod 2 - 1) - \right.$$

$$\frac{i^{-m}}{c} \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^k e^{-ic(m-2k)z} (-(-1)^m + e^{2ic(m-2k)z}) \binom{m}{k}}{2k-m} -$$

$$\frac{1}{a} \left( (-1)^m i^{-v} \binom{m}{\frac{m}{2}} (m \bmod 2 - 1) \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^s e^{-i(b(2s+v)+a(v-2s)z)} (-(-1)^v e^{4ibs} + e^{2i(bv+a(v-2s)z)}) \binom{v}{s}}{2s-v} \right) +$$

$$i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{m+s} e^{-ib(2s+v)} \left( \frac{e^{-i((-2ck+cm+2as-av)z-2bv)}}{-2ck+cm+2as-av} + \frac{e^{i(2bv+azv-2ckz-2asz+m(cz+\pi))}}{2ck-cm+2as-av} + \right.$$

$$\left. \left. \frac{e^{i(4bs+2asz+\pi v+2ckz-cmz-avz)}}{c(m-2k)+a(v-2s)} + \frac{e^{i(4bs+2asz+\pi v-2ckz-avz+m(cz+\pi))}}{2ck-cm-2as+av} \right) \binom{v}{s} \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $\sin^\mu(cz+d) \sin^v(az+b)$**



01.06.21.0787.01

$$\int \sin^\mu(d + cz) \sin^\nu(b + az) dz =$$

$$\frac{i 2^{-\nu} (1 - e^{2i(d+cz)})^{-\mu} \sin^\mu(d + cz)}{c \mu} \left( \binom{\nu}{\frac{\nu}{2}} {}_2F_1\left(-\frac{\mu}{2}, -\mu; 1 - \frac{\mu}{2}; e^{2i(d+cz)}\right) (1 - \nu \bmod 2) + c \mu i^{-\nu} \right.$$

$$\left. \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k e^{ib(v-2k)} \binom{\nu}{k} \left( \frac{e^{i(4bk+2azk-2bv+\pi v-avz)}}{-2ak+av+c\mu} {}_2F_1\left(-\frac{2ak+av+c\mu}{2c}, -\mu; \frac{1}{2}\left(\frac{a(2k-\nu)}{c} - \mu + 2\right)\right); e^{2i(d+cz)}\right) + \right.$$

$$\left. \frac{e^{ia(v-2k)z}}{2ak-av+c\mu} {}_2F_1\left(-\frac{2ak-av+c\mu}{2c}, -\mu; \frac{1}{2}\left(\frac{a(v-2k)}{c} - \mu + 2\right)\right); e^{2i(d+cz)} \right) \Bigg/; \nu \in \mathbb{N}^+$$

01.06.21.0788.01

$$\int \sin^m(cz + d) \sin^\nu(az + b) dz = 2^{-m-\nu} i \left( i (-1)^{m-1} z \binom{m}{\frac{m}{2}} \binom{\nu}{\frac{\nu}{2}} (m \bmod 2 - 1) (\nu \bmod 2 - 1) - \right.$$

$$\frac{i^{-m}}{c} \binom{\nu}{\frac{\nu}{2}} (\nu \bmod 2 - 1) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \frac{(-1)^k e^{-i(d(2k+m)+c(m-2k)z)} (-(-1)^m e^{4ik} + e^{2i(dm+c(m-2k)z)})}{2k-m} - \frac{(-1)^m i^{-\nu}}{a} \binom{m}{\frac{m}{2}} \left. \right)$$

$$(m \bmod 2 - 1) \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \binom{\nu}{s} \frac{(-1)^s e^{-i(b(2s+\nu)+a(v-2s)z)} (-(-1)^\nu e^{4ibs} + e^{2i(bv+a(v-2s)z)})}{2s-\nu} + i^{-m-\nu} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left. \right)$$

$$\sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^{m+s} e^{i(d(2k+m)-b(2s+\nu))} \binom{\nu}{s} \left( \frac{e^{-i(2dm-2bv+(-2ck+cm+2as-av)z)}}{-2ck+cm+2as-av} + \frac{e^{i(-4dk-2czk+2bv-2asz+avz+m(cz+\pi))}}{2ck-cm+2as-av} + \right.$$

$$\left. \frac{e^{i(-2dm-czm+4bs+\pi v+2ckz+2asz-avz)}}{c(m-2k)+a(v-2s)} + \frac{e^{i(-4dk-2czk+4bs+\pi v+2asz-avz+m(cz+\pi))}}{2ck-cm-2as+av} \right) \Bigg/; m \in \mathbb{N}^+ \wedge \nu \in \mathbb{N}^+$$

**Involving  $\sin^m(bz) \sin^\nu(cz')$**

01.06.21.0789.01

$$\begin{aligned}
 \int \sin^m(bz) \sin^v(cz^2) dz &= 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \\
 &\frac{2^{-m-v+1}}{b} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + b(m-2k)z\right)}{m-2k} + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \\
 &\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^{k+v}}{\sqrt{c(v-2k)}} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2}\right) C\left(\frac{c \sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) - S\left(\frac{c \sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2}\right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \\
 &\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{(2bk-bm)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v)\right) C\left(\frac{2bk-bm+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) + \right. \right. \\
 &\left. \left. S\left(\frac{2bk-bm+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) \sin\left(\frac{(2bk-bm)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v)\right) \right) \right) + \\
 &\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(\frac{(2bk-bm)^2}{4(2cs-cv)} + \frac{1}{2}\pi(m+v)\right) C\left(\frac{2bk-bm+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) + \right. \\
 &\left. \left. S\left(\frac{2bk-bm+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) \sin\left(\frac{(2bk-bm)^2}{4(2cs-cv)} + \frac{1}{2}\pi(m+v)\right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0790.01

$$\begin{aligned}
 \int \sin^m(bz) \sin^v(c\sqrt{z}) dz &= 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \\
 &\frac{2^{-m-v+1}}{b} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + b(m-2k)z\right)}{m-2k} + \frac{1}{c^2} \left( 2^{-m-v+2} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \right. \\
 &\left. \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(v-2k)^2} \left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + c(v-2k)\sqrt{z}\right) + c(v-2k)\sqrt{z} \sin\left(\frac{\pi v}{2} + c(v-2k)\sqrt{z}\right) \right) \right) \right) + \\
 &2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \\
 &\left( \frac{1}{(2bk-bm)^{3/2}} \left( \sqrt{2\pi} (2cs-cv) \cos\left(\frac{1}{2}\pi(v-m) - \frac{(cv-2cs)^2}{4(2bk-bm)}\right) C\left(\frac{2\sqrt{z}(2bk-bm)-2cs+cv}{\sqrt{2bk-bm}\sqrt{2\pi}}\right) \right. \right. \\
 &\quad \left. \left. \sqrt{2\pi} (cv-2cs) S\left(\frac{2\sqrt{z}(2bk-bm)-2cs+cv}{\sqrt{2bk-bm}\sqrt{2\pi}}\right) \sin\left(\frac{1}{2}\pi(v-m) - \frac{(cv-2cs)^2}{4(2bk-bm)}\right) \right) + \right. \\
 &\quad \left. 2\sqrt{2bk-bm} \sin\left(\frac{1}{2}\pi(v-m) + (2bk-bm)z + (cv-2cs)\sqrt{z}\right) \right) + \\
 &\frac{1}{(2bk-bm)^{3/2}} \left( \sqrt{2\pi} (cv-2cs) \cos\left(\frac{(2cs-cv)^2}{4(2bk-bm)} + \frac{1}{2}\pi(m+v)\right) C\left(\frac{2\sqrt{z}(2bk-bm)+2cs-cv}{\sqrt{2bk-bm}\sqrt{2\pi}}\right) \right. \\
 &\quad \left. \sqrt{2\pi} (2cs-cv) S\left(\frac{2\sqrt{z}(2bk-bm)+2cs-cv}{\sqrt{2bk-bm}\sqrt{2\pi}}\right) \sin\left(\frac{(2cs-cv)^2}{4(2bk-bm)} + \frac{1}{2}\pi(m+v)\right) \right. \\
 &\quad \left. 2\sqrt{2bk-bm} \sin\left(\frac{1}{2}\pi(m+v) - (2bk-bm)z - (2cs-cv)\sqrt{z}\right) \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(dz + e) \sin^v(cz^r)$

01.06.21.0791.01

$$\int \sin^m(e + dz) \sin^v(cz^2) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$\frac{2^{-m-v+1} (1 - v \bmod 2)}{d} \binom{v}{\frac{v}{2}} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + e(m-2k) + d(m-2k)z\right)}{m-2k} \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}}$$

$$(1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^{k+v}}{\sqrt{c(v-2k)}} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2}\right) C\left(\sqrt{\frac{2}{\pi}} \frac{c(v-2k)z}{\sqrt{c(v-2k)}}\right) - S\left(\sqrt{\frac{2}{\pi}} \frac{c(v-2k)z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2}\right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(-\frac{(2dk-dm)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v)\right) C\left(\frac{2dk-dm+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) - \right.$$

$$\left. S\left(\frac{2dk-dm+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \sin\left(-\frac{(2dk-dm)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v)\right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(-\frac{(2dk-dm)^2}{4(2cs-cv)} + e(2k-m) - \frac{1}{2}\pi(m+v)\right) C\left(\frac{2dk-dm+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) - \right.$$

$$\left. S\left(\frac{2dk-dm+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(-\frac{(2dk-dm)^2}{4(2cs-cv)} + e(2k-m) - \frac{1}{2}\pi(m+v)\right) \right) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0792.01

$$\begin{aligned}
 \int \sin^m(e + dz) \sin^v(c \sqrt{z}) dz &= 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \\
 &\frac{2^{-m-v+1} (1 - v \bmod 2)}{d} \binom{v}{\frac{v}{2}} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + e(m-2k) + d(m-2k)z\right)}{m-2k} + \frac{1}{c^2} 2^{-m-v+2} \binom{m}{\frac{m}{2}} \\
 &(1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^{k+v}}{(v-2k)^2} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + c(v-2k)\sqrt{z}\right) + c(v-2k)\sqrt{z} \sin\left(\frac{\pi v}{2} + c(v-2k)\sqrt{z}\right) \right) + \\
 &2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(2dk-dm)^{3/2}} \right. \\
 &\left. \left( \sqrt{2\pi} (2cs-cv) \cos\left(-\frac{(cv-2cs)^2}{4(2dk-dm)} + 2ek-em + \frac{1}{2}\pi(v-m)\right) C\left(\frac{2\sqrt{z}(2dk-dm)-2cs+cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) + \right. \right. \\
 &\left. \left. \sqrt{2\pi} (cv-2cs) S\left(\frac{2\sqrt{z}(2dk-dm)-2cs+cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) \sin\left(-\frac{(cv-2cs)^2}{4(2dk-dm)} + 2ek-em + \frac{1}{2}\pi \right. \right. \right. \\
 &\left. \left. \left. (v-m)\right) + 2\sqrt{2dk-dm} \sin\left(2ek-em + \frac{1}{2}\pi(v-m) + (2dk-dm)z + (cv-2cs)\sqrt{z}\right) \right) \right) + \\
 &\frac{1}{(2dk-dm)^{3/2}} \left( \sqrt{2\pi} (cv-2cs) \cos\left(-\frac{(2cs-cv)^2}{4(2dk-dm)} + 2ek-em - \frac{1}{2}\pi(m+v)\right) \right. \\
 &\left. C\left(\frac{2\sqrt{z}(2dk-dm)+2cs-cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) + \sqrt{2\pi} (2cs-cv) \right. \\
 &\left. S\left(\frac{2\sqrt{z}(2dk-dm)+2cs-cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) \sin\left(-\frac{(2cs-cv)^2}{4(2dk-dm)} + 2ek-em - \frac{1}{2}\pi(m+v)\right) + \right. \\
 &\left. \left. 2\sqrt{2dk-dm} \sin\left(2ek-em - \frac{1}{2}\pi(m+v) + (2dk-dm)z + (2cs-cv)\sqrt{z}\right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(bz^r) \sin^v(cz^r)$

01.06.21.0793.01

$$\int \sin^m(b z^r) \sin^v(c z^r) dz =$$

$$(-1)^m 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2) - \frac{1}{r} i^{-m} 2^{-m-v} z \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( (-1)^m \Gamma\left(\frac{1}{r}, (ibm - 2ibk) z^r\right) ((ibm - 2ibk) z^r)^{-1/r} + ((2ibk - ibm) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm) z^r\right) \right) -$$

$$\frac{1}{r} (-1)^m i^{-v} 2^{-m-v} z \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v \Gamma\left(\frac{1}{r}, (icv - 2ick) z^r\right) ((icv - 2ick) z^r)^{-1/r} + \right.$$

$$\left. ((2ick - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ick - icv) z^r\right) \right) - \frac{1}{r} (2i)^{-m-v} z \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{m+v} \Gamma\left(\frac{1}{r}, (-2bik + ibm - 2ics + icv) z^r\right) ((-2bik + ibm - 2ics + icv) z^r)^{-1/r} + \right.$$

$$\left. (-1)^v ((2ibk - ibm - 2ics + icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm - 2ics + icv) z^r\right) + \right.$$

$$\left. (-1)^m ((-2bik + ibm + 2ics - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-2bik + ibm + 2ics - icv) z^r\right) + \right.$$

$$\left. ((2ibk - ibm + 2ics - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm + 2ics - icv) z^r\right) \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0794.01

$$\int \sin^m(b z^2) \sin^v(c z^2) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m}}{\sqrt{b(m-2k)}} \binom{m}{k} \left( \cos\left(\frac{m\pi}{2}\right) C\left(\frac{b(m-2k)}{\sqrt{b(m-2k)}} \sqrt{\frac{2}{\pi}} z\right) - S\left(\frac{b(m-2k)}{\sqrt{b(m-2k)}} \sqrt{\frac{2}{\pi}} z\right) \sin\left(\frac{m\pi}{2}\right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi}$$

$$\binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^{k+v}}{\sqrt{c(v-2k)}} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2}\right) C\left(\sqrt{\frac{2}{\pi}} \frac{c(v-2k)z}{\sqrt{c(v-2k)}}\right) - S\left(\sqrt{\frac{2}{\pi}} \frac{c(v-2k)z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2}\right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \cos\left(\frac{1}{2} \pi(m-v)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm - 2cs + cv} z\right) + \right.$$

$$\left. S\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm - 2cs + cv} z\right) \sin\left(\frac{1}{2} \pi(m-v)\right) \right) / (\sqrt{2bk - bm - 2cs + cv}) +$$

$$\left( \cos\left(\frac{1}{2} \pi(m+v)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm + 2cs - cv} z\right) + S\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm + 2cs - cv} z\right) \right.$$

$$\left. \sin\left(\frac{1}{2} \pi(m+v)\right) \right) / (\sqrt{2bk - bm + 2cs - cv}); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0795.01

$$\int \sin^m(b\sqrt{z}) \sin^v(c\sqrt{z}) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2) + \frac{1}{b^2} 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(m-2k)^2} \left( (-1)^{k+m} \binom{m}{k} \left( \cos\left(\frac{\pi m}{2} + b(m-2k)\sqrt{z}\right) + b(m-2k)\sqrt{z} \sin\left(\frac{\pi m}{2} + b(m-2k)\sqrt{z}\right) \right) \right) + \frac{1}{c^2} 2^{-m-v+2}$$

$$\binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^{k+v}}{(v-2k)^2} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + c(v-2k)\sqrt{z}\right) + c(v-2k)\sqrt{z} \sin\left(\frac{\pi v}{2} + c(v-2k)\sqrt{z}\right) \right) +$$

$$2^{-m-v+2} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \cos\left(\frac{1}{2} \pi (v-m) + (2bk - bm - 2cs + cv)\sqrt{z}\right) + (2bk - bm - 2cs + cv) \right. \right.$$

$$\left. \left. \sqrt{z} \sin\left(\frac{1}{2} \pi (v-m) + (2bk - bm - 2cs + cv)\sqrt{z}\right) \right) / (2bk - bm - 2cs + cv)^2 + \right.$$

$$\left. \left( \cos\left(\frac{1}{2} \pi (m+v) - (2bk - bm + 2cs - cv)\sqrt{z}\right) - (2bk - bm + 2cs - cv)\sqrt{z} \right. \right.$$

$$\left. \left. \sin\left(\frac{1}{2} \pi (m+v) - (2bk - bm + 2cs - cv)\sqrt{z}\right) \right) / (2bk - bm + 2cs - cv)^2 \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $\sin^m(dz) \sin^v(cz^r + g)$**

01.06.21.0796.01

$$\int \sin^m(dz) \sin^v(cz^2 + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin(2dkz - \frac{1}{2}m(2dz + \pi))}{2k - m} +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}}$$

$$\left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c \sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) - S\left(\frac{c \sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} + g(v-2k)\right) \right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{(2dk-dm)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) C\left(\frac{2dk-dm+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) + \right.$$

$$\left. S\left(\frac{2dk-dm+2(cv-2cs)z}{\sqrt{2\pi}\sqrt{cv-2cs}}\right) \sin\left(\frac{(2dk-dm)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(-\frac{(2dk-dm)^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) C\left(\frac{2dk-dm+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) - \right.$$

$$\left. \left. S\left(\frac{2dk-dm+2(2cs-cv)z}{\sqrt{2\pi}\sqrt{2cs-cv}}\right) \sin\left(-\frac{(2dk-dm)^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$



01.06.21.0797.01

$$\int \sin^m(dz) \sin^v(\sqrt{z}c + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + d(m-2k)z\right)}{m-2k} +$$

$$\frac{1}{c^2} \left( 2^{-m-v+2} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(v-2k)^2} \left( (-1)^{k+v} \binom{v}{k} \right. \right.$$

$$\left. \left. \left( \cos\left(2gk - gv + c(2k-v)\sqrt{z} - \frac{\pi v}{2}\right) + c(2k-v)\sqrt{z} \sin\left(2gk - gv + c(2k-v)\sqrt{z} - \frac{\pi v}{2}\right) \right) \right) +$$

$$2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(2dk-dm)^{3/2}} \left( \sqrt{2\pi} (cv-2cs) \cos\left(-\frac{(2cs-cv)^2}{4(2dk-dm)} + \right. \right. \right.$$

$$\left. \left. 2gs - gv - \frac{1}{2}\pi(m+v) \right) C\left(\frac{2\sqrt{z}(2dk-dm) + 2cs - cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) + \sqrt{2\pi}(2cs-cv) \right.$$

$$\left. S\left(\frac{2\sqrt{z}(2dk-dm) + 2cs - cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) \sin\left(-\frac{(2cs-cv)^2}{4(2dk-dm)} + 2gs - gv - \frac{1}{2}\pi(m+v)\right) + \right.$$

$$\left. 2\sqrt{2dk-dm} \sin\left(2gs - gv - \frac{1}{2}\pi(m+v) + (2dk-dm)z + (2cs-cv)\sqrt{z}\right) \right) + \frac{1}{(2dk-dm)^{3/2}}$$

$$\left( \sqrt{2\pi}(2cs-cv) \cos\left(\frac{(cv-2cs)^2}{4(2dk-dm)} + 2gs - gv - \frac{1}{2}\pi(v-m)\right) C\left(\frac{2\sqrt{z}(2dk-dm) - 2cs + cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) - \right.$$

$$\left. \sqrt{2\pi}(cv-2cs) S\left(\frac{2\sqrt{z}(2dk-dm) - 2cs + cv}{\sqrt{2dk-dm}\sqrt{2\pi}}\right) \sin\left(\frac{(cv-2cs)^2}{4(2dk-dm)} + 2gs - gv - \frac{1}{2}\pi(v-m)\right) - \right.$$

$$\left. 2\sqrt{2dk-dm} \sin\left(2gs - gv - \frac{1}{2}\pi(v-m) - (2dk-dm)z - (cv-2cs)\sqrt{z}\right) \right) \Big/ ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $\sin^m(dz + e) \sin^v(cz' + g)$

01.06.21.0798.01

$$\int \sin^m(dz + e) \sin^v(cz^2 + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} (-1)^{k+v}$$

$$\binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c \sqrt{\frac{2}{\pi}} (v-2k) z}{\sqrt{c(v-2k)}}\right) - S\left(\frac{c \sqrt{\frac{2}{\pi}} (v-2k) z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} + g(v-2k)\right) \right) +$$

$$\frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(e(2k-m) + 2dkz - \frac{1}{2}m(2dz + \pi)\right)}{2k-m} +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(-\frac{(2dk-dm)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v) - g(2s-v)\right) C\left(\frac{2dk-dm+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) - \right.$$

$$\left. S\left(\frac{2dk-dm+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) \sin\left(-\frac{(2dk-dm)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v) - g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(-\frac{(2dk-dm)^2}{4(2cs-cv)} + e(2k-m) + g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right.$$

$$\left. C\left(\frac{2dk-dm+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) - S\left(\frac{2dk-dm+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) \right.$$

$$\left. \left. \sin\left(-\frac{(2dk-dm)^2}{4(2cs-cv)} + e(2k-m) + g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right) \right) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0799.01

$$\int \sin^m(dz + e) \sin^v(\sqrt{z}c + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{1}{c^2} \left( 2^{-m-v+2} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(v-2k)^2} \left( (-1)^{k+v} \binom{v}{k} \right. \right.$$

$$\left. \left. \left( \cos \left( 2gk - gv + c(2k-v)\sqrt{z} - \frac{\pi v}{2} \right) + c(2k-v)\sqrt{z} \sin \left( 2gk - gv + c(2k-v)\sqrt{z} - \frac{\pi v}{2} \right) \right) \right) \right) +$$

$$\frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin \left( \frac{\pi m}{2} + e(m-2k) + d(m-2k)z \right)}{m-2k} +$$

$$2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(2dk-dm)^{3/2}} \left( \sqrt{2\pi} (2cs-cv) \cos \left( -\frac{(cv-2cs)^2}{4(2dk-dm)} + 2ek-em - \right. \right. \right.$$

$$\left. \left. 2gs + gv + \frac{1}{2}\pi(v-m) \right) C \left( \frac{2\sqrt{z}(2dk-dm) - 2cs + cv}{\sqrt{2dk-dm}\sqrt{2\pi}} \right) + \sqrt{2\pi} (cv-2cs) \right.$$

$$\left. S \left( \frac{2\sqrt{z}(2dk-dm) - 2cs + cv}{\sqrt{2dk-dm}\sqrt{2\pi}} \right) \sin \left( -\frac{(cv-2cs)^2}{4(2dk-dm)} + 2ek-em - 2gs + gv + \frac{1}{2}\pi(v-m) \right) \right) +$$

$$2\sqrt{2dk-dm} \sin \left( 2ek-em - 2gs + gv + \frac{1}{2}\pi(v-m) + (2dk-dm)z + (cv-2cs)\sqrt{z} \right) \left. \right) +$$

$$\frac{1}{(2dk-dm)^{3/2}} \left( \sqrt{2\pi} (cv-2cs) \cos \left( -\frac{(2cs-cv)^2}{4(2dk-dm)} + 2ek-em + 2gs - gv - \frac{1}{2}\pi(m+v) \right) \right.$$

$$C \left( \frac{2\sqrt{z}(2dk-dm) + 2cs - cv}{\sqrt{2dk-dm}\sqrt{2\pi}} \right) + \sqrt{2\pi} (2cs-cv) S \left( \frac{2\sqrt{z}(2dk-dm) + 2cs - cv}{\sqrt{2dk-dm}\sqrt{2\pi}} \right)$$

$$\sin \left( -\frac{(2cs-cv)^2}{4(2dk-dm)} + 2ek-em + 2gs - gv - \frac{1}{2}\pi(m+v) \right) + 2\sqrt{2dk-dm}$$

$$\left. \left. \sin \left( 2ek-em + 2gs - gv - \frac{1}{2}\pi(m+v) + (2dk-dm)z + (2cs-cv)\sqrt{z} \right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $\sin^m(bz^r) \sin^v(cz^r + g)$**

01.06.21.0800.01

$$\int \sin^m(b z^r) \sin^v(c z^r + g) dz =$$

$$\begin{aligned} & (-1)^m 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) - \frac{1}{r} i^{-m} 2^{-m-v} z \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\ & \left( (-1)^m \Gamma\left(\frac{1}{r}, (i b m - 2 i b k) z^r\right) ((i b m - 2 i b k) z^r)^{-1/r} + ((2 i b k - i b m) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2 i b k - i b m) z^r\right) \right) - \\ & \frac{1}{r} \left( (-1)^m i^{-v} 2^{-m-v} z \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{2 i g k - i g v} \Gamma\left(\frac{1}{r}, (i c v - 2 i c k) z^r\right) ((i c v - 2 i c k) z^r)^{-1/r} + \right. \right. \\ & \left. \left. e^{i g v - 2 i g k} ((2 i c k - i c v) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2 i c k - i c v) z^r\right) \right) \right) - \frac{(2 i)^{-m-v} z}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\ & \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{m+v} e^{2 i g s - i g v} \Gamma\left(\frac{1}{r}, (-2 b i k + i b m - 2 i c s + i c v) z^r\right) ((-2 b i k + i b m - 2 i c s + i c v) z^r)^{-1/r} + \right. \\ & (-1)^v e^{2 i g s - i g v} ((2 i b k - i b m - 2 i c s + i c v) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2 i b k - i b m - 2 i c s + i c v) z^r\right) + \\ & (-1)^m e^{i g v - 2 i g s} ((-2 b i k + i b m + 2 i c s - i c v) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-2 b i k + i b m + 2 i c s - i c v) z^r\right) + \\ & \left. e^{i g v - 2 i g s} ((2 i b k - i b m + 2 i c s - i c v) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2 i b k - i b m + 2 i c s - i c v) z^r\right) \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.0801.01

$$\int \sin^m(bz^2) \sin^v(cz^2 + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m}}{\sqrt{b(m-2k)}} \binom{m}{k} \left( \cos\left(\frac{m\pi}{2}\right) C\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) - S\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) \sin\left(\frac{m\pi}{2}\right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c\sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) - S\left(\frac{c\sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} + g(v-2k)\right) \right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \cos\left(\frac{1}{2}\pi(m-v) + g(2s-v)\right) C\left(\sqrt{\frac{2}{\pi}}\sqrt{2bk-bm-2cs+cv}z\right) + S\left(\sqrt{\frac{2}{\pi}}\sqrt{2bk-bm-2cs+cv}z\right) \sin\left(\frac{1}{2}\pi(m-v) + g(2s-v)\right) \right) / (\sqrt{2bk-bm-2cs+cv}) +$$

$$\left( \cos\left(g(2s-v) - \frac{1}{2}\pi(m+v)\right) C\left(\sqrt{\frac{2}{\pi}}\sqrt{2bk-bm+2cs-cv}z\right) - S\left(\sqrt{\frac{2}{\pi}}\sqrt{2bk-bm+2cs-cv}z\right) \sin\left(g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right) / (\sqrt{2bk-bm+2cs-cv}) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0802.01

$$\int \sin^m(\sqrt{z} b) \sin^v(\sqrt{z} c + g) dz = 2^{-m-v} z^{\left(\frac{m}{2}\right)\left(\frac{v}{2}\right)} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{1}{b^2} \left[ 2^{-m-v+2} \left(\frac{v}{2}\right) (1 - v \bmod 2) \right. \\ \left. \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(2k-m)^2} \left( (-1)^k \binom{m}{k} \left( \cos\left(b\sqrt{z}(2k-m) + \frac{m\pi}{2}\right) + b(2k-m)\sqrt{z} \sin\left(b\sqrt{z}(2k-m) + \frac{m\pi}{2}\right) \right) \right) \right] + \\ \frac{1}{c^2} \left[ 2^{-m-v+2} \left(\frac{m}{2}\right) (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(2k-v)^2} \right. \\ \left. \left( (-1)^k \binom{v}{k} \left( \cos\left(c\sqrt{z}(2k-v) + \frac{\pi v}{2} - g(v-2k)\right) + c(2k-v)\sqrt{z} \sin\left(c\sqrt{z}(2k-v) + \frac{\pi v}{2} - g(v-2k)\right) \right) \right) \right] + \\ 2^{-m-v+2} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \left( \cos\left(\frac{1}{2}\pi(m-v) + g(v-2s) + (b(2k-m) + c(v-2s))\sqrt{z}\right) + \right. \right. \\ \left. \left. (b(2k-m) + c(v-2s))\sqrt{z} \sin\left(\frac{1}{2}\pi(m-v) + g(v-2s) + (b(2k-m) + c(v-2s))\sqrt{z}\right) \right) \right) / \\ \left( (b(2k-m) + c(v-2s))^2 + \left( \cos\left(\frac{1}{2}\pi(m+v) - g(v-2s) + (b(2k-m) - c(v-2s))\sqrt{z}\right) + \right. \right. \\ \left. \left. (b(2k-m) - c(v-2s))\sqrt{z} \sin\left(\frac{1}{2}\pi(m+v) - g(v-2s) + (b(2k-m) - c(v-2s))\sqrt{z}\right) \right) \right) / \\ \left. (b(2k-m) - c(v-2s))^2 \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $\sin^m(az^r + e) \sin^v(cz^r + g)$**

01.06.21.0803.01

$$\begin{aligned}
 \int \sin^m(bz^r + e) \sin^v(cz^r + g) dz &= (-1)^m 2^{-m-v} z^{\left(\frac{m}{2}\right)\left(\frac{v}{2}\right)} (1 - m \bmod 2) (1 - v \bmod 2) - \\
 &\frac{1}{r} i^{-m} 2^{-m-v} z^{\left(\frac{v}{2}\right)} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m e^{2iek - iem} \Gamma\left(\frac{1}{r}, (ibm - 2ibk)z^r\right) ((ibm - 2ibk)z^r)^{-1/r} + \right. \\
 &\quad \left. e^{iem - 2iek} ((2ibk - ibm)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm)z^r\right) \right) - \\
 &\frac{1}{r} (-1)^m i^{-v} 2^{-m-v} z^{\left(\frac{m}{2}\right)} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{2igk - igv} \Gamma\left(\frac{1}{r}, (icv - 2ick)z^r\right) ((icv - 2ick)z^r)^{-1/r} + \right. \\
 &\quad \left. e^{igv - 2igk} ((2ick - icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ick - icv)z^r\right) \right) - \\
 &\frac{(2i)^{-m-v} z^{\left(\frac{m-1}{2}\right)\left(\frac{v-1}{2}\right)}}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{m+v} e^{2iek - iem + 2igs - igv} \Gamma\left(\frac{1}{r}, (-2bik + ibm - 2ics + icv)z^r\right) \right. \\
 &\quad \left( (-2bik + ibm - 2ics + icv)z^r \right)^{-1/r} + (-1)^v e^{-2eik + iem + 2igs - igv} \\
 &\quad \left( (2ibk - ibm - 2ics + icv)z^r \right)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm - 2ics + icv)z^r\right) + (-1)^m e^{2iek - iem - 2igs + igv} \\
 &\quad \left( (-2bik + ibm + 2ics - icv)z^r \right)^{-1/r} \Gamma\left(\frac{1}{r}, (-2bik + ibm + 2ics - icv)z^r\right) + e^{-2eik + iem - 2igs + igv} \\
 &\quad \left. \left( (2ibk - ibm + 2ics - icv)z^r \right)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm + 2ics - icv)z^r\right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0804.01

$$\begin{aligned}
 \int \sin^m(bz^2 + e) \sin^v(cz^2 + g) dz &= 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \\
 &2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m}}{\sqrt{b(m-2k)}} \binom{m}{k} \left( \cos\left(\frac{\pi m}{2} + e(m-2k)\right) C\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) - \right. \\
 &\left. S\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) \sin\left(\frac{\pi m}{2} + e(m-2k)\right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \\
 &\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^{k+v}}{\sqrt{c(v-2k)}} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c\sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) - S\left(\frac{c\sqrt{\frac{2}{\pi}}(v-2k)z}{\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} + g(v-2k)\right) \right) + \\
 &2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{2bk - bm - 2cs + cv}} \left( \cos\left(e(2k - m) - \frac{1}{2}\pi(m - v) - g(2s - v)\right) \right. \right. \\
 &\left. \left. C\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm - 2cs + cv} z\right) - S\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm - 2cs + cv} z\right) \right) \right. \\
 &\left. \sin\left(e(2k - m) - \frac{1}{2}\pi(m - v) - g(2s - v)\right) \right) + \frac{1}{\sqrt{2bk - bm + 2cs - cv}} \\
 &\left( \cos\left(e(2k - m) + g(2s - v) - \frac{1}{2}\pi(m + v)\right) C\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm + 2cs - cv} z\right) - \right. \\
 &\left. S\left(\sqrt{\frac{2}{\pi}} \sqrt{2bk - bm + 2cs - cv} z\right) \sin\left(e(2k - m) + g(2s - v) - \frac{1}{2}\pi(m + v)\right) \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$



01.06.21.0805.01

$$\int \sin^m(\sqrt{z} b + e) \sin^v(\sqrt{z} c + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{1}{b^2} 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^k}{(2k-m)^2} \binom{m}{k} \left( \cos\left(-b\sqrt{z}(2k-m) + e(m-2k) - \frac{m\pi}{2}\right) - b(2k-m)\sqrt{z} \sin\left(-b\sqrt{z}(2k-m) + e(m-2k) - \frac{m\pi}{2}\right) \right) + \frac{1}{c^2} 2^{-m-v+2} \binom{m}{\frac{m}{2}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(2k-v)^2} \binom{v}{k} \left( \cos\left(c\sqrt{z}(2k-v) + \frac{\pi v}{2} - g(v-2k)\right) + c(2k-v)\sqrt{z} \sin\left(c\sqrt{z}(2k-v) + \frac{\pi v}{2} - g(v-2k)\right) \right) + 2^{-m-v+2} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{1}{(b(2k-m) + c(v-2s))^2} \left( \cos\left(e(m-2k) - \frac{1}{2}\pi(m-v) - g(v-2s) - (b(2k-m) + c(v-2s))\sqrt{z}\right) - (b(2k-m) + c(v-2s))\sqrt{z} \sin\left(e(m-2k) - \frac{1}{2}\pi(m-v) - g(v-2s) - (b(2k-m) + c(v-2s))\sqrt{z}\right) \right) + \frac{1}{(b(2k-m) - c(v-2s))^2} \left( \cos\left(e(m-2k) - \frac{1}{2}\pi(m+v) + g(v-2s) - (b(2k-m) - c(v-2s))\sqrt{z}\right) - (b(2k-m) - c(v-2s))\sqrt{z} \sin\left(e(m-2k) - \frac{1}{2}\pi(m+v) + g(v-2s) - (b(2k-m) - c(v-2s))\sqrt{z}\right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $\sin^m(dz) \sin^v(cz' + fz)$**

01.06.21.0806.01

$$\int \sin^m(dz) \sin^v(cz^2 + fz) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin(2dkz - \frac{1}{2}m(2dz + \pi))}{2k - m} +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} - \frac{f^2(v-2k)}{4c}\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}}\right) - \right.$$

$$S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{f^2(v-2k)}{4c}\right) \left. \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s}$$

$$\left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{(2dk-dm-2fs+fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v)\right) C\left(\frac{2dk-dm-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) + \right.$$

$$S\left(\frac{2dk-dm-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) \sin\left(\frac{(2dk-dm-2fs+fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v)\right) \left. \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(\frac{(2dk-dm+2fs-fv)^2}{4(2cs-cv)} + \frac{1}{2}\pi(m+v)\right) C\left(\frac{2dk-dm+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) + \right.$$

$$S\left(\frac{2dk-dm+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) \sin\left(\frac{(2dk-dm+2fs-fv)^2}{4(2cs-cv)} + \frac{1}{2}\pi(m+v)\right) \left. \right) \Bigg/; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0807.01

$$\int \sin^m(dz) \sin^v(\sqrt{z}c + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$\frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin(\frac{\pi m}{2} + d(m-2k)z)}{m-2k} + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi} (v-2k) \cos\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}}\right) + \right.$$

$$c\sqrt{2\pi} (v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) +$$

$$2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + f(v-2k)z + c(v-2k)\sqrt{z}\right) \left. \right) \Bigg) +$$

$$\begin{aligned}
 & 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \sqrt{2\pi} (2cs - cv) \cos \left( \frac{1}{2} \pi (v-m) - \frac{(cv - 2cs)^2}{4(2dk - dm - 2fs + fv)} \right) \right) \right. \\
 & \quad C \left( \frac{-2cs + cv + 2(2dk - dm - 2fs + fv) \sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm - 2fs + fv}} \right) + \sqrt{2\pi} (cv - 2cs) \\
 & \quad S \left( \frac{-2cs + cv + 2(2dk - dm - 2fs + fv) \sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm - 2fs + fv}} \right) \sin \left( \frac{1}{2} \pi (v-m) - \frac{(cv - 2cs)^2}{4(2dk - dm - 2fs + fv)} \right) + \\
 & \quad \left. 2\sqrt{2dk - dm - 2fs + fv} \sin \left( \frac{1}{2} \pi (v-m) + (2dk - dm - 2fs + fv)z + (cv - 2cs) \sqrt{z} \right) \right) / \\
 & (2dk - dm - 2fs + fv)^{3/2} + \left( \sqrt{2\pi} (cv - 2cs) \cos \left( \frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + \frac{1}{2} \pi (m+v) \right) \right. \\
 & \quad C \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv) \sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) - \sqrt{2\pi} (2cs - cv) \\
 & \quad S \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv) \sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) \sin \left( \frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + \frac{1}{2} \pi (m+v) \right) - \\
 & \quad \left. 2\sqrt{2dk - dm + 2fs - fv} \sin \left( \frac{1}{2} \pi (m+v) - (2dk - dm + 2fs - fv)z - (2cs - cv) \sqrt{z} \right) \right) / \\
 & (2dk - dm + 2fs - fv)^{3/2} \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(dz + e) \sin^v(cz' + fz)$

01.06.21.0808.01

$$\int \sin^m(dz + e) \sin^v(cz^2 + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos \left( \frac{\pi v}{2} - \frac{f^2(v-2k)}{4c} \right) C \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) - \right.$$

$$\left. S \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) \sin \left( \frac{\pi v}{2} - \frac{f^2(v-2k)}{4c} \right) \right) +$$

$$\frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin \left( e(2k-m) + 2dkz - \frac{1}{2}m(2dz + \pi) \right)}{2k-m} + 2^{-m-v+\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos \left( -\frac{(2dk-dm-2fs+fv)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v) \right) \right.$$

$$C \left( \frac{2dk-dm-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}} \right) - S \left( \frac{2dk-dm-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}} \right) \right.$$

$$\left. \sin \left( -\frac{(2dk-dm-2fs+fv)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v) \right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos \left( -\frac{(2dk-dm+2fs-fv)^2}{4(2cs-cv)} + e(2k-m) - \frac{1}{2}\pi(m+v) \right) \right.$$

$$C \left( \frac{2dk-dm+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}} \right) - S \left( \frac{2dk-dm+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}} \right) \left. \right) \left. \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0809.01

$$\int \sin^m(e + dz) \sin^v(\sqrt{z}c + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi} (v-2k) \cos \left( \frac{\pi v}{2} - \frac{c^2(v-2k)}{4f} \right) C \left( \frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}} \right) + \right.$$

$$c\sqrt{2\pi} (v-2k) S \left( \frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}} \right) \sin \left( \frac{\pi v}{2} - \frac{c^2(v-2k)}{4f} \right) +$$

$$\left. \left. 2\sqrt{f(v-2k)} \sin \left( \frac{\pi v}{2} + f(v-2k)z + c(v-2k)\sqrt{z} \right) \right) \right) +$$

$$\frac{2^{-m-v+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin \left( \frac{\pi m}{2} + e(m-2k) + d(m-2k)z \right)}{m-2k}}{d} + 2^{-m-v}$$

$$\begin{aligned}
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \sqrt{2\pi} (2cs - cv) \cos \left( -\frac{(cv - 2cs)^2}{4(2dk - dm - 2fs + fv)} + 2ek - em + \frac{1}{2}\pi(v-m) \right) \right. \right. \\
 & \quad \left. \left. C \left( \frac{-2cs + cv + 2(2dk - dm - 2fs + fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm - 2fs + fv}} \right) + \right. \right. \\
 & \quad \left. \left. \sqrt{2\pi} (cv - 2cs) S \left( \frac{-2cs + cv + 2(2dk - dm - 2fs + fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm - 2fs + fv}} \right) \right. \right. \\
 & \quad \left. \left. \sin \left( -\frac{(cv - 2cs)^2}{4(2dk - dm - 2fs + fv)} + 2ek - em + \frac{1}{2}\pi(v-m) \right) + 2\sqrt{2dk - dm - 2fs + fv} \right. \right. \\
 & \quad \left. \left. \sin \left( 2ek - em + \frac{1}{2}\pi(v-m) + (2dk - dm - 2fs + fv)z + (cv - 2cs)\sqrt{z} \right) \right) \right) / \\
 & \quad (2dk - dm - 2fs + fv)^{3/2} + \left( \sqrt{2\pi} (cv - 2cs) \cos \left( -\frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + \right. \right. \\
 & \quad \left. \left. 2ek - em - \frac{1}{2}\pi(m+v) \right) C \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) + \right. \\
 & \quad \left. \sqrt{2\pi} (2cs - cv) S \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) \sin \left( -\frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + \right. \right. \\
 & \quad \left. \left. 2ek - em - \frac{1}{2}\pi(m+v) \right) + 2\sqrt{2dk - dm + 2fs - fv} \sin \left( 2ek - em - \frac{1}{2}\pi(m+v) + \right. \right. \\
 & \quad \left. \left. (2dk - dm + 2fs - fv)z + (2cs - cv)\sqrt{z} \right) \right) / (2dk - dm + 2fs - fv)^{3/2} \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(bz^r) \sin^v(cz^r + fz)$

01.06.21.0810.01

$$\int \sin^m(bz^2) \sin^v(cz^2 + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m}}{\sqrt{b(m-2k)}} \binom{m}{k} \left( \cos\left(\frac{m\pi}{2}\right) C\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) - S\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) \sin\left(\frac{m\pi}{2}\right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \binom{v}{k} \left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} - \frac{f^2(v-2k)}{4c}\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) - \right.$$

$$\left. S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{f^2(v-2k)}{4c}\right) \right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \cos\left(\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + \frac{1}{2}\pi(m-v)\right) C\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) + \right.$$

$$\left. S\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) \sin\left(\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + \frac{1}{2}\pi(m-v)\right) \right) /$$

$$\left( \sqrt{2bk-bm-2cs+cv} \right) + \left( \cos\left(\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + \frac{1}{2}\pi(m+v)\right) \right.$$

$$\left. C\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) + S\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) \right.$$

$$\left. \sin\left(\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + \frac{1}{2}\pi(m+v)\right) \right) / \left( \sqrt{2bk-bm+2cs-cv} \right) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0811.01

$$\int \sin^m(b\sqrt{z}) \sin^v(\sqrt{z}c + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \binom{v}{k} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi}(v-2k) \cos\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) + \right.$$

$$\left. c\sqrt{2\pi}(v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) \right) +$$

$$2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + f(v-2k)z + c(v-2k)\sqrt{z}\right) \Bigg) + \frac{1}{b^2} \left( 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right.$$

$$\left. \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(m-2k)^2} \binom{m}{k} \left( (-1)^{k+m} \binom{m}{k} \left( \cos\left(\frac{m\pi}{2} - b(2k-m)\sqrt{z}\right) - b(2k-m)\sqrt{z} \sin\left(\frac{m\pi}{2} - b(2k-m)\sqrt{z}\right) \right) \right) \right) +$$

$$\begin{aligned}
 & 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \\
 & \left( \frac{1}{(fv-2fs)^{3/2}} \left[ \sqrt{2\pi} (-2bk+bm+2cs-cv) \cos \left( \frac{1}{2} \pi (v-m) - \frac{(2bk-bm-2cs+cv)^2}{4(fv-2fs)} \right) \right. \right. \\
 & \quad \left. \left. C \left( \frac{2bk-bm-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi} \sqrt{fv-2fs}} \right) + \sqrt{2\pi} (2bk-bm-2cs+cv) \right. \right. \\
 & \quad \left. \left. S \left( \frac{2bk-bm-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi} \sqrt{fv-2fs}} \right) \sin \left( \frac{1}{2} \pi (v-m) - \frac{(2bk-bm-2cs+cv)^2}{4(fv-2fs)} \right) + \right. \right. \\
 & \quad \left. \left. 2\sqrt{fv-2fs} \sin \left( \frac{1}{2} \pi (v-m) + (fv-2fs)z + (2bk-bm-2cs+cv)\sqrt{z} \right) \right] \right) + \\
 & \frac{1}{(2fs-fv)^{3/2}} \left[ \sqrt{2\pi} (-2bk+bm-2cs+cv) \cos \left( \frac{(2bk-bm+2cs-cv)^2}{4(2fs-fv)} + \frac{1}{2} \pi (m+v) \right) \right. \\
 & \quad \left. C \left( \frac{2bk-bm+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2fs-fv}} \right) - \sqrt{2\pi} (2bk-bm+2cs-cv) \right. \\
 & \quad \left. S \left( \frac{2bk-bm+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2fs-fv}} \right) \sin \left( \frac{(2bk-bm+2cs-cv)^2}{4(2fs-fv)} + \frac{1}{2} \pi (m+v) \right) - \right. \\
 & \quad \left. \left. 2\sqrt{2fs-fv} \sin \left( \frac{1}{2} \pi (m+v) - (2fs-fv)z - (2bk-bm+2cs-cv)\sqrt{z} \right) \right] \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(bz^r + e) \sin^v(cz^r + fz)$

01.06.21.0812.01

$$\int \sin^m(bz^2 + e) \sin^v(cz^2 + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2)(1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{\sqrt{b(m-2k)}} \right) \left( (-1)^{k+m} \binom{m}{k} \left( \cos\left(\frac{\pi m}{2} + e(m-2k)\right) C\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) - S\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) \sin\left(\frac{\pi m}{2} + e(m-2k)\right) \right) \right) \left( (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} - \frac{f^2(v-2k)}{4c}\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) - S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{f^2(v-2k)}{4c}\right) \right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \cos\left(-\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + e(2k-m) - \frac{1}{2}\pi(m-v)\right) C\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) - S\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) \sin\left(-\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + e(2k-m) - \frac{1}{2}\pi(m-v)\right) \right) / (\sqrt{2bk-bm-2cs+cv}) + \left( \cos\left(-\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + e(2k-m) - \frac{1}{2}\pi(m+v)\right) C\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) - S\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) \sin\left(-\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + e(2k-m) - \frac{1}{2}\pi(m+v)\right) \right) / (\sqrt{2bk-bm+2cs-cv}) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0813.01

$$\int \sin^m(\sqrt{z}b + e) \sin^v(\sqrt{z}c + fz) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2)(1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi}(v-2k) \cos\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) + c\sqrt{2\pi}(v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) \right) +$$



$$\begin{aligned}
 & \left. \left. \left. 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + f(v-2k)z + c(v-2k)\sqrt{z}\right)\right)\right)\right) + \\
 & \frac{1}{b^2} \left( 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(m-2k)^2} \left( (-1)^{k+m} \binom{m}{k} \left( \cos\left(2ek - em + b(2k-m)\sqrt{z} - \frac{m\pi}{2}\right) + \right. \right. \right. \\
 & \left. \left. \left. b(2k-m)\sqrt{z} \sin\left(2ek - em + b(2k-m)\sqrt{z} - \frac{m\pi}{2}\right)\right)\right)\right) + 2^{-m-v} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(fv-2fs)^{3/2}} \left( \sqrt{2\pi} (-2bk + bm + 2cs - cv) \cos\left(-\frac{(2bk - bm - 2cs + cv)^2}{4(fv-2fs)} + \right. \right. \right. \\
 & \left. \left. \left. 2ek - em + \frac{1}{2}\pi(v-m) \right) C\left(\frac{2bk - bm - 2cs + cv + 2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) + \right. \right. \\
 & \left. \left. \sqrt{2\pi} (2bk - bm - 2cs + cv) S\left(\frac{2bk - bm - 2cs + cv + 2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) \right. \right. \\
 & \left. \left. \sin\left(-\frac{(2bk - bm - 2cs + cv)^2}{4(fv-2fs)} + 2ek - em + \frac{1}{2}\pi(v-m)\right) + \right. \right. \\
 & \left. \left. \left. 2\sqrt{fv-2fs} \sin\left(2ek - em + \frac{1}{2}\pi(v-m) + (fv-2fs)z + (2bk - bm - 2cs + cv)\sqrt{z}\right)\right)\right)\right) + \\
 & \frac{1}{(2fs-fv)^{3/2}} \left( \sqrt{2\pi} (-2bk + bm - 2cs + cv) \cos\left(-\frac{(2bk - bm + 2cs - cv)^2}{4(2fs-fv)} + 2ek - \right. \right. \\
 & \left. \left. em - \frac{1}{2}\pi(m+v) \right) C\left(\frac{2bk - bm + 2cs - cv + 2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) + \right. \\
 & \left. \sqrt{2\pi} (2bk - bm + 2cs - cv) S\left(\frac{2bk - bm + 2cs - cv + 2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) \right. \\
 & \left. \sin\left(-\frac{(2bk - bm + 2cs - cv)^2}{4(2fs-fv)} + 2ek - em - \frac{1}{2}\pi(m+v)\right) + 2\sqrt{2fs-fv} \right. \\
 & \left. \left. \left. \sin\left(2ek - em - \frac{1}{2}\pi(m+v) + (2fs-fv)z + (2bk - bm + 2cs - cv)\sqrt{z}\right)\right)\right)\right) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(bz^r + dz) \sin^v(cz^r + fz)$

01.06.21.0814.01

$$\begin{aligned}
 \int \sin^m(bz^2 + dz) \sin^v(cz^2 + fz) dz &= 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + \\
 &2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{\sqrt{b(m-2k)}} \left( (-1)^{k+m} \binom{m}{k} \left( \cos \left( \frac{d^2(m-2k)}{4b} - \frac{m\pi}{2} \right) C \left( \frac{d(m-2k) + 2bz(m-2k)}{\sqrt{b(m-2k)} \sqrt{2\pi}} \right) + \right. \right. \\
 &\left. \left. S \left( \frac{d(m-2k) + 2bz(m-2k)}{\sqrt{b(m-2k)} \sqrt{2\pi}} \right) \sin \left( \frac{d^2(m-2k)}{4b} - \frac{m\pi}{2} \right) \right) \right) (1 - v \bmod 2) + \\
 &2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos \left( \frac{\pi v}{2} - \frac{f^2(v-2k)}{4c} \right) C \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) - \right. \\
 &\left. S \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) \sin \left( \frac{\pi v}{2} - \frac{f^2(v-2k)}{4c} \right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \\
 &\left( \cos \left( \frac{(2dk - dm - 2fs + fv)^2}{4(2bk - bm - 2cs + cv)} + \frac{1}{2} \pi(m-v) \right) C \left( \frac{2dk - dm - 2fs + fv + 2(2bk - bm - 2cs + cv)z}{\sqrt{2\pi} \sqrt{2bk - bm - 2cs + cv}} \right) + \right. \\
 &\left. S \left( \frac{2dk - dm - 2fs + fv + 2(2bk - bm - 2cs + cv)z}{\sqrt{2\pi} \sqrt{2bk - bm - 2cs + cv}} \right) \right. \\
 &\left. \sin \left( \frac{(2dk - dm - 2fs + fv)^2}{4(2bk - bm - 2cs + cv)} + \frac{1}{2} \pi(m-v) \right) \right) / \left( \sqrt{2bk - bm - 2cs + cv} \right) + \\
 &\left( \cos \left( \frac{(2dk - dm + 2fs - fv)^2}{4(2bk - bm + 2cs - cv)} + \frac{1}{2} \pi(m+v) \right) C \left( \frac{2dk - dm + 2fs - fv + 2(2bk - bm + 2cs - cv)z}{\sqrt{2\pi} \sqrt{2bk - bm + 2cs - cv}} \right) + \right. \\
 &\left. S \left( \frac{2dk - dm + 2fs - fv + 2(2bk - bm + 2cs - cv)z}{\sqrt{2\pi} \sqrt{2bk - bm + 2cs - cv}} \right) \right. \\
 &\left. \sin \left( \frac{(2dk - dm + 2fs - fv)^2}{4(2bk - bm + 2cs - cv)} + \frac{1}{2} \pi(m+v) \right) \right) / \left( \sqrt{2bk - bm + 2cs - cv} \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0815.01

$$\begin{aligned}
 \int \sin^m(\sqrt{z}b + dz) \sin^v(\sqrt{z}c + fz) dz &= 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \binom{v}{\frac{v}{2}} \\
 &\left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(d(m-2k))^{3/2}} \left( (-1)^{k+m} \binom{m}{k} \left( -b(m-2k) \sqrt{2\pi} \cos \left( \frac{b^2(m-2k)}{4d} - \frac{m\pi}{2} \right) C \left( \frac{b(m-2k) + 2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)} \sqrt{2\pi}} \right) - \right. \right. \\
 &\left. \left. b(m-2k) \sqrt{2\pi} S \left( \frac{b(m-2k) + 2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)} \sqrt{2\pi}} \right) \sin \left( \frac{b^2(m-2k)}{4d} - \frac{m\pi}{2} \right) + \right. \right. \\
 &\left. \left. 2\sqrt{d(m-2k)} \sin \left( \frac{\pi m}{2} + d(m-2k)z + b(m-2k)\sqrt{z} \right) \right) \right) (1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)
 \end{aligned}$$

$$\begin{aligned}
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi}(v-2k) \cos\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) + \right. \right. \\
 & \quad c\sqrt{2\pi}(v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) \sin\left(\frac{\pi v}{2} - \frac{c^2(v-2k)}{4f}\right) + \\
 & \quad \left. \left. 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + f(v-2k)z + c(v-2k)\sqrt{z}\right) \right) \right) + \\
 & 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \sqrt{2\pi}(-2bk+bm+2cs-cv) \cos\left(\frac{1}{2}\pi(v-m) - \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(2bk-bm-2cs+cv)^2}{4(2dk-dm-2fs+fv)} \right) C\left(\frac{2bk-bm-2cs+cv+2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right) + \right. \right. \\
 & \quad \left. \left. \sqrt{2\pi}(2bk-bm-2cs+cv) S\left(\frac{2bk-bm-2cs+cv+2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right) \right. \right. \\
 & \quad \left. \left. \sin\left(\frac{1}{2}\pi(v-m) - \frac{(2bk-bm-2cs+cv)^2}{4(2dk-dm-2fs+fv)}\right) + 2\sqrt{2dk-dm-2fs+fv} \sin\left(\frac{1}{2}\pi(v-m) + \right. \right. \right. \\
 & \quad \left. \left. \left. (2dk-dm-2fs+fv)z + (2bk-bm-2cs+cv)\sqrt{z}\right) \right) \right) / (2dk-dm-2fs+fv)^{3/2} + \\
 & \left( \sqrt{2\pi}(-2bk+bm-2cs+cv) \cos\left(\frac{(2bk-bm+2cs-cv)^2}{4(2dk-dm+2fs-fv)} + \frac{1}{2}\pi(m+v)\right) \right. \\
 & \quad C\left(\frac{2bk-bm+2cs-cv+2(2dk-dm+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm+2fs-fv}}\right) - \sqrt{2\pi}(2bk-bm+2cs-cv) \\
 & \quad S\left(\frac{2bk-bm+2cs-cv+2(2dk-dm+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm+2fs-fv}}\right) \sin\left(\frac{(2bk-bm+2cs-cv)^2}{4(2dk-dm+2fs-fv)} + \right. \\
 & \quad \left. \frac{1}{2}\pi(m+v)\right) - 2\sqrt{2dk-dm+2fs-fv} \sin\left(\frac{1}{2}\pi(m+v) - (2dk-dm+2fs-fv)z - \right. \\
 & \quad \left. \left. (2bk-bm+2cs-cv)\sqrt{z}\right) \right) / (2dk-dm+2fs-fv)^{3/2} \Bigg); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(dz) \sin^v(cz' + fz + g)$

01.06.21.0816.01

$$\int \sin^m(dz) \sin^v(cz^2 + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$\frac{2^{-m-v+1}}{d} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(2dkz - \frac{1}{2}m(2dz + \pi)\right)}{2k - m} + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}}\right) - \right.$$

$$\left. S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}}\right) \sin\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos\left(\frac{(2dk - dm - 2fs + fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) \right.$$

$$C\left(\frac{2dk - dm - 2fs + fv + 2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right) + S\left(\frac{2dk - dm - 2fs + fv + 2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}}\right)$$

$$\left. \sin\left(\frac{(2dk - dm - 2fs + fv)^2}{4(cv-2cs)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos\left(-\frac{(2dk - dm + 2fs - fv)^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right.$$

$$C\left(\frac{2dk - dm + 2fs - fv + 2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right) - S\left(\frac{2dk - dm + 2fs - fv + 2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}}\right)$$

$$\left. \sin\left(-\frac{(2dk - dm + 2fs - fv)^2}{4(2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0817.01

$$\int \sin^m(dz) \sin^v(\sqrt{z}c + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$\frac{2^{-m-v+1} (1 - v \bmod 2)}{d} \binom{v}{\frac{v}{2}} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin\left(\frac{\pi m}{2} + d(m-2k)z\right)}{m-2k} + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}}$$

$$\left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi} (v-2k) \cos\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}}\right) + \right.$$

$$c\sqrt{2\pi} (v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}}\right) \sin\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) +$$

$$\left. \left. 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + g(v-2k) + f(v-2k)z + c(v-2k)\sqrt{z}\right) \right) \right) +$$

$$\begin{aligned}
 & 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \sqrt{2\pi} (cv - 2cs) \cos \left( -\frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + 2gs - \right. \right. \right. \\
 & \left. \left. \left. gv - \frac{1}{2}\pi(m+v) \right) C \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) + \right. \\
 & \left. \sqrt{2\pi} (2cs - cv) S \left( \frac{2cs - cv + 2(2dk - dm + 2fs - fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm + 2fs - fv}} \right) \right. \\
 & \left. \sin \left( -\frac{(2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + 2gs - gv - \frac{1}{2}\pi(m+v) \right) + 2\sqrt{2dk - dm + 2fs - fv} \right. \\
 & \left. \sin \left( 2gs - gv - \frac{1}{2}\pi(m+v) + (2dk - dm + 2fs - fv)z + (2cs - cv)\sqrt{z} \right) \right) \Bigg/ \\
 & (2dk - dm + 2fs - fv)^{3/2} + \left( \sqrt{2\pi} (2cs - cv) \cos \left( \frac{(cv - 2cs)^2}{4(2dk - dm - 2fs + fv)} + 2gs - \right. \right. \\
 & \left. \left. gv - \frac{1}{2}\pi(v-m) \right) C \left( \frac{-2cs + cv + 2(2dk - dm - 2fs + fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm - 2fs + fv}} \right) - \right. \\
 & \left. \sqrt{2\pi} (cv - 2cs) S \left( \frac{-2cs + cv + 2(2dk - dm - 2fs + fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2dk - dm - 2fs + fv}} \right) \sin \left( \frac{(cv - 2cs)^2}{4(2dk - dm - 2fs + fv)} + \right. \right. \\
 & \left. \left. 2gs - gv - \frac{1}{2}\pi(v-m) \right) - 2\sqrt{2dk - dm - 2fs + fv} \sin \left( 2gs - gv - \frac{1}{2}\pi(v-m) - \right. \right. \\
 & \left. \left. (2dk - dm - 2fs + fv)z - (cv - 2cs)\sqrt{z} \right) \right) \Bigg/ (2dk - dm - 2fs + fv)^{3/2} \Bigg/ ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(dz + e) \sin^v(cz' + fz + g)$

01.06.21.0818.01

$$\int \sin^m(dz + e) \sin^v(cz^2 + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left( \cos \left( -\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k) \right) \right. \right.$$

$$\left. \left. C \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) - S \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) \sin \left( -\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k) \right) \right) \right) +$$

$$\frac{2^{-m-v+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin \left( e(2k-m) + 2dkz - \frac{1}{2}m(2dz+\pi) \right)}{2k-m}}{d} + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{\sqrt{cv-2cs}} \left( \cos \left( -\frac{(2dk-dm-2fs+fv)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v) - g(2s-v) \right) \right. \right.$$

$$C \left( \frac{2dk-dm-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}} \right) - S \left( \frac{2dk-dm-2fs+fv+2(cv-2cs)z}{\sqrt{2\pi} \sqrt{cv-2cs}} \right)$$

$$\left. \left. \sin \left( -\frac{(2dk-dm-2fs+fv)^2}{4(cv-2cs)} + e(2k-m) - \frac{1}{2}\pi(m-v) - g(2s-v) \right) \right) \right) +$$

$$\frac{1}{\sqrt{2cs-cv}} \left( \cos \left( -\frac{(2dk-dm+2fs-fv)^2}{4(2cs-cv)} + e(2k-m) + g(2s-v) - \frac{1}{2}\pi(m+v) \right) \right.$$

$$C \left( \frac{2dk-dm+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}} \right) - S \left( \frac{2dk-dm+2fs-fv+2(2cs-cv)z}{\sqrt{2\pi} \sqrt{2cs-cv}} \right)$$

$$\left. \left. \sin \left( -\frac{(2dk-dm+2fs-fv)^2}{4(2cs-cv)} + e(2k-m) + g(2s-v) - \frac{1}{2}\pi(m+v) \right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0819.01

$$\int \sin^m(dz + e) \sin^v(\sqrt{z}c + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$\frac{2^{-m-v+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m} \binom{m}{k} \sin \left( \frac{\pi m}{2} + e(m-2k) + d(m-2k)z \right)}{m-2k}}{d} +$$

$$2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi} (v-2k) \cos \left( -\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k) \right) \right. \right.$$

$$C \left( \frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}} \right) + c\sqrt{2\pi} (v-2k) S \left( \frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}} \right) \sin \left( -\frac{(v-2k)c^2}{4f} +$$

$$\begin{aligned}
 & \left. \frac{\pi v}{2} + g(v-2k) \right) + 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + g(v-2k) + f(v-2k)z + c(v-2k)\sqrt{z}\right) \Bigg) + \\
 & 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \Bigg( \left( \sqrt{2\pi} (2cs - cv) \cos\left(-\frac{(cv-2cs)^2}{4(2dk-dm-2fs+fv)} + 2ek - em - \right. \right. \right. \\
 & \left. \left. \left. 2gs + gv + \frac{1}{2}\pi(v-m)\right) C\left(\frac{-2cs + cv + 2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right) + \sqrt{2\pi}(cv-2cs) \right. \right. \\
 & \left. \left. S\left(\frac{-2cs + cv + 2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right) \sin\left(-\frac{(cv-2cs)^2}{4(2dk-dm-2fs+fv)} + 2ek - \right. \right. \right. \\
 & \left. \left. \left. em - 2gs + gv + \frac{1}{2}\pi(v-m)\right) + 2\sqrt{2dk-dm-2fs+fv} \sin\left(2ek - em - 2gs + gv + \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{2}\pi(v-m) + (2dk-dm-2fs+fv)z + (cv-2cs)\sqrt{z}\right) \right) \Bigg) / (2dk-dm-2fs+fv)^{3/2} + \\
 & \left( \sqrt{2\pi}(cv-2cs) \cos\left(-\frac{(2cs-cv)^2}{4(2dk-dm+2fs-fv)} + 2ek - em + 2gs - gv - \frac{1}{2}\pi(m+v)\right) \right. \\
 & \left. C\left(\frac{2cs - cv + 2(2dk-dm+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm+2fs-fv}}\right) + \sqrt{2\pi}(2cs-cv) \right. \\
 & \left. S\left(\frac{2cs - cv + 2(2dk-dm+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm+2fs-fv}}\right) \sin\left(-\frac{(2cs-cv)^2}{4(2dk-dm+2fs-fv)} + 2ek - em + 2g \right. \right. \\
 & \left. \left. s - gv - \frac{1}{2}\pi(m+v)\right) + 2\sqrt{2dk-dm+2fs-fv} \sin\left(2ek - em + 2gs - gv - \frac{1}{2}\pi(m+v) + \right. \right. \\
 & \left. \left. (2dk-dm+2fs-fv)z + (2cs-cv)\sqrt{z}\right) \right) \Bigg) / (2dk-dm+2fs-fv)^{3/2} \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $\sin^m(bz^r) \sin^v(cz^r + fz + g)$**

01.06.21.0820.01

$$\int \sin^m(bz^2) \sin^v(cz^2 + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{(-1)^{k+m}}{\sqrt{b(m-2k)}} \binom{m}{k} \left( \cos\left(\frac{m\pi}{2}\right) C\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) - S\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) \sin\left(\frac{m\pi}{2}\right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \binom{v}{k} \left( (-1)^{k+v} \left( \cos\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) - S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) \sin\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) \right) \right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \cos\left(\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) C\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) + S\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) \sin\left(\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) \right) / \left( \sqrt{2bk-bm-2cs+cv} \right) +$$

$$\left( \cos\left(-\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) C\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) - S\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) \sin\left(-\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) \right) / \left( \sqrt{2bk-bm+2cs-cv} \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0821.01

$$\int \sin^m(b\sqrt{z}) \sin^v(\sqrt{z}c + fz + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}}$$

$$\left( (-1)^{k+v} \binom{v}{k} \left( -c\sqrt{2\pi}(v-2k) \cos\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) + c\sqrt{2\pi}(v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) \sin\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) + \right.$$



$$\begin{aligned}
 & 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + g(v-2k) + f(v-2k)z + c(v-2k)\sqrt{z}\right) \Bigg) + \frac{1}{b^2} \left( 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \right. \\
 & \left. \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(m-2k)^2} \left( (-1)^{k+m} \binom{m}{k} \left( \cos\left(\frac{m\pi}{2} - b(2k-m)\sqrt{z}\right) - b(2k-m)\sqrt{z} \sin\left(\frac{m\pi}{2} - b(2k-m)\sqrt{z}\right) \right) \right) \right) + 2^{-m-v} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(2fs-fv)^{3/2}} \left( \sqrt{2\pi} (-2bk+bm-2cs+cv) \cos\left(-\frac{(2bk-bm+2cs-cv)^2}{4(2fs-fv)} + \right. \right. \right. \\
 & \left. \left. \left. 2gs-gv - \frac{1}{2}\pi(m+v) \right) C\left(\frac{2bk-bm+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) + \right. \right. \\
 & \left. \left. \sqrt{2\pi} (2bk-bm+2cs-cv) S\left(\frac{2bk-bm+2cs-cv+2(2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2fs-fv}}\right) \right. \right. \\
 & \left. \left. \sin\left(-\frac{(2bk-bm+2cs-cv)^2}{4(2fs-fv)} + 2gs-gv - \frac{1}{2}\pi(m+v)\right) + \right. \right. \\
 & \left. \left. 2\sqrt{2fs-fv} \sin\left(2gs-gv - \frac{1}{2}\pi(m+v) + (2fs-fv)z + (2bk-bm+2cs-cv)\sqrt{z}\right) \right) \right) + \\
 & \frac{1}{(fv-2fs)^{3/2}} \left( \sqrt{2\pi} (-2bk+bm+2cs-cv) \cos\left(\frac{(2bk-bm-2cs+cv)^2}{4(fv-2fs)} + 2gs - \right. \right. \\
 & \left. \left. gv - \frac{1}{2}\pi(v-m) \right) C\left(\frac{2bk-bm-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) - \right. \\
 & \left. \sqrt{2\pi} (2bk-bm-2cs+cv) S\left(\frac{2bk-bm-2cs+cv+2(fv-2fs)\sqrt{z}}{\sqrt{2\pi}\sqrt{fv-2fs}}\right) \right. \\
 & \left. \sin\left(\frac{(2bk-bm-2cs+cv)^2}{4(fv-2fs)} + 2gs-gv - \frac{1}{2}\pi(v-m)\right) - 2\sqrt{fv-2fs} \right. \\
 & \left. \left. \sin\left(2gs-gv - \frac{1}{2}\pi(v-m) - (fv-2fs)z - (2bk-bm-2cs+cv)\sqrt{z}\right) \right) \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $\sin^m(bz^r + e) \sin^v(cz^r + fz + g)$

01.06.21.0822.01

$$\int \sin^m(bz^2 + e) \sin^v(cz^2 + fz + g) dz = 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{\sqrt{b(m-2k)}} \left( (-1)^{k+m} \binom{m}{k} \left[ \cos\left(\frac{\pi m}{2} + e(m-2k)\right) C\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) - \right. \right.$$

$$\left. \left. S\left(\frac{b(m-2k)\sqrt{\frac{2}{\pi}}z}{\sqrt{b(m-2k)}}\right) \sin\left(\frac{\pi m}{2} + e(m-2k)\right) \right] \right) \right) (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left( (-1)^{k+v} \binom{v}{k} \left[ \cos\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) - \right. \right.$$

$$\left. \left. S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi}\sqrt{c(v-2k)}}\right) \sin\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) \right] \right) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left[ \cos\left(-\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + e(2k-m) - \frac{1}{2}\pi(m-v) - g(2s-v)\right) \right. \right.$$

$$C\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) - S\left(\frac{-2fs+fv+2(2bk-bm-2cs+cv)z}{\sqrt{2\pi}\sqrt{2bk-bm-2cs+cv}}\right) \left. \right]$$

$$\sin\left(-\frac{(fv-2fs)^2}{4(2bk-bm-2cs+cv)} + e(2k-m) - \frac{1}{2}\pi(m-v) - g(2s-v)\right) \Big/$$

$$\left( \sqrt{2bk-bm-2cs+cv} \right) + \left[ \cos\left(-\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + e(2k-m) + \right. \right.$$

$$\left. \left. g(2s-v) - \frac{1}{2}\pi(m+v) \right) C\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) - \right.$$

$$\left. \left. S\left(\frac{2fs-fv+2(2bk-bm+2cs-cv)z}{\sqrt{2\pi}\sqrt{2bk-bm+2cs-cv}}\right) \sin\left(-\frac{(2fs-fv)^2}{4(2bk-bm+2cs-cv)} + e(2k-m) + \right. \right.$$

$$\left. \left. g(2s-v) - \frac{1}{2}\pi(m+v) \right) \right] \Big/ \left( \sqrt{2bk-bm+2cs-cv} \right) \Big/ ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0823.01

$$\int \sin^m(\sqrt{z}b + e) \sin^v(\sqrt{z}c + fz + g) dz =$$

$$2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}}$$

$$\begin{aligned}
 & \left( (-1)^{k+v} \binom{v}{k} \left( -c \sqrt{2\pi} (v-2k) \cos \left( -\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k) \right) C \left( \frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}} \right) + \right. \right. \\
 & \quad c \sqrt{2\pi} (v-2k) S \left( \frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi} \sqrt{f(v-2k)}} \right) \sin \left( -\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k) \right) + \\
 & \quad \left. \left. 2 \sqrt{f(v-2k)} \sin \left( \frac{\pi v}{2} + g(v-2k) + f(v-2k)z + c(v-2k)\sqrt{z} \right) \right) \right) + \\
 & \frac{1}{b^2} \left( 2^{-m-v+2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(m-2k)^2} \left( (-1)^{k+m} \binom{m}{k} \left( \cos \left( 2ek - em + b(2k-m)\sqrt{z} - \frac{m\pi}{2} \right) + \right. \right. \right. \\
 & \quad \left. \left. \left. b(2k-m)\sqrt{z} \sin \left( 2ek - em + b(2k-m)\sqrt{z} - \frac{m\pi}{2} \right) \right) \right) \right) + 2^{-m-v} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \frac{1}{(fv-2fs)^{3/2}} \left( \sqrt{2\pi} (-2bk + bm + 2cs - cv) \cos \left( -\frac{(2bk - bm - 2cs + cv)^2}{4(fv-2fs)} + \right. \right. \right. \\
 & \quad \left. \left. \left. 2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m) \right) C \left( \frac{2bk - bm - 2cs + cv + 2(fv-2fs)\sqrt{z}}{\sqrt{2\pi} \sqrt{fv-2fs}} \right) + \right. \\
 & \quad \left. \sqrt{2\pi} (2bk - bm - 2cs + cv) S \left( \frac{2bk - bm - 2cs + cv + 2(fv-2fs)\sqrt{z}}{\sqrt{2\pi} \sqrt{fv-2fs}} \right) \right. \\
 & \quad \left. \sin \left( -\frac{(2bk - bm - 2cs + cv)^2}{4(fv-2fs)} + 2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m) \right) + 2\sqrt{fv-2fs} \right. \\
 & \quad \left. \left. \sin \left( 2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m) + (fv-2fs)z + (2bk - bm - 2cs + cv)\sqrt{z} \right) \right) \right) + \\
 & \frac{1}{(2fs-fv)^{3/2}} \left( \sqrt{2\pi} (-2bk + bm - 2cs + cv) \cos \left( -\frac{(2bk - bm + 2cs - cv)^2}{4(2fs-fv)} + 2ek - em + 2gs - gv - \right. \right. \\
 & \quad \left. \left. \frac{1}{2}\pi(m+v) \right) C \left( \frac{2bk - bm + 2cs - cv + 2(2fs-fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2fs-fv}} \right) + \sqrt{2\pi} (2bk - bm + 2cs - cv) \right. \\
 & \quad \left. S \left( \frac{2bk - bm + 2cs - cv + 2(2fs-fv)\sqrt{z}}{\sqrt{2\pi} \sqrt{2fs-fv}} \right) \sin \left( -\frac{(2bk - bm + 2cs - cv)^2}{4(2fs-fv)} + \right. \right. \\
 & \quad \left. \left. 2ek - em + 2gs - gv - \frac{1}{2}\pi(m+v) \right) + 2\sqrt{2fs-fv} \sin \left( 2ek - em + 2gs - gv - \right. \right.
 \end{aligned}$$

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### Involving $\sin^m(bz^r + dz) \sin^v(cz^r + fz + g)$

01.06.21.0824.01

$$\int \sin^m(bz^2 + dz) \sin^v(cz^2 + fz + g) dz = 2^{-m-v} z \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) (1 - m \bmod 2) (1 - v \bmod 2) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \left(\frac{v}{2}\right) \left(\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{\sqrt{b(m-2k)}} (-1)^{k+m} \binom{m}{k} \left(\cos\left(\frac{d^2(m-2k)}{4b} - \frac{m\pi}{2}\right) C\left(\frac{d(m-2k) + 2bz(m-2k)}{\sqrt{b(m-2k)} \sqrt{2\pi}}\right) + S\left(\frac{d(m-2k) + 2bz(m-2k)}{\sqrt{b(m-2k)} \sqrt{2\pi}}\right) \sin\left(\frac{d^2(m-2k)}{4b} - \frac{m\pi}{2}\right)\right)\right) (1 - v \bmod 2) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \left(\frac{m}{2}\right) (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} \left((-1)^{k+v} \binom{v}{k} \left(\cos\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}}\right) - S\left(\frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}}\right) \sin\left(-\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k)\right)\right)\right) +$$

$$2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left(\cos\left(\frac{(2dk - dm - 2fs + fv)^2}{4(2bk - bm - 2cs + cv)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right) C\left(\frac{2dk - dm - 2fs + fv + 2(2bk - bm - 2cs + cv)z}{\sqrt{2\pi} \sqrt{2bk - bm - 2cs + cv}}\right) + S\left(\frac{2dk - dm - 2fs + fv + 2(2bk - bm - 2cs + cv)z}{\sqrt{2\pi} \sqrt{2bk - bm - 2cs + cv}}\right) \sin\left(\frac{(2dk - dm - 2fs + fv)^2}{4(2bk - bm - 2cs + cv)} + \frac{1}{2}\pi(m-v) + g(2s-v)\right)\right) / \left(\sqrt{2bk - bm - 2cs + cv}\right) + \left(\cos\left(-\frac{(2dk - dm + 2fs - fv)^2}{4(2bk - bm + 2cs - cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right) C\left(\frac{2dk - dm + 2fs - fv + 2(2bk - bm + 2cs - cv)z}{\sqrt{2\pi} \sqrt{2bk - bm + 2cs - cv}}\right) - S\left(\frac{2dk - dm + 2fs - fv + 2(2bk - bm + 2cs - cv)z}{\sqrt{2\pi} \sqrt{2bk - bm + 2cs - cv}}\right) \sin\left(-\frac{(2dk - dm + 2fs - fv)^2}{4(2bk - bm + 2cs - cv)} + g(2s-v) - \frac{1}{2}\pi(m+v)\right)\right) / \left(\sqrt{2bk - bm + 2cs - cv}\right) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.0825.01

$$\int \sin^m(\sqrt{z}bz + dz) \sin^v(\sqrt{z}cz + fz + g) dz = 2^{-m-v} z \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \left(\frac{v}{2}\right)$$

$$\left(\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(d(m-2k))^{3/2}} (-1)^{k+m} \binom{m}{k} \left(-b(m-2k) \sqrt{2\pi} \cos\left(\frac{b^2(m-2k)}{4d} - \frac{m\pi}{2}\right) C\left(\frac{b(m-2k) + 2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)} \sqrt{2\pi}}\right) - S\left(\frac{b(m-2k) + 2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)} \sqrt{2\pi}}\right) \sin\left(\frac{b^2(m-2k)}{4d} - \frac{m\pi}{2}\right)\right)\right)$$

$$\begin{aligned}
 & b(m-2k)\sqrt{2\pi} S\left(\frac{b(m-2k)+2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)}\sqrt{2\pi}}\right)\sin\left(\frac{b^2(m-2k)}{4d}-\frac{m\pi}{2}\right)+ \\
 & \left. 2\sqrt{d(m-2k)}\sin\left(\frac{\pi m}{2}+d(m-2k)z+b(m-2k)\sqrt{z}\right)\right) \Bigg) \\
 & (1-v \bmod 2)+2^{-m-v}\binom{m}{\frac{m}{2}}(1-m \bmod 2)\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}}\left((-1)^{k+v}\binom{v}{k}\right. \\
 & \left. \left(-c\sqrt{2\pi}(v-2k)\cos\left(-\frac{(v-2k)c^2}{4f}+\frac{\pi v}{2}+g(v-2k)\right)C\left(\frac{c(v-2k)+2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right)+\right. \right. \\
 & \left. \left. c\sqrt{2\pi}(v-2k)S\left(\frac{c(v-2k)+2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right)\sin\left(-\frac{(v-2k)c^2}{4f}+\frac{\pi v}{2}+g(v-2k)\right)+\right. \right. \\
 & \left. \left. 2\sqrt{f(v-2k)}\sin\left(\frac{\pi v}{2}+g(v-2k)+f(v-2k)z+c(v-2k)\sqrt{z}\right)\right)\right) + \\
 & 2^{-m-v}\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m}\binom{m}{k}\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v}\binom{v}{s}\left(\left(\sqrt{2\pi}(-2bk+bm-2cs+cv)\cos\left(-\frac{(2bk-bm+2cs-cv)^2}{4(2dk-dm+2fs-fv)}\right)+\right. \right. \\
 & \left. \left. 2gs-gv-\frac{1}{2}\pi(m+v)\right)C\left(\frac{2bk-bm+2cs-cv+2(2dk-dm+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm+2fs-fv}}\right)+\right. \\
 & \left. \sqrt{2\pi}(2bk-bm+2cs-cv)S\left(\frac{2bk-bm+2cs-cv+2(2dk-dm+2fs-fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm+2fs-fv}}\right)\right. \\
 & \left. \sin\left(-\frac{(2bk-bm+2cs-cv)^2}{4(2dk-dm+2fs-fv)}+2gs-gv-\frac{1}{2}\pi(m+v)\right)+2\sqrt{2dk-dm+2fs-fv}\right. \\
 & \left. \sin\left(2gs-gv-\frac{1}{2}\pi(m+v)+(2dk-dm+2fs-fv)z+(2bk-bm+2cs-cv)\sqrt{z}\right)\right) \Bigg) / \\
 & (2dk-dm+2fs-fv)^{3/2}+\left(\sqrt{2\pi}(-2bk+bm+2cs-cv)\cos\left(\frac{(2bk-bm-2cs+cv)^2}{4(2dk-dm-2fs+fv)}\right)+\right. \\
 & \left. 2gs-gv-\frac{1}{2}\pi(v-m)\right)C\left(\frac{2bk-bm-2cs+cv+2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right)- \\
 & \left. \sqrt{2\pi}(2bk-bm-2cs+cv)S\left(\frac{2bk-bm-2cs+cv+2(2dk-dm-2fs+fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk-dm-2fs+fv}}\right)\right)
 \end{aligned}$$

$$\sin\left(\frac{(2bk - bm - 2cs + cv)^2}{4(2dk - dm - 2fs + fv)} + 2gs - gv - \frac{1}{2}\pi(v - m)\right) - 2\sqrt{2dk - dm - 2fs + fv} \sin\left(2gs - gv - \frac{1}{2}\pi(v - m) - (2dk - dm - 2fs + fv)z - (2bk - bm - 2cs + cv)\sqrt{z}\right) \Big/ (2dk - dm - 2fs + fv)^{3/2}; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $\sin^m(bz^r + dz + e) \sin^v(cz^r + fz + g)$

01.06.21.0826.01

$$\begin{aligned}
 \int \sin^m(bz^2 + dz + e) \sin^v(cz^2 + fz + g) dz = & 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{v}{\frac{v}{2}} \\
 & \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{\sqrt{b(m-2k)}} (-1)^{k+m} \binom{m}{k} \left( \cos \left( \frac{(m-2k)d^2}{4b} - e(m-2k) - \frac{m\pi}{2} \right) C \left( \frac{d(m-2k) + 2bz(m-2k)}{\sqrt{b(m-2k)} \sqrt{2\pi}} \right) + \right. \\
 & \left. S \left( \frac{d(m-2k) + 2bz(m-2k)}{\sqrt{b(m-2k)} \sqrt{2\pi}} \right) \sin \left( \frac{(m-2k)d^2}{4b} - e(m-2k) - \frac{m\pi}{2} \right) \right) \Bigg) (1 - v \bmod 2) + \\
 & 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{\sqrt{c(v-2k)}} (-1)^{k+v} \binom{v}{k} \left( \cos \left( -\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k) \right) \right. \\
 & \left. C \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) - S \left( \frac{f(v-2k) + 2cz(v-2k)}{\sqrt{2\pi} \sqrt{c(v-2k)}} \right) \sin \left( -\frac{(v-2k)f^2}{4c} + \frac{\pi v}{2} + g(v-2k) \right) \right) \Bigg) + \\
 & 2^{-m-v+\frac{1}{2}} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \cos \left( -\frac{(2dk - dm - 2fs + fv)^2}{4(2bk - bm - 2cs + cv)} + e(2k - m) - \right. \right. \\
 & \left. \left. \frac{1}{2} \pi(m - v) - g(2s - v) \right) C \left( \frac{2dk - dm - 2fs + fv + 2(2bk - bm - 2cs + cv)z}{\sqrt{2\pi} \sqrt{2bk - bm - 2cs + cv}} \right) - \right. \\
 & \left. S \left( \frac{2dk - dm - 2fs + fv + 2(2bk - bm - 2cs + cv)z}{\sqrt{2\pi} \sqrt{2bk - bm - 2cs + cv}} \right) \sin \left( -\frac{(2dk - dm - 2fs + fv)^2}{4(2bk - bm - 2cs + cv)} + \right. \right. \\
 & \left. \left. e(2k - m) - \frac{1}{2} \pi(m - v) - g(2s - v) \right) \right) \Bigg) / \left( \sqrt{2bk - bm - 2cs + cv} \right) + \\
 & \left( \cos \left( -\frac{(2dk - dm + 2fs - fv)^2}{4(2bk - bm + 2cs - cv)} + e(2k - m) + g(2s - v) - \frac{1}{2} \pi(m + v) \right) \right. \\
 & \left. C \left( \frac{2dk - dm + 2fs - fv + 2(2bk - bm + 2cs - cv)z}{\sqrt{2\pi} \sqrt{2bk - bm + 2cs - cv}} \right) - \right. \\
 & \left. S \left( \frac{2dk - dm + 2fs - fv + 2(2bk - bm + 2cs - cv)z}{\sqrt{2\pi} \sqrt{2bk - bm + 2cs - cv}} \right) \sin \left( -\frac{(2dk - dm + 2fs - fv)^2}{4(2bk - bm + 2cs - cv)} + \right. \right. \\
 & \left. \left. e(2k - m) + g(2s - v) - \frac{1}{2} \pi(m + v) \right) \right) \Bigg) / \left( \sqrt{2bk - bm + 2cs - cv} \right) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.0827.01

$$\begin{aligned}
 \int \sin^m(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + fz + g) dz = & \\
 & 2^{-m-v} z \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) + 2^{-m-v} \binom{v}{\frac{v}{2}} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{(d(m-2k))^{3/2}} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (-1)^{k+m} \binom{m}{k} \left( -b(m-2k) \sqrt{2\pi} \cos\left(\frac{(m-2k)b^2}{4d} - e(m-2k) - \frac{m\pi}{2}\right) C\left(\frac{b(m-2k) + 2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)}\sqrt{2\pi}}\right) - \right. \right. \\
 & \quad b(m-2k) \sqrt{2\pi} S\left(\frac{b(m-2k) + 2d\sqrt{z}(m-2k)}{\sqrt{d(m-2k)}\sqrt{2\pi}}\right) \sin\left(\frac{(m-2k)b^2}{4d} - e(m-2k) - \frac{m\pi}{2}\right) + \\
 & \quad \left. \left. 2\sqrt{d(m-2k)} \sin\left(\frac{\pi m}{2} + e(m-2k) + d(m-2k)z + b(m-2k)\sqrt{z}\right) \right) \right) \\
 & (1 - v \bmod 2) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(f(v-2k))^{3/2}} \left( (-1)^{k+v} \binom{v}{k} \right. \\
 & \quad \left( -c\sqrt{2\pi} (v-2k) \cos\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) C\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) + \right. \\
 & \quad c\sqrt{2\pi} (v-2k) S\left(\frac{c(v-2k) + 2f\sqrt{z}(v-2k)}{\sqrt{2\pi}\sqrt{f(v-2k)}}\right) \sin\left(-\frac{(v-2k)c^2}{4f} + \frac{\pi v}{2} + g(v-2k)\right) + \\
 & \quad \left. \left. 2\sqrt{f(v-2k)} \sin\left(\frac{\pi v}{2} + g(v-2k) + f(v-2k)z + c(v-2k)\sqrt{z}\right) \right) \right) + \\
 & 2^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{s+v} \binom{v}{s} \left( \left( \sqrt{2\pi} (-2bk + bm + 2cs - cv) \cos\left(-\frac{(2bk - bm - 2cs + cv)^2}{4(2dk - dm - 2fs + fv)} + 2ek - \right. \right. \right. \\
 & \quad \left. \left. em - 2gs + gv + \frac{1}{2}\pi(v-m)\right) C\left(\frac{2bk - bm - 2cs + cv + 2(2dk - dm - 2fs + fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk - dm - 2fs + fv}}\right) + \right. \\
 & \quad \left. \sqrt{2\pi} (2bk - bm - 2cs + cv) S\left(\frac{2bk - bm - 2cs + cv + 2(2dk - dm - 2fs + fv)\sqrt{z}}{\sqrt{2\pi}\sqrt{2dk - dm - 2fs + fv}}\right) \right. \\
 & \quad \left. \sin\left(-\frac{(2bk - bm - 2cs + cv)^2}{4(2dk - dm - 2fs + fv)} + 2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m)\right) + \right. \\
 & \quad \left. 2\sqrt{2dk - dm - 2fs + fv} \sin\left(2ek - em - 2gs + gv + \frac{1}{2}\pi(v-m) + \right. \right. \\
 & \quad \left. \left. (2dk - dm - 2fs + fv)z + (2bk - bm - 2cs + cv)\sqrt{z}\right) \right) / (2dk - dm - 2fs + fv)^{3/2} + \\
 & \left( \sqrt{2\pi} (-2bk + bm - 2cs + cv) \cos\left(-\frac{(2bk - bm + 2cs - cv)^2}{4(2dk - dm + 2fs - fv)} + 2ek - em + 2gs - \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. g v - \frac{1}{2} \pi (m + v) \right) C \left( \frac{2 b k - b m + 2 c s - c v + 2 (2 d k - d m + 2 f s - f v) \sqrt{z}}{\sqrt{2 \pi} \sqrt{2 d k - d m + 2 f s - f v}} \right) + \\
 & \sqrt{2 \pi} (2 b k - b m + 2 c s - c v) S \left( \frac{2 b k - b m + 2 c s - c v + 2 (2 d k - d m + 2 f s - f v) \sqrt{z}}{\sqrt{2 \pi} \sqrt{2 d k - d m + 2 f s - f v}} \right) \\
 & \sin \left( -\frac{(2 b k - b m + 2 c s - c v)^2}{4 (2 d k - d m + 2 f s - f v)} + 2 e k - e m + 2 g s - g v - \frac{1}{2} \pi (m + v) \right) + \\
 & 2 \sqrt{2 d k - d m + 2 f s - f v} \sin \left( 2 e k - e m + 2 g s - g v - \frac{1}{2} \pi (m + v) + (2 d k - d m + 2 f s - f v) z + \right. \\
 & \left. (2 b k - b m + 2 c s - c v) \sqrt{z} \right) \Big/ (2 d k - d m + 2 f s - f v)^{3/2} \Big/ ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving rational functions of the direct function

Involving  $\frac{1}{a+b \sin(c z)}$

01.06.21.0828.01

$$\int \frac{1}{a+b \sin(c z)} d z = \frac{2}{\sqrt{a^2-b^2} c} \tan^{-1} \left( \frac{b+a \tan\left(\frac{c z}{2}\right)}{\sqrt{a^2-b^2}} \right)$$

01.06.21.0829.01

$$\int \frac{1}{\sin(z)+1} d z = \frac{2 \sin\left(\frac{z}{2}\right)}{\cos\left(\frac{z}{2}\right)+\sin\left(\frac{z}{2}\right)}$$

01.06.21.0830.01

$$\int \frac{1}{1-\sin(z)} d z = \frac{2 \sin\left(\frac{z}{2}\right)}{\cos\left(\frac{z}{2}\right)-\sin\left(\frac{z}{2}\right)}$$

Involving  $(a+b \sin(c z))^{-n}$

01.06.21.0831.01

$$\int \frac{1}{(a+b \sin(c z))^2} d z = \frac{b \sqrt{a^2-b^2} \cos(c z) + 2 a \tan^{-1} \left( \frac{b+a \tan\left(\frac{c z}{2}\right)}{\sqrt{a^2-b^2}} \right) (a+b \sin(c z))}{(a^2-b^2)^{3/2} c (a+b \sin(c z))}$$

01.06.21.0832.01

$$\int \frac{1}{(\sin(z)+1)^2} d z = -\frac{4 \cos(z)+\cos(2 z)-4 \sin(z)+\sin(2 z)-3}{6(\sin(z)+1)^2}$$

01.06.21.0833.01

$$\int \frac{1}{(1-\sin(z))^2} d z = \frac{4 \cos(z)+\cos(2 z)+4 \sin(z)-\sin(2 z)-3}{6(\sin(z)-1)^2}$$

01.06.21.0834.01

$$\int \frac{1}{(a + b \sin(cz))^3} dz = \frac{1}{2c} \left( \frac{2(2a^2 + b^2)}{(a^2 - b^2)^{5/2}} \tan^{-1} \left( \frac{b + a \tan(\frac{cz}{2})}{\sqrt{a^2 - b^2}} \right) + \frac{b \cos(cz) (4a^2 + 3b \sin(cz)a - b^2)}{(a^2 - b^2)^2 (a + b \sin(cz))^2} \right)$$

01.06.21.0835.01

$$\int \frac{1}{(a + b \sin(cz))^4} dz = \frac{1}{6c} \left( \frac{6a(2a^2 + 3b^2)}{(a^2 - b^2)^{7/2}} \tan^{-1} \left( \frac{b + a \tan(\frac{cz}{2})}{\sqrt{a^2 - b^2}} \right) + \right. \\ \left. (b \cos(cz) (18a^4 - 5b^2 a^2 + 3b(9a^2 + b^2) \sin(cz)a + 2b^4 + b^2(11a^2 + 4b^2) \sin^2(cz))) / ((a^2 - b^2)^3 (a + b \sin(cz))^3) \right)$$

Involving  $\frac{1}{a+b \sin^n(cz)}$

01.06.21.0836.01

$$\int \frac{1}{a + b \sin^2(cz)} dz = \frac{\tan^{-1} \left( \frac{\sqrt{a+b} \tan(cz)}{\sqrt{a}} \right)}{\sqrt{a} \sqrt{a+b} c}$$

01.06.21.0837.01

$$\int \frac{1}{\sin^2(z) + 1} dz = \frac{\tan^{-1}(\sqrt{2} \tan(z))}{\sqrt{2}}$$

01.06.21.0838.01

$$\int \frac{1}{1 - \sin^2(z)} dz = \tan(z)$$

01.06.21.0839.01

$$\int \frac{1}{1 + \sin^3(cz)} dz = \frac{1}{3c} \left( \frac{(-1)^{3/4} (i + \sqrt{3})}{\sqrt{\frac{1}{2}(-3i + \sqrt{3})}} \tan^{-1} \left( \frac{\sqrt[4]{-1} ((i + \sqrt{3}) i \tan(\frac{cz}{2}) + 2)}{\sqrt{2(-3i + \sqrt{3})}} \right) + \right.$$

$$\left. \frac{\sqrt[4]{-1} \sqrt{2} (-i + \sqrt{3})}{\sqrt{3i + \sqrt{3}}} \tan^{-1} \left( \frac{\sqrt[4]{-1} (2i + (-i + \sqrt{3}) \tan(\frac{cz}{2}))}{\sqrt{2(3i + \sqrt{3})}} \right) + \frac{2 \sin(\frac{cz}{2})}{\cos(\frac{cz}{2}) + \sin(\frac{cz}{2})} \right)$$

01.06.21.0840.01

$$\int \frac{1}{a + b \sin^4(cz)} dz = \frac{1}{2\sqrt{a} c} \left( \frac{1}{\sqrt{a+i\sqrt{b}} \sqrt{a}} \tan^{-1} \left( \frac{(\sqrt{a} + i\sqrt{b}) \tan(cz)}{\sqrt{a+i\sqrt{b}} \sqrt{a}} \right) + \frac{1}{\sqrt{a-i\sqrt{b}} \sqrt{b}} \tan^{-1} \left( \frac{(\sqrt{a} - i\sqrt{b}) \tan(cz)}{\sqrt{a-i\sqrt{b}} \sqrt{b}} \right) \right)$$

01.06.21.0841.01

$$\int \frac{1}{1 - \sin^4(cz)} dz = \frac{\sqrt{2} \tan^{-1}(\sqrt{2} \tan(cz)) + 2 \tan(cz)}{4c}$$

Involving  $(a + b \sin^2(cz))^{-n}$

01.06.21.0842.01

$$\int \frac{1}{(a + b \sin^2(cz))^2} dz = \frac{1}{2a^{3/2}c} \left( \frac{2a+b}{(a+b)^{3/2}} \tan^{-1}\left(\frac{\sqrt{a+b} \tan(cz)}{\sqrt{a}}\right) + \frac{\sqrt{a} b \sin(2cz)}{(a+b)(2a+b-b \cos(2cz))} \right)$$

01.06.21.0843.01

$$\int \frac{1}{(1 + \sin^2(cz))^2} dz = \frac{1}{8c} \left( 3\sqrt{2} \tan^{-1}(\sqrt{2} \tan(cz)) - \frac{2 \sin(2cz)}{\cos(2cz) - 3} \right)$$

01.06.21.0844.01

$$\int \frac{1}{(a + b \sin^2(cz))^3} dz = \frac{1}{8a^{5/2}c} \left( \frac{8a^2 + 8ba + 3b^2}{(a+b)^{5/2}} \tan^{-1}\left(\frac{\sqrt{a+b} \tan(cz)}{\sqrt{a}}\right) + \frac{\sqrt{a} b (16a^2 + 16ba + 3b^2 - 3b(2a+b) \cos(2cz)) \sin(2cz)}{(a+b)^2 (2a+b-b \cos(2cz))^2} \right)$$

Involving  $\frac{\sin(dz)}{a+b \sin(cz)}$

01.06.21.0845.01

$$\int \frac{\sin(dz)}{a + b \sin(cz)} dz = \frac{1}{2b\sqrt{a^2-b^2}} \left( \frac{1}{ic-id} \left( e^{(ic-id)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1\left(1 - \frac{d}{c}, 1; 2 - \frac{d}{c}; -\frac{ib e^{icz}}{\sqrt{a^2-b^2}-a}\right) + (\sqrt{a^2-b^2}-a) {}_2F_1\left(1 - \frac{d}{c}, 1; 2 - \frac{d}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}}\right) \right) \right) - \frac{1}{ic+id} \left( e^{(ic+id)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1\left(-\frac{i(ic+id)}{c}, 1; \frac{d}{c} + 2; -\frac{ib e^{icz}}{\sqrt{a^2-b^2}-a}\right) + (\sqrt{a^2-b^2}-a) {}_2F_1\left(-\frac{i(ic+id)}{c}, 1; \frac{d}{c} + 2; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}}\right) \right) \right) \right)$$

01.06.21.0846.01

$$\int \frac{\sin(cz)}{a + b \sin(cz)} dz = \frac{1}{b} \left( z - \frac{2a}{\sqrt{a^2-b^2}c} \tan^{-1}\left(\frac{b + a \tan(\frac{cz}{2})}{\sqrt{a^2-b^2}}\right) \right)$$

01.06.21.0847.01

$$\int \frac{\sin(z)}{\sin(z)+1} dz = \frac{(\cos(\frac{z}{2}) + \sin(\frac{z}{2})) (z \cos(\frac{z}{2}) + (z-2) \sin(\frac{z}{2}))}{\sin(z)+1}$$

01.06.21.0848.01

$$\int \frac{\sin(z)}{1-\sin(z)} dz = \frac{(\cos(\frac{z}{2}) - \sin(\frac{z}{2})) (z \cos(\frac{z}{2}) - (z+2) \sin(\frac{z}{2}))}{\sin(z)-1}$$

01.06.21.0849.01

$$\int \frac{A+B \sin(cz)}{a+b \sin(cz)} dz = \frac{\sqrt{a^2-b^2} B c z + 2(A b - a B) \tan^{-1}\left(\frac{b+a \tan(\frac{cz}{2})}{\sqrt{a^2-b^2}}\right)}{b \sqrt{a^2-b^2} c}$$

01.06.21.0850.01

$$\int \frac{A+B \sin(cz)}{\sin(cz)+1} dz = \frac{(\cos(\frac{cz}{2}) + \sin(\frac{cz}{2})) (B c z \cos(\frac{cz}{2}) + (2A+B(cz-2)) \sin(\frac{cz}{2}))}{c(\sin(cz)+1)}$$

01.06.21.0851.01

$$\int \frac{A+B \sin(cz)}{1-\sin(cz)} dz = \frac{(\cos(\frac{cz}{2}) - \sin(\frac{cz}{2})) (B c z \cos(\frac{cz}{2}) - (2A+B(cz+2)) \sin(\frac{cz}{2}))}{c(\sin(cz)-1)}$$

Involving  $\sin(dz) (a+b \sin(cz))^{-n}$

01.06.21.0852.01

$$\int \frac{\sin(dz)}{(a+b \sin(cz))^2} dz =$$

$$\frac{1}{2b(a^2-b^2)^{3/2}} \left( \frac{1}{c-d} \left( i e^{i(c-d)z} \left( -a(a+\sqrt{a^2-b^2}) {}_2F_1\left(1-\frac{d}{c}, 1; 2-\frac{d}{c}; \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}}\right) + a(a-\sqrt{a^2-b^2}) \right. \right. \right.$$

$${}_2F_1\left(1-\frac{d}{c}, 1; 2-\frac{d}{c}; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}\right) + (a^2+\sqrt{a^2-b^2} a-b^2) {}_2F_1\left(1-\frac{d}{c}, 2; 2-\frac{d}{c}; \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}}\right) +$$

$$\left. \left. \left. (-a^2+\sqrt{a^2-b^2} a+b^2) {}_2F_1\left(1-\frac{d}{c}, 2; 2-\frac{d}{c}; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}\right) \right) \right) -$$

$$\frac{1}{c+d} \left( i e^{i(c+d)z} \left( -a(a+\sqrt{a^2-b^2}) {}_2F_1\left(\frac{c+d}{c}, 1; \frac{d}{c}+2; \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}}\right) + a(a-\sqrt{a^2-b^2}) \right. \right.$$

$${}_2F_1\left(\frac{c+d}{c}, 1; \frac{d}{c}+2; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}\right) + (a^2+\sqrt{a^2-b^2} a-b^2) {}_2F_1\left(\frac{c+d}{c}, 2; \frac{d}{c}+2; \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}}\right) +$$

$$\left. \left. \left. (-a^2+\sqrt{a^2-b^2} a+b^2) {}_2F_1\left(\frac{c+d}{c}, 2; \frac{d}{c}+2; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}\right) \right) \right) \right)$$

01.06.21.0853.01

$$\int \frac{A + B \sin(cz)}{(a + b \sin(cz))^2} dz = \frac{1}{c} \left( \frac{2(Aa - bB)}{(a^2 - b^2)^{3/2}} \tan^{-1} \left( \frac{b + a \tan(\frac{cz}{2})}{\sqrt{a^2 - b^2}} \right) + \frac{(Ab - aB) \cos(cz)}{(a^2 - b^2)(a + b \sin(cz))} \right)$$

01.06.21.0854.01

$$\int \frac{A + B \sin(cz)}{(\sin(cz) + 1)^2} dz = \frac{(\cos(\frac{cz}{2}) + \sin(\frac{cz}{2})) (3B \cos(\frac{cz}{2}) - (A + 2B) \cos(\frac{3cz}{2}) + 3(A + B) \sin(\frac{cz}{2}))}{3c (\sin(cz) + 1)^2}$$

01.06.21.0855.01

$$\int \frac{A + B \sin(cz)}{(1 - \sin(cz))^2} dz = \frac{(\cos(\frac{cz}{2}) - \sin(\frac{cz}{2})) (3B \cos(\frac{cz}{2}) + (A - 2B) \cos(\frac{3cz}{2}) + 3(A - B) \sin(\frac{cz}{2}))}{3c (\sin(cz) - 1)^2}$$

01.06.21.0856.01

$$\int \frac{A + B \sin(cz)}{(a + b \sin(cz))^3} dz = \frac{1}{2c} \left( \frac{2(2Aa^2 - 3bBa + Ab^2)}{(a^2 - b^2)^{5/2}} \tan^{-1} \left( \frac{b + a \tan(\frac{cz}{2})}{\sqrt{a^2 - b^2}} \right) - \frac{(Ba^2 - 3Aba + 2b^2B) \cos(cz)}{(a^2 - b^2)^2 (a + b \sin(cz))} + \frac{(Ab - aB) \cos(cz)}{(a^2 - b^2)(a + b \sin(cz))^2} \right)$$

01.06.21.0857.01

$$\int \frac{A + B \sin(cz)}{(\sin(cz) + 1)^3} dz = \frac{1}{30c (\sin(cz) + 1)^3} \left( \left( \cos\left(\frac{cz}{2}\right) + \sin\left(\frac{cz}{2}\right) \right) \left( 15B \cos\left(\frac{cz}{2}\right) - 5(2A + 3B) \cos\left(\frac{3cz}{2}\right) + 20A \sin\left(\frac{cz}{2}\right) + 15B \sin\left(\frac{cz}{2}\right) - 2A \sin\left(\frac{5cz}{2}\right) - 3B \sin\left(\frac{5cz}{2}\right) \right) \right)$$

01.06.21.0858.01

$$\int \frac{A + B \sin(cz)}{(1 - \sin(cz))^3} dz = \frac{\left( 15B \cos\left(\frac{cz}{2}\right) + 5(2A - 3B) \cos\left(\frac{3cz}{2}\right) + 20A \sin\left(\frac{cz}{2}\right) - 15B \sin\left(\frac{cz}{2}\right) - 2A \sin\left(\frac{5cz}{2}\right) + 3B \sin\left(\frac{5cz}{2}\right) \right) / \left( 30c \left( \cos\left(\frac{cz}{2}\right) - \sin\left(\frac{cz}{2}\right) \right)^5 \right)}{}$$

01.06.21.0859.01

$$\int \frac{A + B \sin(z) + C \sin^2(z)}{(a + b \sin(z))^3} dz = \frac{1}{2} \left( \frac{2((2A + C)a^2 - 3bBa + b^2(A + 2C))}{(a^2 - b^2)^{5/2}} \tan^{-1} \left( \frac{b + a \tan(\frac{z}{2})}{\sqrt{a^2 - b^2}} \right) - \frac{(Ca^3 + bBa^2 - b^2(3A + 4C)a + 2b^3B) \cos(z)}{b(a^2 - b^2)^2 (a + b \sin(z))} + \frac{(Ca^2 - bBa + Ab^2) \cos(z)}{(a^2 - b^3)(a + b \sin(z))^2} \right)$$

Involving  $\frac{\sin(dz)}{a + b \sin^2(cz)}$

01.06.21.0860.01

$$\int \frac{\sin(dz)}{a+b\sin^2(cz)} dz = -\frac{1}{2\sqrt{a}b\sqrt{a+b}} \left( \frac{1}{2c-d} \left( e^{i dz - 2ic z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1\left(1-\frac{d}{2c}, 1; 2-\frac{d}{2c}; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) + (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1\left(1-\frac{d}{2c}, 1; 2-\frac{d}{2c}; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) \right) - \frac{1}{2c+d} \left( e^{-i(2c+d)z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1\left(\frac{d}{2c}+1, 1; \frac{d}{2c}+2; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) + (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1\left(\frac{d}{2c}+1, 1; \frac{d}{2c}+2; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) \right) \right)$$

01.06.21.0861.01

$$\int \frac{\sin(cz)}{a+b\sin^2(cz)} dz = -\frac{1}{\sqrt{b}\sqrt{a+b}c} \tanh^{-1}\left(\frac{\sqrt{b}\cos(cz)}{\sqrt{a+b}}\right)$$

01.06.21.0862.01

$$\int \frac{\sin(2cz)}{a+b\sin^2(cz)} dz = \frac{\log(2a+b-b\cos(2cz))}{bc}$$

Involving  $\frac{\sin^m(cz)}{a+b\sin^n(cz)}$

01.06.21.0863.01

$$\int \frac{\sin^m(cz)}{a+b\sin^2(cz)} dz = \frac{\sqrt{\cos^2(cz)} \sec(cz) \sin^{m+1}(cz)}{ac(m+1)} F_1\left(\frac{m+1}{2}; \frac{1}{2}, 1; \frac{m+3}{2}; \sin^2(cz), -\frac{b\sin^2(cz)}{a}\right)$$

01.06.21.0864.01

$$\int \frac{\sin^2(cz)}{a+b\sin^2(cz)} dz = \frac{1}{b} \left( z - \frac{\sqrt{a}}{\sqrt{a+b}c} \tan^{-1}\left(\frac{\sqrt{a+b}\tan(cz)}{\sqrt{a}}\right) \right)$$

01.06.21.0865.01

$$\int \frac{\sin^2(cz)}{a+b\sin^4(cz)} dz = -\frac{i}{2\sqrt{b}c} \left( \frac{\tan^{-1}\left(\frac{(\sqrt{a}-i\sqrt{b})\tan(cz)}{\sqrt{a-i\sqrt{a}\sqrt{b}}}\right)}{\sqrt{a-i\sqrt{a}\sqrt{b}}} - \frac{\tan^{-1}\left(\frac{(\sqrt{a}+i\sqrt{b})\tan(cz)}{\sqrt{a+i\sqrt{b}\sqrt{a}}}\right)}{\sqrt{a+i\sqrt{b}\sqrt{a}}} \right)$$

Involving  $\sin(dz)(a+b\sin^2(cz))^{-n}$

01.06.21.0866.01

$$\int \frac{\sin(dz)}{(a+b\sin^2(cz))^2} dz = -\frac{1}{4a^{3/2}b(a+b)^{3/2}} +$$

$$\left( \frac{1}{2c-d} \left( e^{i(2c-d)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a}-b \right) {}_2F_1 \left( 1-\frac{d}{2c}, 1; 2-\frac{d}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \right.$$

$$(2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a}+b \right) {}_2F_1 \left( 1-\frac{d}{2c}, 1; 2-\frac{d}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) +$$

$$2\sqrt{a} \left( \left( 2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b} \right) {}_2F_1 \left( 1-\frac{d}{2c}, 2; 2-\frac{d}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \right.$$

$$\left. \left. \left( 2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b} \right) {}_2F_1 \left( 1-\frac{d}{2c}, 2; 2-\frac{d}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) -$$

$$\frac{1}{2c+d} \left( e^{i(2c+d)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a}-b \right) {}_2F_1 \left( \frac{d}{2c}+1, 1; \frac{d}{2c}+2; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right.$$

$$(2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a}+b \right) {}_2F_1 \left( \frac{d}{2c}+1, 1; \frac{d}{2c}+2; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) +$$

$$2\sqrt{a} \left( \left( 2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b} \right) {}_2F_1 \left( \frac{d}{2c}+1, 2; \frac{d}{2c}+2; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \right.$$

$$\left. \left. \left( 2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b} \right) {}_2F_1 \left( \frac{d}{2c}+1, 2; \frac{d}{2c}+2; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) \right)$$

Involving  $\sin^m(cz) (a+b\sin^2(cz))^{-n}$

01.06.21.0867.01

$$\int \frac{\sin^m(cz)}{(a+b\sin^2(cz))^n} dz = \frac{\sqrt{\cos^2(cz)} \sec(cz) \sin^{m+1}(cz)}{c(m+1)a^n} F_1 \left( \frac{m+1}{2}; \frac{1}{2}, n; \frac{m+3}{2}; \sin^2(cz), -\frac{b\sin^2(cz)}{a} \right); v \in \mathbb{N}^+$$

01.06.21.0868.01

$$\int \frac{\sin^2(cz)}{(a+b\sin^2(cz))^2} dz = \frac{1}{2c} \left( \frac{1}{\sqrt{a}(a+b)^{3/2}} \tan^{-1} \left( \frac{\sqrt{a+b} \tan(cz)}{\sqrt{a}} \right) - \frac{\sin(2cz)}{(a+b)(2a+b-b\cos(2cz))} \right)$$

Involving  $\frac{\sin(ez)\sin(dz)}{a+b\sin(cz)}$

01.06.21.0869.01

$$\int \frac{\sin(ez) \sin(dz)}{a + b \sin(cz)} dz =$$

$$-\frac{1}{4b\sqrt{a^2-b^2}} \left( \frac{1}{c+d-e} \left( e^{i(c+d-e)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d-e}{c}, 1; \frac{2c+d-e}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) \right. \right.$$

$$\left. \left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( \frac{c+d-e}{c}, 1; \frac{2c+d-e}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) +$$

$$\frac{1}{c-d+e} \left( e^{i(c-d+e)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c-d+e}{c}, 1; \frac{2c-d+e}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) \right. \right.$$

$$\left. \left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( \frac{c-d+e}{c}, 1; \frac{2c-d+e}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) -$$

$$\frac{1}{c+d+e} \left( e^{i(c+d+e)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d+e}{c}, 1; \frac{2c+d+e}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) \right. \right.$$

$$\left. \left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( \frac{c+d+e}{c}, 1; \frac{2c+d+e}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) -$$

$$\frac{1}{c-d-e} \left( e^{i(c-d-e)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( -\frac{c-d+e}{c}, 1; -\frac{-2c+d+e}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) \right. \right.$$

$$\left. \left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( -\frac{c-d+e}{c}, 1; -\frac{-2c+d+e}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) \right)$$

Involving  $\sin(ez) \sin(dz) (a + b \sin(cz))^{-n}$

01.06.21.0870.01

$$\int \frac{\sin(ez) \sin(dz)}{(a + b \sin(cz))^2} dz =$$

$$\frac{1}{4b(a^2-b^2)^{3/2}} \left( \frac{1}{c+d-e} \left( e^{i(c+d-e)z} \left( -a(a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d-e}{c}, 1; \frac{2c+d-e}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) \right. \right.$$

$$+ a(a - \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d-e}{c}, 1; \frac{2c+d-e}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \left. \right)$$

$$+ (a^2 + \sqrt{a^2-b^2} a - b^2) {}_2F_1 \left( \frac{c+d-e}{c}, 2; \frac{2c+d-e}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right)$$





Involving  $\frac{\sin(ez)\sin(dz)}{a+b\sin^2(cz)}$

01.06.21.0871.01

$$\int \frac{\sin(ez)\sin(dz)}{a+b\sin^2(cz)} dz = -\frac{1}{4\sqrt{a}b\sqrt{a+b}}$$

$$\left( i \left( \frac{1}{2c+d-e} \left( e^{-i(2c+d-e)z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1 \left( \frac{2c+d-e}{2c}, 1; \frac{4c+d-e}{2c}; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1 \left( \frac{2c+d-e}{2c}, 1; \frac{4c+d-e}{2c}; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) \right) \right) + \right. \\ \left. \frac{1}{2c-d+e} \left( e^{-i(2c-d+e)z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1 \left( \frac{2c-d+e}{2c}, 1; \frac{4c-d+e}{2c}; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1 \left( \frac{2c-d+e}{2c}, 1; \frac{4c-d+e}{2c}; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) \right) \right) - \right. \\ \left. \frac{1}{2c+d+e} \left( e^{-i(2c+d+e)z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1 \left( \frac{2c+d+e}{2c}, 1; \frac{4c+d+e}{2c}; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1 \left( \frac{2c+d+e}{2c}, 1; \frac{4c+d+e}{2c}; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) \right) \right) + \frac{1}{-2c+d+e} \right. \\ \left. \left( e^{-i(2c-d-e)z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1 \left( -\frac{-2c+d+e}{2c}, 1; -\frac{-4c+d+e}{2c}; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1 \left( -\frac{-2c+d+e}{2c}, 1; -\frac{-4c+d+e}{2c}; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) \right) \right) \right) \right)$$

Involving  $\sin(ez)\sin(dz)(a+b\sin^2(cz))^{-n}$

01.06.21.0872.01

$$\int \frac{\sin(ez)\sin(dz)}{(a+b\sin^2(cz))^2} dz = \frac{i}{8a^{3/2}b(a+b)^{3/2}}$$

$$\left( \frac{1}{2c+d-e} \left( e^{i(2c+d-e)z} \left( (2a+b) \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1 \left( \frac{2c+d-e}{2c}, 1; \frac{4c+d-e}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. (2a+b) \left( (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1 \left( \frac{2c+d-e}{2c}, 1; \frac{4c+d-e}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) + 2\sqrt{a} \right) \right) \right) \right) \right) - \right. \\ \left. \left( (2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b}) {}_2F_1 \left( \frac{2c+d-e}{2c}, 2; \frac{4c+d-e}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \right. \right. \\ \left. \left. (2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b}) \right. \right. \\ \left. \left. {}_2F_1 \left( \frac{2c+d-e}{2c}, 2; \frac{4c+d-e}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) + \frac{1}{2c-d+e}$$

$$\begin{aligned}
 & \left( e^{i(2c-d+e)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a}-b \right) {}_2F_1 \left( \frac{2c-d+e}{2c}, 1; \frac{4c-d+e}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \\
 & (2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a}+b \right) {}_2F_1 \left( \frac{2c-d+e}{2c}, 1; \frac{4c-d+e}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) + 2\sqrt{a} \\
 & \left. \left( \left( 2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b} \right) {}_2F_1 \left( \frac{2c-d+e}{2c}, 2; \frac{4c-d+e}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \right. \right. \\
 & \left. \left( 2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b} \right) \right. \\
 & \left. \left. {}_2F_1 \left( \frac{2c-d+e}{2c}, 2; \frac{4c-d+e}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) - \frac{1}{2c+d+e} \\
 & \left( e^{i(2c+d+e)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a}-b \right) {}_2F_1 \left( \frac{2c+d+e}{2c}, 1; \frac{4c+d+e}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \\
 & (2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a}+b \right) {}_2F_1 \left( \frac{2c+d+e}{2c}, 1; \frac{4c+d+e}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) + 2\sqrt{a} \\
 & \left. \left( \left( 2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b} \right) {}_2F_1 \left( \frac{2c+d+e}{2c}, 2; \frac{4c+d+e}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \right. \right. \\
 & \left. \left( 2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b} \right) \right. \\
 & \left. \left. {}_2F_1 \left( \frac{2c+d+e}{2c}, 2; \frac{4c+d+e}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) + \frac{1}{-2c+d+e} \\
 & \left( e^{i(2c-d-e)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a}-b \right) {}_2F_1 \left( -\frac{-2c+d+e}{2c}, 1; -\frac{-4c+d+e}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) + \right. \right. \\
 & (2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a}+b \right) {}_2F_1 \left( -\frac{-2c+d+e}{2c}, 1; -\frac{-4c+d+e}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) + \\
 & 2\sqrt{a} \left( \left( 2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b} \right) {}_2F_1 \left( -\frac{-2c+d+e}{2c}, 2; -\frac{-4c+d+e}{2c}; \right. \right. \\
 & \left. \left. \frac{b e^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \left( 2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b} \right) \right. \\
 & \left. \left. {}_2F_1 \left( -\frac{-2c+d+e}{2c}, 2; -\frac{-4c+d+e}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right) \right) \right)
 \end{aligned}$$

**Involving algebraic functions of the direct function**

Involving  $(a + b \sin(cz))^\beta$

01.06.21.0873.01

$$\int (a + b \sin(cz))^\beta dz = \frac{\sec(cz)}{bc(\beta+1)} \sqrt{\frac{b(\sin(cz)+1)}{b-a}} \sqrt{\frac{b-b\sin(cz)}{a+b}} (a+b\sin(cz))^{\beta+1} F_1\left(\beta+1; \frac{1}{2}, \frac{1}{2}; \beta+2; \frac{a+b\sin(cz)}{a-b}, \frac{a+b\sin(cz)}{a+b}\right)$$

01.06.21.0874.01

$$\int (a + a \sin(cz))^\beta dz = \frac{\sqrt{2} \cos(cz) (a(\sin(cz)+1))^\beta}{(2\beta c + c) \sqrt{1-\sin(cz)}} {}_2F_1\left(\beta + \frac{1}{2}, \frac{1}{2}; \beta + \frac{3}{2}; \frac{1}{2}(\sin(cz)+1)\right)$$

01.06.21.0875.01

$$\int (a + b \sin(cz))^{5/2} dz = \frac{1}{30c\sqrt{a+b\sin(cz)}} \left( -4 \sqrt{\frac{a+b\sin(cz)}{a+b}} (23a^3 + 23ba^2 + 9b^2a + 9b^3) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + 32a \sqrt{\frac{a+b\sin(cz)}{a+b}} (a^2 - b^2) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + 2b \cos(cz) (-22a^2 - 28b\sin(cz)a - 3b^2 + 3b^2 \cos(2cz)) \right)$$

01.06.21.0876.01

$$\int (a + b \sin(cz))^{3/2} dz = -\frac{1}{3c\sqrt{a+b\sin(cz)}} \left( 2 \left( 4a \sqrt{\frac{a+b\sin(cz)}{a+b}} (a+b) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + b \cos(cz) (a+b\sin(cz)) - (a^2 - b^2) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{\frac{a+b\sin(cz)}{a+b}} \right) \right)$$

01.06.21.0877.01

$$\int \sqrt{a + b \sin(cz)} dz = -\frac{2}{c \sqrt{\frac{a+b\sin(cz)}{a+b}}} E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{a + b \sin(cz)}$$

01.06.21.0878.01

$$\int \sqrt{a + a \sin(cz)} dz = \frac{2(\sin(\frac{cz}{2}) - \cos(\frac{cz}{2})) \sqrt{a(\sin(cz)+1)}}{c(\cos(\frac{cz}{2}) + \sin(\frac{cz}{2}))}$$

01.06.21.0879.01

$$\int \sqrt{a - a \sin(cz)} dz = \frac{2(\cos(\frac{cz}{2}) + \sin(\frac{cz}{2})) \sqrt{a - a \sin(cz)}}{c(\cos(\frac{cz}{2}) - \sin(\frac{cz}{2}))}$$

01.06.21.0880.01

$$\int \frac{1}{\sqrt{a + b \sin(cz)}} dz = -\frac{2}{c \sqrt{a + b \sin(cz)}} F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{\frac{a + b \sin(cz)}{a+b}}$$

01.06.21.0881.01

$$\int \frac{1}{\sqrt{a+a \sin(c z)}} dz = -\frac{(2+2 i)(-1)^{3 / 4} \tanh ^{-1}\left(\frac{\tan \left(\frac{c z}{4}\right)-1}{\sqrt{2}}\right)\left(\cos \left(\frac{c z}{2}\right)+\sin \left(\frac{c z}{2}\right)\right)}{c \sqrt{a(\sin (c z)+1)}}$$

01.06.21.0882.01

$$\int \frac{1}{\sqrt{a-a \sin(c z)}} dz = \frac{(2-2 i) \sqrt[4]{-1} \tanh ^{-1}\left(\frac{\tan \left(\frac{c z}{4}\right)+1}{\sqrt{2}}\right)\left(\cos \left(\frac{c z}{2}\right)-\sin \left(\frac{c z}{2}\right)\right)}{c \sqrt{a-a \sin (c z)}}$$

01.06.21.0883.01

$$\int \frac{1}{(a+b \sin (c z))^{3 / 2}} dz = -\frac{2}{(a-b)(a+b) c \sqrt{a+b \sin (c z)}}\left((a+b) E\left(\frac{1}{4}(\pi-2 c z)\left|\frac{2 b}{a+b}\right.\right) \sqrt{\frac{a+b \sin (c z)}{a+b}}-b \cos (c z)\right)$$

01.06.21.0884.01

$$\int \frac{1}{(a+b \sin (c z))^{5 / 2}} dz = \left(2\left(-4 a(a+b)^2 E\left(\frac{1}{4}(\pi-2 c z)\left|\frac{2 b}{a+b}\right.\right)\left(\frac{a+b \sin (c z)}{a+b}\right)^{3 / 2}+(a-b)(a+b)^2 F\left(\frac{1}{4}(\pi-2 c z)\left|\frac{2 b}{a+b}\right.\right)\left(\frac{a+b \sin (c z)}{a+b}\right)^{3 / 2}+b \cos (c z)\left(5 a^2+4 b \sin (c z) a-b^2\right)\right) / \left(3(a-b)^2(a+b)^2 c(a+b \sin (c z))^{3 / 2}\right)$$

Involving  $((a+b \sin (c z))^y)^\beta$

01.06.21.0885.01

$$\int((a+b \sin (c z))^y)^\beta dz = \frac{1}{b c(\beta v+1)}\left(F_1\left(\beta v+1 ; \frac{1}{2}, \frac{1}{2} ; \beta v+2 ; \frac{a+b \sin (c z)}{a-b}, \frac{a+b \sin (c z)}{a+b}\right) \sec (c z) \sqrt{\frac{b(\sin (c z)+1)}{b-a}} \sqrt{\frac{b-b \sin (c z)}{a+b}}(a+b \sin (c z))\left((a+b \sin (c z))^y\right)^\beta\right)$$

01.06.21.0886.01

$$\int \sqrt{(a+b \sin (c z))^5} dz = -\frac{1}{30 c(a+b \sin (c z))^3}\left(\sqrt{(a+b \sin (c z))^5}\left(4 \sqrt{\frac{a+b \sin (c z)}{a+b}}\left(23 a^3+23 b a^2+9 b^2 a+9 b^3\right) E\left(\frac{1}{4}(\pi-2 c z)\left|\frac{2 b}{a+b}\right.\right)+2 b \cos (c z)\left(22 a^2+28 b \sin (c z) a+3 b^2-3 b^2 \cos (2 c z)\right)-32 a\left(a^2-b^2\right) F\left(\frac{1}{4}(\pi-2 c z)\left|\frac{2 b}{a+b}\right.\right) \sqrt{\frac{a+b \sin (c z)}{a+b}}\right)\right)$$

01.06.21.0887.01

$$\int \sqrt{(a+b \sin(cz))^3} dz =$$

$$\frac{1}{3c(a+b \sin(cz))^2} \left( \sqrt{(a+b \sin(cz))^3} \left( -8a(a+b) \sqrt{\frac{a+b \sin(cz)}{a+b}} E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + 2 \sqrt{\frac{a+b \sin(cz)}{a+b}} \right. \right.$$

$$\left. \left. (a^2-b^2) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) - 2b \cos(cz)(a+b \sin(cz)) \right) \right)$$

01.06.21.0888.01

$$\int \frac{1}{\sqrt{(a+b \sin(cz))^3}} dz =$$

$$-\frac{2(a+b \sin(cz))}{(a-b)(a+b)c \sqrt{(a+b \sin(cz))^3}} \left( (a+b) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{\frac{a+b \sin(cz)}{a+b}} - b \cos(cz) \right)$$

01.06.21.0889.01

$$\int \frac{1}{\sqrt{(a+b \sin(cz))^5}} dz = \frac{1}{3c \sqrt{(a+b \sin(cz))^5}} \left( \frac{2b \cos(cz)(a+b \sin(cz))(5a^2+4b \sin(cz)a-b^2)}{(a^2-b^2)^2} - \right.$$

$$\left. \frac{2(a+b)}{(a-b)^2} \left( 4a E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + (b-a) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \right) \left( \frac{a+b \sin(cz)}{a+b} \right)^{5/2} \right)$$

Involving  $(a+b \sin(cz))^\beta \sin(dz)$

01.06.21.0890.01

$$\int (a+b \sin(cz))^\beta \sin(dz) dz =$$

$$-\frac{1}{2(d-c\beta)(d+c\beta)} \left( e^{-idz} \left( 1 + \frac{ib e^{icz}}{\sqrt{a^2-b^2}-a} \right)^{-\beta} \left( 1 - \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}} \right)^{-\beta} \left( a - \frac{1}{2} ib e^{-icz} (-1+e^{2icz}) \right)^\beta \right.$$

$$\left. \left( (d-c\beta) F_1 \left( -\frac{d+c\beta}{c}; -\beta, -\beta; -\frac{d}{c} - \beta + 1; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}, \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}} \right) + \right.$$

$$\left. \left. e^{2idz} (d+c\beta) F_1 \left( \frac{d}{c} - \beta; -\beta, -\beta; \frac{d}{c} - \beta + 1; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}, \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}} \right) \right) \right)$$

01.06.21.0891.01

$$\int (a + b \sin(c z))^{\beta} \sin(c z) dz = \frac{1}{b^2 c (\beta + 1) (\beta + 2)}$$

$$\left( \sec(c z) \sqrt{\frac{b (\sin(c z) + 1)}{b - a}} \sqrt{\frac{b - b \sin(c z)}{a + b}} (a + b \sin(c z))^{\beta + 1} \left( (\beta + 1) F_1 \left( \beta + 2; \frac{1}{2}, \frac{1}{2}; \beta + 3; \frac{a + b \sin(c z)}{a - b}, \frac{a + b \sin(c z)}{a + b} \right) \right. \right.$$

$$\left. \left. (a + b \sin(c z)) - a (\beta + 2) F_1 \left( \beta + 1; \frac{1}{2}, \frac{1}{2}; \beta + 2; \frac{a + b \sin(c z)}{a - b}, \frac{a + b \sin(c z)}{a + b} \right) \right) \right)$$

01.06.21.0892.01

$$\int \sqrt{a + b \sin(c z)} \sin(c z) dz =$$

$$-\frac{1}{3 b c \sqrt{a + b \sin(c z)}} \left( 2 \left( a \sqrt{\frac{a + b \sin(c z)}{a + b}} (a + b) E \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) + b \cos(c z) (a + b \sin(c z)) - \right. \right.$$

$$\left. \left. (a^2 - b^2) F \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) \sqrt{\frac{a + b \sin(c z)}{a + b}} \right) \right)$$

01.06.21.0893.01

$$\int \frac{\sin(c z)}{\sqrt{a + b \sin(c z)}} dz = -\frac{2}{b c \sqrt{a + b \sin(c z)}} \left( (a + b) E \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) - a F \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) \right) \sqrt{\frac{a + b \sin(c z)}{a + b}}$$

01.06.21.0894.01

$$\int \frac{\sin(c z)}{(a + b \sin(c z))^{3/2}} dz =$$

$$\left( 2 \left( -a b \cos(c z) + a \sqrt{\frac{a + b \sin(c z)}{a + b}} (a + b) E \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) - (a^2 - b^2) F \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) \sqrt{\frac{a + b \sin(c z)}{a + b}} \right) \right) /$$

$$\left( (a - b) b (a + b) c \sqrt{a + b \sin(c z)} \right)$$

01.06.21.0895.01

$$\int \frac{\sin(c z)}{(a + b \sin(c z))^{5/2}} dz =$$

$$\frac{2}{3 c (a + b \sin(c z))^{3/2}} \left( \frac{1}{(a - b)^2 b} \left( (a^2 + 3 b^2) E \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) + a (b - a) F \left( \frac{1}{4} (\pi - 2 c z) \left| \frac{2 b}{a + b} \right. \right) \right) \left( \frac{a + b \sin(c z)}{a + b} \right)^{3/2} - \right.$$

$$\left. \frac{\cos(c z) (2 a (a^2 + b^2) + b (a^2 + 3 b^2) \sin(c z))}{(a^2 - b^2)^2} \right)$$

Involving  $((a + b \sin(c z))^y)^\beta \sin(d z)$

01.06.21.0896.01

$$\int (a + b \sin(cz))^{\beta} \sin(dz) dz =$$

$$-\frac{1}{2(d-c\beta\nu)(d+c\beta\nu)} \left( e^{-idz} \left( 1 + \frac{ib e^{icz}}{\sqrt{a^2-b^2}-a} \right)^{-\beta\nu} \left( 1 - \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}} \right)^{-\beta\nu} \left( a - \frac{1}{2} ib e^{-icz} (-1 + e^{2icz}) \right)^{\beta\nu} \right.$$

$$\left. \left( (d-c\beta\nu) F_1 \left( -\frac{d+c\beta\nu}{c}; -\beta\nu, -\beta\nu; -\frac{d}{c} - \beta\nu + 1; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}, \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}} \right) + e^{2idz} (d+c\beta\nu) \right.$$

$$\left. \left. F_1 \left( \frac{d}{c} - \beta\nu; -\beta\nu, -\beta\nu; \frac{d}{c} - \beta\nu + 1; \frac{ib e^{icz}}{a+\sqrt{a^2-b^2}}, \frac{ib e^{icz}}{a-\sqrt{a^2-b^2}} \right) \right) (a + b \sin(cz))^{-\beta\nu} ((a + b \sin(cz))^{\nu})^{\beta} \right)$$

01.06.21.0897.01

$$\int \sqrt{(a + b \sin(cz))^5} \sin(cz) dz =$$

$$-\frac{1}{84bc(a+b\sin(cz))^3} \left( \sqrt{(a+b\sin(cz))^5} \left( 8a \sqrt{\frac{a+b\sin(cz)}{a+b}} (3a^3 + 3ba^2 + 29b^2a + 29b^3) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + \right.$$

$$2b \cos(cz) (36a^3 + 44b^2a - 24b^2 \cos(2cz)a + b(72a^2 + 29b^2) \sin(cz) - 3b^3 \sin(3cz)) - \right.$$

$$\left. \left. 8(3a^4 + 2b^2a^2 - 5b^4) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{\frac{a+b\sin(cz)}{a+b}} \right) \right)$$

01.06.21.0898.01

$$\int \sqrt{(a + b \sin(cz))^3} \sin(cz) dz =$$

$$-\frac{1}{10bc(a+b\sin(cz))^2} \left( \sqrt{(a+b\sin(cz))^3} \left( 4 \sqrt{\frac{a+b\sin(cz)}{a+b}} (a^3 + ba^2 + 3b^2a + 3b^3) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + \right.$$

$$2b \cos(cz) (4a^2 + 6b \sin(cz)a + b^2 - b^2 \cos(2cz)) - 4a(a^2 - b^2) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{\frac{a+b\sin(cz)}{a+b}} \right) \right)$$

01.06.21.0899.01

$$\int \frac{\sin(cz)}{\sqrt{(a + b \sin(cz))^3}} dz = \left( 2(a + b \sin(cz)) \left( -ab \cos(cz) + a \sqrt{\frac{a + b \sin(cz)}{a + b}} (a + b) E\left(\frac{1}{4}(\pi - 2cz) \middle| \frac{2b}{a + b}\right) - \right.$$

$$\left. \left. (a^2 - b^2) F\left(\frac{1}{4}(\pi - 2cz) \middle| \frac{2b}{a + b}\right) \sqrt{\frac{a + b \sin(cz)}{a + b}} \right) \right) / (b(a^2 - b^2)c \sqrt{(a + b \sin(cz))^3})$$



01.06.21.0900.01

$$\int \frac{\sin(cz)}{\sqrt{(a+b \sin(cz))^5}} dz =$$

$$\frac{1}{3c \sqrt{(a+b \sin(cz))^5}} \left( \frac{2(a+b)}{(a-b)^2 b} \left( (a^2+3b^2) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + a(b-a) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \right) \left(\frac{a+b \sin(cz)}{a+b}\right)^{5/2} - \frac{2 \cos(cz) (a+b \sin(cz)) (2a(a^2+b^2) + b(a^2+3b^2) \sin(cz))}{(a^2-b^2)^2} \right)$$

Involving  $(a+b \sin(cz))^\beta \sin^\nu(cz)$

01.06.21.0901.01

$$\int \frac{\sin^2(cz)}{\sqrt{a+b \sin(cz)}} dz = \frac{1}{3b^2 c \sqrt{a+b \sin(cz)}} \left( 4a(a+b) E\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \sqrt{\frac{a+b \sin(cz)}{a+b}} - 2 \left( \sqrt{\frac{a+b \sin(cz)}{a+b}} (2a^2+b^2) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + b \cos(cz) (a+b \sin(cz)) \right) \right)$$

01.06.21.0902.01

$$\int \frac{\sin^2(cz)}{\sqrt{a-a \sin(cz)}} dz = - \frac{(\cos(\frac{cz}{2}) - \sin(\frac{cz}{2})) \left( 2(\cos(\frac{cz}{2}) + \sin(\frac{cz}{2}))^3 - (6-6i) \sqrt[4]{-1} \tanh^{-1}\left(\frac{\tan(\frac{cz}{4})+1}{\sqrt{2}}\right) \right)}{3c \sqrt{a-a \sin(cz)}}$$

01.06.21.0903.01

$$\int \frac{\sin^{\frac{1}{2}}(cz)}{a+b \sin(cz)} dz = - \frac{2}{b(a+b)c} \left( (a+b) F\left(\frac{1}{4}(\pi-2cz) \middle| 2\right) - a \Pi\left(\frac{2b}{a+b}; \frac{1}{4}(\pi-2cz) \middle| 2\right) \right)$$

Involving  $(a+b \sin(cz))^\beta$  and rational function of  $\sin(cz)$

01.06.21.0904.01

$$\int \frac{\sqrt{a+b \sin(cz)}}{d+e \sin(cz)} dz =$$

$$- \frac{2}{ce(d+e) \sqrt{a+b \sin(cz)}} \left( b(d+e) F\left(\frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) + (ae-bd) \Pi\left(\frac{2e}{d+e}; \frac{1}{4}(\pi-2cz) \middle| \frac{2b}{a+b}\right) \right) \sqrt{\frac{a+b \sin(cz)}{a+b}}$$

01.06.21.0905.01

$$\int \frac{\sqrt{a+b \sin(cz)}}{(d+e \sin(cz))^2} dz = -\frac{1}{4c} \left[ \frac{4e \sqrt{a+b \sin(cz)} \cos(cz)}{(e^2-d^2)(d+e \sin(cz))} + \right.$$

$$\frac{1}{d^2-e^2} \left[ \frac{1}{\sqrt{-\frac{1}{a+b}} e(ae-bd)} \left( 8id \left( (ae-bd) F \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin(cz)} \right) \right) \left| \frac{a+b}{a-b} \right. \right) + \right.$$

$$bd \Pi \left( \frac{(a+b)e}{ae-bd}; i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin(cz)} \right) \left| \frac{a+b}{a-b} \right. \right) \right]$$

$$\sec(cz) \sqrt{\frac{b(\sin(cz)+1)}{b-a}} \sqrt{\frac{b-b \sin(cz)}{a+b}} + \frac{1}{b \sqrt{-\frac{1}{a+b}} e(bd-ae)}$$

$$\left( i(\cos(cz) + \cos(3cz)) \left( 2(a-b)e(ae-bd) E \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin(cz)} \right) \right) \left| \frac{a+b}{a-b} \right. \right) + \right.$$

$$b \left( b(2d^2-e^2) \Pi \left( \frac{(a+b)e}{ae-bd}; i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin(cz)} \right) \right) \left| \frac{a+b}{a-b} \right. \right) - 2(d+e)$$

$$\left. \left. (bd-ae) F \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a+b \sin(cz)} \right) \right) \left| \frac{a+b}{a-b} \right. \right) \right) \sec^2(cz) \sec(2cz)$$

$$\left. \left. \sqrt{\frac{b(\sin(cz)+1)}{b-a}} \sqrt{\frac{b-b \sin(cz)}{a+b}} + \frac{2(4ad-be) \Pi \left( \frac{2e}{d+e}; \frac{1}{4}(\pi-2cz) \left| \frac{2b}{a+b} \right. \right) \sqrt{\frac{a+b \sin(cz)}{a+b}}}{(d+e) \sqrt{a+b \sin(cz)}} \right) \right]$$

01.06.21.0906.01

$$\int \frac{A+B \sin(cz)}{\sqrt{a+b \sin(cz)}} dz =$$

$$-\frac{2}{bc \sqrt{a+b \sin(cz)}} \left( (a+b) B E \left( \frac{1}{4}(\pi-2cz) \left| \frac{2b}{a+b} \right. \right) + (Ab-aB) F \left( \frac{1}{4}(\pi-2cz) \left| \frac{2b}{a+b} \right. \right) \right) \sqrt{\frac{a+b \sin(cz)}{a+b}}$$

01.06.21.0907.01

$$\int \frac{1}{(d+e \sin(cz)) \sqrt{a+b \sin(cz)}} dz = -\frac{2}{c(d+e) \sqrt{a+b \sin(cz)}} \Pi \left( \frac{2e}{d+e}; \frac{1}{4}(\pi-2cz) \left| \frac{2b}{a+b} \right. \right) \sqrt{\frac{a+b \sin(cz)}{a+b}}$$

01.06.21.0908.01

$$\int \frac{1}{(d + e \sin(cz))^2 \sqrt{a + b \sin(cz)}} dz =$$

$$\frac{1}{4c(ae - bd)} \left( \frac{1}{d^2 - e^2} \left( -\frac{1}{\sqrt{-\frac{1}{a+b}}(ae - bd)} \left( 8id \left( (ae - bd) F \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \right) \middle| \frac{a+b}{a-b} \right) + \right. \right. \right.$$

$$bd \Pi \left( \frac{(a+b)e}{ae - bd}; i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \middle| \frac{a+b}{a-b} \right) \left. \right. \left. \right.$$

$$\sec(cz) \sqrt{\frac{b(\sin(cz) + 1)}{b-a}} \sqrt{\frac{b - b \sin(cz)}{a+b}} \left. \right) - \frac{1}{b \sqrt{-\frac{1}{a+b}}(bd - ae)}$$

$$\left( i(\cos(cz) + \cos(3cz)) \left( 2(a-b)e(ae - bd) E \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \right) \middle| \frac{a+b}{a-b} \right) + \right.$$

$$b \left( b(2d^2 - e^2) \Pi \left( \frac{(a+b)e}{ae - bd}; i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \right) \middle| \frac{a+b}{a-b} \right) - 2$$

$$\left. \left. \left. \left. (d + e)(bd - ae) F \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \right) \middle| \frac{a+b}{a-b} \right) \right) \right) \right)$$

$$\sec^2(cz) \sec(2cz) \sqrt{\frac{b(\sin(cz) + 1)}{b-a}} \sqrt{\frac{b - b \sin(cz)}{a+b}} \left. \right) +$$

$$\left. \frac{2(4bd^2 - 4aed - 3be^2) \Pi \left( \frac{2e}{d+e}; \frac{1}{4}(\pi - 2cz) \middle| \frac{2b}{a+b} \right) \sqrt{\frac{a+b \sin(cz)}{a+b}}}{(d+e) \sqrt{a + b \sin(cz)}} - \frac{4e^2 \cos(cz) \sqrt{a + b \sin(cz)}}{(e^2 - d^2)(d + e \sin(cz))} \right)$$

01.06.21.0909.01

$$\int \frac{\sin(cz)}{(d + e \sin(cz)) \sqrt{a + b \sin(cz)}} dz =$$

$$-\frac{1}{b \sqrt{-\frac{1}{a+b}} ce(bd - ae)} \left( 2i \left( (bd - ae) F \left( i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \right) \middle| \frac{a+b}{a-b} \right) - \right.$$

$$\left. \left. \left. \left. bd \Pi \left( \frac{(a+b)e}{ae - bd}; i \sinh^{-1} \left( \sqrt{-\frac{1}{a+b}} \sqrt{a + b \sin(cz)} \right) \right) \middle| \frac{a+b}{a-b} \right) \right) \sec(cz) \sqrt{\frac{b(\sin(cz) + 1)}{b-a}} \sqrt{\frac{b - b \sin(cz)}{a+b}} \right)$$

Involving  $(a + b \sin(2 c z))^{\beta} \sin(c z)$

01.06.21.0910.01

$$\int (a + b \sin(2 c z))^{5/2} \sin(c z) dz =$$

$$\frac{1}{96 \sqrt{b} c} \left( -26 a \sqrt{a + b \sin(2 c z)} \sin(3 c z) b^{3/2} + 54 a \sin(c z) \sqrt{a + b \sin(2 c z)} b^{3/2} - 28 \cos(c z) \sqrt{a + b \sin(2 c z)} b^{5/2} - \right.$$

$$6 \cos(3 c z) \sqrt{a + b \sin(2 c z)} b^{5/2} + 4 \cos(5 c z) \sqrt{a + b \sin(2 c z)} b^{5/2} -$$

$$45 a \log \left( \sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)} \right) b^2 - 66 a^2 \cos(c z) \sqrt{a + b \sin(2 c z)} \sqrt{b} -$$

$$15 (a + b)^3 \tan^{-1} \left( \frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) + 15 (b^3 + 3 a^2 b) \tanh^{-1} \left( \frac{\sqrt{b} (\cos(c z) + \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) -$$

$$\left. 15 a^3 \log \left( \sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)} \right) \right)$$

01.06.21.0911.01

$$\int (a + b \sin(2 c z))^{3/2} \sin(c z) dz = \frac{1}{16 \sqrt{b} c} \left( -2 \sqrt{a + b \sin(2 c z)} \sin(3 c z) b^{3/2} + \right.$$

$$4 \sin(c z) \sqrt{a + b \sin(2 c z)} b^{3/2} - 3 \log \left( \sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)} \right) b^2 +$$

$$6 a \tanh^{-1} \left( \frac{\sqrt{b} (\cos(c z) + \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) b - 10 a \cos(c z) \sqrt{a + b \sin(2 c z)} \sqrt{b} -$$

$$\left. 3 (a + b)^2 \tan^{-1} \left( \frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) - 3 a^2 \log \left( \sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)} \right) \right)$$

01.06.21.0912.01

$$\int \sqrt{a + b \sin(2 c z)} \sin(c z) dz = \frac{1}{4 \sqrt{b} c} \left( -(a + b) \tan^{-1} \left( \frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) + b \tanh^{-1} \left( \frac{\sqrt{b} (\cos(c z) + \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) - \right.$$

$$\left. a \log \left( \sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)} \right) - 2 \sqrt{b} \cos(c z) \sqrt{a + b \sin(2 c z)} \right)$$

01.06.21.0913.01

$$\int \frac{\sin(c z)}{\sqrt{a + b \sin(2 c z)}} dz = -\frac{1}{2 \sqrt{b} c} \left( \tan^{-1} \left( \frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}} \right) + \log \left( \sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)} \right) \right)$$

01.06.21.0914.01

$$\int \frac{\sin(c z)}{(a + b \sin(2 c z))^{3/2}} dz = -\frac{a \cos(c z) + b \sin(c z)}{(a^2 - b^2) c \sqrt{a + b \sin(2 c z)}}$$

01.06.21.0915.01

$$\int \frac{\sin(c z)}{(a + b \sin(2 c z))^{5/2}} dz = \frac{-3 a (a^2 + b^2) \cos(c z) - b (6 \sin(c z) a^2 - 2 b \cos(3 c z) a + (a^2 + b^2) \sin(3 c z))}{3 (a^2 - b^2)^2 c (a + b \sin(2 c z))^{3/2}}$$

Involving  $((a + b \sin(2 c z))^m)^{\pm \frac{1}{2}} \sin(c z)$

01.06.21.0916.01

$$\int \sqrt{(a + b \sin(2 c z))^5} \sin(c z) dz =$$

$$-\left( \sqrt{(a + b \sin(2 c z))^5} \left( 26 a \sqrt{a + b \sin(2 c z)} \sin(3 c z) b^{3/2} - 54 a \sin(c z) \sqrt{a + b \sin(2 c z)} b^{3/2} + \right. \right.$$

$$28 \cos(c z) \sqrt{a + b \sin(2 c z)} b^{5/2} + 6 \cos(3 c z) \sqrt{a + b \sin(2 c z)} b^{5/2} - 4 \cos(5 c z) \sqrt{a + b \sin(2 c z)} b^{5/2} +$$

$$45 a \log\left(\sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)}\right) b^2 + 66 a^2 \cos(c z) \sqrt{a + b \sin(2 c z)} \sqrt{b} +$$

$$15 (a + b)^3 \tan^{-1}\left(\frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}}\right) - 15 (b^3 + 3 a^2 b) \tanh^{-1}\left(\frac{\sqrt{b} (\cos(c z) + \sin(c z))}{\sqrt{a + b \sin(2 c z)}}\right) +$$

$$\left. \left. 15 a^3 \log\left(\sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)}\right) \right) \right) / \left( 96 \sqrt{b} c (a + b \sin(2 c z))^{5/2} \right)$$

01.06.21.0917.01

$$\int \sqrt{(a + b \sin(2 c z))^3} \sin(c z) dz =$$

$$-\left( \sqrt{(a + b \sin(2 c z))^3} \left( 2 \sqrt{a + b \sin(2 c z)} \sin(3 c z) b^{3/2} - 4 \sin(c z) \sqrt{a + b \sin(2 c z)} b^{3/2} + \right. \right.$$

$$3 \log\left(\sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)}\right) b^2 - 6 a \tanh^{-1}\left(\frac{\sqrt{b} (\cos(c z) + \sin(c z))}{\sqrt{a + b \sin(2 c z)}}\right) b +$$

$$10 a \cos(c z) \sqrt{a + b \sin(2 c z)} \sqrt{b} + 3 (a + b)^2 \tan^{-1}\left(\frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}}\right) +$$

$$\left. \left. 3 a^2 \log\left(\sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)}\right) \right) \right) / \left( 16 \sqrt{b} c (a + b \sin(2 c z))^{3/2} \right)$$

01.06.21.0918.01

$$\int \frac{\sin(c z)}{\sqrt{(a + b \sin(2 c z))^3}} dz = -\frac{(a \cos(c z) + b \sin(c z)) (a + b \sin(2 c z))}{(a^2 - b^2) c \sqrt{(a + b \sin(2 c z))^3}}$$

01.06.21.0919.01

$$\int \frac{\sin(c z)}{\sqrt{(a + b \sin(2 c z))^5}} dz =$$

$$-\left( (a + b \sin(2 c z)) \left( 3 a (a^2 + b^2) \cos(c z) + b \left( 6 \sin(c z) a^2 - 2 b \cos(3 c z) a + (a^2 + b^2) \sin(3 c z) \right) \right) \right) /$$

$$\left( 3 (a^2 - b^2)^2 c \sqrt{(a + b \sin(2 c z))^5} \right)$$

Involving  $(a + b \sin(2 c z))^\beta \sin^\nu(c z)$

01.06.21.0920.01

$$\int (a + b \sin(2cz))^{3/2} \sin^2(cz) dz = \frac{1}{60c\sqrt{a+b\sin(2cz)}} \left( -\frac{6(2a^2+b^2)(\cos(cz)+1)^2 \left(\frac{a+b\sin(2cz)}{(\cos(cz)+1)^2}\right)^{3/2}}{b\sqrt{\sec^4\left(\frac{cz}{2}\right)(a+b\sin(2cz))}} + \right.$$

$$(a+b\sin(2cz))(-10b\cos(2cz)+3b\cos(4cz)-12a\sin(2cz))-10(3a^2+b^2)F\left(\frac{\pi}{4}-cz\left|\frac{2b}{a+b}\right.\right)\sqrt{\frac{a+b\sin(2cz)}{a+b}} -$$

$$\left. 40a\left((a+b)E\left(\frac{\pi}{4}-cz\left|\frac{2b}{a+b}\right.\right)-aF\left(\frac{\pi}{4}-cz\left|\frac{2b}{a+b}\right.\right)\right)\sqrt{\frac{a+b\sin(2cz)}{a+b}}\right)$$

01.06.21.0921.01

$$\int (a + b \sin(2cz))^{3/2} \sin^3(cz) dz =$$

$$\frac{1}{192b^{3/2}c} \left( -3(a+7b)\tan^{-1}\left(\frac{\sqrt{b}(\cos(cz)-\sin(cz))}{\sqrt{a+b\sin(2cz)}}\right)(a+b)^2 + 3(a^3+15b^2a)\tanh^{-1}\left(\frac{\sqrt{b}(\cos(cz)+\sin(cz))}{\sqrt{a+b\sin(2cz)}}\right) - \right.$$

$$\sqrt{b}\left(21\log\left(\sqrt{b}\cos(cz)+\sqrt{b}\sin(cz)+\sqrt{a+b\sin(2cz)}\right)b^{5/2} + 18\sqrt{a+b\sin(2cz)}\sin(3cz)b^2 - \right.$$

$$4\sqrt{a+b\sin(2cz)}\sin(5cz)b^2 - 20\sin(cz)\sqrt{a+b\sin(2cz)}b^2 +$$

$$90a\cos(cz)\sqrt{a+b\sin(2cz)}b - 14a\cos(3cz)\sqrt{a+b\sin(2cz)}b +$$

$$\left. \left. 27a^2\log\left(\sqrt{b}\cos(cz)+\sqrt{b}\sin(cz)+\sqrt{a+b\sin(2cz)}\right)\sqrt{b} + 6a^2\sin(cz)\sqrt{a+b\sin(2cz)}\right)\right)$$

01.06.21.0922.01

$$\int (a + b \sin(2cz))^{3/2} \sin^4(cz) dz = \frac{1}{560bc\sqrt{a+b\sin(2cz)}} \left( 4\left( -\frac{14(2a^2+b^2)(\cos(cz)+1)^2 \left(\frac{a+b\sin(2cz)}{(\cos(cz)+1)^2}\right)^{3/2}}{\sqrt{\sec^4\left(\frac{cz}{2}\right)(a+b\sin(2cz))}} - \frac{1}{b}\left( 2a(a^2+33b^2)\left( (a+b)E\left(\frac{\pi}{4}-cz\left|\frac{2b}{a+b}\right.\right) - aF\left(\frac{\pi}{4}-cz\left|\frac{2b}{a+b}\right.\right) \right) \right. \right.$$

$$\left. \left. \sqrt{\frac{a+b\sin(2cz)}{a+b}}\right) - b\sqrt{\frac{a+b\sin(2cz)}{a+b}}(53a^2+15b^2)F\left(\frac{\pi}{4}-cz\left|\frac{2b}{a+b}\right.\right) \right) +$$

$$\left. (a+b\sin(2cz))\left((4a^2-55b^2)\cos(2cz)+b(28b\cos(4cz)-5b\cos(6cz)+16a(\sin(4cz)-7\sin(2cz)))\right)\right)$$

01.06.21.0923.01

$$\int \sqrt{a + b \sin(2 c z)} \sin^2(c z) dz =$$

$$-\frac{1}{24 b c \sqrt{a + b \sin(2 c z)}} \left( -2 \cos(4 c z) b^2 + 2 b^2 + 12 \sqrt{\frac{a + b \sin(2 c z)}{a + b}} (a + b) E\left(\frac{\pi}{4} - c z \mid \frac{2 b}{a + b}\right) b + \right.$$

$$4 a \sin(2 c z) b + a \sqrt{\frac{a + b \sin(2 c z)}{(\cos(c z) + 1)^2}} \cos(2 c z) \sqrt{\sec^4\left(\frac{c z}{2}\right) (a + b \sin(2 c z))} +$$

$$\left. 3 a \sqrt{\frac{a + b \sin(2 c z)}{(\cos(c z) + 1)^2}} \sqrt{\sec^4\left(\frac{c z}{2}\right) (a + b \sin(2 c z))} + 4 a \cos(c z) \sqrt{\frac{a + b \sin(2 c z)}{(\cos(c z) + 1)^2}} \sqrt{\sec^4\left(\frac{c z}{2}\right) (a + b \sin(2 c z))} \right)$$

01.06.21.0924.01

$$\int \sqrt{a + b \sin(2 c z)} \sin^3(c z) dz =$$

$$\frac{1}{32 b^{3/2} c} \left( -(a^2 + 6 b a + 5 b^2) \tan^{-1}\left(\frac{\sqrt{b} (\cos(c z) - \sin(c z))}{\sqrt{a + b \sin(2 c z)}}\right) + (a^2 + 5 b^2) \tanh^{-1}\left(\frac{\sqrt{b} (\cos(c z) + \sin(c z))}{\sqrt{a + b \sin(2 c z)}}\right) - \right.$$

$$2 \sqrt{b} \left( 6 b \sqrt{a + b \sin(2 c z)} \cos(c z) + 3 a \sqrt{b} \log\left(\sqrt{b} \cos(c z) + \sqrt{b} \sin(c z) + \sqrt{a + b \sin(2 c z)}\right) - \right.$$

$$\left. \left. b \cos(3 c z) \sqrt{a + b \sin(2 c z)} + a \sin(c z) \sqrt{a + b \sin(2 c z)} \right) \right)$$

01.06.21.0925.01

$$\int \sqrt{a + b \sin(2 c z)} \sin^4(c z) dz = \frac{1}{120 b c \sqrt{a + b \sin(2 c z)}} \left( 2 \left( -\frac{20 a (\cos(c z) + 1)^2}{\sqrt{\sec^4\left(\frac{c z}{2}\right) (a + b \sin(2 c z))}} \left(\frac{a + b \sin(2 c z)}{(\cos(c z) + 1)^2}\right)^{3/2} - \frac{2 a^2 + 21 b^2}{b} \left( (a + b) E\left(\frac{\pi}{4} - c z \mid \frac{2 b}{a + b}\right) - a F\left(\frac{\pi}{4} - c z \mid \frac{2 b}{a + b}\right) \right) \right. \right.$$

$$\left. \left. \sqrt{\frac{a + b \sin(2 c z)}{a + b}} - 23 a b \sqrt{\frac{a + b \sin(2 c z)}{a + b}} F\left(\frac{\pi}{4} - c z \mid \frac{2 b}{a + b}\right) \right) + \right.$$

$$\left. (a + b \sin(2 c z)) (2 a \cos(2 c z) - 20 b \sin(2 c z) + 3 b \sin(4 c z)) \right)$$

01.06.21.0926.01

$$\int \frac{\sin^2(c z)}{\sqrt{a + b \sin(2 c z)}} dz = -\frac{1}{2 b c \sqrt{a + b \sin(2 c z)}} \left( 2 \sqrt{\frac{a + b \sin(2 c z)}{(\cos(c z) + 1)^2}} \sqrt{\sec^4\left(\frac{c z}{2}\right) (a + b \sin(2 c z))} \cos^4\left(\frac{c z}{2}\right) + b \sqrt{\frac{a + b \sin(2 c z)}{a + b}} F\left(\frac{\pi}{4} - c z \mid \frac{2 b}{a + b}\right) \right)$$

01.06.21.0927.01

$$\int \frac{\sin^3(cz)}{\sqrt{a+b \sin(2cz)}} dz = \frac{1}{8b^{3/2}c} \left( -(a+3b) \tan^{-1} \left( \frac{\sqrt{b}(\cos(cz) - \sin(cz))}{\sqrt{a+b \sin(2cz)}} \right) + a \tanh^{-1} \left( \frac{\sqrt{b}(\cos(cz) + \sin(cz))}{\sqrt{a+b \sin(2cz)}} \right) - 3b \log \left( \sqrt{b} \cos(cz) + \sqrt{b} \sin(cz) + \sqrt{a+b \sin(2cz)} \right) - 2\sqrt{b} \sin(cz) \sqrt{a+b \sin(2cz)} \right)$$

01.06.21.0928.01

$$\int \frac{\sin^4(cz)}{\sqrt{a+b \sin(2cz)}} dz = \frac{1}{24b^2c \sqrt{a+b \sin(2cz)}} \left( -4a \sqrt{\frac{a+b \sin(2cz)}{a+b}} (a+b) E \left( \frac{\pi}{4} - cz \mid \frac{2b}{a+b} \right) + 2 \sqrt{\frac{a+b \sin(2cz)}{a+b}} (2a^2 - 5b^2) F \left( \frac{\pi}{4} - cz \mid \frac{2b}{a+b} \right) + b \left( -12 \sqrt{\frac{a+b \sin(2cz)}{(\cos(cz)+1)^2}} \sqrt{\sec^4 \left( \frac{cz}{2} \right) (a+b \sin(2cz))} \cos(cz) + \cos(2cz) \left( 2a - 3 \sqrt{\frac{a+b \sin(2cz)}{(\cos(cz)+1)^2}} \sqrt{\sec^4 \left( \frac{cz}{2} \right) (a+b \sin(2cz))} \right) + b \sin(4cz) - 9 \sqrt{\frac{a+b \sin(2cz)}{(\cos(cz)+1)^2}} \sqrt{\sec^4 \left( \frac{cz}{2} \right) (a+b \sin(2cz))} \right) \right)$$

01.06.21.0929.01

$$\int \frac{\sin^2(cz)}{(a+b \sin(2cz))^{3/2}} dz = \frac{1}{2(a-b)b(a+b)c \sqrt{a+b \sin(2cz)}} \left( a^2 - b^2 + b^2 \cos(2cz) - b(a+b) E \left( \frac{\pi}{4} - cz \mid \frac{2b}{a+b} \right) \sqrt{\frac{a+b \sin(2cz)}{a+b}} \right)$$

01.06.21.0930.01

$$\int \frac{\sin^3(cz)}{(a+b \sin(2cz))^{3/2}} dz = \frac{1}{4b^{3/2}c} \left( \tan^{-1} \left( \frac{\sqrt{b}(\cos(cz) - \sin(cz))}{\sqrt{a+b \sin(2cz)}} \right) - \tanh^{-1} \left( \frac{\sqrt{b}(\cos(cz) + \sin(cz))}{\sqrt{a+b \sin(2cz)}} \right) - \frac{2\sqrt{b}(ab \cos(cz) - (a^2 - 2b^2) \sin(cz))}{(a^2 - b^2) \sqrt{a+b \sin(2cz)}} \right)$$

01.06.21.0931.01

$$\int \frac{\sin^4(cz)}{(a+b \sin(2cz))^{3/2}} dz = \left( 2 \cos(2cz) b^3 - 2b^3 + 2a^2 b - a^2 \cos(2cz) b + \sqrt{\frac{a+b \sin(2cz)}{a+b}} (2a^3 + 2ba^2 - 3b^2 a - 3b^3) E \left( \frac{\pi}{4} - cz \mid \frac{2b}{a+b} \right) - 2a(a^2 - b^2) F \left( \frac{\pi}{4} - cz \mid \frac{2b}{a+b} \right) \sqrt{\frac{a+b \sin(2cz)}{a+b}} \right) / \left( 4(a-b)b^2(a+b)c \sqrt{a+b \sin(2cz)} \right)$$



Involving  $\sin(e z) \sin(d z) (a + b \sin(c z))^\beta$

01.06.21.0932.01

$$\int \sin(e z) \sin(d z) (a + b \sin(c z))^\beta dz =$$

$$\frac{1}{4} i \left( 1 + \frac{i b e^{i c z}}{\sqrt{a^2 - b^2} - a} \right)^{-\beta} \left( 1 - \frac{i b e^{i c z}}{a + \sqrt{a^2 - b^2}} \right)^{-\beta} \left( a - \frac{1}{2} i b e^{-i c z} (-1 + e^{2 i c z}) \right)^\beta \left( \frac{1}{c^2 \beta^2 - (d - e)^2} \right.$$

$$\left. \left( e^{-i(d-e)z} \left( e^{2i(d-e)z} (d - e + c \beta) F_1 \left( \frac{d - e - c \beta}{c}; -\beta, -\beta; \frac{-\beta c + c + d - e}{c}; \frac{i b e^{i c z}}{a + \sqrt{a^2 - b^2}}, \frac{i b e^{i c z}}{a - \sqrt{a^2 - b^2}} \right) - (d - e - \right. \right.$$

$$\left. \left. c \beta) F_1 \left( -\frac{d - e + c \beta}{c}; -\beta, -\beta; \frac{-\beta c + c - d + e}{c}; \frac{i b e^{i c z}}{a + \sqrt{a^2 - b^2}}, \frac{i b e^{i c z}}{a - \sqrt{a^2 - b^2}} \right) \right) \right) - \frac{1}{c^2 \beta^2 - (d + e)^2}$$

$$\left( e^{-i(d+e)z} \left( e^{2i(d+e)z} (d + e + c \beta) F_1 \left( \frac{d + e - c \beta}{c}; -\beta, -\beta; \frac{-\beta c + c + d + e}{c}; \frac{i b e^{i c z}}{a + \sqrt{a^2 - b^2}}, \frac{i b e^{i c z}}{a - \sqrt{a^2 - b^2}} \right) - \right.$$

$$\left. \left. (d + e - c \beta) F_1 \left( -\frac{d + e + c \beta}{c}; -\beta, -\beta; -\frac{d + e + c(\beta - 1)}{c}; \frac{i b e^{i c z}}{a + \sqrt{a^2 - b^2}}, \frac{i b e^{i c z}}{a - \sqrt{a^2 - b^2}} \right) \right) \right) \right)$$

Involving  $(a + b \sin^2(c z))^\beta$

01.06.21.0933.01

$$\int (a + b \sin^2(c z))^\beta dz = \frac{1}{b c (\beta + 1)} 2^{-\beta - 1} \sqrt{\frac{b \cos^2(c z)}{a + b}} (2 a + b - b \cos(2 c z))^{\beta + 1}$$

$$\csc(2 c z) \sqrt{-\frac{b \sin^2(c z)}{a}} F_1 \left( \beta + 1; \frac{1}{2}, \frac{1}{2}; \beta + 2; \frac{2 a + b - b \cos(2 c z)}{2(a + b)}, \frac{2 a + b - b \cos(2 c z)}{2 a} \right)$$

01.06.21.0934.01

$$\int (a + b \sin^2(c z))^{5/2} dz = \left( 16 \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} a (23 a^2 + 23 b a + 8 b^2) E \left( c z \left| -\frac{b}{a} \right. \right) - \right.$$

$$64 a (2 a^2 + 3 b a + b^2) \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} F \left( c z \left| -\frac{b}{a} \right. \right) -$$

$$\left. \sqrt{2} b (88 a^2 + 88 b a + 25 b^2 - 28 b (2 a + b) \cos(2 c z) + 3 b^2 \cos(4 c z)) \sin(2 c z) \right) / \left( 240 c \sqrt{2 a + b - b \cos(2 c z)} \right)$$

01.06.21.0935.01

$$\int (a + b \sin^2(cz))^{3/2} dz = \frac{1}{24c\sqrt{2a+b-b\cos(2cz)}} \left( 16\sqrt{\frac{2a+b-b\cos(2cz)}{a}} a(2a+b) E\left(cz \mid -\frac{b}{a}\right) - 8a(a+b)\sqrt{\frac{2a+b-b\cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right) + 2\sqrt{2} b(-2a-b+b\cos(2cz)) \sin(2cz) \right)$$

01.06.21.0936.01

$$\int \sqrt{a + b \sin^2(cz)} dz = \frac{\sqrt{2a+b-b\cos(2cz)}}{c\sqrt{\frac{2a+b-b\cos(2cz)}{a}}} E\left(cz \mid -\frac{b}{a}\right)$$

01.06.21.0937.01

$$\int \frac{1}{\sqrt{a + b \sin^2(cz)}} dz = \frac{1}{c\sqrt{2a+b-b\cos(2cz)}} \sqrt{\frac{2a+b-b\cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right)$$

01.06.21.0938.01

$$\int \frac{1}{(a + b \sin^2(cz))^{3/2}} dz = \frac{1}{2a(a+b)c\sqrt{2a+b-b\cos(2cz)}} \left( 2\sqrt{\frac{2a+b-b\cos(2cz)}{a}} a E\left(cz \mid -\frac{b}{a}\right) + \sqrt{2} b \sin(2cz) \right)$$

01.06.21.0939.01

$$\int \frac{1}{(a + b \sin^2(cz))^{5/2}} dz = \left( 2a^2(2a+b) E\left(cz \mid -\frac{b}{a}\right) \left(\frac{2a+b-b\cos(2cz)}{a}\right)^{3/2} - a^2(a+b) F\left(cz \mid -\frac{b}{a}\right) \left(\frac{2a+b-b\cos(2cz)}{a}\right)^{3/2} - \sqrt{2} b(-5a^2 - 5ba - b^2 + b(2a+b)\cos(2cz)) \sin(2cz) \right) / (3a^2(a+b)^2 c(2a+b-b\cos(2cz))^{3/2})$$

Involving  $(a + b \sin^2(cz))^\beta \sin(dz)$

01.06.21.0940.01

$$\int (a + b \sin^2(cz))^\beta \sin(dz) dz = -\frac{1}{d^2 - 4c^2\beta^2} \left( 2^{-2\beta-1} e^{-idz} \left( 1 - \frac{b e^{2icz}}{2a+b-2\sqrt{a(a+b)}} \right)^{-\beta} \left( 1 - \frac{b e^{2icz}}{2a+b+2\sqrt{a(a+b)}} \right)^{-\beta} (4a - b e^{-2icz} (-1 + e^{2icz})^2)^\beta \right. \\ \left. \left( (d - 2c\beta) F_1\left(-\frac{d+2c\beta}{2c}; -\beta, -\beta; -\frac{d}{2c} - \beta + 1; \frac{b e^{2icz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a+b-2\sqrt{a(a+b)}}\right) + e^{2idz} (d + 2c\beta) F_1\left(\frac{d}{2c} - \beta; -\beta, -\beta; \frac{d}{2c} - \beta + 1; \frac{b e^{2icz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a+b-2\sqrt{a(a+b)}}\right) \right) \right)$$

01.06.21.0941.01

$$\int (a + b \sin^2(cz))^\beta \sin(cz) dz = -\frac{\cos(cz) (-b \cos^2(cz) + a + b)^\beta}{c} \left(1 - \frac{b \cos^2(cz)}{a + b}\right)^{-\beta} {}_2F_1\left(\frac{1}{2}, -\beta; \frac{3}{2}; \frac{b \cos^2(cz)}{a + b}\right)$$

01.06.21.0942.01

$$\int (a - a \sin^2(cz))^\beta \sin(dz) dz = \frac{1}{4c^2 \beta^2 - d^2} \left(2^{-2\beta-1} e^{-idz} (e^{-icz} + e^{icz})^{2\beta} (1 + e^{2icz})^{-2\beta} \cos^{-2\beta}(cz) (a \cos^2(cz))^\beta \right. \\ \left. \left( (d - 2c\beta) {}_2F_1\left(-\frac{d + 2c\beta}{2c}, -2\beta; -\frac{d}{2c} - \beta + 1; -e^{2icz}\right) + e^{2idz} (d + 2c\beta) {}_2F_1\left(\frac{d}{2c} - \beta, -2\beta; \frac{d}{2c} - \beta + 1; -e^{2icz}\right) \right) \right)$$

01.06.21.0943.01

$$\int \sin(cz) (b \sin^2(cz) + a)^{3/2} dz = -\frac{1}{8c} \\ \left( \frac{3 \log(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)}) (a + b)^2}{\sqrt{-b}} + \frac{\cos(cz) \sqrt{2a + b - b \cos(2cz)} (5a + 4b - b \cos(2cz))}{\sqrt{2}} \right)$$

01.06.21.0944.01

$$\int \sqrt{a + b \sin^2(cz)} \sin(cz) dz = \\ -\frac{1}{4c} \left( \sqrt{2} \sqrt{2a + b - b \cos(2cz)} \cos(cz) + \frac{2(a + b) \log(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)})}{\sqrt{-b}} \right)$$

01.06.21.0945.01

$$\int \sqrt{a + a \sin^2(cz)} \sin(cz) dz = \\ -\frac{1}{2c \sqrt{\cos(2cz) - 3}} \left( (\cos(cz) \sqrt{\cos(2cz) - 3} - 2\sqrt{2} \log(\sqrt{2} \cos(cz) + \sqrt{\cos(2cz) - 3})) \sqrt{a(\sin^2(cz) + 1)} \right)$$

01.06.21.0946.01

$$\int \sqrt{a - a \sin^2(cz)} \sin(cz) dz = -\frac{\cos(cz) \sqrt{a \cos^2(cz)}}{2c}$$

01.06.21.0947.01

$$\int \frac{\sin(cz)}{\sqrt{a + b \sin^2(cz)}} dz = \frac{b \log(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)})}{(-b)^{3/2} c}$$

01.06.21.0948.01

$$\int \frac{\sin(cz)}{\sqrt{a + a \sin^2(cz)}} dz = \frac{a(\cos(2cz) - 3)^{3/2} \log(\sqrt{2} \cos(cz) + \sqrt{\cos(2cz) - 3})}{c(-a(\cos(2cz) - 3))^{3/2}}$$

01.06.21.0949.01

$$\int \frac{\sin(cz)}{\sqrt{a - a \sin^2(cz)}} dz = -\frac{\cos(cz) \log(\cos(cz))}{c \sqrt{a \cos^2(cz)}}$$

01.06.21.0950.01

$$\int \frac{\sin(c z)}{(a + b \sin^2(c z))^{3/2}} dz = -\frac{\sqrt{2} \cos(c z)}{(a + b) c \sqrt{2 a + b - b \cos(2 c z)}}$$

01.06.21.0951.01

$$\int \frac{\sin(c z)}{(a + b \sin^2(c z))^{5/2}} dz = \frac{2 \sqrt{2} \cos(c z) (-3 a - 2 b + b \cos(2 c z))}{3 (a + b)^2 c (2 a + b - b \cos(2 c z))^{3/2}}$$

01.06.21.0952.01

$$\int \frac{\sin(c z)}{(b \sin^2(c z) + a)^{7/2}} dz = -\frac{4 \sqrt{2} \cos(c z) (15 a^2 + 20 b a + 8 b^2 - 2 b (5 a + 3 b) \cos(2 c z) + b^2 \cos(4 c z))}{15 (a + b)^3 c (2 a + b - b \cos(2 c z))^{5/2}}$$

01.06.21.0953.01

$$\int (a + b \sin^2(c z))^\beta \sin(2 c z) dz = \frac{(2 a + b - b \cos(2 c z)) (b \sin^2(c z) + a)^\beta}{2 b c (\beta + 1)}$$

Involving  $((a + b \sin^2(c z))^v)^\beta$

01.06.21.0954.01

$$\int ((a + b \sin^2(c z))^v)^\beta dz = \frac{1}{b c (\beta v + 1)} \left( 2^{-\beta v - 1} F_1 \left( \beta v + 1; \frac{1}{2}, \frac{1}{2}; \beta v + 2; \frac{2 a + b - b \cos(2 c z)}{2 (a + b)}, \frac{2 a + b - b \cos(2 c z)}{2 a} \right) \sqrt{\frac{b \cos^2(c z)}{a + b}} \right. \\ \left. (2 a + b - b \cos(2 c z))^{\beta v + 1} \csc(2 c z) \sqrt{-\frac{b \sin^2(c z)}{a}} (b \sin^2(c z) + a)^{-\beta v} ((b \sin^2(c z) + a)^v)^\beta \right)$$

01.06.21.0955.01

$$\int \sqrt{(a + b \sin^2(c z))^5} dz = -\left( \sqrt{(2 a + b - b \cos(2 c z))^5} \left( -32 \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} a (23 a^2 + 23 b a + 8 b^2) E \left( c z \left| -\frac{b}{a} \right. \right) + 128 \right. \right. \\ \left. \left. \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} a (2 a^2 + 3 b a + b^2) F \left( c z \left| -\frac{b}{a} \right. \right) + 2 \sqrt{2} b \right) \right) / (480 c (2 a + b - b \cos(2 c z))^3)$$

01.06.21.0956.01

$$\int \sqrt{(a + b \sin^2(c z))^3} dz =$$

$$\left( \sqrt{(b \sin^2(c z) + a)^3} \left( 16 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(2a + b) E\left(cz \mid -\frac{b}{a}\right) - 8a(a + b) \sqrt{\frac{2a + b - b \cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right) + \right. \right.$$

$$\left. \left. 2\sqrt{2} b(-2a - b + b \cos(2cz)) \sin(2cz) \right) \right) / (6\sqrt{2} c(2a + b - b \cos(2cz))^2)$$

01.06.21.0957.01

$$\int \frac{1}{\sqrt{(a + b \sin^2(c z))^3}} dz = \frac{(2a + b - b \cos(2cz)) \left( 2 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a E\left(cz \mid -\frac{b}{a}\right) + \sqrt{2} b \sin(2cz) \right)}{2a(a + b) c \sqrt{(2a + b - b \cos(2cz))^3}}$$

01.06.21.0958.01

$$\int \frac{1}{\sqrt{(a + b \sin^2(c z))^5}} dz =$$

$$\left( (b \sin^2(c z) + a)^{5/2} \left( 2a^2(2a + b) E\left(cz \mid -\frac{b}{a}\right) \left( \frac{2a + b - b \cos(2cz)}{a} \right)^{3/2} - a^2(a + b) F\left(cz \mid -\frac{b}{a}\right) \left( \frac{2a + b - b \cos(2cz)}{a} \right)^{3/2} - \right. \right.$$

$$\left. \left. \sqrt{2} b(-5a^2 - 5ba - b^2 + b(2a + b) \cos(2cz)) \sin(2cz) \right) \right) /$$

$$\left( 3a^2(a + b)^2 c(2a + b - b \cos(2cz))^{3/2} \sqrt{(b \sin^2(c z) + a)^5} \right)$$

Involving  $\left( (a + b \sin^2(c z))^y \right)^\beta \sin(dz)$

01.06.21.0959.01

$$\int \left( (a + b \sin^2(cz))^{\nu} \right)^{\beta} \sin(dz) dz = -\frac{1}{d^2 - 4c^2\beta^2\nu^2} \left( 2^{-\beta\nu-1} e^{-idz} \left( 1 - \frac{b e^{2icz}}{2a+b-2\sqrt{a(a+b)}} \right)^{-\beta\nu} \left( 1 - \frac{b e^{2icz}}{2a+b+2\sqrt{a(a+b)}} \right)^{-\beta\nu} (4a - b e^{-2icz} (-1 + e^{2icz})^2)^{\beta\nu} \right. \\ \left. \left( (d - 2c\beta\nu) F_1 \left( -\frac{d+2c\beta\nu}{2c}; -\beta\nu, -\beta\nu; -\frac{d}{2c} - \beta\nu + 1; \frac{b e^{2icz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a+b-2\sqrt{a(a+b)}} \right) + e^{2idz} (d + 2c\beta\nu) F_1 \left( \frac{d}{2c} - \beta\nu; -\beta\nu, -\beta\nu; \frac{d}{2c} - \beta\nu + 1; \frac{b e^{2icz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a+b-2\sqrt{a(a+b)}} \right) \right) \right) \\ (2a + b - b \cos(2cz))^{-\beta\nu} \left( (b \sin^2(cz) + a)^{\nu} \right)^{\beta}$$

01.06.21.0960.01

$$\int \left( (a + b \sin^2(cz))^{\nu} \right)^{\beta} \sin(cz) dz = -\frac{1}{c} \cos(cz) (-b \cos^2(cz) + a + b)^{\beta\nu} (b \sin^2(cz) + a)^{-\beta\nu} \left( (b \sin^2(cz) + a)^{\nu} \right)^{\beta} \left( 1 - \frac{b \cos^2(cz)}{a+b} \right)^{-\beta\nu} {}_2F_1 \left( \frac{1}{2}, -\beta\nu; \frac{3}{2}; \frac{b \cos^2(cz)}{a+b} \right)$$

01.06.21.0961.01

$$\int \sqrt{(a + b \sin^2(cz))^5} \sin(cz) dz = \frac{1}{16c(a + b \sin^2(cz))^{5/2}} \left( \left( -\frac{5 \log(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a+b-b \cos(2cz)}) (a+b)^3}{\sqrt{-b}} - \frac{1}{3\sqrt{2}} (\cos(cz) \sqrt{2a+b-b \cos(2cz)} (33a^2 + 53ba + 23b^2 - b(13a+9b) \cos(2cz) + b^2 \cos(4cz))) \right) \sqrt{(b \sin^2(cz) + a)^5} \right)$$

01.06.21.0962.01

$$\int \sqrt{(a + b \sin^2(cz))^3} \sin(cz) dz = \frac{1}{8c(b \sin^2(cz) + a)^{3/2}} \left( \left( -\frac{3 \log(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a+b-b \cos(2cz)}) (a+b)^2}{\sqrt{-b}} - \frac{\cos(cz) \sqrt{2a+b-b \cos(2cz)} (5a+4b-b \cos(2cz))}{\sqrt{2}} \right) \sqrt{(b \sin^2(cz) + a)^3} \right)$$

01.06.21.0963.01

$$\int \frac{\sin(cz)}{\sqrt{(a + b \sin^2(cz))^3}} dz = -\frac{\sqrt{2} \cos(cz) (2a + b - b \cos(2cz))}{(a + b)c \sqrt{(2a + b - b \cos(2cz))^3}}$$

01.06.21.0964.01

$$\int \frac{\sin(c z)}{\sqrt{(a+b \sin^2(c z))^5}} dz = -\frac{\cos(c z)(2 a+b-b \cos(2 c z))(3 a+2 b-b \cos(2 c z))}{6(a+b)^2 c \sqrt{(b \sin^2(c z)+a)^5}}$$

01.06.21.0965.01

$$\int \left((a+b \sin^2(c z))^{\nu}\right)^{\beta} \sin(2 c z) dz = \frac{(2 a+b-b \cos(2 c z))\left((b \sin^2(c z)+a)^{\nu}\right)^{\beta}}{2 b c(\beta \nu+1)}$$

01.06.21.0966.01

$$\int \left((a+b \sin^2(c z))^{\nu}\right)^{\beta} \sin(4 c z) dz = \frac{(2 a+b-b \cos(2 c z))(2 a+b+b(\beta \nu+1) \cos(2 c z))\left((b \sin^2(c z)+a)^{\nu}\right)^{\beta}}{b^2 c(\beta \nu+1)(\beta \nu+2)}$$

Involving  $(a+b \sin^2(c z))^{\beta} \sin^{\nu}(c z)$

01.06.21.0967.01

$$\int (a+b \sin^2(c z))^{\beta} \sin^{\nu}(c z) dz = \frac{1}{\nu c+c}$$

$$\left(2^{\beta} F_1\left(\frac{\nu+1}{2}; \frac{1}{2}, -\beta; \frac{\nu+3}{2}; \sin^2(c z), -\frac{b \sin^2(c z)}{a}\right) \sqrt{\cos^2(c z)} \sec(c z) \sin^{\nu+1}(c z) (b \sin^2(c z)+a)^{\beta} \left(\frac{2 b \sin^2(c z)}{a}+2\right)^{-\beta}\right)$$

01.06.21.0968.01

$$\int (a+b \sin^2(c z))^{3/2} \sin^2(c z) dz = \left(16 \sqrt{\frac{2 a+b-b \cos(2 c z)}{a}} a\left(3 a^2+13 b a+8 b^2\right) E\left(c z \mid -\frac{b}{a}\right)-\right.$$

$$16 a\left(3 a^2+7 b a+4 b^2\right) \sqrt{\frac{2 a+b-b \cos(2 c z)}{a}} F\left(c z \mid -\frac{b}{a}\right)-$$

$$\left.\sqrt{2} b\left(48 a^2+68 b a+25 b^2-4 b(9 a+7 b) \cos(2 c z)+3 b^2 \cos(4 c z)\right) \sin(2 c z)\right) / \left(240 b c \sqrt{2 a+b-b \cos(2 c z)}\right)$$

01.06.21.0969.01

$$\int (a+b \sin^2(c z))^{3/2} \sin^3(c z) dz = \frac{1}{16 c} \left(\frac{(a+b)^2(5 b-a) \log\left(\sqrt{2} \sqrt{-b} \cos(c z)+\sqrt{2 a+b-b \cos(2 c z)}\right)}{(-b)^{3/2}}-\right.$$

$$\left.\frac{1}{3 \sqrt{2} b}\left(\cos(c z) \sqrt{2 a+b-b \cos(2 c z)}\left(3 a^2+29 b a+23 b^2-b(7 a+9 b) \cos(2 c z)+b^2 \cos(4 c z)\right)\right)\right)$$

01.06.21.0970.01

$$\int (a + b \sin^2(cz))^{3/2} \sin^4(cz) dz = \left( -128 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(a^3 - 2ba^2 - 12b^2a - 8b^3) E\left(cz \mid -\frac{b}{a}\right) + \right. \\ \left. 64 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(2a^3 - 3ba^2 - 13b^2a - 8b^3) F\left(cz \mid -\frac{b}{a}\right) + \right. \\ \left. \sqrt{2} b(-32a^3 - 496ba^2 - 684b^2a - 250b^3 + b(144a^2 + 480ba + 299b^2) \cos(2cz) - \right. \\ \left. 2b^2(26a + 27b) \cos(4cz) + 5b^3 \cos(6cz)) \sin(2cz) \right) / \left( 2240b^2c \sqrt{2a + b - b \cos(2cz)} \right)$$

01.06.21.0971.01

$$\int \sqrt{a + b \sin^2(cz)} \sin^2(cz) dz = \left( 8 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(a + 2b) E\left(cz \mid -\frac{b}{a}\right) - 8a(a + b) \sqrt{\frac{2a + b - b \cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right) + \right. \\ \left. 2\sqrt{2} b(-2a - b + b \cos(2cz)) \sin(2cz) \right) / \left( 24bc \sqrt{2a + b - b \cos(2cz)} \right)$$

01.06.21.0972.01

$$\int \sqrt{a + b \sin^2(cz)} \sin^3(cz) dz = \frac{1}{8c} \left( \frac{\cos(cz) \sqrt{2a + b - b \cos(2cz)} (-a - 4b + b \cos(2cz))}{\sqrt{2} b} + \right. \\ \left. \frac{(a + b)(3b - a) \log\left(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)}\right)}{(-b)^{3/2}} \right)$$

01.06.21.0973.01

$$\int \sqrt{a + b \sin^2(cz)} \sin^4(cz) dz = \left( -16 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(2a^2 - 3ba - 8b^2) E\left(cz \mid -\frac{b}{a}\right) + 32 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(a^2 - ba - 2b^2) F\left(cz \mid -\frac{b}{a}\right) - \right. \\ \left. \sqrt{2} b(8a^2 + 48ba + 25b^2 - 4b(4a + 7b) \cos(2cz) + 3b^2 \cos(4cz)) \sin(2cz) \right) / \left( 240b^2c \sqrt{2a + b - b \cos(2cz)} \right)$$



01.06.21.0974.01

$$\int \sqrt{a + b \sin^2(cz)} \sin^5(cz) dz = \frac{1}{96c} \left( \frac{1}{b^2} \left( \sqrt{2} \cos(cz) \sqrt{2a + b - b \cos(2cz)} (3a^2 - 5ba - 23b^2 + b(a + 9b) \cos(2cz) - b^2 \cos(4cz)) \right) - \frac{1}{(-b)^{5/2}} \left( 6(a + b)(a^2 - 2ba + 5b^2) \log\left(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)}\right) \right) \right)$$

01.06.21.0975.01

$$\int \frac{\sin^\nu(cz)}{\sqrt{a + b \sin^2(cz)}} dz = F_1\left(\frac{\nu + 1}{2}; \frac{1}{2}, \frac{1}{2}; \frac{\nu + 3}{2}; \sin^2(cz), -\frac{b \sin^2(cz)}{a}\right) \sqrt{\cos^2(cz)} \sqrt{\frac{2a + b - b \cos(2cz)}{a}} \sec(cz) \sin^{\nu+1}(cz) / \left(c(\nu + 1) \sqrt{2b \sin^2(cz) + 2a}\right)$$

01.06.21.0976.01

$$\int \frac{\sin^2(cz)}{\sqrt{a + b \sin^2(cz)}} dz = \frac{\sqrt{2a + b - b \cos(2cz)} \left(E\left(cz \mid -\frac{b}{a}\right) - F\left(cz \mid -\frac{b}{a}\right)\right)}{bc \sqrt{\frac{2a + b - b \cos(2cz)}{a}}}$$

01.06.21.0977.01

$$\int \frac{\sin^3(cz)}{\sqrt{a + b \sin^2(cz)}} dz = -\frac{1}{4(-b)^{3/2}c} \left( 2(a - b) \log\left(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)}\right) - \sqrt{2} \sqrt{-b} \cos(cz) \sqrt{2a + b - b \cos(2cz)} \right)$$

01.06.21.0978.01

$$\int \frac{\sin^4(cz)}{\sqrt{a + b \sin^2(cz)}} dz = \left( -8 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(a - b) E\left(cz \mid -\frac{b}{a}\right) + 4 \sqrt{\frac{2a + b - b \cos(2cz)}{a}} a(2a - b) F\left(cz \mid -\frac{b}{a}\right) + \sqrt{2} b(-2a - b + b \cos(2cz)) \sin(2cz) \right) / \left(12b^2c \sqrt{2a + b - b \cos(2cz)}\right)$$

01.06.21.0979.01

$$\int \frac{\sin^5(cz)}{\sqrt{a + b \sin^2(cz)}} dz = \frac{1}{8c} \left( \frac{\cos(cz) \sqrt{2a + b - b \cos(2cz)} (3a - 4b + b \cos(2cz))}{\sqrt{2} b^2} + \frac{b(3a^2 - 2ba + 3b^2) \log\left(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a + b - b \cos(2cz)}\right)}{(-b)^{7/2}} \right)$$

01.06.21.0980.01

$$\int \frac{\sin^6(cz)}{\sqrt{a+b\sin^2(cz)}} dz = \left( 16 \sqrt{\frac{2a+b-b\cos(2cz)}{a}} a(8a^2-7ba+8b^2) E\left(cz \mid -\frac{b}{a}\right) - \right. \\ \left. 16a(8a^2-3ba+4b^2) \sqrt{\frac{2a+b-b\cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right) - \right. \\ \left. \sqrt{2} b(-32a^2+28ba+25b^2+4b(a-7b)\cos(2cz)+3b^2\cos(4cz)) \sin(2cz) \right) / \left( (240b^3c\sqrt{2a+b-b\cos(2cz)}) \right)$$

01.06.21.0981.01

$$\int \frac{\sin^7(cz)}{\sqrt{a+b\sin^2(cz)}} dz = \frac{1}{16c} \left( \frac{(b-a)(5a^2+2ba+5b^2) \log\left(\sqrt{2}\sqrt{-b}\cos(cz) + \sqrt{2a+b-b\cos(2cz)}\right)}{(-b)^{7/2}} - \right. \\ \left. \frac{1}{3\sqrt{2}b^3} \left( \cos(cz)\sqrt{2a+b-b\cos(2cz)}(15a^2-19ba+23b^2+b(5a-9b)\cos(2cz)+b^2\cos(4cz)) \right) \right)$$

01.06.21.0982.01

$$\int \frac{\sin^2(cz)}{(a+b\sin^2(cz))^{3/2}} dz = \left( -2 \sqrt{\frac{2a+b-b\cos(2cz)}{a}} a E\left(cz \mid -\frac{b}{a}\right) + 2 \sqrt{\frac{2a+b-b\cos(2cz)}{a}} (a+b) F\left(cz \mid -\frac{b}{a}\right) - \sqrt{2} b \sin(2cz) \right) / \\ \left( 2b(a+b)c\sqrt{2a+b-b\cos(2cz)} \right)$$

01.06.21.0983.01

$$\int \frac{\sin^3(cz)}{(a+b\sin^2(cz))^{3/2}} dz = \frac{1}{b^2c} \left( \frac{\sqrt{2}ab\cos(cz)}{(a+b)\sqrt{2a+b-b\cos(2cz)}} + \sqrt{-b} \log\left(\sqrt{2}\sqrt{-b}\cos(cz) + \sqrt{2a+b-b\cos(2cz)}\right) \right)$$

01.06.21.0984.01

$$\int \frac{\sin^4(cz)}{(a+b\sin^2(cz))^{3/2}} dz = \left( a \left( 2 \sqrt{\frac{2a+b-b\cos(2cz)}{a}} (2a+b) E\left(cz \mid -\frac{b}{a}\right) - 4(a+b) \sqrt{\frac{2a+b-b\cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right) + \sqrt{2} b \sin(2cz) \right) \right) / \\ \left( 2b^2(a+b)c\sqrt{2a+b-b\cos(2cz)} \right)$$

01.06.21.0985.01

$$\int \frac{\sin^5(cz)}{(a+b\sin^2(cz))^{3/2}} dz = \frac{1}{2c} \left( \frac{\cos(cz)(-6a^2 - 3ba - b^2 + b(a+b)\cos(2cz))}{\sqrt{2} b^2 (a+b) \sqrt{2a+b-b\cos(2cz)}} + \frac{b(b-3a) \log(\sqrt{2} \sqrt{-b} \cos(cz) + \sqrt{2a+b-b\cos(2cz)})}{(-b)^{7/2}} \right)$$

01.06.21.0986.01

$$\int \frac{\sin^2(cz)}{(a+b\sin^2(cz))^{5/2}} dz = \left( -2a^2(a-b) E\left(cz \mid -\frac{b}{a}\right) \left(\frac{2a+b-b\cos(2cz)}{a}\right)^{3/2} + 2a^2(a+b) F\left(cz \mid -\frac{b}{a}\right) \left(\frac{2a+b-b\cos(2cz)}{a}\right)^{3/2} - \sqrt{2} b(4a^2 + ba - b^2 - (a-b)b\cos(2cz)) \sin(2cz) \right) / (6ab(a+b)^2 c (2a+b-b\cos(2cz))^{3/2})$$

01.06.21.0987.01

$$\int \frac{\sin^3(cz)}{(a+b\sin^2(cz))^{5/2}} dz = \frac{\sqrt{2} \cos(cz)(-5a - 3b + (a+3b)\cos(2cz))}{3(a+b)^2 c (2a+b-b\cos(2cz))^{3/2}}$$

01.06.21.0988.01

$$\int \frac{\sin^4(cz)}{(a+b\sin^2(cz))^{5/2}} dz = - \left( 2a^2(a+2b) E\left(cz \mid -\frac{b}{a}\right) \left(\frac{2a+b-b\cos(2cz)}{a}\right)^{3/2} - a(2a^2 + 5ba + 3b^2) F\left(cz \mid -\frac{b}{a}\right) \left(\frac{2a+b-b\cos(2cz)}{a}\right)^{3/2} - \sqrt{2} b(-a^2 - 4ba - 2b^2 + b(a+2b)\cos(2cz)) \sin(2cz) \right) / (3b^2(a+b)^2 c (2a+b-b\cos(2cz))^{3/2})$$

Involving  $(a+b\sin^2(cz))^\beta$  and rational function of  $\sin(cz)$

01.06.21.0989.01

$$\int \frac{1}{(d+e\sin(cz))\sqrt{a+b\sin^2(cz)}} dz = \frac{1}{ce\sqrt{2a+b-b\cos(2cz)}} \sqrt{\frac{2a+b-b\cos(2cz)}{a}} \left( \frac{e}{d} \Pi\left(\frac{e^2}{d^2}; cz \mid -\frac{b}{a}\right) - \frac{1}{\sqrt{1-\frac{d^2}{e^2}} \sqrt{\frac{bd^2}{ae^2} + 1}} \tanh^{-1} \left( \frac{\cos(cz)}{\sqrt{1-\frac{d^2}{e^2}} \sqrt{\frac{2a+b-b\cos(2cz)}{a}}} \sqrt{\frac{2bd^2}{ae^2} + 2} \right) \right)$$

01.06.21.0990.01

$$\int \frac{\sin(cz)}{(d + e \sin(cz)) \sqrt{a + b \sin^2(cz)}} dz =$$

$$\left( \sqrt{\frac{2a + b - b \cos(2cz)}{a}} \left( \frac{d}{\sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{bd^2}{ae^2} + 1}} \tanh^{-1} \left( \frac{\sqrt{\frac{2bd^2}{ae^2} + 2 \cos(cz)}}{\sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{2a+b-b \cos(2cz)}{a}}} \right) + \right. \right.$$

$$\left. \left. e F\left(cz \mid -\frac{b}{a}\right) - e \Pi\left(\frac{e^2}{d^2}; cz \mid -\frac{b}{a}\right) \right) \right) / (c e^2 \sqrt{2a + b - b \cos(2cz)})$$

01.06.21.0991.01

$$\int \frac{1}{(d + e \sin(cz))^2 \sqrt{a + b \sin^2(cz)}} dz = \frac{\cos(cz) \sqrt{2a + b - b \cos(2cz)} e^3}{\sqrt{2} c (d^2 - e^2) (bd^2 + ae^2) (d + e \sin(cz))} +$$

$$\frac{\tanh^{-1} \left( \frac{\sqrt{\frac{2bd^2}{ae^2} + 2 \cos(cz)}}{\sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{2a+b-b \cos(2cz)}{a}}} \right) \left( d(2bd^2 + ae^2 - be^2) \sqrt{\frac{2a+b-b \cos(2cz)}{a}} \right)}{c \sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{bd^2}{ae^2} + 1} e(e^2 - d^2) (bd^2 + ae^2) \sqrt{2a + b - b \cos(2cz)}} + \frac{(e^2 \sqrt{2a + b - b \cos(2cz)}) E\left(cz \mid -\frac{b}{a}\right)}{c (d^2 - e^2) (bd^2 + ae^2) \sqrt{\frac{2a+b-b \cos(2cz)}{a}}} -$$

$$\frac{\sqrt{\frac{2a+b-b \cos(2cz)}{a}} F\left(cz \mid -\frac{b}{a}\right)}{c (d^2 - e^2) \sqrt{2a + b - b \cos(2cz)}} + \frac{\left( (2bd^2 + ae^2 - be^2) \sqrt{\frac{2a+b-b \cos(2cz)}{a}} \right) \Pi\left(\frac{e^2}{d^2}; cz \mid -\frac{b}{a}\right)}{c (d^2 - e^2) (bd^2 + ae^2) \sqrt{2a + b - b \cos(2cz)}}$$

01.06.21.0992.01

$$\int \frac{1}{(d + e \sin(cz))^3 \sqrt{a + b \sin^2(cz)}} dz = \frac{3 d e^2 (2 b d^2 + a e^2 - b e^2) \sqrt{2 a + b - b \cos(2 c z)} E\left(c z \left| -\frac{b}{a} \right. \right)}{2 c (d^2 - e^2)^2 (b d^2 + a e^2)^2 \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}}} +$$

$$\left( (a^2 (2 d^2 + e^2) e^4 + a b (5 d^4 + 2 e^2 d^2 - e^4) e^2 + b^2 (6 d^6 - 5 e^2 d^4 + 2 e^4 d^2)) \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} \Pi\left(\frac{e^2}{d^2}; c z \left| -\frac{b}{a} \right. \right) \right) /$$

$$\left( 2 c d (d^2 - e^2)^2 (b d^2 + a e^2)^2 \sqrt{2 a + b - b \cos(2 c z)} \right) +$$

$$(4 \sqrt{2} e^3 \cos(c z) (e \sin(c z) - d)^5 (d + e \sin(c z))^3 (-14 b^2 d^4 - 28 a b d^4 + 6 b^2 e \sin(3 c z) d^3 - 16 a^2 e^2 d^2 +$$

$$8 b^2 e^2 d^2 + 8 a b e^2 d^2 - 3 (4 a + 3 b) e (2 b d^2 + a e^2 - b e^2) \sin(c z) d - 3 b^2 e^3 \sin(3 c z) d +$$

$$3 a b e^3 \sin(3 c z) d + 4 a^2 e^4 + 2 a b e^4 + 2 b (7 b d^4 + 4 a e^2 d^2 - 4 b e^2 d^2 - a e^4) \cos(2 c z)) /$$

$$\left( c (d^2 - e^2)^2 (b d^2 + a e^2)^2 \sqrt{2 a + b - b \cos(2 c z)} (2 d^2 - e^2 + e^2 \cos(2 c z))^5 \right) -$$

$$\frac{d (4 b d^2 + 3 a e^2 - b e^2) \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} F\left(c z \left| -\frac{b}{a} \right. \right)}{2 c (d^2 - e^2)^2 (b d^2 + a e^2) \sqrt{2 a + b - b \cos(2 c z)}} -$$

$$\left( (a^2 (2 d^2 + e^2) e^4 + a b (5 d^4 + 2 e^2 d^2 - e^4) e^2 + b^2 (6 d^6 - 5 e^2 d^4 + 2 e^4 d^2)) \tanh^{-1} \left( \frac{\sqrt{\frac{2 b d^2}{a e^2} + 2 \cos(c z)}}{\sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}}} \right) \right)$$

$$\left. \sqrt{\frac{2 a + b - b \cos(2 c z)}{a}} \right) / \left( 2 c \sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{b d^2}{a e^2} + 1} e (d^2 - e^2)^2 (b d^2 + a e^2)^2 \sqrt{2 a + b - b \cos(2 c z)} \right)$$

01.06.21.0993.01

$$\int \frac{\sin(cz)}{(d + e \sin(cz))^2 \sqrt{a + b \sin^2(cz)}} dz =$$

$$\frac{d \cos(cz) \sqrt{2a + b - b \cos(2cz)} e^2}{\sqrt{2} c (d^2 - e^2) (b d^2 + a e^2) (d + e \sin(cz))} - \frac{(b d^4 + a e^4)}{c \sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{b d^2}{a e^2} + 1} e^2 (e^2 - d^2) (b d^2 + a e^2) \sqrt{2a + b - b \cos(2cz)}}$$

$$\sqrt{\frac{2a + b - b \cos(2cz)}{a}} \tanh^{-1} \left( \frac{\sqrt{\frac{2b d^2}{a e^2} + 2} \cos(cz)}{\sqrt{1 - \frac{d^2}{e^2}} \sqrt{\frac{2a + b - b \cos(2cz)}{a}}} \right) - \frac{d e \sqrt{2a + b - b \cos(2cz)}}{c (d^2 - e^2) (b d^2 + a e^2) \sqrt{\frac{2a + b - b \cos(2cz)}{a}}} E \left( cz \left| -\frac{b}{a} \right. \right) +$$

$$\frac{d}{c e (d^2 - e^2) \sqrt{2a + b - b \cos(2cz)}} \sqrt{\frac{2a + b - b \cos(2cz)}{a}} F \left( cz \left| -\frac{b}{a} \right. \right) +$$

$$\frac{(b d^4 + a e^4)}{c d e (e^2 - d^2) (b d^2 + a e^2) \sqrt{2a + b - b \cos(2cz)}} \sqrt{\frac{2a + b - b \cos(2cz)}{a}} \Pi \left( \frac{e^2}{d^2}; cz \left| -\frac{b}{a} \right. \right)$$

01.06.21.0994.01

$$\int \frac{\sqrt{a + b \sin^2(cz)}}{d + e \sin^2(cz)} dz = \frac{\sqrt{\frac{2a + b - b \cos(2cz)}{a}} \left( b d F \left( cz \left| -\frac{b}{a} \right. \right) + (a e - b d) \Pi \left( -\frac{e}{d}; cz \left| -\frac{b}{a} \right. \right) \right)}{c d e \sqrt{2a + b - b \cos(2cz)}}$$

01.06.21.0995.01

$$\int \frac{1}{(e \sin^2(cz) + d) \sqrt{a + b \sin^2(cz)}} dz = \frac{1}{c d \sqrt{2a + b - b \cos(2cz)}} \sqrt{\frac{2a + b - b \cos(2cz)}{a}} \Pi \left( -\frac{e}{d}; cz \left| -\frac{b}{a} \right. \right)$$

01.06.21.0996.01

$$\int \frac{\sin(cz)}{(e \sin^2(cz) + d) \sqrt{a + b \sin^2(cz)}} dz = \frac{1}{c \sqrt{-d - e} \sqrt{a e - b d}} \tan^{-1} \left( \frac{2 \sqrt{a e - b d} \cos(cz)}{\sqrt{-2d - 2e} \sqrt{2a + b - b \cos(2cz)}} \right)$$

01.06.21.0997.01

$$\int \frac{1}{(e \sin^2(cz) + d)^2 \sqrt{a + b \sin^2(cz)}} dz =$$

$$\left( \sqrt{\frac{2a + b - b \cos(2cz)}{a}} \left( 2 \Pi\left(-\frac{e}{d}; cz \mid -\frac{b}{a}\right) - \frac{1}{(d+e)(bd-ae)} \left( ade \left( E\left(cz \mid -\frac{b}{a}\right) + \frac{(bd-ae)F\left(cz \mid -\frac{b}{a}\right)}{ae} \right) + \frac{\sqrt{\frac{b \sin^2(cz)}{a} + 1} e \sin(2cz)}{2(e \sin^2(cz) + d)} - \frac{d\left(\frac{e^2}{d^2} + \frac{b}{a}\right) \Pi\left(-\frac{e}{d}; cz \mid -\frac{b}{a}\right)}{e} \right) \right) \right) / \left( 2cd^2 \sqrt{2a + b - b \cos(2cz)} \right)$$

01.06.21.0998.01

$$\int \frac{\sin(cz)}{(e \sin^2(cz) + d)^2 \sqrt{a + b \sin^2(cz)}} dz =$$

$$\left( (b(2d+e) - ae) \tan^{-1}\left(\frac{2\sqrt{ae-bd} \cos(cz)}{\sqrt{-2d-2e} \sqrt{2a+b-b \cos(2cz)}}\right) - \frac{2e(d+e)\sqrt{ae-bd} \cos(cz) \sqrt{2a+b-b \cos(2cz)}}{\sqrt{-2d-2e} (2d+e-e \cos(2cz))} \right) / (2c(-d-e)^{3/2} (ae-bd)^{3/2})$$

Involving  $\sin(ez) \sin(dz) (a + b \sin^2(cz))^\beta$

01.06.21.0999.01

$$\int \sin(ez) \sin(dz) (a + b \sin^2(cz))^\beta dz = \frac{1}{4} i \left( 1 - \frac{b e^{2icz}}{2a + b - 2\sqrt{a(a+b)}} \right)^{-\beta} \left( 1 - \frac{b e^{2icz}}{2a + b + 2\sqrt{a(a+b)}} \right)^{-\beta}$$

$$(a + b \sin^2(cz))^\beta \left( \frac{1}{4c^2 \beta^2 - (d-e)^2} \left( e^{-i(d-e)z} \left( e^{2i(d-e)z} (d-e+2c\beta) F_1\left(\frac{d-e-2c\beta}{2c}; -\beta, -\beta; \frac{-2\beta c + 2c + d - e}{2c}; \frac{b e^{2icz}}{2a + b + 2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a + b - 2\sqrt{a(a+b)}} \right) - (d-e-2c\beta) F_1\left(-\frac{d-e+2c\beta}{2c}; -\beta, -\beta; \frac{-2\beta c + 2c - d + e}{2c}; \frac{b e^{2icz}}{2a + b + 2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a + b - 2\sqrt{a(a+b)}} \right) \right) \right) - \frac{1}{4c^2 \beta^2 - (d+e)^2} \left( e^{-i(d+e)z} \left( e^{2i(d+e)z} (d+e+2c\beta) F_1\left(\frac{d+e-2c\beta}{2c}; -\beta, -\beta; \frac{-2\beta c + 2c + d + e}{2c}; \frac{b e^{2icz}}{2a + b + 2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a + b - 2\sqrt{a(a+b)}} \right) - (d+e-2c\beta) F_1\left(-\frac{d+e+2c\beta}{2c}; -\beta, -\beta; -\frac{d+e+2c(\beta-1)}{2c}; \frac{b e^{2icz}}{2a + b + 2\sqrt{a(a+b)}}, \frac{b e^{2icz}}{2a + b - 2\sqrt{a(a+b)}} \right) \right) \right)$$

Involving  $(a + b \sin^2(cz))^\beta$  and algebraic function of  $\sin(cz)$

01.06.21.1000.01

$$\int (a + b \sin^2(cz))^y (d + e \sin^2(cz))^\beta \sin(cz) dz = -\frac{1}{c} \left( F_1 \left( \frac{1}{2}; -\nu, -\beta; \frac{3}{2}; \frac{b \cos^2(cz)}{a+b}, \frac{e \cos^2(cz)}{d+e} \right) \cos(cz) (b \sin^2(cz) + a)^y \left( \frac{b \sin^2(cz) + a}{a+b} \right)^{-\nu} (e \sin^2(cz) + d)^\beta \left( \frac{e \sin^2(cz) + d}{d+e} \right)^{-\beta} \right)$$

01.06.21.1001.01

$$\int \frac{(d + e \sin^2(cz))^\beta \sin(cz)}{\sqrt{a + b \sin^2(cz)}} dz = -\frac{1}{c \sqrt{b \sin^2(cz) + a}} \left( F_1 \left( \frac{1}{2}; \frac{1}{2}, -\beta; \frac{3}{2}; \frac{b \cos^2(cz)}{a+b}, \frac{e \cos^2(cz)}{d+e} \right) \cos(cz) \sqrt{\frac{b \sin^2(cz) + a}{a+b}} (e \sin^2(cz) + d)^\beta \left( \frac{e \sin^2(cz) + d}{d+e} \right)^{-\beta} \right)$$

Other integrals

01.06.21.1002.01

$$\int \sqrt{\frac{a + b \sin(ez)}{c + d \sin(ez)}} dz = -\left( \sqrt{2} (bc - ad) \sqrt{\frac{(c + d) \cot^2\left(\frac{1}{4}(\pi - 2ez)\right)}{d - c}} \right. \\ \left. \left( b(c + d) \Pi \left( \frac{ad - bc}{(a + b)d}; \sin^{-1} \left( \sqrt{-\frac{(a + b) \csc^2\left(\frac{1}{4}(\pi - 2ez)\right)(c + d \sin(ez))}{2ad - 2bc}} \right) \right) \left| \frac{2(ad - bc)}{(a + b)(d - c)} \right. \right) - \right. \\ \left. (a + b) d F \left( \sin^{-1} \left( \sqrt{-\frac{(a + b) \csc^2\left(\frac{1}{4}(\pi - 2ez)\right)(c + d \sin(ez))}{2ad - 2bc}} \right) \right) \left| \frac{2(ad - bc)}{(a + b)(d - c)} \right) \right) \\ \sec(ez) \left( \cos\left(\frac{ez}{2}\right) - \sin\left(\frac{ez}{2}\right) \right)^4 \sqrt{\frac{(c + d) \csc^2\left(\frac{1}{4}(\pi - 2ez)\right)(a + b \sin(ez))}{ad - bc}} \sqrt{\frac{a + b \sin(ez)}{c + d \sin(ez)}} \\ \sqrt{\frac{(a + b)(c + d \sin(ez))}{(ad - bc)(\sin(ez) - 1)}} / ((a + b)d(c + d)e(a + b \sin(ez)))$$



01.06.21.1003.01

$$\int \frac{\sqrt{a+b \sin(ez)}}{\sqrt{c+d \sin(ez)}} dz = - \left( \sqrt{2} (bc-ad) \sqrt{\frac{(c+d) \cot^2\left(\frac{1}{4}(\pi-2ez)\right)}{d-c}} \right. \\ \left. \left( b(c+d) \Pi \left( \frac{ad-bc}{(a+b)d}; \sin^{-1} \left( \sqrt{-\frac{(a+b) \csc^2\left(\frac{1}{4}(\pi-2ez)\right)(c+d \sin(ez))}{2ad-2bc}} \right) \right) \right) \frac{2(ad-bc)}{(a+b)(d-c)} \right) - \\ (a+b)d F \left( \sin^{-1} \left( \sqrt{-\frac{(a+b) \csc^2\left(\frac{1}{4}(\pi-2ez)\right)(c+d \sin(ez))}{2ad-2bc}} \right) \right) \frac{2(ad-bc)}{(a+b)(d-c)} \right) \sec(ez) \\ \left( \cos\left(\frac{ez}{2}\right) - \sin\left(\frac{ez}{2}\right) \right)^4 \sqrt{\frac{(c+d) \csc^2\left(\frac{1}{4}(\pi-2ez)\right)(a+b \sin(ez))}{ad-bc}} \sqrt{\frac{(a+b)(c+d \sin(ez))}{(ad-bc)(\sin(ez)-1)}} \Big/ \\ \left( (a+b)d(c+d)e \sqrt{a+b \sin(ez)} \sqrt{c+d \sin(ez)} \right)$$

01.06.21.1004.01

$$\int \sqrt{\frac{a+b \sin^2(ez)}{(c+d \sin^2(ez))^3}} dz = \cos(ez) \sqrt{\frac{2a+b-b \cos(2ez)}{(2c+d-d \cos(2ez))^3}} \\ \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \left( \frac{a \sqrt{\frac{a+b}{a}} (2c+d-d \cos(2ez))}{\sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}}} E \left( \sin^{-1} \left( \frac{\sqrt{2} \sqrt{\frac{a+b}{a}} \sin(ez)}{\sqrt{\frac{2a+b-b \cos(2ez)}{a}}} \right) \right) \right) \frac{bc-ad}{ac+bc} \Bigg) + \\ 2 \sqrt{\frac{2a+b-b \cos(2ez)}{a}} (ad-bc) \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \sin(ez) \Bigg) \Big/ \left( a(c+d)e \sqrt{\frac{2a+b-b \cos(2ez)}{a}} \right)$$

01.06.21.1005.01

$$\int \frac{1}{(a+b \sin^2(ez)) \sqrt{\frac{a+b \sin^2(ez)}{c+d \sin^2(ez)}}} dz = \\ \frac{\cos(ez)}{a \sqrt{\frac{a+b}{a}} e \sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}} \sqrt{\frac{2a+b-b \cos(2ez)}{a}} \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \sqrt{\frac{b \sin^2(ez)+a}{d \sin^2(ez)+c}}} E \left( \sin^{-1} \left( \frac{\sqrt{\frac{2a+2b}{a}} \sin(ez)}{\sqrt{\frac{2a+b-b \cos(2ez)}{a}}} \right) \right) \frac{bc-ad}{ac+bc} \Bigg)$$

01.06.21.1006.01

$$\int \frac{\sqrt{\frac{a+b \sin^2(ez)}{c+d \sin^2(ez)}}}{c+d \sin^2(ez)} dz =$$

$$\sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}} \sec(ez) \left( \sqrt{\frac{a+b}{a}} a(2c+d-d \cos(2ez)) E \left( \sin^{-1} \left( \frac{\sqrt{\frac{2a+2b}{a}} \sin(ez)}{\sqrt{\frac{2a+b-b \cos(2ez)}{a}}} \right) \right) \left( \frac{bc-ad}{ac+bc} \right) + \right.$$

$$\left. 2 \sqrt{\frac{2a+b-b \cos(2ez)}{a}} (ad-bc) \sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}} \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \sin(ez) \right)$$

$$\sqrt{\frac{b \sin^2(ez)+a}{d \sin^2(ez)+c}} \left( ac(c+d) e \sqrt{\frac{2a+b-b \cos(2ez)}{a}} \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \right)$$

01.06.21.1007.01

$$\int \frac{1}{\sqrt{(a+b \sin^2(ez))(c+d \sin^2(ez))}} dz = \left( (2a+b-b \cos(2ez)) \sqrt{-\frac{c \cot^2(ez)}{c+d}} \right.$$

$$\left. \sqrt{\frac{a(2c+d-d \cos(2ez)) \csc^2(ez)}{ad-bc}} F \left( \sin^{-1} \left( \sqrt{\frac{a(2c+d-d \cos(2ez)) \csc^2(ez)}{2ad-2bc}} \right) \right) \left( \frac{ad-bc}{a(c+d)} \right) \tan(ez) \right) /$$

$$\left( ae \sqrt{-(2a+b-b \cos(2ez))(-2c-d+d \cos(2ez))} \sqrt{\frac{c(2a+b-b \cos(2ez)) \csc^2(ez)}{bc-ad}} \right)$$

01.06.21.1008.01

$$\int \frac{1}{\sqrt{(a+b \sin^2(ez))(c+d \sin^2(ez))} (f+g \sin^2(ez))} dz =$$

$$\left( \sqrt{b \sin^2(ez)+a} \sqrt{d \sin^2(ez)+c} \left( \frac{1}{\sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}}} \left( a^2 c g \cos(ez) \sqrt{\frac{2a+b-b \cos(2ez)}{a}} \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \Pi \left( \frac{bf-ag}{af+bf}; \sin^{-1} \left( \frac{\sqrt{\frac{2a+2b}{a}} \sin(ez)}{\sqrt{\frac{2a+b-b \cos(2ez)}{a}}} \right) \right) \frac{bc-ad}{ac+bc} \right) \right) +$$

$$\sqrt{\frac{a+b}{a}} b \sqrt{-\frac{c \cot^2(ez)}{c+d}} \sqrt{\frac{a(2c+d-d \cos(2ez)) \csc^2(ez)}{ad-bc}} (ad-bc) \sqrt{\frac{c(2a+b-b \cos(2ez)) \csc^2(ez)}{bc-ad}}$$

$$\left. \left. \left. f F \left( \sin^{-1} \left( \sqrt{\frac{a(2c+d-d \cos(2ez)) \csc^2(ez)}{2ad-2bc}} \right) \right) \frac{ad-bc}{a(c+d)} \sin^2(ez) \tan(ez) \right) \right) /$$

$$\left( a \sqrt{\frac{a+b}{a}} c e f (a g - b f) \sqrt{2a+b-b \cos(2ez)} \sqrt{2c+d-d \cos(2ez)} \sqrt{(b \sin^2(ez)+a)(d \sin^2(ez)+c)} \right)$$

01.06.21.1009.01

$$\int \frac{\sin^2(ez)}{\sqrt{(b \sin^2(ez) + a)(d \sin^2(ez) + c)^3}} dz =$$

$$- \left( \cos(ez) \left( \sqrt{\frac{a+b}{a}} a(2c+d-d \cos(2ez)) E \left( \sin^{-1} \left( \frac{\sqrt{\frac{2a+2b}{a}} \sin(ez)}{\sqrt{\frac{2a+b-b \cos(2ez)}{a}}} \right) \right) \frac{bc-ad}{ac+bc} \right) + \right.$$

$$\left. \sqrt{\frac{2a+b-b \cos(2ez)}{a}} (bc-ad) \sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}} \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \right.$$

$$\left. \left( \frac{1}{\sqrt{\frac{-c \cot^2(ez)}{c+d}}} \left( \sqrt{\frac{c(2a+b-b \cos(2ez)) \csc^2(ez)}{bc-ad}} \sqrt{\frac{a(2c+d-d \cos(2ez)) \csc^2(ez)}{ad-bc}} \right) \right. \right.$$

$$\left. \left. F \left( \sin^{-1} \left( \sqrt{\frac{a(2c+d-d \cos(2ez)) \csc^2(ez)}{2ad-2bc}} \right) \right) \frac{ad-bc}{a(c+d)} \right) - 2 \right) \sin(ez) \right)$$

$$\sqrt{b \sin^2(ez) + a} (d \sin^2(ez) + c)^{3/2} \Big/ \left( (c+d)(ad-bc) e \sqrt{\frac{a \cos^2(ez)}{2a+b-b \cos(2ez)}} \right.$$

$$\left. \sqrt{2a+b-b \cos(2ez)} \sqrt{\frac{2a+b-b \cos(2ez)}{a}} \sqrt{2c+d-d \cos(2ez)} \right.$$

$$\left. \sqrt{\frac{a(2c+d-d \cos(2ez))}{c(2a+b-b \cos(2ez))}} \sqrt{(b \sin^2(ez) + a)(d \sin^2(ez) + c)^3} \right)$$

**Involving functions of the direct function and a power function**

**Involving powers of the direct function and a power function**

Involving powers of sin and power

**Involving  $z^{\alpha-1} \sin^{\nu}(az)$**

01.06.21.1010.01

$$\int z^{\alpha-1} \sin^{\nu}(a z) dz = \frac{2^{-\nu} (1 - \nu \bmod 2)}{\alpha} z^{\alpha} \binom{\nu}{\frac{\nu}{2}} - (2i)^{-\nu} z^{\alpha} \sum_{j=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^j \binom{\nu}{j} (\Gamma(\alpha, ia(2j-\nu)z) (ia(2j-\nu)z)^{-\alpha} + (-1)^{\nu} (ia(\nu-2j)z)^{-\alpha} \Gamma(\alpha, ia(\nu-2j)z)) /; \alpha \neq 0 \wedge \nu \in \mathbb{N}^+$$

01.06.21.1011.01

$$\int \frac{\sin^{\nu}(a z)}{z} dz = 2^{-\nu} \binom{\nu}{\frac{\nu}{2}} \log(z) (1 - \nu \bmod 2) + 2^{1-\nu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \cos\left(\frac{\pi \nu}{2}\right) \text{Ci}(a(\nu-2k)z) + \sin\left(\frac{\pi \nu}{2}\right) \text{Si}(a(\nu-2k)z) \right) /; \nu \in \mathbb{N}^+$$

01.06.21.1012.01

$$\int z^{\alpha-1} \sin^2(a z) dz = \frac{1}{4} z^{\alpha} \left( 2^{-\alpha} \Gamma(\alpha, -2ia z) (-ia z)^{-\alpha} + 2^{-\alpha} (ia z)^{-\alpha} \Gamma(\alpha, 2ia z) + \frac{2}{\alpha} \right)$$

01.06.21.1013.01

$$\int z^{\alpha-1} \sin^3(a z) dz = \frac{1}{8} i 3^{-\alpha} z^{\alpha} (a^2 z^2)^{-\alpha} \left( -3^{\alpha+1} \Gamma(\alpha, ia z) (-ia z)^{\alpha} + \Gamma(\alpha, 3ia z) (-ia z)^{\alpha} + 3^{\alpha+1} (ia z)^{\alpha} \Gamma(\alpha, -ia z) - (ia z)^{\alpha} \Gamma(\alpha, -3ia z) \right)$$

01.06.21.1014.01

$$\int z^n \sin^{\nu}(a z) dz = n! \sin^{\nu}(a z) (1 - e^{2ia z})^{-\nu} \sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (-ia \nu)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{\nu}{2}, \dots, -\frac{\nu}{2}, -\nu; 1 - \frac{\nu}{2}, \dots, 1 - \frac{\nu}{2}; e^{2ia z} \right) /; n \in \mathbb{N}$$

01.06.21.1015.01

$$\int z \sin^{\nu}(a z) dz = \frac{1}{2a^2} \left( \sin^{\nu+1}(a z) \left( \frac{2az \cos(a z)}{\nu+1} {}_2F_1 \left( 1, \frac{\nu+2}{2}; \frac{\nu+3}{2}; \sin^2(a z) \right) - 2^{-\nu-1} \sqrt{\pi} \Gamma(\nu+1) {}_3\tilde{F}_2 \left( 1, \frac{\nu+2}{2}, \frac{\nu+2}{2}; \frac{\nu+3}{2}, \frac{\nu+4}{2}; \sin^2(a z) \right) \sin(a z) \right) \right)$$

01.06.21.1016.01

$$\int \frac{\sin^2(a z)}{z} dz = \frac{1}{2} (\log(z) - \text{Ci}(2a z))$$

01.06.21.1017.01

$$\int \frac{\sin^3(a z)}{z} dz = \frac{1}{4} (3 \text{Si}(a z) - \text{Si}(3a z))$$

01.06.21.1018.01

$$\int \frac{\sin^4(a z)}{z} dz = \frac{1}{8} (-4 \text{Ci}(2a z) + \text{Ci}(4a z) + 3 \log(z))$$

01.06.21.1019.01

$$\int \frac{\sin^5(a z)}{z} dz = \frac{1}{16} (10 \text{Si}(a z) - 5 \text{Si}(3a z) + \text{Si}(5a z))$$

$$\int z \sin^2(a z) dz = -\frac{\cos(2 a z) + 2 a z (\sin(2 a z) - a z)}{8 a^2}$$

$$\int z \sin^3(a z) dz = -\frac{27 a z \cos(a z) - 3 a z \cos(3 a z) - 27 \sin(a z) + \sin(3 a z)}{36 a^2}$$

$$\int z \sin^4(a z) dz = \frac{-16 \cos(2 a z) + \cos(4 a z) + 4 a z (6 a z - 8 \sin(2 a z) + \sin(4 a z))}{128 a^2}$$

$$\int z \sin^5(a z) dz = \frac{1}{3600 a^2} (-2250 a z \cos(a z) + 375 a z \cos(3 a z) - 45 a z \cos(5 a z) + 2250 \sin(a z) - 125 \sin(3 a z) + 9 \sin(5 a z))$$

$$\int z^2 \sin^2(a z) dz = \frac{4 a^3 z^3 - 6 a \cos(2 a z) z + (3 - 6 a^2 z^2) \sin(2 a z)}{24 a^3}$$

$$\int z^2 \sin^3(a z) dz = \frac{-81 (a^2 z^2 - 2) \cos(a z) + (9 a^2 z^2 - 2) \cos(3 a z) - 6 a z (\sin(3 a z) - 27 \sin(a z))}{108 a^3}$$

$$\int z^2 \sin^4(a z) dz = \frac{1}{256 a^3} (32 a^3 z^3 - 64 a^2 \sin(2 a z) z^2 + 8 a^2 \sin(4 a z) z^2 - 64 a \cos(2 a z) z + 4 a \cos(4 a z) z + 32 \sin(2 a z) - \sin(4 a z))$$

$$\int z^2 \sin^5(a z) dz = \frac{1}{54000 a^3} (-675 a^2 \cos(5 a z) z^2 + 67500 a \sin(a z) z - 3750 a \sin(3 a z) z + 270 a \sin(5 a z) z - 33750 (a^2 z^2 - 2) \cos(a z) + 625 (9 a^2 z^2 - 2) \cos(3 a z) + 54 \cos(5 a z))$$

$$\int z^2 \sin^6(a z) dz = \frac{1}{13824 a^3} (1440 a^3 z^3 - 3240 a^2 \sin(2 a z) z^2 + 648 a^2 \sin(4 a z) z^2 - 72 a^2 \sin(6 a z) z^2 - 3240 a \cos(2 a z) z + 324 a \cos(4 a z) z - 24 a \cos(6 a z) z + 1620 \sin(2 a z) - 81 \sin(4 a z) + 4 \sin(6 a z))$$

$$\int z^3 \sin^2(a z) dz = \frac{2 a^4 z^4 + (3 - 6 a^2 z^2) \cos(2 a z) + (6 a z - 4 a^3 z^3) \sin(2 a z)}{16 a^4}$$

$$\int z^3 \sin^3(a z) dz = \frac{1}{108 a^4} (-81 a z (a^2 z^2 - 6) \cos(a z) + 3 a z (3 a^2 z^2 - 2) \cos(3 a z) - 2 (-117 a^2 z^2 + (9 a^2 z^2 - 2) \cos(2 a z) + 242) \sin(a z))$$

01.06.21.1031.01

$$\int z^3 \sin^4(az) dz = \frac{1}{1024 a^4} (-192(2a^2 z^2 - 1) \cos(2az) + 3(8a^2 z^2 - 1) \cos(4az) + 4az(24a^3 z^3 + (96 - 64a^2 z^2) \sin(2az) + (8a^2 z^2 - 3) \sin(4az)))$$

01.06.21.1032.01

$$\int z^{n+\frac{1}{2}} \sin^v(az) dz = \frac{2^{1-v} z^{n+\frac{3}{2}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)}{2n+3} - (2i)^{-v} z^{n+\frac{3}{2}} \sum_{j=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^j \binom{v}{j} \left( \operatorname{erfc}(\sqrt{ia(2j-v)z}) \Gamma\left(n + \frac{3}{2}\right) + e^{-ia(2j-v)z} \sum_{k=0}^n \frac{(ia(2j-v)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - e^{-ia(2j-v)z} \sum_{k=n+1}^{-1} \frac{(ia(2j-v)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) (ia(2j-v)z)^{-n-\frac{3}{2}} + (-1)^v (ia(v-2j)z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}(\sqrt{ia(v-2j)z}) \Gamma\left(n + \frac{3}{2}\right) + e^{-ia(v-2j)z} \sum_{k=0}^n \frac{(ia(v-2j)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - e^{-ia(v-2j)z} \sum_{k=n+1}^{-1} \frac{(ia(v-2j)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) \Bigg/; n \in \mathbb{Z} \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin^v(az+b)$

01.06.21.1033.01

$$\int z^{\alpha-1} \sin^v(b+az) dz = \frac{2^{-v} (1 - v \bmod 2) z^\alpha \binom{v}{\frac{v}{2}}}{\alpha} - 2^{-v} z^\alpha \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} (a^2(2k-v)^2 z^2)^{-\alpha} \left( e^{-i(\frac{\pi v}{2} - b(v-2k))z} \Gamma(\alpha, ia(2k-v)z) (-ia(2k-v)z)^\alpha + e^{i(\frac{\pi v}{2} - b(v-2k))z} (ia(2k-v)z)^\alpha \Gamma(\alpha, -ia(2k-v)z) \right) \Big/; \alpha \neq 0 \wedge n \in \mathbb{N}^+$$

01.06.21.1034.01

$$\int \frac{\sin^v(az+b)}{z} dz = 2^{-v} \binom{v}{\frac{v}{2}} \log(z) (1 - v \bmod 2) + 2^{1-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \cos\left(\frac{\pi v}{2} - b(v-2k)\right) \operatorname{Ci}(a(2k-v)z) - \sin\left(\frac{\pi v}{2} - b(v-2k)\right) \operatorname{Si}(a(2k-v)z) \right) \Big/; n \in \mathbb{N}^+$$

01.06.21.1035.01

$$\int z^{\alpha-1} \sin^2(az+b) dz = \frac{1}{\alpha} (2^{-\alpha-2} z^\alpha (a^2 z^2)^{-\alpha} (\alpha \Gamma(\alpha, 2ia z) (\cos(b) - i \sin(b))^2 (-ia z)^\alpha + 2^{\alpha+1} (a^2 z^2)^\alpha + (ia z)^\alpha \alpha \Gamma(\alpha, -2ia z) (\cos(b) + i \sin(b))^2))$$

01.06.21.1036.01

$$\int z^{\alpha-1} \sin^3(az+b) dz = \frac{1}{8} i 3^{-\alpha} e^{-3ib} z^\alpha (a^2 z^2)^{-\alpha} (-3^{\alpha+1} e^{2ib} \Gamma(\alpha, ia z) (-ia z)^\alpha + \Gamma(\alpha, 3ia z) (-ia z)^\alpha + 3^{\alpha+1} e^{4ib} (ia z)^\alpha \Gamma(\alpha, -ia z) - e^{6ib} (ia z)^\alpha \Gamma(\alpha, -3ia z))$$

01.06.21.1037.01

$$\int z^n \sin^v(a z + b) dz = n! \sin^v(a z + b) (1 - e^{2i(a z + b)})^{-v} \sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (-i a v)^{j+1}} {}_{j+2}F_{j+1}\left(-\frac{v}{2}, \dots, -\frac{v}{2}, -v; 1 - \frac{v}{2}, \dots, 1 - \frac{v}{2}; e^{2i(a z + b)}\right); n \in \mathbb{N}$$

01.06.21.1038.01

$$\int z \sin^v(a z + b) dz = \frac{1}{2 a^2} \sin^{v+1}(b + a z) \left( 2 b \cos(b + a z) {}_2F_1\left(\frac{1}{2}, \frac{1-v}{2}; \frac{3}{2}; \cos^2(b + a z)\right) \sin^2(b + a z)^{\frac{1}{2}(v-1)} + \frac{2(b + a z) \cos(b + a z) {}_2F_1\left(1, \frac{v+2}{2}; \frac{v+3}{2}; \sin^2(b + a z)\right)}{v+1} - 2^{-v-1} \sqrt{\pi} \Gamma(v+1) {}_3\tilde{F}_2\left(1, \frac{v+2}{2}, \frac{v+2}{2}; \frac{v+3}{2}, \frac{v+4}{2}; \sin^2(b + a z)\right) \sin(b + a z) \right)$$

01.06.21.1039.01

$$\int \frac{\sin^2(b + a z)}{z^2} dz = \frac{\cos(2(b + a z)) + 2 a z \operatorname{Ci}(2 a z) \sin(2 b) + 2 a z \cos(2 b) \operatorname{Si}(2 a z) - 1}{2 z}$$

01.06.21.1040.01

$$\int \frac{\sin^2(a z + b)}{z} dz = \frac{1}{2} (-\cos(2 b) \operatorname{Ci}(2 a z) + \log(z) + \sin(2 b) \operatorname{Si}(2 a z))$$

01.06.21.1041.01

$$\int \frac{\sin^3(a z + b)}{z} dz = \frac{1}{4} (3 \operatorname{Ci}(a z) \sin(b) - \operatorname{Ci}(3 a z) \sin(3 b) + 3 \cos(b) \operatorname{Si}(a z) - \cos(3 b) \operatorname{Si}(3 a z))$$

01.06.21.1042.01

$$\int \frac{\sin^4(a z + b)}{z} dz = \frac{1}{8} (-4 \cos(2 b) \operatorname{Ci}(2 a z) + \cos(4 b) \operatorname{Ci}(4 a z) + 3 \log(z) + 4 \sin(2 b) \operatorname{Si}(2 a z) - \sin(4 b) \operatorname{Si}(4 a z))$$

01.06.21.1043.01

$$\int \frac{\sin^5(a z + b)}{z} dz = \frac{1}{16} (10 \operatorname{Ci}(a z) \sin(b) - 5 \operatorname{Ci}(3 a z) \sin(3 b) + \operatorname{Ci}(5 a z) \sin(5 b) + 10 \cos(b) \operatorname{Si}(a z) - 5 \cos(3 b) \operatorname{Si}(3 a z) + \cos(5 b) \operatorname{Si}(5 a z))$$

01.06.21.1044.01

$$\int z \sin^2(b + a z) dz = -\frac{\cos(2(b + a z)) + 2 a z (\sin(2(b + a z)) - a z)}{8 a^2}$$

01.06.21.1045.01

$$\int z \sin^3(b + a z) dz = \frac{3 a z (\cos(3(b + a z)) - 9 \cos(b + a z)) + 27 \sin(b + a z) - \sin(3(b + a z))}{36 a^2}$$

01.06.21.1046.01

$$\int z \sin^4(b + a z) dz = \frac{1}{128 a^2} (-16 \cos(2(b + a z)) + \cos(4(b + a z)) + 4 a z (6 a z - 8 \sin(2(b + a z)) + \sin(4(b + a z))))$$



$$01.06.21.1047.01$$

$$\int z \sin^5(b + az) dz = \frac{1}{3600 a^2} (9 \sin(5(b + az)) - 5(3az(150 \cos(b + az) - 25 \cos(3(b + az)) + 3 \cos(5(b + az))) + 25(\sin(3(b + az)) - 18 \sin(b + az)))$$

$$01.06.21.1048.01$$

$$\int z^2 \sin^2(b + az) dz = \frac{4a^3 z^3 - 6a \cos(2(b + az))z + (3 - 6a^2 z^2) \sin(2(b + az))}{24 a^3}$$

$$01.06.21.1049.01$$

$$\int z^2 \sin^3(b + az) dz = \frac{1}{108 a^3} (-81(a^2 z^2 - 2) \cos(b + az) + (9a^2 z^2 - 2) \cos(3(b + az)) - 6az(\sin(3(b + az)) - 27 \sin(b + az)))$$

$$01.06.21.1050.01$$

$$\int z^2 \sin^4(b + az) dz = \frac{1}{256 a^3} (4az(8a^2 z^2 - 16 \cos(2(b + az)) + \cos(4(b + az))) + 32(1 - 2a^2 z^2) \sin(2(b + az)) + (8a^2 z^2 - 1) \sin(4(b + az)))$$

$$01.06.21.1051.01$$

$$\int z^2 \sin^5(b + az) dz = \frac{1}{54000 a^3} (-33750(a^2 z^2 - 2) \cos(b + az) + 625(9a^2 z^2 - 2) \cos(3(b + az)) + 54 \cos(5(b + az)) + 15az(-45az \cos(5(b + az)) + 4500 \sin(b + az) - 250 \sin(3(b + az)) + 18 \sin(5(b + az))))$$

$$01.06.21.1052.01$$

$$\int z^2 \sin^6(b + az) dz = \frac{1}{13824 a^3} (12az(120a^2 z^2 - 270 \cos(2(b + az)) + 27 \cos(4(b + az)) - 2 \cos(6(b + az))) - 1620(2a^2 z^2 - 1) \sin(2(b + az)) + 81(8a^2 z^2 - 1) \sin(4(b + az)) + 4(1 - 18a^2 z^2) \sin(6(b + az)))$$

$$01.06.21.1053.01$$

$$\int z^3 \sin^2(b + az) dz = \frac{2a^4 z^4 + (3 - 6a^2 z^2) \cos(2(b + az)) + (6az - 4a^3 z^3) \sin(2(b + az))}{16 a^4}$$

$$01.06.21.1054.01$$

$$\int z^3 \sin^3(b + az) dz = \frac{1}{108 a^4} (-81(a^2 z^2 - 6)az \cos(b + az) + (9a^3 z^3 - 6az) \cos(3(b + az)) + 2(117a^2 z^2 + (2 - 9a^2 z^2) \cos(2(b + az)) - 242) \sin(b + az))$$

$$01.06.21.1055.01$$

$$\int z^3 \sin^4(b + az) dz = \frac{1}{1024 a^4} (192(1 - 2a^2 z^2) \cos(2(b + az)) + 3(8a^2 z^2 - 1) \cos(4(b + az)) + 4az(24a^3 z^3 + 32(3 - 2a^2 z^2) \sin(2(b + az)) + (8a^2 z^2 - 3) \sin(4(b + az))))$$

01.06.21.1056.01

$$\int z^{n+\frac{1}{2}} \sin^v(a z + b) dz =$$

$$\frac{2^{1-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) z^{n+\frac{3}{2}}}{2n+3} - 2^{-v} \sqrt{z} (-ia)^{-n-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \left( (-1)^s \binom{v}{s} \right) \left( e^{i(\frac{\pi v}{2} - b(v-2s))} \sqrt{ia(2s-v)z} \operatorname{erfc}(\sqrt{-ia(2s-v)z}) - \right.$$

$$\left. (-1)^n e^{-i(\frac{\pi v}{2} - b(v-2s))} \sqrt{-ia(2s-v)z} \operatorname{erfc}(\sqrt{ia(2s-v)z}) \right) \Gamma\left(n + \frac{3}{2}\right) +$$

$$e^{i(\frac{\pi v}{2} - b(v-2s) + a(2s-v)z)} \sqrt{ia(2s-v)z} \left( \sum_{k=0}^n \frac{(-ia(2s-v)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(-ia(2s-v)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) -$$

$$\left. (-1)^n e^{-i(\frac{\pi v}{2} - b(v-2s) + a(2s-v)z)} \sqrt{-ia(2s-v)z} \left( \sum_{k=0}^n \frac{(ia(2s-v)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \sum_{k=n+1}^{-1} \frac{(ia(2s-v)z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) \right) /$$

$$\left( (2s-v)^{n+1} \sqrt{a^2(2s-v)^2 z^2} \right); n \in \mathbb{Z} \wedge \alpha \neq 0 \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin^v(a z^r)$

01.06.21.1057.01

$$\int z^{\alpha-1} \sin^v(a z^r) dz = \frac{2^{-v} (1 - v \bmod 2)}{\alpha} z^\alpha \binom{v}{\frac{v}{2}} - \frac{(2i)^{-v} z^\alpha}{r}$$

$$\sum_{i=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^i \binom{v}{i} \left( (-1)^v \Gamma\left(\frac{\alpha}{r}, -ia(2i-v)z^r\right) (-ia(2i-v)z^r)^{-\frac{\alpha}{r}} + (ia(2i-v)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, ia(2i-v)z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.1058.01

$$\int \frac{\sin^v(a z^r)}{z} dz =$$

$$2^{-v} \binom{v}{\frac{v}{2}} \log(z) (1 - v \bmod 2) + \frac{2^{1-v}}{r} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \cos\left(\frac{\pi v}{2}\right) \operatorname{Ci}(a(v-2k)z^r) + \sin\left(\frac{\pi v}{2}\right) \operatorname{Si}(a(v-2k)z^r) \right); v \in \mathbb{N}^+$$

01.06.21.1059.01

$$\int z^n \sin^v(a z^2) dz =$$

$$\frac{2^{-v} z^{n+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)}{n+1} - 2^{-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-\frac{1}{2}i\pi v} \Gamma\left(\frac{n+1}{2}, -ia(v-2k)z^2\right) (-ia(v-2k)z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{\frac{1}{2}i\pi v} (ia(v-2k)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ia(v-2k)z^2\right) \right); n \in \mathbb{Z} \wedge n \neq -1 \wedge v \in \mathbb{N}^+$$

01.06.21.1060.01

$$\int z^{2n} \sin^v(a z^2) dz = \frac{2^{-v} z^{2n+1} \left(\frac{v}{2}\right) (1-v \bmod 2)}{2n+1} -$$

$$i^{-v} 2^{-v-1} z^{2n+1} \sum_{j=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^j \binom{v}{j} \left( (-1)^v \operatorname{erfc} \left( \sqrt{-i a (2j-v) z^2} \right) \Gamma \left( n + \frac{1}{2} \right) + e^{i a (2j-v) z^2} \sum_{k=0}^{n-1} \frac{(-i a (2j-v) z^2)^{k+\frac{1}{2}}}{\left( n + \frac{1}{2} \right)_{k-n+1}} -$$

$$e^{i a (2j-v) z^2} \sum_{k=n}^{-1} \frac{(-i a (2j-v) z^2)^{k+\frac{1}{2}}}{\left( n + \frac{1}{2} \right)_{k-n+1}} \right) (-i a (2j-v) z^2)^{\frac{1}{2}(-2n-1)} +$$

$$\left( i a (2j-v) z^2 \right)^{\frac{1}{2}(-2n-1)} \left( \operatorname{erfc} \left( \sqrt{i a (2j-v) z^2} \right) \Gamma \left( n + \frac{1}{2} \right) + e^{-i a (2j-v) z^2} \sum_{k=0}^{n-1} \frac{(i a (2j-v) z^2)^{k+\frac{1}{2}}}{\left( n + \frac{1}{2} \right)_{k-n+1}} -$$

$$e^{-i a (2j-v) z^2} \sum_{k=n}^{-1} \frac{(i a (2j-v) z^2)^{k+\frac{1}{2}}}{\left( n + \frac{1}{2} \right)_{k-n+1}} \right) \Bigg) ; n \in \mathbb{Z} \wedge v \in \mathbb{N}^+$$

01.06.21.1061.01

$$\int z^{2n-1} \sin^v(a z^2) dz = \frac{2^{-v-1} z^{2n} \left(\frac{v}{2}\right) (1-v \bmod 2)}{n} -$$

$$i^{-v} 2^{-v-1} z^{2n} \sum_{j=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^j \binom{v}{j} \left( (-1)^v (-i a (2j-v) z^2)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(i a (2j-v) z^2)}{(-n)!} + e^{i a (2j-v) z^2} \sum_{k=0}^{n-1} \frac{(-i a (2j-v) z^2)^k}{(n)_{k-n+1}} -$$

$$e^{i a (2j-v) z^2} \sum_{k=n}^{-1} \frac{(-i a (2j-v) z^2)^k}{(n)_{k-n+1}} \right) + (i a (2j-v) z^2)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(-i a (2j-v) z^2)}{(-n)!} +$$

$$e^{-i a (2j-v) z^2} \sum_{k=0}^{n-1} \frac{(i a (2j-v) z^2)^k}{(n)_{k-n+1}} - e^{-i a (2j-v) z^2} \sum_{k=n}^{-1} \frac{(i a (2j-v) z^2)^k}{(n)_{k-n+1}} \right) \Bigg) ; n \in \mathbb{Z} \wedge n \neq 0 \wedge v \in \mathbb{N}^+$$

01.06.21.1062.01

$$\int z^n \sin^v(a \sqrt{z}) dz = \frac{2^{-v} z^{n+1} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{n + 1} - i^{-v} 2^{1-v} z^{n+1} \sum_{j=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^j \binom{v}{j} (i a (2j - v) \sqrt{z})^{-2(n+1)} \left( \frac{(-1)^{2(n+1)-1} \text{Ei}(-i a (2j - v) \sqrt{z})}{(-2(n+1))!} + (-1)^v \left( \frac{(-1)^{2(n+1)-1} \text{Ei}(i a (2j - v) \sqrt{z})}{(-2(n+1))!} + e^{i a (2j - v) \sqrt{z}} \sum_{k=0}^{2(n+1)-1} \frac{(-i a (2j - v) \sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} - e^{i a (2j - v) \sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{(-i a (2j - v) \sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} \right) + e^{-i a (2j - v) \sqrt{z}} \sum_{k=0}^{2(n+1)-1} \frac{(i a (2j - v) \sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} - e^{-i a (2j - v) \sqrt{z}} \sum_{k=2(n+1)}^{-1} \frac{(i a (2j - v) \sqrt{z})^k}{(2(n+1))_{k-2(n+1)+1}} \right); n \in \mathbb{Z} \wedge n \neq 0 \wedge v \in \mathbb{N}^+$$

**Involving  $z^{\alpha-1} \sin^v(a z^r + b)$**

01.06.21.1063.01

$$\int z^{\alpha-1} \sin^v(a z^r + b) dz = \frac{2^{-v} \left(\frac{v}{2}\right) (1 - v \bmod 2) z^\alpha}{\alpha} - \frac{1}{r} \left( (2^{-v} z^\alpha) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{i b (v-2k) - \frac{i \pi v}{2}} \Gamma\left(\frac{\alpha}{r}, -i a (v-2k) z^r\right) (-i a (v-2k) z^r\right)^{-\frac{\alpha}{r}} + e^{\frac{i \pi v}{2} - i b (v-2k)} (i a (v-2k) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, i a (v-2k) z^r\right) \right); \alpha \neq 0 \wedge v \in \mathbb{N}^+$$

01.06.21.1064.01

$$\int \frac{\sin^v(a z^r + b)}{z} dz = 2^{-v} \left(\frac{v}{2}\right) \log(z) (1 - v \bmod 2) + \frac{1}{r} \left( 2^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-\frac{i}{2} i (-4 b k + 2 b v + \pi v)} (e^{i \pi v} \text{Ei}(-i a (v-2k) z^r) + e^{2 i b (v-2k)} \text{Ei}(i a (v-2k) z^r)) \right); v \in \mathbb{N}^+$$

01.06.21.1065.01

$$\int z^n \sin^v(a z^2 + b) dz = \frac{2^{-v} z^{n+1} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{n + 1} - 2^{-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{i b (v-2k) - \frac{i \pi v}{2}} \Gamma\left(\frac{n+1}{2}, -i a (v-2k) z^2\right) (-i a (v-2k) z^2\right)^{\frac{1}{2}(-n-1)} + e^{\frac{i \pi v}{2} - i b (v-2k)} (i a (v-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i a (v-2k) z^2\right) \right); n \in \mathbb{Z} \wedge n \neq -1 \wedge v \in \mathbb{N}^+$$

01.06.21.1066.01

$$\int z^{2n} \sin^v(a z^2 + b) dz = \frac{2^{-v} z^{2n+1} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{2n+1} - 2^{-v-1} z^{2n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{i b (v-2k) - \frac{i \pi v}{2}} \left( \operatorname{erfc}\left(\sqrt{-i a (v-2k) z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{i a (v-2k) z^2} \sum_{j=0}^{n-1} \frac{(-i a (v-2k) z^2)^{j+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{j-n+1}} - e^{i a (v-2k) z^2} \sum_{j=n}^{-1} \frac{(-i a (v-2k) z^2)^{j+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{j-n+1}} \right) (-i a (v-2k) z^2)^{\frac{1}{2}(-2n-1)} + e^{\frac{i \pi v}{2} - i b (v-2k)} (i a (v-2k) z^2)^{\frac{1}{2}(-2n-1)} \left( \operatorname{erfc}\left(\sqrt{i a (v-2k) z^2}\right) \Gamma\left(n + \frac{1}{2}\right) + e^{-i a (v-2k) z^2} \sum_{j=0}^{n-1} \frac{(i a (v-2k) z^2)^{j+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{j-n+1}} - e^{-i a (v-2k) z^2} \sum_{j=n}^{-1} \frac{(i a (v-2k) z^2)^{j+\frac{1}{2}}}{\left(n + \frac{1}{2}\right)_{j-n+1}} \right) \right) /; n \in \mathbb{Z} \wedge v \in \mathbb{N}^+$$

01.06.21.1067.01

$$\int z^{2n-1} \sin^v(a z^2 + b) dz = \frac{2^{-v-1} z^{2n} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{n} - 2^{-v-1} z^{2n} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{i b (v-2k) - \frac{i \pi v}{2}} \left( \frac{(-1)^{n-1} \operatorname{Ei}(i a (v-2k) z^2)}{(-n)!} + e^{i a (v-2k) z^2} \sum_{j=0}^{n-1} \frac{(-i a (v-2k) z^2)^j}{(n)_{j-n+1}} - e^{i a (v-2k) z^2} \sum_{j=n}^{-1} \frac{(-i a (v-2k) z^2)^j}{(n)_{j-n+1}} \right) (-i a (v-2k) z^2)^{-n} + e^{\frac{i \pi v}{2} - i b (v-2k)} (i a (v-2k) z^2)^{-n} \left( \frac{(-1)^{n-1} \operatorname{Ei}(-i a (v-2k) z^2)}{(-n)!} + e^{-i a (v-2k) z^2} \sum_{j=0}^{n-1} \frac{(i a (v-2k) z^2)^j}{(n)_{j-n+1}} - e^{-i a (v-2k) z^2} \sum_{j=n}^{-1} \frac{(i a (v-2k) z^2)^j}{(n)_{j-n+1}} \right) \right) /; n \in \mathbb{Z} \wedge n \neq 0 \wedge v \in \mathbb{N}^+$$

01.06.21.1068.01

$$\int z^n \sin^v(\sqrt{z} a + b) dz = \frac{2^{-v} z^{n+1} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{n + 1} -$$

$$2^{1-v} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{i b (v-2k) - \frac{i \pi v}{2}} \left( \frac{(-1)^{2(n+1)-1} \operatorname{Ei}(i a (v-2k) \sqrt{z})}{(-2(n+1))!} + e^{i a (v-2k) \sqrt{z}} \sum_{j=0}^{2(n+1)-1} \frac{(-i a (v-2k) \sqrt{z})^j}{(2(n+1))_{j-2(n+1)+1}} - \right. \right.$$

$$e^{i a (v-2k) \sqrt{z}} \sum_{j=2(n+1)}^{-1} \frac{(-i a (v-2k) \sqrt{z})^j}{(2(n+1))_{j-2(n+1)+1}} \left. (-i a (v-2k) \sqrt{z})^{-2(n+1)} + \right.$$

$$e^{\frac{i \pi v}{2} - i b (v-2k)} (i a (v-2k) \sqrt{z})^{-2(n+1)} \left( e^{-i a (v-2k) \sqrt{z}} \sum_{j=0}^{2(n+1)-1} \frac{(i a (v-2k) \sqrt{z})^j}{(2(n+1))_{j-2(n+1)+1}} - e^{-i a (v-2k) \sqrt{z}} \right.$$

$$\left. \left. \sum_{j=2(n+1)}^{-1} \frac{(i a (v-2k) \sqrt{z})^j}{(2(n+1))_{j-2(n+1)+1}} + \frac{(-1)^{2(n+1)-1} \operatorname{Ei}(-i a (v-2k) \sqrt{z})}{(-2(n+1))!} \right) \right) ; n \in \mathbb{Z} \wedge n \neq -1 \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin^v(c z^r + f z)$

01.06.21.1069.01

$$\int z^n \sin^v(c z^2 + f z) dz = 2^{-n-v-1} (-f)^n \left( \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{v-2k} \right.$$

$$\left( (-1)^k e^{-\frac{i(f^2(2k-v)^2 + 2c\pi v(2k-v))}{4c(2k-v)}} (f(2k-v) + 2cz(2k-v)) \binom{v}{k} \left( e^{\frac{if^2(2k-v)}{2c}} \sum_{j=0}^n \left( \frac{i(f(2k-v) + 2cz(2k-v))^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left( -\frac{2f(2k-v) + 4cz(2k-v)}{f(2k-v)} \right)^j \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f(2k-v) + 2cz(2k-v))^2}{4c(2k-v)}\right) + \right.$$

$$e^{i\pi v} \sum_{j=0}^n \left( -\frac{i(f(2k-v) + 2cz(2k-v))^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \left( -\frac{2f(2k-v) + 4cz(2k-v)}{f(2k-v)} \right)^j \binom{n}{j}$$

$$\left. \left. \Gamma\left(\frac{j+1}{2}, -\frac{i(f(2k-v) + 2cz(2k-v))^2}{4c(2k-v)}\right) \right) \right) \right) c^{-n-1} + \frac{2^{-v} z^{n+1} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{n + 1} ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1070.01

$$\int z^n \sin^v(\sqrt{z} c + f z) dz =$$

$$2^{-v-1} f^{-2n-2} c^{2n} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(2k-v)^2} \left( (-1)^k 4^{-n} e^{-\frac{i(2k-v)c^2 - i\pi v}{4f} - \frac{i\pi v}{2}} \binom{v}{k} \left( e^{\frac{ic^2(2k-v)}{2f}} \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{c(2k-v) + 2f\sqrt{z}(2k-v)}{c(2k-v)} \right)^{h+j} \right. \right. \\ \left. \left. \left( \frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c(2k-v)(c(2k-v) + 2f\sqrt{z}(2k-v)) \right. \right. \right. \\ \left. \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) + 2fi(2k-v) \right. \right. \right. \\ \left. \left. \left. \sqrt{\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) \right) \right) + \right. \\ \left. e^{i\pi v} \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{c(2k-v) + 2f\sqrt{z}(2k-v)}{c(2k-v)} \right)^{h+j} \left( -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \\ \left. \binom{n}{j} \left( c(2k-v)(c(2k-v) + 2f\sqrt{z}(2k-v)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) - \right. \right. \\ \left. \left. 2if(2k-v) \sqrt{-\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \right. \\ \left. \left. \left. -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) \right) \right) \right) + \frac{2^{-v} z^{n+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{n+1} ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving  $z^n \sin^v(cz^r + fz + g)$

01.06.21.1071.01

$$\int z^n \sin^v(c z^2 + f z + g) dz = 2^{-n-v-1} (-f)^n c^{-n-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{v-2k} \left( (-1)^k e^{-\frac{i(f^2(2k-v)^2 + 4c(\frac{\pi v}{2} - g)(v-2k))(2k-v)}{4c(2k-v)}} \right.$$

$$(f(2k-v) + 2cz(2k-v)) \binom{v}{k} \left( e^{\frac{if^2(2k-v)}{2c}} \sum_{j=0}^n \left( \frac{i(f(2k-v) + 2cz(2k-v))^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \left( -\frac{2f(2k-v) + 4cz(2k-v)}{f(2k-v)} \right)^j \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f(2k-v) + 2cz(2k-v))^2}{4c(2k-v)}\right) \right) +$$

$$e^{2i(\frac{\pi v}{2} - g)(v-2k)} \sum_{j=0}^n \left( -\frac{i(f(2k-v) + 2cz(2k-v))^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \left( -\frac{2f(2k-v) + 4cz(2k-v)}{f(2k-v)} \right)^j$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f(2k-v) + 2cz(2k-v))^2}{4c(2k-v)}\right) \right) \right) + \frac{2^{-v} z^{n+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{n+1} /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$



01.06.21.1072.01

$$\int z^n \sin^v(\sqrt{z} c + f z + g) dz = 2^{-v-1} f^{-2n-2} c^{2n} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(2k-v)^2} \left( (-1)^k 4^{-n} e^{-\frac{i(2k-v)c^2}{4f} - i\left(\frac{\pi v}{2} - g(v-2k)\right)} \binom{v}{k} \right.$$

$$\left. \left( e^{\frac{ic^2(2k-v)}{2f}} \sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{c(2k-v) + 2f\sqrt{z}(2k-v)}{c(2k-v)} \right)^{h+j} \left( \frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right.$$

$$\left. \left( c(2k-v)(c(2k-v) + 2f\sqrt{z}(2k-v)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)}\right) + \right. \right.$$

$$\left. 2f i(2k-v) \sqrt{\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)}} \right. \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)}\right) \right) \right) + e^{2i\left(\frac{\pi v}{2} - g(v-2k)\right)}$$

$$\sum_{j=0}^n \sum_{h=0}^j 4^j \left( -\frac{c(2k-v) + 2f\sqrt{z}(2k-v)}{c(2k-v)} \right)^{h+j} \left( -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h}$$

$$\binom{n}{j} \left( c(2k-v)(c(2k-v) + 2f\sqrt{z}(2k-v)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)}\right) - \right.$$

$$\left. 2if(2k-v) \sqrt{-\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{f(2k-v)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right.$$

$$\left. \left. -\frac{i(c(2k-v) + 2f\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) \right) \right) + \frac{2^{-v} z^{n+1} \left(\frac{v}{2}\right) (1-v \bmod 2)}{n+1} ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving powers of the direct function and algebraic functions**

Involving powers of sin and algebraic functions

### Involving $(az + b)^\beta$

01.06.21.1073.01

$$\int (az + b)^\beta \sin^\nu(cz) dz = \frac{2^{-\nu} (b + az)^{\beta+1} (1 - \nu \bmod 2) \left(\frac{\nu}{2}\right) -}{a(\beta + 1)} -$$

$$\frac{2^{-\nu} (b + az)^{\beta+1} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( i^\nu e^{\frac{ibc(v-2k)}{a}} \left( \frac{ic(v-2k)(b+az)}{a} \right)^{-\beta-1} \Gamma\left(\beta+1, \frac{ic(v-2k)(b+az)}{a}\right) + \right.$$

$$\left. i^{-\nu} e^{-\frac{ibc(v-2k)}{a}} \left( -\frac{ic(v-2k)(b+az)}{a} \right)^{-\beta-1} \Gamma\left(\beta+1, -\frac{ic(v-2k)(b+az)}{a}\right) \right) /; \nu \in \mathbb{N}$$

01.06.21.1074.01

$$\int (az + b)^\beta \sin^2(cz) dz =$$

$$\frac{1}{ac(\beta + 1)} \left( 2^{-\beta-3} (b + az)^\beta \left( \frac{c^2 (b + az)^2}{a^2} \right)^{-\beta} \left( a(\beta + 1) \Gamma\left(\beta + 1, -\frac{2ic(b + az)}{a}\right) \left( i \cos\left(\frac{2bc}{a}\right) + \sin\left(\frac{2bc}{a}\right) \right) \left( \frac{ic(b + az)}{a} \right)^\beta + \right.$$

$$\left. 2^{\beta+2} \left( \frac{c^2 (b + az)^2}{a^2} \right)^\beta c(b + az) + \left( -\frac{ic(b + az)}{a} \right)^\beta a(\beta + 1) \Gamma\left(\beta + 1, \frac{2ic(b + az)}{a}\right) \left( \sin\left(\frac{2bc}{a}\right) - i \cos\left(\frac{2bc}{a}\right) \right) \right)$$

01.06.21.1075.01

$$\int \frac{\sin^\nu(cz)}{\sqrt{az + b}} dz =$$

$$\frac{2^{1-\nu} \sqrt{b + az} (1 - \nu \bmod 2) \left(\frac{\nu}{2}\right) + \frac{2^{-\nu} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{i^\nu}{\sqrt{-\frac{ic(v-2k)}{a}}} e^{\frac{ibc(v-2k)}{a}} \operatorname{erfi} \left( \sqrt{-\frac{ic(v-2k)}{a}} \sqrt{b + az} \right) + \right.$$

$$\left. \frac{i^{-\nu}}{\sqrt{\frac{ic(v-2k)}{a}}} e^{-\frac{ibc(v-2k)}{a}} \operatorname{erfi} \left( \sqrt{\frac{ic(v-2k)}{a}} \sqrt{b + az} \right) \right) /; \nu \in \mathbb{N}$$

01.06.21.1076.01

$$\int \frac{\sin^2(cz)}{\sqrt{az + b}} dz =$$

$$\frac{1}{2c} \sqrt{\frac{c}{a}} \left( -\sqrt{\pi} \cos\left(\frac{2bc}{a}\right) C\left(\frac{2\sqrt{\frac{c}{a}} \sqrt{b + az}}{\sqrt{\pi}}\right) - \sqrt{\pi} S\left(\frac{2\sqrt{\frac{c}{a}} \sqrt{b + az}}{\sqrt{\pi}}\right) \sin\left(\frac{2bc}{a}\right) + 2\sqrt{\frac{c}{a}} \sqrt{b + az} \right)$$

### Involving products of the direct function and a power function

Involving products of two direct functions and a power function

Involving  $z^{\alpha-1} \sin(cz) \sin(az)$

01.06.21.1077.01

$$\int z^{\alpha-1} \sin(cz) \sin(az) dz = -\frac{1}{4} z^\alpha (\Gamma(\alpha, -i(a-c)z) (-i(a-c)z)^{-\alpha} + (i(a-c)z)^{-\alpha} \Gamma(\alpha, i(a-c)z) - (-i(a+c)z)^{-\alpha} \Gamma(\alpha, -i(a+c)z) - (i(a+c)z)^{-\alpha} \Gamma(\alpha, i(a+c)z))$$

01.06.21.1078.01

$$\int z^n \sin(cz) \sin(az) dz = \frac{1}{4} n! \left( -(-i(a-c))^{-n-1} e^{i(a-c)z} \sum_{k=0}^n \frac{(-i(a-c)z)^k}{k!} - (i(a-c))^{-n-1} e^{-i(a-c)z} \sum_{k=0}^n \frac{(i(a-c)z)^k}{k!} + (-i(a+c))^{-n-1} e^{i(a+c)z} \sum_{k=0}^n \frac{(-i(a+c)z)^k}{k!} + (i(a+c))^{-n-1} e^{-i(a+c)z} \sum_{k=0}^n \frac{(i(a+c)z)^k}{k!} \right); n \in \mathbb{N}$$

01.06.21.1079.01

$$\int z^{-n} \sin(cz) \sin(az) dz = -\frac{i}{4(c^2 - a^2)(n-1)!} \left( e^{-i(a-c)z} \left( -(a+c)(n-1)! (i(a-c))^n \sum_{k=1}^{n-1} \frac{(i(a-c))^{k-n} z^{k-n}}{(1-n)_k} + (-1)^n e^{i(a-c)z} ((a+c) \text{Ei}(-i(a-c)z) (i(a-c))^n + (a-c)(-i(a+c))^n \text{Ei}(i(a+c)z)) - (a-c)(-i(a+c))^n e^{2iaz} (n-1)! \sum_{k=1}^{n-1} \frac{(-i(a+c))^{k-n} z^{k-n}}{(1-n)_k} \right) + e^{-i(2a+c)z} \left( (a+c) e^{3iaz} (n-1)! (-i(a-c))^n \sum_{k=1}^{n-1} \frac{(-i(a-c))^{k-n} z^{k-n}}{(1-n)_k} - (-1)^n e^{i(2a+c)z} ((a+c) \text{Ei}(i(a-c)z) (-i(a-c))^n + (a-c)(i(a+c))^n \text{Ei}(-i(a+c)z)) + (a-c)(i(a+c))^n e^{iaz} (n-1)! \sum_{k=1}^{n-1} \frac{(i(a+c))^{k-n} z^{k-n}}{(1-n)_k} \right) \right); n \in \mathbb{N}^+$$

01.06.21.1080.01

$$\int \frac{\sin(cz) \sin(az)}{z} dz = \frac{1}{2} (\text{Ci}((a-c)z) - \text{Ci}((a+c)z))$$

Involving  $z^{\alpha-1} \sin(cz) \sin(az + b)$

01.06.21.1081.01

$$\int z^{\alpha-1} \sin(cz) \sin(b+az) dz = \frac{1}{4} e^{-ib} z^\alpha (-e^{2ib} \Gamma(\alpha, -i(a-c)z) (-i(a-c)z)^{-\alpha} - (i(a-c)z)^{-\alpha} \Gamma(\alpha, i(a-c)z) + e^{2ib} (-i(a+c)z)^{-\alpha} \Gamma(\alpha, -i(a+c)z) + (i(a+c)z)^{-\alpha} \Gamma(\alpha, i(a+c)z))$$

Involving  $z^{\alpha-1} \sin(cz + d) \sin(az + b)$

01.06.21.1082.01

$$\int z^{\alpha-1} \sin(d+cz) \sin(b+az) dz = -\frac{1}{4} e^{-i(b+d)} z^\alpha (e^{2ib} \Gamma(\alpha, -i(a-c)z) (-i(a-c)z)^{-\alpha} + e^{2id} (i(a-c)z)^{-\alpha} \Gamma(\alpha, i(a-c)z) - e^{2i(b+d)} (-i(a+c)z)^{-\alpha} \Gamma(\alpha, -i(a+c)z) - (i(a+c)z)^{-\alpha} \Gamma(\alpha, i(a+c)z))$$

### Involving $z^n \sin(dz) \sin(cz^r)$

01.06.21.1083.01

$$\int z^n \sin(dz) \sin(cz^2) dz = \frac{1}{8c^{n+1}} i e^{-\frac{id^2}{4c}} \left( -(-i)^n \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (i(d+2cz))^{j+1} \left( -\frac{i(d+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+2cz)^2}{4c}\right) + (-i)^n \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-i(d-2cz))^{j+1} \left( -\frac{i(d-2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d-2cz)^2}{4c}\right) + e^{\frac{id^2}{2c}} i^n \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-i(d+2cz))^{j+1} \left( \frac{i(d+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+2cz)^2}{4c}\right) - i^n e^{\frac{id^2}{2c}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (i(d-2cz))^{j+1} \left( \frac{i(d-2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d-2cz)^2}{4c}\right) \right) /; n \in \mathbb{N}$$

01.06.21.1084.01

$$\int z^n \sin(e+dz) \sin(c\sqrt{z}) dz = -2^{-2n-3} (id)^{-2n-2} \left( -e^{ie-\frac{ic^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-ic+2id\sqrt{z})^{h+j} \left( \frac{i(-ic+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2id\sqrt{\frac{i(-ic+2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ic+2id\sqrt{z})^2}{4d}\right) - ic(-ic+2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-ic+2id\sqrt{z})^2}{4d}\right) \right) + e^{ie-\frac{ic^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (ic+2id\sqrt{z})^{h+j} \left( \frac{i(ic+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(ic+2id\sqrt{z}) \right) \right)$$

$$\begin{aligned}
 & \left( \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ic+2id\sqrt{z})^2}{4d}\right) + 2\sqrt{\frac{i(ic+2id\sqrt{z})^2}{d}} \, di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ic+2id\sqrt{z})^2}{4d}\right) \right) + \\
 & e^{\frac{ic^2}{4d}-ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-ic-2id\sqrt{z})^{h+j} \left( -\frac{i(-ic-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( -ic(-ic-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ic-2id\sqrt{z})^2}{4d}\right) - \right. \\
 & \left. 2id\sqrt{-\frac{i(-ic-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ic-2id\sqrt{z})^2}{4d}\right) \right) - \\
 & e^{\frac{ic^2}{4d}-ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (ic-2id\sqrt{z})^{h+j} \left( -\frac{i(ic-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( ic(ic-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ic-2id\sqrt{z})^2}{4d}\right) - \right. \\
 & \left. 2id\sqrt{-\frac{i(ic-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(ic-2id\sqrt{z})^2}{4d}\right) \right) \Bigg| ; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(dz + e) \sin(cz')$**

01.06.21.1085.01

$$\int z^n \sin(dz + e) \sin(cz^2) dz =$$

$$\frac{1}{8} \left( (-ic)^{-n-1} e^{\frac{id^2}{4c} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2icz)^{j+1} \left( -\frac{i(-id - 2icz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2icz)^2}{4c}\right) - \right.$$

$$(-ic)^{-n-1} e^{\frac{id^2}{4c} + ie} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id - 2icz)^{j+1} \left( -\frac{i(id - 2icz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(id - 2icz)^2}{4c}\right) -$$

$$(ic)^{-n-1} e^{-\frac{id^2}{4c} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2icz)^{j+1} \left( \frac{i(-id + 2icz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-id + 2icz)^2}{4c}\right) +$$

$$\left. (ic)^{-n-1} e^{\frac{id^2}{4c} - ie} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2icz)^{j+1} \left( \frac{i(id + 2icz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2icz)^2}{4c}\right) \right) ; n \in \mathbb{N}$$

01.06.21.1086.01

$$\int z^n \sin(e + dz) \sin(c\sqrt{z}) dz =$$

$$-2^{-2n-3} (id)^{-2n-2} \left( -e^{ie - \frac{ic^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-ic + 2id\sqrt{z})^{h+j} \left( \frac{i(-ic + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \right.$$

$$\binom{j}{h} \binom{n}{j} \left( 2id \sqrt{\frac{i(-ic + 2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ic + 2id\sqrt{z})^2}{4d}\right) - \right.$$

$$\left. ic(-ic + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-ic + 2id\sqrt{z})^2}{4d}\right) \right) +$$

$$e^{ie - \frac{ic^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (ic + 2id\sqrt{z})^{h+j} \left( \frac{i(ic + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(ic + 2id\sqrt{z}) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ic + 2id\sqrt{z})^2}{4d}\right) + 2 \sqrt{\frac{i(ic + 2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ic + 2id\sqrt{z})^2}{4d}\right) \right) +$$

$$\begin{aligned}
 & e^{\frac{ic^2}{4d}-ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-ic-2id\sqrt{z})^{h+j} \left( -\frac{i(-ic-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( -ic(-ic-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ic-2id\sqrt{z})^2}{4d}\right) - \right. \\
 & \left. 2id \sqrt{-\frac{i(-ic-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ic-2id\sqrt{z})^2}{4d}\right) \right) - \\
 & e^{\frac{ic^2}{4d}-ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (ic-2id\sqrt{z})^{h+j} \left( -\frac{i(ic-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( ic(ic-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ic-2id\sqrt{z})^2}{4d}\right) - \right. \\
 & \left. 2id \sqrt{-\frac{i(ic-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(ic-2id\sqrt{z})^2}{4d}\right) \right) \Bigg| ; n \in \mathbb{N}
 \end{aligned}$$

### Involving $z^{\alpha-1} \sin(bz^r) \sin(cz^r)$

01.06.21.1087.01

$$\begin{aligned}
 \int z^{\alpha-1} \sin(bz^r) \sin(cz^r) dz = & \frac{z^\alpha}{4r} \left( -\Gamma\left(\frac{\alpha}{r}, (-ib+ic)z^r\right) ((-ib+ic)z^r)^{-\frac{\alpha}{r}} + \right. \\
 & \left. ((ib+ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib+ic)z^r\right) + ((-ib-ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-ib-ic)z^r\right) - ((ib-ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-ic)z^r\right) \right)
 \end{aligned}$$

01.06.21.1088.01

$$\begin{aligned}
 \int z^n \sin(bz^2) \sin(cz^2) dz = & \\
 -\frac{1}{8} z^{n+1} \left( \Gamma\left(\frac{n+1}{2}, (-ib+ic)z^2\right) ((-ib+ic)z^2)^{\frac{1}{2}(-n-1)} - ((ib+ic)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib+ic)z^2\right) - \right. \\
 & \left. ((-ib-ic)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib-ic)z^2\right) + ((ib-ic)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib-ic)z^2\right) \right) ; n \in \mathbb{N}
 \end{aligned}$$

01.06.21.1089.01

$$\int z^n \sin(\sqrt{z} b) \sin(\sqrt{z} c) dz = \frac{1}{2} \left( -\Gamma(2(n+1), (-ib+ic)\sqrt{z}) (-ib+ic)^{-2(n+1)} + (ib+ic)^{-2(n+1)} \Gamma(2(n+1), (ib+ic)\sqrt{z}) + (-ib-ic)^{-2(n+1)} \Gamma(2(n+1), (-ib-ic)\sqrt{z}) - (ib-ic)^{-2(n+1)} \Gamma(2(n+1), (ib-ic)\sqrt{z}) \right) /; n \in \mathbb{N}$$

### Involving $z^n \sin(dz) \sin(cz^2 + g)$

01.06.21.1090.01

$$\int z^n \sin(dz) \sin(cz^2 + g) dz = \frac{1}{8} i c^{-2n-1} e^{-\frac{i(d^2+4cg)}{4c}} \left( e^{2ig} \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (i(2cz-d))^{j+1} \left( -\frac{i(2cz-d)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(2cz-d)^2}{4c}\right) \right) (-ic)^n - e^{2ig} \left( \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (i(d+2cz))^{j+1} \left( -\frac{i(d+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+2cz)^2}{4c}\right) \right) (-ic)^n - (ic)^n e^{\frac{id^2}{2c}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (-i(2cz-d))^{j+1} \left( \frac{i(2cz-d)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2cz-d)^2}{4c}\right) + (ic)^n e^{\frac{id^2}{2c}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-i(d+2cz))^{j+1} \left( \frac{i(d+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+2cz)^2}{4c}\right) \right) /; n \in \mathbb{N}$$



01.06.21.1091.01

$$\int z^n \sin(dz) \sin(\sqrt{z} c + g) dz = (-1)^n 2^{-2n-3} d^{-2(n+1)} e^{-\frac{i(c^2+4dg)}{4d}}$$

$$\left( -e^{\frac{ic^2}{2d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-i(c+2d\sqrt{z}))^{h+j} \left( \frac{i(c+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c(c+2d\sqrt{z}) \right. \right.$$

$$\left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c+2d\sqrt{z})^2}{4d} \right) + 2\sqrt{\frac{i(c+2d\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c+2d\sqrt{z})^2}{4d} \right) \right) +$$

$$e^{\frac{i(c^2+4dg)}{2d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c-2d\sqrt{z}))^{h+j} \left( \frac{i(c-2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c(c-2d\sqrt{z}) \right.$$

$$\left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c-2d\sqrt{z})^2}{4d} \right) + 2\sqrt{\frac{i(c-2d\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c-2d\sqrt{z})^2}{4d} \right) \right) +$$

$$e^{2ig} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c+2d\sqrt{z}))^{h+j} \left( -\frac{i(c+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2id\sqrt{-\frac{i(c+2d\sqrt{z})^2}{d}} \right.$$

$$\left. \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(c+2d\sqrt{z})^2}{4d} \right) - c(c+2d\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(c+2d\sqrt{z})^2}{4d} \right) \right) +$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-i(c-2d\sqrt{z}))^{h+j} \left( -\frac{i(c-2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( c(c-2d\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(c-2d\sqrt{z})^2}{4d} \right) - \right.$$

$$\left. 2id\sqrt{-\frac{i(c-2d\sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(c-2d\sqrt{z})^2}{4d} \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n \sin(dz + e) \sin(cz' + g)$

01.06.21.1092.01

$$\int z^n \sin(e + dz) \sin(cz^2 + g) dz = \frac{1}{8} i c^{-2n-1} e^{-\frac{i(d^2+4c(e+g))}{4c}}$$

$$\left( e^{2ig} \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (i(2cz-d))^{j+1} \left( -\frac{i(2cz-d)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(2cz-d)^2}{4c}\right) \right) (-ic)^n - \right.$$

$$e^{2i(e+g)} \left( \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (i(d+2cz))^{j+1} \left( -\frac{i(d+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+2cz)^2}{4c}\right) \right) (-ic)^n -$$

$$(ic)^n e^{\frac{i(d^2+4c)}{2c}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (-i(2cz-d))^{j+1} \left( \frac{i(2cz-d)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2cz-d)^2}{4c}\right) +$$

$$(ic)^n e^{\frac{id^2}{2c}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-i(d+2cz))^{j+1} \left( \frac{i(d+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+2cz)^2}{4c}\right) \Big/ ; n \in \mathbb{N}$$

01.06.21.1093.01

$$\int z^n \sin(dz + e) \sin(\sqrt{z} c + g) dz = (-1)^n 2^{-2n-3} d^{-2(n+1)} e^{-\frac{i(c^2+4d(e+g))}{4d}}$$

$$\left( -e^{\frac{ic^2}{2d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-i(c+2d\sqrt{z}))^{h+j} \left( \frac{i(c+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c(c+2d\sqrt{z}) \right) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2d\sqrt{z})^2}{4d}\right) + 2\sqrt{\frac{i(c+2d\sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2d\sqrt{z})^2}{4d}\right) \right) +$$

$$e^{\frac{i(c^2+4dg)}{2d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c-2d\sqrt{z}))^{h+j} \left( \frac{i(c-2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c(c-2d\sqrt{z}) \right)$$

$$\left. \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c-2d\sqrt{z})^2}{4d}\right) + 2\sqrt{\frac{i(c-2d\sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c-2d\sqrt{z})^2}{4d}\right) \right) +$$

$$e^{2i(e+g)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c+2d\sqrt{z}))^{h+j} \left( -\frac{i(c+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( 2 i d \sqrt{-\frac{i(c+2 d \sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2 d \sqrt{z})^2}{4 d}\right) - \right. \\ \left. c(c+2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2 d \sqrt{z})^2}{4 d}\right) \right) + \\ e^{2 i e} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c)^{-h-j+2 n} (-i(c-2 d \sqrt{z}))^{h+j} \left(-\frac{i(c-2 d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\ \binom{n}{j} \left( c(c-2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c-2 d \sqrt{z})^2}{4 d}\right) - \right. \\ \left. 2 i d \sqrt{-\frac{i(c-2 d \sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c-2 d \sqrt{z})^2}{4 d}\right) \right) / ; n \in \mathbb{N}$$

### Involving $z^{\alpha-1} \sin(b z^r) \sin(c z^r + g)$

01.06.21.1094.01

$$\int z^{\alpha-1} \sin(b z^r) \sin(c z^r + g) dz = \\ \frac{1}{4 r} z^{\alpha} \left( -e^{-i g} \Gamma\left(\frac{\alpha}{r}, (-i b + i c) z^r\right) ((-i b + i c) z^r)^{-\frac{\alpha}{r}} + e^{-i g} ((i b + i c) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (i b + i c) z^r\right) + \right. \\ \left. e^{i g} ((-i b - i c) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-i b - i c) z^r\right) - e^{i g} ((i b - i c) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (i b - i c) z^r\right) \right)$$

01.06.21.1095.01

$$\int z^n \sin(b z^2) \sin(c z^2 + g) dz = \\ -\frac{1}{8} z^{n+1} \left( e^{-i g} \Gamma\left(\frac{n+1}{2}, (-i b + i c) z^2\right) ((-i b + i c) z^2)^{\frac{1}{2}(-n-1)} - e^{-i g} ((i b + i c) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b + i c) z^2\right) - \right. \\ \left. e^{i g} ((-i b - i c) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-i b - i c) z^2\right) + e^{i g} ((i b - i c) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b - i c) z^2\right) \right) / ; n \in \mathbb{N}$$

01.06.21.1096.01

$$\int z^n \sin(\sqrt{z} b) \sin(\sqrt{z} c + g) dz = \\ \frac{1}{2} \left( -e^{-i g} \Gamma(2(n+1), (-i b + i c) \sqrt{z}) (-i b + i c)^{-2(n+1)} + (i b + i c)^{-2(n+1)} e^{-i g} \Gamma(2(n+1), (i b + i c) \sqrt{z}) + \right. \\ \left. (-i b - i c)^{-2(n+1)} e^{i g} \Gamma(2(n+1), (-i b - i c) \sqrt{z}) - (i b - i c)^{-2(n+1)} e^{i g} \Gamma(2(n+1), (i b - i c) \sqrt{z}) \right) / ; n \in \mathbb{N}$$

### Involving $z^{\alpha-1} \sin(bz^r + e) \sin(cz^r + g)$

01.06.21.1097.01

$$\int z^{\alpha-1} \sin(bz^r + e) \sin(cz^r + g) dz = \frac{z^\alpha}{4r} \left( -e^{-ig+ie} \Gamma\left(\frac{\alpha}{r}, (-ib+ic)z^r\right) ((-ib+ic)z^r)^{-\frac{\alpha}{r}} + e^{-ig-ie} ((ib+ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib+ic)z^r\right) + e^{ig+ie} ((-ib-ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-ib-ic)z^r\right) - e^{ig-ie} ((ib-ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-ic)z^r\right) \right)$$

01.06.21.1098.01

$$\int z^n \sin(bz^2 + e) \sin(cz^2 + g) dz = -\frac{1}{8} z^{n+1} \left( e^{ie-ig} \Gamma\left(\frac{n+1}{2}, (-ib+ic)z^2\right) ((-ib+ic)z^2)^{\frac{1}{2}(-n-1)} - e^{-ie-ig} ((ib+ic)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib+ic)z^2\right) - e^{ie+ig} ((-ib-ic)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib-ic)z^2\right) + e^{-ie+ig} ((ib-ic)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib-ic)z^2\right) \right); n \in \mathbb{N}$$

01.06.21.1099.01

$$\int z^n \sin(\sqrt{z}b + e) \sin(\sqrt{z}c + g) dz = \frac{1}{2} \left( -e^{ie-ig} \Gamma(2(n+1), (-ib+ic)\sqrt{z}) (-ib+ic)^{-2(n+1)} + (ib+ic)^{-2(n+1)} e^{-ie-ig} \Gamma(2(n+1), (ib+ic)\sqrt{z}) + (-ib-ic)^{-2(n+1)} e^{ie+ig} \Gamma(2(n+1), (-ib-ic)\sqrt{z}) - (ib-ic)^{-2(n+1)} e^{-ie+ig} \Gamma(2(n+1), (ib-ic)\sqrt{z}) \right); n \in \mathbb{N}$$

### Involving $z^n \sin(dz) \sin(cz^r + fz)$

01.06.21.1100.01

$$\int z^n \sin(dz) \sin(cz^2 + fz) dz = \frac{1}{8} i c^{-2n-1} e^{-\frac{i(d+f)^2}{4c}} \left( e^{\frac{idf}{c}} \left( \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (i(-d+f+2cz))^{j+1} \left( -\frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-d+f+2cz)^2}{4c}\right) \right) \right. \\ \left. (-ic)^n - \left( \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j} (i(d+f+2cz))^{j+1} \left( -\frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+f+2cz)^2}{4c}\right) \right) \right) \\ (-ic)^n - (ic)^n e^{\frac{i(d^2+f^2)}{2c}} \\ \left. \sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j} (-i(-d+f+2cz))^{j+1} \left( \frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-d+f+2cz)^2}{4c}\right) + (ic)^n \right. \\ \left. e^{\frac{i(d+f)^2}{2c}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} (-i(d+f+2cz))^{j+1} \left( \frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+f+2cz)^2}{4c}\right) \right); n \in \mathbb{N}$$

01.06.21.1101.01

$$\int z^n \sin(dz) \sin(\sqrt{z} c + fz + g) dz =$$

$$(-1)^n 2^{-2n-3} e^{-ig} \left( e^{\frac{ic^2}{4f-4d}} \left( e^{\frac{1}{2}i\left(\frac{c^2}{d-f}+4g\right)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} \left( i(c+2(f-d)\sqrt{z}) \right)^{h+j} \left( \frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)} \right) \right) + \right.$$

$$\left. 2 \sqrt{\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} (d-f) i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)} \right) \right) +$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} \left( i(2(d-f)\sqrt{z}-c) \right)^{h+j} \left( \frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\left. \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)} \right) \right) - \right.$$

$$\left. 2i(d-f) \sqrt{-\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)} \right) \right) \left( d-f \right)^{-2(n+1)} +$$

$$e^{-\frac{ic^2}{4(d+f)}} (d+f)^{-2(n+1)} \left( e^{2ig} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} \left( i(c+2(d+f)\sqrt{z}) \right)^{h+j} \left( -\frac{i(c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( 2i(d+f) \sqrt{-\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) - \right.$$

$$\left. c(c+2(d+f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) -$$

$$e^{\frac{ic^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} \left( -i(c+2(d+f)\sqrt{z}) \right)^{h+j} \left( \frac{i(c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\left( \binom{j}{h} \binom{n}{j} \left( c(c+2(d+f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) + \right.$$

$$\left. 2 \sqrt{\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} (d+f) i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) \Bigg) /; n \in \mathbb{N}$$

### Involving $z^n \sin(dz + e) \sin(cz' + fz)$

01.06.21.1102.01

$$\int z^n \sin(dz + e) \sin(cz^2 + fz) dz = \frac{1}{8} i c^{-2n-1} e^{-\frac{i(d^2+2fd+f^2+4ce)}{4c}}$$

$$\left( e^{\frac{idf}{c}} \left( \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (i(-d+f+2cz))^{j+1} \left( -\frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(-d+f+2cz)^2}{4c} \right) \right) \right.$$

$$\left. (-ic)^n - e^{2ie} \left( \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j} (i(d+f+2cz))^{j+1} \left( -\frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \right) \right.$$

$$\left. \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(d+f+2cz)^2}{4c} \right) \right) (-ic)^n - (ic)^n e^{\frac{i(d^2+f^2+4ce)}{2c}}$$

$$\sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j} (-i(-d+f+2cz))^{j+1} \left( \frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(-d+f+2cz)^2}{4c} \right) + (ic)^n$$

$$e^{\frac{i(d+f)^2}{2c}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} (-i(d+f+2cz))^{j+1} \left( \frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(d+f+2cz)^2}{4c} \right) \Bigg) /; n \in \mathbb{N}$$

01.06.21.1103.01

$$\int z^n \sin(dz + e) \sin(\sqrt{z} c + fz + g) dz =$$

$$(-1)^n 2^{-2n-3} e^{-i(e+g)} \left( \left( e^{\frac{1}{4}i\left(\frac{c^2}{d-f}+8g\right)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} \left( i(c+2(f-d)\sqrt{z}) \right)^{h+j} \left( \frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) + \right. \\
 & \left. 2\sqrt{\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} (d-f) i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \right) + \\
 & e^{-\frac{i(c^2+8e(f-d))}{4(d-f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (i(2(d-f)\sqrt{z}-c))^{h+j} \left( -\frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) - \right. \\
 & \left. 2i(d-f) \sqrt{-\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \right) (d-f)^{-2n-2} + \\
 & e^{-\frac{ic^2}{4(d+f)}} (d+f)^{-2n-2} \left( e^{2i(e+g)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c+2(d+f)\sqrt{z}))^{h+j} \left( -\frac{i(c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2i(d+f) \sqrt{-\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) - \right. \right. \\
 & \left. \left. c(c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) \right) - \\
 & e^{\frac{ic^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-i(c+2(d+f)\sqrt{z}))^{h+j} \left( \frac{i(c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c(c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) + \right. \\
 & \left. \sqrt{\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} (d+f) i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) +
 \end{aligned}$$

### Involving $z^n \sin(b z^r) \sin(c z^r + f z)$

01.06.21.1104.01

$$\int z^n \sin(b z^2) \sin(c z^2 + f z) dz = \frac{1}{8} \left( -(-i(b-c))^{-n-1} e^{\frac{if^2}{4(b-c)}} \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(c-b)z))^{j+1} \left( \frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(c-b)z)^2}{4(b-c)}\right) - (i(b-c))^{-n-1} e^{\frac{if^2}{4c-4b}} \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(c-b)z))^{j+1} \left( -\frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(c-b)z)^2}{4(b-c)}\right) + (-i(b+c))^{-n-1} e^{\frac{if^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(b+c)z))^{j+1} \left( \frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(b+c)z)^2}{4(b+c)}\right) + (i(b+c))^{-n-1} e^{-\frac{if^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(b+c)z))^{j+1} \left( -\frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(b+c)z)^2}{4(b+c)}\right) \right); n \in \mathbb{N}$$

01.06.21.1105.01

$$\int z^n \sin(b \sqrt{z}) \sin(\sqrt{z} c + f z) dz = (-1)^n 2^{-2n-3} f^{-2(n+1)} \left( e^{\frac{i(b-c)^2}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c-2f\sqrt{z}))^{h+j} \left( \frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) + 2 \sqrt{\frac{i(-b+c+2f\sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \right) - e^{-\frac{i(b+c)^2}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2f\sqrt{z}))^{h+j} \left( \frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \right)$$



$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(b+c+2f\sqrt{z})^2}{4f} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(b+c+2f\sqrt{z})^2}{f}} f i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(b+c+2f\sqrt{z})^2}{4f} \right) \right) + \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2f\sqrt{z}))^{h+j} \left( -\frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b+c+2f\sqrt{z})^2}{4f} \right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(b+c+2f\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b+c+2f\sqrt{z})^2}{4f} \right) \right) + \\
 & e^{-\frac{i(b-c)^2}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c-2f\sqrt{z}))^{h+j} \left( -\frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-b+c+2f\sqrt{z})^2}{4f} \right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(-b+c+2f\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-b+c+2f\sqrt{z})^2}{4f} \right) \right) /; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(bz^r + e) \sin(cz^r + fz)$**

01.06.21.1106.01

$$\int z^n \sin(bz^2 + e) \sin(cz^2 + fz) dz =$$

$$\frac{1}{8} e^{-ie} \left( -e^{\frac{if^2}{4(b-c)}} \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(c-b)z))^{j+1} \left( \frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(c-b)z)^2}{4(b-c)}\right) \right)$$

$$(-i(b-c))^{-n-1} - (i(b-c))^{-n-1} e^{-\frac{i(f^2-8be+8ce)}{4(b-c)}}$$

$$\sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(c-b)z))^{j+1} \left( -\frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(c-b)z)^2}{4(b-c)}\right) +$$

$$(-i(b+c))^{-n-1} e^{\frac{if^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(b+c)z))^{j+1} \left( \frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(b+c)z)^2}{4(b+c)}\right) + (i(b+c))^{-n-1} e^{\frac{i(-f^2+8be+8ce)}{4(b+c)}}$$

$$\sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(b+c)z))^{j+1} \left( -\frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(b+c)z)^2}{4(b+c)}\right) \Big/; n \in \mathbb{N}$$

01.06.21.1107.01

$$\int z^n \sin(\sqrt{z} b + e) \sin(\sqrt{z} c + fz) dz =$$

$$(-1)^n 2^{-2n-3} e^{-ie} f^{-2(n+1)} \left( e^{\frac{i(b^2-2cb+c^2+8ef)}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c-2f\sqrt{z}))^{h+j} \right)$$

$$\left( \frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \right) +$$

$$2 \sqrt{\frac{i(-b+c+2f\sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \Big)$$

$$e^{\frac{i(b+c)^2}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2f\sqrt{z}))^{h+j} \left( \frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(b+c+2f\sqrt{z})^2}{4f} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(b+c+2f\sqrt{z})^2}{f}} f i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(b+c+2f\sqrt{z})^2}{4f} \right) \right) + \\
 & e^{-\frac{i(b-c)^2}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c-2f\sqrt{z}))^{h+j} \left( -\frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-b+c+2f\sqrt{z})^2}{4f} \right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(-b+c+2f\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-b+c+2f\sqrt{z})^2}{4f} \right) \right) - \\
 & e^{2ie-\frac{i(b+c)^2}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2f\sqrt{z}))^{h+j} \left( -\frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b+c+2f\sqrt{z})^2}{4f} \right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(b+c+2f\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b+c+2f\sqrt{z})^2}{4f} \right) \right) \Bigg| ; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(bz^r + dz) \sin(cz^r + fz)$**

01.06.21.1108.01

$$\int z^n \sin(bz^2 + dz) \sin(cz^2 + fz) dz =$$

$$\frac{1}{8} \left( -e^{\frac{i(d-f)^2}{4(b-c)}} \left( \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (-i(d-f+2bz-2cz))^{j+1} \left( \frac{i(d-f+2bz-2cz)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right. \right.$$

$$\left. \Gamma \left( \frac{j+1}{2}, \frac{i(d-f+2bz-2cz)^2}{4(b-c)} \right) \right) (-i(b-c))^{-n-1} - (i(b-c))^{-n-1} e^{-\frac{i(d-f)^2}{4(b-c)}} \sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j}$$

$$(i(d-f+2bz-2cz))^{j+1} \left( -\frac{i(d-f+2bz-2cz)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(d-f+2bz-2cz)^2}{4(b-c)} \right) +$$

$$(-i(b+c))^{-n-1} e^{\frac{i(d+f)^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} (-i(d+f+2(b+c)z))^{j+1} \left( \frac{i(d+f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(d+f+2(b+c)z)^2}{4(b+c)} \right) + (i(b+c))^{-n-1} e^{-\frac{i(d+f)^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j}$$

$$(i(d+f+2(b+c)z))^{j+1} \left( -\frac{i(d+f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(d+f+2(b+c)z)^2}{4(b+c)} \right) \Bigg) ; n \in \mathbb{N}$$

01.06.21.1109.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin(\sqrt{z} c + fz) dz = -(-1)^n 2^{-2n-3}$$

$$\left( -e^{-\frac{i(b+c)^2}{4(d+f)}} \left( e^{\frac{i(b+c)^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2(d+f)\sqrt{z}))^{h+j} \left( \frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\binom{j}{h} \binom{n}{j} \left( (-b-c)(b+c+2(d+f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) - \right.$$

$$\left. \left. 2i(d+f) \sqrt{\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) \right) +$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2(d+f)\sqrt{z}))^{h+j} \left( -\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( (-b-c)(b+c+2(d+f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) + \right. \\
 & \left. 2 \sqrt{-\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f}} (d+f) i \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) (d+f)^{-2n-2} + \\
 & \frac{1}{(d-f)^{2n+2}} \left( e^{\frac{i(b-c)^2}{4(d-f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c+2(d-f)\sqrt{z}))^{h+j} \right. \\
 & \left. \left( \frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (c-b)(b-c+2(d-f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) - \right. \right. \\
 & \left. \left. 2i(d-f) \sqrt{\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) \right) \right) + \frac{1}{(d-f)^{2n+2}} \\
 & \left( e^{-\frac{i(b-c)^2}{4(d-f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c+2(d-f)\sqrt{z}))^{h+j} \left( -\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( (c-b)(b-c+2(d-f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) + \right. \right. \\
 & \left. \left. 2 \sqrt{-\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f}} (d-f) i \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) \right) \right) /; n \in \mathbb{N}
 \end{aligned}$$

Involving  $z^n \sin(dz) \sin(cz' + fz + g)$

01.06.21.1110.01

$$\int z^n \sin(dz) \sin(cz^2 + fz + g) dz = \frac{1}{8} i c^{-2n-1} e^{-\frac{i(d^2+2fd+f^2+4cg)}{4c}}$$

$$\left( e^{i\left(\frac{df}{c}+2g\right)} \left( \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (i(-d+f+2cz))^{j+1} \left( -\frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-d+f+2cz)^2}{4c}\right) \right) \right.$$

$$\left. (-ic)^n - e^{2ig} \left( \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j} (i(d+f+2cz))^{j+1} \left( -\frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+f+2cz)^2}{4c}\right) \right) \right) (-ic)^n - (ic)^n e^{\frac{i(d^2+f^2)}{2c}}$$

$$\sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j} (-i(-d+f+2cz))^{j+1} \left( \frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-d+f+2cz)^2}{4c}\right) + (ic)^n$$

$$e^{\frac{i(d+f)^2}{2c}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} (-i(d+f+2cz))^{j+1} \left( \frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+f+2cz)^2}{4c}\right) \Big/ ; n \in \mathbb{N}$$

01.06.21.1111.01

$$\int z^n \sin(dz) \sin(\sqrt{z}c + fz + g) dz =$$

$$(-1)^n 2^{-2n-3} e^{-ig} \left( e^{\frac{ic^2}{4f-4d}} \left( e^{\frac{1}{2}i\left(\frac{c^2}{d-f}+4g\right)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} \left( i(c+2(f-d)\sqrt{z}) \right)^{h+j} \left( \frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \right) + \right.$$

$$\left. 2\sqrt{\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} (d-f) i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \right) +$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} \left( i(2(d-f)\sqrt{z}-c) \right)^{h+j} \left( -\frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) - \right.$$

$$\begin{aligned}
 & 2i(d-f) \sqrt{-\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \Bigg) (d-f)^{-2(n+1)} + \\
 & e^{-\frac{ic^2}{4(d+f)}} (d+f)^{-2(n+1)} \left( e^{2ig} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c+2(d+f)\sqrt{z}))^{h+j} \left(-\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}\right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \binom{j}{h} \binom{n}{j} \left( 2i(d+f) \sqrt{-\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) - \right. \\
 & \left. c(c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) - \\
 & e^{\frac{ic^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (-i(c+2(d+f)\sqrt{z}))^{h+j} \left(\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c(c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) + \right. \\
 & \left. 2 \sqrt{\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} (d+f) i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) \Bigg) /; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(dz + e) \sin(cz' + fz + g)$**

01.06.21.1112.01

$$\int z^n \sin(dz + e) \sin(cz^2 + fcz + g) dz = \frac{1}{8c} i c^{-2n} e^{-\frac{i(d^2+2fd+f^2+4c(e+g))}{4c}}$$

$$\left( e^{i\left(\frac{df}{c}+2g\right)} \left( \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (i(-d+f+2cz))^{j+1} \left( -\frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-d+f+2cz)^2}{4c}\right) \right) \right.$$

$$\left. (-ic)^n - e^{2i(e+g)} \left( \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j} (i(d+f+2cz))^{j+1} \left( -\frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+f+2cz)^2}{4c}\right) \right) \right)$$

$$\left( (-ic)^n - (ic)^n e^{\frac{i(d^2+f^2+4ce)}{2c}} \sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j} (-i(-d+f+2cz))^{j+1} \left( \frac{i(-d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-d+f+2cz)^2}{4c}\right) + (ic)^n \right.$$

$$\left. e^{\frac{i(d+f)^2}{2c}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} (-i(d+f+2cz))^{j+1} \left( \frac{i(d+f+2cz)^2}{c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+f+2cz)^2}{4c}\right) \right) /; n \in \mathbb{N}$$

01.06.21.1113.01

$$\int z^n \sin(dz + e) \sin(\sqrt{z} c + fcz + g) dz =$$

$$(-1)^n 2^{-2n-3} e^{-i(e+g)} \left( \left( e^{\frac{1}{4}i\left(\frac{c^2}{d-f}+8g\right)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} (i(c+2(f-d)\sqrt{z}))^{h+j} \left( \frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right) \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) + \right. \right.$$

$$\left. \left. 2\sqrt{\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} (d-f) i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \right) \right) +$$

$$e^{-\frac{i(c^2+8e(f-d))}{4(d-f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} (i(2(d-f)\sqrt{z}-c))^{h+j} \left( -\frac{i(c+2(f-d)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\left. \binom{j}{h} \binom{n}{j} \left( c(c+2(f-d)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) - \right.$$



$$\begin{aligned}
 & 2i(d-f) \sqrt{-\frac{i(c+2(f-d)\sqrt{z})^2}{d-f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2(f-d)\sqrt{z})^2}{4(d-f)}\right) \Bigg) (d-f)^{-2n-2} + \\
 & e^{-\frac{ic^2}{4(d+f)}} (d+f)^{-2n-2} \left( e^{2i(e+g)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic)^{-h-j+2n} \left( i(c+2(d+f)\sqrt{z}) \right)^{h+j} \left( -\frac{i(c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \binom{j}{h} \binom{n}{j} \left( 2i(d+f) \sqrt{-\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) - \right. \\
 & \left. c(c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) - \\
 & e^{\frac{ic^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic)^{-h-j+2n} \left( -i(c+2(d+f)\sqrt{z}) \right)^{h+j} \left( \frac{i(c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c(c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) + \right. \\
 & \left. 2 \sqrt{\frac{i(c+2(d+f)\sqrt{z})^2}{d+f}} (d+f) i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) \Bigg) /; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(bz^r) \sin(cz^r + fz + g)$**

01.06.21.1114.01

$$\int z^n \sin(b z^2) \sin(c z^2 + f z + g) dz =$$

$$\frac{1}{8} e^{-ig} \left( -e^{\frac{1}{4}i\left(\frac{f^2}{b-c}+8g\right)} \left( \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(c-b)z))^{j+1} \left( \frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(c-b)z)^2}{4(b-c)}\right) \right) \right. \\ \left. (-i(b-c))^{-n-1} - (i(b-c))^{-n-1} e^{\frac{if^2}{4c-4b}} \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(c-b)z))^{j+1} \left( -\frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(c-b)z)^2}{4(b-c)}\right) + \right. \\ \left. (-i(b+c))^{-n-1} e^{\frac{if^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(b+c)z))^{j+1} \left( \frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(b+c)z)^2}{4(b+c)}\right) + (i(b+c))^{-n-1} e^{2ig-\frac{if^2}{4(b+c)}} \right. \\ \left. \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(b+c)z))^{j+1} \left( -\frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(b+c)z)^2}{4(b+c)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.1115.01

$$\int z^n \sin(\sqrt{z} b) \sin(\sqrt{z} c + f z + g) dz = -(-1)^n 2^{-2n-3} e^{-ig} f^{-2n-2}$$

$$\left( e^{-\frac{i(b+c)^2}{4f}} \left( -e^{\frac{i(b^2+c^2)}{2f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c-2f\sqrt{z}))^{h+j} \left( \frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \right) \right. \\ \left. \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) + 2\sqrt{\frac{i(-b+c+2f\sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \right) \right) + \\ e^{\frac{i(b+c)^2}{2f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2f\sqrt{z}))^{h+j} \left( \frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\ \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(b+c+2f\sqrt{z})^2}{4f}\right) + \right.$$

$$\begin{aligned}
 & 2\sqrt{\frac{i(b+c+2f\sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(b+c+2f\sqrt{z})^2}{4f}\right) + \\
 & e^{2ig} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2f\sqrt{z}))^{h+j} \left(-\frac{i(b+c+2f\sqrt{z})^2}{f}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(b+c+2f\sqrt{z})^2}{4f}\right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(b+c+2f\sqrt{z})^2}{f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(b+c+2f\sqrt{z})^2}{4f}\right) \right) - \\
 & e^{-\frac{i(b^2-2cb+c^2-8fg)}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c-2f\sqrt{z}))^{h+j} \left(-\frac{i(-b+c+2f\sqrt{z})^2}{f}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(-b+c+2f\sqrt{z})^2}{f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \right) /; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(bz^r + e) \sin(cz^r + fz + g)$**

01.06.21.1116.01

$$\int z^n \sin(bz^2 + e) \sin(cz^2 + fz + g) dz = \frac{1}{8} e^{-i(e+g)}$$

$$\left( -e^{\frac{1}{4}i\left(\frac{f^2}{b-c} + 8g\right)} \left( \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(c-b)z))^{j+1} \left( \frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(c-b)z)^2}{4(b-c)}\right) \right) \right.$$

$$\left. (-i(b-c))^{-n-1} - (i(b-c))^{-n-1} e^{-\frac{i(f^2-8be+8ce)}{4(b-c)}} \right.$$

$$\left. \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(c-b)z))^{j+1} \left( -\frac{i(f+2(c-b)z)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(c-b)z)^2}{4(b-c)}\right) + \right.$$

$$\left. (-i(b+c))^{-n-1} e^{\frac{if^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (if)^{n-j} (-i(f+2(b+c)z))^{j+1} \left( \frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f+2(b+c)z)^2}{4(b+c)}\right) + (i(b+c))^{-n-1} e^{\frac{i(-f^2+8b(e+g)+8c(e+g))}{4(b+c)}} \right.$$

$$\left. \sum_{j=0}^n 2^{j-n} (-if)^{n-j} (i(f+2(b+c)z))^{j+1} \left( -\frac{i(f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(f+2(b+c)z)^2}{4(b+c)}\right) \right) /; n \in \mathbb{N}$$

01.06.21.1117.01

$$\int z^n \sin(\sqrt{z} b + e) \sin(\sqrt{z} c + fz + g) dz =$$

$$-(-1)^n 2^{-2n-3} e^{-i(e+g)} f^{-2(n+1)} \left( -e^{\frac{i(b^2-2cb+c^2+8ef)}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c-2f\sqrt{z}))^{h+j} \right.$$

$$\left. \left( \frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \right) + \right.$$

$$\left. 2\sqrt{\frac{i(-b+c+2f\sqrt{z})^2}{f}} f i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-b+c+2f\sqrt{z})^2}{4f}\right) \right) +$$

$$e^{-\frac{i(b+c)^2}{4f}} \left( e^{\frac{i(b+c)^2}{2f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2f\sqrt{z}))^{h+j} \left( \frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \right.$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(b+c+2f\sqrt{z})^2}{4f} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(b+c+2f\sqrt{z})^2}{f}} f i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(b+c+2f\sqrt{z})^2}{4f} \right) \right) + \\
 & e^{2i(e+g)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2f\sqrt{z}))^{h+j} \left( -\frac{i(b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b+c)(b+c+2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b+c+2f\sqrt{z})^2}{4f} \right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(b+c+2f\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b+c+2f\sqrt{z})^2}{4f} \right) \right) \Bigg) - \\
 & e^{-\frac{i(b^2-2cb+c^2-8fg)}{4f}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c-2f\sqrt{z}))^{h+j} \left( -\frac{i(-b+c+2f\sqrt{z})^2}{f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b-c)(b-c-2f\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-b+c+2f\sqrt{z})^2}{4f} \right) - \right. \\
 & \left. 2if \sqrt{-\frac{i(-b+c+2f\sqrt{z})^2}{f}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-b+c+2f\sqrt{z})^2}{4f} \right) \right) \Bigg) /; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n \sin(bz^r + dz) \sin(cz^r + fz + g)$**

01.06.21.1118.01

$$\int z^n \sin(bz^2 + dz) \sin(cz^2 + fz + g) dz =$$

$$\frac{1}{8} e^{-ig} \left( -e^{-\frac{i(d^2-2fd+f^2+8(b-c)g)}{4(b-c)}} \left( \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (-i(d-f+2bz-2cz))^{j+1} \left( \frac{i(d-f+2bz-2cz)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left( \frac{j+1}{2}, \frac{i(d-f+2bz-2cz)^2}{4(b-c)} \right) \right) (-i(b-c))^{-n-1} - \right.$$

$$\left. (i(b-c))^{-n-1} e^{-\frac{i(d-f)^2}{4(b-c)}} \sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j} (i(d-f+2bz-2cz))^{j+1} \left( -\frac{i(d-f+2bz-2cz)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left( \frac{j+1}{2}, -\frac{i(d-f+2bz-2cz)^2}{4(b-c)} \right) + (-i(b+c))^{-n-1} e^{\frac{i(d+f)^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} \right.$$

$$\left. (-i(d+f+2(b+c)z))^{j+1} \left( \frac{i(d+f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left( \frac{j+1}{2}, \frac{i(d+f+2(b+c)z)^2}{4(b+c)} \right) + \right.$$

$$\left. (i(b+c))^{-n-1} e^{-\frac{i(d^2+2fd+f^2-8(b+c)g)}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j} (i(d+f+2(b+c)z))^{j+1} \right.$$

$$\left. \left( -\frac{i(d+f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left( \frac{j+1}{2}, -\frac{i(d+f+2(b+c)z)^2}{4(b+c)} \right) \right) /; n \in \mathbb{N}$$

01.06.21.1119.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin(\sqrt{z} c + fz + g) dz = -(-1)^n 2^{-2n-3} e^{-ig} \left( e^{\frac{i(b^2-2cb+c^2+8dg-8fg)}{4(d-f)}} \right.$$

$$\left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c+2(d-f)\sqrt{z}))^{h+j} \left( \frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( (c-b)(b-c+2(d-f)\sqrt{z}) \Gamma\left( \frac{1}{2}(h+j+1), \frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) - \right. \right.$$

$$\left. \left. 2i(d-f) \sqrt{\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f}} \Gamma\left( \frac{1}{2}(h+j+2), \frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) \right) \right) (d-f)^{-2(n+1)} +$$

$$\begin{aligned}
 & e^{-\frac{i(b-c)^2}{4(d-f)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c+2(d-f)\sqrt{z}))^{h+j} \left( -\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \quad \left( \begin{matrix} j \\ h \end{matrix} \right) \binom{n}{j} \left( (c-b)(b-c+2(d-f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) + \right. \\
 & \quad \left. \left. 2 \sqrt{-\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f}} (d-f) i \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)} \right) \right) \right) (d-f)^{-2(n+1)} - \\
 & e^{\frac{i(b+c)^2}{4(d+f)}} (d+f)^{-2(n+1)} \left( e^{\frac{i(b+c)^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2(d+f)\sqrt{z}))^{h+j} \right. \\
 & \quad \left( \frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad \left( (-b-c)(b+c+2(d+f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) - \right. \\
 & \quad \left. 2 i(d+f) \sqrt{\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) + \\
 & e^{2ig} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2(d+f)\sqrt{z}))^{h+j} \left( -\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \quad \left( \begin{matrix} j \\ h \end{matrix} \right) \binom{n}{j} \left( (-b-c)(b+c+2(d+f)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) + \right. \\
 & \quad \left. 2 \sqrt{-\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f}} (d+f) i \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)} \right) \right) \Bigg) /; n \in \mathbb{N}
 \end{aligned}$$

### Involving $z^n \sin(bz^r + dz + e) \sin(cz^r + fz + g)$

01.06.21.1120.01

$$\int z^n \sin(bz^2 + dz + e) \sin(cz^2 + fz + g) dz =$$

$$\frac{1}{8} e^{-i(e+g)} \left( (-i(b-c))^{-n-1} e^{\frac{i(d^2-2fd+f^2+8(b-c)g)}{4(b-c)}} \sum_{j=0}^n 2^{j-n} (i(d-f))^{n-j} (-i(d-f+2bz-2cz))^{j+1} \right.$$

$$\left( \frac{i(d-f+2bz-2cz)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d-f+2bz-2cz)^2}{4(b-c)}\right) -$$

$$(i(b-c))^{-n-1} e^{-\frac{i(d^2-2fd+f^2-8be+8ce)}{4(b-c)}} \sum_{j=0}^n 2^{j-n} (-i(d-f))^{n-j} (i(d-f+2bz-2cz))^{j+1}$$

$$\left( -\frac{i(d-f+2bz-2cz)^2}{b-c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d-f+2bz-2cz)^2}{4(b-c)}\right) +$$

$$(-i(b+c))^{-n-1} e^{\frac{i(d+f)^2}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (i(d+f))^{n-j} (-i(d+f+2(b+c)z))^{j+1} \left( \frac{i(d+f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+f+2(b+c)z)^2}{4(b+c)}\right) + (i(b+c))^{-n-1} e^{-\frac{i(d^2+2fd+f^2-8ce-8cg-8b(e+g))}{4(b+c)}} \sum_{j=0}^n 2^{j-n} (-i(d+f))^{n-j}$$

$$(i(d+f+2(b+c)z))^{j+1} \left( -\frac{i(d+f+2(b+c)z)^2}{b+c} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+f+2(b+c)z)^2}{4(b+c)}\right) \Bigg) /; n \in \mathbb{N}$$

01.06.21.1121.01

$$\int z^n \sin(\sqrt{z}bz + dz + e) \sin(\sqrt{z}cz + fz + g) dz = (-1)^n 2^{-2n-3} e^{-i(e+g)} \left( \frac{1}{(d-f)^{2n+2}} \left( e^{\frac{i(b^2-2cb+c^2+8dg-8fg)}{4(d-f)}} \right.$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b-c))^{-h-j+2n} (-i(b-c+2(d-f)\sqrt{z}))^{h+j} \left( \frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\left. \binom{j}{h} \binom{n}{j} \left( -(b-c)(b-c+2(d-f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)}\right) - \right.$$



$$\begin{aligned}
 & 2i(d-f) \sqrt{\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)}\right) \Bigg) + \\
 & \frac{1}{(d-f)^{2n+2}} \left( e^{-\frac{i(b^2-2cb+c^2-8de+8ef)}{4(d-f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b-c))^{-h-j+2n} (i(b-c+2(d-f)\sqrt{z}))^{h+j} \right. \\
 & \left. \left( -\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( 2i(d-f) \sqrt{-\frac{i(b-c+2(d-f)\sqrt{z})^2}{d-f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)}\right) - \right. \right. \\
 & \left. \left. (b-c)(b-c+2(d-f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(b-c+2(d-f)\sqrt{z})^2}{4(d-f)}\right) \right) \right) - \frac{1}{(d+f)^{2n+2}} \left( e^{-\frac{i(b+c)^2}{4(d+f)}} \right. \\
 & \left. \left( e^{\frac{i(b+c)^2}{2(d+f)}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i(b+c))^{-h-j+2n} (-i(b+c+2(d+f)\sqrt{z}))^{h+j} \left( \frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \right. \right. \\
 & \left. \left. \binom{j}{h} \binom{n}{j} \left( -(b+c)(b+c+2(d+f)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) - \right. \right. \right. \\
 & \left. \left. 2i(d+f) \sqrt{\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) \right) \right) + \\
 & e^{2i(e+g)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i(b+c))^{-h-j+2n} (i(b+c+2(d+f)\sqrt{z}))^{h+j} \left( -\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2i(d+f) \sqrt{-\frac{i(b+c+2(d+f)\sqrt{z})^2}{d+f}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(b+c+2(d+f)\sqrt{z})^2}{4(d+f)}\right) - \right. \right. \\
 & \left. \left. \dots \right) \right)
 \end{aligned}$$

Involving products of several direct functions and a power function

**Involving  $z^{\alpha-1} \sin(a z) \sin(b z) \sin(c z)$**

01.06.21.1122.01

$$\int z^{\alpha-1} \sin(a z) \sin(b z) \sin(c z) dz = \frac{1}{8} i z^{\alpha} \left( (-i(a-b-c)z)^{-\alpha} \Gamma(\alpha, -i(a-b-c)z) + (i(a-b-c)z)^{-\alpha} \Gamma(\alpha, i(a-b-c)z) + (-i(a+b-c)z)^{-\alpha} \Gamma(\alpha, -i(a+b-c)z) - (i(a+b-c)z)^{-\alpha} \Gamma(\alpha, i(a+b-c)z) + (-i(a-b+c)z)^{-\alpha} \Gamma(\alpha, -i(a-b+c)z) - (i(a-b+c)z)^{-\alpha} \Gamma(\alpha, i(a-b+c)z) - (-i(a+b+c)z)^{-\alpha} \Gamma(\alpha, -i(a+b+c)z) + (i(a+b+c)z)^{-\alpha} \Gamma(\alpha, i(a+b+c)z) \right)$$

01.06.21.1123.01

$$\int \frac{\sin(a z) \sin(b z) \sin(c z)}{z} dz = \frac{1}{4} (-\text{Si}((a-b-c)z) + \text{Si}((a+b-c)z) + \text{Si}((a-b+c)z) - \text{Si}((a+b+c)z))$$

**Involving  $z^{\alpha-1} \prod_{k=1}^n \sin(a_k z)$**

01.06.21.1124.01

$$\int z^{\alpha-1} \prod_{k=1}^n \sin(a_k z) dz = (-2)^{-n-1} z^{\alpha} \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \left( \left( e^{\frac{1}{2} \pi i \sum_{j=1}^n k_j} \Gamma\left(\alpha, -i z \sum_{j=1}^n k_j a_j\right) \left(-i a \sum_{j=1}^n k_j a_j\right)^{-\alpha} + e^{-\frac{1}{2} \pi i \sum_{j=1}^n k_j} \Gamma\left(\alpha, i z \sum_{j=1}^n k_j a_j\right) \left(i z \sum_{j=1}^n k_j a_j\right)^{-\alpha} \right) \right)$$

01.06.21.1125.01

$$\int \frac{1}{z} \prod_{k=1}^n \sin(a_k z) dz = (-2)^{-n} \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \left( \cos\left(\frac{1}{2} \pi \sum_{j=1}^n k_j\right) \text{Ci}\left(z \sum_{j=1}^n k_j a_j\right) - \sin\left(\frac{1}{2} \pi \sum_{j=1}^n k_j\right) \text{Si}\left(z \sum_{j=1}^n k_j a_j\right) \right)$$

**Involving products of powers of the direct function and a power function**

Involving product of power of the direct function, the direct function and a power function

**Involving  $z^{\alpha-1} \sin(c z) \sin^{\nu}(a z)$**

01.06.21.1126.01

$$\int z^{\alpha-1} \sin(cz) \sin^v(az) dz = 2^{-v-1} z^\alpha \left( i \binom{v}{\frac{v}{2}} ((-icz)^{-\alpha} \Gamma(\alpha, -icz) - (icz)^{-\alpha} \Gamma(\alpha, icz)) (1 - v \bmod 2) - \right. \\ \left. i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \Gamma(\alpha, -i(c-2as+av)z) (-i(c-2as+av)z)^{-\alpha} - \right. \right. \\ \left. \left. e^{i\pi v} (i(c-2as+av)z)^{-\alpha} \Gamma(\alpha, i(c-2as+av)z) + e^{i\pi v} (-i(c+2as-av)z)^{-\alpha} \right. \right. \\ \left. \left. \Gamma(\alpha, -i(c+2as-av)z) - (i(c+2as-av)z)^{-\alpha} \Gamma(\alpha, i(c+2as-av)z) \right) \right); v \in \mathbb{N}^+$$

01.06.21.1127.01

$$\int z^n \sin(cz) \sin^v(az) dz = -\frac{in!}{2} \sin^v(az) (1 - e^{2iaz})^{-v} \\ \left( e^{icz} \sum_{p=0}^n \frac{(-1)^p z^{n-p}}{(n-p)! (ic-ia v)^{p+1}} {}_{p+2}F_{p+1} \left( \frac{c-av}{2a}, \dots, \frac{c-av}{2a}, -v; \frac{c-av}{2a} + 1, \dots, \frac{c-av}{2a} + 1; e^{2iaz} \right) - \right. \\ \left. e^{-icz} \sum_{p=0}^n \frac{(-1)^p z^{n-p}}{(n-p)! (-ic-ia v)^{p+1}} {}_{p+2}F_{p+1} \left( -\frac{c+av}{2a}, \dots, -\frac{c+av}{2a}, -v; 1 - \frac{c+av}{2a}, \dots, 1 - \frac{c+av}{2a}; e^{2iaz} \right) \right); n \in \mathbb{N}$$

### Involving $z^{\alpha-1} \sin(cz + d) \sin^v(az)$

01.06.21.1128.01

$$\int z^{\alpha-1} \sin(d + cz) \sin^v(az) dz = \\ 2^{-v-1} z^\alpha \left( i e^{id} \binom{v}{\frac{v}{2}} ((-icz)^{-\alpha} \Gamma(\alpha, -icz) - e^{-2id} (icz)^{-\alpha} \Gamma(\alpha, icz)) (1 - v \bmod 2) - i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{id} \binom{v}{s} \right. \\ \left( \Gamma(\alpha, -i(c-2as+av)z) (-i(c-2as+av)z)^{-\alpha} - e^{i(\pi v - 2d)} (i(c-2as+av)z)^{-\alpha} \Gamma(\alpha, i(c-2as+av)z) + \right. \\ \left. e^{i\pi v} (-i(c+2as-av)z)^{-\alpha} \Gamma(\alpha, -i(c+2as-av)z) - \right. \\ \left. e^{-2id} (i(c+2as-av)z)^{-\alpha} \Gamma(\alpha, i(c+2as-av)z) \right) \right); v \in \mathbb{N}^+$$

01.06.21.1129.01

$$\int z^n \sin(cz + d) \sin^v(az) dz = \frac{1}{2} i (1 - e^{2iaz})^{-v} n! \sin^v(az) \\ \left( e^{-i(d+cz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ic-ia v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c+av}{2a}, \dots, -\frac{c+av}{2a}, -v; 1 - \frac{c+av}{2a}, \dots, 1 - \frac{c+av}{2a}; e^{2iaz} \right) - \right. \\ \left. e^{i(d+cz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ic-ia v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( \frac{c-av}{2a}, \dots, \frac{c-av}{2a}, -v; \frac{c-av}{2a} + 1, \dots, \frac{c-av}{2a} + 1; e^{2iaz} \right) \right); n \in \mathbb{N}$$

### Involving $z^{\alpha-1} \sin(cz) \sin^v(az+b)$

01.06.21.1130.01

$$\int z^{\alpha-1} \sin(cz) \sin^v(b+az) dz = 2^{-v-1} z^\alpha \left( i \binom{v}{\frac{v}{2}} ((-ic z)^{-\alpha} \Gamma(\alpha, -ic z) - (ic z)^{-\alpha} \Gamma(\alpha, ic z)) (1-v \bmod 2) - \right. \\ \left. i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-ib(2s+v)} \binom{v}{s} \left( e^{2ibv} \Gamma(\alpha, -i(c-2as+av)z) (-i(c-2as+av)z)^{-\alpha} - \right. \right. \\ \left. \left. e^{i(4bs+\pi v)} (i(c-2as+av)z)^{-\alpha} \Gamma(\alpha, i(c-2as+av)z) + e^{i(4bs+\pi v)} (-i(c+2as-av)z)^{-\alpha} \right. \right. \\ \left. \left. \Gamma(\alpha, -i(c+2as-av)z) - e^{2ibv} (i(c+2as-av)z)^{-\alpha} \Gamma(\alpha, i(c+2as-av)z) \right) \right); v \in \mathbb{N}^+$$

01.06.21.1131.01

$$\int z^n \sin(cz) \sin^v(az+b) dz = \frac{1}{2} i (1 - e^{2i(b+az)})^{-v} n! \sin^v(az+b) \\ \left( e^{-ic z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ic - iav)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c+av}{2a}, \dots, -\frac{c+av}{2a}, -v; 1 - \frac{c+av}{2a}, \dots, 1 - \frac{c+av}{2a}; e^{2i(b+az)} \right) - \right. \\ \left. e^{ic z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ic - iav)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( \frac{c-av}{2a}, \dots, \frac{c-av}{2a}, -v; \frac{c-av}{2a} + 1, \dots, \frac{c-av}{2a} + 1; e^{2i(b+az)} \right) \right); n \in \mathbb{N}$$

### Involving $z^{\alpha-1} \sin(cz+d) \sin^v(az+b)$

01.06.21.1132.01

$$\int z^{\alpha-1} \sin(d+cz) \sin^v(b+az) dz = \\ 2^{-v-1} z^\alpha \left( i e^{id} \binom{v}{\frac{v}{2}} ((-ic z)^{-\alpha} \Gamma(\alpha, -ic z) - e^{-2id} (ic z)^{-\alpha} \Gamma(\alpha, ic z)) (1-v \bmod 2) - i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{i(d-b(2s+v))} \right. \\ \left. \binom{v}{s} \left( e^{2ibv} \Gamma(\alpha, -i(c-2as+av)z) (-i(c-2as+av)z)^{-\alpha} - e^{i(-2d+4bs+\pi v)} (i(c-2as+av)z)^{-\alpha} \right. \right. \\ \left. \left. \Gamma(\alpha, i(c-2as+av)z) + e^{i(4bs+\pi v)} (-i(c+2as-av)z)^{-\alpha} \Gamma(\alpha, -i(c+2as-av)z) - \right. \right. \\ \left. \left. e^{2i(bv-d)} (i(c+2as-av)z)^{-\alpha} \Gamma(\alpha, i(c+2as-av)z) \right) \right); v \in \mathbb{N}^+$$

01.06.21.1133.01

$$\int z^n \sin(cz+d) \sin^v(az+b) dz = \frac{1}{2} i (1 - e^{2i(b+az)})^{-v} n! \sin^v(az+b) \left( e^{-i(d+cz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ic - ia v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c+av}{2a}, \dots, -\frac{c+av}{2a}, -v; 1 - \frac{c+av}{2a}, \dots, 1 - \frac{c+av}{2a}; e^{2i(b+az)} \right) - e^{i(d+cz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ic - ia v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( \frac{c-av}{2a}, \dots, \frac{c-av}{2a}, -v; \frac{c-av}{2a} + 1, \dots, \frac{c-av}{2a} + 1; e^{2i(b+az)} \right) \right) /; n \in \mathbb{N}$$

### Involving $z^n \sin(bz^r) \sin^v(cz)$

01.06.21.1134.01

$$\int z^n \sin(bz^2) \sin^v(cz) dz = 2^{-v-2} \left( i \left( \frac{v}{2} \right) \left( (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma \left( \frac{n+1}{2}, -ibz^2 \right) - (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma \left( \frac{n+1}{2}, ibz^2 \right) \right) (1 - v \bmod 2) z^{n+1} + \frac{1}{b^{2n+1}} \left( i^{-v} \sum_{j=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^j e^{-\frac{ic^2(v-2j)^2}{4b}} \binom{v}{j} \left( \sum_{h=0}^n 2^{h-n} (-ic(v-2j))^{n-h} (i(-2cj+cv+2bz)^2)^{h+1} \left( -\frac{i(-2cj+cv+2bz)^2}{b} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \Gamma \left( \frac{h+1}{2}, -\frac{i(-2cj+cv+2bz)^2}{4b} \right) (-ib)^n + (-1)^v \left( \sum_{h=0}^n 2^{h-n} (ic(v-2j))^{n-h} (i(2cj-cv+2bz)^2)^{h+1} \left( -\frac{i(2cj-cv+2bz)^2}{b} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \Gamma \left( \frac{h+1}{2}, -\frac{i(2cj-cv+2bz)^2}{4b} \right) \right) (-ib)^n + (-1)^v (ib)^n e^{\frac{ic^2(v-2j)^2}{2b}} \sum_{h=0}^n 2^{h-n} (ic(v-2j))^{n-h} (-i(-2cj+cv+2bz))^{h+1} \left( \frac{i(-2cj+cv+2bz)^2}{b} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \Gamma \left( \frac{h+1}{2}, \frac{i(-2cj+cv+2bz)^2}{4b} \right) + (ib)^n e^{-\frac{ic^2(v-2j)^2}{2b}} \sum_{h=0}^n 2^{h-n} (-ic(v-2j))^{n-h} (i(-2cj+cv-2bz))^{h+1} \left( \frac{i(2cj-cv+2bz)^2}{b} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \Gamma \left( \frac{h+1}{2}, \frac{i(2cj-cv+2bz)^2}{4b} \right) \right) \right) /; v \in \mathbb{N}^+ \wedge n \in \mathbb{N}$$

01.06.21.1135.01

$$\begin{aligned}
 & \int z^n \sin(b \sqrt{z}) \sin^v(c z) dz = \\
 & i 2^{-v} z^{n+1} \left(\frac{v}{2}\right) \left( (-i b \sqrt{z})^{-2(n+1)} \Gamma(2(n+1), -i b \sqrt{z}) - (i b \sqrt{z})^{-2(n+1)} \Gamma(2(n+1), i b \sqrt{z}) \right) (1 - v \bmod 2) + \\
 & 2^{-2n-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{-\frac{i b^2}{4c(2k-v)}} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} (-i b + 2 i c (2k-v) \sqrt{z})^{h+j} \left( \frac{i (-i b + 2 i c (2k-v) \sqrt{z})^2}{c(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right. \\
 & \left. \left. \left( 2 i c (2k-v) \sqrt{\frac{i (-i b + 2 i c (2k-v) \sqrt{z})^2}{c(2k-v)}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i (-i b + 2 i c (2k-v) \sqrt{z})^2}{4 c (2k-v)} \right) - i b \right. \right. \right. \\
 & \left. \left. \left. (-i b + 2 i c (2k-v) \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), \frac{i (-i b + 2 i c (2k-v) \sqrt{z})^2}{4 c (2k-v)} \right) \right) \right) \right) (i c (2k-v))^{-2n-2} + \\
 & (-1)^v e^{-\frac{i b^2}{4c(2k-v)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} (i b + 2 i c (2k-v) \sqrt{z})^{h+j} \left( \frac{i (i b + 2 i c (2k-v) \sqrt{z})^2}{c(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( b i (i b + 2 i c (2k-v) \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), \frac{i (i b + 2 i c (2k-v) \sqrt{z})^2}{4 c (2k-v)} \right) + 2 c i \right. \right. \\
 & \left. \left. (2k-v) \sqrt{\frac{i (i b + 2 i c (2k-v) \sqrt{z})^2}{c(2k-v)}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i (i b + 2 i c (2k-v) \sqrt{z})^2}{4 c (2k-v)} \right) \right) \right) \\
 & (i c (2k-v))^{-2n-2} - e^{-\frac{i b^2}{4c(v-2k)}} (i c (v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} \\
 & (-i b + 2 i c (v-2k) \sqrt{z})^{h+j} \left( \frac{i (-i b + 2 i c (v-2k) \sqrt{z})^2}{c(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 i c (v-2 k) \sqrt{\frac{i(-i b+2 i c(v-2 k) \sqrt{z})^2}{c(v-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-i b+2 i c(v-2 k) \sqrt{z})^2}{4 c(v-2 k)}\right) - \right. \\
 & \left. i b(-i b+2 i c(v-2 k) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-i b+2 i c(v-2 k) \sqrt{z})^2}{4 c(v-2 k)}\right) \right) + \\
 & e^{-\frac{i b^2}{4 c(v-2 k)}} (i c(v-2 k))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2 n} (i b+2 i c(v-2 k) \sqrt{z})^{h+j} \\
 & \left( \frac{i(i b+2 i c(v-2 k) \sqrt{z})^2}{c(v-2 k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( b i(i b+2 i c(v-2 k) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(i b+2 i c(v-2 k) \sqrt{z})^2}{4 c(v-2 k)}\right) + 2 c i(v-2 k) \right. \\
 & \left. \sqrt{\frac{i(i b+2 i c(v-2 k) \sqrt{z})^2}{c(v-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(i b+2 i c(v-2 k) \sqrt{z})^2}{4 c(v-2 k)}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin(b z^r + e) \sin^v(c z)$**

01.06.21.1136.01

$$\int z^n \sin(bz^2 + e) \sin^v(cz) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( e^{ie} (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - e^{-ie} (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i \left( -\frac{c^2(v-2s)^2}{b} + 4e - 2\pi(v+1) \right)} \left( \sum_{j=0}^n 2^{j-n} (ic(v-2s))^{n-j} (-ic(v-2s) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-ic(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-ic(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} + \right.$$

$$e^{-\frac{1}{4}i \left( -\frac{c^2(v-2s)^2}{b} + 4e - 2\pi(1-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-ic(v-2s))^{n-j} (ic(v-2s) - 2ibz)^{j+1} \right.$$

$$\left. \left. \left( -\frac{i(ic(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(ic(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} + \right.$$

$$(ib)^{-n-1} e^{\frac{1}{4}i \left( -\frac{c^2(v-2s)^2}{b} + 4e + 2\pi(v-1) \right)} \sum_{j=0}^n 2^{j-n} (ic(v-2s))^{n-j} (2ibz - ic(v-2s))^{j+1}$$

$$\left( \frac{i(2ibz - ic(v-2s))^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ibz - ic(v-2s))^2}{4b}\right) +$$

$$(ib)^{-n-1} e^{\frac{1}{4}i \left( -\frac{c^2(v-2s)^2}{b} + 4e - 2\pi(v+1) \right)} \sum_{j=0}^n 2^{j-n} (-ic(v-2s))^{n-j} (ci(v-2s) + 2ibz)^{j+1}$$

$$\left( \frac{i(ci(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(ci(v-2s) + 2ibz)^2}{4b}\right) \Big/; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1137.01

$$\int z^n \sin(\sqrt{z} b + e) \sin^v(cz) dz = (-1)^n 2^{-v} i \left(\frac{v}{2}\right) \left( e^{-ie} \Gamma(2(n+1), ib\sqrt{z}) - e^{ie} \Gamma(2(n+1), -ib\sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} +$$

$$2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{ib^2}{4c(v-2s)} - ie + \frac{1}{2}i\pi(v+1)} \right.$$

$$\left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2ic(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right) \right)$$



$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( -i b (-i b - 2 i c (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (-i b - 2 i c (v - 2 s) \sqrt{z})^2}{4 c (v - 2 s)} \right) - 2 i c \right. \\
 & \left. (v - 2 s) \sqrt{-\frac{i (-i b - 2 i c (v - 2 s) \sqrt{z})^2}{c (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (-i b - 2 i c (v - 2 s) \sqrt{z})^2}{4 c (v - 2 s)} \right) \right) \\
 & (-i c (v - 2 s))^{-2(n+1)} + e^{\frac{i b^2}{4 c (v - 2 s)} + i e + \frac{1}{2} i \pi (v - 1)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} (i b - 2 i c (v - 2 s) \sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i (i b - 2 i c (v - 2 s) \sqrt{z})^2}{c (v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( i b (i b - 2 i c (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (i b - 2 i c (v - 2 s) \sqrt{z})^2}{4 c (v - 2 s)} \right) - 2 i c (v - 2 s) \right. \right. \\
 & \left. \left. \sqrt{-\frac{i (i b - 2 i c (v - 2 s) \sqrt{z})^2}{c (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (i b - 2 i c (v - 2 s) \sqrt{z})^2}{4 c (v - 2 s)} \right) \right) \right) \\
 & (-i c (v - 2 s))^{-2(n+1)} + e^{-\frac{i b^2}{4 c (v - 2 s)} - i e + \frac{1}{2} i \pi (1 - v)} (i c (v - 2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} \\
 & (-i b + 2 i c (v - 2 s) \sqrt{z})^{h+j} \left( \frac{i (-i b + 2 i c (v - 2 s) \sqrt{z})^2}{c (v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( 2 i c (v - 2 s) \sqrt{\frac{i (-i b + 2 i c (v - 2 s) \sqrt{z})^2}{c (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), \frac{i (-i b + 2 i c (v - 2 s) \sqrt{z})^2}{4 c (v - 2 s)} \right) - \right. \\
 & \left. i b (-i b + 2 i c (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), \frac{i (-i b + 2 i c (v - 2 s) \sqrt{z})^2}{4 c (v - 2 s)} \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & e^{-\frac{ib^2}{4c(v-2s)} + ie^{-\frac{1}{2}i\pi(v+1)}} (ic(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2ic(v-2s)\sqrt{z})^{h+j} \\
 & \left( \frac{i(ib+2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( bi(ib+2ic(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) + 2ci(v-2s) \right. \\
 & \left. \sqrt{\frac{i(ib+2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin(bz^r + dz) \sin^v(cvz)$

01.06.21.1138.01

$$\int z^n \sin(bz^2 + dz) \sin^v(cz) dz = i 2^{-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{-\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left( \frac{i(id + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left( -\frac{i(-id - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( -e^{-\frac{i(-id+ic(v-2s))^2}{4b}} \left( \sum_{j=0}^n 2^{j-n} (id - ic(v-2s))^{n-j} (-id + ic(v-2s) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-id + ic(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id + ic(v-2s) - 2ibz)^2}{4b}\right) \right) \right) (-ib)^{-n-1} +$$

$$(-1)^{v+1} e^{-\frac{i(-id-ic(v-2s))^2}{4b}} \left( \sum_{j=0}^n 2^{j-n} (id + ic(v-2s))^{n-j} (-id - ic(v-2s) - 2ibz)^{j+1} \right.$$

$$\left. \left. \left( -\frac{i(-id - ic(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - ic(v-2s) - 2ibz)^2}{4b}\right) \right) \right) (-ib)^{-n-1} +$$

$$(ib)^{-n-1} e^{\frac{i(id+ic(v-2s))^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id - ic(v-2s))^{n-j} (id + ic(v-2s) + 2ibz)^{j+1}$$

$$\left( \frac{i(id + ic(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + ic(v-2s) + 2ibz)^2}{4b}\right) +$$

$$(-1)^v (ib)^{-n-1} e^{\frac{i(id-ic(v-2s))^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id + ic(v-2s))^{n-j} (id - ic(v-2s) + 2ibz)^{j+1}$$

$$\left( \frac{i(id - ic(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id - ic(v-2s) + 2ibz)^2}{4b}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1139.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin^v(cz) dz =$$

$$2^{-2n-v-2} i \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( e^{\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \right)$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( -ib(-ib-2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) - \right. \\
 & \left. 2id \sqrt{-\frac{i(-ib-2id\sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) \right) - \\
 & e^{-\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2id\sqrt{z})^{h+j} \left( \frac{i(ib+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( bi(ib+2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) \right) \Bigg) (id)^{-2n-2} + \\
 & 2^{-2n-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{\frac{b^2}{4(-id+ic(2k-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} \right. \right. \\
 & \left. \left. (-ib+2(-id+ic(2k-v))\sqrt{z})^{h+j} \left( -\frac{(-ib+2(-id+ic(2k-v))\sqrt{z})^2}{-id+ic(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right) \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2(-id+ic(2k-v)) \sqrt{-\frac{(-ib+2(-id+ic(2k-v))\sqrt{z})^2}{-id+ic(2k-v)}} \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+ic(2k-v))\sqrt{z})^2}{4(-id+ic(2k-v))} \right) - ib(-ib+2(-id+ic(2k-v))\sqrt{z}) \right) \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+ic(2k-v))\sqrt{z})^2}{4(-id+ic(2k-v))} \right) \right) \right) \Bigg) (-id+ic(2k-v))^{-2n-2} +
 \end{aligned}$$

$$\begin{aligned}
 & (-1)^v e^{\frac{b^2}{4(id+ic(2k-v))}} (id+ic(2k-v))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+ic(2k-v))\sqrt{z})^{h+j} \\
 & \left( -\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{id+ic(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2(id+ic(2k-v))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), -\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{4(id+ic(2k-v))} \right) + 2\sqrt{-\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{id+ic(2k-v)}} \right. \\
 & \left. \left. (id+ic(2k-v)) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{4(id+ic(2k-v))} \right) \right) \right) - \\
 & e^{\frac{b^2}{4(-id+ic(v-2k))}} (-id+ic(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2(-id+ic(v-2k))\sqrt{z})^{h+j} \\
 & \left( -\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{-id+ic(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2(-id+ic(v-2k)) \right. \\
 & \left. \sqrt{-\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{-id+ic(v-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{4(-id+ic(v-2k))} \right) \right) - \\
 & \left. \left. ib(-ib+2(-id+ic(v-2k))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{4(-id+ic(v-2k))} \right) \right) \right) + \\
 & e^{\frac{b^2}{4(id+ic(v-2k))}} (id+ic(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+ic(v-2k))\sqrt{z})^{h+j} \\
 & \left( -\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{id+ic(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2(id+ic(v-2k))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), -\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{4(id+ic(v-2k))} \right) + 2\sqrt{-\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{id+ic(v-2k)}} \right. \\
 & \left. \left. \left( 1 \quad (ib+2(id+ic(v-2k))\sqrt{z})^2 \right) \right) \right) \right)
 \end{aligned}$$

### Involving $z^n \sin(bz^r + dz + e) \sin^v(cvz)$

01.06.21.1140.01

$$\int z^n \sin(bz^2 + dz + e) \sin^v(cz) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{ie - \frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{id + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) -$$

$$2^{-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( -e^{-\frac{i(-id+ic(v-2s))^2}{4b} - ie} \left( \sum_{j=0}^n 2^{j-n} (id - ic(v-2s))^{n-j} (-id + ic(v-2s) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-id + ic(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id + ic(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} + \right.$$

$$\left. (-1)^{v+1} e^{-\frac{i(-id-ic(v-2s))^2}{4b} - ie} \left( \sum_{j=0}^n 2^{j-n} (id + ic(v-2s))^{n-j} (-id - ic(v-2s) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-id - ic(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - ic(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} + \right.$$

$$\left. (ib)^{-n-1} e^{\frac{i(id+ic(v-2s))^2}{4b} + ie} \sum_{j=0}^n 2^{j-n} (-id - ic(v-2s))^{n-j} (id + ic(v-2s) + 2ibz)^{j+1} \right.$$

$$\left. \left( \frac{i(id + ic(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + ic(v-2s) + 2ibz)^2}{4b}\right) + \right.$$

$$\left. (-1)^v (ib)^{-n-1} e^{\frac{i(id-ic(v-2s))^2}{4b} + ie} \sum_{j=0}^n 2^{j-n} (-id + ic(v-2s))^{n-j} (id - ic(v-2s) + 2ibz)^{j+1} \right.$$

$$\left. \left( \frac{i(id - ic(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id - ic(v-2s) + 2ibz)^2}{4b}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1141.01

$$\int z^n \sin(\sqrt{z} b + dz + e) \sin^v(cz) dz =$$

$$2^{-2n-v-2} i^{\left(\frac{v}{2}\right)} (1 - v \bmod 2) \left( e^{\frac{ib^2}{4d} - ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \right)$$

$$\binom{j}{h} \binom{n}{j} \left( -ib(-ib - 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib - 2id\sqrt{z})^2}{4d}\right) - \right.$$

$$\left. 2id \sqrt{-\frac{i(-ib - 2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib - 2id\sqrt{z})^2}{4d}\right) \right) -$$

$$e^{ie - \frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib + 2id\sqrt{z})^{h+j} \left( \frac{i(ib + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h}$$

$$\binom{n}{j} \left( bi(ib + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib + 2id\sqrt{z})^2}{4d}\right) + \right.$$

$$\left. 2 \sqrt{\frac{i(ib + 2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib + 2id\sqrt{z})^2}{4d}\right) \right) (id)^{-2n-2} +$$

$$2^{-2n-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{\frac{b^2}{4(-id+ic(2k-v))} - ie} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} \right. \right.$$

$$\left. (-ib + 2(-id + ic(2k-v))\sqrt{z})^{h+j} \left( -\frac{(-ib + 2(-id + ic(2k-v))\sqrt{z})^2}{-id + ic(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right)$$

$$\binom{j}{h} \binom{n}{j} \left( 2(-id + ic(2k-v)) \sqrt{-\frac{(-ib + 2(-id + ic(2k-v))\sqrt{z})^2}{-id + ic(2k-v)}} \right)$$

$$\begin{aligned}
 & \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+ic(2k-v))\sqrt{z})^2}{4(-id+ic(2k-v))}\right) - ib(-ib+2(-id+ic(2k-v))\sqrt{z}) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+ic(2k-v))\sqrt{z})^2}{4(-id+ic(2k-v))}\right) \Bigg) (-id+ic(2k-v))^{-2n-2} + \\
 & (-1)^v e^{\frac{b^2}{4(id+ic(2k-v))}+ie} (id+ic(2k-v))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+ic(2k-v))\sqrt{z})^{h+j} \\
 & \left(-\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{id+ic(2k-v)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left[ bi(ib+2(id+ic(2k-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{4(id+ic(2k-v))}\right) + 2\sqrt{-\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{id+ic(2k-v)}} \right. \\
 & \left. (id+ic(2k-v)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ib+2(id+ic(2k-v))\sqrt{z})^2}{4(id+ic(2k-v))}\right) \right] - \\
 & e^{\frac{b^2}{4(-id+ic(v-2k))}-ie} (-id+ic(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2(-id+ic(v-2k))\sqrt{z})^{h+j} \\
 & \left(-\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{-id+ic(v-2k)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left[ 2(-id+ic(v-2k)) \sqrt{-\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{-id+ic(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{4(-id+ic(v-2k))}\right) - \right. \\
 & \left. ib(-ib+2(-id+ic(v-2k))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+ic(v-2k))\sqrt{z})^2}{4(-id+ic(v-2k))}\right) \right] + \\
 & e^{\frac{b^2}{4(id+ic(v-2k))}+ie} (id+ic(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+ic(v-2k))\sqrt{z})^{h+j}
 \end{aligned}$$



$$\left( -\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{id+ic(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2(id+ic(v-2k))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{4(id+ic(v-2k))} \right) + 2\sqrt{-\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{id+ic(v-2k)}} \right) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+2(id+ic(v-2k))\sqrt{z})^2}{4(id+ic(v-2k))} \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n \sin(bz^r) \sin^v(fz+g)$**

01.06.21.1142.01

$$\int z^n \sin(bz^2) \sin^v(fz + g) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{b} + 4g(v-2s) - 2\pi(v+1)\right)} \left( \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (-if(v-2s) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-if(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-if(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} + \right.$$

$$e^{-\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{b} - 4g(v-2s) - 2\pi(1-v)\right)} \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (if(v-2s) - 2ibz)^{j+1} \right.$$

$$\left. \left. \left( -\frac{i(if(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(if(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} + \right.$$

$$(ib)^{-n-1} e^{\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{b} - 4g(v-2s) + 2\pi(v-1)\right)} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (2ibz - if(v-2s))^{j+1}$$

$$\left( \frac{i(2ibz - if(v-2s))^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ibz - if(v-2s))^2}{4b}\right) +$$

$$(ib)^{-n-1} e^{\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{b} + 4g(v-2s) - 2\pi(v+1)\right)} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s) + 2ibz)^{j+1}$$

$$\left( \frac{i(fi(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2s) + 2ibz)^2}{4b}\right) \Big/; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1143.01

$$\int z^n \sin(b\sqrt{z}) \sin^v(g + fz) dz = (-1)^n 2^{-v} i \left(\frac{v}{2}\right) \left( \Gamma(2(n+1), ib\sqrt{z}) - \Gamma(2(n+1), -ib\sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} +$$

$$2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{ib^2}{4f(v-2s)} + \frac{1}{2}i\pi(v+1) - ig(v-2s)} \right.$$

$$\left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2if(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right) \right)$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( -i b (-i b - 2 i f (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (-i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) - 2 i f \right. \\
 & \left. (v - 2 s) \sqrt{-\frac{i (-i b - 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (-i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) \right) \\
 & (-i f (v - 2 s))^{-2(n+1)} + e^{\frac{i b^2}{4 f (v - 2 s)} + \frac{1}{2} i \pi (v - 1) - i g (v - 2 s)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} \right. \\
 & \left. (i b - 2 i f (v - 2 s) \sqrt{z})^{h+j} \left( -\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( i b (i b - 2 i f (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) - 2 i f (v - 2 s) \right. \right. \\
 & \left. \left. \sqrt{-\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) \right) \right) \\
 & (-i f (v - 2 s))^{-2(n+1)} + e^{-\frac{i b^2}{4 f (v - 2 s)} + \frac{1}{2} i \pi (1 - v) + g i (v - 2 s)} (i f (v - 2 s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} (-i b + 2 i f (v - 2 s) \sqrt{z})^{h+j} \left( \frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( 2 i f (v - 2 s) \sqrt{\frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), \frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) - \right. \\
 & \left. i b (-i b + 2 i f (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), \frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) \right) + \\
 & e^{-\frac{i b^2}{4 f (v - 2 s)} - \frac{1}{2} i \pi (v + 1) + g i (v - 2 s)} (i f (v - 2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} (i b + 2 i f (v - 2 s) \sqrt{z})^{h+j}
 \end{aligned}$$

$$\left( \frac{i(i b + 2 i f(v - 2 s) \sqrt{z})^2}{f(v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( b i(i b + 2 i f(v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2}(h + j + 1), \frac{i(i b + 2 i f(v - 2 s) \sqrt{z})^2}{4 f(v - 2 s)} \right) + 2 f i(v - 2 s) \right.$$

$$\left. \sqrt{\frac{i(i b + 2 i f(v - 2 s) \sqrt{z})^2}{f(v - 2 s)}} \Gamma \left( \frac{1}{2}(h + j + 2), \frac{i(i b + 2 i f(v - 2 s) \sqrt{z})^2}{4 f(v - 2 s)} \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n \sin(b z^r + e) \sin^v(f z + g)$**

01.06.21.1144.01

$$\int z^n \sin(bz^2 + e) \sin^v(g + fz) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( e^{ie} (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - e^{-ie} (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b} + 4g(v-2s) + 4e - 2\pi(v+1) \right)} \left( \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (-if(v-2s) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left( -\frac{i(-if(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-if(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} +$$

$$e^{-\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b} - 4g(v-2s) + 4e - 2\pi(1-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (if(v-2s) - 2ibz)^{j+1} \right.$$

$$\left. \left( -\frac{i(if(v-2s) - 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(if(v-2s) - 2ibz)^2}{4b}\right) \right) (-ib)^{-n-1} +$$

$$(ib)^{-n-1} e^{\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b} - 4g(v-2s) + 4e + 2\pi(v-1) \right)} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (2ibz - if(v-2s))^{j+1}$$

$$\left( \frac{i(2ibz - if(v-2s))^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ibz - if(v-2s))^2}{4b}\right) +$$

$$(ib)^{-n-1} e^{\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b} + 4g(v-2s) + 4e - 2\pi(v+1) \right)} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s) + 2ibz)^{j+1}$$

$$\left( \frac{i(fi(v-2s) + 2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2s) + 2ibz)^2}{4b}\right) \Big/; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1145.01

$$\int z^n \sin(\sqrt{z} b + e) \sin^v(fz + g) dz =$$

$$(-1)^n 2^{-v} i \left(\frac{v}{2}\right) \left( e^{-ie} \Gamma(2(n+1), ib\sqrt{z}) - e^{ie} \Gamma(2(n+1), -ib\sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} +$$

$$2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{ib^2}{4f(v-2s)} - ie + \frac{1}{2}i\pi(v+1) - ig(v-2s)} \right.$$

$$\left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2if(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right) \right)$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( -i b (-i b - 2 i f (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (-i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) - 2 i f \right. \\
 & \quad \left. (v - 2 s) \sqrt{-\frac{i (-i b - 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (-i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) \right) \\
 & (-i f (v - 2 s))^{-2(n+1)} + e^{\frac{i b^2}{4 f (v - 2 s)} + i e + \frac{1}{2} i \pi (v - 1) - i g (v - 2 s)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} \right. \\
 & \quad \left. (i b - 2 i f (v - 2 s) \sqrt{z})^{h+j} \left( -\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \quad \left( i b (i b - 2 i f (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) - 2 i f (v - 2 s) \right. \\
 & \quad \left. \left. \sqrt{-\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (i b - 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) \right) \right) \\
 & (-i f (v - 2 s))^{-2(n+1)} + e^{-\frac{i b^2}{4 f (v - 2 s)} - i e + \frac{1}{2} i \pi (1 - v) + g i (v - 2 s)} (i f (v - 2 s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} (-i b + 2 i f (v - 2 s) \sqrt{z})^{h+j} \left( \frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( 2 i f (v - 2 s) \sqrt{\frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{f (v - 2 s)}} \Gamma \left( \frac{1}{2} (h + j + 2), \frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) - \right. \\
 & \quad \left. i b (-i b + 2 i f (v - 2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), \frac{i (-i b + 2 i f (v - 2 s) \sqrt{z})^2}{4 f (v - 2 s)} \right) \right) + \\
 & e^{-\frac{i b^2}{4 f (v - 2 s)} + i e - \frac{1}{2} i \pi (v + 1) + g i (v - 2 s)} (i f (v - 2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n}
 \end{aligned}$$

$$\begin{aligned}
 & (ib + 2if(v-2s)\sqrt{z})^{h+j} \left( \frac{i(ib + 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( bi(ib + 2if(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib + 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) + 2fi(v-2s) \right. \\
 & \left. \sqrt{\frac{i(ib + 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib + 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin(bz^r + dz) \sin^v(fz + g)$**

01.06.21.1146.01

$$\int z^n \sin(bz^2 + dz) \sin^v(fz + g) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{-\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{id + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{id + 2ibz}{4b}\right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{id - 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{id - 2ibz}{4b}\right) \right) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{ig(2s-v) - \frac{i(-id+if(2s-v))^2}{4b}} \left( \sum_{j=0}^n 2^{j-n} (id - if(2s-v))^{n-j} (-id + if(2s-v) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left(-\frac{i(-id + if(2s-v) - 2ibz)}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id + if(2s-v) - 2ibz)}{4b}\right) \right) \right) (-ib)^{-n-1} -$$

$$e^{ig(v-2s) - \frac{i(-id+if(v-2s))^2}{4b}} \left( \sum_{j=0}^n 2^{j-n} (id - if(v-2s))^{n-j} (-id + if(v-2s) - 2ibz)^{j+1} \right.$$

$$\left. \left. \left(-\frac{i(-id + if(v-2s) - 2ibz)}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id + if(v-2s) - 2ibz)}{4b}\right) \right) \right) (-ib)^{-n-1} +$$

$$(-1)^v (ib)^{-n-1} e^{\frac{i(id+if(2s-v))^2}{4b} + gi(2s-v)} \sum_{j=0}^n 2^{j-n} (-id - if(2s-v))^{n-j} (id + if(2s-v) + 2ibz)^{j+1}$$

$$\left(\frac{id + if(2s-v) + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{id + if(2s-v) + 2ibz}{4b}\right) +$$

$$(ib)^{-n-1} e^{\frac{i(id+if(v-2s))^2}{4b} + gi(v-2s)} \sum_{j=0}^n 2^{j-n} (-id - if(v-2s))^{n-j} (id + if(v-2s) + 2ibz)^{j+1}$$

$$\left(\frac{id + if(v-2s) + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{id + if(v-2s) + 2ibz}{4b}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1147.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin^v(fz + g) dz =$$

$$(-1)^n 2^{-2n-v-2} i \left(\frac{v}{2}\right) (1 - v \bmod 2) \left( e^{-\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib + 2id\sqrt{z})^{h+j} \right.$$



$$\begin{aligned}
 & \left( \frac{i(ib+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( b i (i b + 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), \frac{i (i b + 2 i d \sqrt{z})^2}{4 d} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i (i b + 2 i d \sqrt{z})^2}{d}} d i \Gamma \left( \frac{1}{2} (h + j + 2), \frac{i (i b + 2 i d \sqrt{z})^2}{4 d} \right) \right) - \\
 & e^{\frac{i b^2}{4 d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} (-i b - 2 i d \sqrt{z})^{h+j} \left( -\frac{i (-i b - 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( -i b (-i b - 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{i (-i b - 2 i d \sqrt{z})^2}{4 d} \right) - \right. \\
 & \left. 2 i d \sqrt{-\frac{i (-i b - 2 i d \sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{i (-i b - 2 i d \sqrt{z})^2}{4 d} \right) \right) d^{-2n-2} + \\
 & 2^{-2n-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{\frac{b^2}{4(-id+if(2k-v))+gi(2k-v)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} \right. \right. \\
 & \left. \left. (-i b + 2(-i d + i f(2k-v)) \sqrt{z}) \right)^{h+j} \left( -\frac{(-i b + 2(-i d + i f(2k-v)) \sqrt{z})^2}{-i d + i f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2(-i d + i f(2k-v)) \sqrt{-\frac{(-i b + 2(-i d + i f(2k-v)) \sqrt{z})^2}{-i d + i f(2k-v)}} \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{(-i b + 2(-i d + i f(2k-v)) \sqrt{z})^2}{4(-i d + i f(2k-v))} \right) - i b \right. \right. \\
 & \left. \left. (-i b + 2(-i d + i f(2k-v)) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{(-i b + 2(-i d + i f(2k-v)) \sqrt{z})^2}{4(-i d + i f(2k-v))} \right) \right) \right) \right) \\
 & (-i d + i f(2k-v))^{-2n-2} + (-1)^v e^{\frac{b^2}{4(id+if(2k-v))+gi(2k-v)}} (i d + i f(2k-v))^{-2n-2}
 \end{aligned}$$

$$\begin{aligned}
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+if(2k-v))\sqrt{z})^{h+j} \left( -\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{id+if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( bi(ib+2(id+if(2k-v))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{4(id+if(2k-v))} \right) + \right. \\
 & \left. 2 \sqrt{-\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{id+if(2k-v)}} (id+if(2k-v)) \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{4(id+if(2k-v))} \right) \right) - e^{\frac{b^2}{4(-id+if(v-2k))+gi(v-2k)}} \\
 & (-id+if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2(-id+if(v-2k))\sqrt{z})^{h+j} \\
 & \left( -\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2(-id+if(v-2k)) \right. \\
 & \left. \sqrt{-\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{4(-id+if(v-2k))} \right) - \right. \\
 & \left. ib(-ib+2(-id+if(v-2k))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{4(-id+if(v-2k))} \right) \right) + \\
 & e^{\frac{b^2}{4(id+if(v-2k))+gi(v-2k)}} (id+if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+if(v-2k))\sqrt{z})^{h+j} \\
 & \left( -\frac{(ib+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2(id+if(v-2k))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), -\frac{(ib+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) + 2 \sqrt{-\frac{(ib+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)}} \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) \right) \right)
 \end{aligned}$$

### Involving $z^n \sin(bz^r + dz + e) \sin^v(fz + g)$

01.06.21.1148.01

$$\int z^n \sin(bz^2 + dz + e) \sin^v(fz + g) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{ie - \frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{id + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{i(-id+if(2s-v))^2}{4b} - ie + gi(2s-v)} \left( \sum_{j=0}^n 2^{j-n} (id - if(2s-v))^{n-j} (-id + if(2s-v) - 2ibz)^{j+1} \right. \right.$$

$$\left. \left. \left(-\frac{i(-id + if(2s-v) - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id + if(2s-v) - 2ibz)^2}{4b}\right) \right) \right) (-ib)^{-n-1} -$$

$$e^{-\frac{i(-id+if(v-2s))^2}{4b} - ie + gi(v-2s)} \left( \sum_{j=0}^n 2^{j-n} (id - if(v-2s))^{n-j} (-id + if(v-2s) - 2ibz)^{j+1} \right.$$

$$\left. \left. \left(-\frac{i(-id + if(v-2s) - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id + if(v-2s) - 2ibz)^2}{4b}\right) \right) \right) (-ib)^{-n-1} +$$

$$(-1)^v (ib)^{-n-1} e^{\frac{i(id+if(2s-v))^2}{4b} + ie + gi(2s-v)} \sum_{j=0}^n 2^{j-n} (-id - if(2s-v))^{n-j} (id + if(2s-v) + 2ibz)^{j+1}$$

$$\left(\frac{id + if(2s-v) + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + if(2s-v) + 2ibz)^2}{4b}\right) +$$

$$(ib)^{-n-1} e^{\frac{i(id+if(v-2s))^2}{4b} + ie + gi(v-2s)} \sum_{j=0}^n 2^{j-n} (-id - if(v-2s))^{n-j} (id + if(v-2s) + 2ibz)^{j+1}$$

$$\left(\frac{id + if(v-2s) + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + if(v-2s) + 2ibz)^2}{4b}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1149.01

$$\int z^n \sin(\sqrt{z} b + dz + e) \sin^v(fz + g) dz =$$

$$(-1)^n 2^{-2n-v-2} i \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( e^{i e - \frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib + 2id\sqrt{z})^{h+j} \right.$$

$$\left. \left( \frac{i(ib + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib + 2id\sqrt{z})^2}{4d}\right) \right. \right.$$

$$\left. \left. 2\sqrt{\frac{i(ib + 2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib + 2id\sqrt{z})^2}{4d}\right) \right) \right) -$$

$$e^{\frac{ib^2}{4d} - ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\binom{j}{h} \binom{n}{j} \left( -ib(-ib - 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib - 2id\sqrt{z})^2}{4d}\right) - \right.$$

$$\left. \left. 2id\sqrt{-\frac{i(-ib - 2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib - 2id\sqrt{z})^2}{4d}\right) \right) \right) d^{-2n-2} +$$

$$2^{-2n-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{\frac{b^2}{4(-id+if(2k-v))} - ie + g i(2k-v)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} \right. \right.$$

$$\left. \left. (-ib + 2(-id + if(2k-v))\sqrt{z})^{h+j} \left( -\frac{(-ib + 2(-id + if(2k-v))\sqrt{z})^2}{-id + if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \left. \binom{j}{h} \binom{n}{j} \left( 2(-id + if(2k-v)) \sqrt{-\frac{(-ib + 2(-id + if(2k-v))\sqrt{z})^2}{-id + if(2k-v)}} \right. \right. \right.$$

$$\begin{aligned}
 & \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) - ib \\
 & \left. (-ib+2(-id+if(2k-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) \right) \Bigg) \\
 & (-id+if(2k-v))^{-2n-2} + (-1)^v e^{\frac{b^2}{4(id+if(2k-v))} + ie+gi(2k-v)} (id+if(2k-v))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(id+if(2k-v))\sqrt{z})^{h+j} \left( -\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{id+if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( b i (ib+2(id+if(2k-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{4(id+if(2k-v))}\right) \right) + \\
 & 2 \sqrt{-\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{id+if(2k-v)}} (id+if(2k-v)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \left. -\frac{(ib+2(id+if(2k-v))\sqrt{z})^2}{4(id+if(2k-v))}\right) \Bigg) - e^{\frac{b^2}{4(-id+if(v-2k))} - ie+gi(v-2k)} \\
 & (-id+if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2(-id+if(v-2k))\sqrt{z})^{h+j} \\
 & \left( -\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2(-id+if(v-2k)) \right. \\
 & \left. \sqrt{-\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{4(-id+if(v-2k))}\right) - \right. \\
 & \left. ib(-ib+2(-id+if(v-2k))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+2(-id+if(v-2k))\sqrt{z})^2}{4(-id+if(v-2k))}\right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & e^{\frac{b^2}{4(i d+i f(v-2 k))+i e+g i(v-2 k)}}(i d+i f(v-2 k))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j(-1)^{j-h} 4^j(i b)^{-h-j+2 n}(i b+2(i d+i f(v-2 k)) \sqrt{z})^{h+j} \\
 & \left(-\frac{(i b+2(i d+i f(v-2 k)) \sqrt{z})^2}{i d+i f(v-2 k)}\right)^{\frac{1}{2}(-h-j-1)}\binom{j}{h}\binom{n}{j}\left(b i(i b+2(i d+i f(v-2 k)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1),-\frac{(i b+2(i d+i f(v-2 k)) \sqrt{z})^2}{4(i d+i f(v-2 k))}\right)+2 \sqrt{-\frac{(i b+2(i d+i f(v-2 k)) \sqrt{z})^2}{i d+i f(v-2 k)}}\right) \\
 & (i d+i f(v-2 k)) \Gamma\left(\frac{1}{2}(h+j+2),-\frac{(i b+2(i d+i f(v-2 k)) \sqrt{z})^2}{4(i d+i f(v-2 k))}\right)\right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin(b z) \sin^v(c z^r)$

01.06.21.1150.01

$$\int z^n \sin(bz) \sin^v(cz^2) dz = i 2^{-v-1} \left(\frac{v}{2}\right) ((-ib)^{-n-1} \Gamma(n+1, -ibz) - (ib)^{-n-1} \Gamma(n+1, ibz)) (1 - v \bmod 2) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{ib^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (ib)^{n-j} (-ib + 2ic(2s-v)z)^{j+1} \right. \right.$$

$$\left. \left. \left( \frac{i(-ib + 2ic(2s-v)z)^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-ib + 2ic(2s-v)z)^2}{4c(2s-v)}\right) \right) (ic(2s-v))^{-n-1} + \right.$$

$$\left. (-1)^v e^{-\frac{ib^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (-ib)^{n-j} (ib + 2ic(2s-v)z)^{j+1} \left( \frac{i(ib + 2ic(2s-v)z)^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right. \right.$$

$$\left. \left. \Gamma\left(\frac{j+1}{2}, \frac{i(ib + 2ic(2s-v)z)^2}{4c(2s-v)}\right) \right) (ic(2s-v))^{-n-1} - e^{-\frac{ib^2}{4c(v-2s)}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (ib)^{n-j} \right.$$

$$\left. (-ib + 2ic(v-2s)z)^{j+1} \left( \frac{i(-ib + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-ib + 2ic(v-2s)z)^2}{4c(v-2s)}\right) + \right.$$

$$\left. e^{-\frac{ib^2}{4c(v-2s)}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-ib)^{n-j} (ib + 2ic(v-2s)z)^{j+1} \left( \frac{i(ib + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(ib + 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1151.01

$$\int z^n \sin(bz) \sin^v(c\sqrt{z}) dz =$$

$$i^{-v-1} 2^{-2n-v-2} (ib)^{-2n-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{ic^2(v-2s)^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-ic(v-2s) + 2ib\sqrt{z})^{h+j} \right.$$

$$\left. \left( \frac{i(-ic(v-2s) + 2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right.$$

$$\left. \left( 2ib \sqrt{\frac{i(-ic(v-2s) + 2ib\sqrt{z})^2}{b}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ic(v-2s) + 2ib\sqrt{z})^2}{4b}\right) \right) -$$

$$\begin{aligned}
 & i c(v-2 s)(-i c(v-2 s)+2 i b \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-i c(v-2 s)+2 i b \sqrt{z})^2}{4 b}\right) + \\
 & e^{-\frac{i c^2(v-2 s)^2}{4 b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2 s))^{-h-j+2 n}(i c(v-2 s)+2 i b \sqrt{z})^{h+j} \left(\frac{i(i c(v-2 s)+2 i b \sqrt{z})^2}{b}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c i(v-2 s)(i c(v-2 s)+2 i b \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(i c(v-2 s)+2 i b \sqrt{z})^2}{4 b}\right) + \right. \\
 & \left. 2 \sqrt{\frac{i(i c(v-2 s)+2 i b \sqrt{z})^2}{b}} b i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(i c(v-2 s)+2 i b \sqrt{z})^2}{4 b}\right) \right) + (-1)^{v+1} e^{\frac{i c^2(v-2 s)^2}{4 b}} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2 s))^{-h-j+2 n}(-i c(v-2 s)-2 i b \sqrt{z})^{h+j} \left(-\frac{i(-i c(v-2 s)-2 i b \sqrt{z})^2}{b}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( -i c(v-2 s)(-i c(v-2 s)-2 i b \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i c(v-2 s)-2 i b \sqrt{z})^2}{4 b}\right) - \right. \\
 & \left. 2 i b \sqrt{-\frac{i(-i c(v-2 s)-2 i b \sqrt{z})^2}{b}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-i c(v-2 s)-2 i b \sqrt{z})^2}{4 b}\right) \right) - e^{\frac{i c^2(v-2 s)^2}{4 b}} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2 s))^{-h-j+2 n}(i c(v-2 s)-2 i b \sqrt{z})^{h+j} \left(-\frac{i(i c(v-2 s)-2 i b \sqrt{z})^2}{b}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( i c(v-2 s)(i c(v-2 s)-2 i b \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(i c(v-2 s)-2 i b \sqrt{z})^2}{4 b}\right) - \right. \\
 & \left. 2 i b \sqrt{-\frac{i(i c(v-2 s)-2 i b \sqrt{z})^2}{b}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(i c(v-2 s)-2 i b \sqrt{z})^2}{4 b}\right) \right) -
 \end{aligned}$$



$$\frac{2^{-v-1} (1 - v \bmod 2)}{b} z^n \left(\frac{v}{2}\right) \left(\Gamma(n+1, -i b z) (-i b z)^{-n} + (i b z)^{-n} \Gamma(n+1, i b z)\right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin(dz + e) \sin^v(cz^r)$

01.06.21.1152.01

$$\int z^n \sin(e + dz) \sin^v(cz^2) dz =$$

$$i 2^{-v-1} \left(\frac{v}{2}\right) \left((-i d)^{-n-1} e^{ie} \Gamma(n+1, -i d z) - (i d)^{-n-1} e^{-ie} \Gamma(n+1, i d z)\right) (1 - v \bmod 2) - i^{-v-1} 2^{-v-2}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{id^2}{4c(2s-v)} - ie} \left( \sum_{j=0}^n 2^{j-n} (i d)^{n-j} (-i d + 2 i c (2s-v) z)^{j+1} \left( \frac{i(-i d + 2 i c (2s-v) z)^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right) \right)$$

$$\Gamma\left(\frac{j+1}{2}, \frac{i(-i d + 2 i c (2s-v) z)^2}{4 c (2s-v)}\right) \left( (i c (2s-v))^{-n-1} + \right)$$

$$(-1)^v e^{ie - \frac{id^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (-i d)^{n-j} (i d + 2 i c (2s-v) z)^{j+1} \left( \frac{i(i d + 2 i c (2s-v) z)^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right)$$

$$\Gamma\left(\frac{j+1}{2}, \frac{i(i d + 2 i c (2s-v) z)^2}{4 c (2s-v)}\right) \left( (i c (2s-v))^{-n-1} - e^{-\frac{id^2}{4c(v-2s)} - ie} (i c (v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i d)^{n-j} \right)$$

$$(-i d + 2 i c (v-2s) z)^{j+1} \left( \frac{i(-i d + 2 i c (v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-i d + 2 i c (v-2s) z)^2}{4 c (v-2s)}\right) +$$

$$e^{ie - \frac{id^2}{4c(v-2s)}} (i c (v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i d)^{n-j} (i d + 2 i c (v-2s) z)^{j+1} \left( \frac{i(i d + 2 i c (v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(i d + 2 i c (v-2s) z)^2}{4 c (v-2s)}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1153.01

$$\int z^n \sin(e + dz) \sin^v(c\sqrt{z}) dz =$$

$$\frac{2^{-v-1} e^{ie} (1 - v \bmod 2)}{d} z^n \left(\frac{v}{2}\right) \left(-(-i d z)^{-n} \Gamma(n+1, -i d z) - e^{-2ie} (i d z)^{-n} \Gamma(n+1, i d z)\right) + 2^{-2n-v-2} (i d)^{-2n-2}$$

$$\begin{aligned}
 & i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{i e^{-\frac{ic^2(v-2s)^2}{4d}}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-ic(v-2s) + 2id\sqrt{z})^{h+j} \right. \\
 & \quad \left. \left( \frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \quad \left. \left( 2id \sqrt{\frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) - ic(v-2s) \right. \right. \\
 & \quad \left. \left. (-ic(v-2s) + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) \right) \right) + e^{i e^{-\frac{ic^2(v-2s)^2}{4d}}} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s) + 2id\sqrt{z})^{h+j} \left( \frac{i(ic(v-2s) + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \quad \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(ic(v-2s) + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) \right) + \\
 & \quad 2 \sqrt{\frac{i(ic(v-2s) + 2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) \Bigg) + \\
 & (-1)^{v+1} e^{\frac{ic^2(v-2s)^2}{4d} - ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-ic(v-2s) - 2id\sqrt{z})^{h+j} \\
 & \quad \left( \frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad \left( -ic(v-2s)(-ic(v-2s) - 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{4d}\right) - 2id \right.
 \end{aligned}$$

$$\sqrt{-\frac{i(-ic(v-2s)-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ic(v-2s)-2id\sqrt{z})^2}{4d}\right) - e^{\frac{ic^2(v-2s)^2}{4d} - ic}$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s)-2id\sqrt{z})^{h+j} \left(-\frac{i(ic(v-2s)-2id\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)}$$

$$\binom{j}{h} \binom{n}{j} \left( ic(v-2s)(ic(v-2s)-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ic(v-2s)-2id\sqrt{z})^2}{4d}\right) - 2id \right.$$

$$\left. \sqrt{-\frac{i(ic(v-2s)-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(ic(v-2s)-2id\sqrt{z})^2}{4d}\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin(bz^r) \sin^v(cz^r)$

01.06.21.1154.01

$$\int z^{\alpha-1} \sin(bz^r) \sin^v(cz^r) dz = \frac{i 2^{-v-1} (1-v \bmod 2)}{r} z^\alpha \left(\frac{v}{2}\right) \left( (-ibz^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -ibz^r\right) - (ibz^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, ibz^r\right) \right) -$$

$$\frac{2^{-v-1} z^\alpha i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \Gamma\left(\frac{\alpha}{r}, (-ib-2ics+icv)z^r\right) ((-ib-2ics+icv)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. (-1)^{v+1} ((ib-2ics+icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-2ics+icv)z^r\right) + ((-ib+2ics-icv)z^r)^{-\frac{\alpha}{r}} \right.$$

$$\left. \Gamma\left(\frac{\alpha}{r}, (-ib+2ics-icv)z^r\right) - ((ib+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib+2ics-icv)z^r\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1155.01

$$\int z^n \sin(bz^2) \sin^v(cz^2) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1-v \bmod 2) - 2^{-v-2} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\left( e^{-\frac{1}{2}i\pi(1-v)} \Gamma\left(\frac{n+1}{2}, (-ib+ic(v-2s))z^2\right) ((-ib+ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} + e^{\frac{1}{2}i\pi(v+1)} ((ib+ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} \right.$$

$$\left. \Gamma\left(\frac{n+1}{2}, (ib+ic(v-2s))z^2\right) + e^{-\frac{1}{2}i\pi(v+1)} ((-ib-ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib-ic(v-2s))z^2\right) + \right.$$

$$\left. e^{\frac{1}{2}i\pi(1-v)} ((ib-ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib-ic(v-2s))z^2\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1156.01

$$\int z^n \sin(b\sqrt{z}) \sin^v(c\sqrt{z}) dz = (-1)^n i 2^{-v} b^{-2(n+1)} \left( \frac{v}{\frac{v}{2}} \right) \left( \Gamma(2(n+1), ib\sqrt{z}) - \Gamma(2(n+1), -ib\sqrt{z}) \right) (1 - v \bmod 2) -$$

$$2^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{2}i\pi(1-v)} \Gamma(2(n+1), (-ib+ic(v-2s))\sqrt{z}) (-ib+ic(v-2s))^{-2(n+1)} + \right.$$

$$e^{\frac{1}{2}i\pi(v+1)} (ib+ic(v-2s))^{-2(n+1)} \Gamma(2(n+1), (ib+ic(v-2s))\sqrt{z}) +$$

$$e^{-\frac{1}{2}i\pi(v+1)} (-ib-ic(v-2s))^{-2(n+1)} \Gamma(2(n+1), (-ib-ic(v-2s))\sqrt{z}) +$$

$$\left. e^{\frac{1}{2}i\pi(1-v)} (ib-ic(v-2s))^{-2(n+1)} \Gamma(2(n+1), (ib-ic(v-2s))\sqrt{z}) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin(bz^r + e) \sin^v(cz^r)$

01.06.21.1157.01

$$\int z^{\alpha-1} \sin(bz^r + e) \sin^v(cz^r) dz = \frac{i 2^{-v-1} (1 - v \bmod 2)}{r} z^\alpha \left( \frac{v}{\frac{v}{2}} \right) \left( e^{ie} (-ibz^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -ibz^r\right) - e^{-ie} (ibz^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, ibz^r\right) \right) -$$

$$\frac{1}{r} \left( (2i)^{-v-1} z^\alpha \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{ie} \Gamma\left(\frac{\alpha}{r}, (-ib-2ics+icv)z^r\right) ((-ib-2ics+icv)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$(1)^{v+1} e^{-ie} ((ib-2ics+icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-2ics+icv)z^r\right) + e^{ie} ((-ib+2ics-icv)z^r)^{-\frac{\alpha}{r}}$$

$$\left. \Gamma\left(\frac{\alpha}{r}, (-ib+2ics-icv)z^r\right) - e^{-ie} ((ib+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib+2ics-icv)z^r\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1158.01

$$\int z^n \sin(bz^2 + e) \sin^v(cz^2) dz =$$

$$-2^{-v-2} \left( \frac{v}{\frac{v}{2}} \right) \left( e^{ie-\frac{i\pi}{2}} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) (-ibz^2)^{\frac{1}{2}(-n-1)} + e^{-ie+\frac{i\pi}{2}} (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) z^{n+1} -$$

$$2^{-v-2} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{ie-\frac{1}{2}i\pi(1-v)} \Gamma\left(\frac{n+1}{2}, (-ib+ic(v-2s))z^2\right) ((-ib+ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$e^{-ie+\frac{1}{2}i\pi(v+1)} ((ib+ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib+ic(v-2s))z^2\right) +$$

$$e^{ie-\frac{1}{2}i\pi(v+1)} ((-ib-ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib-ic(v-2s))z^2\right) +$$

$$\left. e^{-ie+\frac{1}{2}i\pi(1-v)} ((ib-ic(v-2s))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib-ic(v-2s))z^2\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1159.01

$$\int z^n \sin(\sqrt{z} b + e) \sin^v(c \sqrt{z}) dz =$$

$$(-1)^n 2^{-v} b^{-2(n+1)} \left(\frac{v}{\frac{v}{2}}\right) \left( e^{i e - \frac{i\pi}{2}} \Gamma(2(n+1), -i b \sqrt{z}) + e^{-i e + \frac{i\pi}{2}} \Gamma(2(n+1), i b \sqrt{z}) \right) (1 - v \bmod 2) -$$

$$2^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{i e - \frac{1}{2} i \pi (1-v)} \Gamma(2(n+1), (-i b + i c (v-2s)) \sqrt{z}) (-i b + i c (v-2s))^{-2(n+1)} + \right.$$

$$e^{-i e + \frac{1}{2} i \pi (v+1)} (i b + i c (v-2s))^{-2(n+1)} \Gamma(2(n+1), (i b + i c (v-2s)) \sqrt{z}) +$$

$$e^{i e - \frac{1}{2} i \pi (v+1)} (-i b - i c (v-2s))^{-2(n+1)} \Gamma(2(n+1), (-i b - i c (v-2s)) \sqrt{z}) +$$

$$\left. e^{-i e + \frac{1}{2} i \pi (1-v)} (i b - i c (v-2s))^{-2(n+1)} \Gamma(2(n+1), (i b - i c (v-2s)) \sqrt{z}) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n \sin(b z^r + d z) \sin^v(c z^r)$**

01.06.21.1160.01

$$\int z^n \sin(bz^2 + dz) \sin^v(cz^2) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{-\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{id + 2ibz}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{d^2}{4(-ib+ic(2s-v))}} \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib+ic(2s-v))z)^{j+1} \right.$$

$$\left. \left( -\frac{(-id + 2(-ib+ic(2s-v))z)^2}{-ib+ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib+ic(2s-v))z)^2}{4(-ib+ic(2s-v))}\right) \right) \right)$$

$$(-ib+ic(2s-v))^{-n-1} + (-1)^v e^{\frac{d^2}{4(ib+ic(2s-v))}} (ib+ic(2s-v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib+ic(2s-v))z)^{j+1}$$

$$\left( -\frac{(id + 2(ib+ic(2s-v))z)^2}{ib+ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib+ic(2s-v))z)^2}{4(ib+ic(2s-v))}\right) -$$

$$\frac{d^2}{e^{4(-ib+ic(v-2s))}} (-ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib+ic(v-2s))z)^{j+1}$$

$$\left( -\frac{(-id + 2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))}\right) +$$

$$\frac{d^2}{e^{4(ib+ic(v-2s))}} (ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib+ic(v-2s))z)^{j+1}$$

$$\left( -\frac{(id + 2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))}\right) \Big) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1161.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin^v(c\sqrt{z}) dz =$$

$$i 2^{-2n-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2) \left( (-id)^{-2n-2} e^{\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2id\sqrt{z})^{h+j} \right.$$

$$\begin{aligned}
 & \left( -\frac{i(-ib-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ib(-ib-2id\sqrt{z}) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) - \right. \\
 & \left. 2id \sqrt{-\frac{i(-ib-2id\sqrt{z})^2}{d}} \Gamma\left( \frac{1}{2}(h+j+2), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) \right) - \\
 & (id)^{-2n-2} e^{-\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2id\sqrt{z})^{h+j} \left( \frac{i(ib+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( bi(ib+2id\sqrt{z}) \Gamma\left( \frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma\left( \frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) \right) + 2^{-2n-v-2} i^{-v-1} \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{-\frac{i(-ib+ic(2k-v))^2}{4d}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(2k-v))^{-h-j+2n} (-ib+ic(2k-v)-2id\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left( -\frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-ib+ic(2k-v)) \right. \\
 & \left. (-ib+ic(2k-v)-2id\sqrt{z}) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{4d} \right) - 2id \right. \\
 & \left. \left. \sqrt{-\frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{d}} \Gamma\left( \frac{1}{2}(h+j+2), -\frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{4d} \right) \right) \right) \\
 & (-id)^{-2n-2} - e^{-\frac{i(-ib+ic(v-2k))^2}{4d}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(v-2k))^{-h-j+2n} (-ib+ic(v-2k)-2id\sqrt{z})^{h+j} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (-ib+ic(v-2k)) \right. \\
 & \left. (-ib+ic(v-2k)-2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{4d} \right) - 2id \right. \\
 & \left. \sqrt{-\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{4d} \right) \right) \Bigg) \\
 & (-id)^{-2n-2} + (-1)^v (id)^{-2n-2} e^{\frac{i(ib+ic(2k-v))^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(2k-v))^{-h-j+2n} \\
 & (ib+ic(2k-v)+2id\sqrt{z})^{h+j} \left( \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib+ic(2k-v))(ib+ic(2k-v)+2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{4d} \right) \right. \\
 & \left. 2\sqrt{\frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{4d} \right) \right) \Bigg) + \\
 & (id)^{-2n-2} e^{\frac{i(ib+ic(v-2k))^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2k))^{-h-j+2n} (ib+ic(v-2k)+2id\sqrt{z})^{h+j} \\
 & \left( \frac{i(ib+ic(v-2k)+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (ib+ic(v-2k))(ib+ic(v-2k)+2id\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), \frac{i(ib+ic(v-2k)+2id\sqrt{z})^2}{4d} \right) + 2\sqrt{\frac{i(ib+ic(v-2k)+2id\sqrt{z})^2}{d}} \right. \\
 & \left. di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+ic(v-2k)+2id\sqrt{z})^2}{4d} \right) \right) \Bigg) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$



### Involving $z^n \sin(bz^r + dz + e) \sin^v(cz^r)$

01.06.21.1162.01

$$\int z^n \sin(bz^2 + dz + e) \sin^v(cz^2) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\begin{aligned} & \left( (ib)^{-n-1} e^{ie - \frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{i(id + 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right. \\ & \left. (-ib)^{-n-1} e^{\frac{id^2}{4b} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) - \\ & i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{d^2}{4(-ib+ic(2s-v))} - ie} \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib + ic(2s-v))z)^{j+1} \right. \right. \\ & \left. \left. \left( -\frac{(-id + 2(-ib + ic(2s-v))z)^2}{-ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib + ic(2s-v))z)^2}{4(-ib + ic(2s-v))}\right) \right) \right) \\ & (-ib + ic(2s-v))^{-n-1} + (-1)^v e^{\frac{d^2}{4(ib+ic(2s-v))} + ie} (ib + ic(2s-v))^{-n-1} \\ & \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib + ic(2s-v))z)^{j+1} \left( -\frac{(id + 2(ib + ic(2s-v))z)^2}{ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \\ & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib + ic(2s-v))z)^2}{4(ib + ic(2s-v))}\right) - \\ & e^{\frac{d^2}{4(-ib+ic(v-2s))} - ie} (-ib + ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib + ic(v-2s))z)^{j+1} \\ & \left( -\frac{(-id + 2(-ib + ic(v-2s))z)^2}{-ib + ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib + ic(v-2s))z)^2}{4(-ib + ic(v-2s))}\right) + \\ & e^{\frac{d^2}{4(ib+ic(v-2s))} + ie} (ib + ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib + ic(v-2s))z)^{j+1} \\ & \left( -\frac{(id + 2(ib + ic(v-2s))z)^2}{ib + ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib + ic(v-2s))z)^2}{4(ib + ic(v-2s))}\right) \Big) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1163.01

$$\int z^n \sin(\sqrt{z} b + dz + e) \sin^v(c \sqrt{z}) dz =$$

$$i 2^{-2n-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( (-id)^{-2n-2} e^{\frac{ib^2}{4d} - ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2id\sqrt{z})^{h+j} \right.$$

$$\left. \left( -\frac{i(-ib - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ib(-ib - 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib - 2id\sqrt{z})^2}{4d}\right) \right. \right.$$

$$\left. \left. 2id \sqrt{-\frac{i(-ib - 2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib - 2id\sqrt{z})^2}{4d}\right) \right) \right) -$$

$$(id)^{-2n-2} e^{ie - \frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib + 2id\sqrt{z})^{h+j} \left( \frac{i(ib + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\binom{j}{h} \binom{n}{j} \left( b i (ib + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib + 2id\sqrt{z})^2}{4d}\right) + \right.$$

$$\left. 2 \sqrt{\frac{i(ib + 2id\sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib + 2id\sqrt{z})^2}{4d}\right) \right) \right) +$$

$$2^{-2n-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{-\frac{i(-ib+ic(2k-v))^2}{4d} - ie} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib + ic(2k-v))^{-h-j+2n} \right. \right.$$

$$\left. \left. (-ib + ic(2k-v) - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ib + ic(2k-v) - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \right) \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( (-ib + ic(2k-v)) (-ib + ic(2k-v) - 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \right.$$

$$\begin{aligned}
 & \left. - \frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{4d} \right) - 2id \sqrt{-\frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{d}} \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib+ic(2k-v)-2id\sqrt{z})^2}{4d}\right)\right) \Bigg) (-id)^{-2n-2} - \\
 & e^{-\frac{i(-ib+ic(v-2k))^2}{4d}} - ie \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(v-2k))^{-h-j+2n} (-ib+ic(v-2k)-2id\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-ib+ic(v-2k)) \right. \\
 & \left. (-ib+ic(v-2k)-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{4d}\right) - 2id \right. \\
 & \left. \sqrt{-\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib+ic(v-2k)-2id\sqrt{z})^2}{4d}\right) \right) \Bigg) \\
 & (-id)^{-2n-2} + (-1)^v (id)^{-2n-2} e^{\frac{i(ib+ic(2k-v))^2}{4d}} + ie \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(2k-v))^{-h-j+2n} \\
 & (ib+ic(2k-v)+2id\sqrt{z})^{h+j} \left( \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib+ic(2k-v))(ib+ic(2k-v)+2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{4d}\right) \right. \\
 & \left. + 2 \sqrt{\frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{4d}\right) \right) \Bigg) + \\
 & (id)^{-2n-2} e^{\frac{i(ib+ic(v-2k))^2}{4d}} + ie \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2k))^{-h-j+2n} (ib+ic(v-2k)+2id\sqrt{z})^{h+j}
 \end{aligned}$$

$$\left( \frac{i(i b + i c(v - 2k) + 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (i b + i c(v - 2k))(i b + i c(v - 2k) + 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2}(h + j + 1), \frac{i(i b + i c(v - 2k) + 2 i d \sqrt{z})^2}{4 d} \right) + 2 \sqrt{\frac{i(i b + i c(v - 2k) + 2 i d \sqrt{z})^2}{d}} \right) d i \Gamma \left( \frac{1}{2}(h + j + 2), \frac{i(i b + i c(v - 2k) + 2 i d \sqrt{z})^2}{4 d} \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin(d z) \sin^v(c z' + g)$

01.06.21.1164.01

$$\int z^n \sin(d z) \sin^v(c z^2 + g) dz =$$

$$i(-1)^n 2^{-v-1} \binom{v}{\frac{v}{2}} \left( (-i d)^{-n-1} \Gamma(n+1, i d z) - (i d)^{-n-1} \Gamma(n+1, -i d z) \right) (1 - v \bmod 2) - 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{i d^2}{4 c(v-2s)} + \frac{i \pi v}{2} - i g(v-2s) + \frac{i \pi}{2}} \sum_{j=0}^n 2^{j-n} (i d)^{n-j} (-i d - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(-i d - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(-i d - 2 i c(v-2s) z)^2}{4 c(v-2s)} \right) (-i c(v-2s))^{-n-1} + e^{\frac{i d^2}{4 c(v-2s)} + \frac{i \pi v}{2} - i g(v-2s) - \frac{i \pi}{2}} \sum_{j=0}^n 2^{j-n} (-i d)^{n-j} (i d - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(i d - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(i d - 2 i c(v-2s) z)^2}{4 c(v-2s)} \right) (-i c(v-2s))^{-n-1} + e^{-\frac{i d^2}{4 c(v-2s)} + g i(v-2s) - \frac{i \pi v}{2} + \frac{i \pi}{2}} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i d)^{n-j} (-i d + 2 i c(v-2s) z)^{j+1} \left( \frac{i(-i d + 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(-i d + 2 i c(v-2s) z)^2}{4 c(v-2s)} \right) + e^{-\frac{i d^2}{4 c(v-2s)} + g i(v-2s) - \frac{i \pi v}{2} - \frac{i \pi}{2}} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i d)^{n-j} (i d + 2 i c(v-2s) z)^{j+1} \left( \frac{i(i d + 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(i d + 2 i c(v-2s) z)^2}{4 c(v-2s)} \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1165.01

$$\int z^n \sin(dz) \sin^v(\sqrt{z} c + g) dz = (-1)^n 2^{-v-1} i \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} \Gamma(n+1, idz) - (id)^{-n-1} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) +$$

$$2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2 i(v-2s)^2}{4d} - i g(v-2s) + \frac{i\pi v}{2} + \frac{i\pi}{2}} \right.$$

$$\left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-ic(v-2s) - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \left( \binom{j}{h} \binom{n}{j} \left( -ic(v-2s) (-ic(v-2s) - 2id\sqrt{z}) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{4d} \right) - 2 \right. \right. \right.$$

$$\left. \left. \left. id \sqrt{-\frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{d}} \Gamma\left( \frac{1}{2}(h+j+2), -\frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{4d} \right) \right) \right) \right)$$

$$(-id)^{-2(n+1)} + e^{\frac{c^2 i(v-2s)^2}{4d} + i g(v-2s) - \frac{i\pi v}{2} + \frac{i\pi}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} \right.$$

$$(ic(v-2s) - 2id\sqrt{z})^{h+j} \left( -\frac{i(ic(v-2s) - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( ic(v-2s) (ic(v-2s) - 2id\sqrt{z}) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(ic(v-2s) - 2id\sqrt{z})^2}{4d} \right) - 2i \right.$$

$$\left. \left. \left. d \sqrt{-\frac{i(ic(v-2s) - 2id\sqrt{z})^2}{d}} \Gamma\left( \frac{1}{2}(h+j+2), -\frac{i(ic(v-2s) - 2id\sqrt{z})^2}{4d} \right) \right) \right) \right)$$

$$(-id)^{-2(n+1)} + (id)^{-2(n+1)} e^{-\frac{ic^2(v-2s)^2}{4d} - i g(v-2s) + \frac{i\pi v}{2} - \frac{i\pi}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n}$$

$$\begin{aligned}
 & (-ic(v-2s) + 2id\sqrt{z})^{h+j} \left( \frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( 2id\sqrt{\frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) - \right. \\
 & \left. ic(v-2s)(-ic(v-2s) + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) \right) + \\
 & (id)^{-2(n+1)} e^{-\frac{ic^2(v-2s)^2}{4d} + g i(v-2s) - \frac{i\pi v}{2} - \frac{i\pi}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s) + 2id\sqrt{z})^{h+j} \\
 & \left( \frac{i(ic(v-2s) + 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i(v-2s)(ic(v-2s) + 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) + \right. \\
 & \left. 2\sqrt{\frac{i(ic(v-2s) + 2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ic(v-2s) + 2id\sqrt{z})^2}{4d}\right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin(dz + e) \sin^v(cz' + g)$**

01.06.21.1166.01

$$\int z^n \sin(dz + e) \sin^v(cz^2 + g) dz =$$

$$i(-1)^n 2^{-v-1} \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} e^{-ie} \Gamma(n+1, idz) - (id)^{-n-1} e^{ie} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{id^2}{4c(v-2s)} - ie + \frac{i\pi v}{2} - ig(v-2s) + \frac{i\pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ic(v-2s)z)^{j+1} \right. \right.$$

$$\left. \left( -\frac{i(-id - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) (-ic(v-2s))^{-n-1} +$$

$$e^{\frac{id^2}{4c(v-2s)} + ie + \frac{i\pi v}{2} - ig(v-2s) - \frac{i\pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id - 2ic(v-2s)z)^{j+1} \left( -\frac{i(id - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(id - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) (-ic(v-2s))^{-n-1} +$$

$$e^{-\frac{id^2}{4c(v-2s)} - ie + ig(v-2s) - \frac{i\pi v}{2} + \frac{i\pi}{2}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2ic(v-2s)z)^{j+1}$$

$$\left( \frac{i(-id + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-id + 2ic(v-2s)z)^2}{4c(v-2s)}\right) +$$

$$e^{-\frac{id^2}{4c(v-2s)} + ie + ig(v-2s) - \frac{i\pi v}{2} - \frac{i\pi}{2}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ic(v-2s)z)^{j+1}$$

$$\left( \frac{i(id + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ic(v-2s)z)^2}{4c(v-2s)}\right) \Big/; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1167.01

$$\int z^n \sin(dz + e) \sin^v(\sqrt{z}c + g) dz =$$

$$(-1)^n 2^{-v-1} i \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} e^{-ie} \Gamma(n+1, idz) - (id)^{-n-1} e^{ie} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) +$$

$$2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2 i(v-2s)^2}{4d} - ig(v-2s) - ie + \frac{i\pi v}{2} + \frac{i\pi}{2}} \right.$$

$$\left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-ic(v-2s) - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ic(v-2s) - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \right) \right)$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( -i c(v-2s) (-i c(v-2s) - 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{i(-i c(v-2s) - 2 i d \sqrt{z})^2}{4 d} \right) - 2 \right. \\
 & \quad \left. i d \sqrt{-\frac{i(-i c(v-2s) - 2 i d \sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2} (h+j+2), -\frac{i(-i c(v-2s) - 2 i d \sqrt{z})^2}{4 d} \right) \right) \\
 & (-i d)^{-2(n+1)} + e^{\frac{c^2 i(v-2s)^2}{4 d} + g i(v-2s) - i e - \frac{i \pi v}{2} + \frac{i \pi}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} \right. \\
 & \quad \left. (i c(v-2s) - 2 i d \sqrt{z})^{h+j} \left( -\frac{i(i c(v-2s) - 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \quad \left( i c(v-2s) (i c(v-2s) - 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{i(i c(v-2s) - 2 i d \sqrt{z})^2}{4 d} \right) - 2 i d \right. \\
 & \quad \left. \sqrt{-\frac{i(i c(v-2s) - 2 i d \sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2} (h+j+2), -\frac{i(i c(v-2s) - 2 i d \sqrt{z})^2}{4 d} \right) \right) \Big) (-i d)^{-2(n+1)} + \\
 & (i d)^{-2(n+1)} e^{-\frac{c^2 i(v-2s)^2}{4 d} - i g(v-2s) + i e + \frac{i \pi v}{2} - \frac{i \pi}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n} \\
 & \quad (-i c(v-2s) + 2 i d \sqrt{z})^{h+j} \left( \frac{i(-i c(v-2s) + 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad \left( 2 i d \sqrt{\frac{i(-i c(v-2s) + 2 i d \sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i(-i c(v-2s) + 2 i d \sqrt{z})^2}{4 d} \right) - \right. \\
 & \quad \left. i c(v-2s) (-i c(v-2s) + 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), \frac{i(-i c(v-2s) + 2 i d \sqrt{z})^2}{4 d} \right) \right) \Big) +
 \end{aligned}$$



$$\begin{aligned}
 & (i d)^{-2(n+1)} e^{-\frac{ic^2(v-2s)^2}{4d} + g i(v-2s) + i e - \frac{i\pi v}{2} - \frac{i\pi}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} \\
 & (i c(v-2s) + 2 i d \sqrt{z})^{h+j} \left( \frac{i(i c(v-2s) + 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i(v-2s) (i c(v-2s) + 2 i d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(i c(v-2s) + 2 i d \sqrt{z})^2}{4d}\right) + \right. \\
 & \left. 2 \sqrt{\frac{i(i c(v-2s) + 2 i d \sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(i c(v-2s) + 2 i d \sqrt{z})^2}{4d}\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^{\alpha-1} \sin(b z^r) \sin^v(c z^r + g)$

01.06.21.1168.01

$$\begin{aligned}
 \int z^{\alpha-1} \sin(b z^r) \sin^v(c z^r + g) dz &= \frac{i 2^{-v-1} (1 - v \bmod 2)}{r} z^\alpha \left(\frac{v}{2}\right) \left( (-i b z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -i b z^r\right) - (i b z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, i b z^r\right) \right) - \\
 & \frac{(2i)^{-v-1} z^\alpha \left(\frac{v-1}{2}\right)}{r} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{2i g s - i g v} \Gamma\left(\frac{\alpha}{r}, (-i b - 2i c s + i c v) z^r\right) ((-i b - 2i c s + i c v) z^r)^{-\frac{\alpha}{r}} + \right. \\
 & (-1)^{v+1} e^{2i g s - i g v} ((i b - 2i c s + i c v) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (i b - 2i c s + i c v) z^r\right) + e^{i g v - 2i g s} ((-i b + 2i c s - i c v) z^r)^{-\frac{\alpha}{r}} \\
 & \left. \Gamma\left(\frac{\alpha}{r}, (-i b + 2i c s - i c v) z^r\right) - e^{i g v - 2i g s} ((i b + 2i c s - i c v) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (i b + 2i c s - i c v) z^r\right) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1169.01

$$\begin{aligned}
 \int z^n \sin(b z^2) \sin^v(c z^2 + g) dz &= \\
 i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) & \left( (-i b z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -i b z^2\right) - (i b z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i b z^2\right) \right) (1 - v \bmod 2) - \\
 2^{-v-2} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} & (-1)^s \binom{v}{s} \left( e^{-\frac{1}{2} i \pi (1-v) - i g (v-2s)} \Gamma\left(\frac{n+1}{2}, (-i b + i c (v-2s)) z^2\right) ((-i b + i c (v-2s)) z^2)^{\frac{1}{2}(-n-1)} + \right. \\
 e^{\frac{1}{2} i \pi (v+1) - i g (v-2s)} & ((i b + i c (v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b + i c (v-2s)) z^2\right) + \\
 e^{i g (v-2s) - \frac{1}{2} i \pi (v+1)} & ((-i b - i c (v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-i b - i c (v-2s)) z^2\right) + \\
 e^{\frac{1}{2} i \pi (1-v) + i g (v-2s)} & ((i b - i c (v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b - i c (v-2s)) z^2\right) \left. \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1170.01

$$\int z^n \sin(b\sqrt{z}) \sin^v(\sqrt{z}c + g) dz = (-1)^n i 2^{-v} b^{-2(n+1)} \left(\frac{v}{2}\right) \left(\Gamma(2(n+1), ib\sqrt{z}) - \Gamma(2(n+1), -ib\sqrt{z})\right) (1 - v \bmod 2) -$$

$$2^{-v} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{2}i\pi(1-v)-ig(v-2s)} \Gamma(2(n+1), (-ib+ic(v-2s))\sqrt{z}) \left((-ib+ic(v-2s))\sqrt{z}\right)^{-2(n+1)} + \right.$$

$$e^{\frac{1}{2}i\pi(v+1)-ig(v-2s)} \left((ib+ic(v-2s))\sqrt{z}\right)^{-2(n+1)} \Gamma(2(n+1), (ib+ic(v-2s))\sqrt{z}) +$$

$$e^{ig(v-2s)-\frac{1}{2}i\pi(v+1)} \left((-ib-ic(v-2s))\sqrt{z}\right)^{-2(n+1)} \Gamma(2(n+1), (-ib-ic(v-2s))\sqrt{z}) +$$

$$\left. e^{\frac{1}{2}i\pi(1-v)+ig(v-2s)} \left((ib-ic(v-2s))\sqrt{z}\right)^{-2(n+1)} \Gamma(2(n+1), (ib-ic(v-2s))\sqrt{z}) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin(bz^r + e) \sin^v(cz^r + g)$

01.06.21.1171.01

$$\int z^{\alpha-1} \sin(bz^r + e) \sin^v(cz^r + g) dz =$$

$$\frac{i 2^{-v-1} z^\alpha}{r} \left(\frac{v}{2}\right) \left( e^{ie} (-ibz^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, -ibz^r\right) - e^{-ie} (ibz^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, ibz^r\right) \right) (1 - v \bmod 2) - \frac{(2i)^{-v-1} z^\alpha}{r}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{ie+2igs-igv} \Gamma\left(\frac{\alpha}{r}, (-ib-2ics+icv)z^r\right) \left((-ib-2ics+icv)z^r\right)^{-\frac{\alpha}{r}} + (-1)^{v+1} e^{-ie+2igs-igv}$$

$$\left((ib-2ics+icv)z^r\right)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-2ics+icv)z^r\right) + e^{ie-2igs+igv} \left((-ib+2ics-icv)z^r\right)^{-\frac{\alpha}{r}}$$

$$\Gamma\left(\frac{\alpha}{r}, (-ib+2ics-icv)z^r\right) - e^{-ie-2igs+igv} \left((ib+2ics-icv)z^r\right)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib+2ics-icv)z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.1172.01

$$\int z^n \sin(bz^2 + e) \sin^v(cz^2 + g) dz =$$

$$-2^{-v-2} \left(\frac{v}{2}\right) \left( e^{ie-\frac{i\pi}{2}} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) (-ibz^2)^{\frac{1}{2}(-n-1)} + e^{-ie+\frac{i\pi}{2}} (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) z^{n+1} -$$

$$2^{-v-2} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{ie-\frac{1}{2}i\pi(1-v)-ig(v-2s)} \Gamma\left(\frac{n+1}{2}, (-ib+ic(v-2s))z^2\right) \left((-ib+ic(v-2s))z^2\right)^{\frac{1}{2}(-n-1)} + \right.$$

$$e^{-ie+\frac{1}{2}i\pi(v+1)-ig(v-2s)} \left((ib+ic(v-2s))z^2\right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib+ic(v-2s))z^2\right) +$$

$$e^{ie-\frac{1}{2}i\pi(v+1)+ig(v-2s)} \left((-ib-ic(v-2s))z^2\right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib-ic(v-2s))z^2\right) +$$

$$\left. e^{-ie+\frac{1}{2}i\pi(1-v)+ig(v-2s)} \left((ib-ic(v-2s))z^2\right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib-ic(v-2s))z^2\right) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1173.01

$$\int z^n \sin(\sqrt{z} b + e) \sin^v(\sqrt{z} c + g) dz =$$

$$(-1)^n 2^{-v} b^{-2(n+1)} \binom{v}{\frac{v}{2}} \left( e^{i e - \frac{i\pi}{2}} \Gamma(2(n+1), -i b \sqrt{z}) + e^{-i e + \frac{i\pi}{2}} \Gamma(2(n+1), i b \sqrt{z}) \right) (1 - v \bmod 2) -$$

$$2^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{i e - \frac{1}{2} i \pi (1-v) - i g (v-2s)} \Gamma(2(n+1), (-i b + i c (v-2s)) \sqrt{z}) (-i b + i c (v-2s))^{-2(n+1)} + \right.$$

$$e^{-i e + \frac{1}{2} i \pi (v+1) - i g (v-2s)} (i b + i c (v-2s))^{-2(n+1)} \Gamma(2(n+1), (i b + i c (v-2s)) \sqrt{z}) +$$

$$e^{i e - \frac{1}{2} i \pi (v+1) + i g (v-2s)} (-i b - i c (v-2s))^{-2(n+1)} \Gamma(2(n+1), (-i b - i c (v-2s)) \sqrt{z}) +$$

$$\left. e^{-i e + \frac{1}{2} i \pi (1-v) + i g (v-2s)} (i b - i c (v-2s))^{-2(n+1)} \Gamma(2(n+1), (i b - i c (v-2s)) \sqrt{z}) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n \sin(bz^r + dz) \sin^v(cz^r + g)$**

01.06.21.1174.01

$$\int z^n \sin(bz^2 + dz) \sin^v(cz^2 + g) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{-\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{i(id + 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{d^2}{4(-ib+ic(2s-v))} + gi(2s-v)} \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib + ic(2s-v))z)^{j+1} \right.$$

$$\left. \left( -\frac{(-id + 2(-ib + ic(2s-v))z)^2}{-ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib + ic(2s-v))z)^2}{4(-ib + ic(2s-v))}\right) \right) \right)$$

$$(-ib + ic(2s-v))^{-n-1} + (-1)^v e^{\frac{d^2}{4(ib+ic(2s-v))} + gi(2s-v)} (ib + ic(2s-v))^{-n-1}$$

$$\sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib + ic(2s-v))z)^{j+1} \left( -\frac{(id + 2(ib + ic(2s-v))z)^2}{ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib + ic(2s-v))z)^2}{4(ib + ic(2s-v))}\right) -$$

$$e^{\frac{d^2}{4(-ib+ic(v-2s))} + gi(v-2s)} (-ib + ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib + ic(v-2s))z)^{j+1}$$

$$\left( -\frac{(-id + 2(-ib + ic(v-2s))z)^2}{-ib + ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib + ic(v-2s))z)^2}{4(-ib + ic(v-2s))}\right) +$$

$$e^{\frac{d^2}{4(ib+ic(v-2s))} + gi(v-2s)} (ib + ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib + ic(v-2s))z)^{j+1}$$

$$\left( -\frac{(id + 2(ib + ic(v-2s))z)^2}{ib + ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib + ic(v-2s))z)^2}{4(ib + ic(v-2s))}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1175.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin^v(\sqrt{z} c + g) dz =$$

$$i (-1)^n 2^{-2n-v-2} d^{-2n-2} \left(\frac{v}{2}\right) (1 - v \bmod 2) \left( e^{-\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib + 2id\sqrt{z})^{h+j} \right.$$

$$\begin{aligned}
 & \left( \frac{i(ib+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) + \right. \\
 & \left. 2\sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) \right) - \\
 & e^{\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib-2id\sqrt{z})^{h+j} \left( \frac{i(-ib-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( -ib(-ib-2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) - \right. \\
 & \left. 2id\sqrt{-\frac{i(-ib-2id\sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) \right) - \\
 & (-1)^n i^{-v-1} 2^{-2n-v-2} d^{-2n-2} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{\frac{i(ib+ic(2k-v))^2}{4d} + g i(2k-v)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(2k-v))^{-h-j+2n} \right. \\
 & \left. (ib+ic(2k-v)+2id\sqrt{z})^{h+j} \left( \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right) \\
 & \left( (ib+ic(2k-v))(ib+ic(2k-v)+2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{4d} \right) + \right. \\
 & \left. 2\sqrt{\frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+ic(2k-v)+2id\sqrt{z})^2}{4d} \right) \right) + \\
 & e^{\frac{i(ib+ic(v-2k))^2}{4d} + g i(v-2k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2k))^{-h-j+2n} (ib+ic(v-2k)+2id\sqrt{z})^{h+j}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (i b+i c(v-2 k))(i b+i c(v-2 k)+2 i d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{4 d}\right) \right)+ \\
 & \left. 2 \sqrt{\frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{4 d}\right) \right) + \\
 & (-1)^{v+1} e^{i g(2 k-v)-\frac{i(-i b+i c(2 k-v))^2}{4 d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b+i c(2 k-v))^{-h-j+2 n} (-i b+i c(2 k-v)-2 i d \sqrt{z})^{h+j} \\
 & \left( -\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-i b+i c(2 k-v)) \\
 & (-i b+i c(2 k-v)-2 i d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{4 d}\right) - \\
 & \left. 2 i d \sqrt{-\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{4 d}\right) \right) - \\
 & e^{i g(v-2 k)-\frac{i(-i b+i c(v-2 k))^2}{4 d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b+i c(v-2 k))^{-h-j+2 n} (-i b+i c(v-2 k)-2 i d \sqrt{z})^{h+j} \\
 & \left( -\frac{i(-i b+i c(v-2 k)-2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (-i b+i c(v-2 k))(-i b+i c(v-2 k)-2 i d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{i(-i b+i c(v-2 k)-2 i d \sqrt{z})^2}{4 d}\right) -2 i d \sqrt{-\frac{i(-i b+i c(v-2 k)-2 i d \sqrt{z})^2}{d}} \Gamma\left( \right. \right. \\
 & \left. \left. -\dots \right) \right)
 \end{aligned}$$

### Involving $z^n \sin(bz^r + dz + e) \sin^v(cz^r + g)$

01.06.21.1176.01

$$\int z^n \sin(bz^2 + dz + e) \sin^v(cz^2 + g) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\begin{aligned} & \left( (ib)^{-n-1} e^{ie - \frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{i(id + 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right. \\ & \left. (-ib)^{-n-1} e^{\frac{id^2}{4b} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) - \\ & i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{d^2}{4(-ib+ic(2s-v))} - ie + gi(2s-v)} \right. \\ & \left. \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib + ic(2s-v))z)^{j+1} \left(-\frac{(-id + 2(-ib + ic(2s-v))z)^2}{-ib + ic(2s-v)}\right)^{\frac{1}{2}(-j-1)} \right. \right. \\ & \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib + ic(2s-v))z)^2}{4(-ib + ic(2s-v))}\right) \right) (-ib + ic(2s-v))^{-n-1} + \right. \\ & \left. (-1)^v e^{\frac{d^2}{4(ib+ic(2s-v))} + ie + gi(2s-v)} (ib + ic(2s-v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib + ic(2s-v))z)^{j+1} \right. \\ & \left. \left( -\frac{(id + 2(ib + ic(2s-v))z)^2}{ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib + ic(2s-v))z)^2}{4(ib + ic(2s-v))}\right) - \right. \\ & \left. e^{\frac{d^2}{4(-ib+ic(v-2s))} - ie + gi(v-2s)} (-ib + ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id + 2(-ib + ic(v-2s))z)^{j+1} \right. \\ & \left. \left( -\frac{(-id + 2(-ib + ic(v-2s))z)^2}{-ib + ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + 2(-ib + ic(v-2s))z)^2}{4(-ib + ic(v-2s))}\right) + \right. \\ & \left. e^{\frac{d^2}{4(ib+ic(v-2s))} + ie + gi(v-2s)} (ib + ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2(ib + ic(v-2s))z)^{j+1} \right. \\ & \left. \left( -\frac{(id + 2(ib + ic(v-2s))z)^2}{ib + ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + 2(ib + ic(v-2s))z)^2}{4(ib + ic(v-2s))}\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1177.01

$$\int z^n \sin(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + g) dz =$$

$$\begin{aligned} & (-1)^n 2^{-2n-v-2} i \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( e^{i e - \frac{i b^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} (i b + 2 i d \sqrt{z})^{h+j} \right. \\ & \left. \left( \frac{i(i b + 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( b i (i b + 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(i b + 2 i d \sqrt{z})^2}{4d} \right) \right. \right. \\ & \left. \left. 2 \sqrt{\frac{i(i b + 2 i d \sqrt{z})^2}{d}} d i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(i b + 2 i d \sqrt{z})^2}{4d} \right) \right) \right) - \\ & e^{\frac{i b^2}{4d} - i e} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2n} (-i b - 2 i d \sqrt{z})^{h+j} \left( -\frac{i(-i b - 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \\ & \binom{j}{h} \binom{n}{j} \left( -i b (-i b - 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-i b - 2 i d \sqrt{z})^2}{4d} \right) \right. \\ & \left. 2 i d \sqrt{-\frac{i(-i b - 2 i d \sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-i b - 2 i d \sqrt{z})^2}{4d} \right) \right) \right) d^{-2n-2} + \\ & 2^{-2n-v-2} (i d)^{-2n-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{\frac{i(i b + i c(2k-v))^2}{4d} + i e + g i(2k-v)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b + i c(2k-v))^{-h-j+2n} \right. \\ & \left. (i b + i c(2k-v) + 2 i d \sqrt{z})^{h+j} \left( \frac{i(i b + i c(2k-v) + 2 i d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\ & \left. \left( (i b + i c(2k-v)) (i b + i c(2k-v) + 2 i d \sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(i b + i c(2k-v) + 2 i d \sqrt{z})^2}{4d} \right) \right. \right. \end{aligned}$$



$$\begin{aligned}
 & 2\sqrt{\frac{i(i b+i c(2 k-v)+2 i d \sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(i b+i c(2 k-v)+2 i d \sqrt{z})^2}{4 d}\right) \Bigg) + \\
 & e^{\frac{i(i b+i c(v-2 k))^2}{4 d}+i e+g i(v-2 k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b+i c(v-2 k))^{-h-j+2 n}(i b+i c(v-2 k)+2 i d \sqrt{z})^{h+j} \\
 & \left(\frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left(i b+i c(v-2 k)(i b+i c(v-2 k)+2 i d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{4 d}\right)\right) + \\
 & 2\sqrt{\frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{d}} d i \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(i b+i c(v-2 k)+2 i d \sqrt{z})^2}{4 d}\right) \Bigg) + \\
 & (-1)^{v+1} e^{-\frac{i(-i b+i c(2 k-v))^2}{4 d}-i e+g i(2 k-v)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b+i c(2 k-v))^{-h-j+2 n}(-i b+i c(2 k-v)-2 i d \sqrt{z})^{h+j} \\
 & \left(-\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left(-i b+i c(2 k-v)\right) \\
 & (-i b+i c(2 k-v)-2 i d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{4 d}\right) - \\
 & 2 i d \sqrt{-\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-i b+i c(2 k-v)-2 i d \sqrt{z})^2}{4 d}\right) \Bigg) - \\
 & e^{-\frac{i(-i b+i c(v-2 k))^2}{4 d}-i e+g i(v-2 k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b+i c(v-2 k))^{-h-j+2 n}(-i b+i c(v-2 k)-2 i d \sqrt{z})^{h+j} \\
 & \left(-\frac{i(-i b+i c(v-2 k)-2 i d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}
 \end{aligned}$$

$$\left( (-ib + ic(v - 2k))(-ib + ic(v - 2k) - 2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h + j + 1), \right. \right. \\ \left. \left. -\frac{i(-ib + ic(v - 2k) - 2id\sqrt{z})^2}{4d} \right) - 2id\sqrt{-\frac{i(-ib + ic(v - 2k) - 2id\sqrt{z})^2}{d}} \Gamma\left( \right. \right. \\ \left. \left. \frac{1}{2}(h + j + 2), -\frac{i(-ib + ic(v - 2k) - 2id\sqrt{z})^2}{4d} \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving  $z^n \sin(dz) \sin^v(cz + fz)$

01.06.21.1178.01

$$\int z^n \sin(dz) \sin^v(cz^2 + fz) dz = i(-1)^n 2^{-v-1} \left(\frac{v}{2}\right) ((-id)^{-n-1} \Gamma(n+1, idz) - (id)^{-n-1} \Gamma(n+1, -idz)) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{1}{2}i\pi(v+1) - \frac{i(-id-if(v-2s))^2}{4c(v-2s)}} \left( \sum_{j=0}^n 2^{j-n} (id + if(v-2s))^{n-j} \right. \right.$$

$$\left. (-id - if(v-2s) - 2ic(v-2s)z)^{j+1} \left( -\frac{i(-id - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) (-ic(v-2s))^{-n-1} +$$

$$e^{\frac{1}{2}i\pi(v-1) - \frac{i(id-if(v-2s))^2}{4c(v-2s)}} \left( \sum_{j=0}^n 2^{j-n} (-id + if(v-2s))^{n-j} (id - if(v-2s) - 2ic(v-2s)z)^{j+1} \right.$$

$$\left. \left( -\frac{i(id - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(id - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right)$$

$$(-ic(v-2s))^{-n-1} + e^{\frac{i(-id+if(v-2s))^2}{4c(v-2s)} + \frac{1}{2}i\pi(1-v)} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id - if(v-2s))^{n-j}$$

$$(-id + if(v-2s) + 2ic(v-2s)z)^{j+1} \left( \frac{i(-id + if(v-2s) + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}$$

$$\Gamma\left(\frac{j+1}{2}, \frac{i(-id + if(v-2s) + 2ic(v-2s)z)^2}{4c(v-2s)}\right) + e^{\frac{i(id+if(v-2s))^2}{4c(v-2s)} - \frac{1}{2}i\pi(v+1)} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n}$$

$$(-id - if(v-2s))^{n-j} (id + if(v-2s) + 2ic(v-2s)z)^{j+1} \left( \frac{i(id + if(v-2s) + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + if(v-2s) + 2ic(v-2s)z)^2}{4c(v-2s)}\right) \Bigg) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1179.01

$$\int z^n \sin(dz) \sin^v(\sqrt{z}c + fz) dz =$$

$$(-1)^n 2^{-v-1} i \left(\frac{v}{2}\right) ((-id)^{-n-1} \Gamma(n+1, idz) - (id)^{-n-1} \Gamma(n+1, -idz)) (1 - v \bmod 2) + 2^{-2n-v-2}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2(v-2s)^2}{4(-id+if(v-2s))} + \frac{1}{2}i\pi(1-v)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ci(v-2s) + 2(-id + if(v-2s))\sqrt{z})^{h+j} \right. \right.$$

$$\begin{aligned}
 & \left( -\frac{(ci(v-2s) + 2(-id + if(v-2s))\sqrt{z})^2}{-id + if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(ci(v-2s) + \right. \\
 & \left. 2(-id + if(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ci(v-2s) + 2(-id + if(v-2s))\sqrt{z})^2}{4(-id + if(v-2s))}\right) + 2 \right. \\
 & \left. (-id + if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ci(v-2s) + 2(-id + if(v-2s))\sqrt{z})^2}{4(-id + if(v-2s))}\right) \right. \\
 & \left. \sqrt{-\frac{(ci(v-2s) + 2(-id + if(v-2s))\sqrt{z})^2}{-id + if(v-2s)}} \right) \left. \right) (-id + if(v-2s))^{-2(n+1)} + \\
 & e^{\frac{c^2(v-2s)^2}{4(id+if(v-2s))} - \frac{1}{2}i\pi(v+1)} (id + if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} \\
 & (ci(v-2s) + 2(id + if(v-2s))\sqrt{z})^{h+j} \left( -\frac{(ci(v-2s) + 2(id + if(v-2s))\sqrt{z})^2}{id + if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(ci(v-2s) + 2(id + if(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(ci(v-2s) + 2(id + if(v-2s))\sqrt{z})^2}{4(id + if(v-2s))}\right) + 2 \sqrt{-\frac{(ci(v-2s) + 2(id + if(v-2s))\sqrt{z})^2}{id + if(v-2s)}} \right. \\
 & \left. (id + if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ci(v-2s) + 2(id + if(v-2s))\sqrt{z})^2}{4(id + if(v-2s))}\right) \right) \left. \right) + \\
 & e^{\frac{c^2(v-2s)^2}{4(-id-if(v-2s))} + \frac{1}{2}i\pi(v+1)} (-id - if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} \\
 & (2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^{h+j} \left( -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)}
 \end{aligned}$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( 2(-id - if(v-2s)) \sqrt{-\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \quad \left. \left. -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))} \right) - ic(v-2s)(2(-id - if(v-2s))\sqrt{z} - \right. \\
 & \quad \left. ic(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))} \right) \right) + \\
 & e^{\frac{c^2(v-2s)^2}{4(id - if(v-2s))} + \frac{1}{2}i\pi(v-1)} (id - if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} \\
 & (2(id - if(v-2s))\sqrt{z} - ic(v-2s))^{h+j} \left( -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(id - if(v-2s)) \sqrt{\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \quad \left. \left. -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))} \right) - ic(v-2s)(2(id - if(v-2s))\sqrt{z} - ic(v-2s)) \right. \\
 & \quad \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))} \right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin(dz + e) \sin^v(cz' + fz)$

01.06.21.1180.01

$$\int z^n \sin(dz + e) \sin^v(cz^2 + fz) dz =$$

$$\begin{aligned} & i(-1)^n 2^{-v-1} \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} e^{-ie} \Gamma(n+1, idz) - (id)^{-n-1} e^{ie} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) - \\ & 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-id-if(v-2s))^2}{4c(v-2s)} - ie + \frac{1}{2}i\pi(v+1)} \left( \sum_{j=0}^n 2^{j-n} (id + if(v-2s))^{n-j} \right. \right. \\ & \quad \left. \left. (-id - if(v-2s) - 2ic(v-2s)z)^{j+1} \left( -\frac{i(-id - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \right. \\ & \quad \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) \right) (-ic(v-2s))^{-n-1} + \\ & e^{-\frac{i(id-if(v-2s))^2}{4c(v-2s)} + ie + \frac{1}{2}i\pi(v-1)} \left( \sum_{j=0}^n 2^{j-n} (-id + if(v-2s))^{n-j} (id - if(v-2s) - 2ic(v-2s)z)^{j+1} \right. \\ & \quad \left. \left( -\frac{i(id - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(id - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) \\ & (-ic(v-2s))^{-n-1} + e^{\frac{i(-id+if(v-2s))^2}{4c(v-2s)} - ie + \frac{1}{2}i\pi(1-v)} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id - if(v-2s))^{n-j} \\ & (-id + if(v-2s) + 2ic(v-2s)z)^{j+1} \left( \frac{i(-id + if(v-2s) + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\ & \Gamma\left(\frac{j+1}{2}, \frac{i(-id + if(v-2s) + 2ic(v-2s)z)^2}{4c(v-2s)}\right) + e^{\frac{i(id+if(v-2s))^2}{4c(v-2s)} + ie - \frac{1}{2}i\pi(v+1)} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} \\ & (-id - if(v-2s))^{n-j} (id + if(v-2s) + 2ic(v-2s)z)^{j+1} \left( \frac{i(id + if(v-2s) + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\ & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + if(v-2s) + 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1181.01

$$\int z^n \sin(dz + e) \sin^v(\sqrt{z}c + fz) dz =$$

$$(-1)^n 2^{-v-1} \binom{v}{\frac{v}{2}} \left( e^{-ie + \frac{i\pi}{2}} \Gamma(n+1, idz) (-id)^{-n-1} + (id)^{-n-1} e^{ie - \frac{i\pi}{2}} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) + 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\begin{aligned}
 & \left( \frac{c^2(v-2s)^2}{e^{4(-id+if(v-2s))}} - i e + \frac{1}{2} i \pi(1-v) \right) \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ci(v-2s) + 2(-id+if(v-2s))\sqrt{z})^{h+j} \right. \\
 & \quad \left. \left( -\frac{(ci(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{-id+if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(ci(v-2s) + \right. \right. \\
 & \quad \left. \left. 2(-id+if(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ci(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{4(-id+if(v-2s))}\right) + 2 \right. \right. \\
 & \quad \left. \left. (-id+if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ci(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{4(-id+if(v-2s))}\right) \right) \right. \\
 & \quad \left. \left. \sqrt{-\frac{(ci(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{-id+if(v-2s)}} \right) \right) (-id+if(v-2s))^{-2(n+1)} + \\
 & \quad \frac{c^2(v-2s)^2}{e^{4(id+if(v-2s))}} + i e - \frac{1}{2} i \pi(v+1) (id+if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} \\
 & \quad (ci(v-2s) + 2(id+if(v-2s))\sqrt{z})^{h+j} \left( -\frac{(ci(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{id+if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \quad \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(ci(v-2s) + 2(id+if(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \quad \left. \left. -\frac{(ci(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{4(id+if(v-2s))}\right) + 2 \sqrt{-\frac{(ci(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{id+if(v-2s)}} \right. \\
 & \quad \left. \left. (id+if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ci(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{4(id+if(v-2s))}\right) \right) \right) + \\
 & \quad \frac{c^2(v-2s)^2}{e^{4(-id-if(v-2s))}} - i e + \frac{1}{2} i \pi(v+1) (-id-if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n}
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2(-id - if(v-2s))\sqrt{z} - ic(v-2s) \right)^{h+j} \left( -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(-id - if(v-2s))\sqrt{-\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))} - ic(v-2s)(2(-id - if(v-2s))\sqrt{z} - \right. \right. \\
 & \left. \left. ic(v-2s))\Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))}\right) \right) \right) + \\
 & e^{\frac{c^2(v-2s)^2}{4(id-if(v-2s))} + ie + \frac{1}{2}i\pi(v-1)} (id - if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} \\
 & \left( 2(id - if(v-2s))\sqrt{z} - ic(v-2s) \right)^{h+j} \left( -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(id - if(v-2s))\sqrt{-\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))} - ic(v-2s)(2(id - if(v-2s))\sqrt{z} - ic(v-2s)) \right) \right) \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin(bz^r) \sin^v(cz^r + fz)$



01.06.21.1182.01

$$\int z^n \sin(bz^2) \sin^v(cz^2 + fz) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{b+2cs-cv} - 2\pi(1-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} \right. \right.$$

$$\left. \left. (fi(v-2s) + 2(-ib+ic(v-2s))z)^{j+1} \left( -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))}\right) \right) (-ib+ic(v-2s))^{-n-1} + \right.$$

$$\left. e^{\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{-b+2cs-cv} - 2\pi(v+1) \right)} (ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s) + 2(ib+ic(v-2s))z)^{j+1} \right.$$

$$\left. \left( -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))}\right) \right) +$$

$$e^{-\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{-b+2cs-cv} - 2\pi(v+1) \right)} (-ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j}$$

$$(2(-ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{-ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}$$

$$\Gamma\left(\frac{j+1}{2}, -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{4(-ib-ic(v-2s))}\right) + e^{\frac{1}{4}i \left( 2\pi(v-1) - \frac{f^2(v-2s)^2}{b+2cs-cv} \right)} (ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n}$$

$$(if(v-2s))^{n-j} (2(ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{4(ib-ic(v-2s))}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1183.01

$$\int z^n \sin(b\sqrt{z}) \sin^v(\sqrt{z}c + fz) dz =$$

$$(-1)^{n+1} 2^{-v} i \binom{v}{\frac{v}{2}} \left( \Gamma(2(n+1), -ib\sqrt{z}) - \Gamma(2(n+1), ib\sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} + 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\begin{aligned}
 & \left( e^{\frac{1}{2}i\pi(v+1) - \frac{i(-ib-ic(v-2s))^2}{4f(v-2s)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib-ic(v-2s))^{-h-j+2n} (-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left( -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (-ib-ic(v-2s))(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z}) \right) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) - 2 \right. \\
 & \left. if(v-2s) \sqrt{-\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \right) \right) (-if(v-2s))^{-2(n+1)} + \\
 & e^{\frac{1}{2}i\pi(v-1) - \frac{i(ib-ic(v-2s))^2}{4f(v-2s)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib-ic(v-2s))^{-h-j+2n} (ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (ib-ic(v-2s))(ib-ic(v-2s) - \right. \right. \\
 & \left. \left. 2if(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) - 2 \right. \right. \\
 & \left. \left. if(v-2s) \sqrt{-\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right.
 \end{aligned}$$



### Involving $z^n \sin(bz^r + e) \sin^v(cz^r + fz)$

01.06.21.1184.01

$$\int z^n \sin(bz^2 + e) \sin^v(cz^2 + fz) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( e^{ie} (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - e^{-ie} (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b+2cs-cv} + 4e-2\pi(1-v) \right)} \right) \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} \right.$$

$$\left. (fi(v-2s) + 2(-ib+ic(v-2s))z)^{j+1} \left( -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right)$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))}\right) \left( -ib+ic(v-2s) \right)^{-n-1} +$$

$$e^{\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{-b+2cs-cv} + 4e-2\pi(v+1) \right)} (ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s) + 2(ib+ic(v-2s))z)^{j+1}$$

$$\left( -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))}\right) +$$

$$e^{-\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{-b+2cs-cv} + 4e-2\pi(v+1) \right)} (-ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j}$$

$$(2(-ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{-ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{4(-ib-ic(v-2s))}\right) +$$

$$e^{\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b+2cs-cv} + 4e+2\pi(v-1) \right)} (ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j}$$

$$(2(ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{4(ib-ic(v-2s))}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

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$$\begin{aligned}
 & \int z^n \sin(\sqrt{z} b + e) \sin^v(\sqrt{z} c + f z) dz = \\
 & (-1)^n 2^{-v} i \left( \frac{v}{2} \right) \left( e^{-ie} \Gamma(2(n+1), ib\sqrt{z}) - e^{ie} \Gamma(2(n+1), -ib\sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} + \\
 & 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-ib-ic(v-2s))^2}{4f(v-2s)} - ie + \frac{1}{2}i\pi(v+1)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib-ic(v-2s))^{-h-j+2n} \right. \right. \\
 & \left. \left. (-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right. \right. \\
 & \left. \left. \binom{j}{h} \binom{n}{j} \left( (-ib-ic(v-2s))(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z}) \right) \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) - 2 \right. \right. \\
 & \left. \left. if(v-2s) \sqrt{-\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) \right) \right) \left( -if(v-2s) \right)^{-2(n+1)} + \\
 & e^{-\frac{i(ib-ic(v-2s))^2}{4f(v-2s)} + ie + \frac{1}{2}i\pi(v-1)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib-ic(v-2s))^{-h-j+2n} (ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (ib-ic(v-2s))(ib-ic(v-2s) - \right. \right. \\
 & \left. \left. 2if(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) - 2 \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & i f(v-2s) \sqrt{-\frac{i(i b-i c(v-2 s)-2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left. -\frac{i(i b-i c(v-2 s)-2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)}\right) \Bigg) (-i f(v-2 s))^{-2(n+1)} + \\
 & e^{\frac{i(-i b+i c(v-2 s))^2}{4 f(v-2 s)}-i e+\frac{1}{2} i \pi(1-v)} (i f(v-2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b+i c(v-2 s))^{-h-j+2 n} \\
 & (-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^{h+j} \left(\frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (-i b+i c(v-2 s))(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1),\right. \right. \\
 & \left. \left. \frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)}\right) + \right. \\
 & \left. 2 f i(v-2 s) \sqrt{\frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \right. \\
 & \left. \left. \frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)}\right) \right) + e^{\frac{i(i b+i c(v-2 s))^2}{4 f(v-2 s)}+i e-\frac{1}{2} i \pi(v+1)} (i f(v-2 s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b+i c(v-2 s))^{-h-j+2 n} (i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^{h+j} \\
 & \left(\frac{i(i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (i b+i c(v-2 s))
 \end{aligned}$$

$$\begin{aligned} & (ib + ic(v-2s) + 2if(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib + ic(v-2s) + 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + \\ & 2fi(v-2s) \sqrt{\frac{i(ib + ic(v-2s) + 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \\ & \left. \frac{i(ib + ic(v-2s) + 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+ \end{aligned}$$

### Involving $z^n \sin(bz^r + dz) \sin^v(cz^r + fz)$

01.06.21.1186.01

$$\int z^n \sin(bz^2 + dz) \sin^v(cz^2 + fz) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\begin{aligned} & \left( (ib)^{-n-1} e^{-\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id + 2ibz)^{j+1} \left(\frac{i(id + 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + 2ibz)^2}{4b}\right) - \right. \\ & \left. (-ib)^{-n-1} e^{\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id - 2ibz)^{j+1} \left(-\frac{i(-id - 2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - 2ibz)^2}{4b}\right) \right) - \\ & i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{(-id+if(2s-v))^2}{4(-ib+ic(2s-v))}} \left( \sum_{j=0}^n 2^{j-n} (id - if(2s-v))^{n-j} \right. \right. \\ & \left. \left. (-id + if(2s-v) + 2(-ib + ic(2s-v))z)^{j+1} \left( -\frac{(-id + if(2s-v) + 2(-ib + ic(2s-v))z)^2}{-ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \right) \right. \\ & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + if(2s-v) + 2(-ib + ic(2s-v))z)^2}{4(-ib + ic(2s-v))}\right) \right) (-ib + ic(2s-v))^{-n-1} + \\ & (-1)^v e^{-\frac{(id+if(2s-v))^2}{4(ib+ic(2s-v))}} (ib + ic(2s-v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id - if(2s-v))^{n-j} \\ & \left. (id + if(2s-v) + 2(ib + ic(2s-v))z)^{j+1} \left( -\frac{(id + if(2s-v) + 2(ib + ic(2s-v))z)^2}{ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \right) \\ & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id + if(2s-v) + 2(ib + ic(2s-v))z)^2}{4(ib + ic(2s-v))}\right) - e^{-\frac{(-id+if(v-2s))^2}{4(-ib+ic(v-2s))}} \end{aligned}$$

$$\begin{aligned}
 & (-ib + ic(v - 2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id - if(v - 2s))^{n-j} (-id + if(v - 2s) + 2(-ib + ic(v - 2s))z)^{j+1} \\
 & \left( -\frac{(-id + if(v - 2s) + 2(-ib + ic(v - 2s))z)^2}{-ib + ic(v - 2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(-id + if(v - 2s) + 2(-ib + ic(v - 2s))z)^2}{4(-ib + ic(v - 2s))}\right) + \\
 & e^{-\frac{(id+if(v-2s))^2}{4(ib+ic(v-2s))}} (ib + ic(v - 2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id - if(v - 2s))^{n-j} (id + if(v - 2s) + 2(ib + ic(v - 2s))z)^{j+1} \\
 & \left( -\frac{(id + if(v - 2s) + 2(ib + ic(v - 2s))z)^2}{ib + ic(v - 2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(id + if(v - 2s) + 2(ib + ic(v - 2s))z)^2}{4(ib + ic(v - 2s))}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1187.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin^v(\sqrt{z} c + fz) dz =$$

$$\begin{aligned}
 & i^{-v-1} 2^{-2n-v-2} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{-\frac{(-ib+ic(2k-v))^2}{4(-id+if(2k-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib + ic(2k - v))^{-h-j+2n} (-ib + ic(2k - v) + \right. \right. \\
 & \left. \left. 2(-id + if(2k - v))\sqrt{z} \right)^{h+j} \left( -\frac{(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z})^2}{-id + if(2k - v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( (-ib + ic(2k - v))(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z}) \right) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z})^2}{4(-id + if(2k - v))}\right) + 2 \right. \\
 & \left. (-id + if(2k - v)) \Gamma\left(\frac{1}{2}(h + j + 2), -\frac{(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z})^2}{4(-id + if(2k - v))}\right) \right. \\
 & \left. \left. \sqrt{-\frac{(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z})^2}{-id + if(2k - v)}} \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & (-id + if(2k - v))^{-2n-2} + (-1)^v e^{-\frac{(ib+ic(2k-v))^2}{4(id+if(2k-v))}} (id + if(2k - v))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib + ic(2k - v))^{-h-j+2n} (ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^{h+j} \\
 & \left( \frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{id + if(2k - v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib + ic(2k - v))(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h + j + 1), -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{4(id + if(2k - v))} \right) + \right. \\
 & \left. 2(id + if(2k - v)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{4(id + if(2k - v))} \right) \right) \\
 & \left. \sqrt{\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{id + if(2k - v)}} \right) - e^{-\frac{(ib+ic(v-2k))^2}{4(-id+if(v-2k))}} (-id + if(v - 2k))^{-2n-2}
 \end{aligned}$$

$$\begin{aligned}
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib + ic(v - 2k))^{-h-j+2n} (-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^{h+j} \\
 & \left( \frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{-id + if(v - 2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (-ib + ic(v - 2k))(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h + j + 1), -\frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{4(-id + if(v - 2k))} \right) + \right. \\
 & \left. 2(-id + if(v - 2k)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{4(-id + if(v - 2k))} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{-\frac{(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)}} \right\} + e^{-\frac{(ib+ic(v-2k))^2}{4(id+if(v-2k))}} (id+if(v-2k))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2k))^{-h-j+2n} (ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^{h+j} \\
 & \left( \frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib+ic(v-2k))(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) \right. \\
 & \left. + 2(id+if(v-2k)) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) \right) \\
 & \left. \sqrt{-\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)}} \right) \\
 & i 2^{-2n-v-2} (id)^{-2n-2} \left( \frac{v}{2} \right) (1-v \bmod 2) \left( e^{-\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2id\sqrt{z})^{h+j} \right. \\
 & \left. \left( \frac{i(ib+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) \right. \right. \\
 & \left. \left. + 2 \sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) \right) \right)
 \end{aligned}$$

$$e^{\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib-2id\sqrt{z})^{h+j} \left( -\frac{i(-ib-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h}$$

$$\binom{n}{j} \left( -ib(-ib-2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) - \right.$$

$$\left. 2id \sqrt{-\frac{i(-ib-2id\sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib-2id\sqrt{z})^2}{4d} \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin(bz^r + dz + e) \sin^v(cz^r + fz)$

01.06.21.1188.01

$$\int z^n \sin(bz^2 + dz + e) \sin^v(cz^2 + fz) dz = i 2^{-v-2} \left( \frac{v}{2} \right) (1 - v \bmod 2)$$

$$\left( (ib)^{-n-1} e^{\frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id+2ibz)^{j+1} \left( \frac{i(id+2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \frac{i(id+2ibz)^2}{4b} \right) - \right.$$

$$\left. (-ib)^{-n-1} e^{\frac{id^2}{4b} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id-2ibz)^{j+1} \left( -\frac{i(-id-2ibz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{i(-id-2ibz)^2}{4b} \right) \right) -$$

$$i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{(-id+if(2s-v))^2}{4(-ib+ic(2s-v))} - ie} \left( \sum_{j=0}^n 2^{j-n} (id-if(2s-v))^{n-j} \right. \right.$$

$$\left. \left. (-id+if(2s-v) + 2(-ib+ic(2s-v))z \right)^{j+1} \left( -\frac{(-id+if(2s-v) + 2(-ib+ic(2s-v))z)^2}{-ib+ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \right)$$

$$\binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{(-id+if(2s-v) + 2(-ib+ic(2s-v))z)^2}{4(-ib+ic(2s-v))} \right) \left( (-ib+ic(2s-v))^{-n-1} + \right.$$

$$\left. (-1)^v e^{\frac{(id+if(2s-v))^2}{4(ib+ic(2s-v))}} (ib+ic(2s-v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id-if(2s-v))^{n-j} \right.$$

$$\left. (id+if(2s-v) + 2(ib+ic(2s-v))z \right)^{j+1} \left( -\frac{(id+if(2s-v) + 2(ib+ic(2s-v))z)^2}{ib+ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \right)$$

$$\binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{(id+if(2s-v) + 2(ib+ic(2s-v))z)^2}{4(ib+ic(2s-v))} \right) -$$

$$\begin{aligned}
 & e^{-\frac{(-id+if(v-2s))^2}{4(-ib+ic(v-2s))}} (-ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id-if(v-2s))^{n-j} \\
 & (-id+if(v-2s)+2(-ib+ic(v-2s))z)^{j+1} \left( -\frac{(-id+if(v-2s)+2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id+if(v-2s)+2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))}\right) + \\
 & e^{i\frac{(id+if(v-2s))^2}{4(ib+ic(v-2s))}} (ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id-if(v-2s))^{n-j} (id+if(v-2s)+2(ib+ic(v-2s))z)^{j+1} \\
 & \left( -\frac{(id+if(v-2s)+2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(id+if(v-2s)+2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))}\right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1189.01

$$\int z^n \sin(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + fz) dz =$$

$$\begin{aligned}
 & i^{-v-1} 2^{-2n-v-2} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{-\frac{(-ib+ic(2k-v))^2}{4(-id+if(2k-v))}} i e \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(2k-v))^{-h-j+2n} (-ib+ic(2k-v) + \right. \right. \\
 & \left. \left. 2(-id+if(2k-v))\sqrt{z}\right)^{h+j} \left( -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{-id+if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( (-ib+ic(2k-v))(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) + 2 \right. \right. \\
 & \left. \left. (-id+if(2k-v)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) \right. \right. \\
 & \left. \left. \sqrt{-\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{-id+if(2k-v)}} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & (-id + if(2k - v))^{-2n-2} + (-1)^v e^{i e^{-\frac{(ib+ic(2k-v))^2}{4(id+if(2k-v))}}} (id + if(2k - v))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib + ic(2k - v))^{-h-j+2n} (ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^{h+j} \\
 & \left( \frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{id + if(2k - v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib + ic(2k - v))(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h + j + 1), -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{4(id + if(2k - v))} \right) + \right. \\
 & \left. 2(id + if(2k - v)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{4(id + if(2k - v))} \right) \right) \\
 & \left. \sqrt{\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{id + if(2k - v)}} - e^{-\frac{(ib+ic(v-2k))^2}{4(-id+if(v-2k))}} -ie (-id + if(v - 2k))^{-2n-2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib + ic(v - 2k))^{-h-j+2n} (-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^{h+j} \\
 & \left( \frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{-id + if(v - 2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (-ib + ic(v - 2k))(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h + j + 1), -\frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{4(-id + if(v - 2k))} \right) + \right. \\
 & \left. 2(-id + if(v - 2k)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{4(-id + if(v - 2k))} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{-\frac{(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)}} \right) + e^{\frac{ie^{-(ib+ic(v-2k))^2}}{4(id+if(v-2k))}} (id+if(v-2k))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2k))^{-h-j+2n} (ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^{h+j} \\
 & \left( \frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib+ic(v-2k))(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) + \right. \\
 & \left. 2(id+if(v-2k)) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) \right) \\
 & \left. \sqrt{-\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)}} \right) - \\
 & i 2^{-2n-v-2} (id)^{-2n-2} \left( \frac{v}{2} \right) (1-v \bmod 2) \left( e^{ie^{-\frac{ib^2}{4d}}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2id\sqrt{z})^{h+j} \right. \\
 & \left. \left( \frac{i(ib+2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) + \right. \right. \\
 & \left. \left. 2\sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d} \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & e^{\frac{ib^2}{4d} - ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib - 2id\sqrt{z})^{h+j} \left( -\frac{i(-ib - 2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( -ib(-ib - 2id\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib - 2id\sqrt{z})^2}{4d} \right) - \right. \\
 & \left. 2id \sqrt{-\frac{i(-ib - 2id\sqrt{z})^2}{d}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib - 2id\sqrt{z})^2}{4d} \right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin(dz) \sin^v(cz^r + fz + g)$

01.06.21.1190.01

$$\int z^n \sin(dz) \sin^v(cz^2 + fcz + g) dz = i(-1)^n 2^{-v-1} \left(\frac{v}{2}\right) \left( (-id)^{-n-1} \Gamma(n+1, idz) - (id)^{-n-1} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-id-if(v-2s))^2}{4c(v-2s)} + \frac{1}{2}i\pi(v+1)-ig(v-2s)} \left( \sum_{j=0}^n 2^{j-n} (id+if(v-2s))^{n-j} \right. \right.$$

$$\left. \left. (-id-if(v-2s)-2ic(v-2s)z)^{j+1} \left( -\frac{i(-id-if(v-2s)-2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id-if(v-2s)-2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) \right) (-ic(v-2s))^{-n-1} +$$

$$e^{-\frac{i(id-if(v-2s))^2}{4c(v-2s)} + \frac{1}{2}i\pi(v-1)-ig(v-2s)} \left( \sum_{j=0}^n 2^{j-n} (-id+if(v-2s))^{n-j} (id-if(v-2s)-2ic(v-2s)z)^{j+1} \right.$$

$$\left. \left. \left( -\frac{i(id-if(v-2s)-2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(id-if(v-2s)-2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) \right)$$

$$(-ic(v-2s))^{-n-1} + e^{\frac{i(-id+if(v-2s))^2}{4c(v-2s)} + \frac{1}{2}i\pi(1-v)+g(v-2s)} (ic(v-2s))^{-n-1}$$

$$\sum_{j=0}^n 2^{j-n} (id-if(v-2s))^{n-j} (-id+if(v-2s)+2ic(v-2s)z)^{j+1}$$

$$\left( \frac{i(-id+if(v-2s)+2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-id+if(v-2s)+2ic(v-2s)z)^2}{4c(v-2s)}\right) +$$

$$e^{\frac{i(id+if(v-2s))^2}{4c(v-2s)} - \frac{1}{2}i\pi(v+1)+g(v-2s)} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id-if(v-2s))^{n-j}$$

$$(id+if(v-2s)+2ic(v-2s)z)^{j+1} \left( \frac{i(id+if(v-2s)+2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id+if(v-2s)+2ic(v-2s)z)^2}{4c(v-2s)}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1191.01

$$\int z^n \sin(dz) \sin^v(\sqrt{z} cz + fcz + g) dz =$$

$$(-1)^n 2^{-v-1} i \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} \Gamma(n+1, idz) - (id)^{-n-1} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) + 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$



$$\begin{aligned}
 & \left( e^{\frac{c^2(v-2s)^2}{4(-id+if(v-2s))} + g i(v-2s) + \frac{1}{2} i \pi(1-v)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} (c i(v-2s) + 2(-id+if(v-2s)) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(c i(v-2s) + 2(-id+if(v-2s)) \sqrt{z})^2}{-id+if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2s) (c i(v-2s) + \right. \right. \right. \\
 & \left. \left. \left. 2(-id+if(v-2s)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(c i(v-2s) + 2(-id+if(v-2s)) \sqrt{z})^2}{4(-id+if(v-2s))}\right) \right) + 2 \right. \right. \\
 & \left. \left. (-id+if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(c i(v-2s) + 2(-id+if(v-2s)) \sqrt{z})^2}{4(-id+if(v-2s))}\right) \right) \right. \\
 & \left. \left. \sqrt{-\frac{(c i(v-2s) + 2(-id+if(v-2s)) \sqrt{z})^2}{-id+if(v-2s)}} \right) \right) (-id+if(v-2s))^{-2(n+1)} + \\
 & e^{\frac{c^2(v-2s)^2}{4(id+if(v-2s))} + g i(v-2s) - \frac{1}{2} i \pi(v+1)} (id+if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} \\
 & (c i(v-2s) + 2(id+if(v-2s)) \sqrt{z})^{h+j} \left( -\frac{(c i(v-2s) + 2(id+if(v-2s)) \sqrt{z})^2}{id+if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c i(v-2s) (c i(v-2s) + 2(id+if(v-2s)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(c i(v-2s) + 2(id+if(v-2s)) \sqrt{z})^2}{4(id+if(v-2s))}\right) + 2 \sqrt{-\frac{(c i(v-2s) + 2(id+if(v-2s)) \sqrt{z})^2}{id+if(v-2s)}} \right. \\
 & \left. \left. (id+if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(c i(v-2s) + 2(id+if(v-2s)) \sqrt{z})^2}{4(id+if(v-2s))}\right) \right) \right) + \\
 & e^{\frac{c^2(v-2s)^2}{4(-id-if(v-2s))} - i g(v-2s) + \frac{1}{2} i \pi(v+1)} (-id-if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n}
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2(-id - if(v-2s))\sqrt{z} - ic(v-2s) \right)^{h+j} \left( -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(-id - if(v-2s))\sqrt{-\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))} - ic(v-2s)(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))\right) \right) + \\
 & \left. ic(v-2s) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))}\right) \right) \\
 & e^{\frac{c^2(v-2s)^2}{4(id-if(v-2s))} - ig(v-2s) + \frac{1}{2}i\pi(v-1)} (id - if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} \\
 & \left( 2(id - if(v-2s))\sqrt{z} - ic(v-2s) \right)^{h+j} \left( -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(id - if(v-2s))\sqrt{-\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))} - ic(v-2s)(2(id - if(v-2s))\sqrt{z} - ic(v-2s)) \right) \right) \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))}\right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin(dz + e) \sin^v(cz' + fz + g)$

01.06.21.1192.01

$$\begin{aligned}
 & \int z^n \sin(dz + e) \sin^v(cz^2 + fz + g) dz = \\
 & (-1)^n i 2^{-v-1} \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} e^{-ie} \Gamma(n+1, idz) - (id)^{-n-1} e^{ie} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) - \\
 & 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-id-if(v-2s))^2}{4c(v-2s)} - ie + \frac{1}{2}i\pi(v+1) - ig(v-2s)} \left( \sum_{j=0}^n 2^{j-n} (id + if(v-2s))^{n-j} \right. \right. \\
 & \quad \left. \left. (-id - if(v-2s) - 2ic(v-2s)z)^{j+1} \left( -\frac{i(-id - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \right. \\
 & \quad \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) \right) (-ic(v-2s))^{-n-1} + \\
 & e^{-\frac{i(id-if(v-2s))^2}{4c(v-2s)} + ie + \frac{1}{2}i\pi(v-1) - ig(v-2s)} \left( \sum_{j=0}^n 2^{j-n} (-id + if(v-2s))^{n-j} (id - if(v-2s) - 2ic(v-2s)z)^{j+1} \right. \\
 & \quad \left. \left( -\frac{i(id - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(id - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) \\
 & (-ic(v-2s))^{-n-1} + e^{\frac{i(-id+if(v-2s))^2}{4c(v-2s)} - ie + \frac{1}{2}i\pi(1-v) + g(v-2s)} (ic(v-2s))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (id - if(v-2s))^{n-j} (-id + if(v-2s) + 2ic(v-2s)z)^{j+1} \\
 & \quad \left( \frac{i(-id + if(v-2s) + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-id + if(v-2s) + 2ic(v-2s)z)^2}{4c(v-2s)}\right) + \\
 & e^{\frac{i(id+if(v-2s))^2}{4c(v-2s)} + ie - \frac{1}{2}i\pi(v+1) + g(v-2s)} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id - if(v-2s))^{n-j} \\
 & \quad (id + if(v-2s) + 2ic(v-2s)z)^{j+1} \left( \frac{i(id + if(v-2s) + 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id + if(v-2s) + 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1193.01

$$\begin{aligned}
 & \int z^n \sin(dz + e) \sin^v(\sqrt{z}c + fz + g) dz = \\
 & (-1)^n 2^{-v-1} i \binom{v}{\frac{v}{2}} \left( (-id)^{-n-1} e^{-ie} \Gamma(n+1, idz) - (id)^{-n-1} e^{ie} \Gamma(n+1, -idz) \right) (1 - v \bmod 2) + 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{c^2(v-2s)^2}{e^{4(-id+if(v-2s))}} + g i(v-2s) - i e + \frac{1}{2} i \pi(1-v) \right) \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} (c i(v-2s) + 2(-id+if(v-2s))\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{(c i(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{-id+if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2s)(c i(v-2s) + \right. \right. \\
 & \left. \left. 2(-id+if(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(c i(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{4(-id+if(v-2s))}\right) + 2 \right. \right. \\
 & \left. \left. (-id+if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(c i(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{4(-id+if(v-2s))}\right) \right) \right. \\
 & \left. \left. \sqrt{-\frac{(c i(v-2s) + 2(-id+if(v-2s))\sqrt{z})^2}{-id+if(v-2s)}} \right) \right) (-id+if(v-2s))^{-2(n+1)} + \\
 & \frac{c^2(v-2s)^2}{e^{4(id+if(v-2s))}} + g i(v-2s) + i e - \frac{1}{2} i \pi(v+1) (id+if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} \\
 & (c i(v-2s) + 2(id+if(v-2s))\sqrt{z})^{h+j} \left( -\frac{(c i(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{id+if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( c i(v-2s)(c i(v-2s) + 2(id+if(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(c i(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{4(id+if(v-2s))}\right) + 2 \sqrt{-\frac{(c i(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{id+if(v-2s)}} \right. \\
 & \left. \left. (id+if(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(c i(v-2s) + 2(id+if(v-2s))\sqrt{z})^2}{4(id+if(v-2s))}\right) \right) \right) + \\
 & \frac{c^2(v-2s)^2}{e^{4(-id-if(v-2s))}} - i g(v-2s) - i e + \frac{1}{2} i \pi(v+1) (-id-if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n}
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2(-id - if(v-2s))\sqrt{z} - ic(v-2s) \right)^{h+j} \left( -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(-id - if(v-2s))\sqrt{-\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{-id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))} - ic(v-2s)(2(-id - if(v-2s))\sqrt{z} - ic(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(-id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(-id - if(v-2s))}\right) \right) + \right. \\
 & \left. e^{\frac{c^2(v-2s)^2}{4(id-if(v-2s))} - ig(v-2s) + ie + \frac{1}{2}i\pi(v-1)} (id - if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} \right. \\
 & \left. \left( 2(id - if(v-2s))\sqrt{z} - ic(v-2s) \right)^{h+j} \left( -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2(id - if(v-2s))\sqrt{-\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id - if(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))} - ic(v-2s)(2(id - if(v-2s))\sqrt{z} - ic(v-2s)) \right) \right) \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(id - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id - if(v-2s))}\right) \right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin(bz^r) \sin^v(cz^r + fz + g)$**

01.06.21.1194.01

$$\begin{aligned}
 & \int z^n \sin(bz^2) \sin^v(cz^2 + fz + g) dz = \\
 & i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) - \\
 & 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b+2cs-cv} - 4g(v-2s) - 2\pi(1-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} \right. \right. \\
 & \left. \left. (fi(v-2s) + 2(-ib+ic(v-2s))z)^{j+1} \left( -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \right. \right. \\
 & \left. \left. -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))} \right) \right) \left( (-ib+ic(v-2s))^{-n-1} + e^{\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{-b+2cs-cv} + 4g(v-2s) - 2\pi(v+1) \right)} \right) \\
 & (ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s) + 2(ib+ic(v-2s))z)^{j+1} \\
 & \left( -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))} \right) + \\
 & e^{-\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{-b+2cs-cv} + 4g(v-2s) - 2\pi(v+1) \right)} (-ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} \\
 & (2(-ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{-ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{4(-ib-ic(v-2s))} \right) + \\
 & e^{\frac{1}{4}i \left( -\frac{f^2(v-2s)^2}{b+2cs-cv} - 4g(v-2s) + 2\pi(v-1) \right)} (ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} \\
 & (2(ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{4(ib-ic(v-2s))} \right) \Bigg) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1195.01

$$\begin{aligned}
 & \int z^n \sin(\sqrt{z} b) \sin^v(\sqrt{z} c + fz + g) dz = \\
 & (-1)^n 2^{-v} i \binom{v}{\frac{v}{2}} \left( \Gamma(2(n+1), ib\sqrt{z}) - \Gamma(2(n+1), -ib\sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} +
 \end{aligned}$$

$$\begin{aligned}
 & 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-ib-ic(v-2s))^2}{4f(v-2s)} + \frac{1}{2}i\pi(v+1)-ig(v-2s)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib-ic(v-2s))^{-h-j+2n} \right. \right. \\
 & \quad \left. \left. (-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right. \right. \\
 & \quad \left. \left. \binom{j}{h} \binom{n}{j} \left( (-ib-ic(v-2s))(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z}) \right. \right. \right. \\
 & \quad \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) - 2 \right. \right. \\
 & \quad \left. \left. if(v-2s) \sqrt{-\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \right. \right. \\
 & \quad \left. \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \right) \right) \right) \\
 & \quad (-if(v-2s))^{-2(n+1)} + e^{-\frac{i(ib-ic(v-2s))^2}{4f(v-2s)} + \frac{1}{2}i\pi(v-1)-ig(v-2s)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib-ic(v-2s))^{-h-j+2n} \right. \\
 & \quad \left. (ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \quad \left. \left. \binom{j}{h} \binom{n}{j} \left( (ib-ic(v-2s))(ib-ic(v-2s) - 2if(v-2s)\sqrt{z}) \right. \right. \right. \\
 & \quad \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) - 2 \right. \right. \\
 & \quad \left. \left. if(v-2s) \sqrt{-\frac{i(ib-ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \Gamma \left( \frac{1}{2} (h+j+2), -\frac{i(i b-i c(v-2 s)-2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)} \right) \right) \right) \right) \\
 & (-i f(v-2 s))^{-2(n+1)} + e^{\frac{i(-i b+i c(v-2 s))^2}{4 f(v-2 s)} + \frac{1}{2} i \pi(1-v)+g i(v-2 s)} (i f(v-2 s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b+i c(v-2 s))^{-h-j+2 n} (-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (-i b+i c(v-2 s))(-i b+i c(v-2 s)+ \right. \\
 & \left. 2 i f(v-2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), \frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)} \right) \right) + \\
 & 2 f i(v-2 s) \sqrt{\frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)}} \Gamma \left( \frac{1}{2} (h+j+2), \right. \\
 & \left. \frac{i(-i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)} \right) \left. \right) + e^{\frac{i(i b+i c(v-2 s))^2}{4 f(v-2 s)} - \frac{1}{2} i \pi(v+1)+g i(v-2 s)} \\
 & (i f(v-2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b+i c(v-2 s))^{-h-j+2 n} (i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (i b+i c(v-2 s)) \right. \\
 & \left. (i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), \frac{i(i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)} \right) \right) + \\
 & 2 f i(v-2 s) \sqrt{\frac{i(i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{f(v-2 s)}} \Gamma \left( \frac{1}{2} (h+j+2), \right. \\
 & \left. \frac{i(i b+i c(v-2 s)+2 i f(v-2 s) \sqrt{z})^2}{4 f(v-2 s)} \right) \left. \right) \left. \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$



### Involving $z^n \sin(bz^r + e) \sin^v(cz^r + fz + g)$

01.06.21.1196.01

$$\int z^n \sin(bz^2 + e) \sin^v(cz^2 + fz + g) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( e^{ie} (-ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, -ibz^2\right) - e^{-ie} (ibz^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ibz^2\right) \right) (1 - v \bmod 2) -$$

$$2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{b+2cs-cv} - 4g(v-2s) + 4e - 2\pi(1-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} \right. \right.$$

$$\left. \left. (fi(v-2s) + 2(-ib+ic(v-2s))z)^{j+1} \left( -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \right. \right.$$

$$\left. \left. -\frac{(fi(v-2s) + 2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))} \right) \right) (-ib+ic(v-2s))^{-n-1} + e^{\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{-b+2cs-cv} + 4g(v-2s) + 4e - 2\pi(v+1) \right)}$$

$$(ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s) + 2(ib+ic(v-2s))z)^{j+1}$$

$$\left( -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s) + 2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))} \right) +$$

$$e^{-\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{-b+2cs-cv} + 4g(v-2s) + 4e - 2\pi(v+1) \right)} (-ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j}$$

$$(2(-ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{-ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(-ib-ic(v-2s))z - if(v-2s))^2}{4(-ib-ic(v-2s))} \right) +$$

$$e^{\frac{1}{4}i \left( \frac{f^2(v-2s)^2}{b+2cs-cv} - 4g(v-2s) + 4e + 2\pi(v-1) \right)} (ib-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j}$$

$$(2(ib-ic(v-2s))z - if(v-2s))^{j+1} \left( -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{ib-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(2(ib-ic(v-2s))z - if(v-2s))^2}{4(ib-ic(v-2s))} \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1197.01

$$\int z^n \sin(\sqrt{z} b + e) \sin^v(\sqrt{z} c + f z + g) dz =$$

$$(-1)^n 2^{-v} i \left( \frac{v}{2} \right) \left( e^{-ie} \Gamma(2(n+1), i b \sqrt{z}) - e^{ie} \Gamma(2(n+1), -i b \sqrt{z}) \right) (1 - v \bmod 2) b^{-2(n+1)} +$$

$$2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-ib-ic(v-2s))^2}{4f(v-2s)} - ie + \frac{1}{2} i \pi (v+1) - i g (v-2s)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib - ic(v-2s))^{-h-j+2n} \right. \right.$$

$$\left. \left. (-ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \left. \binom{j}{h} \binom{n}{j} \left( (-ib - ic(v-2s)) (-ib - ic(v-2s) - 2if(v-2s)\sqrt{z}) \right) \right. \right.$$

$$\left. \left. \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) - 2 \right. \right.$$

$$\left. \left. i f(v-2s) \sqrt{-\frac{i(-ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \right. \right.$$

$$\left. \left. \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) \right) \right) \left( -i f(v-2s) \right)^{-2(n+1)} +$$

$$e^{-\frac{i(ib-ic(v-2s))^2}{4f(v-2s)} + ie + \frac{1}{2} i \pi (v-1) - i g (v-2s)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib - ic(v-2s))^{-h-j+2n} \right.$$

$$\left. \left. (ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \left( \frac{i(ib - ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \right. \right.$$

$$\left. \left. \binom{j}{h} \binom{n}{j} \left( (ib - ic(v-2s)) (ib - ic(v-2s) - 2if(v-2s)\sqrt{z}) \right) \right. \right.$$

$$\begin{aligned}
 & \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ib-ic(v-2s)-2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right)^{-2} \\
 & if(v-2s)\sqrt{-\frac{i(ib-ic(v-2s)-2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(ib-ic(v-2s)-2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \Bigg) \\
 & (-if(v-2s))^{-2(n+1)} + e^{\frac{i(-ib+ic(v-2s))^2}{4f(v-2s)} - ie + \frac{1}{2}i\pi(1-v) + gi(v-2s)} (if(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(v-2s))^{-h-j+2n} (-ib+ic(v-2s)+2if(v-2s)\sqrt{z})^{h+j} \\
 & \left(\frac{i(-ib+ic(v-2s)+2if(v-2s)\sqrt{z})^2}{f(v-2s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left((-ib+ic(v-2s))(-ib+ic(v-2s)+\right. \\
 & \left.2if(v-2s)\sqrt{z})\Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-ib+ic(v-2s)+2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right)\right) + \\
 & 2fi(v-2s)\sqrt{\frac{i(-ib+ic(v-2s)+2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \left.\frac{i(-ib+ic(v-2s)+2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \Bigg) + e^{\frac{i(ib+ic(v-2s))^2}{4f(v-2s)} + ie - \frac{1}{2}i\pi(v+1) + gi(v-2s)} \\
 & (if(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2s))^{-h-j+2n} (ib+ic(v-2s)+2if(v-2s)\sqrt{z})^{h+j} \\
 & \left(\frac{i(ib+ic(v-2s)+2if(v-2s)\sqrt{z})^2}{f(v-2s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (ib+ic(v-2s))
 \end{aligned}$$

$$\begin{aligned} & (ib + ic(v-2s) + 2if(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib + ic(v-2s) + 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + \\ & 2fi(v-2s) \sqrt{\frac{i(ib + ic(v-2s) + 2if(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \\ & \left. \frac{i(ib + ic(v-2s) + 2if(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+ \end{aligned}$$

### Involving $z^n \sin(bz' + dz) \sin^v(cz' + fz + g)$

01.06.21.1198.01

$$\begin{aligned} \int z^n \sin(bz^2 + dz) \sin^v(cz^2 + fz + g) dz &= i^{-v} 2^{-v-2} e^{-\frac{id^2}{4b}} \\ & \left( -i^{n+v} e^{\frac{id^2}{2b}} \left(\frac{v}{2}\right) (v \bmod 2 - 1) \left( \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-i(d+2bz))^{j+1} \left(\frac{i(d+2bz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+2bz)^2}{4b}\right) \right) \right. \\ & \left. b^{-n-1} + (-1)^{n-1} i^{n+v} \left(\frac{v}{2}\right) (v \bmod 2 - 1) \right. \\ & \left. \left( \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (i(d+2bz))^{j+1} \left(-\frac{i(d+2bz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+2bz)^2}{4b}\right) \right) b^{-n-1} + \right. \\ & \left. e^{\frac{id^2}{4b}} i \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-ig(2s-v)} \binom{v}{s} \left( (-1)^v e^{\frac{1}{4}i\left(\frac{d-2fs+fv}{b-2cs+cv} + 8g(2s-v)\right)} \left( \sum_{j=0}^n 2^{j-n} (i(d-2fs+fv))^{n-j} \right. \right. \right. \\ & \left. \left. (-i(d+fv-2s) + 2(b-2cs+cv)z) \right)^{j+1} \left( \frac{i(d+fv-2s) + 2(b-2cs+cv)z)^2}{b-2cs+cv} \right)^{\frac{1}{2}(-j-1)} \right. \\ & \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+fv-2s) + 2(b-2cs+cv)z)^2}{4(b-2cs+cv)} \right) \right) (-i(b-2cs+cv))^{-n-1} + \right. \\ & \left. e^{-\frac{i(d-2fs+fv)^2}{4(b-2cs+cv)}} (i(b-2cs+cv))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i(d-2fs+fv))^{n-j} \right. \\ & \left. (i(d+fv-2s) + 2(b-2cs+cv)z) \right)^{j+1} \left( -\frac{i(d+fv-2s) + 2(b-2cs+cv)z)^2}{b-2cs+cv} \right)^{\frac{1}{2}(-j-1)} \end{aligned}$$

$$\begin{aligned}
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+f(v-2s)+2(b-2cs+cv)z)^2}{4(b-2cs+cv)}\right) - \\
 & e^{\frac{i(d+2fs-fv)^2}{4(b+2cs-cv)}} (-i(b+2cs-cv))^{-n-1} \sum_{j=0}^n 2^{j-n} (i(d+2fs-fv))^{n-j} \\
 & (-i(d+2fs-fv+2bz+4csz-2cvz))^{j+1} \left(\frac{i(d+2fs-fv+2bz+4csz-2cvz)^2}{b+2cs-cv}\right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d+2fs-fv+2bz+4csz-2cvz)^2}{4(b+2cs-cv)}\right) + \\
 & (-1)^v e^{2ig(2s-v)-\frac{i(d+2fs-fv)^2}{4(b+2cs-cv)}} (i(b+2cs-cv))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i(d+2fs-fv))^{n-j} \\
 & (i(d+2fs-fv+2bz+4csz-2cvz))^{j+1} \left(-\frac{i(d+2fs-fv+2bz+4csz-2cvz)^2}{b+2cs-cv}\right)^{\frac{1}{2}(-j-1)} \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d+2fs-fv+2bz+4csz-2cvz)^2}{4(b+2cs-cv)}\right) \right] /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1199.01

$$\int z^n \sin(\sqrt{z} b + dz) \sin^v(\sqrt{z} c + fz + g) dz = i^{-v-1} 2^{-2n-v-2}$$

$$\begin{aligned}
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{ig(2k-v)-\frac{(-ib+ic(2k-v))^2}{4(-id+if(2k-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(2k-v))^{-h-j+2n} (-ib+ic(2k-v) + \right. \right. \\
 & \left. \left. 2(-id+if(2k-v))\sqrt{z}\right)^{h+j} \left( -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{-id+if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( (-ib+ic(2k-v))(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z}) \right) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) + 2 \right. \\
 & \left. (-id+if(2k-v)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) \right)
 \end{aligned}$$

$$\left( \sqrt{-\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{-id+if(2k-v)}} \right)$$

$$(-id+if(2k-v))^{-2n-2} + (-1)^v e^{ig(2k-v)-\frac{(ib+ic(2k-v))^2}{4(id+if(2k-v))}} (id+if(2k-v))^{-2n-2}$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(2k-v))^{-h-j+2n} (ib+ic(2k-v)+2(id+if(2k-v))\sqrt{z})^{h+j}$$

$$\left( -\frac{(ib+ic(2k-v)+2(id+if(2k-v))\sqrt{z})^2}{id+if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( (ib+ic(2k-v))(ib+ic(2k-v)+2(id+if(2k-v))\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+ic(2k-v)+2(id+if(2k-v))\sqrt{z})^2}{4(id+if(2k-v))} \right) + \right.$$

$$\left. 2(id+if(2k-v)) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+ic(2k-v)+2(id+if(2k-v))\sqrt{z})^2}{4(id+if(2k-v))} \right) \right)$$

$$\left( \sqrt{-\frac{(ib+ic(2k-v)+2(id+if(2k-v))\sqrt{z})^2}{id+if(2k-v)}} \right)$$

$$e^{ig(v-2k)-\frac{(ib+ic(v-2k))^2}{4(-id+if(v-2k))}} (-id+if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(v-2k))^{-h-j+2n}$$

$$(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^{h+j}$$

$$\left( -\frac{(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( (-ib+ic(v-2k))(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z}) \Gamma \left( \right. \right.$$

$$\begin{aligned}
 & \left. \frac{1}{2}(h+j+1), -\frac{(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^2}{4(-id+if(v-2k))} \right) + \\
 & 2(-id+if(v-2k))\Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^2}{4(-id+if(v-2k))}\right) \\
 & \left. \sqrt{-\frac{(-ib+ic(v-2k)+2(-id+if(v-2k))\sqrt{z})^2}{-id+if(v-2k)}} \right) + \\
 & e^{ig(v-2k)-\frac{(ib+ic(v-2k))^2}{4(id+if(v-2k))}}(id+if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2k))^{-h-j+2n} \\
 & (ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^{h+j} \\
 & \left( \frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib+ic(v-2k))(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z}) \Gamma\left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), -\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))} \right) \right) + \\
 & 2(id+if(v-2k))\Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{4(id+if(v-2k))}\right) \\
 & \left. \left. \sqrt{-\frac{(ib+ic(v-2k)+2(id+if(v-2k))\sqrt{z})^2}{id+if(v-2k)}} \right) \right) - \\
 & i 2^{-2n-v-2} (id)^{-2n-2} \left(\frac{v}{2}\right) (1-v \bmod 2) \left( e^{-\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2id\sqrt{z})^{h+j} \right)
 \end{aligned}$$

$$\left(\frac{i(ib+2id\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d}\right) + \right. \\ \left. 2\sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d}\right) \right) - \\ e^{\frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib-2id\sqrt{z})^{h+j} \left(\frac{i(-ib-2id\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\ \binom{n}{j} \left( -ib(-ib-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib-2id\sqrt{z})^2}{4d}\right) - \right. \\ \left. 2id\sqrt{-\frac{i(-ib-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib-2id\sqrt{z})^2}{4d}\right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n \sin(bz^r + dz + e) \sin^v(cz^r + fz + g)$**

01.06.21.1200.01

$$\int z^n \sin(bz^2 + dz + e) \sin^v(cz^2 + fz + g) dz = i 2^{-v-2} \left(\frac{v}{2}\right) (1 - v \bmod 2) \\ \left( (ib)^{-n-1} e^{ie - \frac{id^2}{4b}} \sum_{j=0}^n 2^{j-n} (-id)^{n-j} (id+2ibz)^{j+1} \left(\frac{i(id+2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(id+2ibz)^2}{4b}\right) - \right. \\ \left. (-ib)^{-n-1} e^{\frac{id^2}{4b} - ie} \sum_{j=0}^n 2^{j-n} (id)^{n-j} (-id-2ibz)^{j+1} \left(-\frac{i(-id-2ibz)^2}{b}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id-2ibz)^2}{4b}\right) \right) - \\ i^{-v-1} 2^{-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{(-id+if(2s-v))^2}{4(-ib+ic(2s-v))} - ie + g(2s-v)} \left( \sum_{j=0}^n 2^{j-n} (id - if(2s-v))^{n-j} \right. \right. \\ \left. \left. (-id + if(2s-v) + 2(-ib + ic(2s-v))z)^{j+1} \left( -\frac{(-id + if(2s-v) + 2(-ib + ic(2s-v))z)^2}{-ib + ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \right) \right) \\ \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id + if(2s-v) + 2(-ib + ic(2s-v))z)^2}{4(-ib + ic(2s-v))}\right) \right) (-ib + ic(2s-v))^{-n-1} +$$



$$\begin{aligned}
 & (-1)^v e^{-\frac{(id+if(2s-v))^2}{4(ib+ic(2s-v))}+ie+gi(2s-v)} (ib+ic(2s-v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id-if(2s-v))^{n-j} \\
 & (id+if(2s-v)+2(ib+ic(2s-v))z)^{j+1} \left( -\frac{(id+if(2s-v)+2(ib+ic(2s-v))z)^2}{ib+ic(2s-v)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id+if(2s-v)+2(ib+ic(2s-v))z)^2}{4(ib+ic(2s-v))}\right) - \\
 & e^{-\frac{(-id+if(v-2s))^2}{4(-ib+ic(v-2s))}-ie+gi(v-2s)} (-ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (id-if(v-2s))^{n-j} \\
 & (-id+if(v-2s)+2(-ib+ic(v-2s))z)^{j+1} \left( -\frac{(-id+if(v-2s)+2(-ib+ic(v-2s))z)^2}{-ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-id+if(v-2s)+2(-ib+ic(v-2s))z)^2}{4(-ib+ic(v-2s))}\right) + \\
 & e^{-\frac{(id+if(v-2s))^2}{4(ib+ic(v-2s))}+ie+gi(v-2s)} (ib+ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id-if(v-2s))^{n-j} \\
 & (id+if(v-2s)+2(ib+ic(v-2s))z)^{j+1} \left( -\frac{(id+if(v-2s)+2(ib+ic(v-2s))z)^2}{ib+ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(id+if(v-2s)+2(ib+ic(v-2s))z)^2}{4(ib+ic(v-2s))}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1201.01

$$\int z^n \sin(\sqrt{z} b + dz + e) \sin^v(\sqrt{z} c + fz + g) dz = i^{-v-1} 2^{-2n-v-2}$$

$$\begin{aligned}
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^{v+1} e^{-\frac{(-ib+ic(2k-v))^2}{4(-id+if(2k-v))}-ie+gi(2k-v)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(2k-v))^{-h-j+2n} (-ib+ic(2k-v) + \right. \right. \\
 & \left. \left. 2(-id+if(2k-v))\sqrt{z}\right)^{h+j} \left( -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{-id+if(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( (-ib+ic(2k-v))(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+ic(2k-v)+2(-id+if(2k-v))\sqrt{z})^2}{4(-id+if(2k-v))}\right) + 2 \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (-id + if(2k - v)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z})^2}{4(-id + if(2k - v))} \right) \\
 & \left. \sqrt{-\frac{(-ib + ic(2k - v) + 2(-id + if(2k - v))\sqrt{z})^2}{-id + if(2k - v)}} \right) \\
 & (-id + if(2k - v))^{-2n-2} + (-1)^v e^{-\frac{(ib+ic(2k-v))^2}{4(id+if(2k-v))} + ie+gi(2k-v)} (id + if(2k - v))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib + ic(2k - v))^{-h-j+2n} (ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^{h+j} \\
 & \left( -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{id + if(2k - v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib + ic(2k - v))(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z}) \Gamma \left( \frac{1}{2}(h + j + 1), -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{4(id + if(2k - v))} \right) \right) + \\
 & 2(id + if(2k - v)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{4(id + if(2k - v))} \right) \\
 & \left. \sqrt{-\frac{(ib + ic(2k - v) + 2(id + if(2k - v))\sqrt{z})^2}{id + if(2k - v)}} \right) - \\
 & e^{-\frac{(-ib+ic(v-2k))^2}{4(-id+if(v-2k))} - ie+gi(v-2k)} (-id + if(v - 2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib + ic(v - 2k))^{-h-j+2n} \\
 & (-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^{h+j} \\
 & \left( -\frac{(-ib + ic(v - 2k) + 2(-id + if(v - 2k))\sqrt{z})^2}{-id + if(v - 2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}
 \end{aligned}$$

$$\begin{aligned}
 & \left( (-ib + ic(v-2k))(-ib + ic(v-2k) + 2(-id + if(v-2k))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \quad \left. \left. \frac{1}{2}(h+j+1), -\frac{(-ib + ic(v-2k) + 2(-id + if(v-2k))\sqrt{z})^2}{4(-id + if(v-2k))} \right) \right) + \\
 & 2(-id + if(v-2k)) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(-ib + ic(v-2k) + 2(-id + if(v-2k))\sqrt{z})^2}{4(-id + if(v-2k))} \right) \\
 & \quad \left. \sqrt{-\frac{(-ib + ic(v-2k) + 2(-id + if(v-2k))\sqrt{z})^2}{-id + if(v-2k)}} \right) + \\
 & e^{-\frac{(ib+ic(v-2k))^2}{4(id+if(v-2k))} + ie + gi(v-2k)} (id + if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib + ic(v-2k))^{-h-j+2n} \\
 & \quad (ib + ic(v-2k) + 2(id + if(v-2k))\sqrt{z})^{h+j} \\
 & \quad \left( -\frac{(ib + ic(v-2k) + 2(id + if(v-2k))\sqrt{z})^2}{id + if(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib + ic(v-2k))(ib + ic(v-2k) + 2(id + if(v-2k))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \quad \left. \left. \frac{1}{2}(h+j+1), -\frac{(ib + ic(v-2k) + 2(id + if(v-2k))\sqrt{z})^2}{4(id + if(v-2k))} \right) \right) + \\
 & 2(id + if(v-2k)) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib + ic(v-2k) + 2(id + if(v-2k))\sqrt{z})^2}{4(id + if(v-2k))} \right) \\
 & \quad \left. \sqrt{-\frac{(ib + ic(v-2k) + 2(id + if(v-2k))\sqrt{z})^2}{id + if(v-2k)}} \right) \Bigg) - \\
 & i 2^{-2n-v-2} (id)^{-2n-2} \left( \frac{v}{2} \right) (1 - v \bmod 2) \left( e^{ie - \frac{ib^2}{4d}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib + 2id\sqrt{z})^{h+j} \right)
 \end{aligned}$$

$$\left(\frac{i(ib+2id\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ib+2id\sqrt{z})^2}{4d}\right) + \right. \\ \left. 2\sqrt{\frac{i(ib+2id\sqrt{z})^2}{d}} di \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ib+2id\sqrt{z})^2}{4d}\right) \right) - \\ e^{\frac{ib^2}{4d}-ie} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib-2id\sqrt{z})^{h+j} \left( \frac{i(-ib-2id\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \\ \binom{j}{h} \binom{n}{j} \left( -ib(-ib-2id\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib-2id\sqrt{z})^2}{4d}\right) - \right. \\ \left. 2id\sqrt{-\frac{i(-ib-2id\sqrt{z})^2}{d}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib-2id\sqrt{z})^2}{4d}\right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving product of powers of two direct functions and a power function

### Involving $z^{\alpha-1} \sin^\mu(cz) \sin^\nu(az)$

01.06.21.1202.01

$$\int z^{\alpha-1} \sin^m(cz) \sin^\nu(az) dz = \frac{(-1)^m 2^{-m-\nu} (1-m \bmod 2) (1-\nu \bmod 2)}{\alpha} z^\alpha \binom{m}{\frac{m}{2}} \binom{\nu}{\frac{\nu}{2}} - 2^{-m-\nu} i^{-m} z^\alpha \binom{\nu}{\frac{\nu}{2}} (1-\nu \bmod 2) \\ \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k-m} \binom{m}{k} \left( \Gamma(\alpha, ic(m-2k)z) (ic(m-2k)z)^{-\alpha} + e^{im\pi} ((2ick-icm)z)^{-\alpha} \Gamma(\alpha, (2ick-icm)z) \right) - \\ (-1)^m i^{-\nu} 2^{-m-\nu} z^\alpha \binom{m}{\frac{m}{2}} (1-m \bmod 2) \\ \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s \binom{\nu}{s} \left( \Gamma(\alpha, -ia(v-2s)z) (-ia(v-2s)z)^{-\alpha} + e^{i\pi\nu} ((iav-2ias)z)^{-\alpha} \Gamma(\alpha, (iav-2ias)z) \right) + 2^{-m-\nu} i^{-m-\nu} z^\alpha \\ \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k-m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s \binom{\nu}{s} \left( -e^{i\pi\nu} \Gamma(\alpha, (-2ick+icm-2ias+ia\nu)z) ((-2ick+icm-2ias+ia\nu)z)^{-\alpha} - \right. \\ \left. e^{i\pi m+i\pi\nu} ((2ick-icm-2ias+ia\nu)z)^{-\alpha} \Gamma(\alpha, (2ick-icm-2ias+ia\nu)z) - \right. \\ \left. ((-2ick+icm+2ias-ia\nu)z)^{-\alpha} \Gamma(\alpha, (-2ick+icm+2ias-ia\nu)z) - \right. \\ \left. e^{im\pi} ((2ick-icm+2ias-ia\nu)z)^{-\alpha} \Gamma(\alpha, (2ick-icm+2ias-ia\nu)z) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1203.01

$$\int z^n \sin^\mu(cz) \sin^\nu(az) dz =$$

$$2^{-\nu} \left(\frac{\nu}{2}\right) n! (1 - \nu \bmod 2) \sin^\mu(cz) \left( \sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (-ic\mu)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{\mu}{2}, \dots, -\frac{\mu}{2}, -\mu; 1 - \frac{\mu}{2}, \dots, 1 - \frac{\mu}{2}; e^{2icz} \right) \right)$$

$$(1 - e^{2icz})^{-\mu} + 2^{-\nu} n! \sin^\mu(cz) \left( \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( e^{ia(v-2k)z - \frac{i\pi\nu}{2}} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ia(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c\mu - a(v-2k)}{2c}, \dots, -\frac{c\mu - a(v-2k)}{2c}, -\mu; 1 - \frac{c\mu - a(v-2k)}{2c}, \dots, 1 - \frac{c\mu - a(v-2k)}{2c}; e^{2icz} \right) + \right.$$

$$e^{\frac{i\pi\nu}{2} - ia(v-2k)z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ia(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{a(v-2k) + c\mu}{2c}, \dots, -\frac{a(v-2k) + c\mu}{2c}, -\mu; 1 - \frac{a(v-2k) + c\mu}{2c}, \dots, 1 - \frac{a(v-2k) + c\mu}{2c}; e^{2icz} \right) \left. \right) \Bigg/ (1 - e^{2icz})^{-\mu} ; n \in \mathbb{N} \wedge \nu \in \mathbb{N}^+$$

**Involving  $z^{\alpha-1} \sin^\mu(cz) \sin^\nu(az + b)$**

01.06.21.1204.01

$$\int z^{\alpha-1} \sin^\mu(cz) \sin^\nu(b + az) dz = \frac{(-1)^m 2^{-m-\nu} z^\alpha \binom{m}{\frac{m}{2}} \binom{\nu}{\frac{\nu}{2}} (1 - m \bmod 2) (1 - \nu \bmod 2)}{\alpha} - i^{-m} 2^{-m-\nu} z^\alpha \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k-m} \binom{m}{k} \left( \Gamma(\alpha, ic(m-2k)z) (ic(m-2k)z)^{-\alpha} + e^{im\pi} ((2ick - icm)z)^{-\alpha} \Gamma(\alpha, (2ick - icm)z) - \right.$$

$$(-1)^m i^{-\nu} 2^{-m-\nu} z^\alpha \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s e^{-2bis - ibv} \binom{\nu}{s} \left( e^{2ibv} \Gamma(\alpha, -ia(v-2s)z) (-ia(v-2s)z)^{-\alpha} + \right.$$

$$e^{4ibs + i\pi\nu} ((iav - 2ias)z)^{-\alpha} \Gamma(\alpha, (iav - 2ias)z) + (2i)^{-m-\nu} z^\alpha \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k-m} \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s e^{-2bis - ibv} \binom{\nu}{s} \left( -e^{4ibs + i\pi\nu} \Gamma(\alpha, (-2cick + icm - 2ias + iav)z) ((-2cick + icm - 2ias + iav)z)^{-\alpha} - \right.$$

$$e^{i\pi m + 4ibs + i\pi\nu} ((2ick - icm - 2ias + iav)z)^{-\alpha} \Gamma(\alpha, (2ick - icm - 2ias + iav)z) +$$

$$e^{2ibv} (-\Gamma(\alpha, (-2cick + icm + 2ias - iav)z) ((-2cick + icm + 2ias - iav)z)^{-\alpha} -$$

$$e^{im\pi} ((2ick - icm + 2ias - iav)z)^{-\alpha} \Gamma(\alpha, (2ick - icm + 2ias - iav)z) \Bigg) ; m \in \mathbb{N}^+ \wedge \nu \in \mathbb{N}^+$$

01.06.21.1205.01

$$\int z^n \sin^\mu(cz) \sin^\nu(az+b) dz =$$

$$2^{-\nu} \binom{\nu}{\frac{\nu}{2}} n! (1 - \nu \bmod 2) \sin^\mu(cz) (1 - e^{2icz})^{-\mu} \sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (-ic\mu)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{\mu}{2}, \dots, -\frac{\mu}{2}, -\mu; 1 - \frac{\mu}{2}, \dots, 1 - \frac{\mu}{2}; e^{2icz} \right) +$$

$$2^{-\nu} n! \sin^\mu(cz) (1 - e^{2icz})^{-\mu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( e^{\frac{i\pi\nu}{2} - ib(v-2k) - ia(v-2k)z} \right.$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ia(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{a(-2k+v) + c\mu}{2c}, \dots, -\frac{a(-2k+v) + c\mu}{2c}, \right.$$

$$\left. -\mu; 1 - \frac{a(-2k+v) + c\mu}{2c}, \dots, 1 - \frac{a(-2k+v) + c\mu}{2c}; e^{2icz} \right) + e^{\frac{1}{2}i\pi\nu + bi(v-2k) + ai(v-2k)z}$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j} (ai(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{-a(-2k+v) + c\mu}{2c}, \dots, -\frac{-a(-2k+v) + c\mu}{2c}, \right.$$

$$\left. -\mu; 1 - \frac{-a(-2k+v) + c\mu}{2c}, \dots, 1 - \frac{-a(-2k+v) + c\mu}{2c}; e^{2icz} \right) \Bigg) /; n \in \mathbb{N} \wedge \nu \in \mathbb{N}^+$$

01.06.21.1206.01

$$\int z^n \sin^m(cz) \sin^\nu(b+az) dz =$$

$$2^{-m} \binom{m}{\frac{m}{2}} n! (1 - m \bmod 2) \sin^\nu(b+az) \left( \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ia\nu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{\nu}{2}, \dots, -\frac{\nu}{2}, -\nu; 1 - \frac{\nu}{2}, \dots, 1 - \frac{\nu}{2}; e^{2i(b+az)} \right) \right)$$

$$(1 - e^{2i(b+az)})^{-\nu} + 2^{-m} n! \sin^\nu(b+az) \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \right.$$

$$\left( e^{-\frac{1}{2}i(-2czm + \pi m + 4ckz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ic(m-2k) - ia\nu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{a\nu - c(m-2k)}{2a}, \dots, -\frac{a\nu - c(m-2k)}{2a}, \right.$$

$$\left. -\nu; 1 - \frac{a\nu - c(m-2k)}{2a}, \dots, 1 - \frac{a\nu - c(m-2k)}{2a}; e^{2i(b+az)} \right) + e^{\frac{1}{2}i(-2czm + \pi m + 4ckz)}$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ic(m-2k) - ia\nu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c(m-2k) + a\nu}{2a}, \dots, -\frac{c(m-2k) + a\nu}{2a}, \right.$$

$$\left. -\nu; 1 - \frac{c(m-2k) + a\nu}{2a}, \dots, 1 - \frac{c(m-2k) + a\nu}{2a}; e^{2i(b+az)} \right) \Bigg) (1 - e^{2i(b+az)})^{-\nu} /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+$$

**Involving  $z^{\alpha-1} \sin^\mu(cz+d) \sin^\nu(az+b)$**

01.06.21.1207.01

$$\int z^{\alpha-1} \sin^m(d + cz) \sin^v(b + az) dz =$$

$$\frac{(-1)^m 2^{-m-v}}{\alpha} z^\alpha \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) - 2^{-m-v} i^{-m} z^\alpha \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k-m} e^{2idk+idm} \binom{m}{k}$$

$$\left( e^{-2idm} \Gamma(\alpha, ic(m-2k)z) (ic(m-2k)z)^{-\alpha} + e^{im\pi-4idk} ((2ick-icm)z)^{-\alpha} \Gamma(\alpha, (2ick-icm)z) \right) -$$

$$(-1)^m i^{-v} 2^{-m-v} z^\alpha \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-2bis-ibv} \binom{v}{s}$$

$$\left( e^{2ibv} \Gamma(\alpha, -ia(v-2s)z) (-ia(v-2s)z)^{-\alpha} + e^{4ibs+i\pi v} ((iav-2ias)z)^{-\alpha} \Gamma(\alpha, (iav-2ias)z) \right) +$$

$$2^{-m-v} i^{-m-v} z^\alpha \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k-m} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{2idk+idm-2ibs-ibv} \binom{v}{s}$$

$$\left( -e^{-2dim+4ibs+i\pi v} \Gamma(\alpha, (-2cick+icm-2ias+iav)z) ((-2cick+icm-2ias+iav)z)^{-\alpha} - \right.$$

$$e^{-4dik+4ibs+i\pi v+im\pi} ((2ick-icm-2ias+iav)z)^{-\alpha} \Gamma(\alpha, (2ick-icm-2ias+iav)z) +$$

$$e^{2ibv} \left( -e^{-2idm} \Gamma(\alpha, (-2cick+icm+2ias-iav)z) ((-2cick+icm+2ias-iav)z)^{-\alpha} - e^{im\pi-4idk} \right.$$

$$\left. \left. (2ick-icm+2ias-iav)z \right)^{-\alpha} \Gamma(\alpha, (2ick-icm+2ias-iav)z) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1208.01

$$\int z^n \sin^\mu(cz + d) \sin^v(az + b) dz = 2^{-v} \binom{v}{\frac{v}{2}} n! (1 - v \bmod 2) \sin^\mu(d + cz) (1 - e^{2i(d+cz)})^{-\mu}$$

$$\sum_{j=0}^n \frac{((-1)^j z^{n-j})}{(n-j)! (-ic\mu)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{\mu}{2}, \dots, -\frac{\mu}{2}, -\mu; 1 - \frac{\mu}{2}, \dots, 1 - \frac{\mu}{2}; e^{2i(d+cz)} \right) + 2^{-v} (1 - e^{2i(d+cz)})^{-\mu} n! \sin^\mu(d + cz)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-\frac{1}{2}i(4bk+4azk-2bv+\pi v-2avz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ia(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c\mu - a(v-2k)}{2c}, \right.$$

$$\dots, -\frac{c\mu - a(v-2k)}{2c}, -\mu; 1 - \frac{c\mu - a(v-2k)}{2c}, \dots, 1 - \frac{c\mu - a(v-2k)}{2c}; e^{2i(d+cz)} \right) +$$

$$e^{\frac{1}{2}i(4bk+4azk-2bv+\pi v-2avz)} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ia(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{a(v-2k) + c\mu}{2c}, \dots, \right.$$

$$\left. -\frac{a(v-2k) + c\mu}{2c}, -\mu; 1 - \frac{a(v-2k) + c\mu}{2c}, \dots, 1 - \frac{a(v-2k) + c\mu}{2c}; e^{2i(d+cz)} \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving  $z^n \sin^m(bz) \sin^v(cz^r)$

01.06.21.1209.01

$$\int z^n \sin^m(bz) \sin^v(cz^2) dz =$$

$$\begin{aligned} & \frac{(-1)^m 2^{-m-v} (1-m \bmod 2) (1-v \bmod 2)}{n+1} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} - (-1)^m i^{-v} 2^{-m-v-1} z^{n+1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \\ & \left( (-1)^v \Gamma\left(\frac{n+1}{2}, (icv-2ick)z^2\right) ((icv-2ick)z^2)^{\frac{1}{2}(-n-1)} + ((2ick-icv)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (2ick-icv)z^2\right) \right) - \\ & i^{-m} 2^{-m-v} z^{n+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m \Gamma(n+1, (ibm-2ibk)z) ((ibm-2ibk)z)^{-n-1} + \right. \\ & \left. ((2ibk-ibm)z)^{-n-1} \Gamma(n+1, (2ibk-ibm)z) \right) - \\ & 2^{-m-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{ib^2(2k-m)^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (ib(2k-m))^{n-j} (2ic(2s-v)z-ib(2k-m))^{j+1} \right. \right. \\ & \left. \left. \left( \frac{i(2ic(2s-v)z-ib(2k-m))^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(2s-v)z-ib(2k-m))^2}{4c(2s-v)}\right) \right) \right) \\ & (ic(2s-v))^{-n-1} + (-1)^{m+v} e^{-\frac{ib^2(m-2k)^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (ib(m-2k))^{n-j} (2ic(2s-v)z-ib(m-2k))^{j+1} \right. \\ & \left. \left( \frac{i(2ic(2s-v)z-ib(m-2k))^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(2s-v)z-ib(m-2k))^2}{4c(2s-v)}\right) \right) \\ & (ic(2s-v))^{-n-1} + e^{-\frac{ib^2(2k-m)^2}{4c(v-2s)}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (ib(2k-m))^{n-j} (2ic(v-2s)z-ib(2k-m))^{j+1} \\ & \left( \frac{i(2ic(v-2s)z-ib(2k-m))^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(v-2s)z-ib(2k-m))^2}{4c(v-2s)}\right) + \\ & (-1)^m e^{-\frac{ib^2(m-2k)^2}{4c(v-2s)}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (ib(m-2k))^{n-j} (2ic(v-2s)z-ib(m-2k))^{j+1} \\ & \left( \frac{i(2ic(v-2s)z-ib(m-2k))^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\ & \left. \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(v-2s)z-ib(m-2k))^2}{4c(v-2s)}\right) \right); n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+ \end{aligned}$$



01.06.21.1210.01

$$\int z^n \sin^m(bz) \sin^v(c\sqrt{z}) dz =$$

$$\frac{(-1)^m 2^{-m-v} (1-m \bmod 2) (1-v \bmod 2)}{n+1} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} + \frac{1}{b} \left( i^{m+1} 2^{-m-v} z^n \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{2k-m} \binom{m}{k} \right. \\ \left. (e^{im\pi} (-ib(m-2k)z)^{-n} \Gamma(n+1, -ib(m-2k)z) - (-ib(2k-m)z)^{-n} \Gamma(n+1, -ib(2k-m)z)) \right) - (-1)^m$$

$$i^{-v} 2^{-m-v+1} z^{n+1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v \Gamma(2(n+1), (icv-2ick)\sqrt{z}) ((icv-2ick)\sqrt{z})^{-2(n+1)} + \right.$$

$$\left. ((2ick-icv)\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (2ick-icv)\sqrt{z}) \right) + 2^{-m-2n-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{ic^2(v-2s)^2}{4b(2k-m)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-2ib\sqrt{z}(2k-m) - ic(v-2s))^{h+j} \right. \right.$$

$$\left. \left( -\frac{i(-2ib\sqrt{z}(2k-m) - ic(v-2s))^2}{b(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2s)(-2ib\sqrt{z}(2k-m) - \right. \right.$$

$$\left. ic(v-2s) \right) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-2ib\sqrt{z}(2k-m) - ic(v-2s))^2}{4b(2k-m)} \right) -$$

$$2ib(2k-m) \sqrt{-\frac{i(-2ib\sqrt{z}(2k-m) - ic(v-2s))^2}{b(2k-m)}} \Gamma\left( \frac{1}{2}(h+j+2), \right.$$

$$\left. \left. -\frac{i(-2ib\sqrt{z}(2k-m) - ic(v-2s))^2}{4b(2k-m)} \right) \right) \left. \right) \left. \right) (-ib(2k-m))^{-2n-2} +$$

$$e^{\frac{ic^2(v-2s)^2}{4b(2k-m)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s) - 2ib(2k-m)\sqrt{z})^{h+j} \right)$$

$$\begin{aligned}
 & \left( -\frac{i(i c(v-2 s)-2 i b(2 k-m) \sqrt{z})^2}{b(2 k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( i c(v-2 s) \right. \\
 & \left. (i c(v-2 s)-2 i b(2 k-m) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(i c(v-2 s)-2 i b(2 k-m) \sqrt{z})^2}{4 b(2 k-m)}\right) \right) - \\
 & 2 i b(2 k-m) \sqrt{-\frac{i(i c(v-2 s)-2 i b(2 k-m) \sqrt{z})^2}{b(2 k-m)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \left. -\frac{i(i c(v-2 s)-2 i b(2 k-m) \sqrt{z})^2}{4 b(2 k-m)}\right) \left. \right) \left( (-i b(2 k-m))^{-2 n-2} + (-1)^{m+v} e^{\frac{i c^2(v-2 s)^2}{4 b(m-2 k)}} \right) \\
 & (-i b(m-2 k))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2 s))^{-h-j+2 n} (-2 i b \sqrt{z}(m-2 k)-i c(v-2 s))^{h+j} \\
 & \left( -\frac{i(-2 i b \sqrt{z}(m-2 k)-i c(v-2 s))^2}{b(m-2 k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i c(v-2 s) \right. \\
 & \left. (-2 i b \sqrt{z}(m-2 k)-i c(v-2 s)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-2 i b \sqrt{z}(m-2 k)-i c(v-2 s))^2}{4 b(m-2 k)}\right) \right) - \\
 & 2 i b(m-2 k) \sqrt{-\frac{i(-2 i b \sqrt{z}(m-2 k)-i c(v-2 s))^2}{b(m-2 k)}} \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-2 i b \sqrt{z}(m-2 k)-i c(v-2 s))^2}{4 b(m-2 k)}\right) \right) \left. \right) + (-1)^m e^{\frac{i c^2(v-2 s)^2}{4 b(m-2 k)}} \\
 & (-i b(m-2 k))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2 s))^{-h-j+2 n} (i c(v-2 s)-2 i b(m-2 k) \sqrt{z})^{h+j} \\
 & \left( -\frac{i(i c(v-2 s)-2 i b(m-2 k) \sqrt{z})^2}{b(m-2 k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( i c(v-2 s) \right.
 \end{aligned}$$

$$\left. \left. \left. \left( i c (v - 2 s) - 2 i b (m - 2 k) \sqrt{z} \right) \Gamma \left( \frac{1}{2} (h + j + 1), - \frac{i (i c (v - 2 s) - 2 i b (m - 2 k) \sqrt{z})^2}{4 b (m - 2 k)} \right) - \right. \right. \right.$$

$$2 i b (m - 2 k) \sqrt{- \frac{i (i c (v - 2 s) - 2 i b (m - 2 k) \sqrt{z})^2}{b (m - 2 k)}} \Gamma \left( \frac{1}{2} (h + j + 2), \right.$$

$$\left. \left. \left. - \frac{i (i c (v - 2 s) - 2 i b (m - 2 k) \sqrt{z})^2}{4 b (m - 2 k)} \right) \right) \right) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $z^n \sin^m(dz + e) \sin^v(cz^r)$

01.06.21.1211.01

$$\int z^n \sin^m(e + dz) \sin^v(cz^2) dz =$$

$$\frac{(-1)^m 2^{-m-v} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} - (-1)^m i^{-v} 2^{-m-v-1} z^{n+1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( (-1)^v \Gamma\left(\frac{n+1}{2}, (icv - 2ick)z^2\right) ((icv - 2ick)z^2)^{\frac{1}{2}(-n-1)} + (2ick - icv)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (2ick - icv)z^2\right) \right) -$$

$$i^{-m} 2^{-m-v} z^{n+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} ((-1)^m e^{2iek - iem} \Gamma(n+1, (idm - 2idk)z) ((idm - 2idk)z)^{-n-1} +$$

$$e^{iem - 2iek} (2idk - idm)z)^{-n-1} \Gamma(n+1, (2idk - idm)z) -$$

$$2^{-m-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{id^2(2k-m)^2}{4c(2s-v)}} i e^{(2k-m)}$$

$$\left( \sum_{j=0}^n 2^{j-n} (id(2k-m))^{n-j} (2ic(2s-v)z - id(2k-m))^{j+1} \left( \frac{i(2ic(2s-v)z - id(2k-m))^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(2s-v)z - id(2k-m))^2}{4c(2s-v)}\right) \right) (ic(2s-v))^{-n-1} + (-1)^{m+v} e^{-\frac{id^2(m-2k)^2}{4c(2s-v)}} i e^{(m-2k)}$$

$$\left( \sum_{j=0}^n 2^{j-n} (id(m-2k))^{n-j} (2ic(2s-v)z - id(m-2k))^{j+1} \left( \frac{i(2ic(2s-v)z - id(m-2k))^2}{c(2s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}$$

$$\Gamma\left(\frac{j+1}{2}, \frac{i(2ic(2s-v)z - id(m-2k))^2}{4c(2s-v)}\right) \right) (ic(2s-v))^{-n-1} + e^{-\frac{id^2(2k-m)^2}{4c(v-2s)}} i e^{(2k-m)} (ic(v-2s))^{-n-1}$$

$$\sum_{j=0}^n 2^{j-n} (id(2k-m))^{n-j} (2ic(v-2s)z - id(2k-m))^{j+1} \left( \frac{i(2ic(v-2s)z - id(2k-m))^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(v-2s)z - id(2k-m))^2}{4c(v-2s)}\right) + (-1)^m e^{-\frac{id^2(m-2k)^2}{4c(v-2s)}} i e^{(m-2k)} (ic(v-2s))^{-n-1}$$

$$\sum_{j=0}^n 2^{j-n} (id(m-2k))^{n-j} (2ic(v-2s)z - id(m-2k))^{j+1} \left( \frac{i(2ic(v-2s)z - id(m-2k))^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2ic(v-2s)z - id(m-2k))^2}{4c(v-2s)}\right) \Bigg) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1212.01

$$\int z^n \sin^m(dz + e) \sin^v(c\sqrt{z}) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} + \frac{1}{d} \left( i^{m+1} 2^{-m-v} z^n \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \right.$$

$$\left. \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{2k - m} \left( (-1)^k e^{2iek + iem} \binom{m}{k} \left( e^{im\pi - 4iek} (-id(m - 2k)z)^{-n} \Gamma(n + 1, -id(m - 2k)z) - e^{-2iem} (-id(2k - m)z)^{-n} \Gamma(n + 1, -id(2k - m)z) \right) \right) \right) - (-1)^m i^{-v} 2^{-m-v+1} z^{n+1}$$

$$\binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v \Gamma(2(n + 1), (icv - 2ick)\sqrt{z}) ((icv - 2ick)\sqrt{z})^{-2(n+1)} + \right.$$

$$\left. \left( (2ick - icv)\sqrt{z} \right)^{-2(n+1)} \Gamma(2(n + 1), (2ick - icv)\sqrt{z}) \right) + 2^{-m-2n-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s$$

$$\binom{v}{s} \left( (-1)^v e^{\frac{ic^2(v-2s)^2}{4d(2k-m)} - ie(2k-m)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-2id\sqrt{z}(2k-m) - ic(v-2s))^{h+j} \right. \right.$$

$$\left. \left( -\frac{i(-2id\sqrt{z}(2k-m) - ic(v-2s))^2}{d(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2s)(-2id\sqrt{z}(2k-m) - ic(v-2s)) \right. \right.$$

$$\left. \left. ic(v-2s) \right) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-2id\sqrt{z}(2k-m) - ic(v-2s))^2}{4d(2k-m)} \right) \right) -$$

$$2id(2k-m) \sqrt{-\frac{i(-2id\sqrt{z}(2k-m) - ic(v-2s))^2}{d(2k-m)}} \Gamma\left( \frac{1}{2}(h+j+2), \right.$$

$$\left. \left. -\frac{i(-2id\sqrt{z}(2k-m) - ic(v-2s))^2}{4d(2k-m)} \right) \right) \left. \right) \left. \right) \left. \right) (-id(2k-m))^{-2n-2} +$$

$$\begin{aligned}
 & e^{\frac{ic^2(v-2s)^2}{4d(2k-m)} - ie(2k-m)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s) - 2id(2k-m)\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(ic(v-2s) - 2id(2k-m)\sqrt{z})^2}{d(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ic(v-2s) \right. \right. \\
 & \left. \left. (ic(v-2s) - 2id(2k-m)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ic(v-2s) - 2id(2k-m)\sqrt{z})^2}{4d(2k-m)}\right) \right. \right. \\
 & \left. \left. 2id(2k-m) \sqrt{-\frac{i(ic(v-2s) - 2id(2k-m)\sqrt{z})^2}{d(2k-m)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. \left. -\frac{i(ic(v-2s) - 2id(2k-m)\sqrt{z})^2}{4d(2k-m)} \right) \right) \right) \left( (-id(2k-m))^{-2n-2} + (-1)^{m+v} e^{\frac{ic^2(v-2s)^2}{4d(m-2k)} - ie(m-2k)} \right. \\
 & \left. (-id(m-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-2id\sqrt{z}(m-2k) - ic(v-2s))^{h+j} \right. \\
 & \left. \left( -\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2s) \right. \right. \\
 & \left. \left. (-2id\sqrt{z}(m-2k) - ic(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{4d(m-2k)}\right) \right. \right. \\
 & \left. \left. 2id(m-2k) \sqrt{-\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{d(m-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. \left. -\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{4d(m-2k)} \right) \right) \right) \left( (-1)^m e^{\frac{ic^2(v-2s)^2}{4d(m-2k)} - ie(m-2k)} \right. \\
 & \left. (-id(m-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s) - 2id(m-2k)\sqrt{z})^{h+j} \right)
 \end{aligned}$$

$$\left( -\frac{i(i c(v-2 s)-2 i d(m-2 k) \sqrt{z})^2}{d(m-2 k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} i c(v-2 s) \left( i c(v-2 s)-2 i d(m-2 k) \sqrt{z} \right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(i c(v-2 s)-2 i d(m-2 k) \sqrt{z})^2}{4 d(m-2 k)}\right) - 2 i d(m-2 k) \sqrt{-\frac{i(i c(v-2 s)-2 i d(m-2 k) \sqrt{z})^2}{d(m-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(i c(v-2 s)-2 i d(m-2 k) \sqrt{z})^2}{4 d(m-2 k)}\right) \Bigg) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin^m(b z^r) \sin^v(c z^r)$

01.06.21.1213.01

$$\int z^{\alpha-1} \sin^m(b z^r) \sin^v(c z^r) dz = \frac{(-1)^m 2^{-m-v} (1-m \bmod 2) (1-v \bmod 2)}{\alpha} z^\alpha \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} - \frac{i^{-m} 2^{-m-v} z^\alpha}{r} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m \Gamma\left(\frac{\alpha}{r}, (i b m-2 i b k) z^r\right) ((i b m-2 i b k) z^r)^{-\frac{\alpha}{r}} + ((2 i b k-i b m) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2 i b k-i b m) z^r\right) \right) - \frac{(-1)^m i^{-v} 2^{-m-v} z^\alpha}{r} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v \Gamma\left(\frac{\alpha}{r}, (i c v-2 i c k) z^r\right) ((i c v-2 i c k) z^r)^{-\frac{\alpha}{r}} + ((2 i c k-i c v) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2 i c k-i c v) z^r\right) \right) - \frac{i^{-m-v} 2^{-m-v} z^\alpha}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{m+v} \Gamma\left(\frac{\alpha}{r}, (-2 b i k+i b m-2 i c s+i c v) z^r\right) ((-2 b i k+i b m-2 i c s+i c v) z^r)^{-\frac{\alpha}{r}} + (-1)^v ((2 i b k-i b m-2 i c s+i c v) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2 i b k-i b m-2 i c s+i c v) z^r\right) + (-1)^m ((-2 b i k+i b m+2 i c s-i c v) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-2 b i k+i b m+2 i c s-i c v) z^r\right) + ((2 i b k-i b m+2 i c s-i c v) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2 i b k-i b m+2 i c s-i c v) z^r\right) \right) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1214.01

$$\int z^n \sin^m(b z^2) \sin^v(c z^2) dz =$$

$$\begin{aligned}
 & -2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{i m \pi}{2}} \Gamma\left(\frac{n+1}{2}, -i b(m-2k) z^2\right) (-i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} + \right. \\
 & \quad \left. e^{\frac{i m \pi}{2}} (i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i b(m-2k) z^2\right) \right) - \\
 & 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i v \pi}{2}} \Gamma\left(\frac{n+1}{2}, -i c(v-2s) z^2\right) (-i c(v-2s) z^2)^{\frac{1}{2}(-n-1)} + \right. \\
 & \quad \left. e^{\frac{i v \pi}{2}} (i c(v-2s) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i c(v-2s) z^2\right) \right) - 2^{-m-v-1} z^{n+1} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(m-v)\pi}{2}} \Gamma\left(\frac{n+1}{2}, (i c(v-2s) - i b(m-2k)) z^2\right) ((i c(v-2s) - i b(m-2k)) z^2)^{\frac{1}{2}(-n-1)} + \right. \\
 & \quad e^{\frac{1}{2} i(m+v)\pi} ((b i(m-2k) + c i(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (b i(m-2k) + c i(v-2s)) z^2\right) + \\
 & \quad e^{-\frac{i(m+v)\pi}{2}} ((-i b(m-2k) - i c(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-i b(m-2k) - i c(v-2s)) z^2\right) + \\
 & \quad \left. e^{\frac{1}{2} i(m-v)\pi} ((i b(m-2k) - i c(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b(m-2k) - i c(v-2s)) z^2\right) \right) + \\
 & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$



01.06.21.1215.01

$$\int z^n \sin^m(\sqrt{z} b + e) \sin^v(c \sqrt{z}) dz = (-1)^n 2^{-m-v+1} \left(\frac{v}{2}\right) (1 - v \bmod 2) b^{-2(n+1)} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^{-2(n+1)}$$

$$\left( e^{i e(m-2k) - \frac{i m \pi}{2}} \Gamma(2(n+1), -i b(m-2k) \sqrt{z}) + e^{\frac{i m \pi}{2} - i e(m-2k)} \Gamma(2(n+1), i b(m-2k) \sqrt{z}) \right) +$$

$$\frac{2^{-m-v} z^{n+1} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + (-1)^n 2^{-m-v+1} c^{-2(n+1)} \left(\frac{m}{2}\right) (1 - m \bmod 2)$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} (v-2s)^{-2(n+1)} \left( e^{-\frac{i v \pi}{2}} \Gamma(2(n+1), -i c(v-2s) \sqrt{z}) + e^{\frac{i v \pi}{2}} \Gamma(2(n+1), i c(v-2s) \sqrt{z}) \right) -$$

$$2^{-m-v+1} z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{i e(m-2k) - \frac{1}{2} i(m-v)\pi} \Gamma(2(n+1), (i c(v-2s) - i b(m-2k)) \sqrt{z}) \right.$$

$$\left. \left( (i c(v-2s) - i b(m-2k)) \sqrt{z} \right)^{-2(n+1)} + e^{\frac{1}{2} i(m+v)\pi - i e(m-2k)} \left( (b i(m-2k) + c i(v-2s)) \sqrt{z} \right)^{-2(n+1)} \right.$$

$$\Gamma(2(n+1), (b i(m-2k) + c i(v-2s)) \sqrt{z}) + e^{i e(m-2k) - \frac{1}{2} i(m+v)\pi} \left( (-i b(m-2k) - i c(v-2s)) \sqrt{z} \right)^{-2(n+1)}$$

$$\Gamma(2(n+1), (-i b(m-2k) - i c(v-2s)) \sqrt{z}) + e^{\frac{1}{2} i(m-v)\pi - i e(m-2k)} \left( (i b(m-2k) - i c(v-2s)) \sqrt{z} \right)^{-2(n+1)}$$

$$\left. \Gamma(2(n+1), (i b(m-2k) - i c(v-2s)) \sqrt{z}) \right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin^m(dz) \sin^v(cz^r + g)$

01.06.21.1216.01

$$\int z^n \sin^m(dz) \sin^v(cz^2 + g) dz =$$

$$-2^{-m-v-1} \left(\frac{m}{2}\right) (1 - m \bmod 2) \left( \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{i g(v-2k) - \frac{i \pi v}{2}} \Gamma\left(\frac{n+1}{2}, -i c(v-2k) z^2\right) (-i c(v-2k) z^2\right)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{\frac{i \pi v}{2} - i g(v-2k)} \left( i c(v-2k) z^2\right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i c(v-2k) z^2\right) \right) z^{n+1} +$$

$$\frac{2^{-m-v} z^{n+1} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + (-1)^n 2^{-m-v} \left(\frac{v}{2}\right) (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( e^{\frac{i m \pi}{2}} \Gamma(n+1, i d(m-2k) z) (-i d(m-2k))^{-n-1} + e^{-\frac{i m \pi}{2}} \Gamma(n+1, -i d(m-2k) z) \right) -$$

$$2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{d^2 i(m-2k)^2}{4c(v-2s)} + \frac{i \pi v}{2} - i g(v-2s) + \frac{i m \pi}{2}} \right.$$

$$\begin{aligned}
 & \left( \sum_{j=0}^n 2^{j-n} (i d(m-2k))^{n-j} (-i d(m-2k) - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(-i d(m-2k) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-i d(m-2k) - 2 i c(v-2s) z)^2}{4 c(v-2s)}\right) (-i c(v-2s))^{-n-1} + \right. \\
 & e^{\frac{d^2 i(m-2k)^2}{4 c(v-2s)} + \frac{i \pi v}{2} - i g(v-2s) - \frac{i m \pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (-i d(m-2k))^{n-j} (i d(m-2k) - 2 i c(v-2s) z)^{j+1} \right. \\
 & \left. \left( -\frac{i(i d(m-2k) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(i d(m-2k) - 2 i c(v-2s) z)^2}{4 c(v-2s)}\right) \right) \\
 & (-i c(v-2s))^{-n-1} + e^{\frac{i d^2(m-2k)^2}{4 c(v-2s)} + g i(v-2s) - \frac{i \pi v}{2} + \frac{i m \pi}{2}} (i c(v-2s))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (i d(m-2k))^{n-j} (2 i c(v-2s) z - i d(m-2k))^{j+1} \left( \frac{i(2 i c(v-2s) z - i d(m-2k))^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(2 i c(v-2s) z - i d(m-2k))^2}{4 c(v-2s)}\right) + e^{-\frac{i d^2(m-2k)^2}{4 c(v-2s)} + g i(v-2s) - \frac{i \pi v}{2} - \frac{i m \pi}{2}} (i c(v-2s))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (-i d(m-2k))^{n-j} (d i(m-2k) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(d i(m-2k) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d i(m-2k) + 2 c i(v-2s) z)^2}{4 c(v-2s)}\right) \right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1217.01

$$\int z^n \sin^m(dz) \sin^v(\sqrt{z} c + g) dz =$$

$$\begin{aligned}
 & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} + (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\
 & \left( e^{\frac{i m \pi}{2}} \Gamma(n+1, i d(m-2k) z) (-i d(m-2k))^{-n-1} + e^{-\frac{1}{2} i m \pi} (i d(m-2k))^{-n-1} \Gamma(n+1, -i d(m-2k) z) \right) + \\
 & 2^{-m-v+1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+n} (c(v-2k))^{-2(n+1)} \binom{v}{k} \left( e^{i g(v-2k) - \frac{i \pi v}{2}} \Gamma(2(n+1), -i c(v-2k) \sqrt{z}) + \right. \\
 & \left. e^{\frac{i \pi v}{2} - i g(v-2k)} \Gamma(2(n+1), i c(v-2k) \sqrt{z}) \right) + 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}
 \end{aligned}$$

$$\begin{aligned}
 & \left( e^{\frac{c^2 i(v-2s)^2}{4d(m-2k)} - i g(v-2s) + \frac{i\pi v}{2} + \frac{im\pi}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n} (-2 i d \sqrt{z} (m-2k) - i c(v-2s))^{h+j} \right. \right. \\
 & \left. \left( -\frac{i(-2 i d \sqrt{z} (m-2k) - i c(v-2s))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i c(v-2s) (-2 i d \sqrt{z} (m-2k) - \right. \right. \\
 & \left. \left. i c(v-2s) \right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-2 i d \sqrt{z} (m-2k) - i c(v-2s))^2}{4 d(m-2k)}\right) - \right. \\
 & \left. 2 i d(m-2k) \sqrt{-\frac{i(-2 i d \sqrt{z} (m-2k) - i c(v-2s))^2}{d(m-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(-2 i d \sqrt{z} (m-2k) - i c(v-2s))^2}{4 d(m-2k)}\right) \right) \left. \right) \left. \right) (-i d(m-2k))^{-2(n+1)} +
 \end{aligned}$$

$$\begin{aligned}
 & e^{\frac{c^2 i(v-2s)^2}{4d(m-2k)} + g i(v-2s) - \frac{i\pi v}{2} + \frac{im\pi}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} (i c(v-2s) - 2 i d(m-2k) \sqrt{z})^{h+j} \right. \\
 & \left( -\frac{i(i c(v-2s) - 2 i d(m-2k) \sqrt{z})^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( i c(v-2s) \right. \\
 & \left. (i c(v-2s) - 2 i d(m-2k) \sqrt{z}) \right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(i c(v-2s) - 2 i d(m-2k) \sqrt{z})^2}{4 d(m-2k)}\right) - \\
 & \left. 2 i d(m-2k) \sqrt{-\frac{i(i c(v-2s) - 2 i d(m-2k) \sqrt{z})^2}{d(m-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(i c(v-2s) - 2 i d(m-2k) \sqrt{z})^2}{4 d(m-2k)}\right) \right) \left. \right) \left. \right) (-i d(m-2k))^{-2(n+1)} +
 \end{aligned}$$

$$e^{-\frac{ic^2(v-2s)^2}{4d(m-2k)} - ig(v-2s) + \frac{i\pi v}{2} - \frac{im\pi}{2}} (i d(m-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n}$$

$$\begin{aligned}
 & (2 i d(m-2 k) \sqrt{z}-i c(v-2 s))^{h+j}\left(\frac{i\left(2 i d(m-2 k) \sqrt{z}-i c(v-2 s)\right)^2}{d(m-2 k)}\right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j}\left(2 i d(m-2 k) \sqrt{\frac{i\left(2 i d(m-2 k) \sqrt{z}-i c(v-2 s)\right)^2}{d(m-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2),\right.\right. \\
 & \left.\left.\frac{i\left(2 i d(m-2 k) \sqrt{z}-i c(v-2 s)\right)^2}{4 d(m-2 k)}\right)-i c(v-2 s)\left(2 i d(m-2 k) \sqrt{z}-i c(v-2 s)\right)\right. \\
 & \left.\left.\Gamma\left(\frac{1}{2}(h+j+1), \frac{i\left(2 i d(m-2 k) \sqrt{z}-i c(v-2 s)\right)^2}{4 d(m-2 k)}\right)\right)\right)+e^{\frac{i c^2(v-2 s)^2}{4 d(m-2 k)}+g i(v-2 s)-\frac{i \pi v}{2}-\frac{i m \pi}{2}} \\
 & (i d(m-2 k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j(-1)^{j-h} 4^j(i c(v-2 s))^{-h-j+2 n}\left(2 d i \sqrt{z}(m-2 k)+c i(v-2 s)\right)^{h+j} \\
 & \left(\frac{i\left(2 d i \sqrt{z}(m-2 k)+c i(v-2 s)\right)^2}{d(m-2 k)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} c i(v-2 s) \\
 & \left(2 d i \sqrt{z}(m-2 k)+c i(v-2 s)\right) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i\left(2 d i \sqrt{z}(m-2 k)+c i(v-2 s)\right)^2}{4 d(m-2 k)}\right)+ \\
 & 2 d i(m-2 k) \sqrt{\frac{i\left(2 d i \sqrt{z}(m-2 k)+c i(v-2 s)\right)^2}{d(m-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left.\left.\frac{i\left(2 d i \sqrt{z}(m-2 k)+c i(v-2 s)\right)^2}{4 d(m-2 k)}\right)\right) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^n \sin^m(d z+e) \sin^v(c z^r+g)$

01.06.21.1218.01

$$\int z^n \sin^m(e+d z) \sin^v(c z^2+g) d z =$$

$$-2^{-m-v-1} \binom{m}{\frac{m}{2}}(1-m \bmod 2)\left(\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor}(-1)^k \binom{v}{k}\left(e^{i g(v-2 k)-\frac{i \pi v}{2}} \Gamma\left(\frac{n+1}{2},-i c(v-2 k) z^2\right)\left(-i c(v-2 k) z^2\right)^{\frac{1}{2}(-n-1)}+\right.\right.$$

$$\begin{aligned}
 & \left. e^{\frac{i\pi v}{2} - i g(v-2k)} (i c(v-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i c(v-2k) z^2\right) \right\} z^{n+1} + \\
 & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} + (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{i m \pi}{2} - i e(m-2k)} \Gamma(n+1, i d(m-2k) z) (-i d(m-2k))^{-n-1} + \right. \\
 & \quad \left. e^{i e(m-2k) - \frac{i m \pi}{2}} (i d(m-2k))^{-n-1} \Gamma(n+1, -i d(m-2k) z) \right) - \\
 & 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{d^2 i(m-2k)^2}{4c(v-2s)} - i e(m-2k) + \frac{i\pi v}{2} - i g(v-2s) + \frac{i m \pi}{2}} \right. \\
 & \quad \left( \sum_{j=0}^n 2^{j-n} (i d(m-2k))^{n-j} (-i d(m-2k) - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(-i d(m-2k) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-i d(m-2k) - 2 i c(v-2s) z)^2}{4c(v-2s)}\right) \right) (-i c(v-2s))^{-n-1} + \right. \\
 & \quad \left. e^{\frac{d^2 i(m-2k)^2}{4c(v-2s)} + i e(m-2k) + \frac{i\pi v}{2} - i g(v-2s) - \frac{i m \pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (-i d(m-2k))^{n-j} (i d(m-2k) - 2 i c(v-2s) z)^{j+1} \right. \right. \\
 & \quad \left. \left. \left( -\frac{i(i d(m-2k) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(i d(m-2k) - 2 i c(v-2s) z)^2}{4c(v-2s)}\right) \right) \right) \\
 & \quad (-i c(v-2s))^{-n-1} + e^{-\frac{i d^2(m-2k)^2}{4c(v-2s)} - i e(m-2k) + g i(v-2s) - \frac{i\pi v}{2} + \frac{i m \pi}{2}} (i c(v-2s))^{-n-1} \\
 & \quad \sum_{j=0}^n 2^{j-n} (i d(m-2k))^{n-j} (2 i c(v-2s) z - i d(m-2k))^{j+1} \left( \frac{i(2 i c(v-2s) z - i d(m-2k))^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \quad \Gamma\left(\frac{j+1}{2}, \frac{i(2 i c(v-2s) z - i d(m-2k))^2}{4c(v-2s)}\right) + e^{-\frac{i d^2(m-2k)^2}{4c(v-2s)} + i e(m-2k) + g i(v-2s) - \frac{i\pi v}{2} - \frac{i m \pi}{2}} (i c(v-2s))^{-n-1} \\
 & \quad \sum_{j=0}^n 2^{j-n} (-i d(m-2k))^{n-j} (d i(m-2k) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(d i(m-2k) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \quad \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d i(m-2k) + 2 c i(v-2s) z)^2}{4c(v-2s)}\right) \right) \right\} ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1219.01

$$\int z^n \sin^m(dz + e) \sin^v(\sqrt{z} c + g) dz = \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} +$$

$$(-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{im\pi}{2} - ie(m-2k)} \Gamma(n + 1, id(m-2k)z) (-id(m-2k))^{-n-1} +$$

$$e^{ie(m-2k) - \frac{im\pi}{2}} (id(m-2k))^{-n-1} \Gamma(n + 1, -id(m-2k)z) \right) + 2^{-m-v+1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+n} \binom{v}{k}$$

$$(c(v-2k))^{-2(n+1)} \left( e^{ig(v-2k) - \frac{i\pi v}{2}} \Gamma(2(n+1), -ic(v-2k)\sqrt{z}) + e^{\frac{i\pi v}{2} - ig(v-2k)} \Gamma(2(n+1), ic(v-2k)\sqrt{z}) \right) +$$

$$2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2 i(v-2s)^2}{4d(m-2k)} - ig(v-2s) - ie(m-2k) + \frac{i\pi v}{2} + \frac{im\pi}{2}}$$

$$\left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (-2id\sqrt{z}(m-2k) - ic(v-2s))^{h+j}$$

$$\left( -\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2s)(-2id\sqrt{z}(m-2k) -$$

$$ic(v-2s)) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{4d(m-2k)} \right) -$$

$$2id(m-2k) \sqrt{-\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{d(m-2k)}} \Gamma\left( \frac{1}{2}(h+j+2),$$

$$-\frac{i(-2id\sqrt{z}(m-2k) - ic(v-2s))^2}{4d(m-2k)} \right) \right) \left( (-id(m-2k))^{-2(n+1)} +$$

$$e^{\frac{c^2 i(v-2s)^2}{4d(m-2k)} + g i(v-2s) - ie(m-2k) - \frac{i\pi v}{2} + \frac{im\pi}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ic(v-2s) - 2id$$

$$\begin{aligned}
 & (m-2k)\sqrt{z} \left( -\frac{i(i c(v-2s) - 2 i d(m-2k)\sqrt{z})^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( i c(v-2s) \right. \\
 & \left. (i c(v-2s) - 2 i d(m-2k)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(i c(v-2s) - 2 i d(m-2k)\sqrt{z})^2}{4 d(m-2k)} \right) \right. \\
 & \left. 2 i d(m-2k) \sqrt{-\frac{i(i c(v-2s) - 2 i d(m-2k)\sqrt{z})^2}{d(m-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(i c(v-2s) - 2 i d(m-2k)\sqrt{z})^2}{4 d(m-2k)} \right) \right) \left( (-i d(m-2k))^{-2(n+1)} + \right. \\
 & \left. e^{-\frac{i c^2(v-2s)^2}{4 d(m-2k)} - i g(v-2s) + e i(m-2k) + \frac{i \pi v}{2} - \frac{i m \pi}{2}} (i d(m-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n} \right. \\
 & \left. (2 i d(m-2k)\sqrt{z} - i c(v-2s)) \left( \frac{i(2 i d(m-2k)\sqrt{z} - i c(v-2s))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2 i d(m-2k) \sqrt{\frac{i(2 i d(m-2k)\sqrt{z} - i c(v-2s))^2}{d(m-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. \frac{i(2 i d(m-2k)\sqrt{z} - i c(v-2s))^2}{4 d(m-2k)} \right) - i c(v-2s)(2 i d(m-2k)\sqrt{z} - i c(v-2s)) \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(2 i d(m-2k)\sqrt{z} - i c(v-2s))^2}{4 d(m-2k)} \right) \right) \right) + e^{-\frac{i c^2(v-2s)^2}{4 d(m-2k)} + g i(v-2s) + e i(m-2k) - \frac{i \pi v}{2} - \frac{i m \pi}{2}} \\
 & (i d(m-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} (2 d i \sqrt{z} (m-2k) + c i(v-2s))^{h+j} \\
 & \left( \frac{i(2 d i \sqrt{z} (m-2k) + c i(v-2s))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2s) \right.
 \end{aligned}$$

$$\left. \left. \left. (2di\sqrt{z}(m-2k) + ci(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(2di\sqrt{z}(m-2k) + ci(v-2s))^2}{4d(m-2k)}\right) + \right. \right. \right. \\ \left. \left. \left. 2di(m-2k) \sqrt{\frac{i(2di\sqrt{z}(m-2k) + ci(v-2s))^2}{d(m-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right. \\ \left. \left. \left. \frac{i(2di\sqrt{z}(m-2k) + ci(v-2s))^2}{4d(m-2k)}\right) \right) \right) \right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} \sin^m(bz^r) \sin^v(cz^r + g)$

01.06.21.1220.01

$$\int z^{\alpha-1} \sin^m(bz^r) \sin^v(cz^r + g) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^\alpha \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{\alpha} - \frac{1}{r} \left( i^{-m} 2^{-m-v} z^\alpha \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \right. \\ \left. \left( (-1)^m \Gamma\left(\frac{\alpha}{r}, (ibm - 2ibk)z^r\right) ((ibm - 2ibk)z^r)^{-\frac{\alpha}{r}} + ((2ibk - ibm)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ibk - ibm)z^r\right) \right) \right) - \\ \frac{1}{r} \left( (-1)^m i^{-v} 2^{-m-v} z^\alpha \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{2igk-igv} \Gamma\left(\frac{\alpha}{r}, (icv - 2ick)z^r\right) ((icv - 2ick)z^r)^{-\frac{\alpha}{r}} + \right. \right. \\ \left. \left. e^{igv-2igk} ((2ick - icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ick - icv)z^r\right) \right) \right) - \\ \frac{1}{r} \left( (2i)^{-m-v} z^\alpha \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{m+v} e^{2igs-igv} \Gamma\left(\frac{\alpha}{r}, (-2bik + ibm - 2ics + icv)z^r\right) \right. \right. \\ \left. \left. ((-2bik + ibm - 2ics + icv)z^r)^{-\frac{\alpha}{r}} + (-1)^v e^{2igs-igv} ((2ibk - ibm - 2ics + icv)z^r)^{-\frac{\alpha}{r}} \right. \right. \\ \left. \left. \Gamma\left(\frac{\alpha}{r}, (2ibk - ibm - 2ics + icv)z^r\right) + (-1)^m e^{igv-2igs} ((-2bik + ibm + 2ics - icv)z^r)^{-\frac{\alpha}{r}} \right. \right. \\ \left. \left. \Gamma\left(\frac{\alpha}{r}, (-2bik + ibm + 2ics - icv)z^r\right) + e^{igv-2igs} ((2ibk - ibm + 2ics - icv)z^r)^{-\frac{\alpha}{r}} \right. \right. \\ \left. \left. \Gamma\left(\frac{\alpha}{r}, (2ibk - ibm + 2ics - icv)z^r\right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$



01.06.21.1221.01

$$\int z^n \sin^m(b z^2) \sin^v(c z^2 + g) dz =$$

$$\begin{aligned} & -2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{i m \pi}{2}} \Gamma\left(\frac{n+1}{2}, -i b(m-2k) z^2\right) (-i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} + \right. \\ & \quad \left. e^{\frac{i m \pi}{2}} (i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i b(m-2k) z^2\right) \right) - \\ & 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{i g(v-2s) - \frac{i v \pi}{2}} \Gamma\left(\frac{n+1}{2}, -i c(v-2s) z^2\right) (-i c(v-2s) z^2)^{\frac{1}{2}(-n-1)} + \right. \\ & \quad \left. e^{\frac{i v \pi}{2} - i g(v-2s)} (i c(v-2s) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i c(v-2s) z^2\right) \right) - 2^{-m-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\ & \quad \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{2} i \pi(m-v) - i g(v-2s)} \Gamma\left(\frac{n+1}{2}, (i c(v-2s) - i b(m-2k)) z^2\right) ((i c(v-2s) - i b(m-2k)) z^2)^{\frac{1}{2}(-n-1)} + \right. \\ & \quad \left. e^{\frac{1}{2} i(m+v)\pi - i g(v-2s)} ((b i(m-2k) + c i(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (b i(m-2k) + c i(v-2s)) z^2\right) + \right. \\ & \quad \left. e^{i g(v-2s) - \frac{1}{2} i(m+v)\pi} ((-i b(m-2k) - i c(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-i b(m-2k) - i c(v-2s)) z^2\right) + \right. \\ & \quad \left. e^{\frac{1}{2} i \pi(m-v) + g i(v-2s)} ((i b(m-2k) - i c(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b(m-2k) - i c(v-2s)) z^2\right) \right) + \\ & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \end{aligned}$$

$\mathbb{N}^+$

01.06.21.1222.01

$$\begin{aligned}
 \int z^n \sin^m(b \sqrt{z}) \sin^v(\sqrt{z} c + g) dz &= (-1)^n 2^{-m-v+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) b^{-2(n+1)} \\
 &\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^{-2(n+1)} \left( e^{-\frac{im\pi}{2}} \Gamma(2(n+1), -ib(m-2k)\sqrt{z}) + e^{\frac{im\pi}{2}} \Gamma(2(n+1), ib(m-2k)\sqrt{z}) \right) + \\
 &\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + (-1)^n 2^{-m-v+1} c^{-2(n+1)} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \\
 &\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} (v-2s)^{-2(n+1)} \left( e^{ig(v-2s) - \frac{iv\pi}{2}} \Gamma(2(n+1), -ic(v-2s)\sqrt{z}) + e^{\frac{iv\pi}{2} - ig(v-2s)} \Gamma(2(n+1), ic(v-2s)\sqrt{z}) \right) - \\
 &2^{-m-v+1} z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{2}i\pi(m-v) - ig(v-2s)} \Gamma(2(n+1), (ic(v-2s) - ib(m-2k))\sqrt{z}) \right. \\
 &\left. ((ic(v-2s) - ib(m-2k))\sqrt{z})^{-2(n+1)} + e^{\frac{1}{2}i(m+v)\pi - ig(v-2s)} ((ib(m-2k) + ci(v-2s))\sqrt{z})^{-2(n+1)} \right. \\
 &\left. \Gamma(2(n+1), (ib(m-2k) + ci(v-2s))\sqrt{z}) + e^{ig(v-2s) - \frac{1}{2}i(m+v)\pi} ((-ib(m-2k) - ic(v-2s))\sqrt{z})^{-2(n+1)} \right. \\
 &\left. \Gamma(2(n+1), (-ib(m-2k) - ic(v-2s))\sqrt{z}) + e^{\frac{1}{2}i\pi(m-v) + gi(v-2s)} ((ib(m-2k) - ic(v-2s))\sqrt{z})^{-2(n+1)} \right. \\
 &\left. \Gamma(2(n+1), (ib(m-2k) - ic(v-2s))\sqrt{z}) \right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^{\alpha-1} \sin^m(bz^r + e) \sin^v(cz^r + g)$

01.06.21.1223.01

$$\int z^{\alpha-1} \sin^m(bz^r + e) \sin^v(cz^r + g) dz = \frac{(-1)^m 2^{-m-v} (1-m \bmod 2) (1-v \bmod 2)}{\alpha} z^\alpha \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} -$$

$$\frac{i^{-m} 2^{-m-v} z^\alpha}{r} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m e^{2ike-ime} \Gamma\left(\frac{\alpha}{r}, (ibm-2ibk)z^r\right) ((ibm-2ibk)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. e^{ime-2ike} ((2ibk-ibm)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ibk-ibm)z^r\right) \right) -$$

$$\frac{(-1)^m i^{-v} 2^{-m-v} z^\alpha}{r} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{2igk-igv} \Gamma\left(\frac{\alpha}{r}, (icv-2ick)z^r\right) ((icv-2ick)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. e^{igv-2igk} ((2ick-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ick-icv)z^r\right) \right) -$$

$$\frac{i^{-m-v} 2^{-m-v} z^\alpha}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{m+v} e^{2ike-ime+2igs-igv} \Gamma\left(\frac{\alpha}{r}, (-2bik+ibm-2ics+icv)z^r\right) \right.$$

$$\left. ((-2bik+ibm-2ics+icv)z^r)^{-\frac{\alpha}{r}} + (-1)^v e^{-2ike+ime+2igs-igv} ((2bik-ibm-2ics+icv)z^r)^{-\frac{\alpha}{r}} \right.$$

$$\left. \Gamma\left(\frac{\alpha}{r}, (2bik-ibm-2ics+icv)z^r\right) + (-1)^m e^{2ike-ime-2igs+igv} \right.$$

$$\left. ((-2bik+ibm+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-2bik+ibm+2ics-icv)z^r\right) + e^{-2ike+ime-2igs+igv} \right.$$

$$\left. ((2bik-ibm+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2bik-ibm+2ics-icv)z^r\right) \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1224.01

$$\int z^n \sin^m(bz^2 + e) \sin^v(cz^2 + g) dz =$$

$$\begin{aligned} & -2^{-m-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{ie(m-2k) - \frac{im\pi}{2}} \Gamma\left(\frac{n+1}{2}, -ib(m-2k)z^2\right) (-ib(m-2k)z^2)^{\frac{1}{2}(-n-1)} + \right. \\ & \quad \left. e^{\frac{im\pi}{2} - ie(m-2k)} (ib(m-2k)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ib(m-2k)z^2\right) \right) - \\ & 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{ig(v-2s) - \frac{iv\pi}{2}} \Gamma\left(\frac{n+1}{2}, -ic(v-2s)z^2\right) (-ic(v-2s)z^2)^{\frac{1}{2}(-n-1)} + \right. \\ & \quad \left. e^{\frac{iv\pi}{2} - ig(v-2s)} (ic(v-2s)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ic(v-2s)z^2\right) \right) - \\ & 2^{-m-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{ie(m-2k) - ig(v-2s) - \frac{1}{2}i(m-v)\pi} \Gamma\left(\frac{n+1}{2}, (ic(v-2s) - ib(m-2k))z^2\right) \right. \\ & \quad \left( (ic(v-2s) - ib(m-2k))z^2 \right)^{\frac{1}{2}(-n-1)} + e^{-ie(m-2k) + \frac{1}{2}i\pi(m+v) - ig(v-2s)} \left( (bi(m-2k) + ci(v-2s))z^2 \right)^{\frac{1}{2}(-n-1)} \\ & \quad \Gamma\left(\frac{n+1}{2}, (bi(m-2k) + ci(v-2s))z^2\right) + e^{ie(m-2k) + gi(v-2s) - \frac{1}{2}i(m+v)\pi} \\ & \quad \left( (-ib(m-2k) - ic(v-2s))z^2 \right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib(m-2k) - ic(v-2s))z^2\right) + \\ & \quad \left. e^{-ie(m-2k) + \frac{1}{2}i\pi(m-v) + gi(v-2s)} \left( (ib(m-2k) - ic(v-2s))z^2 \right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib(m-2k) - ic(v-2s))z^2\right) \right) + \\ & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} \quad ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1225.01

$$\int z^n \sin^m(\sqrt{z} b + e) \sin^v(\sqrt{z} c + g) dz = (-1)^n 2^{-m-v+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) b^{-2(n+1)} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^{-2(n+1)}$$

$$\left( e^{i e(m-2k) - \frac{i m \pi}{2}} \Gamma(2(n+1), -i b(m-2k) \sqrt{z}) + e^{\frac{i m \pi}{2} - i e(m-2k)} \Gamma(2(n+1), i b(m-2k) \sqrt{z}) \right) +$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + (-1)^n 2^{-m-v+1} c^{-2(n+1)} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} (v-2s)^{-2(n+1)} \left( e^{i g(v-2s) - \frac{i v \pi}{2}} \Gamma(2(n+1), -i c(v-2s) \sqrt{z}) + e^{\frac{i v \pi}{2} - i g(v-2s)} \Gamma(2(n+1), i c(v-2s) \sqrt{z}) \right) -$$

$$2^{-m-v+1} z^{n+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{i(m-2k) - i g(v-2s) - \frac{1}{2} i(m-v)\pi} \Gamma(2(n+1), (i c(v-2s) - i b(m-2k)) \sqrt{z}) \right.$$

$$\left. \left( (i c(v-2s) - i b(m-2k)) \sqrt{z} \right)^{-2(n+1)} + e^{-i e(m-2k) + \frac{1}{2} i \pi(m+v) - i g(v-2s)} \right.$$

$$\left. \left( (b i(m-2k) + c i(v-2s)) \sqrt{z} \right)^{-2(n+1)} \Gamma(2(n+1), (b i(m-2k) + c i(v-2s)) \sqrt{z}) + \right.$$

$$e^{e i(m-2k) + g i(v-2s) - \frac{1}{2} i(m+v)\pi} \left( (-i b(m-2k) - i c(v-2s)) \sqrt{z} \right)^{-2(n+1)} \Gamma(2(n+1),$$

$$\left. (-i b(m-2k) - i c(v-2s)) \sqrt{z} \right) + e^{-i e(m-2k) + \frac{1}{2} i \pi(m-v) + g i(v-2s)} \left( (i b(m-2k) - i c(v-2s)) \sqrt{z} \right)^{-2(n+1)}$$

$$\Gamma(2(n+1), (i b(m-2k) - i c(v-2s)) \sqrt{z}) \Big) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin^m(dz) \sin^v(cz^2 + fz)$

01.06.21.1226.01

$$\int z^n \sin^m(dz) \sin^v(cz^2 + fz) dz =$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( e^{\frac{i m \pi}{2}} \Gamma(n+1, i d(m-2k)z) (-i d(m-2k))^{-n-1} + e^{-\frac{1}{2} i m \pi} (i d(m-2k))^{-n-1} \Gamma(n+1, -i d(m-2k)z) \right) -$$

$$2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i \pi v}{2}} \left( \sum_{j=0}^n 2^{j-n} (i f(v-2k))^{n-j} (-i f(v-2k) - 2i c z(v-2k))^{j+1} \right. \right.$$

$$\left. \left( -\frac{i(-i f(v-2k) - 2i c z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-i f(v-2k) - 2i c z(v-2k))^2}{4c(v-2k)}\right) \right)$$

$$(-i c(v-2k))^{-n-1} + e^{-\frac{i(v-2k)f^2}{4c} - \frac{i \pi v}{2}} (i c(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f(v-2k))^{n-j} (f i(v-2k) + 2c i z(v-2k))^{j+1}$$

$$\begin{aligned}
 & \left( \frac{i(f i(v-2k) + 2c i z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f i(v-2k) + 2c i z(v-2k))^2}{4c(v-2k)}\right) - 2^{-m-v-1} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{1}{2} i \pi(m+v) - \frac{i(-i d(m-2k) - i f(v-2s))^2}{4c(v-2s)}} \left( \sum_{j=0}^n 2^{j-n} (d i(m-2k) + f i(v-2s))^{n-j} (-i d(m-2k) - \right. \right. \\
 & \quad \left. \left. i f(v-2s) - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(-i d(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \right. \\
 & \quad \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-i d(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{4c(v-2s)}\right) \right) (-i c(v-2s))^{-n-1} + \right. \\
 & \quad \left. e^{\frac{1}{2} i \pi(v-m) - \frac{i(i d(m-2k) - i f(v-2s))^2}{4c(v-2s)}} \left( \sum_{j=0}^n 2^{j-n} (i f(v-2s) - i d(m-2k))^{n-j} (d i(m-2k) - i f(v-2s) - \right. \right. \\
 & \quad \left. \left. 2 i c(v-2s) z)^{j+1} \left( -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right. \right. \\
 & \quad \left. \left. \Gamma\left(\frac{j+1}{2}, -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{4c(v-2s)}\right) \right) (-i c(v-2s))^{-n-1} + \right. \\
 & \quad \left. e^{\frac{i(i f(v-2s) - i d(m-2k))^2}{4c(v-2s)} + \frac{1}{2} i \pi(m-v)} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i d(m-2k) - i f(v-2s))^{n-j} (-i d(m-2k) + \right. \\
 & \quad \left. f i(v-2s) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{4c(v-2s)}\right) \right) + \\
 & \quad \left. e^{\frac{i(d i(m-2k) + f i(v-2s))^2}{4c(v-2s)} - \frac{1}{2} i \pi(m+v)} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i d(m-2k) - i f(v-2s))^{n-j} \right. \\
 & \quad \left. (d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{4c(v-2s)}\right) \right) \Bigg/ ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1227.01

$$\int z^n \sin^m(dz) \sin^v(\sqrt{z} c + fz) dz =$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} + (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( e^{\frac{im\pi}{2}} \Gamma(n+1, id(m-2k)z) (-id(m-2k))^{-n-1} + e^{-\frac{im\pi}{2}} (id(m-2k))^{-n-1} \Gamma(n+1, -id(m-2k)z) \right) +$$

$$2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+n-1} (f(v-2k))^{-2(n+1)} \binom{v}{k}$$

$$\left( e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k))^{-h-j+2n} (ci(v-2k) + 2fi\sqrt{z}(v-2k))^{h+j} \right.$$

$$\left. \left( \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2k)(ci(v-2k) + 2fi\sqrt{z}(v-2k)) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) + 2fi(v-2k) \right. \right.$$

$$\left. \left. \sqrt{\frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \right) +$$

$$e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2k))^{-h-j+2n} (-ic(v-2k) - 2if\sqrt{z}(v-2k))^{h+j}$$

$$\left( -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2k) \right.$$

$$\left. (-ic(v-2k) - 2if\sqrt{z}(v-2k)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) - \right.$$

$$\left. 2if(v-2k) \sqrt{-\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. \left. - \frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2(v-2s)^2}{4(if(v-2s) - id(m-2k))} + \frac{1}{2}i\pi(m-v)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} \right. \right. \\
 & \quad (ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^{h+j} \\
 & \quad \left. \left. \left( - \frac{(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2}{if(v-2s) - id(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right. \\
 & \quad \left. \left. \binom{n}{j} \left( ci(v-2s)(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z}) \right. \right. \right. \\
 & \quad \left. \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), - (ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2 \right) \right. \right. \right. \\
 & \quad \left. \left. \left. (4(if(v-2s) - id(m-2k))) \right) + 2(if(v-2s) - id(m-2k)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \quad \left. \left. \left. - (ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2 \right) / (4(if(v-2s) - id(m-2k))) \right) \right) \right) \\
 & \quad \left. \left. \left. \left. \sqrt{\left( - (ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2 \right) / (if(v-2s) - id(m-2k)) \right) \right) \right) \right) \\
 & (if(v-2s) - id(m-2k))^{-2(n+1)} + e^{\frac{c^2(v-2s)^2}{4(di(m-2k) + fi(v-2s))} - \frac{1}{2}i\pi(m+v)} (di(m-2k) + fi(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ci(v-2s) + 2(di(m-2k) + fi(v-2s))\sqrt{z})^{h+j} \\
 & \left( - \frac{(ci(v-2s) + 2(di(m-2k) + fi(v-2s))\sqrt{z})^2}{di(m-2k) + fi(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( ci(v-2s)(ci(v-2s) + 2(di(m-2k) + fi(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \quad \left. \left. - \frac{(ci(v-2s) + 2(di(m-2k) + fi(v-2s))\sqrt{z})^2}{4(di(m-2k) + fi(v-2s))} \right) + 2(di(m-2k) + fi(v-2s)) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{1}{2} (h+j+2), -\frac{(c i (v-2 s)+2(d i(m-2 k)+f i(v-2 s)) \sqrt{z})^2}{4(d i(m-2 k)+f i(v-2 s))} \right) \\
 & \sqrt{\left( -(c i (v-2 s)+2(d i(m-2 k)+f i(v-2 s)) \sqrt{z})^2 / (d i(m-2 k)+f i(v-2 s)) \right)} + \\
 & e^{\frac{c^2(v-2s)^2}{4(-id(m-2k)-if(v-2s))} + \frac{1}{2} i \pi (m+v)} (-i d(m-2 k)-i f(v-2 s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2 s))^{-h-j+2 n} (2(-i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^{h+j} \\
 & \left( -(2(-i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2 / (-i d(m-2 k)-i f(v-2 s)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( 2(-i d(m-2 k)-i f(v-2 s)) \sqrt{\left( -(2(-i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2 / \right. \right. \\
 & \quad \left. \left. (-i d(m-2 k)-i f(v-2 s)) \right) \right) \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \quad \left. -(2(-i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2 / (4(-i d(m-2 k)-i f(v-2 s))) \right) - \\
 & \quad i c(v-2 s) (2(-i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s)) \Gamma\left(\frac{1}{2}(h+j+1), \right. \\
 & \quad \left. -(2(-i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2 / (4(-i d(m-2 k)-i f(v-2 s))) \right) \Big) + \\
 & e^{\frac{c^2(v-2s)^2}{4(id(m-2k)-if(v-2s))} + \frac{1}{2} i \pi (v-m)} (i d(m-2 k)-i f(v-2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j \\
 & (-i c(v-2 s))^{-h-j+2 n} (2(i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^{h+j} \\
 & \left( -\frac{(2(i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2}{i d(m-2 k)-i f(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(i d(m-2 k)-i f(v-2 s)) \right. \\
 & \quad \left. \sqrt{\left( -(2(i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2 / (i d(m-2 k)-i f(v-2 s)) \right)} \right) \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(2(i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s))^2}{4(i d(m-2 k)-i f(v-2 s))} \right) - \\
 & \quad i c(v-2 s) (2(i d(m-2 k)-i f(v-2 s)) \sqrt{z}-i c(v-2 s)) \Gamma\left(\frac{1}{2}(h+j+1), \right.
 \end{aligned}$$

### Involving $z^n \sin^m(dz + e) \sin^v(cz' + fz)$

01.06.21.1228.01

$$\int z^n \sin^m(dz + e) \sin^v(cz' + fz) dz = \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} +$$

$$(-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{im\pi}{2} - ie(m-2k)} \Gamma(n + 1, id(m-2k)z) (-id(m-2k))^{-n-1} + \right.$$

$$\left. e^{ie(m-2k) - \frac{im\pi}{2}} (id(m-2k))^{-n-1} \Gamma(n + 1, -id(m-2k)z) \right) -$$

$$2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i\pi v}{2}} \left( \sum_{j=0}^n 2^{j-n} (if(v-2k))^{n-j} (-if(v-2k) - 2icz(v-2k))^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-if(v-2k) - 2icz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-if(v-2k) - 2icz(v-2k))^2}{4c(v-2k)}\right) \right) \right)$$

$$(-ic(v-2k))^{-n-1} + e^{-\frac{i(v-2k)f^2}{4c} - \frac{i\pi v}{2}} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2k))^{n-j} (fi(v-2k) + 2icz(v-2k))^{j+1}$$

$$\left( \frac{i(fi(v-2k) + 2icz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2k) + 2icz(v-2k))^2}{4c(v-2k)}\right) \right) -$$

$$2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-id(m-2k) - if(v-2s))^2}{4c(v-2s)} - ie(m-2k) + \frac{1}{2}i\pi(m+v)} \right.$$

$$\left( \sum_{j=0}^n 2^{j-n} (di(m-2k) + fi(v-2s))^{n-j} (-id(m-2k) - if(v-2s) - 2ic(v-2s)z)^{j+1} \right.$$

$$\left. \left( -\frac{i(-id(m-2k) - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right.$$

$$\left. \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(m-2k) - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) (-ic(v-2s))^{-n-1} +$$

$$e^{-\frac{i(id(m-2k) - if(v-2s))^2}{4c(v-2s)} + ie(m-2k) + \frac{1}{2}i\pi(v-m)} \left( \sum_{j=0}^n 2^{j-n} (if(v-2s) - id(m-2k))^{n-j} (di(m-2k) - \right.$$

$$\begin{aligned}
 & i f(v-2s) - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{4 c(v-2s)}\right) \left( -i c(v-2s) \right)^{-n-1} + \\
 & e^{\frac{i(i f(v-2s) - i d(m-2k))^2}{4 c(v-2s)} - i e(m-2k) + \frac{1}{2} i \pi(m-v)} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i d(m-2k) - i f(v-2s))^{n-j} (-i d(m-2k) + \\
 & f i(v-2s) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{4 c(v-2s)}\right) + \\
 & e^{\frac{i(d i(m-2k) + f i(v-2s))^2}{4 c(v-2s)} + e i(m-2k) - \frac{1}{2} i \pi(m+v)} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i d(m-2k) - i f(v-2s))^{n-j} \\
 & (d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{4 c(v-2s)}\right) \Bigg) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1229.01

$$\begin{aligned}
 \int z^n \sin^m(dz + e) \sin^v(\sqrt{z} c + fz) dz = & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + \\
 & (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{i m \pi}{2} - i e(m-2k)} \Gamma(n+1, i d(m-2k) z) (-i d(m-2k))^{-n-1} + \right. \\
 & \left. e^{i e(m-2k) - \frac{i m \pi}{2}} (i d(m-2k))^{-n-1} \Gamma(n+1, -i d(m-2k) z) \right) + 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+n-1} \\
 & (f(v-2k))^{-2(n+1)} \binom{v}{k} \left( e^{-\frac{i(v-2k)c^2}{4f} - \frac{i \pi v}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k))^{-h-j+2n} (c i(v-2k) + 2 f i \sqrt{z} (v-2k))^{h+j} \right. \\
 & \left. \left( \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2k) (c i(v-2k) + 2 f i \sqrt{z} (v-2k)) \Gamma \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{1}{2} (h+j+1), \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) + 2 f i (v-2k) \\
 & \sqrt{\frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f (v-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) + \\
 & e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c (v-2k))^{-h-j+2n} (-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^{h+j} \\
 & \left( -\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f (v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i c (v-2k) \right. \\
 & \left. (-i c (v-2k) - 2 i f \sqrt{z} (v-2k)) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) \right) - \\
 & 2 i f (v-2k) \sqrt{-\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f (v-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \right. \\
 & \left. \left. -\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) \right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2(v-2s)^2}{4(i f (v-2s) - i d (m-2k))} - i e (m-2k) + \frac{1}{2} i \pi (m-v)} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c (v-2s))^{-h-j+2n} (c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z})^2}{i f (v-2s) - i d (m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right. \\
 & \left. \left. \binom{n}{j} (c i (v-2s) (c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z}) \right) \right. \\
 & \left. \Gamma \left( \frac{1}{2} (h+j+1), -(c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z})^2 / \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( (4(i f(v-2s) - i d(m-2k))) \right) + 2(i f(v-2s) - i d(m-2k)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -(c i(v-2s) + 2(i f(v-2s) - i d(m-2k)) \sqrt{z})^2 / (4(i f(v-2s) - i d(m-2k))) \right) \right) \\
 & \left. \sqrt{\left( -(c i(v-2s) + 2(i f(v-2s) - i d(m-2k)) \sqrt{z})^2 / (i f(v-2s) - i d(m-2k)) \right)} \right) \\
 & (i f(v-2s) - i d(m-2k))^{-2(n+1)} + e^{\frac{c^2(v-2s)^2}{4(d i(m-2k) + f i(v-2s))} + i(m-2k) - \frac{1}{2} i \pi(m+v)} (d i(m-2k) + f i(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} (c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^{h+j} \\
 & \left( -\frac{(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2}{d i(m-2k) + f i(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i(v-2s) (c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2}{4(d i(m-2k) + f i(v-2s))} \right) + 2(d i(m-2k) + f i(v-2s)) \right) \\
 & \left( \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2}{4(d i(m-2k) + f i(v-2s))} \right) \right) \\
 & \left. \sqrt{\left( -(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2 / (d i(m-2k) + f i(v-2s)) \right)} \right) + \\
 & e^{\frac{c^2(v-2s)^2}{4(-i d(m-2k) - i f(v-2s))} - i e(m-2k) + \frac{1}{2} i \pi(m+v)} (-i d(m-2k) - i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n} (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^{h+j} \\
 & \left( -2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s) \right)^2 / (-i d(m-2k) - i f(v-2s))^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( 2(-i d(m-2k) - i f(v-2s)) \sqrt{\left( -2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s) \right)^2 / \right. \\
 & \left. (-i d(m-2k) - i f(v-2s)) \right) \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \left. -2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s) \right)^2 / (4(-i d(m-2k) - i f(v-2s))) - \\
 & i c(v-2s) (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\left(2(-id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s)\right)^2 / (4(-id(m-2k)-if(v-2s))) \Big) + \\
 & \frac{z^{2(v-2s)^2}}{e^{4(id(m-2k)-if(v-2s))+e i(m-2k)+\frac{1}{2}i\pi(v-m)}} (id(m-2k)-if(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (2(id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s))^{h+j} \\
 & \left( -\frac{(2(id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s))^2}{id(m-2k)-if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(id(m-2k)-if(v-2s)) \right. \\
 & \left. \sqrt{\left(2(id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s)\right)^2 / (id(m-2k)-if(v-2s))} \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(2(id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s))^2}{4(id(m-2k)-if(v-2s))}\right) - \right. \\
 & \left. ic(v-2s)(2(id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(2(id(m-2k)-if(v-2s))\sqrt{z}-ic(v-2s))^2}{4(id(m-2k)-if(v-2s))}\right) \right) \Big) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin^m(bz^r) \sin^v(cz^r + fz)$**

01.06.21.1230.01

$$\begin{aligned}
 \int z^n \sin^m(bz^2) \sin^v(cz^2 + fz) dz = & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2)(1-v \bmod 2)}{n+1} - \\
 & 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{1}{2}im\pi} z^{n+1} \Gamma\left(\frac{n+1}{2}, -ib(m-2k)z^2\right) (-ib(m-2k)z^2)^{\frac{1}{2}(-n-1)} + \right. \\
 & \left. e^{\frac{im\pi}{2}} z^{n+1} (ib(m-2k)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, ib(m-2k)z^2\right) \right) - \\
 & 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2 + i\pi v}{4c} + \frac{i\pi v}{2}} \left( \sum_{j=0}^n 2^{j-n} (if(v-2k))^{n-j} (-if(v-2k) - 2icz(v-2k))^{j+1} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{i(-if(v-2k)-2icz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-if(v-2k)-2icz(v-2k))^2}{4c(v-2k)}\right) \\
 & (-ic(v-2k))^{-n-1} + e^{\frac{i(v-2k)f^2-i\pi v}{4c}} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2k))^{n-j} (fi(v-2k)+2ciz(v-2k))^{j+1} \\
 & \left( \frac{i(fi(v-2k)+2ciz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2k)+2ciz(v-2k))^2}{4c(v-2k)}\right) - \\
 & 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{-2bk+bm+2cs-cv}-2\pi(m-v)\right)} \left( \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s)+ \right. \right. \\
 & \left. \left. 2(ic(v-2s)-ib(m-2k))z\right)^{j+1} \left( -\frac{(fi(v-2s)+2(ic(v-2s)-ib(m-2k))z)^2}{ic(v-2s)-ib(m-2k)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s)+2(ic(v-2s)-ib(m-2k))z)^2}{4(ic(v-2s)-ib(m-2k))}\right) \right) (ic(v-2s)-ib(m-2k))^{-n-1} + \\
 & e^{\frac{1}{4}i\left(\frac{f^2(v-2s)^2}{2bk-bm+2cs-cv}-2\pi(m+v)\right)} (bi(m-2k)+ci(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2s))^{n-j} (fi(v-2s)+ \\
 & 2(bi(m-2k)+ci(v-2s))z)^{j+1} \left( -\frac{(fi(v-2s)+2(bi(m-2k)+ci(v-2s))z)^2}{bi(m-2k)+ci(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(fi(v-2s)+2(bi(m-2k)+ci(v-2s))z)^2}{4(bi(m-2k)+ci(v-2s))}\right) + e^{\frac{1}{4}i\left(\frac{f^2(v-2s)^2}{2bk-bm+2cs-cv}-2\pi(m+v)\right)} \\
 & (-ib(m-2k)-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (2(-ib(m-2k)-ic(v-2s))z-if(v-2s))^{j+1} \\
 & \left( -\frac{(2(-ib(m-2k)-ic(v-2s))z-if(v-2s))^2}{-ib(m-2k)-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(2(-ib(m-2k)-ic(v-2s))z-if(v-2s))^2}{4(-ib(m-2k)-ic(v-2s))}\right) + e^{\frac{1}{4}i\left(2\pi(v-m)-\frac{f^2(v-2s)^2}{-2bk+bm+2cs-cv}\right)} \\
 & (ib(m-2k)-ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (2(ib(m-2k)-ic(v-2s))z-if(v-2s))^{j+1} \\
 & \left( -\frac{(2(ib(m-2k)-ic(v-2s))z-if(v-2s))^2}{ib(m-2k)-ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(2(ib(m-2k)-ic(v-2s))z-if(v-2s))^2}{4(ib(m-2k)-ic(v-2s))}\right) \Bigg| ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1231.01

$$\int z^n \sin^m(\sqrt{z} b) \sin^v(\sqrt{z} c + f z) dz = -(-1)^{n+1} 2^{-m-v+1} \left(\frac{v}{2}\right) (1-v \bmod 2)$$

$$\left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k (m-2k)^{-2(n+1)} \binom{m}{k} \left( e^{-\frac{1}{2} i m \pi} \Gamma(2(n+1), -i b(m-2k)\sqrt{z}) + e^{\frac{i m \pi}{2}} \Gamma(2(n+1), i b(m-2k)\sqrt{z}) \right) \right)$$

$$b^{-2(n+1)} + \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \left(\frac{v}{2}\right) (1-m \bmod 2) (1-v \bmod 2)}{n+1} + 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2k))^{-h-j+2n} (-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^{h+j} \right. \right.$$

$$\left. \left( -\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-i c(v-2k) \right.$$

$$\left. (-i c(v-2k) - 2 i f \sqrt{z} (v-2k)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f(v-2k)}\right) - 2 \right.$$

$$i f(v-2k) \sqrt{-\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f(v-2k)}} \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f(v-2k)}\right) \right) \right) (-i f(v-2k))^{-2(n+1)} +$$

$$e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2}} (i f(v-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k))^{-h-j+2n} (c i(v-2k) + 2 f i \sqrt{z} (v-2k))^{h+j}$$

$$\left( \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2k) (c i(v-2k) + 2 f i \sqrt{z} (v-2k)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f(v-2k)}\right) + 2 f i(v-2k) \right)$$



$$\begin{aligned}
 & \left. \left. \left. \sqrt{\frac{i(c i(v-2k) + 2 f i \sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c i(v-2k) + 2 f i \sqrt{z}(v-2k))^2}{4 f(v-2k)}\right)\right)\right)\right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{1}{2} i \pi(m+v) - \frac{i(-i b(m-2k) - i c(v-2s))^2}{4 f(v-2s)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j \right. \right. \\
 & \quad (-i b(m-2k) - i c(v-2s))^{-h-j+2n} (-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^{h+j} \\
 & \quad \left. \left. \left( -\frac{1}{f(v-2s)} \left( i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right. \\
 & \quad \left. \left. \binom{n}{j} \left( (-i b(m-2k) - i c(v-2s)) (-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right) \right. \right. \\
 & \quad \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} \left( i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right) \right) - \right. \\
 & \quad \left. \left. 2 i f(v-2s) \sqrt{\left( -\frac{1}{f(v-2s)} \left( i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right)} \right) \right) \\
 & \quad \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{1}{4 f(v-2s)} \left( i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right) \right) \right) \right) \\
 & (-i f(v-2s))^{-2(n+1)} + e^{\frac{1}{2} i \pi(v-m) - \frac{i(i b(m-2k) - i c(v-2s))^2}{4 f(v-2s)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b(m-2k) - i c(v-2s))^{-h-j+2n} \right. \\
 & \quad (b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^{h+j} \\
 & \quad \left. \left. \left( -\frac{i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right. \\
 & \quad \left. \left. \left( i b(m-2k) - i c(v-2s) \right) (b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right) \right) \\
 & \quad \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} \left( i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right) \right) - \right. \\
 & \quad \left. \left. 2 i f(v-2s) \sqrt{\left( -\frac{1}{f(v-2s)} \left( i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right)} \right) \right) \\
 & \quad \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{1}{4 f(v-2s)} \left( i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2 \right) \right) \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & (-i f(v-2s))^{-2(n+1)} + e^{\frac{i(i c(v-2s) - i b(m-2k))^2}{4 f(v-2s)} + \frac{1}{2} i \pi(m-v)} (i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s) - i b(m-2k))^{-h-j+2n} (-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (i c(v-2s) - i b(m-2k)) (-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z}) \right. \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), \frac{1}{4 f(v-2s)} \left( i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2 \right)^2 \right) + \\
 & \quad 2 f i(v-2s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{1}{4 f(v-2s)} \left( i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2 \right)^2 \right) \\
 & \quad \left. \sqrt{\left( \frac{1}{f(v-2s)} \left( i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2 \right)^2 \right)} \right) + \\
 & e^{\frac{i(b i(m-2k) + c i(v-2s))^2}{4 f(v-2s)} - \frac{1}{2} i \pi(m+v)} (i f(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b i(m-2k) + c i(v-2s))^{-h-j+2n} \\
 & (b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (b i(m-2k) + c i(v-2s)) (b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z}) \right. \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{4 f(v-2s)} \right) + \\
 & \quad 2 f i(v-2s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{4 f(v-2s)} \right) \\
 & \quad \left. \sqrt{\frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)}} \right) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n \sin^m(b z^r + e) \sin^v(c z^r + f z)$

01.06.21.1232.01

$$\int z^n \sin^m(bz^2 + e) \sin^v(cz^2 + fz) dz = \frac{2^{-m-v} z^{n+1} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} -$$

$$2^{-m-v-1} \left(\frac{v}{2}\right) (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{i e(m-2k) - \frac{i m \pi}{2}} z^{n+1} \Gamma\left(\frac{n+1}{2}, -i b(m-2k) z^2\right) (-i b(m-2k) z^2\right)^{\frac{1}{2}(-n-1)} +$$

$$e^{\frac{i m \pi}{2} - i e(m-2k)} z^{n+1} (i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i b(m-2k) z^2\right) -$$

$$2^{-m-v-1} \left(\frac{m}{2}\right) (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i \pi v}{2}} \left( \sum_{j=0}^n 2^{j-n} (i f(v-2k))^{n-j} (-i f(v-2k) - 2i c z(v-2k))^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-i f(v-2k) - 2i c z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-i f(v-2k) - 2i c z(v-2k))^2}{4c(v-2k)}\right) \right) \right)$$

$$(-i c(v-2k))^{-n-1} + e^{-\frac{i(v-2k)f^2}{4c} - \frac{i \pi v}{2}} (i c(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f(v-2k))^{n-j} (f i(v-2k) + 2i c z(v-2k))^{j+1}$$

$$\left( \frac{(f i(v-2k) + 2i c z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f i(v-2k) + 2i c z(v-2k))^2}{4c(v-2k)}\right) -$$

$$2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4} i \left( -\frac{f^2(v-2s)^2}{-2bk-bm+2cs-cv} + 4e(m-2k) - 2\pi(m-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-i f(v-2s))^{n-j} (f i(v-2s) + \right. \right.$$

$$2(i c(v-2s) - i b(m-2k)) z)^{j+1} \left. \left. \left( -\frac{(f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^2}{i c(v-2s) - i b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \right) \right)$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^2}{4(i c(v-2s) - i b(m-2k))}\right) (i c(v-2s) - i b(m-2k))^{-n-1} +$$

$$e^{\frac{1}{4} i \left( \frac{f^2(v-2s)^2}{2bk-bm+2cs-cv} + 4e(m-2k) - 2\pi(m+v) \right)} (b i(m-2k) + c i(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f(v-2s))^{n-j} (f i(v-2s) +$$

$$2(b i(m-2k) + c i(v-2s)) z)^{j+1} \left( -\frac{(f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^2}{b i(m-2k) + c i(v-2s)} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^2}{4(b i(m-2k) + c i(v-2s))}\right) + e^{-\frac{1}{4} i \left( \frac{f^2(v-2s)^2}{2bk-bm+2cs-cv} + 4e(m-2k) - 2\pi(m+v) \right)}$$

$$(-i b(m-2k) - i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i f(v-2s))^{n-j} (2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^{j+1}$$

$$\left( -\frac{(2(-ib(m-2k) - ic(v-2s))z - if(v-2s))^2}{-ib(m-2k) - ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}$$

$$\Gamma\left(\frac{j+1}{2}, -\frac{(2(-ib(m-2k) - ic(v-2s))z - if(v-2s))^2}{4(-ib(m-2k) - ic(v-2s))}\right) + e^{\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{-2bk+bm+2cs-cv} + 4e(m-2k)+2\pi(v-m)\right)}$$

$$(ib(m-2k) - ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (if(v-2s))^{n-j} (2(ib(m-2k) - ic(v-2s))z - if(v-2s))^{j+1}$$

$$\left( -\frac{(2(ib(m-2k) - ic(v-2s))z - if(v-2s))^2}{ib(m-2k) - ic(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}$$

$$\Gamma\left(\frac{j+1}{2}, -\frac{(2(ib(m-2k) - ic(v-2s))z - if(v-2s))^2}{4(ib(m-2k) - ic(v-2s))}\right) \Bigg|; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1233.01

$$\int z^n \sin^m(\sqrt{z} b + e) \sin^v(\sqrt{z} c + fz) dz = -(-1)^{n+1} 2^{-m-v+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k (m-2k)^{-2(n+1)} \binom{m}{k} \right)$$

$$\left( e^{ie(m-2k) - \frac{im\pi}{2}} \Gamma(2(n+1), -ib(m-2k)\sqrt{z}) + e^{\frac{im\pi}{2} - ie(m-2k)} \Gamma(2(n+1), ib(m-2k)\sqrt{z}) \right) b^{-2(n+1)} +$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} + 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)c^2 + i\pi v}{4f} + \frac{i\pi v}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2k))^{-h-j+2n} (-ic(v-2k) - 2if\sqrt{z}(v-2k))^{h+j} \right) \right)$$

$$\left( -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-ic(v-2k))$$

$$(-ic(v-2k) - 2if\sqrt{z}(v-2k)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)}\right) - 2$$

$$if(v-2k) \sqrt{-\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)}}$$

$$\begin{aligned}
 & \left. \left. \left. \Gamma \left( \frac{1}{2} (h+j+2), -\frac{i(-ic(v-2k)-2if\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \right) \right) (-if(v-2k))^{-2(n+1)} + \\
 & e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2}} (if(v-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k))^{-h-j+2n} (ci(v-2k) + 2fi\sqrt{z}(v-2k))^{h+j} \\
 & \left( \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2k)(ci(v-2k) + 2fi\sqrt{z}(v-2k)) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2} (h+j+1), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) + 2fi(v-2k) \right. \\
 & \left. \left. \sqrt{\frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-ib(m-2k)-ic(v-2s))^2}{4f(v-2s)} - i(m-2k) + \frac{1}{2}i\pi(m+v)} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib(m-2k) - ic(v-2s))^{-h-j+2n} (-ib(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{1}{f(v-2s)} \left( i(-ib(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^2 \right) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right. \\
 & \left. \left. \binom{n}{j} \left( (-ib(m-2k) - ic(v-2s)) (-ib(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z}) \right) \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h+j+1), -\frac{1}{4f(v-2s)} \left( i(-ib(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^2 \right) \right) \right) - \right. \\
 & \left. 2if(v-2s) \sqrt{\left( -\frac{1}{f(v-2s)} \left( i(-ib(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^2 \right) \right)} \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h+j+2), -\frac{1}{4f(v-2s)} \left( i(-ib(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^2 \right) \right) \right) \right) \right) \\
 & (-if(v-2s))^{-2(n+1)} + e^{-\frac{i(ib(m-2k)-ic(v-2s))^2}{4f(v-2s)} + i(m-2k) + \frac{1}{2}i\pi(v-m)}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b(m-2k) - i c(v-2s))^{-h-j+2n} (b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (i b(m-2k) - i c(v-2s))(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right. \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} (i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right) \right. \\
 & \left. 2 i f(v-2s) \sqrt{\left(-\frac{1}{f(v-2s)} (i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right)} \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{1}{4 f(v-2s)} (i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right) \right) \right) \right) \\
 & (-i f(v-2s))^{-2(n+1)} + e^{\frac{i(i c(v-2s) - i b(m-2k))^2}{4 f(v-2s)} - i e(m-2k) + \frac{1}{2} i \pi(m-v)} (i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s) - i b(m-2k))^{-h-j+2n} (-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (i c(v-2s) - i b(m-2k))(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z}) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), \frac{1}{4 f(v-2s)} (i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2)\right) \right) + \\
 & 2 f i(v-2s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{1}{4 f(v-2s)} (i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2)\right) \\
 & \sqrt{\left(\frac{1}{f(v-2s)} (i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2)\right)} \Bigg) + \\
 & e^{\frac{i(b i(m-2k) + c i(v-2s))^2}{4 f(v-2s)} + i e(m-2k) - \frac{1}{2} i \pi(m+v)} (i f(v-2s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j \\
 & (b i(m-2k) + c i(v-2s))^{-h-j+2n} (b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^{h+j}
 \end{aligned}$$

$$\left( \frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( (b i(m-2k) + c i(v-2s))(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z}) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{4 f(v-2s)}\right) + \right.$$

$$\left. 2 f i(v-2s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{4 f(v-2s)}\right) \right)$$

$$\left. \sqrt{\frac{i(b i(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)}} \right) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^n \sin^m(bz^r + dz) \sin^v(cz^r + fz)$

01.06.21.1234.01

$$\int z^n \sin^m(bz^2 + dz) \sin^v(cz^2 + fz) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} - i^{-m} 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{id^2(2k-m)}{4b}} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (id(2k-m))^{n-j} (-id(2k-m) - 2ibz(2k-m))^{j+1} \left( -\frac{i(-id(2k-m) - 2ibz(2k-m))^2}{b(2k-m)} \right)^{\frac{1}{2}(-j-1)} \right) \right)$$

$$\left( \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(2k-m) - 2ibz(2k-m))^2}{4b(2k-m)}\right) \right) (-ib(2k-m))^{-n-1} +$$

$$(-1)^m e^{\frac{id^2(m-2k)}{4b}} (-ib(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (id(m-2k))^{n-j} (-id(m-2k) - 2ibz(m-2k))^{j+1}$$

$$\left( -\frac{i(-id(m-2k) - 2ibz(m-2k))^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(m-2k) - 2ibz(m-2k))^2}{4b(m-2k)}\right) \Bigg) -$$

$$\begin{aligned}
 & (-1)^m i^{-v} 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{-\frac{if^2(2k-v)}{4c}} \right. \\
 & \left. \sum_{j=0}^n 2^{j-n} (-if(2k-v))^{n-j} (fi(2k-v) + 2ciz(2k-v))^{j+1} \left( \frac{i(fi(2k-v) + 2ciz(2k-v))^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(2k-v) + 2ciz(2k-v))^2}{4c(2k-v)}\right) \right) (ic(2k-v))^{-n-1} + \\
 & e^{-\frac{if^2(v-2k)}{4c}} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2k))^{n-j} (fi(v-2k) + 2ciz(v-2k))^{j+1} \\
 & \left. \left( \frac{i(fi(v-2k) + 2ciz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2k) + 2ciz(v-2k))^2}{4c(v-2k)}\right) \right) - \\
 & i^{-m-v} 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(if(2s-v)-id(2k-m))^2}{4(ic(2s-v)-ib(2k-m))}} \left( \sum_{j=0}^n 2^{j-n} (id(2k-m) - if(2s-v))^{n-j} \right. \right. \\
 & \left. \left. (-id(2k-m) + fi(2s-v) + 2(ic(2s-v) - ib(2k-m))z)^{j+1} (-(-id(2k-m) + fi(2s-v) + \right. \right. \\
 & \left. \left. 2(ic(2s-v) - ib(2k-m))z)^2 / (ic(2s-v) - ib(2k-m)) \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \right. \right. \\
 & \left. \left. -(-id(2k-m) + fi(2s-v) + 2(ic(2s-v) - ib(2k-m))z)^2 / (4(ic(2s-v) - ib(2k-m))) \right) \right) \\
 & (ic(2s-v) - ib(2k-m))^{-n-1} + (-1)^{m+v} e^{-\frac{(if(2s-v)-id(m-2k))^2}{4(ic(2s-v)-ib(m-2k))}} (ic(2s-v) - ib(m-2k))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (id(m-2k) - if(2s-v))^{n-j} (-id(m-2k) + fi(2s-v) + 2(ic(2s-v) - ib(m-2k))z)^{j+1} \\
 & \left. (-(-id(m-2k) + fi(2s-v) + 2(ic(2s-v) - ib(m-2k))z)^2 / (ic(2s-v) - ib(m-2k)))^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-id(m-2k) + fi(2s-v) + 2(ic(2s-v) - ib(m-2k))z)^2 / \right. \right. \\
 & \left. \left. (4(ic(2s-v) - ib(m-2k))) \right) + e^{-\frac{(if(v-2s)-id(2k-m))^2}{4(ic(v-2s)-ib(2k-m))}} (ic(v-2s) - ib(2k-m))^{-n-1} \right. \\
 & \left. \sum_{j=0}^n 2^{j-n} (id(2k-m) - if(v-2s))^{n-j} (-id(2k-m) + fi(v-2s) + 2(ic(v-2s) - ib(2k-m))z)^{j+1} \right. \\
 & \left. (-(-id(2k-m) + fi(v-2s) + 2(ic(v-2s) - ib(2k-m))z)^2 / (ic(v-2s) - ib(2k-m)))^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-id(2k-m) + fi(v-2s) + 2(ic(v-2s) - ib(2k-m))z)^2 / \right. \right. \\
 & \left. \left. (4(ic(v-2s) - ib(2k-m))) \right) + (-1)^m e^{-\frac{(if(v-2s)-id(m-2k))^2}{4(ic(v-2s)-ib(m-2k))}} (ic(v-2s) - ib(m-2k))^{-n-1} \right)
 \end{aligned}$$



$$\sum_{j=0}^n 2^{j-n} (i d(m-2k) - i f(v-2s))^{n-j} (-i d(m-2k) + f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^{j+1} \\ (-(-i d(m-2k) + f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^2 / (i c(v-2s) - i b(m-2k)))^{\frac{1}{2}(-j-1)} \\ \left( \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d(m-2k) + f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^2 / \right. \right. \\ \left. \left. (4(i c(v-2s) - i b(m-2k))) \right) \right); n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1235.01

$$\int z^n \sin^m(\sqrt{z} b + d z) \sin^v(\sqrt{z} c + f z) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} + i^{-m} 2^{-m-2n-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{i b^2 (2k-m)}{4d}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b(2k-m))^{-h-j+2n} (-i b(2k-m) - 2 i d \sqrt{z} (2k-m))^{h+j} \right. \right.$$

$$\left. \left. \left( \frac{i(-i b(2k-m) - 2 i d \sqrt{z} (2k-m))^2}{d(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i b(2k-m) \right. \right.$$

$$\left. \left. (-i b(2k-m) - 2 i d \sqrt{z} (2k-m)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i b(2k-m) - 2 i d \sqrt{z} (2k-m))^2}{4d(2k-m)}\right) \right) - \right.$$

$$2 i d(2k-m) \sqrt{-\frac{i(-i b(2k-m) - 2 i d \sqrt{z} (2k-m))^2}{d(2k-m)}} \Gamma\left(\frac{1}{2}(h+j+2), \right.$$

$$\left. \left. \left. -\frac{i(-i b(2k-m) - 2 i d \sqrt{z} (2k-m))^2}{4d(2k-m)} \right) \right) \right) \left( (-i d(2k-m))^{-2n-2} + (-1)^m e^{\frac{i b^2 (m-2k)}{4d}} \right)$$

$$(-i d(m-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b(m-2k))^{-h-j+2n} (-i b(m-2k) - 2 i d \sqrt{z} (m-2k))^{h+j}$$

$$\left( \frac{i(-i b(m-2k) - 2 i d \sqrt{z} (m-2k))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i b(m-2k) \right.$$

$$\begin{aligned}
 & (-i b(m-2k) - 2 i d \sqrt{z} (m-2k)) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{i(-i b(m-2k) - 2 i d \sqrt{z} (m-2k))^2}{4 d(m-2k)} \right) - \\
 & 2 i d(m-2k) \sqrt{-\frac{i(-i b(m-2k) - 2 i d \sqrt{z} (m-2k))^2}{d(m-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \right. \\
 & \left. -\frac{i(-i b(m-2k) - 2 i d \sqrt{z} (m-2k))^2}{4 d(m-2k)} \right) \Bigg) + (-1)^m i^{-v} 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{-\frac{i c^2(2k-v)}{4f}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(2k-v))^{-h-j+2n} (c i(2k-v) + 2 f i \sqrt{z} (2k-v))^{h+j} \right. \right. \\
 & \left. \left. \left( \frac{i(c i(2k-v) + 2 f i \sqrt{z} (2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(2k-v) (c i(2k-v) + 2 f i \sqrt{z} (2k-v)) \right) \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h+j+1), \frac{i(c i(2k-v) + 2 f i \sqrt{z} (2k-v))^2}{4 f(2k-v)} \right) + 2 f i(2k-v) \right. \right. \\
 & \left. \left. \sqrt{\frac{i(c i(2k-v) + 2 f i \sqrt{z} (2k-v))^2}{f(2k-v)}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i(c i(2k-v) + 2 f i \sqrt{z} (2k-v))^2}{4 f(2k-v)} \right) \right) \Bigg) \\
 & (i f(2k-v))^{-2n-2} + e^{-\frac{i c^2(v-2k)}{4f}} (i f(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k))^{-h-j+2n} \\
 & (c i(v-2k) + 2 f i \sqrt{z} (v-2k))^{h+j} \left( \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i(v-2k) (c i(v-2k) + 2 f i \sqrt{z} (v-2k)) \Gamma \left( \frac{1}{2} (h+j+1), \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f(v-2k)} \right) + \right. \\
 & \left. 2 f i(v-2k) \sqrt{\frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f(v-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) \right) \right) + i^{-m-v} 2^{-m-2n-v-1}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s} \left( (-1)^v e^{-\frac{(ic(2k-v)-ib(2s-m))^2}{4(if(2k-v)-id(2s-m))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2k-v) - ib(2s-m))^{-h-j+2n} \right. \right.$$

$$\left. \left. (-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z})^{h+j} \right. \right.$$

$$\left. \left. \left( -(-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z})^2 \right) / \right. \right.$$

$$\left. \left. (if(2k-v) - id(2s-m))^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right.$$

$$\left. \left. \left( ic(2k-v) - ib(2s-m) \right) (-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z}) \right) \right.$$

$$\Gamma\left(\frac{1}{2}(h+j+1), -(-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z})^2 / \right.$$

$$\left. \left. (4(if(2k-v) - id(2s-m))) \right) \right) + 2(if(2k-v) - id(2s-m))$$

$$\Gamma\left(\frac{1}{2}(h+j+2), -(-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z})^2 / \right.$$

$$\left. \left. (4(if(2k-v) - id(2s-m))) \right) \right) \sqrt{\left( -(-ib(2s-m) + ci(2k-v) + \right.}$$

$$\left. \left. 2(if(2k-v) - id(2s-m))\sqrt{z} \right)^2 / (if(2k-v) - id(2s-m)) \right) \right)$$

$$(if(2k-v) - id(2s-m))^{-2n-2} + (-1)^{m+v} e^{-\frac{(ic(2k-v)-ib(m-2s))^2}{4(if(2k-v)-id(m-2s))}} (if(2k-v) - id(m-2s))^{-2n-2}$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2k-v) - ib(m-2s))^{-h-j+2n}$$

$$(-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})^{h+j} \left( -(-ib(m-2s) + ci(2k-v) + \right.$$

$$\left. 2(if(2k-v) - id(m-2s))\sqrt{z} \right)^2 / (if(2k-v) - id(m-2s))^{\frac{1}{2}(-h-j-1)} \binom{j}{h}$$

$$\binom{n}{j} \left( ic(2k-v) - ib(m-2s) \right) (-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})$$

$$\Gamma\left(\frac{1}{2}(h+j+1), -(-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})^2 / \right.$$

$$\left. \left. (4(if(2k-v) - id(m-2s))) \right) \right) + 2(if(2k-v) - id(m-2s))$$

$$\Gamma\left(\frac{1}{2}(h+j+2), -(-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})^2 / \right.$$

$$\left. \left. (4(if(2k-v) - id(m-2s))) \right) \right) \sqrt{\left( -(-ib(m-2s) + ci(2k-v) + \right.}$$

$$\left. \left. 2(if(2k-v) - id(m-2s))\sqrt{z} \right)^2 / (if(2k-v) - id(m-2s)) \right) \right) +$$

$$\begin{aligned}
 & e^{-\frac{(ic(v-2k)-ib(2s-m))^2}{4(if(v-2k)-id(2s-m))}} (if(v-2k)-id(2s-m))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k)-ib(2s-m))^{-h-j+2n} \\
 & \quad (-ib(2s-m)+ci(v-2k)+2(if(v-2k)-id(2s-m))\sqrt{z})^{h+j} \\
 & \quad \left( -(-ib(2s-m)+ci(v-2k)+2(if(v-2k)-id(2s-m))\sqrt{z})^2 \right) / \\
 & \quad (if(v-2k)-id(2s-m))^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad \left( (ic(v-2k)-ib(2s-m))(-ib(2s-m)+ci(v-2k)+2(if(v-2k)-id(2s-m))\sqrt{z}) \right) \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), -(-ib(2s-m)+ci(v-2k)+2(if(v-2k)-id(2s-m))\sqrt{z})^2 \right) / \\
 & \quad (4(if(v-2k)-id(2s-m))) + 2(if(v-2k)-id(2s-m)) \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+2), -(-ib(2s-m)+ci(v-2k)+2(if(v-2k)-id(2s-m))\sqrt{z})^2 \right) / \\
 & \quad (4(if(v-2k)-id(2s-m))) \sqrt{\left( -(-ib(2s-m)+ci(v-2k)+ \right. \\
 & \quad \left. 2(if(v-2k)-id(2s-m))\sqrt{z})^2 \right) / (if(v-2k)-id(2s-m))} + \\
 & (-1)^m e^{-\frac{(ic(v-2k)-ib(m-2s))^2}{4(if(v-2k)-id(m-2s))}} (if(v-2k)-id(m-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k)- \\
 & \quad ib(m-2s))^{-h-j+2n} (-ib(m-2s)+ci(v-2k)+2(if(v-2k)-id(m-2s))\sqrt{z})^{h+j} \\
 & \quad \left( -(-ib(m-2s)+ci(v-2k)+2(if(v-2k)-id(m-2s))\sqrt{z})^2 \right) / \\
 & \quad (if(v-2k)-id(m-2s))^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad \left( (ic(v-2k)-ib(m-2s))(-ib(m-2s)+ci(v-2k)+2(if(v-2k)-id(m-2s))\sqrt{z}) \right) \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), -(-ib(m-2s)+ci(v-2k)+2(if(v-2k)-id(m-2s))\sqrt{z})^2 \right) / \\
 & \quad (4(if(v-2k)-id(m-2s))) + 2(if(v-2k)-id(m-2s)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \quad \left. -(-ib(m-2s)+ci(v-2k)+2(if(v-2k)-id(m-2s))\sqrt{z})^2 \right) / (4(if(v-2k)- \\
 & \quad id(m-2s))) \sqrt{\left( -(-ib(m-2s)+ci(v-2k)+2(if(v-2k)-id(m-2s)) \right. \\
 & \quad \left. \sqrt{z})^2 \right) / (if(v-2k)-id(m-2s))} \Big) / ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin^m(dz) \sin^v(cz^r + fz + g)$**

01.06.21.1236.01

$$\int z^n \sin^m(dz) \sin^v(cz^2 + fz + g) dz =$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} + (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( e^{\frac{im\pi}{2}} \Gamma(n + 1, id(m - 2k)z) (-id(m - 2k))^{-n-1} + e^{-\frac{1}{2}im\pi} (id(m - 2k))^{-n-1} \Gamma(n + 1, -id(m - 2k)z) \right) -$$

$$2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i\pi v}{2} - ig(v-2k)} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (if(v-2k))^{n-j} (-if(v-2k) - 2icz(v-2k))^{j+1} \left( -\frac{i(-if(v-2k) - 2icz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-if(v-2k) - 2icz(v-2k))^2}{4c(v-2k)}\right) \right) (-ic(v-2k))^{-n-1} + \right.$$

$$\left. e^{-\frac{i(v-2k)f^2}{4c} - \frac{i\pi v}{2} + gi(v-2k)} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2k))^{n-j} (fi(v-2k) + 2ciz(v-2k))^{j+1} \right.$$

$$\left. \left( \frac{i(fi(v-2k) + 2ciz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2k) + 2ciz(v-2k))^2}{4c(v-2k)}\right) \right) -$$

$$2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-id(m-2k) - f(v-2s))^2}{4c(v-2s)} + \frac{1}{2}i\pi(m+v) - ig(v-2s)} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (di(m-2k) + fi(v-2s))^{n-j} (-id(m-2k) - if(v-2s) - 2ic(v-2s)z)^{j+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(-id(m-2k) - if(v-2s) - 2ic(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right. \right.$$

$$\left. \left. \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(m-2k) - if(v-2s) - 2ic(v-2s)z)^2}{4c(v-2s)}\right) \right) (-ic(v-2s))^{-n-1} + \right.$$

$$\left. e^{-\frac{i(id(m-2k) - f(v-2s))^2}{4c(v-2s)} + \frac{1}{2}i\pi(v-m) - ig(v-2s)} \left( \sum_{j=0}^n 2^{j-n} (if(v-2s) - id(m-2k))^{n-j} (di(m-2k) - \right. \right.$$

$$\begin{aligned}
 & i f(v-2s) - 2 i c(v-2s) z)^{j+1} \left( -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s) z)^2}{4 c(v-2s)}\right) (-i c(v-2s))^{-n-1} + \\
 & e^{\frac{i(i f(v-2s) - i d(m-2k))^2}{4 c(v-2s)} + \frac{1}{2} i \pi(m-v) + g i(v-2s)} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i d(m-2k) - i f(v-2s))^{n-j} (-i d(m-2k) + \\
 & f i(v-2s) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{4 c(v-2s)}\right) + \\
 & e^{\frac{i(d i(m-2k) + f i(v-2s))^2}{4 c(v-2s)} - \frac{1}{2} i \pi(m+v) + g i(v-2s)} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i d(m-2k) - i f(v-2s))^{n-j} \\
 & (d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^{j+1} \left( \frac{i(d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(d i(m-2k) + f i(v-2s) + 2 c i(v-2s) z)^2}{4 c(v-2s)}\right) \Big/; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1237.01

$$\int z^n \sin^m(dz) \sin^v(\sqrt{z} c + f z + g) dz =$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( e^{\frac{i m \pi}{2}} \Gamma(n+1, i d(m-2k) z) (-i d(m-2k))^{-n-1} + e^{-\frac{1}{2} i m \pi} (i d(m-2k))^{-n-1} \Gamma(n+1, -i d(m-2k) z) \right) +$$

$$2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+n-1} (f(v-2k))^{-2(n+1)} \binom{v}{k}$$

$$\left( e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2} + g i(v-2k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k))^{-h-j+2n} (c i(v-2k) + 2 f i \sqrt{z} (v-2k))^{h+j} \right)$$

$$\left( \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2k) (c i(v-2k) + 2 f i \sqrt{z} (v-2k)) \Gamma \left(
 \right.$$

$$\begin{aligned}
 & \left. \frac{1}{2} (h+j+1), \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) + 2 f i (v-2k) \\
 & \sqrt{\frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f (v-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) + \\
 & e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2} - i g (v-2k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c (v-2k))^{-h-j+2n} (-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^{h+j} \\
 & \left( -\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f (v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i c (v-2k) \right. \\
 & \left. (-i c (v-2k) - 2 i f \sqrt{z} (v-2k)) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) \right) - \\
 & 2 i f (v-2k) \sqrt{-\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f (v-2k)}} \Gamma \left( \frac{1}{2} (h+j+2), \right. \\
 & \left. \left. -\frac{i(-i c (v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f (v-2k)} \right) \right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{\frac{c^2 (v-2s)^2}{4(i f (v-2s) - i d (m-2k))} + g i (v-2s) + \frac{1}{2} i \pi (m-v)} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c (v-2s))^{-h-j+2n} (c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z})^2}{i f (v-2s) - i d (m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right. \\
 & \left. \left. \binom{n}{j} (c i (v-2s) (c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z}) \right) \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h+j+1), -(c i (v-2s) + 2 (i f (v-2s) - i d (m-2k)) \sqrt{z})^2 \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( (4(i f(v-2s) - i d(m-2k))) \right) + 2(i f(v-2s) - i d(m-2k)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. - (c i(v-2s) + 2(i f(v-2s) - i d(m-2k)) \sqrt{z})^2 \right) / (4(i f(v-2s) - i d(m-2k))) \right) \\
 & \left. \sqrt{\left( - (c i(v-2s) + 2(i f(v-2s) - i d(m-2k)) \sqrt{z})^2 \right) / (i f(v-2s) - i d(m-2k)) \right) \right) \\
 & (i f(v-2s) - i d(m-2k))^{-2(n+1)} + e^{\frac{c^2(v-2s)^2}{4(d i(m-2k) + f i(v-2s))} + g i(v-2s) - \frac{1}{2} i \pi(m+v)} (d i(m-2k) + f i(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s))^{-h-j+2n} (c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^{h+j} \\
 & \left( - \frac{(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2}{d i(m-2k) + f i(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i(v-2s) (c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. - \frac{(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2}{4(d i(m-2k) + f i(v-2s))} \right) + 2(d i(m-2k) + f i(v-2s)) \right) \\
 & \left( \Gamma\left(\frac{1}{2}(h+j+2), - \frac{(c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2}{4(d i(m-2k) + f i(v-2s))} \right) \right) \\
 & \left. \sqrt{\left( - (c i(v-2s) + 2(d i(m-2k) + f i(v-2s)) \sqrt{z})^2 \right) / (d i(m-2k) + f i(v-2s)) \right) \right) + \\
 & e^{\frac{c^2(v-2s)^2}{4(-i d(m-2k) - i f(v-2s))} - i g(v-2s) + \frac{1}{2} i \pi(m+v)} (-i d(m-2k) - i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2s))^{-h-j+2n} (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^{h+j} \\
 & \left( - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2 / (-i d(m-2k) - i f(v-2s)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( 2(-i d(m-2k) - i f(v-2s)) \sqrt{\left( - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2 \right) / \right. \\
 & \left. (-i d(m-2k) - i f(v-2s)) \right) \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \left. - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2 / (4(-i d(m-2k) - i f(v-2s))) \right) - \\
 & i c(v-2s) (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), \right.
 \end{aligned}$$



$$\begin{aligned}
 & -\left(2(-id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s)\right)^2 / (4(-id(m-2k) - if(v-2s))) \Big) + \\
 & \frac{c^2(v-2s)^2}{e^{4(id(m-2k) - if(v-2s)) - ig(v-2s) + \frac{1}{2}i\pi(v-m)}} (id(m-2k) - if(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2s))^{-h-j+2n} (2(id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s))^{h+j} \\
 & \left( -\frac{(2(id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s))^2}{id(m-2k) - if(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(id(m-2k) - if(v-2s)) \right. \\
 & \left. \sqrt{\left(2(id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s)\right)^2 / (id(m-2k) - if(v-2s))} \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(2(id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id(m-2k) - if(v-2s))}\right) - \right. \\
 & \left. ic(v-2s)(2(id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s)) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(2(id(m-2k) - if(v-2s))\sqrt{z} - ic(v-2s))^2}{4(id(m-2k) - if(v-2s))}\right) \right) \Big) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^n \sin^m(dz + e) \sin^v(cz^r + fz + g)$

01.06.21.1238.01

$$\begin{aligned}
 \int z^n \sin^m(dz + e) \sin^v(cz^2 + fz + g) dz = & \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} + \\
 & (-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{im\pi}{2} - ie(m-2k)} \Gamma(n+1, id(m-2k)z) (-id(m-2k))^{-n-1} + \right. \\
 & \left. e^{ie(m-2k) - \frac{im\pi}{2}} (id(m-2k))^{-n-1} \Gamma(n+1, -id(m-2k)z) \right) - \\
 & 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i\pi v}{2} - ig(v-2k)} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sum_{j=0}^n 2^{j-n} (i f(v-2k))^{n-j} (-i f(v-2k) - 2 i c z(v-2k))^{j+1} \left( -\frac{i(-i f(v-2k) - 2 i c z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-i f(v-2k) - 2 i c z(v-2k))^2}{4 c(v-2k)}\right) \right) (-i c(v-2k))^{-n-1} + \\
 & e^{-\frac{i(v-2k)f^2}{4c} - \frac{i\pi v}{2} + g i(v-2k)} (i c(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f(v-2k))^{n-j} (f i(v-2k) + 2 c i z(v-2k))^{j+1} \\
 & \left( \frac{i(f i(v-2k) + 2 c i z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f i(v-2k) + 2 c i z(v-2k))^2}{4 c(v-2k)}\right) - \\
 & 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(-i d(m-2k) - i f(v-2s))^2}{4 c(v-2s)} - i e(m-2k) + \frac{1}{2} i \pi(m+v) - i g(v-2s)} \right. \\
 & \left. \sum_{j=0}^n 2^{j-n} (d i(m-2k) + f i(v-2s))^{n-j} (-i d(m-2k) - i f(v-2s) - 2 i c(v-2s)z)^{j+1} \right. \\
 & \left. \left( -\frac{i(-i d(m-2k) - i f(v-2s) - 2 i c(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right. \\
 & \left. \Gamma\left(\frac{j+1}{2}, -\frac{i(-i d(m-2k) - i f(v-2s) - 2 i c(v-2s)z)^2}{4 c(v-2s)}\right) \right) (-i c(v-2s))^{-n-1} + \\
 & e^{-\frac{i(i d(m-2k) - i f(v-2s))^2}{4 c(v-2s)} + i e(m-2k) - i g(v-2s) + \frac{1}{2} i(v-m)\pi} \left( \sum_{j=0}^n 2^{j-n} (i f(v-2s) - i d(m-2k))^{n-j} (d i(m-2k) - \right. \\
 & \left. i f(v-2s) - 2 i c(v-2s)z)^{j+1} \left( -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(d i(m-2k) - i f(v-2s) - 2 i c(v-2s)z)^2}{4 c(v-2s)}\right) \right) \\
 & (-i c(v-2s))^{-n-1} + e^{\frac{i(i f(v-2s) - i d(m-2k))^2}{4 c(v-2s)} - i e(m-2k) + \frac{1}{2} i \pi(m-v) + g i(v-2s)} (i c(v-2s))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (i d(m-2k) - i f(v-2s))^{n-j} (-i d(m-2k) + f i(v-2s) + 2 c i(v-2s)z)^{j+1} \\
 & \left( \frac{i(-i d(m-2k) + f i(v-2s) + 2 c i(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}
 \end{aligned}$$

$$\Gamma\left(\frac{j+1}{2}, \frac{i(-id(m-2k) + fi(v-2s) + 2ci(v-2s)z)^2}{4c(v-2s)}\right) +$$

$$e^{\frac{i(d(m-2k)+fi(v-2s))^2}{4c(v-2s)} + e^{i(m-2k)+gi(v-2s)-\frac{1}{2}i(m+v)\pi}} (ic(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-id(m-2k) - if(v-2s))^{n-j}$$

$$(di(m-2k) + fi(v-2s) + 2ci(v-2s)z)^{j+1} \left(\frac{i(di(m-2k) + fi(v-2s) + 2ci(v-2s)z)^2}{c(v-2s)}\right)^{\frac{1}{2}(-j-1)}$$

$$\left(\binom{n}{j}\Gamma\left(\frac{j+1}{2}, \frac{i(di(m-2k) + fi(v-2s) + 2ci(v-2s)z)^2}{4c(v-2s)}\right)\right); n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1239.01

$$\int z^n \sin^m(dz + e) \sin^v(\sqrt{z}c + fz + g) dz = \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} +$$

$$(-1)^n 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{im\pi}{2} - ie(m-2k)} \Gamma(n+1, id(m-2k)z) (-id(m-2k))^{-n-1} + \right.$$

$$\left. e^{ie(m-2k) - \frac{im\pi}{2}} (id(m-2k))^{-n-1} \Gamma(n+1, -id(m-2k)z) \right) + 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+n-1} \binom{v}{k}$$

$$(f(v-2k))^{-2(n+1)} \left( e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2} + gi(v-2k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k))^{-h-j+2n} (ci(v-2k) + 2fi\sqrt{z}(v-2k))^{h+j} \right.$$

$$\left. \left(\frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2k)(ci(v-2k) + 2fi\sqrt{z}(v-2k)) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)}\right) + 2fi(v-2k) \right) \right.$$

$$\left. \sqrt{\frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)}\right) \right) +$$

$$e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2} - ig(v-2k)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ic(v-2k))^{-h-j+2n} (-ic(v-2k) - 2if\sqrt{z}(v-2k))^{h+j}$$

$$\begin{aligned}
 & \left( -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2k) \right. \\
 & \left. (-ic(v-2k) - 2if\sqrt{z}(v-2k)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)}\right) \right. \\
 & \left. 2if(v-2k) \sqrt{-\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)}\right) \right) \Bigg) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{c^2(v-2s)^2}{e^{4(i f(v-2s) - i d(m-2k))} + g i(v-2s) - i e(m-2k) + \frac{1}{2} i \pi(m-v)} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left( -\frac{(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2}{if(v-2s) - id(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \\
 & \left. \binom{n}{j} (ci(v-2s)(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2 / \right. \right. \\
 & \left. \left. (4(if(v-2s) - id(m-2k))) \right) + 2(if(v-2s) - id(m-2k)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2 / (4(if(v-2s) - id(m-2k))) \right) \right. \\
 & \left. \left. \sqrt{\left( -(ci(v-2s) + 2(if(v-2s) - id(m-2k))\sqrt{z})^2 / (if(v-2s) - id(m-2k)) \right)} \right) \right) \Bigg) \\
 & (if(v-2s) - id(m-2k))^{-2(n+1)} + \frac{c^2(v-2s)^2}{e^{4(d i(m-2k) + f i(v-2s))} + g i(v-2s) + e i(m-2k) - \frac{1}{2} i(m+v) \pi} \\
 & (d i(m-2k) + f i(v-2s))^{-2(n+1)}
 \end{aligned}$$

$$\begin{aligned}
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c (v-2s))^{-h-j+2n} (c i (v-2s) + 2 (d i (m-2k) + f i (v-2s)) \sqrt{z})^{h+j} \\
 & \left( \frac{(c i (v-2s) + 2 (d i (m-2k) + f i (v-2s)) \sqrt{z})^2}{d i (m-2k) + f i (v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i (v-2s) (c i (v-2s) + 2 (d i (m-2k) + f i (v-2s)) \sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), \right. \right. \\
 & \left. \left. - \frac{(c i (v-2s) + 2 (d i (m-2k) + f i (v-2s)) \sqrt{z})^2}{4 (d i (m-2k) + f i (v-2s))} \right) + 2 (d i (m-2k) + f i (v-2s)) \right. \\
 & \left. \Gamma \left( \frac{1}{2} (h+j+2), - \frac{(c i (v-2s) + 2 (d i (m-2k) + f i (v-2s)) \sqrt{z})^2}{4 (d i (m-2k) + f i (v-2s))} \right) \right) \\
 & \left. \sqrt{\left( - (c i (v-2s) + 2 (d i (m-2k) + f i (v-2s)) \sqrt{z})^2 / (d i (m-2k) + f i (v-2s)) \right)} \right) + \\
 & \frac{c^2 (v-2s)^2}{e^{4(-i d(m-2k)-i f(v-2s))}} - i g (v-2s) - i e (m-2k) + \frac{1}{2} i \pi (m+v) (-i d(m-2k) - i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c (v-2s))^{-h-j+2n} (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s))^{h+j} \\
 & \left( - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s))^2 / (-i d(m-2k) - i f(v-2s)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( 2(-i d(m-2k) - i f(v-2s)) \sqrt{\left( - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s))^2 / \right. \right. \\
 & \left. \left. (-i d(m-2k) - i f(v-2s)) \right) \Gamma \left( \frac{1}{2} (h+j+2), \right. \right. \\
 & \left. \left. - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s))^2 / (4(-i d(m-2k) - i f(v-2s))) \right) - \right. \\
 & \left. i c (v-2s) (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s)) \Gamma \left( \frac{1}{2} (h+j+1), \right. \right. \\
 & \left. \left. - (2(-i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s))^2 / (4(-i d(m-2k) - i f(v-2s))) \right) \right) \right) + \\
 & \frac{c^2 (v-2s)^2}{e^{4(i d(m-2k)-i f(v-2s))}} - i g (v-2s) + e i (m-2k) + \frac{1}{2} i (v-m) \pi (i d(m-2k) - i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c (v-2s))^{-h-j+2n} (2(i d(m-2k) - i f(v-2s)) \sqrt{z} - i c (v-2s))^{h+j}
 \end{aligned}$$

$$\left( -\frac{(2(i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2}{i d(m-2k) - i f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\binom{j}{h} \binom{n}{j} \left( 2(i d(m-2k) - i f(v-2s)) \sqrt{\left( -(2(i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2 / (i d(m-2k) - i f(v-2s)) \right)} \right)$$

$$\Gamma\left( \frac{1}{2}(h+j+2), -\frac{(2(i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2}{4(i d(m-2k) - i f(v-2s))} \right) -$$

$$i c(v-2s) (2(i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s)) \Gamma\left( \frac{1}{2}(h+j+1), \right.$$

$$\left. -\frac{(2(i d(m-2k) - i f(v-2s)) \sqrt{z} - i c(v-2s))^2}{4(i d(m-2k) - i f(v-2s))} \right) \Bigg) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $z^n \sin^m(bz^r) \sin^v(cz^f + fz + g)$**

01.06.21.1240.01

$$\int z^n \sin^m(bz^2) \sin^v(cz^2 + fz + g) dz = \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} -$$

$$2^{-m-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{1}{2} i m \pi} z^{n+1} \Gamma\left( \frac{n+1}{2}, -i b(m-2k) z^2 \right) (-i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{\frac{i m \pi}{2}} z^{n+1} (i b(m-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left( \frac{n+1}{2}, i b(m-2k) z^2 \right) \right) -$$

$$2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i\pi v}{2} - i g(v-2k)} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (i f(v-2k))^{n-j} (-i f(v-2k) - 2 i c z(v-2k))^{j+1} \left( -\frac{i(-i f(v-2k) - 2 i c z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \right) \right)$$

$$\binom{n}{j} \Gamma\left( \frac{j+1}{2}, -\frac{i(-i f(v-2k) - 2 i c z(v-2k))^2}{4 c(v-2k)} \right) \left( -i c(v-2k) \right)^{-n-1} +$$

$$\begin{aligned}
 & e^{-\frac{i(v-2k)f^2}{4c} - \frac{i\pi v}{2} + g i(v-2k)} (i c(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f(v-2k))^{n-j} (f i(v-2k) + 2 c i z(v-2k))^{j+1} \\
 & \left( \frac{(f i(v-2k) + 2 c i z(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(f i(v-2k) + 2 c i z(v-2k))^2}{4 c(v-2k)}\right) \Bigg| - \\
 & 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4} i \left( -\frac{f^2(v-2s)^2}{-2bk+bm+2cs-cv} - 4g(v-2s) - 2\pi(m-v) \right)} \left( \sum_{j=0}^n 2^{j-n} (-i f(v-2s))^{n-j} (f i(v-2s) + \right. \right. \\
 & \left. \left. 2(i c(v-2s) - i b(m-2k)) z\right)^{j+1} \left( -\frac{(f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^2}{i c(v-2s) - i b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(f i(v-2s) + 2(i c(v-2s) - i b(m-2k)) z)^2}{4(i c(v-2s) - i b(m-2k))}\right) \right) (i c(v-2s) - i b(m-2k))^{-n-1} + \\
 & e^{\frac{1}{4} i \left( \frac{f^2(v-2s)^2}{2bk-bm+2cs-cv} + 4g(v-2s) - 2\pi(m+v) \right)} (b i(m-2k) + c i(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f(v-2s))^{n-j} (f i(v-2s) + \\
 & \left. 2(b i(m-2k) + c i(v-2s)) z\right)^{j+1} \left( -\frac{(f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^2}{b i(m-2k) + c i(v-2s)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^2}{4(b i(m-2k) + c i(v-2s))}\right) + e^{-\frac{1}{4} i \left( \frac{f^2(v-2s)^2}{2bk-bm+2cs-cv} + 4g(v-2s) - 2\pi(m+v) \right)} \\
 & (-i b(m-2k) - i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i f(v-2s))^{n-j} (2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^{j+1} \\
 & \left( -\frac{(2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{-i b(m-2k) - i c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{4(-i b(m-2k) - i c(v-2s))}\right) + e^{\frac{1}{4} i \left( -\frac{f^2(v-2s)^2}{-2bk+bm+2cs-cv} - 4g(v-2s) + 2\pi(v-m) \right)} \\
 & (i b(m-2k) - i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i f(v-2s))^{n-j} (2(i b(m-2k) - i c(v-2s)) z - i f(v-2s))^{j+1} \\
 & \left( -\frac{(2(i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{i b(m-2k) - i c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(2(i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{4(i b(m-2k) - i c(v-2s))}\right) \Bigg| ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1241.01

$$\int z^n \sin^m(b \sqrt{z}) \sin^v(\sqrt{z} c + f z + g) dz = -(-1)^{n+1} 2^{-m-v+1} \left(\frac{v}{2}\right) (1-v \bmod 2)$$

$$\left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k (m-2k)^{-2(n+1)} \binom{m}{k} \left( e^{-\frac{1}{2} i m \pi} \Gamma(2(n+1), -i b(m-2k) \sqrt{z}) + e^{\frac{i m \pi}{2}} \Gamma(2(n+1), i b(m-2k) \sqrt{z}) \right) \right)$$

$$b^{-2(n+1)} + \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \left(\frac{v}{2}\right) (1-m \bmod 2) (1-v \bmod 2)}{n+1} + 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2} - i g(v-2k)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2k))^{-h-j+2n} (-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^{h+j} \right. \right.$$

$$\left. \left( -\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-i c(v-2k) \right.$$

$$\left. (-i c(v-2k) - 2 i f \sqrt{z} (v-2k)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f(v-2k)}\right) - 2 \right.$$

$$i f(v-2k) \sqrt{-\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{f(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \right.$$

$$\left. \left. -\frac{i(-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^2}{4 f(v-2k)} \right) \right) \left( (-i f(v-2k))^{-2(n+1)} + e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2} + g i(v-2k)} \right)$$

$$(i f(v-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k))^{-h-j+2n} (c i(v-2k) + 2 f i \sqrt{z} (v-2k))^{h+j}$$

$$\left( \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(v-2k) (c i(v-2k) + 2 f i \sqrt{z} (v-2k)) \Gamma\left( \right. \right.$$

$$\left. \left. \frac{1}{2}(h+j+1), \frac{i(c i(v-2k) + 2 f i \sqrt{z} (v-2k))^2}{4 f(v-2k)} \right) + 2 f i(v-2k) \right)$$



$$\begin{aligned}
 & \left. \sqrt{\frac{i(c i(v-2k) + 2 f i \sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(c i(v-2k) + 2 f i \sqrt{z}(v-2k))^2}{4 f(v-2k)}\right)\right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(i b(m-2k) - i c(v-2s))^2}{4 f(v-2s)} + \frac{1}{2} i \pi(v-m) - i g(v-2s)} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b(m-2k) - i c(v-2s))^{-h-j+2n} (b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right. \\
 & \left. \left. (i b(m-2k) - i c(v-2s))(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} (i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right) \right. \right. \\
 & \left. \left. 2 i f(v-2s) \sqrt{\left(-\frac{1}{f(v-2s)} (i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right)} \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{1}{4 f(v-2s)} (i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right) \right) \right) \right) \\
 & (-i f(v-2s))^{-2(n+1)} + e^{-\frac{i(-i b(m-2k) - i c(v-2s))^2}{4 f(v-2s)} + \frac{1}{2} i \pi(m+v) - i g(v-2s)} \text{Sum}\left(\text{Sum}\left((-1)^{j-h} 4^j \right. \right. \\
 & \left. \left. (-i b(m-2k) - i c(v-2s))^{-h-j+2n} (-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left(-\frac{1}{f(v-2s)} (i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right. \\
 & \left. \left. \binom{n}{j} (i(-i b(m-2k) - i c(v-2s))(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} (i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right) \right) \right) - 2 i f \\
 & (v-2s) \sqrt{\left(-\frac{1}{f(v-2s)} (i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2)\right)} \Gamma\left(\frac{1}{2}(h+j+2), \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. - \frac{1}{4 f(v-2 s)} \left( i \left( -i b(m-2 k) - i c(v-2 s) - 2 i f(v-2 s) \sqrt{z} \right)^2 \right) \right\}, \{h, 0, j\}, \{j, 0, n\} \\
 & (-i f(v-2 s))^{-2(n+1)} + e^{\frac{i(i c(v-2 s)-i b(m-2 k))^2}{4 f(v-2 s)} + \frac{1}{2} i \pi(m-v)+g i(v-2 s)} (i f(v-2 s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2 s) - i b(m-2 k))^{-h-j+2 n} \left( -i b(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^{h+j} \\
 & \left( \frac{i \left( -i b(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2}{f(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (i c(v-2 s) - i b(m-2 k)) \left( -i b(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right) \right. \\
 & \Gamma\left(\frac{1}{2}(h+j+1), \frac{1}{4 f(v-2 s)} \left( i \left( -i b(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2 \right) \right) + \\
 & 2 f i(v-2 s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{1}{4 f(v-2 s)} \left( i \left( -i b(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2 \right) \right) \\
 & \left. \sqrt{\left( \frac{1}{f(v-2 s)} \left( i \left( -i b(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2 \right) \right)} \right) + \\
 & e^{\frac{i(b i(m-2 k)+c i(v-2 s))^2}{4 f(v-2 s)} - \frac{1}{2} i \pi(m+v)+g i(v-2 s)} (i f(v-2 s))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j \\
 & (b i(m-2 k) + c i(v-2 s))^{-h-j+2 n} \left( b i(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^{h+j} \\
 & \left( \frac{i \left( b i(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2}{f(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (b i(m-2 k) + c i(v-2 s)) \left( b i(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right) \right. \\
 & \Gamma\left(\frac{1}{2}(h+j+1), \frac{i \left( b i(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2}{4 f(v-2 s)} \right) + \\
 & 2 f i(v-2 s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{i \left( b i(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2}{4 f(v-2 s)} \right) \\
 & \left. \sqrt{\frac{i \left( b i(m-2 k) + c i(v-2 s) + 2 f i(v-2 s) \sqrt{z} \right)^2}{f(v-2 s)}} \right) \Bigg\} ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^n \sin^m(bz^r + e) \sin^v(cz^r + f z + g)$

01.06.21.1242.01

$$\int z^n \sin^m(bz^2 + e) \sin^v(cz^2 + f z + g) dz = \frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} -$$

$$2^{-m-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{i e (m-2k) - \frac{i m \pi}{2}} z^{n+1} \Gamma\left(\frac{n+1}{2}, -i b (m-2k) z^2\right) (-i b (m-2k) z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{\frac{i m \pi}{2} - i e (m-2k)} z^{n+1} (i b (m-2k) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, i b (m-2k) z^2\right) \right) -$$

$$2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)f^2}{4c} + \frac{i\pi v}{2} - i g (v-2k)} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (i f (v-2k))^{n-j} (-i f (v-2k) - 2 i c z (v-2k))^{j+1} \left( -\frac{i (-i f (v-2k) - 2 i c z (v-2k))^2}{c (v-2k)} \right)^{\frac{1}{2}(-j-1)} \right) \right.$$

$$\left. \left( \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i (-i f (v-2k) - 2 i c z (v-2k))^2}{4 c (v-2k)}\right) \right) (-i c (v-2k))^{-n-1} + \right.$$

$$\left. e^{-\frac{i(v-2k)f^2}{4c} - \frac{i\pi v}{2} + g i (v-2k)} (i c (v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i f (v-2k))^{n-j} (f i (v-2k) + 2 c i z (v-2k))^{j+1} \right.$$

$$\left. \left( \frac{i (f i (v-2k) + 2 c i z (v-2k))^2}{c (v-2k)} \right)^{\frac{1}{2}(-j-1)} \left( \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i (f i (v-2k) + 2 c i z (v-2k))^2}{4 c (v-2k)}\right) \right) \right) -$$

$$2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{1}{4} i \left( -\frac{f^2 (v-2s)^2}{-2bk+bm+2cs-cv} - 4g(v-2s) + 4e(m-2k) - 2\pi(m-v) \right)} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (-i f (v-2s))^{n-j} (f i (v-2s) + 2 (i c (v-2s) - i b (m-2k)) z)^{j+1} \right) \right.$$

$$\left. \left( -\frac{(f i (v-2s) + 2 (i c (v-2s) - i b (m-2k)) z)^2}{i c (v-2s) - i b (m-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right.$$

$$\left. \Gamma\left(\frac{j+1}{2}, -\frac{(f i (v-2s) + 2 (i c (v-2s) - i b (m-2k)) z)^2}{4 (i c (v-2s) - i b (m-2k))}\right) \right) (i c (v-2s) - i b (m-2k))^{-n-1} +$$

$$e^{\frac{1}{4} i \left( \frac{f^2 (v-2s)^2}{2bk-bm+2cs-cv} + 4g(v-2s) + 4e(m-2k) - 2\pi(m+v) \right)} (b i (m-2k) + c i (v-2s))^{-n-1}$$

$$\sum_{j=0}^n 2^{j-n} (-i f(v-2s))^{n-j} (f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^{j+1}$$

$$\left( -\frac{(f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^2}{b i(m-2k) + c i(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}\right),$$

$$-\frac{(f i(v-2s) + 2(b i(m-2k) + c i(v-2s)) z)^2}{4(b i(m-2k) + c i(v-2s))} + e^{-\frac{1}{4}i\left(\frac{f^2(v-2s)^2}{2bk-bm+2cs-cv} + 4g(v-2s) + 4e(m-2k) - 2\pi(m+v)\right)}$$

$$(-i b(m-2k) - i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i f(v-2s))^{n-j} (2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^{j+1}$$

$$\left( -\frac{(2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{-i b(m-2k) - i c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}\right),$$

$$-\frac{(2(-i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{4(-i b(m-2k) - i c(v-2s))} + e^{\frac{1}{4}i\left(-\frac{f^2(v-2s)^2}{-2bk+bm+2cs-cv} - 4g(v-2s) + 4e(m-2k) + 2\pi(v-m)\right)}$$

$$(i b(m-2k) - i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i f(v-2s))^{n-j} (2(i b(m-2k) - i c(v-2s)) z - i f(v-2s))^{j+1}$$

$$\left( -\frac{(2(i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{i b(m-2k) - i c(v-2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j}$$

$$\Gamma\left(\frac{j+1}{2}, -\frac{(2(i b(m-2k) - i c(v-2s)) z - i f(v-2s))^2}{4(i b(m-2k) - i c(v-2s))}\right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1243.01

$$\int z^n \sin^m(\sqrt{z} b + e) \sin^v(\sqrt{z} c + f z + g) dz = -2^{-m-v+1} (-1)^{n+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (m-2k)^{-2(n+1)} \right)$$

$$\left( e^{i e(m-2k) - \frac{i m \pi}{2}} \Gamma(2(n+1), -i b(m-2k) \sqrt{z}) + e^{\frac{i m \pi}{2} - i e(m-2k)} \Gamma(2(n+1), i b(m-2k) \sqrt{z}) \right) \Big| b^{-2(n+1)} +$$

$$\frac{2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n+1} + 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i(v-2k)c^2}{4f} + \frac{i\pi v}{2} - i g(v-2k)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i c(v-2k))^{-h-j+2n} (-i c(v-2k) - 2 i f \sqrt{z} (v-2k))^{h+j} \right) \right)$$

$$\begin{aligned}
 & \left( -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ic(v-2k) \right. \\
 & \left. (-ic(v-2k) - 2if\sqrt{z}(v-2k)) \Gamma\left( \frac{1}{2}(h+j+1), -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) - 2 \right. \\
 & \left. if(v-2k) \sqrt{-\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma\left( \frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(-ic(v-2k) - 2if\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \left( (-if(v-2k))^{-2(n+1)} + e^{-\frac{i(v-2k)c^2}{4f} - \frac{i\pi v}{2} + gi(v-2k)} \right) \\
 & (if(v-2k))^{-2(n+1)} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k))^{-h-j+2n} (ci(v-2k) + 2fi\sqrt{z}(v-2k))^{h+j} \\
 & \left( \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2k)(ci(v-2k) + 2fi\sqrt{z}(v-2k)) \Gamma\left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) + 2fi(v-2k) \right. \\
 & \left. \left. \sqrt{\frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma\left( \frac{1}{2}(h+j+2), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \right) + \\
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(ib(m-2k) - ic(v-2s))^2}{4f(v-2s)} + e^{i(m-2k) - ig(v-2s) + \frac{1}{2}i(v-m)\pi}} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib(m-2k) - ic(v-2s))^{-h-j+2n} (bi(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{i(bi(m-2k) - ic(v-2s) - 2if(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (i b(m-2k) - i c(v-2s))(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right. \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} \left(i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right) - \\
 & \quad 2 i f(v-2s) \sqrt{\left(-\frac{1}{f(v-2s)} \left(i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right)} \\
 & \quad \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{1}{4 f(v-2s)} \left(i(b i(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right)\right) \\
 & (-i f(v-2s))^{-2(n+1)} + e^{-\frac{i(-i b(m-2k) - i c(v-2s))^2}{4 f(v-2s)} - i e(m-2k) + \frac{1}{2} i \pi(m+v) - i g(v-2s)} \text{Sum} \left( \right. \\
 & \quad \text{Sum} \left( (-1)^{j-h} 4^j (-i b(m-2k) - i c(v-2s))^{-h-j+2n} (-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^{h+j} \right. \\
 & \quad \left. \left(-\frac{1}{f(v-2s)} \left(i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \\
 & \quad \left. \binom{n}{j} \left(-i b(m-2k) - i c(v-2s)\right) (-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z}) \right. \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), -\frac{1}{4 f(v-2s)} \left(i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right) - 2 i f \\
 & \quad (v-2s) \sqrt{\left(-\frac{1}{f(v-2s)} \left(i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right)} \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \quad \left. -\frac{1}{4 f(v-2s)} \left(i(-i b(m-2k) - i c(v-2s) - 2 i f(v-2s) \sqrt{z})^2\right)\right), \{h, 0, j\}, \{j, 0, n\} \left. \right) \\
 & (-i f(v-2s))^{-2(n+1)} + e^{\frac{i(i c(v-2s) - i b(m-2k))^2}{4 f(v-2s)} - i e(m-2k) + \frac{1}{2} i \pi(m-v) + g i(v-2s)} (i f(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2s) - i b(m-2k))^{-h-j+2n} (-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (i c(v-2s) - i b(m-2k)) (-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z}) \right. \\
 & \quad \Gamma\left(\frac{1}{2}(h+j+1), \frac{1}{4 f(v-2s)} \left(i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2\right)\right) + \\
 & \quad 2 f i(v-2s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{1}{4 f(v-2s)} \left(i(-i b(m-2k) + c i(v-2s) + 2 f i(v-2s) \sqrt{z})^2\right)\right) \left. \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\left(\frac{1}{f(v-2s)} \left(i(-ib(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2\right)\right)} + \\
 & e^{\frac{i(bi(m-2k) + ci(v-2s))^2}{4f(v-2s)} + e^{i(m-2k) + g i(v-2s) - \frac{1}{2}i(m+v)\pi}} (if(v-2s))^{-2(n+1)} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (bi(m-2k) + ci(v-2s))^{-h-j+2n} (bi(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z})^{h+j} \\
 & \left(\frac{i(bi(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left(bi(m-2k) + ci(v-2s)\right) (bi(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z}) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(bi(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + \\
 & 2fi(v-2s) \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(bi(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \\
 & \left.\sqrt{\frac{i(bi(m-2k) + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)}}\right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n \sin^m(bz^r + dz) \sin^v(cz^r + fz + g)$**

01.06.21.1244.01

$$\int z^n \sin^m(bz^2 + dz) \sin^v(cz^2 + fz + g) dz =$$

$$\begin{aligned}
 & \frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{n+1} - i^{-m} 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left(e^{\frac{id^2(2k-m)}{4b}}\right) \\
 & \left(\sum_{j=0}^n 2^{j-n} (id(2k-m))^{n-j} (-id(2k-m) - 2ibz(2k-m))^{j+1} \left(-\frac{i(-id(2k-m) - 2ibz(2k-m))^2}{b(2k-m)}\right)^{\frac{1}{2}(-j-1)}\right) \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(2k-m) - 2ibz(2k-m))^2}{4b(2k-m)}\right) (-ib(2k-m))^{-n-1} +
 \end{aligned}$$

$$\begin{aligned}
 & (-1)^m e^{\frac{id^2(m-2k)}{4b}} (-ib(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (id(m-2k))^{n-j} (-id(m-2k) - 2ibz(m-2k))^{j+1} \\
 & \left( -\frac{i(-id(m-2k) - 2ibz(m-2k))^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(m-2k) - 2ibz(m-2k))^2}{4b(m-2k)}\right) \Bigg) - \\
 & (-1)^m i^{-\nu} 2^{-m-\nu-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( (-1)^\nu e^{ig(2k-\nu) - \frac{if^2(2k-\nu)}{4c}} \right. \\
 & \left. \left( \sum_{j=0}^n 2^{j-n} (-if(2k-\nu))^{n-j} (fi(2k-\nu) + 2ciz(2k-\nu))^{j+1} \left( \frac{ifi(2k-\nu) + 2ciz(2k-\nu))^2}{c(2k-\nu)} \right)^{\frac{1}{2}(-j-1)} \right. \right. \\
 & \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{ifi(2k-\nu) + 2ciz(2k-\nu))^2}{4c(2k-\nu)}\right) \right) (ic(2k-\nu))^{-n-1} + \right. \\
 & \left. e^{ig(v-2k) - \frac{if^2(v-2k)}{4c}} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2k))^{n-j} (fi(v-2k) + 2ciz(v-2k))^{j+1} \right. \\
 & \left. \left( \frac{ifi(v-2k) + 2ciz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{ifi(v-2k) + 2ciz(v-2k))^2}{4c(v-2k)}\right) \Bigg) - \\
 & i^{-m-\nu} 2^{-m-\nu-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s \binom{\nu}{s} \left( (-1)^\nu e^{ig(2s-\nu) - \frac{(if(2s-\nu) - id(2k-m))^2}{4(ic(2s-\nu) - ib(2k-m))}} \left( \sum_{j=0}^n 2^{j-n} (id(2k-m) - if(2s-\nu))^{n-j} \right. \right. \\
 & \left. \left. (-id(2k-m) + fi(2s-\nu) + 2(ic(2s-\nu) - ib(2k-m))z)^{j+1} (-id(2k-m) + fi(2s-\nu) + \right. \right. \\
 & \left. \left. 2(ic(2s-\nu) - ib(2k-m))z)^2 / (ic(2s-\nu) - ib(2k-m)) \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \right. \right. \\
 & \left. \left. -(-id(2k-m) + fi(2s-\nu) + 2(ic(2s-\nu) - ib(2k-m))z)^2 / (4(ic(2s-\nu) - ib(2k-m))) \right) \Bigg) \right) \\
 & (ic(2s-\nu) - ib(2k-m))^{-n-1} + (-1)^{m+\nu} e^{ig(2s-\nu) - \frac{(if(2s-\nu) - id(2k-m))^2}{4(ic(2s-\nu) - ib(m-2k))}} (ic(2s-\nu) - ib(m-2k))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (id(m-2k) - if(2s-\nu))^{n-j} (-id(m-2k) + fi(2s-\nu) + 2(ic(2s-\nu) - ib(m-2k))z)^{j+1} \\
 & (-id(m-2k) + fi(2s-\nu) + 2(ic(2s-\nu) - ib(m-2k))z)^2 / (ic(2s-\nu) - ib(m-2k)) \Bigg)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-id(m-2k) + fi(2s-\nu) + 2(ic(2s-\nu) - ib(m-2k))z)^2 / \right. \\
 & \left. (4(ic(2s-\nu) - ib(m-2k))) \right) + e^{ig(v-2s) - \frac{(if(v-2s) - id(2k-m))^2}{4(ic(v-2s) - ib(2k-m))}} (ic(v-2s) - ib(2k-m))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (id(2k-m) - if(v-2s))^{n-j} (-id(2k-m) + fi(v-2s) + 2(ic(v-2s) - ib(2k-m))z)^{j+1}
 \end{aligned}$$



$$\begin{aligned} & \left( -(-i d(2k - m) + f i(v - 2s) + 2(i c(v - 2s) - i b(2k - m)) z)^2 / (i c(v - 2s) - i b(2k - m)) \right)^{\frac{1}{2}(-j-1)} \\ & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d(2k - m) + f i(v - 2s) + 2(i c(v - 2s) - i b(2k - m)) z)^2 / \right. \\ & \quad \left. (4(i c(v - 2s) - i b(2k - m))) \right) + (-1)^m e^{i g(v-2s) - \frac{(i f(v-2s) - i d(m-2k))^2}{4(i c(v-2s) - i b(m-2k))}} (i c(v - 2s) - i b(m - 2k))^{-n-1} \\ & \sum_{j=0}^n 2^{j-n} (i d(m - 2k) - i f(v - 2s))^{n-j} (-i d(m - 2k) + f i(v - 2s) + 2(i c(v - 2s) - i b(m - 2k)) z)^{j+1} \\ & \left( -(-i d(m - 2k) + f i(v - 2s) + 2(i c(v - 2s) - i b(m - 2k)) z)^2 / (i c(v - 2s) - i b(m - 2k)) \right)^{\frac{1}{2}(-j-1)} \\ & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d(m - 2k) + f i(v - 2s) + 2(i c(v - 2s) - i b(m - 2k)) z)^2 / \right. \\ & \quad \left. (4(i c(v - 2s) - i b(m - 2k))) \right) \Bigg) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1245.01

$$\int z^n \sin^m(\sqrt{z} b + d z) \sin^v(\sqrt{z} c + g + f z) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} + i^{-m} 2^{-m-2n-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{i b^2(2k-m)}{4d}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b(2k - m))^{-h-j+2n} (-i b(2k - m) - 2 i d \sqrt{z} (2k - m))^{h+j} \right. \right.$$

$$\left. \left( -\frac{i(-i b(2k - m) - 2 i d \sqrt{z} (2k - m))^2}{d(2k - m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -i b(2k - m) \right. \right.$$

$$\left. \left. (-i b(2k - m) - 2 i d \sqrt{z} (2k - m)) \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{i(-i b(2k - m) - 2 i d \sqrt{z} (2k - m))^2}{4 d(2k - m)}\right) \right) - \right.$$

$$\left. \left. 2 i d(2k - m) \sqrt{-\frac{i(-i b(2k - m) - 2 i d \sqrt{z} (2k - m))^2}{d(2k - m)}} \Gamma\left(\frac{1}{2}(h + j + 2), \right. \right.$$

$$\left. \left. \left. -\frac{i(-i b(2k - m) - 2 i d \sqrt{z} (2k - m))^2}{4 d(2k - m)} \right) \right) \right) \left( (-i d(2k - m))^{-2n-2} + (-1)^m e^{\frac{i b^2(m-2k)}{4d}} \right.$$

$$\left. \left. (-i d(m - 2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b(m - 2k))^{-h-j+2n} (-i b(m - 2k) - 2 i d \sqrt{z} (m - 2k))^{h+j} \right) \right)$$

$$\begin{aligned}
 & \left( \frac{i(-ib(m-2k) - 2id\sqrt{z}(m-2k))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ib(m-2k) \right. \\
 & \left. (-ib(m-2k) - 2id\sqrt{z}(m-2k)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib(m-2k) - 2id\sqrt{z}(m-2k))^2}{4d(m-2k)} \right) \right. \\
 & \left. 2id(m-2k) \sqrt{-\frac{i(-ib(m-2k) - 2id\sqrt{z}(m-2k))^2}{d(m-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(-ib(m-2k) - 2id\sqrt{z}(m-2k))^2}{4d(m-2k)} \right) \right) \Bigg) + (-1)^m i^{-v} 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{ig(2k-v) - \frac{ic^2(2k-v)}{4f}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2k-v))^{-h-j+2n} (ci(2k-v) + 2fi\sqrt{z}(2k-v))^{h+j} \right. \right. \\
 & \left. \left( \frac{i(ci(2k-v) + 2fi\sqrt{z}(2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(2k-v)(ci(2k-v) + 2fi\sqrt{z}(2k-v)) \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ci(2k-v) + 2fi\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) + 2fi(2k-v) \right. \right. \\
 & \left. \left. \sqrt{\frac{i(ci(2k-v) + 2fi\sqrt{z}(2k-v))^2}{f(2k-v)}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(ci(2k-v) + 2fi\sqrt{z}(2k-v))^2}{4f(2k-v)} \right) \right) \right) \\
 & (if(2k-v))^{-2n-2} + e^{ig(v-2k) - \frac{ic^2(v-2k)}{4f}} (if(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2k))^{-h-j+2n} \\
 & (ci(v-2k) + 2fi\sqrt{z}(v-2k))^{h+j} \left( \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( ci(v-2k)(ci(v-2k) + 2fi\sqrt{z}(v-2k)) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(ci(v-2k) + 2fi\sqrt{z}(v-2k))^2}{4f(v-2k)} \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 f i (v-2 k) \sqrt{\frac{i(c i(v-2 k)+2 f i \sqrt{z}(v-2 k))^2}{f(v-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left.\frac{i(c i(v-2 k)+2 f i \sqrt{z}(v-2 k))^2}{4 f(v-2 k)}\right) + i^{-m-v} 2^{-m-2 n-v-1} \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s} \left( (-1)^v e^{i g(2 k-v)-\frac{(i c(2 k-v)-i b(2 s-m))^2}{4(i f(2 k-v)-i d(2 s-m))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(2 k-v)-i b(2 s-m))^{-h-j+2 n} \right. \right. \\
 & \left. \left. (-i b(2 s-m)+c i(2 k-v)+2(i f(2 k-v)-i d(2 s-m)) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -(-i b(2 s-m)+c i(2 k-v)+2(i f(2 k-v)-i d(2 s-m)) \sqrt{z})^2 \right) / \right. \right. \\
 & \left. \left. (i f(2 k-v)-i d(2 s-m)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (i c(2 k-v)-i b(2 s-m))(-i b(2 s-m)+c i(2 k-v)+2(i f(2 k-v)-i d(2 s-m)) \sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -(-i b(2 s-m)+c i(2 k-v)+2(i f(2 k-v)-i d(2 s-m)) \sqrt{z})^2 \right) / \right. \right. \\
 & \left. \left. (4(i f(2 k-v)-i d(2 s-m))) \right) + 2(i f(2 k-v)-i d(2 s-m)) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+2), -(-i b(2 s-m)+c i(2 k-v)+2(i f(2 k-v)-i d(2 s-m)) \sqrt{z})^2 \right) / \right. \\
 & \left. \left. (4(i f(2 k-v)-i d(2 s-m))) \right) \sqrt{\left( -(-i b(2 s-m)+c i(2 k-v)+ \right. \right.} \\
 & \left. \left. 2(i f(2 k-v)-i d(2 s-m)) \sqrt{z})^2 \right) / (i f(2 k-v)-i d(2 s-m)) \right) \left. \right) \\
 & (i f(2 k-v)-i d(2 s-m))^{-2 n-2} + (-1)^{m+v} e^{i g(2 k-v)-\frac{(i c(2 k-v)-i b(m-2 s))^2}{4(i f(2 k-v)-i d(m-2 s))}} (i f(2 k-v)-i d(m-2 s))^{-2 n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(2 k-v)-i b(m-2 s))^{-h-j+2 n} \\
 & \left. (-i b(m-2 s)+c i(2 k-v)+2(i f(2 k-v)-i d(m-2 s)) \sqrt{z})^{h+j} \right. \\
 & \left. \left( \frac{(-i b(m-2 s)+c i(2 k-v)+2(i f(2 k-v)-i d(m-2 s)) \sqrt{z})^2}{i f(2 k-v)-i d(m-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (i c(2 k-v)-i b(m-2 s))(-i b(m-2 s)+c i(2 k-v)+2(i f(2 k-v)-i d(m-2 s)) \sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -(-i b(m-2 s)+c i(2 k-v)+2(i f(2 k-v)-i d(m-2 s)) \sqrt{z})^2 \right) / \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. (4(i f(2 k-v)-i d(m-2 s)))\right) + 2(i f(2 k-v)-i d(m-2 s)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(-i b(m-2 s)+c i(2 k-v)+2(i f(2 k-v)-i d(m-2 s)) \sqrt{z})^2 / \right. \\
 & \left. (4(i f(2 k-v)-i d(m-2 s)))\right) \sqrt{\left(-(-i b(m-2 s)+c i(2 k-v)+\right. \\
 & \left. 2(i f(2 k-v)-i d(m-2 s)) \sqrt{z})^2 / (i f(2 k-v)-i d(m-2 s))\right)} + \\
 & (-1)^m e^{i g(v-2 k)-\frac{(i c(v-2 k)-i b(m-2 s))^2}{4(i f(v-2 k)-i d(m-2 s))}} (i f(v-2 k)-i d(m-2 s))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2 k)- \\
 & i b(m-2 s))^{-h-j+2 n}(-i b(m-2 s)+c i(v-2 k)+2(i f(v-2 k)-i d(m-2 s)) \sqrt{z})^{h+j} \\
 & \left(-\frac{(-i b(m-2 s)+c i(v-2 k)+2(i f(v-2 k)-i d(m-2 s)) \sqrt{z})^2}{i f(v-2 k)-i d(m-2 s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left((i c(v-2 k)-i b(m-2 s))(-i b(m-2 s)+c i(v-2 k)+2(i f(v-2 k)-i d(m-2 s)) \sqrt{z})\right) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(-i b(m-2 s)+c i(v-2 k)+2(i f(v-2 k)-i d(m-2 s)) \sqrt{z})^2 / \right. \\
 & \left. (4(i f(v-2 k)-i d(m-2 s)))\right) + 2(i f(v-2 k)-i d(m-2 s)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(-i b(m-2 s)+c i(v-2 k)+2(i f(v-2 k)-i d(m-2 s)) \sqrt{z})^2 / \right. \\
 & \left. (4(i f(v-2 k)-i d(m-2 s)))\right) \sqrt{\left(-(-i b(m-2 s)+c i(v-2 k)+\right. \\
 & \left. 2(i f(v-2 k)-i d(m-2 s)) \sqrt{z})^2 / (i f(v-2 k)-i d(m-2 s))\right)} + \\
 & e^{i g(v-2 k)-\frac{(i c(v-2 k)-i b(2 s-m))^2}{4(i f(v-2 k)-i d(2 s-m))}} (i f(v-2 k)-i d(2 s-m))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2 k)- \\
 & i b(2 s-m))^{-h-j+2 n}(-i b(2 s-m)+c i(v-2 k)+2(i f(v-2 k)-i d(2 s-m)) \sqrt{z})^{h+j} \\
 & \left(-\frac{(-i b(2 s-m)+c i(v-2 k)+2(i f(v-2 k)-i d(2 s-m)) \sqrt{z})^2}{i f(v-2 k)-i d(2 s-m)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left((i c(v-2 k)-i b(2 s-m))(-i b(2 s-m)+c i(v-2 k)+2(i f(v-2 k)-i d(2 s-m)) \sqrt{z})\right) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(-i b(2 s-m)+c i(v-2 k)+2(i f(v-2 k)-i d(2 s-m)) \sqrt{z})^2 / \right. \\
 & \left. (4(i f(v-2 k)-i d(2 s-m)))\right) + 2(i f(v-2 k)-i d(2 s-m)) \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left.-(-i b(2 s-m)+c i(v-2 k)+2(i f(v-2 k)-i d(2 s-m)) \sqrt{z})^2 / (4(i f(v-2 k)-\right. \\
 & \left. i d(2 s-m)))\right) \sqrt{\left(-(-i b(2 s-m)+c i(v-2 k)+2(i f(v-2 k)-i d(2 s-m))\right)
 \end{aligned}$$

### Involving $z^n \sin^m(bz^r + dz + e) \sin^v(cz^r + fz + g)$

01.06.21.1246.01

$$\int z^n \sin^m(bz^2 + dz + e) \sin^v(cz^2 + fz + g) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} - i^{-m} 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{id^2(2k-m)}{4b} - ie(2k-m)} \left( \sum_{j=0}^n 2^{j-n} (id(2k-m))^{n-j} (-id(2k-m) - 2ibz(2k-m))^{j+1} \right. \right. \\ \left. \left. \left( -\frac{i(-id(2k-m) - 2ibz(2k-m))^2}{b(2k-m)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(2k-m) - 2ibz(2k-m))^2}{4b(2k-m)}\right) \right) \right)$$

$$(-ib(2k-m))^{-n-1} + (-1)^m e^{\frac{id^2(m-2k)}{4b} - ie(m-2k)} (-ib(m-2k))^{-n-1}$$

$$\sum_{j=0}^n 2^{j-n} (id(m-2k))^{n-j} (-id(m-2k) - 2ibz(m-2k))^{j+1}$$

$$\left( -\frac{i(-id(m-2k) - 2ibz(m-2k))^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(-id(m-2k) - 2ibz(m-2k))^2}{4b(m-2k)}\right) \Bigg| -$$

$$(-1)^m i^{-v} 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{ig(2k-v) - \frac{if^2(2k-v)}{4c}} \right.$$

$$\left. \left( \sum_{j=0}^n 2^{j-n} (-if(2k-v))^{n-j} (fi(2k-v) + 2ciz(2k-v))^{j+1} \left( \frac{i(fi(2k-v) + 2ciz(2k-v))^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(2k-v) + 2ciz(2k-v))^2}{4c(2k-v)}\right) \right) \right) (ic(2k-v))^{-n-1} +$$

$$e^{ig(v-2k) - \frac{if^2(v-2k)}{4c}} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-if(v-2k))^{n-j} (fi(v-2k) + 2ciz(v-2k))^{j+1}$$

$$\left( \frac{i(fi(v-2k) + 2ciz(v-2k))^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(fi(v-2k) + 2ciz(v-2k))^2}{4c(v-2k)}\right) \Bigg| -$$

$$2^{-m-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(if(2s-v) - id(2k-m))^2}{4(ic(2s-v) - ib(2k-m))} - ie(2k-m) + gi(2s-v)} \right.$$

$$\begin{aligned}
 & \left( \sum_{j=0}^n 2^{j-n} (i d (2 k - m) - i f (2 s - v))^{n-j} (-i d (2 k - m) + f i (2 s - v) + 2 (i c (2 s - v) - i b (2 k - m)) z)^{j+1} \right. \\
 & \quad \left. (-(-i d (2 k - m) + f i (2 s - v) + 2 (i c (2 s - v) - i b (2 k - m)) z)^2 / (i c (2 s - v) - i b (2 k - m)))^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d (2 k - m) + f i (2 s - v) + 2 (i c (2 s - v) - i b (2 k - m)) z)^2 / \right. \right. \\
 & \quad \left. \left. (4 (i c (2 s - v) - i b (2 k - m)))\right) \right) (i c (2 s - v) - i b (2 k - m))^{-n-1} + \\
 & (-1)^{m+v} e^{-\frac{(i f (2 s - v) - i d (m - 2 k))^2}{4 (i c (2 s - v) - i b (m - 2 k))} - i e (m - 2 k) + g i (2 s - v)} (i c (2 s - v) - i b (m - 2 k))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (i d (m - 2 k) - i f (2 s - v))^{n-j} (-i d (m - 2 k) + f i (2 s - v) + 2 (i c (2 s - v) - i b (m - 2 k)) z)^{j+1} \\
 & \quad \left. (-(-i d (m - 2 k) + f i (2 s - v) + 2 (i c (2 s - v) - i b (m - 2 k)) z)^2 / (i c (2 s - v) - i b (m - 2 k)))^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d (m - 2 k) + f i (2 s - v) + 2 (i c (2 s - v) - i b (m - 2 k)) z)^2 / (4 (i c (2 s - v) - \right. \right. \\
 & \quad \left. \left. i b (m - 2 k)))\right) + e^{-\frac{(i f (v - 2 s) - i d (2 k - m))^2}{4 (i c (v - 2 s) - i b (2 k - m))} - i e (2 k - m) + g i (v - 2 s)} (i c (v - 2 s) - i b (2 k - m))^{-n-1} \right. \\
 & \sum_{j=0}^n 2^{j-n} (i d (2 k - m) - i f (v - 2 s))^{n-j} (-i d (2 k - m) + f i (v - 2 s) + 2 (i c (v - 2 s) - i b (2 k - m)) z)^{j+1} \\
 & \quad \left. (-(-i d (2 k - m) + f i (v - 2 s) + 2 (i c (v - 2 s) - i b (2 k - m)) z)^2 / (i c (v - 2 s) - i b (2 k - m)))^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d (2 k - m) + f i (v - 2 s) + 2 (i c (v - 2 s) - i b (2 k - m)) z)^2 / (4 (i c (v - 2 s) - \right. \right. \\
 & \quad \left. \left. i b (2 k - m)))\right) + (-1)^m e^{-\frac{(i f (v - 2 s) - i d (m - 2 k))^2}{4 (i c (v - 2 s) - i b (m - 2 k))} - i e (m - 2 k) + g i (v - 2 s)} (i c (v - 2 s) - i b (m - 2 k))^{-n-1} \right. \\
 & \sum_{j=0}^n 2^{j-n} (i d (m - 2 k) - i f (v - 2 s))^{n-j} (-i d (m - 2 k) + f i (v - 2 s) + 2 (i c (v - 2 s) - i b (m - 2 k)) z)^{j+1} \\
 & \quad \left. (-(-i d (m - 2 k) + f i (v - 2 s) + 2 (i c (v - 2 s) - i b (m - 2 k)) z)^2 / (i c (v - 2 s) - i b (m - 2 k)))^{\frac{1}{2}(-j-1)} \right. \\
 & \quad \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(-i d (m - 2 k) + f i (v - 2 s) + 2 (i c (v - 2 s) - i b (m - 2 k)) z)^2 / \right. \right. \\
 & \quad \left. \left. (4 (i c (v - 2 s) - i b (m - 2 k)))\right) \right) \Bigg/ ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1247.01

$$\int z^n \sin^m(\sqrt{z} b + d z + e) \sin^v(\sqrt{z} c + f z + g) dz =$$

$$\frac{(-1)^m 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{n + 1} + i^{-m} 2^{-m-2n-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\begin{aligned}
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{ib^2(2k-m)-ie(2k-m)}{4d}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib(2k-m))^{-h-j+2n} (-ib(2k-m)-2id\sqrt{z}(2k-m))^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{i(-ib(2k-m)-2id\sqrt{z}(2k-m))^2}{d(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ib(2k-m) \right. \right. \right. \\
 & \left. \left. \left. (-ib(2k-m)-2id\sqrt{z}(2k-m)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib(2k-m)-2id\sqrt{z}(2k-m))^2}{4d(2k-m)} \right) \right. \right. \right. \\
 & \left. \left. \left. 2id(2k-m) \sqrt{-\frac{i(-ib(2k-m)-2id\sqrt{z}(2k-m))^2}{d(2k-m)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. \left. \left. -\frac{i(-ib(2k-m)-2id\sqrt{z}(2k-m))^2}{4d(2k-m)} \right) \right) \right) \right) \left( (-id(2k-m))^{-2n-2} + (-1)^m e^{\frac{ib^2(m-2k)-ie(m-2k)}{4d}} \right. \\
 & \left. (-id(m-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib(m-2k))^{-h-j+2n} (-ib(m-2k)-2id\sqrt{z}(m-2k))^{h+j} \right. \\
 & \left. \left( -\frac{i(-ib(m-2k)-2id\sqrt{z}(m-2k))^2}{d(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( -ib(m-2k) \right. \right. \\
 & \left. \left. (-ib(m-2k)-2id\sqrt{z}(m-2k)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib(m-2k)-2id\sqrt{z}(m-2k))^2}{4d(m-2k)} \right) \right. \right. \\
 & \left. \left. 2id(m-2k) \sqrt{-\frac{i(-ib(m-2k)-2id\sqrt{z}(m-2k))^2}{d(m-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. \left. \left. -\frac{i(-ib(m-2k)-2id\sqrt{z}(m-2k))^2}{4d(m-2k)} \right) \right) \right) \right) + (-1)^m i^{-v} 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{ig(2k-v)-\frac{ic^2(2k-v)}{4f}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2k-v))^{-h-j+2n} (ci(2k-v)+2fi\sqrt{z}(2k-v))^{h+j} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{i(c i(2k-v) + 2f i \sqrt{z}(2k-v))^2}{f(2k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( c i(2k-v) (c i(2k-v) + 2f i \sqrt{z}(2k-v)) \right. \\
 & \left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c i(2k-v) + 2f i \sqrt{z}(2k-v))^2}{4f(2k-v)} \right) + 2f i(2k-v) \right. \\
 & \left. \sqrt{\frac{i(c i(2k-v) + 2f i \sqrt{z}(2k-v))^2}{f(2k-v)}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c i(2k-v) + 2f i \sqrt{z}(2k-v))^2}{4f(2k-v)} \right) \right) \\
 & (i f(2k-v))^{-2n-2} + e^{i g(v-2k) - \frac{ic^2(v-2k)}{4f}} (i f(v-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k))^{-h-j+2n} \\
 & (c i(v-2k) + 2f i \sqrt{z}(v-2k))^{h+j} \left( \frac{i(c i(v-2k) + 2f i \sqrt{z}(v-2k))^2}{f(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( c i(v-2k) (c i(v-2k) + 2f i \sqrt{z}(v-2k)) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(c i(v-2k) + 2f i \sqrt{z}(v-2k))^2}{4f(v-2k)} \right) + \right. \\
 & \left. 2f i(v-2k) \sqrt{\frac{i(c i(v-2k) + 2f i \sqrt{z}(v-2k))^2}{f(v-2k)}} \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(c i(v-2k) + 2f i \sqrt{z}(v-2k))^2}{4f(v-2k)} \right) \right) \\
 & 2^{-m-2n-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s} \left( (-1)^v e^{-\frac{(ic(2k-v) - ib(2s-m))^2}{4(if(2k-v) - id(2s-m))}} - i e^{(2s-m)g + i(2k-v)} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(2k-v) - i b(2s-m))^{-h-j+2n} (-i b(2s-m) + c i(2k-v) + \right. \right. \\
 & \left. \left. 2(i f(2k-v) - i d(2s-m)) \sqrt{z} \right)^{h+j} \left( -i b(2s-m) + c i(2k-v) + \right. \right. \\
 & \left. \left. 2(i f(2k-v) - i d(2s-m)) \sqrt{z} \right)^2 / (i f(2k-v) - i d(2s-m)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \left. \binom{n}{j} \left( (i c(2k-v) - i b(2s-m)) (-i b(2s-m) + c i(2k-v) + 2(i f(2k-v) - i d(2s-m)) \sqrt{z}) \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \Gamma\left(\frac{1}{2}(h+j+1), -(-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z})^2 / \right. \\
 & \quad \left. (4(if(2k-v) - id(2s-m)))\right) + 2(if(2k-v) - id(2s-m)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(-ib(2s-m) + ci(2k-v) + 2(if(2k-v) - id(2s-m))\sqrt{z})^2 / \right. \\
 & \quad \left. (4(if(2k-v) - id(2s-m)))\right) \sqrt{\left(-(-ib(2s-m) + ci(2k-v) + \right. \\
 & \quad \left. 2(if(2k-v) - id(2s-m))\sqrt{z})^2 / (if(2k-v) - id(2s-m))\right)} \\
 & (if(2k-v) - id(2s-m))^{-2n-2} + (-1)^{m+v} e^{-\frac{(ic(2k-v)-ib(m-2s))^2}{4(if(2k-v)-id(m-2s))} - ie^{(m-2s)+gi(2k-v)}} \\
 & (if(2k-v) - id(m-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2k-v) - ib(m-2s))^{-h-j+2n} \\
 & \quad (-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})^{h+j} \left(-(-ib(m-2s) + ci(2k-v) + \right. \\
 & \quad \left. 2(if(2k-v) - id(m-2s))\sqrt{z})^2 / (if(2k-v) - id(m-2s))\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( (ic(2k-v) - ib(m-2s))(-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z}) \right) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})^2 / \right. \\
 & \quad \left. (4(if(2k-v) - id(m-2s)))\right) + 2(if(2k-v) - id(m-2s)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(-ib(m-2s) + ci(2k-v) + 2(if(2k-v) - id(m-2s))\sqrt{z})^2 / \right. \\
 & \quad \left. (4(if(2k-v) - id(m-2s)))\right) \sqrt{\left(-(-ib(m-2s) + ci(2k-v) + \right. \\
 & \quad \left. 2(if(2k-v) - id(m-2s))\sqrt{z})^2 / (if(2k-v) - id(m-2s))\right)} + \\
 & e^{-\frac{(ic(v-2k)-ib(2s-m))^2}{4(if(v-2k)-id(2s-m))} - ie^{(2s-m)+gi(v-2k)}} (if(v-2k) - id(2s-m))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j \\
 & (ic(v-2k) - ib(2s-m))^{-h-j+2n} (-ib(2s-m) + ci(v-2k) + 2(if(v-2k) - id(2s-m)) \\
 & \quad \sqrt{z})^{h+j} \left(-(-ib(2s-m) + ci(v-2k) + 2(if(v-2k) - id(2s-m))\sqrt{z})^2 / \right. \\
 & \quad \left. (if(v-2k) - id(2s-m))\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ic(v-2k) - ib(2s-m))(-ib(2s-m) + ci(v-2k) + 2(if(v-2k) - id(2s-m))\sqrt{z}) \right) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(-ib(2s-m) + ci(v-2k) + 2(if(v-2k) - id(2s-m))\sqrt{z})^2 / \right. \\
 & \quad \left. (4(if(v-2k) - id(2s-m)))\right) + 2(if(v-2k) - id(2s-m)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(-ib(2s-m) + ci(v-2k) + 2(if(v-2k) - id(2s-m))\sqrt{z})^2 / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( 4(i f(v-2k) - i d(2s-m)) \right) \sqrt{\left( -i b(2s-m) + c i(v-2k) + \right. \right. \\
 & \quad \left. \left. 2(i f(v-2k) - i d(2s-m)) \sqrt{z} \right)^2 / (i f(v-2k) - i d(2s-m)) \right) + \\
 & (-1)^m e^{-\frac{(i c(v-2k) - i b(m-2s))^2}{4(i f(v-2k) - i d(m-2s))} - i e(m-2s) + g i(v-2k)} (i f(v-2k) - i d(m-2s))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(v-2k) - i b(m-2s))^{-h-j+2n} \\
 & \quad (-i b(m-2s) + c i(v-2k) + 2(i f(v-2k) - i d(m-2s)) \sqrt{z})^{h+j} \\
 & \quad \left( -i b(m-2s) + c i(v-2k) + 2(i f(v-2k) - i d(m-2s)) \sqrt{z} \right)^2 / \\
 & \quad (i f(v-2k) - i d(m-2s))^{1/2(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad \left( (i c(v-2k) - i b(m-2s)) (-i b(m-2s) + c i(v-2k) + 2(i f(v-2k) - i d(m-2s)) \sqrt{z}) \right. \\
 & \quad \Gamma\left( \frac{1}{2}(h+j+1), -(-i b(m-2s) + c i(v-2k) + 2(i f(v-2k) - i d(m-2s)) \sqrt{z})^2 / \right. \\
 & \quad \left. \left. (4(i f(v-2k) - i d(m-2s))) \right) + 2(i f(v-2k) - i d(m-2s)) \Gamma\left( \frac{1}{2}(h+j+2), \right. \right. \\
 & \quad \left. \left. -(-i b(m-2s) + c i(v-2k) + 2(i f(v-2k) - i d(m-2s)) \sqrt{z})^2 / (4(i f(v-2k) - \right. \right. \\
 & \quad \left. \left. i d(m-2s))) \right) \sqrt{\left( -i b(m-2s) + c i(v-2k) + 2(i f(v-2k) - i d(m-2s)) \right. \right. \\
 & \quad \left. \left. \sqrt{z} \right)^2 / (i f(v-2k) - i d(m-2s)) \right) \Bigg) / ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving products of powers of several direct functions and a power function

### Involving $z^{\alpha-1} \sin^2(az) \sin(bz) \sin(cz)$

01.06.21.1248.01

$$\begin{aligned}
 & \int z^{\alpha-1} \sin^2(az) \sin(bz) \sin(cz) dz = \\
 & \frac{1}{16} z^\alpha \left( -(-i(2a-b-c)z)^{-\alpha} \Gamma(\alpha, -i(2a-b-c)z) - (i(2a-b-c)z)^{-\alpha} \Gamma(\alpha, i(2a-b-c)z) - \right. \\
 & \quad 2(-i(b-c)z)^{-\alpha} \Gamma(\alpha, -i(b-c)z) - 2(i(b-c)z)^{-\alpha} \Gamma(\alpha, i(b-c)z) + (-i(2a+b-c)z)^{-\alpha} \Gamma(\alpha, -i(2a+b-c)z) + \\
 & \quad (i(2a+b-c)z)^{-\alpha} \Gamma(\alpha, i(2a+b-c)z) + (-i(2a-b+c)z)^{-\alpha} \Gamma(\alpha, -i(2a-b+c)z) + \\
 & \quad (i(2a-b+c)z)^{-\alpha} \Gamma(\alpha, i(2a-b+c)z) + 2(-i(b+c)z)^{-\alpha} \Gamma(\alpha, -i(b+c)z) + 2(i(b+c)z)^{-\alpha} \Gamma(\alpha, i(b+c)z) - \\
 & \quad \left. (-i(2a+b+c)z)^{-\alpha} \Gamma(\alpha, -i(2a+b+c)z) - (i(2a+b+c)z)^{-\alpha} \Gamma(\alpha, i(2a+b+c)z) \right)
 \end{aligned}$$

01.06.21.1249.01

$$\begin{aligned}
 & \int \frac{\sin^2(az) \sin(bz) \sin(cz)}{z} dz = \\
 & \frac{1}{8} (\text{Ci}((2a-b-c)z) + 2 \text{Ci}(b-c)z) - \text{Ci}((2a+b-c)z) - \text{Ci}(2a-b+c)z - 2 \text{Ci}(b+c)z + \text{Ci}((2a+b+c)z)
 \end{aligned}$$

### Involving rational functions of the direct function and a power function

Involving  $\frac{z}{a+b \sin(cz+d)}$

01.06.21.1250.01

$$\int \frac{z}{1 - \sin(z)} dz = \frac{2 \sin\left(\frac{z}{2}\right) z}{\cos\left(\frac{z}{2}\right) - \sin\left(\frac{z}{2}\right)} + z - 2 \tanh^{-1}\left(\tan\left(\frac{z}{2}\right)\right) + \log(\cos(z))$$

01.06.21.1251.01

$$\int \frac{z}{\sin(z) + 1} dz = \frac{2 \sin\left(\frac{z}{2}\right) z}{\cos\left(\frac{z}{2}\right) + \sin\left(\frac{z}{2}\right)} - z + 2 \tanh^{-1}\left(\tan\left(\frac{z}{2}\right)\right) + \log(\cos(z))$$

01.06.21.1252.01

$$\int \frac{z}{a + b \sin(cz)} dz = \frac{1}{c^2} \left( \frac{\pi \tan^{-1} \left( \frac{b+a \tan\left(\frac{cz}{2}\right)}{\sqrt{a^2-b^2}} \right)}{\sqrt{a^2-b^2}} + \right.$$

$$\frac{1}{\sqrt{b^2-a^2}} \left( (\pi - 2cz) \tanh^{-1} \left( \frac{(a+b) \cot\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) + 2 \cos^{-1} \left( -\frac{a}{b} \right) \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) + \right.$$

$$\left. \left( \cos^{-1} \left( -\frac{a}{b} \right) - 2i \tanh^{-1} \left( \frac{(a+b) \cot\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) - 2i \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) \right) \right)$$

$$\log \left( \frac{\left(\frac{1}{2} - \frac{i}{2}\right) \sqrt{b^2-a^2} e^{\frac{icz}{2}}}{\sqrt{b} \sqrt{a+b \sin(cz)}} \right) + \left( \cos^{-1} \left( -\frac{a}{b} \right) + \right.$$

$$\left. 2i \left( \tanh^{-1} \left( \frac{(a+b) \cot\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) + \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) \right) \right) \log \left( \frac{\left(\frac{1}{2} + \frac{i}{2}\right) \sqrt{b^2-a^2} e^{-\frac{icz}{2}}}{\sqrt{b} \sqrt{a+b \sin(cz)}} \right) -$$

$$\left( \cos^{-1} \left( -\frac{a}{b} \right) - 2i \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) \right) \log \left( \frac{(a+b) \left( ia - ib + \sqrt{b^2-a^2} \right) \left( i + \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)}{b \left( a + b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)} \right) -$$

$$\left( \cos^{-1} \left( -\frac{a}{b} \right) + 2i \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(\pi - 2cz)\right)}{\sqrt{b^2-a^2}} \right) \right) \log \left( \frac{(a+b) \left( -a + b - i \sqrt{b^2-a^2} \right) \left( i \tan\left(\frac{1}{4}(\pi - 2cz)\right) + 1 \right)}{b \left( a + b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)} \right) +$$

$$i \left( \operatorname{Li}_2 \left( \frac{\left( a - i \sqrt{b^2-a^2} \right) \left( a + b - \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)}{b \left( a + b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)} \right) \right) -$$

$$\operatorname{Li}_2 \left( \frac{\left( a + i \sqrt{b^2-a^2} \right) \left( a + b - \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)}{b \left( a + b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(\pi - 2cz)\right) \right)} \right) \right)$$

01.06.21.1253.01

$$\int \frac{z}{a + b \sin(d + cz)} dz =$$

$$\frac{1}{c^2} \left( \frac{\pi \tan^{-1} \left( \frac{b+a \tan\left(\frac{1}{2}(d+cz)\right)}{\sqrt{a^2-b^2}} \right)}{\sqrt{a^2-b^2}} + \frac{1}{\sqrt{b^2-a^2}} \left( -(2d+2cz-\pi) \tanh^{-1} \left( \frac{(a+b) \cot\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) \right) - \right.$$

$$\left. 2 \left( d - \cos^{-1} \left( -\frac{a}{b} \right) \right) \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) + \right.$$

$$\left. \left( \cos^{-1} \left( -\frac{a}{b} \right) + 2i \left( \tanh^{-1} \left( \frac{(a+b) \cot\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) + \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) \right) \right) \right)$$

$$\log \left( \frac{\sqrt[4]{-1} \sqrt{b^2-a^2} e^{-\frac{1}{2}i(d+cz)}}{\sqrt{2} \sqrt{b} \sqrt{a+b \sin(d+cz)}} \right) +$$

$$\left( \cos^{-1} \left( -\frac{a}{b} \right) - 2i \tanh^{-1} \left( \frac{(a+b) \cot\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) - 2i \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) \right)$$

$$\log \left( -\frac{(-1)^{3/4} \sqrt{b^2-a^2} e^{\frac{1}{2}i(d+cz)}}{\sqrt{2} \sqrt{b} \sqrt{a+b \sin(d+cz)}} \right) - \left( \cos^{-1} \left( -\frac{a}{b} \right) - 2i \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) \right)$$

$$\log \left( \frac{(a+b) \left( ia - ib + \sqrt{b^2-a^2} \right) \left( i + \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)}{b \left( a+b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)} \right) -$$

$$\left( \cos^{-1} \left( -\frac{a}{b} \right) + 2i \tanh^{-1} \left( \frac{(a-b) \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right)}{\sqrt{b^2-a^2}} \right) \right)$$

$$\log \left( \frac{(a+b) \left( -a+b-i\sqrt{b^2-a^2} \right) \left( i \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) + 1 \right)}{b \left( a+b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)} \right) +$$

$$i \operatorname{Li}_2 \left( \frac{\left( a-i\sqrt{b^2-a^2} \right) \left( a+b-\sqrt{b^2-a^2} \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)}{b \left( a+b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)} \right) -$$

$$\operatorname{Li}_2 \left( \frac{\left( a+i\sqrt{b^2-a^2} \right) \left( a+b-\sqrt{b^2-a^2} \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)}{b \left( a+b + \sqrt{b^2-a^2} \tan\left(\frac{1}{4}(-2d-2cz+\pi)\right) \right)} \right) \right)$$



Involving  $\frac{z \sin(cz)}{(a+b \sin^2(cz))^\beta}$

01.06.21.1255.01

$$\int \frac{z \sin(cz)}{(a+b \sin^2(cz))^{3/2}} dz = \frac{1}{(a+b)c^2} \left( \frac{1}{\sqrt{-b}} \tan^{-1} \left( \frac{\sqrt{2} \sqrt{-b} \sin(cz)}{\sqrt{2a+b-b \cos(2cz)}} \right) - \frac{\sqrt{2} cz \cos(cz)}{\sqrt{2a+b-b \cos(2cz)}} \right)$$

**Involving functions of the direct function and algebraic functions**

**Involving products of the direct function and algebraic functions**

Involving products of two direct functions and algebraic functions

**Involving  $(f + ez)^{\alpha-1} \sin(d + cz) \sin(b + az)$**

01.06.21.1256.01

$$\begin{aligned} \int (f + ez)^{\alpha-1} \sin(d + cz) \sin(b + az) dz = & \frac{1}{4e} \left( (f + ez)^\alpha \left( \frac{(a-c)^2 (f + ez)^2}{e^2} \right)^{-\alpha} \left( \frac{(a+c)^2 (f + ez)^2}{e^2} \right)^{-\alpha} \right. \\ & \left( \left( \Gamma \left( \alpha, -\frac{i(a+c)(f + ez)}{e} \right) \right) \left( \cos \left( b + d - \frac{(a+c)f}{e} \right) + i \sin \left( b + d - \frac{(a+c)f}{e} \right) \right) \left( \frac{i(a+c)(f + ez)}{e} \right)^\alpha + \right. \\ & \left. \left( -\frac{i(a+c)(f + ez)}{e} \right)^\alpha \Gamma \left( \alpha, \frac{i(a+c)(f + ez)}{e} \right) \left( \cos \left( b + d - \frac{(a+c)f}{e} \right) - i \sin \left( b + d - \frac{(a+c)f}{e} \right) \right) \right) \\ & \left( \frac{(a-c)^2 (f + ez)^2}{e^2} \right)^\alpha - \left( \frac{i(a-c)(f + ez)}{e} \right)^\alpha \left( \frac{(a+c)^2 (f + ez)^2}{e^2} \right)^\alpha \Gamma \left( \alpha, \frac{i(c-a)(f + ez)}{e} \right) \\ & \left( \cos \left( b - d + \frac{(c-a)f}{e} \right) + i \sin \left( b - d + \frac{(c-a)f}{e} \right) \right) - \left( \frac{i(c-a)(f + ez)}{e} \right)^\alpha \left( \frac{(a+c)^2 (f + ez)^2}{e^2} \right)^\alpha \\ & \left. \Gamma \left( \alpha, \frac{i(a-c)(f + ez)}{e} \right) \left( \cos \left( b - d + \frac{(c-a)f}{e} \right) - i \sin \left( b - d + \frac{(c-a)f}{e} \right) \right) \right) \end{aligned}$$

01.06.21.1257.01

$$\begin{aligned} \int \frac{\sin(d + cz) \sin(b + az)}{f + ez} dz = & \frac{1}{2e} \left( \cos \left( \frac{be - de - af + cf}{e} \right) \text{Ci} \left( \frac{(a-c)(f + ez)}{e} \right) - \cos \left( b + d - \frac{(a+c)f}{e} \right) \text{Ci} \left( \frac{(a+c)(f + ez)}{e} \right) - \right. \\ & \left. \sin \left( \frac{be - de - af + cf}{e} \right) \text{Si} \left( \frac{(a-c)(f + ez)}{e} \right) + \sin \left( b + d - \frac{(a+c)f}{e} \right) \text{Si} \left( \frac{(a+c)(f + ez)}{e} \right) \right) \end{aligned}$$

01.06.21.1258.01

$$\int \frac{\sin(az) \sin(b + az)}{b + az} dz = -\frac{\cos(b) \text{Ci}(2(b + az)) - \cos(b) \log(b + az) + \sin(b) \text{Si}(2(b + az))}{2a}$$

**Involving functions of the direct function and exponential function**

## Involving powers of the direct function and exponential function

### Involving powers of sin and exp

#### Involving $e^{bz} \sin^v(az)$

01.06.21.1259.01

$$\int e^{bz} \sin^v(az) dz = \frac{e^{bz} (1 - e^{2iaz})^{-v} \sin^v(az)}{b - iav} {}_2F_1\left(-\frac{ib + av}{2a}, -v; 1 - \frac{ib}{2a} - \frac{v}{2}; e^{2iaz}\right)$$

01.06.21.1260.01

$$\int e^{bz} \sin^v(az) dz = \frac{2^{-v} e^{bz} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{b} + 2^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{i\pi v}{2}} \left( \frac{e^{(-2aik + b + iav)z}}{-2aik + b + iav} + \frac{e^{i(-azv + \pi v + 2akz - ibz)}}{b + ai(2k - v)} \right) \binom{v}{k}; v \in \mathbb{N}$$

01.06.21.1261.01

$$\int e^{bz} \sin^2(az) dz = \frac{e^{bz} (4a^2 - 2b \sin(2az)a + b^2 - b^2 \cos(2az))}{2(b^3 + 4a^2b)}$$

01.06.21.1262.01

$$\int e^{az} \sin^2(az) dz = -\frac{e^{az} (\cos(2az) + 2 \sin(2az) - 5)}{10a}$$

01.06.21.1263.01

$$\int e^{2az} \sin^2(az) dz = -\frac{e^{2az} (\cos(2az) + \sin(2az) - 2)}{8a}$$

01.06.21.1264.01

$$\int e^{bz} \sin^3(az) dz = \frac{1}{4(9a^4 + 10b^2a^2 + b^4)} (e^{bz} (-3a(9a^2 + b^2) \cos(az) + 3a(a^2 + b^2) \cos(3az) - 2b(-13a^2 - b^2 + (a^2 + b^2) \cos(2az)) \sin(az)))$$

01.06.21.1265.01

$$\int e^{bz} \sin^4(az) dz = \frac{1}{8(b^5 + 20a^2b^3 + 64a^4b)} (e^{bz} (192a^4 - 128b \sin(2az)a^3 + 16b \sin(4az)a^3 + 60b^2a^2 - 8b^3 \sin(2az)a + 4b^3 \sin(4az)a + 3b^4 - 4b^2(16a^2 + b^2) \cos(2az) + b^2(4a^2 + b^2) \cos(4az)))$$

01.06.21.1266.01

$$\int e^{2az} \sin^4(az) dz = \frac{e^{2az} (-10 \cos(2az) + \cos(4az) - 10 \sin(2az) + 2 \sin(4az) + 15)}{80a}$$

01.06.21.1267.01

$$\int e^{-2az} \sin^4(az) dz = -\frac{e^{-2az} (-10 \cos(2az) + \cos(4az) + 10 \sin(2az) - 2 \sin(4az) + 15)}{80a}$$



01.06.21.1268.01

$$\int \frac{\sin^3(az)}{\sqrt{e^{bz}}} dz = (-6a(36a^2 + b^2) \cos(az) + 6a(4a^2 + b^2) \cos(3az) + 2b(-52a^2 - b^2 + (4a^2 + b^2) \cos(2az)) \sin(az)) / (2(144a^4 + 40b^2a^2 + b^4) \sqrt{e^{bz}})$$

**Involving  $e^{bz+e} \sin^v(az)$**

01.06.21.1269.01

$$\int e^{bz+e} \sin^v(az) dz = \frac{e^{bz+e} (1 - e^{2iaz})^{-v} \sin^v(az)}{b - ia v} {}_2F_1\left(-\frac{ib + av}{2a}, -v; 1 - \frac{ib}{2a} - \frac{v}{2}; e^{2iaz}\right)$$

01.06.21.1270.01

$$\int e^{bz+e} \sin^v(az) dz = \frac{2^{-v} e^{e+bz} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{b} + 2^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{i\pi v}{2}} \left( \frac{e^{(-2aik+b+ia)vz}}{-2aik+b+ia v} + \frac{e^{i(-av+\pi v+2akz-ibz)}}{b+ai(2k-v)} \right) \binom{v}{k}; v \in \mathbb{N}$$

**Involving  $e^{pz} \sin^v(az + b)$**

01.06.21.1271.01

$$\int e^{pz} \sin^v(az + b) dz = \frac{e^{pz} (1 - e^{2i(b+az)})^{-v} \sin^v(b + az)}{p - ia v} {}_2F_1\left(-\frac{ip + av}{2a}, -v; \frac{1}{2} \left(-\frac{ip}{a} - v + 2\right); e^{2i(b+az)}\right)$$

01.06.21.1272.01

$$\int e^{pz} \sin^v(az + b) dz = \frac{2^{-v} e^{pz} (1 - v \bmod 2) \left(\frac{v}{2}\right)}{p} + 2^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{1}{2}i(\pi v + 2b(2k+v))} \left( \frac{e^{2ibv + (-2aik+pv+ia)vz}}{-2aik+pv+ia v} + \frac{e^{i(4bk+2azk+\pi v-ipz-avz)}}{p+ai(2k-v)} \right) \binom{v}{k}; v \in \mathbb{N}$$

**Involving  $e^{pz+e} \sin^v(az + b)$**

01.06.21.1273.01

$$\int e^{pz+e} \sin^v(az + b) dz = \frac{e^{pz+e} (1 - e^{2i(b+az)})^{-v} \sin^v(b + az)}{p - ia v} {}_2F_1\left(-\frac{ip + av}{2a}, -v; \frac{1}{2} \left(-\frac{ip}{a} - v + 2\right); e^{2i(b+az)}\right)$$

01.06.21.1274.01

$$\int e^{pz+e} \sin^v(az + b) dz = \frac{2^{-v} e^{pz+e} (1 - v \bmod 2) \left(\frac{v}{2}\right)}{p} + 2^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{1}{2}i(\pi v + 2b(2k+v))} \left( \frac{e^{2ibv + (-2aik+pv+ia)vz}}{-2aik+pv+ia v} + \frac{e^{i(4bk+2azk+\pi v-ipz-avz)}}{p+ai(2k-v)} \right) \binom{v}{k}; v \in \mathbb{N}$$

**Involving  $e^{bz^f} \sin^v(cz)$**

01.06.21.1275.01

$$\int e^{bz^2} \sin^v(cz) dz = \frac{1}{\sqrt{b}} 2^{-v-1} \sqrt{\pi} \left( \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b} z) (1 - v \bmod 2) + i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{\frac{c^2(v-2s)^2}{4b}} \binom{v}{s} \left( (-1)^v \operatorname{erfi}\left(\frac{2ics - icv + 2bz}{2\sqrt{b}}\right) + \operatorname{erfi}\left(\frac{ci(v-2s) + 2bz}{2\sqrt{b}}\right) \right) \right); v \in \mathbb{N}^+$$

01.06.21.1276.01

$$\int e^{\sqrt{z} b} \sin^v(cz) dz = \frac{2^{1-v} e^{\sqrt{z} b} (b\sqrt{z} - 1) \binom{v}{\frac{v}{2}} (1 - v \bmod 2)}{b^2} + i^{-v} 2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( 2 e^{b\sqrt{z}} \left( \frac{e^{i\pi v + (2ick - icv)z}}{2ick - icv} + \frac{e^{(icv - 2ick)z}}{icv - 2ick} \right) - \frac{b e^{\frac{b^2}{8ick - 4icv}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(icv-2ick)\sqrt{z}}{2\sqrt{icv-2ick}}\right)}{(icv - 2ick)^{3/2}} - \frac{b e^{\frac{b^2}{4icv-8ick} + i\pi v} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(2ick-icv)\sqrt{z}}{2\sqrt{2ick-icv}}\right)}{(2ick - icv)^{3/2}} \right); v \in \mathbb{N}^+$$

### Involving $e^{bz^2+e} \sin^v(cz)$

01.06.21.1277.01

$$\int e^{bz^2+e} \sin^v(cz) dz = \frac{2^{-v-1} e^e \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b} z) (1 - v \bmod 2)}{\sqrt{b}} + \frac{i^{-v} 2^{-v-1} \sqrt{\pi}}{\sqrt{b}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{c^2(v-2k)^2 - 4be}{4b}} \binom{v}{k} \left( \operatorname{erfi}\left(\frac{-2cik + icv + 2bz}{2\sqrt{b}}\right) + e^{i\pi v} \operatorname{erfi}\left(\frac{2ick - icv + 2bz}{2\sqrt{b}}\right) \right); v \in \mathbb{N}^+$$

01.06.21.1278.01

$$\int e^{\sqrt{z} b+e} \sin^v(cz) dz = \frac{2^{1-v} e^{\sqrt{z} b+e} (b\sqrt{z} - 1) \binom{v}{\frac{v}{2}} (1 - v \bmod 2)}{b^2} + i^{-v} 2^{-v-1} e^e \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( 2 e^{b\sqrt{z}} \left( \frac{e^{i\pi v + (2ick - icv)z}}{2ick - icv} + \frac{e^{(icv - 2ick)z}}{icv - 2ick} \right) - \frac{b e^{\frac{b^2}{8ick - 4icv}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(icv-2ick)\sqrt{z}}{2\sqrt{icv-2ick}}\right)}{(icv - 2ick)^{3/2}} - \frac{b e^{\frac{b^2}{4icv-8ick} + i\pi v} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(2ick-icv)\sqrt{z}}{2\sqrt{2ick-icv}}\right)}{(2ick - icv)^{3/2}} \right); v \in \mathbb{N}^+$$

### Involving $e^{bz'+dz} \sin^v(cz)$

01.06.21.1279.01

$$\int e^{bz'+dz} \sin^v(cz) dz = \frac{2^{-v-1} e^{-\frac{d^2}{4b}} \sqrt{\pi} (1-v \bmod 2) \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) + \frac{1}{\sqrt{b}} 2^{-v-1} \sqrt{\pi} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-\frac{d^2+2ci(2s+v)d-c^2(v-2s)^2}{4b}} \binom{v}{s} \left( e^{\frac{2icds}{b}} \operatorname{erfi}\left(\frac{d-2ics+icv+2bz}{2\sqrt{b}}\right) + (-1)^v e^{\frac{icdv}{b}} \operatorname{erfi}\left(\frac{d+2ics-icv+2bz}{2\sqrt{b}}\right) \right)}{; v \in \mathbb{N}^+}$$

01.06.21.1280.01

$$\int e^{\sqrt{z}bz'+dz} \sin^v(cz) dz = 2^{-v} \binom{v}{\frac{v}{2}} \left( \frac{e^{\sqrt{z}bz'+dz} b e^{-\frac{b^2}{4d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2d\sqrt{z}}{2\sqrt{d}}\right)}{d} - \frac{e^{(d-2ics+icv)z}}{d-2ics+icv} \right) (1-v \bmod 2) + 2^{-v} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{e^{b\sqrt{z}} \left( \frac{(-1)^v e^{(d+2ics-icv)z}}{d+2ics-icv} + \frac{e^{(d-2ics+icv)z}}{d-2ics+icv} \right) - \frac{b e^{-\frac{b^2}{4d+8ics-4icv}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d-2ics+icv)\sqrt{z}}{2\sqrt{d-2ics+icv}}\right)}{2(d-2ics+icv)^{3/2}} - \frac{(-1)^v b e^{-\frac{b^2}{4d-8ics+4icv}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d+2ics-icv)\sqrt{z}}{2\sqrt{d+2ics-icv}}\right)}{2(d+2ics-icv)^{3/2}}}{; v \in \mathbb{N}^+}$$

### Involving $e^{bz'+dz+e} \sin^v(cz)$

01.06.21.1281.01

$$\int e^{bz'+dz+e} \sin^v(cz) dz = \frac{2^{-v-1} \sqrt{\pi} (1-v \bmod 2) \binom{v}{\frac{v}{2}} e^{-\frac{d^2}{4b}} \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) + \frac{1}{\sqrt{b}} 2^{-v-1} \sqrt{\pi} i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{d^2+2ci(2k+v)d-c^2(v-2k)^2-4be}{4b}} \binom{v}{k} \left( e^{\frac{2icdk}{b}} \operatorname{erfi}\left(\frac{d-2ick+icv+2bz}{2\sqrt{b}}\right) + e^{\frac{icdv}{b}+i\pi v} \operatorname{erfi}\left(\frac{d+2ick-icv+2bz}{2\sqrt{b}}\right) \right)}{; v \in \mathbb{N}^+}$$

01.06.21.1282.01

$$\int e^{\sqrt{z} b+d z+e} \sin^{\nu}(c z) d z = 2^{-\nu} \binom{\nu}{\frac{\nu}{2}} \left( \frac{e^{\sqrt{z} b+d z} b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{d} - \frac{e^{(d-2 i c k+i c v) z}}{2 d^{3 / 2}} \right) (1-\nu \bmod 2) +$$

$$2^{-\nu-1} i^{-\nu} e^e \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( 2 e^{b \sqrt{z}} \left( \frac{e^{i \pi \nu+(d+2 i c k-i c v) z}}{d+2 i c k-i c v} + \frac{e^{(d-2 i c k+i c v) z}}{d-2 i c k+i c v} \right) - \right.$$

$$\left. \frac{b e^{-4 d+8 i c k-4 i c v} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d-2 i c k+i c v) \sqrt{z}}{2 \sqrt{d-2 i c k+i c v}}\right)}{(d-2 i c k+i c v)^{3 / 2}} - \frac{b e^{-4 d-8 i c k+4 i c v+i \pi \nu} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d+2 i c k-i c v) \sqrt{z}}{2 \sqrt{d+2 i c k-i c v}}\right)}{(d+2 i c k-i c v)^{3 / 2}} \right) ; \nu \in \mathbb{N}^+$$

### Involving $e^{b z^f} \sin^{\nu}(f z+g)$

01.06.21.1283.01

$$\int e^{b z^2} \sin^{\nu}(f z+g) d z = \frac{2^{-\nu-1} \sqrt{\pi} \binom{\nu}{\frac{\nu}{2}} \operatorname{erfi}(\sqrt{b} z) (1-\nu \bmod 2)}{\sqrt{b}} + i^{-\nu} 2^{-\nu-1} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{\frac{f^2(\nu-2 k)^2}{4 b}+g i(\nu-2 k)} \operatorname{erfi}\left(\frac{-2 f i k+i f \nu+2 b z}{2 \sqrt{b}}\right)}{\sqrt{b}} - \frac{e^{\frac{1}{4}\left(-\frac{2 i f k-i f \nu^2}{b}+8 i g k-4 i g \nu+4 \pi i\right)} \operatorname{erf}\left(\frac{2 i f k-i f \nu+2 b z}{2 \sqrt{-b}}\right)}{\sqrt{-b}} \right) ; \nu \in \mathbb{N}^+$$

01.06.21.1284.01

$$\int e^{\sqrt{z} b} \sin^{\nu}(f z+g) d z =$$

$$(2 i)^{-\nu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( -\frac{b e^{\frac{i b^2}{4 f(\nu-2 k)}-2 i g k+i g \nu} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(i f \nu-2 i f k) \sqrt{z}}{2 \sqrt{i f(\nu-2 k)}}\right)}{2(i f \nu-2 i f k)^{3 / 2}} + \frac{e^{\sqrt{z} b+\frac{1}{2}(-4 i g k+2 i g \nu)+(i f \nu-2 i f k) z}}{i f \nu-2 i f k} + \right.$$

$$\left. \frac{(-1)^{\nu} e^{\sqrt{z} b+\frac{1}{2}(4 i g k-2 i g \nu)+(2 i f k-i f \nu) z}}{2 i f k-i f \nu} - \frac{(-1)^{\nu} b e^{\frac{i b^2}{4 f(2 k-\nu)}+2 i g k-i g \nu} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(2 i f k-i f \nu) \sqrt{z}}{2 \sqrt{2 i f k-i f \nu}}\right)}{2(2 i f k-i f \nu)^{3 / 2}} \right) +$$

$$\frac{2^{1-\nu} e^{\sqrt{z} b} (b \sqrt{z}-1) \binom{\nu}{\frac{\nu}{2}} (1-\nu \bmod 2)}{b^2} ; \nu \in \mathbb{N}^+$$

**Involving  $e^{bz^2+e} \sin^v(fz+g)$**

01.06.21.1285.01

$$\int e^{bz^2+e} \sin^v(fz+g) dz = \frac{2^{-v-1} e^e \sqrt{\pi} \left(\frac{v}{2}\right) \operatorname{erfi}(\sqrt{b} z) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\frac{f^2(v-2k)^2}{4b} + g i(v-2k)+e} \operatorname{erfi}\left(\frac{-2fik+ifv+2bz}{2\sqrt{b}}\right) e^{\frac{1}{4}\left(-\frac{(2ifk-ifv)^2}{b} + 4e+8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{2ifk-ifv+2bz}{2\sqrt{-b}}\right)}{\sqrt{b}} - \frac{\phantom{e^{\frac{f^2(v-2k)^2}{4b} + g i(v-2k)+e} \operatorname{erfi}\left(\frac{-2fik+ifv+2bz}{2\sqrt{b}}\right) e^{\frac{1}{4}\left(-\frac{(2ifk-ifv)^2}{b} + 4e+8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{2ifk-ifv+2bz}{2\sqrt{-b}}\right)}}{\sqrt{-b}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1286.01

$$\int e^{\sqrt{z}bz+e} \sin^v(fz+g) dz = (2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( -\frac{b e^{\frac{ib^2}{4f(v-2k)}+e-2igk+igv} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(ifv-2ifk)\sqrt{z}}{2\sqrt{if(v-2k)}}\right)}{2(ifv-2ifk)^{3/2}} + \frac{e^{\sqrt{z}bz+\frac{1}{2}(2e-4igk+2igv)+(ifv-2ifk)z}}}{ifv-2ifk} + \frac{(-1)^v e^{\sqrt{z}bz+\frac{1}{2}(2e+4igk-2igv)+(2ifk-ifv)z}}}{2ifk-ifv} - \frac{(-1)^v b e^{\frac{ib^2}{4f(2k-v)}+e+2igk-igv} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(2ifk-ifv)\sqrt{z}}{2\sqrt{2ifk-ifv}}\right)}{2(2ifk-ifv)^{3/2}} \right) + \frac{2^{1-v} e^{\sqrt{z}bz+e} (b\sqrt{z}-1) \left(\frac{v}{2}\right) (1-v \bmod 2)}{b^2} /; v \in \mathbb{N}^+$$

**Involving  $e^{bz^2+dz} \sin^v(fz+g)$**

01.06.21.1287.01

$$\int e^{bz^2+dz} \sin^v(fz+g) dz = \frac{2^{-v-1} e^{-\frac{d^2}{4b}} \sqrt{\pi} \left(\frac{v}{2}\right) \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{(d+fi(v-2k))^2}{4b} + gi(v-2k)} \operatorname{erfi}\left(\frac{d-2fik+ifv+2bz}{2\sqrt{b}}\right) e^{\frac{1}{4}\left(-\frac{(d+2ifk-ifv)^2}{b} + 8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{d+2ifk-ifv+2bz}{2\sqrt{-b}}\right)}{\sqrt{b}} - \frac{\phantom{e^{-\frac{(d+fi(v-2k))^2}{4b} + gi(v-2k)} \operatorname{erfi}\left(\frac{d-2fik+ifv+2bz}{2\sqrt{b}}\right) e^{\frac{1}{4}\left(-\frac{(d+2ifk-ifv)^2}{b} + 8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{d+2ifk-ifv+2bz}{2\sqrt{-b}}\right)}}{\sqrt{-b}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1288.01

$$\int e^{\sqrt{z} b+d z} \sin^{\nu}(f z+g) d z ==$$

$$\left( \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{\sqrt{z} b+\frac{1}{2}(-4 i g k+2 i g v)+(d-2 i f k+i f v) z}}{d-2 i f k+i f v} - \frac{b e^{-\frac{b^2}{4(d+i i(\nu-2 k))}-2 i g k+i g v} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+i i(\nu-2 k)}}\right)}{2(d-2 i f k+i f v)^{3/2}} + \right. \right.$$

$$\left. \frac{(-1)^{\nu} e^{\sqrt{z} b+\frac{1}{2}(4 i g k-2 i g v)+(d+2 i f k-i f v) z}}{d+2 i f k-i f v} - \frac{(-1)^{\nu} b e^{-\frac{b^2}{4(d+i i(2 k-\nu))+2 i g k-i g v}+2 i g k-i g v} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right)}{2(d+2 i f k-i f v)^{3/2}} \right) \right)$$

$$(2 i)^{-\nu}+2^{-\nu} \left( \frac{e^{\sqrt{z} b+d z}}{d} - \frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3/2}} \right) \binom{\nu}{\frac{\nu}{2}} (1-\nu \bmod 2) ; \nu \in \mathbb{N}^{+}$$

**Involving  $e^{b z^2+d z+e} \sin^{\nu}(f z+g)$**

01.06.21.1289.01

$$\int e^{b z^2+d z+e} \sin^{\nu}(g+f z) d z == \frac{2^{-\nu-1} e^{-\frac{d^2}{4 b}} \sqrt{\pi} \binom{\nu}{\frac{\nu}{2}} \operatorname{erfi}\left(\frac{d+2 b z}{2 \sqrt{b}}\right) (1-\nu \bmod 2)}{\sqrt{b}} + i^{-\nu} 2^{-\nu-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k}$$

$$\left( \frac{e^{-\frac{(d+i i(\nu-2 k))^2}{4 b}+e+g i(\nu-2 k)} \operatorname{erfi}\left(\frac{d-2 i f k+i f v+2 b z}{2 \sqrt{b}}\right)}{\sqrt{b}} - \frac{e^{\frac{1}{4}\left(-\frac{(d+2 i f k-i f v)^2}{b}+4 e+8 i g k-4 i g v+4 \pi i v\right)} \operatorname{erf}\left(\frac{d+2 i f k-i f v+2 b z}{2 \sqrt{-b}}\right)}{\sqrt{-b}} \right) ; \nu \in \mathbb{N}^{+}$$

01.06.21.1290.01

$$\int e^{\sqrt{z} b+d z+e} \sin^{\nu}(f z+g) d z =$$

$$\left( \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{\sqrt{z} b+\frac{1}{2}(2 e-4 i g k+2 i g v)+(d-2 i f k+i f v) z}}{d-2 i f k+i f v} - \frac{b e^{-\frac{b^2}{4(d+f i(2 k-\nu))+e-2 i g k+i g v}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+f i(2 k-\nu)}}\right)}{2(d-2 i f k+i f v)^{3/2}} \right) + \right.$$

$$\left. \frac{(-1)^{\nu} e^{\sqrt{z} b+\frac{1}{2}(2 e+4 i g k-2 i g v)+(d+2 i f k-i f v) z}}{d+2 i f k-i f v} - \frac{(-1)^{\nu} b e^{-\frac{b^2}{4(d+f i(2 k-\nu))+e+2 i g k-i g v}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right)}{2(d+2 i f k-i f v)^{3/2}} \right) \right) \left( \frac{\nu}{\frac{\nu}{2}} \right) (1-\nu \bmod 2) ; \nu \in \mathbb{N}^+$$

$$(2 i)^{-\nu} + 2^{-\nu} \left( \frac{e^{\sqrt{z} b+e+d z}}{d} - \frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3/2}} \right) \left( \frac{\nu}{\frac{\nu}{2}} \right) (1-\nu \bmod 2) ; \nu \in \mathbb{N}^+$$

### Involving $e^{bz} \sin^{\nu}(c z^r)$

01.06.21.1291.01

$$\int e^{bz} \sin^{\nu}(c z^2) d z = \frac{e^{bz} (1-\nu \bmod 2)}{2^{\nu} b} \left( \frac{\nu}{\frac{\nu}{2}} \right) +$$

$$\frac{i^{-\nu} 2^{-\nu-1} \sqrt{\pi}}{\sqrt{i c}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{(-1)^k}{\sqrt{\nu-2 k}} e^{\frac{b^2}{8 i c k-4 i c v}} \binom{\nu}{k} \left( e^{\frac{b^2}{2 i c v-4 i c k}+i \pi v} \operatorname{erf}\left(\frac{2 i c(\nu-2 k) z-b}{2 \sqrt{i c} \sqrt{\nu-2 k}}\right) + \operatorname{erfi}\left(\frac{b+2 c i(\nu-2 k) z}{2 \sqrt{i c} \sqrt{\nu-2 k}}\right) \right) ; \nu \in \mathbb{N}^+$$

01.06.21.1292.01

$$\int e^{bz} \sin^{\nu}(c \sqrt{z}) d z = \frac{e^{bz} (1-\nu \bmod 2)}{2^{\nu} b} \left( \frac{\nu}{\frac{\nu}{2}} \right) + \frac{2^{-\nu-1} i^{-\nu}}{b^{3/2}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k e^{\frac{(4 k^2+\nu^2) c^2}{4 b}+i(2 k-\nu) \sqrt{z} c} \binom{\nu}{k}$$

$$\left( -i c e^{i c\left(\frac{i c k v}{b}+(v-2 k) \sqrt{z}\right)} \sqrt{\pi} (2 k-\nu) \left( (-1)^{\nu} \operatorname{erfi}\left(\frac{2 \sqrt{z} b+2 i c k-i c v}{2 \sqrt{b}}\right) + \operatorname{erfi}\left(\frac{-2 \sqrt{z} b+2 i c k-i c v}{2 \sqrt{b}}\right) \right) + \right.$$

$$\left. 2 \sqrt{b} e^{-\frac{(4 k^2+\nu^2) c^2}{4 b}+i \pi v+b z} + 2 \sqrt{b} e^{-\frac{(4 k^2+\nu^2) c^2}{4 b}+2 i(v-2 k) \sqrt{z} c+b z} \right) ; \nu \in \mathbb{N}^+$$

### Involving $e^{bz+e} \sin^{\nu}(c z^r)$

01.06.21.1293.01

$$\int e^{bz+e} \sin^{\nu}(c z^2) d z = \frac{e^{bz+e} (1-\nu \bmod 2)}{2^{\nu} b} \left( \frac{\nu}{\frac{\nu}{2}} \right) +$$

$$\frac{i^{-\nu} 2^{-\nu-1} \sqrt{\pi}}{\sqrt{i c}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} \frac{(-1)^k}{\sqrt{\nu-2 k}} e^{\frac{b^2}{8 i c k-4 i c v}+e} \binom{\nu}{k} \left( e^{\frac{b^2}{2 i c v-4 i c k}+i \pi v} \operatorname{erf}\left(\frac{2 i c(\nu-2 k) z-b}{2 \sqrt{i c} \sqrt{\nu-2 k}}\right) + \operatorname{erfi}\left(\frac{b+2 c i(\nu-2 k) z}{2 \sqrt{i c} \sqrt{\nu-2 k}}\right) \right) ; \nu \in \mathbb{N}^+$$

01.06.21.1294.01

$$\int e^{bz+e} \sin^v(c\sqrt{z}) dz = \frac{e^{bz+e} (1-v \bmod 2)}{2^v b} \left(\frac{v}{2}\right) + \frac{2^{-v-1} i^{-v}}{b^{3/2}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{\frac{(4k^2+v^2)c^2}{4b} + i(2k-v)\sqrt{z} c+e} \binom{v}{k} \left( -i c e^{i c \left(\frac{ickv}{b} + (v-2k)\sqrt{z}\right)} \sqrt{\pi} (2k-v) \left( (-1)^v \operatorname{erfi}\left(\frac{2\sqrt{z} b + 2ick - icv}{2\sqrt{b}}\right) + \operatorname{erfi}\left(\frac{-2\sqrt{z} b + 2ick - icv}{2\sqrt{b}}\right) \right) + 2\sqrt{b} e^{-\frac{(4k^2+v^2)c^2}{4b} + i\pi v + bz} + 2\sqrt{b} e^{-\frac{(4k^2+v^2)c^2}{4b} + 2i(v-2k)\sqrt{z} c + bz} \right) /; v \in \mathbb{N}^+$$

### Involving $e^{bz^r} \sin^v(cz^r)$

01.06.21.1295.01

$$\int e^{bz^r} \sin^v(cz^r) dz = -\frac{2^{-v} z (-bz^r)^{-1/r} (1-v \bmod 2)}{r} \left(\frac{v}{2}\right) \Gamma\left(\frac{1}{r}, -bz^r\right) - \frac{2^{-v} i^{-v} z^{\lfloor \frac{v-1}{2} \rfloor}}{r} \sum_{i=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^i \binom{v}{i} \left( (-1)^v \Gamma\left(\frac{1}{r}, (ic(v-2i)-b)z^r\right) ((ic(v-2i)-b)z^r)^{-1/r} + ((-b-ic(v-2i))z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-ic(v-2i))z^r\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1296.01

$$\int e^{bz^2} \sin^v(cz^2) dz = \frac{2^{-v-1} \sqrt{\pi} (1-v \bmod 2)}{\sqrt{b}} \left(\frac{v}{2}\right) \operatorname{erfi}(\sqrt{b} z) + 2^{-v-1} i^{-v} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \left( (-1)^s \binom{v}{s} \left( (-1)^v \sqrt{b+2ics-icv} (b+ci(v-2s)) \operatorname{erfi}(\sqrt{b+2ics-icv} z) + (b+2ics-icv) \sqrt{b+ci(v-2s)} \operatorname{erfi}(\sqrt{b+ci(v-2s)} z) \right) \right) / ((b+2ics-icv)(b+ci(v-2s))) /; v \in \mathbb{N}^+$$

01.06.21.1297.01

$$\int e^{b\sqrt{z}} \sin^v(c\sqrt{z}) dz = \frac{2^{1-v} e^{b\sqrt{z}} (b\sqrt{z}-1) (1-v \bmod 2)}{b^2} \left(\frac{v}{2}\right) + 2^{1-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{(b-2ick+icv)\sqrt{z}} \left( \frac{e^{-\frac{1}{2}i\pi v} \sqrt{z}}{b-2ick+icv} - \frac{e^{-\frac{1}{2}i\pi v}}{(b-2ick+icv)^2} \right) + e^{(b+2ick-icv)\sqrt{z}} \left( \frac{e^{\frac{i\pi v}{2} \sqrt{z}}}{b+2ick-icv} - \frac{e^{\frac{i\pi v}{2}}}{(b+2ick-icv)^2} \right) \right) /; v \in \mathbb{N}^+$$

### Involving $e^{bz^r+e} \sin^v(cz^r)$



01.06.21.1298.01

$$\int e^{bz^r+e} \sin^v(cz^r) dz = -\frac{2^{-v} e^e z (-bz^r)^{-1/r} \left(\frac{v}{2}\right) \Gamma\left(\frac{1}{r}, -bz^r\right) (1-v \bmod 2)}{r} -$$

$$\frac{(2i)^{-v} z^{\lfloor \frac{v-1}{2} \rfloor}}{r} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^e \binom{v}{k} \left( (-1)^v \Gamma\left(\frac{1}{r}, (-b-2ick+icv)z^r\right) ((-b-2ick+icv)z^r)^{-1/r} + \right.$$

$$\left. ((-b-ic(v-2k))z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-ic(v-2k))z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.1299.01

$$\int e^{bz^2+e} \sin^v(cz^2) dz = \frac{2^{-v-1} e^e \sqrt{\pi} \left(\frac{v}{2}\right) \operatorname{erfi}(\sqrt{b}z) (1-v \bmod 2)}{\sqrt{b}} +$$

$$i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^e \operatorname{erfi}\left(\frac{2bz-4ickz+2icvz}{2\sqrt{b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{e^{e+i\pi v} \operatorname{erf}\left(\frac{2bz+4ickz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{-b-2ick+icv}} \right); v \in \mathbb{N}^+$$

01.06.21.1300.01

$$\int e^{\sqrt{z}bz+e} \sin^v(c\sqrt{z}) dz = \frac{2^{1-v} e^{\sqrt{z}bz+e} (b\sqrt{z}-1) \left(\frac{v}{2}\right) (1-v \bmod 2)}{b^2} + 2^{2-v} e^{\sqrt{z}bz+e}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(b^2+c^2(2k-v)^2)^2} \left( (-1)^k \binom{v}{k} \left( (\sqrt{z}b^3-b^2+c^2(2k-v)^2\sqrt{z}b+c^2(2k-v)^2) \cos\left(c\sqrt{z}(2k-v)+\frac{\pi v}{2}\right) + \right.$$

$$\left. c(2k-v)(\sqrt{z}b^2-2b+c^2(2k-v)^2\sqrt{z}) \sin\left(c\sqrt{z}(2k-v)+\frac{\pi v}{2}\right) \right) \right); v \in \mathbb{N}^+$$

### Involving $e^{bz^r+dz} \sin^v(cz^r)$

01.06.21.1301.01

$$\int e^{bz^2+dz} \sin^v(cz^2) dz = \frac{2^{-v-1} \sqrt{\pi} (1-v \bmod 2)}{\sqrt{b}} \left(\frac{v}{2}\right) e^{\frac{d^2}{4b}} \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) +$$

$$2^{-v-1} i^{-v} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{d^2}{4(b-2ick+icv)}} \operatorname{erfi}\left(\frac{d+2(b-2ick+icv)z}{2\sqrt{b+ci(v-2k)}}\right)}{\sqrt{b+ci(v-2k)}} - \frac{e^{-\frac{d^2}{4b-8ick+4icv}+i\pi v} \operatorname{erf}\left(\frac{d+2(b+2ick-icv)z}{2\sqrt{ic(v-2k)-b}}\right)}{\sqrt{ic(v-2k)-b}} \right); v \in \mathbb{N}^+$$

01.06.21.1302.01

$$\int e^{\sqrt{z} b+d z} \sin^{\nu}(c \sqrt{z}) d z=2^{-\nu}\left(\frac{\nu}{\frac{\nu}{2}}\right)\left(\frac{e^{\sqrt{z} b+d z}}{d}-\frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3 / 2}}\right)(1-\nu \bmod 2)+$$

$$\frac{i^{-\nu} 2^{-\nu-1}}{d^{3 / 2}} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor}(-1)^k e^{-\frac{b^2+2 c i(2 k+\nu) b-c^2\left(4 k^2+\nu^2\right)}{4 d}}\binom{\nu}{k}\left(-e^{\frac{(-k c^2+i b c+\pi i d) \nu}{d}} \sqrt{\pi}(b+2 i c k-i c \nu) \operatorname{erfi}\left(\frac{b+2 i c k-i c \nu+2 d \sqrt{z}}{2 \sqrt{d}}\right)+\right.$$

$$2 \sqrt{d} e^{\frac{b^2+2\left(2 \sqrt{z} d+c i(2 k+\nu) b-c^2\left(4 k^2+\nu^2\right)+4 d^2 z+4 c d i(\nu-2 k) \sqrt{z}\right)}{4 d}}+2 \sqrt{d} e^{\frac{b^2+2\left(2 \sqrt{z} d+c i(2 k+\nu) b-c^2\left(4 k^2+\nu^2\right)+4 d(i \pi \nu+d z)+4 c d i(2 k-\nu) \sqrt{z}\right)}{4 d}}-$$

$$\left. e^{\frac{i c k(2 b+i c \nu)}{d}} \sqrt{\pi}(b+c i(\nu-2 k)) \operatorname{erfi}\left(\frac{b+c i(\nu-2 k)+2 d \sqrt{z}}{2 \sqrt{d}}\right)\right) ; \nu \in \mathbb{N}^+$$

### Involving $e^{b z^r+d z+e} \sin^{\nu}(c z^r)$

01.06.21.1303.01

$$\int e^{b z^2+d z+e} \sin^{\nu}(c z^2) d z=\frac{2^{-\nu-1} \sqrt{\pi}(1-\nu \bmod 2)}{\sqrt{b}}\left(\frac{\nu}{\frac{\nu}{2}}\right) e^{-\frac{d^2}{4 b}} \operatorname{erfi}\left(\frac{d+2 b z}{2 \sqrt{b}}\right)+$$

$$2^{-\nu-1} e^e \sqrt{\pi} i^{-\nu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor}(-1)^k \binom{\nu}{k}\left(\frac{e^{-\frac{d^2}{4(b-2 i c k+i c \nu)}} \operatorname{erfi}\left(\frac{d+2(b-2 i c k+i c \nu) z}{2 \sqrt{b+c i(\nu-2 k)}}\right)-\frac{e^{-\frac{d^2}{-4 b-8 i c k+4 i c \nu}+i \pi \nu} \operatorname{erf}\left(\frac{d+2(b+2 i c k-i c \nu) z}{2 \sqrt{i c(\nu-2 k)-b}}\right)}{\sqrt{b+c i(\nu-2 k)}}-\frac{\operatorname{erf}\left(\frac{d+2(b+2 i c k-i c \nu) z}{2 \sqrt{i c(\nu-2 k)-b}}\right)}{\sqrt{i c(\nu-2 k)-b}}\right) ; \nu \in \mathbb{N}^+$$

01.06.21.1304.01

$$\int e^{\sqrt{z} b+e+d z} \sin^{\nu}(c \sqrt{z}) d z=2^{-\nu}\left(\frac{\nu}{\frac{\nu}{2}}\right)\left(\frac{e^{\sqrt{z} b+e+d z}}{d}-\frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3 / 2}}\right)(1-\nu \bmod 2)+\frac{i^{-\nu} 2^{-\nu-1}}{d^{3 / 2}}$$

$$\sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor}(-1)^k e^{-\frac{b^2+2 c i(2 k+\nu) b-4 d e-c^2\left(4 k^2+\nu^2\right)}{4 d}}\binom{\nu}{k}\left(-e^{\frac{(-k c^2+i b c+\pi i d) \nu}{d}} \sqrt{\pi}(b+2 i c k-i c \nu) \operatorname{erfi}\left(\frac{b+2 i c k-i c \nu+2 d \sqrt{z}}{2 \sqrt{d}}\right)+\right.$$

$$2 \sqrt{d} e^{\frac{b^2+2\left(2 \sqrt{z} d+c i(2 k+\nu) b-c^2\left(4 k^2+\nu^2\right)+4 d^2 z+4 c d i(\nu-2 k) \sqrt{z}\right)}{4 d}}+2 \sqrt{d} e^{\frac{b^2+2\left(2 \sqrt{z} d+c i(2 k+\nu) b-c^2\left(4 k^2+\nu^2\right)+4 d(i \pi \nu+d z)+4 c d i(2 k-\nu) \sqrt{z}\right)}{4 d}}-$$

$$\left. e^{\frac{i c k(2 b+i c \nu)}{d}} \sqrt{\pi}(b+c i(\nu-2 k)) \operatorname{erfi}\left(\frac{b+c i(\nu-2 k)+2 d \sqrt{z}}{2 \sqrt{d}}\right)\right) ; \nu \in \mathbb{N}^+$$

### Involving $e^{d z} \sin^{\nu}(c z^r+g)$

01.06.21.1305.01

$$\int e^{dz} \sin^v(cz^2 + g) dz = \frac{2^{-v} e^{dz} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{d} + i^{-v} 2^{-v-1} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\frac{id^2}{4c(v-2k)} + gi(v-2k)} \operatorname{erfi}\left(\frac{d-4ickz+2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} - \frac{e^{\frac{1}{4}\left(-\frac{d^2}{2ick-icv} + 8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{d+4ickz-2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1306.01

$$\int e^{dz} \sin^v(\sqrt{z}c + g) dz = (2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(icv-2ick) + \frac{1}{2}(2igv-4igk)+dz}}{d} + \frac{(-1)^v e^{\sqrt{z}(2ick-icv) + \frac{1}{2}(4igk-2igv)+dz}}{d} - \frac{(-1)^v e^{\frac{c^2(2k-v)^2}{4d} + 2igk-igv} \sqrt{\pi} (2ick-icv) \operatorname{erfi}\left(\frac{2\sqrt{z}d+ci(2k-v)}{2\sqrt{d}}\right)}{2d^{3/2}} \right)$$

$$\left. \frac{ic e^{\frac{c^2(v-2k)^2}{4d} - 2igk+igv} \sqrt{\pi} (v-2k) \operatorname{erfi}\left(\frac{2\sqrt{z}d+ci(v-2k)}{2\sqrt{d}}\right)}{2d^{3/2}} \right) + \frac{2^{-v} e^{dz} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{d} /; v \in \mathbb{N}^+$$

**Involving  $e^{dz+e} \sin^v(cz^f + g)$**

01.06.21.1307.01

$$\int e^{dz+e} \sin^v(cz^2 + g) dz = \frac{2^{-v} e^{e+dz} \left(\frac{v}{2}\right) (1 - v \bmod 2)}{d} + i^{-v} 2^{-v-1} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\frac{id^2}{4c(v-2k)} + e+gi(v-2k)} \operatorname{erfi}\left(\frac{d-4ickz+2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} - \frac{e^{\frac{1}{4}\left(-\frac{d^2}{2ick-icv} + 4e+8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{d+4ickz-2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1308.01

$$\int e^{dz+e} \sin^v(\sqrt{z} c + g) dz = \left( \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(icv-2ick)+\frac{1}{2}(2e-4igk+2igv)+dz}}}{d} + \frac{(-1)^v e^{\sqrt{z}(2ick-icv)+\frac{1}{2}(2e+4igk-2igv)+dz}}}{d} - \frac{(-1)^v e^{\frac{c^2(2k-v)^2}{4d}+e+2igk-igv} \sqrt{\pi} (2ick-icv) \operatorname{erfi}\left(\frac{2\sqrt{z} d+ci(2k-v)}{2\sqrt{d}}\right)}{2d^{3/2}} - \frac{ic e^{\frac{c^2(v-2k)^2}{4d}+e-2igk+igv} \sqrt{\pi} (v-2k) \operatorname{erfi}\left(\frac{2\sqrt{z} d+ci(v-2k)}{2\sqrt{d}}\right)}{2d^{3/2}} \right) \right) (2i)^{-v} + \frac{2^{-v} e^{e+dz} \left(\frac{v}{2}\right) (1-v \bmod 2)}{d} ; v \in \mathbb{N}^+$$

**Involving  $e^{bz^r} \sin^v(cz^r + g)$**

01.06.21.1309.01

$$\int e^{bz^r} \sin^v(cz^r + g) dz = -\frac{2^{-v} z (-bz^r)^{-1/r} (1-v \bmod 2) \left(\frac{v}{2}\right) \Gamma\left(\frac{1}{r}, -bz^r\right)}{r} - \frac{2^{-v} z i^{-v}}{r} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-2igk-igv} \binom{v}{k} \left( (-1)^v e^{4igk} \Gamma\left(\frac{1}{r}, (-b-2ick+icv)z^r\right) ((-b-2ick+icv)z^r)^{-1/r} + e^{2igv} ((-b-ic(v-2k))z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-ic(v-2k))z^r\right) \right) ; v \in \mathbb{N}^+$$

01.06.21.1310.01

$$\int e^{bz^2} \sin^v(cz^2 + g) dz = \frac{2^{-v-1} \sqrt{\pi} \left(\frac{v}{2}\right) \operatorname{erfi}(\sqrt{b} z) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{g i(v-2k)} \operatorname{erfi}\left(\frac{2bz-4ickz+2icvz}{2\sqrt{b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{e^{2igk-igv+i\pi v} \operatorname{erf}\left(\frac{2bz+4ickz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{-b-2ick+icv}} \right) ; v \in \mathbb{N}^+$$

01.06.21.1311.01

$$\int e^{\sqrt{z} b} \sin^v(\sqrt{z} c + g) dz = \frac{2^{1-v} e^{\sqrt{z} b} (b\sqrt{z} - 1) \left(\frac{v}{2}\right) (1-v \bmod 2)}{b^2} + 2^{2-v} e^{\sqrt{z} b} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(b^2 + c^2(2k-v)^2)^2} \left( (-1)^k \binom{v}{k} \left( (\sqrt{z} b^3 - b^2 + c^2(2k-v)^2 \sqrt{z} b + c^2(2k-v)^2) \cos\left(c\sqrt{z}(2k-v) + \frac{\pi v}{2} - g(v-2k)\right) + c(2k-v) (\sqrt{z} b^2 - 2b + c^2(2k-v)^2 \sqrt{z}) \sin\left(c\sqrt{z}(2k-v) + \frac{\pi v}{2} - g(v-2k)\right) \right) \right) ; v \in \mathbb{N}^+$$

### Involving $e^{bz^r+e} \sin^v(cz^r+g)$

01.06.21.1312.01

$$\int e^{bz^r+e} \sin^v(cz^r+g) dz = -\frac{2^{-v} e^e z (-bz^r)^{-1/r} (1-v \bmod 2)}{r} \left(\frac{v}{\frac{v}{2}}\right) \Gamma\left(\frac{1}{r}, -bz^r\right) -$$

$$\frac{2^{-v} z i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{e-2igk-igv} \binom{v}{k} \left( (-1)^v e^{4igk} \Gamma\left(\frac{1}{r}, (-b-2ick+icv)z^r\right) ((-b-2ick+icv)z^r)^{-1/r} + \right.$$

$$\left. e^{2igv} ((-b-ic(v-2k))z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-ic(v-2k))z^r\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1313.01

$$\int e^{bz^2+e} \sin^v(cz^2+g) dz = \frac{2^{-v-1} e^e \sqrt{\pi} \left(\frac{v}{\frac{v}{2}}\right) \operatorname{erfi}(\sqrt{b}z) (1-v \bmod 2)}{\sqrt{b}} +$$

$$i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{e+gi(v-2k)} \operatorname{erfi}\left(\frac{2bz-4ickz+2icvz}{2\sqrt{b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{e^{e+2igk-igv+i\pi v} \operatorname{erf}\left(\frac{2bz+4ickz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{-b-2ick+icv}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1314.01

$$\int e^{\sqrt{z}bz+e} \sin^v(\sqrt{z}c+g) dz = \frac{2^{1-v} e^{\sqrt{z}bz+e} (b\sqrt{z}-1) \left(\frac{v}{\frac{v}{2}}\right) (1-v \bmod 2)}{b^2} + 2^{2-v} e^{\sqrt{z}bz+e} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{(b^2+c^2(2k-v)^2)^2}$$

$$\left( (-1)^k \binom{v}{k} \left( (\sqrt{z}b^3-b^2+c^2(2k-v)^2\sqrt{z}b+c^2(2k-v)^2) \cos\left(c\sqrt{z}(2k-v)+\frac{\pi v}{2}-g(v-2k)\right) + \right.$$

$$\left. c(2k-v)(\sqrt{z}b^2-2b+c^2(2k-v)^2\sqrt{z}) \sin\left(c\sqrt{z}(2k-v)+\frac{\pi v}{2}-g(v-2k)\right) \right) /; v \in \mathbb{N}^+$$

### Involving $e^{bz^r+dz} \sin^v(cz^r+g)$

01.06.21.1315.01

$$\int e^{bz^2+dz} \sin^v(cz^2+g) dz = \frac{2^{-v-1} e^{-\frac{d^2}{4b}} \sqrt{\pi} \left(\frac{v}{\frac{v}{2}}\right) \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( \frac{e^{-\frac{d^2}{4(b+ci(v-2k))+g(i(v-2k))}} \operatorname{erfi}\left(\frac{d+2bz-4ickz+2icvz}{2\sqrt{b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{e^{\frac{1}{4}\left(-\frac{d^2}{b+2ick-icv}+8igk-4igv+4\pi iv\right)}} \operatorname{erf}\left(\frac{d+2bz+4ickz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{-b-2ick+icv}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1316.01

$$\int e^{\sqrt{z} b+dz} \sin^v(\sqrt{z} c+g) dz =$$

$$(2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(b-2ick+icv)+\frac{1}{2}(-4igk+2igv)+dz}}{d} + \frac{(-1)^v e^{\sqrt{z}(b+2ick-icv)+\frac{1}{2}(4igk-2igv)+dz}}{d} - \frac{1}{2d^{3/2}} \left( (-1)^v e^{-\frac{(b+ci(2k-v))^2}{4d}-2igk-igv} \sqrt{\pi} (b+2ick-icv) \operatorname{erfi}\left(\frac{b+ci(2k-v)+2d\sqrt{z}}{2\sqrt{d}}\right) - e^{-\frac{(b+ci(v-2k))^2}{4d}-2igk+igv} \sqrt{\pi} (b+ci(v-2k)) \operatorname{erfi}\left(\frac{b+ci(v-2k)+2d\sqrt{z}}{2\sqrt{d}}\right) \right) \right) +$$

$$2^{-v} \left( \frac{e^{\sqrt{z} b+dz}}{d} - \frac{b e^{-\frac{b^2}{4d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2d\sqrt{z}}{2\sqrt{d}}\right)}{2d^{3/2}} \right) \binom{v}{\frac{v}{2}} (1-v \bmod 2) ; v \in \mathbb{N}^+$$

**Involving  $e^{bz^r+dz+e} \sin^v(cz^r+g)$**

01.06.21.1317.01

$$\int e^{bz^2+dz+e} \sin^v(cz^2+g) dz = \frac{2^{-v-1} e^{-\frac{d^2}{4b}} \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) (1-v \bmod 2)}{\sqrt{b}} +$$

$$i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{d^2}{4(b+ci(v-2k))}+e+gi(v-2k)} \operatorname{erfi}\left(\frac{d+2bz-4ickz+2icvz}{2\sqrt{b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{e^{\frac{1}{4}\left(-\frac{d^2}{b+2ick-icv}+4e+8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{d+2bz+4ickz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{-b-2ick+icv}} \right) ; v \in \mathbb{N}^+$$

01.06.21.1318.01

$$\int e^{\sqrt{z} b+d z+e} \sin^{\nu}(\sqrt{z} c+g) d z=$$

$$(2 i)^{-\nu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{\sqrt{z}(b-2 i c k+i c v)+\frac{1}{2}(2 e-4 i g k+2 i g v)+d z}}{d} + \frac{(-1)^{\nu} e^{\sqrt{z}(b+2 i c k-i c v)+\frac{1}{2}(2 e+4 i g k-2 i g v)+d z}}{d} - \frac{1}{2 d^{3/2}} \left( (-1)^{\nu} e^{-\frac{(b+c i(2 k-\nu))^2}{4 d}+e+2 i g k-i g v} \sqrt{\pi} (b+2 i c k-i c v) \operatorname{erfi}\left(\frac{b+c i(2 k-\nu)+2 d \sqrt{z}}{2 \sqrt{d}}\right) \right) - \frac{e^{-\frac{(b+c i(\nu-2 k))^2}{4 d}+e-2 i g k+i g v} \sqrt{\pi} (b+c i(\nu-2 k)) \operatorname{erfi}\left(\frac{b+c i(\nu-2 k)+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3/2}} \right) + 2^{-\nu} \left( \frac{e^{\sqrt{z} b+e+d z}}{d} - \frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3/2}} \right) \binom{\nu}{\frac{\nu}{2}} (1-\nu \bmod 2) ; \nu \in \mathbb{N}^+$$

**Involving  $e^{d z} \sin^{\nu}(c z^r+f z)$**

01.06.21.1319.01

$$\int e^{d z} \sin^{\nu}(c z^2+f z) d z=$$

$$\frac{2^{-\nu} e^{d z} \binom{\nu}{\frac{\nu}{2}} (1-\nu \bmod 2)}{d} + i^{-\nu} 2^{-\nu-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{\frac{i(d+f i(\nu-2 k))^2}{4 c(\nu-2 k)}} \operatorname{erfi}\left(\frac{d-2 i f k+i f v-4 i c k z+2 i c v z}{2 \sqrt{i c v-2 i c k}}\right)}{\sqrt{i c v-2 i c k}} - \frac{e^{\frac{1}{4}\left(-\frac{(d+2 i f k-i f v)^2}{2 i c k-i c v}+4 \pi i v\right)} \operatorname{erf}\left(\frac{d+2 i f k-i f v+4 i c k z-2 i c v z}{2 \sqrt{i c v-2 i c k}}\right)}{\sqrt{i c v-2 i c k}} \right) ; \nu \in \mathbb{N}^+$$

01.06.21.1320.01

$$\int e^{dz} \sin^v(\sqrt{z} c + fz) dz =$$

$$(2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{(d-2ifk+ifv)z+(icv-2ick)\sqrt{z}}}{d-2ifk+ifv} - \frac{ic e^{\frac{c^2(v-2k)^2}{4(d+fi(v-2k))}} \sqrt{\pi} (v-2k) \operatorname{erfi}\left(\frac{ci(v-2k)+2(d-2ifk+ifv)\sqrt{z}}{2\sqrt{d+fi(v-2k)}}\right)}{2(d-2ifk+ifv)^{3/2}} + \right.$$

$$\left. \frac{(-1)^v e^{(d+2ifk-ifv)z+(2ick-icv)\sqrt{z}}}{d+2ifk-ifv} - \frac{(-1)^v e^{\frac{c^2(2k-v)^2}{4(d+fi(2k-v))}} \sqrt{\pi} (2ick-icv) \operatorname{erfi}\left(\frac{ci(2k-v)+2(d+2ifk-ifv)\sqrt{z}}{2\sqrt{d+2ifk-ifv}}\right)}{2(d+2ifk-ifv)^{3/2}} \right) + \frac{2^{-v} e^{dz} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{d} ; v \in \mathbb{N}^+$$

**Involving  $e^{dz+e} \sin^v(cz^r + fz)$**

01.06.21.1321.01

$$\int e^{dz+e} \sin^v(cz^2 + fz) dz = \frac{2^{-v} e^{e+dz} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{d} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( \frac{e^{\frac{i(d+fi(v-2k))^2}{4c(v-2k)}+e} \operatorname{erfi}\left(\frac{d-2ifk+ifv-4ickz+2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} - \frac{e^{\frac{1}{4}\left(-\frac{(d+2ifk-ifv)^2}{2ick-icv}+4e+4\pi iv\right)} \operatorname{erf}\left(\frac{d+2ifk-ifv+4ickz-2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} \right) ; v \in \mathbb{N}^+$$



01.06.21.1322.01

$$\int e^{dz+e} \sin^v(\sqrt{z} c + fz) dz =$$

$$(2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{e+(d-2ifk+ifv)z+(icv-2ick)\sqrt{z}}}{d-2ifk+ifv} - \frac{ic e^{\frac{c^2(v-2k)^2}{4(d+fi(v-2k))}+e} \sqrt{\pi} (v-2k) \operatorname{erfi}\left(\frac{ci(v-2k)+2(d-2ifk+ifv)\sqrt{z}}{2\sqrt{d+fi(v-2k)}}\right)}{2(d-2ifk+ifv)^{3/2}} \right) +$$

$$\frac{(-1)^v e^{e+(d+2ifk-ifv)z+(2ick-icv)\sqrt{z}}}{d+2ifk-ifv} -$$

$$\left( (-1)^v e^{\frac{c^2(2k-v)^2}{4(d+fi(2k-v))}+e} \sqrt{\pi} (2ick-icv) \operatorname{erfi}\left(\frac{ci(2k-v)+2(d+2ifk-ifv)\sqrt{z}}{2\sqrt{d+2ifk-ifv}}\right) \right) /$$

$$(2(d+2ifk-ifv)^{3/2}) + \frac{2^{-v} e^{e+dz} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{d} \quad ; v \in \mathbb{N}^+$$

**Involving  $e^{bz^r} \sin^v(cz^r + fz)$**

01.06.21.1323.01

$$\int e^{bz^2} \sin^v(cz^2 + fz) dz = \frac{2^{-v-1} \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b} z) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( \frac{e^{\frac{f^2(v-2k)^2}{4(b+ci(v-2k))}} \operatorname{erfi}\left(\frac{-2fik-4iczk+ifv+2bz+2icvz}{2\sqrt{b-2ick+icv}}\right) - e^{\frac{1}{4}\left(-\frac{(2ifk-ifv)^2}{b+2ick-icv}+4\pi iv\right)} \operatorname{erf}\left(\frac{2ifk+4iczk-ifv+2bz-2icvz}{2\sqrt{-b-2ick+icv}}\right) \right) / ; v \in \mathbb{N}^+$$

01.06.21.1324.01

$$\int e^{\sqrt{z}} b \sin^v(\sqrt{z} c + f z) dz =$$

$$(2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{(ifv-2ifk)z+(b-2ick+icv)\sqrt{z}}}{ifv-2ifk} - \frac{e^{\frac{i(b+ci(v-2k))^2}{4f(v-2k)}} \sqrt{\pi} (b+ci(v-2k)) \operatorname{erfi}\left(\frac{b+ci(v-2k)+2(ifv-2ifk)\sqrt{z}}{2\sqrt{if(v-2k)}}\right)}{2(ifv-2ifk)^{3/2}} + \right.$$

$$\left. \frac{(-1)^v e^{(2ifk-ifv)z+(b+2ick-icv)\sqrt{z}}}{2ifk-ifv} - \left( (-1)^v e^{\frac{i(b+ci(2k-v))^2}{4f(2k-v)}} \sqrt{\pi} (b+2ick-icv) \operatorname{erfi}\left(\frac{b+ci(2k-v)+2(2ifk-ifv)\sqrt{z}}{2\sqrt{2ifk-ifv}}\right) \right) / (2(2ifk-ifv)^{3/2}) \right) +$$

$$\frac{2^{1-v} e^{\sqrt{z}} b (b\sqrt{z} - 1) \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{b^2} ; v \in \mathbb{N}^+$$

**Involving  $e^{bz^r+e} \sin^v(cz^r + fz)$**

01.06.21.1325.01

$$\int e^{bz^2+e} \sin^v(cz^2 + fz) dz = \frac{2^{-v-1} e^e \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b} z) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( \frac{e^{\frac{f^2(v-2k)^2}{4(b+ci(v-2k))}+e} \operatorname{erfi}\left(\frac{-2fik-4icz k+ifv+2bz+2icvz}{2\sqrt{b-2ick+icv}}\right) - e^{\frac{1}{4}\left(\frac{(2ifk-ifv)^2}{b+2ick-icv}+4e+4\pi iv\right)} \operatorname{erf}\left(\frac{2ifk+4icz k-ifv+2bz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{\quad}{\sqrt{-b-2ick+icv}} \right) ; v \in \mathbb{N}^+$$

01.06.21.1326.01

$$\int e^{\sqrt{z} b+e} \sin^v(\sqrt{z} c+fz) dz = (2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{e+(ifv-2ifk)z+(b-2ick+icv)\sqrt{z}}}{ifv-2ifk} - \frac{e^{\frac{i(b+ci(v-2k))^2}{4f(v-2k)}+e} \sqrt{\pi} (b+ci(v-2k)) \operatorname{erfi}\left(\frac{b+ci(v-2k)+2(ifv-2ifk)\sqrt{z}}{2\sqrt{if(v-2k)}}\right)}{2(ifv-2ifk)^{3/2}} + \frac{(-1)^v e^{e+(2ifk-ifv)z+(b+2ick-icv)\sqrt{z}}}{2ifk-ifv} - \left( (-1)^v e^{\frac{i(b+ci(2k-v))^2}{4f(2k-v)}+e} \sqrt{\pi} (b+2ick-icv) \operatorname{erfi}\left(\frac{b+ci(2k-v)+2(2ifk-ifv)\sqrt{z}}{2\sqrt{2ifk-ifv}}\right) \right) / (2(2ifk-ifv)^{3/2}) \right) + \frac{2^{1-v} e^{\sqrt{z} b+e} (b\sqrt{z}-1) \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{b^2} ; v \in \mathbb{N}^+$$

**Involving  $e^{bz^r+dz} \sin^v(cz^r+fz)$**

01.06.21.1327.01

$$\int e^{bz^2+dz} \sin^v(cz^2+fz) dz = \frac{2^{-v-1} e^{-\frac{d^2}{4b}} \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) (1-v \bmod 2)}{\sqrt{b}} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{(d+fi(v-2k))^2}{4(b+ci(v-2k))}} \operatorname{erfi}\left(\frac{d-2ifk+ifv+2bz-4ickz+2icvz}{2\sqrt{b-2ick+icv}}\right)}{\sqrt{b-2ick+icv}} - \frac{e^{\frac{1}{4}\left(4\pi iv - \frac{(d+2ifk-ifv)^2}{b+2ick-icv}\right)} \operatorname{erf}\left(\frac{d+2ifk-ifv+2bz+4ickz-2icvz}{2\sqrt{-b-2ick+icv}}\right)}{\sqrt{-b-2ick+icv}} \right) ; v \in \mathbb{N}^+$$

01.06.21.1328.01

$$\int e^{\sqrt{z} b+d z} \sin^v(\sqrt{z} c+f z) d z=(2 i)^{-v}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor}(-1)^k\binom{v}{k}\left(\frac{e^{\sqrt{z}(b-2 i c k+i c v)+(d-2 i f k+i f v) z}}{d-2 i f k+i f v}-\frac{e^{-\frac{(b+c i(v-2 k))^2}{4(d+f i(v-2 k))}} \sqrt{\pi}(b+c i(v-2 k)) \operatorname{erfi}\left(\frac{b+c i(v-2 k)+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+f i(v-2 k)}}\right)}{2(d-2 i f k+i f v)^{3 / 2}}+\frac{(-1)^v e^{\sqrt{z}(b+2 i c k-i c v)+(d+2 i f k-i f v) z}}{d+2 i f k-i f v}-\left((-1)^v e^{-\frac{(b+c i(2 k-v))^2}{4(d+f i(2 k-v))}} \sqrt{\pi}(b+2 i c k-i c v) \operatorname{erfi}\left(\frac{b+c i(2 k-v)+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right)\right) / (2(d+2 i f k-i f v)^{3 / 2})\right)+2^{-v}\left(\frac{e^{\sqrt{z} b+d z}}{d}-\frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3 / 2}}\right)\binom{v}{\frac{v}{2}}(1-v \bmod 2) ; v \in \mathbb{N}^+$$

### Involving $e^{b z^2+d z+e} \sin^v(c z^2+f z)$

01.06.21.1329.01

$$\int e^{b z^2+d z+e} \sin^v\left(c z^2+f z\right) d z=\frac{2^{-v-1} e^{-\frac{d^2}{4 b}} \sqrt{\pi}\binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\frac{d+2 b z}{2 \sqrt{b}}\right)(1-v \bmod 2)}{\sqrt{b}}+$$

$$i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor}(-1)^k\binom{v}{k}\left(\frac{e^{-\frac{(d+f i(v-2 k))^2}{4(b+c i(v-2 k))}} \operatorname{erfi}\left(\frac{d-2 i f k+i f v+2 b z-4 i c k z+2 i c v z}{2 \sqrt{b-2 i c k+i c v}}\right)}{\sqrt{b-2 i c k+i c v}}-\frac{e^{\frac{1}{4}\left(-\frac{(d+2 i f k-i f v)^2}{b+2 i c k-i c v}+4 e+4 \pi i v\right)} \operatorname{erf}\left(\frac{d+2 i f k-i f v+2 b z+4 i c k z-2 i c v z}{2 \sqrt{-b-2 i c k+i c v}}\right)}{\sqrt{-b-2 i c k+i c v}}\right) ; v \in \mathbb{N}^+$$

01.06.21.1330.01

$$\int e^{\sqrt{z} b+d z+e} \sin^v(\sqrt{z} c+f z) d z=(2 i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor}(-1)^k\binom{v}{k} \left[ \frac{e^{e+(d-2 i f k+i f v) z+(b-2 i c k+i c v) \sqrt{z}} e^{-\frac{(b+c i(v-2 k))^2}{4(d+f i(v-2 k))}} \sqrt{\pi}(b+c i(v-2 k)) \operatorname{erfi}\left(\frac{b+c i(v-2 k)+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+f i(v-2 k)}}\right)}{d-2 i f k+i f v} - \frac{e^{-\frac{(b+c i(2 k-v))^2}{4(d+f i(2 k-v))}} \sqrt{\pi}(b+2 i c k-i c v)}{2(d-2 i f k+i f v)^{3 / 2}} \right. + \left. \frac{(-1)^v e^{e+(d+2 i f k-i f v) z+(b+2 i c k-i c v) \sqrt{z}}}{d+2 i f k-i f v} - \left( (-1)^v e^{-\frac{(b+c i(2 k-v))^2}{4(d+f i(2 k-v))}} \sqrt{\pi}(b+2 i c k-i c v) \operatorname{erfi}\left(\frac{b+c i(2 k-v)+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right) \right) / (2(d+2 i f k-i f v)^{3 / 2}) \right] + 2^{-v} \left[ \frac{e^{\sqrt{z} b+e+d z}}{d} - \frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3 / 2}} \right] \binom{v}{\frac{v}{2}}(1-v \bmod 2) ; v \in \mathbb{N}^+$$

**Involving  $e^{d z} \sin^v(c z^r+f z+g)$**

01.06.21.1331.01

$$\int e^{d z} \sin^v\left(c z^2+f z+g\right) d z= \frac{2^{-v} e^{d z} \binom{v}{\frac{v}{2}}(1-v \bmod 2)}{d} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor}(-1)^k\binom{v}{k} \left[ \frac{e^{\frac{i(d+f i(v-2 k))^2}{4 c(v-2 k)}+g i(v-2 k)} \operatorname{erfi}\left(\frac{d-2 i f k+i f v-4 i c k z+2 i c v z}{2 \sqrt{i c v-2 i c k}}\right)}{\sqrt{i c v-2 i c k}} - \frac{e^{\frac{1}{4}\left(-\frac{(d+2 i f k-i f v)^2}{2 i c k-i c v}+8 i g k-4 i g v+4 \pi i v\right)} \operatorname{erf}\left(\frac{d+2 i f k-i f v+4 i c k z-2 i c v z}{2 \sqrt{i c v-2 i c k}}\right)}{\sqrt{i c v-2 i c k}} \right] ; v \in \mathbb{N}^+$$

01.06.21.1332.01

$$\int e^{dz} \sin^v(\sqrt{z} c + fz + g) dz = (2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z} (icv-2ick) + \frac{1}{2}(-4igk+2igv)+(d-2ifk+ifv)z}}{d-2ifk+ifv} - \frac{ic e^{\frac{c^2(v-2k)^2}{4(d+fi(v-2k))} - 2igk+igv} \sqrt{\pi} (v-2k) \operatorname{erfi}\left(\frac{ci(v-2k)+2(d-2ifk+ifv)\sqrt{z}}{2\sqrt{d+fi(v-2k)}}\right)}{2(d-2ifk+ifv)^{3/2}} + \frac{(-1)^v e^{\sqrt{z} (2ick-icv) + \frac{1}{2}(4igk-2igv)+(d+2ifk-ifv)z}}{d+2ifk-ifv} - \frac{\left( (-1)^v e^{\frac{c^2(2k-v)^2}{4(d+fi(2k-v))} + 2igk-igv} \sqrt{\pi} (2ick-icv) \operatorname{erfi}\left(\frac{ci(2k-v)+2(d+2ifk-ifv)\sqrt{z}}{2\sqrt{d+2ifk-ifv}}\right) \right)}{(2(d+2ifk-ifv)^{3/2})} + \frac{2^{-v} e^{dz} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{d} \right) /; v \in \mathbb{N}^+$$

**Involving  $e^{dz+e} \sin^v(cz^f + fz + g)$**

01.06.21.1333.01

$$\int e^{dz+e} \sin^v(cz^2 + fz + g) dz = \frac{2^{-v} e^{e+dz} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{d} + i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\frac{i(d+fi(v-2k))^2}{4c(v-2k)} + e+gi(v-2k)} \operatorname{erfi}\left(\frac{d-2ifk+ifv-4ickz+2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} - \frac{e^{\frac{1}{4}\left(-\frac{(d+2ifk-ifv)^2}{2ick-icv} + 4e+8igk-4igv+4\pi iv\right)} \operatorname{erf}\left(\frac{d+2ifk-ifv+4ickz-2icvz}{2\sqrt{icv-2ick}}\right)}{\sqrt{icv-2ick}} \right) /; v \in \mathbb{N}^+$$

01.06.21.1334.01

$$\int e^{dz+e} \sin^v(\sqrt{z} c + fz + g) dz = (2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(icv-2ick)+\frac{1}{2}(2e-4igk+2igv)+(d-2ifk+ifv)z}}}{d-2ifk+ifv} - \right. \\ \left. \left( ic e^{\frac{c^2(v-2k)^2}{4(d+fi(v-2k))}+e-2igk+igv} \sqrt{\pi} (v-2k) \operatorname{erfi} \left( \frac{ci(v-2k)+2(d-2ifk+ifv)\sqrt{z}}{2\sqrt{d+fi(v-2k)}} \right) \right) / \right. \\ \left. (2(d-2ifk+ifv)^{3/2}) + \frac{(-1)^v e^{\sqrt{z}(2ick-icv)+\frac{1}{2}(2e+4igk-2igv)+(d+2ifk-ifv)z}}}{d+2ifk-ifv} - \right. \\ \left. \left( (-1)^v e^{\frac{c^2(2k-v)^2}{4(d+fi(2k-v))}+e+2igk-igv} \sqrt{\pi} (2ick-icv) \operatorname{erfi} \left( \frac{ci(2k-v)+2(d+2ifk-ifv)\sqrt{z}}{2\sqrt{d+2ifk-ifv}} \right) \right) / \right. \\ \left. (2(d+2ifk-ifv)^{3/2}) \right) + \frac{2^{-v} e^{e+dz} \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{d} ; v \in \mathbb{N}^+$$

Involving  $e^{bz^r} \sin^v(cz^r + fz + g)$

01.06.21.1335.01

$$\int e^{bz^2} \sin^v(cz^2 + fz + g) dz = \frac{2^{-v-1} \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b} z) (1-v \bmod 2)}{\sqrt{b}} + \\ i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\frac{f^2(v-2k)^2}{4(b+ci(v-2k))}+gi(v-2k)} \operatorname{erfi} \left( \frac{-2fik-4icz k+ifv+2bz+2icvz}}{2\sqrt{b-2ick+icv}} \right)}{\sqrt{b-2ick+icv}} - \right. \\ \left. \frac{e^{\frac{1}{4} \left( -\frac{(2ifk-ifv)^2}{b+2ick-icv} + 8igk-4igv+4\pi iv \right)} \operatorname{erf} \left( \frac{2ifk+4icz k-ifv+2bz-2icvz}}{2\sqrt{-b-2ick+icv}} \right)}{\sqrt{-b-2ick+icv}} \right) / ; v \in \mathbb{N}^+$$

01.06.21.1336.01

$$\int e^{b\sqrt{z}} \sin^v(\sqrt{z}c + fz + g) dz = (2i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(b-2ick+icv) + \frac{1}{2}(2igv-4igk) + (ifv-2ifk)z}}}{ifv-2ifk} - \right. \\ \left. \left( e^{\frac{i(b+ci(v-2k))^2}{4f(v-2k)} - 2igk+igv} \sqrt{\pi} (b+ci(v-2k)) \operatorname{erfi} \left( \frac{b+ci(v-2k) + 2(ifv-2ifk)\sqrt{z}}{2\sqrt{if(v-2k)}} \right) \right) / \right. \\ \left. (2(ifv-2ifk)^{3/2}) + \frac{(-1)^v e^{\sqrt{z}(b+2ick-icv) + \frac{1}{2}(4igk-2igv) + (2ifk-ifv)z}}}{2ifk-ifv} - \right. \\ \left. \left( (-1)^v e^{\frac{i(b+ci(2k-v))^2}{4f(2k-v)} + 2igk-igv} \sqrt{\pi} (b+2ick-icv) \operatorname{erfi} \left( \frac{b+ci(2k-v) + 2(2ifk-ifv)\sqrt{z}}{2\sqrt{2ifk-ifv}} \right) \right) / \right. \\ \left. (2(2ifk-ifv)^{3/2}) \right) + \frac{2^{1-v} e^{b\sqrt{z}} (b\sqrt{z} - 1) \binom{v}{\frac{v}{2}} (1-v \bmod 2)}{b^2} ; v \in \mathbb{N}^+$$

**Involving  $e^{bz^2+e} \sin^v(cz^r + fz + g)$**

01.06.21.1337.01

$$\int e^{bz^2+e} \sin^v(cz^2 + fz + g) dz = \frac{2^{-v-1} e^e \sqrt{\pi} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b}z) (1-v \bmod 2)}{\sqrt{b}} + \\ i^{-v} 2^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\frac{f^2(v-2k)^2}{4(b+ci(v-2k))} + gi(v-2k)+e} \operatorname{erfi} \left( \frac{-2fik-4icz k + ifv + 2bz + 2icvz}{2\sqrt{b-2ick+icv}} \right)}{\sqrt{b-2ick+icv}} - \right. \\ \left. \frac{e^{\frac{1}{4} \left( -\frac{(2ifk-ifv)^2}{b+2ick-icv} + 4e + 8igk - 4igv + 4\pi iv \right)} \operatorname{erf} \left( \frac{2ifk + 4icz k - ifv + 2bz - 2icvz}{2\sqrt{-b-2ick+icv}} \right)}{\sqrt{-b-2ick+icv}} \right) ; v \in \mathbb{N}^+$$



01.06.21.1338.01

$$\int e^{\sqrt{z} b+e} \sin^v(\sqrt{z} c+f z+g) dz =$$

$$\left( \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z} (b-2 i c k+i c v)+\frac{1}{2}(2 e-4 i g k+2 i g v)+(i f v-2 i f k) z}}{i f v-2 i f k} - \left( e^{\frac{i(b+c i(v-2 k))^2}{4 f(v-2 k)}+e-2 i g k+i g v} \sqrt{\pi} \right. \right. \right.$$

$$\left. \left. (b+c i(v-2 k)) \operatorname{erfi} \left( \frac{b+c i(v-2 k)+2(i f v-2 i f k) \sqrt{z}}{2 \sqrt{i f(v-2 k)}} \right) \right) / (2(i f v-2 i f k)^{3/2}) + \right.$$

$$\left. \frac{(-1)^v e^{\sqrt{z} (b+2 i c k-i c v)+\frac{1}{2}(2 e+4 i g k-2 i g v)+(2 i f k-i f v) z}}{2 i f k-i f v} - \left( (-1)^v e^{\frac{i(b+c i(2 k-v))^2}{4 f(2 k-v)}+e+2 i g k-i g v} \sqrt{\pi} \right. \right.$$

$$\left. \left. (b+2 i c k-i c v) \operatorname{erfi} \left( \frac{b+c i(2 k-v)+2(2 i f k-i f v) \sqrt{z}}{2 \sqrt{2 i f k-i f v}} \right) \right) / (2(2 i f k-i f v)^{3/2}) \right)$$

$$(2 i)^{-v} + \frac{2^{1-v} e^{\sqrt{z} b+e} (b \sqrt{z}-1) \left( \frac{v}{2} \right) (1-v \bmod 2)}{b^2} ; v \in \mathbb{N}^+$$

**Involving  $e^{b z^r+d z} \sin^v(c z^r+f z+g)$**

01.06.21.1339.01

$$\int e^{b z^2+d z} \sin^v(c z^2+f z+g) dz = \frac{2^{-v-1} e^{-\frac{d^2}{4 b}} \sqrt{\pi} (1-v \bmod 2) \left( \frac{v}{2} \right) \operatorname{erfi} \left( \frac{d+2 b z}{2 \sqrt{b}} \right) +$$

$$2^{-v-1} i^{-v} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{(d+f i(v-2 k))^2}{4(b+c i(v-2 k))}+g i(v-2 k)} \operatorname{erfi} \left( \frac{d-2 i f k+i f v+2 b z-4 i c k z+2 i c v z}{2 \sqrt{b-2 i c k+i c v}} \right)}{\sqrt{b-2 i c k+i c v}} - \right.$$

$$\left. \frac{e^{\frac{1}{4} \left( -\frac{(d+2 i f k-i f v)^2}{b+2 i c k-i c v}+8 i g k-4 i g v+4 \pi i v \right)} \operatorname{erf} \left( \frac{d+2 i f k-i f v+2 b z+4 i c k z-2 i c v z}{2 \sqrt{-b-2 i c k+i c v}} \right)}{\sqrt{-b-2 i c k+i c v}} \right) ; v \in \mathbb{N}^+$$

01.06.21.1340.01

$$\int e^{\sqrt{z} b+d z} \sin^v(\sqrt{z} c+f z+g) d z =$$

$$(2 i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(b-2 i c k+i c v)+\frac{1}{2}(-4 i g k+2 i g v)+(d-2 i f k+i f v) z}}{d-2 i f k+i f v} - \left( e^{-\frac{(b+c i(v-2 k))^2}{4(d+f i(v-2 k))}-2 i g k+i g v} \sqrt{\pi} \right. \right.$$

$$\left. \left. (b+c i(v-2 k)) \operatorname{erfi}\left(\frac{b+c i(v-2 k)+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+f i(v-2 k)}}\right)\right) / (2(d-2 i f k+i f v)^{3 / 2}) + \right.$$

$$\left. \frac{(-1)^v e^{\sqrt{z}(b+2 i c k-i c v)+\frac{1}{2}(4 i g k-2 i g v)+(d+2 i f k-i f v) z}}{d+2 i f k-i f v} - \frac{1}{2(d+2 i f k-i f v)^{3 / 2}} \right.$$

$$\left. \left( (-1)^v e^{-\frac{(b+c i(2 k-v))^2}{4(d+f i(2 k-v))}+2 i g k-i g v} \sqrt{\pi} (b+2 i c k-i c v) \operatorname{erfi}\left(\frac{b+c i(2 k-v)+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right)\right) \right) +$$

$$2^{-v} \left( \frac{e^{\sqrt{z} b+d z}}{d} - \frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3 / 2}} \right) \binom{v}{\frac{v}{2}} (1-v \bmod 2) ; v \in \mathbb{N}^+$$

**Involving  $e^{b z^r+d z+e} \sin^v(c z^r+f z+g)$**

01.06.21.1341.01

$$\int e^{b z^2+d z+e} \sin^v(c z^2+f z+g) d z = \frac{2^{-v-1} e^{-\frac{d^2}{4 b}} \sqrt{\pi} (1-v \bmod 2)}{\sqrt{b}} \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\frac{d+2 b z}{2 \sqrt{b}}\right) + 2^{-v-1} i^{-v} \sqrt{\pi}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{(d+f i(v-2 k))^2}{4(b+c i(v-2 k))}+e+g i(v-2 k)} \operatorname{erfi}\left(\frac{d-2 i f k+i f v+2 b z-4 i c k z+2 i c v z}{2 \sqrt{b-2 i c k+i c v}}\right)}{\sqrt{b-2 i c k+i c v}} - \left( e^{\frac{1}{4}\left(-\frac{(d+2 i f k-i f v)^2}{b+2 i c k-i c v}+4 e+8 i g k-4 i g v+4 \pi i v\right)} \right.$$

$$\left. \operatorname{erf}\left(\frac{d+2 i f k-i f v+2 b z+4 i c k z-2 i c v z}{2 \sqrt{b-2 i c k+i c v}}\right)\right) / \left(\sqrt{b-2 i c k+i c v}\right) ; v \in \mathbb{N}^+$$

01.06.21.1342.01

$$\int e^{\sqrt{z} b+d z+e} \sin^v(\sqrt{z} c+f z+g) d z =$$

$$(2 i)^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{\sqrt{z}(b-2 i c k+i c v)+\frac{1}{2}(2 e-4 i g k+2 i g v)+(d-2 i f k+i f v) z}}}{d-2 i f k+i f v} - \left( e^{-\frac{(b+c i(v-2 k))^2}{4(d+f i(v-2 k))}+e-2 i g k+i g v} \sqrt{\pi} \right. \right.$$

$$\left. \left. (b+c i(v-2 k)) \operatorname{erfi}\left(\frac{b+c i(v-2 k)+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+f i(v-2 k)}}\right)\right) \right) / (2(d-2 i f k+i f v)^{3/2}) +$$

$$\frac{(-1)^v e^{\sqrt{z}(b+2 i c k-i c v)+\frac{1}{2}(2 e+4 i g k-2 i g v)+(d+2 i f k-i f v) z}}{d+2 i f k-i f v} - \frac{1}{2(d+2 i f k-i f v)^{3/2}}$$

$$\left( (-1)^v e^{-\frac{(b+c i(2 k-v))^2}{4(d+f i(2 k-v))}+e+2 i g k-i g v} \sqrt{\pi} (b+2 i c k-i c v) \operatorname{erfi}\left(\frac{b+c i(2 k-v)+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right) \right) \Bigg) +$$

$$2^{-v} \left( \frac{e^{\sqrt{z} b+e+d z}}{d} - \frac{b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{2 d^{3/2}} \right) \binom{v}{\frac{v}{2}} (1-v \bmod 2) / ; v \in \mathbb{N}^+$$

Involving powers of sin and rational functions of exp

Involving  $(a + b e^{dz})^\beta \sin^v(cz)$

01.06.21.1343.01

$$\int \frac{\sin^v(cz)}{(a + b e^{dz})^n} dz = -\frac{2^{-v} b^{-n} e^{-dnz} (1-v \bmod 2)}{dn} \binom{v}{\frac{v}{2}} {}_2F_1\left(n, n; n+1; -\frac{a e^{-dz}}{b}\right) -$$

$$\frac{2^{-v} i^{1-v} a^{-n}}{c} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^k e^{ic(v-2k)z}}{v-2k} \binom{v}{k} \left( {}_2F_1\left(\frac{ic(v-2k)}{d}, n; \frac{d-2ick+icv}{d}; -\frac{b e^{dz}}{a}\right) - \right.$$

$$\left. e^{-2iczv+i\pi v+4ickz} {}_2F_1\left(\frac{ic(2k-v)}{d}, n; \frac{d+2ick-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) / ; n \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $e^{pz} \sin^v(cz) (a + b e^{dz})^{-n}$

01.06.21.1344.01

$$\int \frac{e^{pz} \sin^v(cz)}{(a + b e^{dz})^n} dz =$$

$$2^{-v} i^{-v} a^{-n} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{i\pi v + (2ick + p - icv)z}}{2ick + p - icv} {}_2F_1\left(\frac{2ick + p - icv}{d}, n; \frac{d + 2ick + p - icv}{d}; -\frac{b e^{dz}}{a}\right) + \frac{e^{(p+ci(v-2k))z}}{p + ci(v-2k)} \right.$$

$$\left. {}_2F_1\left(\frac{p + ci(v-2k)}{d}, n; \frac{d - 2ick + p + icv}{d}; -\frac{b e^{dz}}{a}\right) \right) +$$

$$\frac{2^{-v} a^{-n} (1 - v \bmod 2)}{p} e^{pz} \left(\frac{v}{2}\right) {}_2F_1\left(\frac{p}{d}, n; \frac{p}{d} + 1; -\frac{b e^{dz}}{a}\right); n \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving powers of sin and algebraic functions of exp

### Involving $(a + b e^{dz})^\beta \sin^v(cz)$

01.06.21.1345.01

$$\int (a + b e^{dz})^\beta \sin^v(cz) dz = \frac{2^{-v} \left(\frac{e^{-dz} a}{b} + 1\right)^{-\beta} (a + b e^{dz})^\beta (1 - v \bmod 2)}{d\beta} \left(\frac{v}{2}\right) {}_2F_1\left(-\beta, -\beta; 1 - \beta; -\frac{a e^{-dz}}{b}\right) -$$

$$\frac{2^{-v} i^{1-v} (a + b e^{dz})^\beta \left(\frac{e^{dz} b}{a} + 1\right)^{-\beta} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^k e^{ic(v-2k)z}}{v-2k} \binom{v}{k} \left( {}_2F_1\left(\frac{ic(v-2k)}{d}, -\beta; \frac{d - 2ick + icv}{d}; -\frac{b e^{dz}}{a}\right) -$$

$$e^{-2icz + i\pi v + 4ickz} {}_2F_1\left(\frac{ic(2k-v)}{d}, -\beta; \frac{d + 2ick - icv}{d}; -\frac{b e^{dz}}{a}\right) \right); v \in \mathbb{N}^+$$

### Involving $e^{pz}(a + b e^{dz})^\beta \sin^v(cz)$

01.06.21.1346.01

$$\int e^{pz} (a + b e^{dz})^\beta \sin^v(cz) dz = (2i)^{-v} \left(\frac{e^{dz} b}{a} + 1\right)^{-\beta} (a + b e^{dz})^\beta$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{i\pi v + (2ick + p - icv)z}}{2ick + p - icv} {}_2F_1\left(\frac{2ick + p - icv}{d}, -\beta; \frac{d + 2ick + p - icv}{d}; -\frac{b e^{dz}}{a}\right) +$$

$$\frac{e^{(p+ci(v-2k))z}}{p + ci(v-2k)} {}_2F_1\left(\frac{p + ci(v-2k)}{d}, -\beta; \frac{d - 2ick + p + icv}{d}; -\frac{b e^{dz}}{a}\right) \right) +$$

$$\frac{2^{-v} (1 - v \bmod 2)}{p} e^{pz} (a + b e^{dz})^\beta \left(\frac{e^{dz} b}{a} + 1\right)^{-\beta} \left(\frac{v}{2}\right) {}_2F_1\left(\frac{p}{d}, -\beta; \frac{p}{d} + 1; -\frac{b e^{dz}}{a}\right); v \in \mathbb{N}^+$$

Involving products of the direct function and exponential function

Involving products of two direct functions and exponential function

**Involving  $e^{bz} \sin(cz) \sin(az)$**

01.06.21.1347.01

$$\int e^{bz} \sin(cz) \sin(az) dz = \frac{(e^{bz} (\sin(az) (b(a^2 + b^2 + c^2) \sin(cz) - c(-a^2 + b^2 + c^2) \cos(cz)) - a \cos(az) ((a^2 + b^2 - c^2) \sin(cz) - 2bc \cos(cz))))}{(a^4 + 2(b^2 - c^2)a^2 + (b^2 + c^2)^2)}$$

**Involving  $e^{pz} \sin(cz) \sin(az + b)$**

01.06.21.1348.01

$$\int e^{pz} \sin(cz) \sin(b + az) dz = \frac{1}{2} e^{pz} \left( \frac{\cos((a - c)z) (p \cos(b) + (a - c) \sin(b))}{a^2 - 2ca + c^2 + p^2} + \frac{((a - c) \cos(b) - p \sin(b)) \sin((a - c)z)}{a^2 - 2ca + c^2 + p^2} - \frac{\cos((a + c)z) (p \cos(b) + (a + c) \sin(b))}{a^2 + 2ca + c^2 + p^2} - \frac{((a + c) \cos(b) - p \sin(b)) \sin((a + c)z)}{a^2 + 2ca + c^2 + p^2} \right)$$

**Involving  $e^{pz} \sin(cz + d) \sin(az + b)$**

01.06.21.1349.01

$$\int e^{pz} \sin(d + cz) \sin(b + az) dz = \frac{1}{2} e^{pz} \left( \frac{\cos((a - c)z) (p \cos(b - d) + (a - c) \sin(b - d))}{a^2 - 2ca + c^2 + p^2} + \frac{((a - c) \cos(b - d) - p \sin(b - d)) \sin((a - c)z)}{a^2 - 2ca + c^2 + p^2} - \frac{\cos((a + c)z) (p \cos(b + d) + (a + c) \sin(b + d))}{a^2 + 2ca + c^2 + p^2} - \frac{((a + c) \cos(b + d) - p \sin(b + d)) \sin((a + c)z)}{a^2 + 2ca + c^2 + p^2} \right)$$

**Involving  $e^{pz^2} \sin(bz) \sin(cz)$**

01.06.21.1350.01

$$\int e^{pz^2} \sin(bz) \sin(cz) dz = \frac{\sqrt{\pi}}{8\sqrt{p}} e^{\frac{(b-c)^2}{4p}} \left( e^{\frac{bc}{p}} i \operatorname{erf}\left(\frac{b+c+2ipz}{2\sqrt{p}}\right) - i e^{\frac{bc}{p}} \operatorname{erf}\left(\frac{b+c-2ipz}{2\sqrt{p}}\right) + \operatorname{erfi}\left(\frac{ib-ic+2pz}{2\sqrt{p}}\right) - \operatorname{erfi}\left(\frac{ib-ic-2pz}{2\sqrt{p}}\right) \right)$$

01.06.21.1351.01

$$\int e^{p\sqrt{z}} \sin(bz) \sin(cz) dz = \frac{1}{8} \left( \frac{e^{\frac{ip^2}{4c-4b}} p \sqrt{\pi} \operatorname{erf}\left(\frac{-p+2i(b-c)\sqrt{z}}{2\sqrt{i(b-c)}}\right)}{(i(b-c))^{3/2}} + \frac{e^{\frac{ip^2}{4(b+c)}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2i(b+c)\sqrt{z}}{2\sqrt{i(b+c)}}\right)}{(i(b+c))^{3/2}} + \frac{4e^{p\sqrt{z}} \sin((b-c)z)}{b-c} - \frac{e^{\frac{ip^2}{4b-4c}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2i(b-c)\sqrt{z}}{2\sqrt{i(b-c)}}\right)}{(i(b-c))^{3/2}} - \frac{4e^{p\sqrt{z}} \sin((b+c)z)}{b+c} - \frac{e^{-\frac{ip^2}{4(b+c)}} p \sqrt{\pi} \operatorname{erf}\left(\frac{-p+2i(b+c)\sqrt{z}}{2\sqrt{i(b+c)}}\right)}{(i(b+c))^{3/2}} \right)$$

**Involving  $e^{pz} \sin(bz^r) \sin(cz)$**

01.06.21.1352.01

$$\int e^{pz} \sin(bz^2) \sin(cz) dz = -\frac{\sqrt{\pi}}{8\sqrt{ib}} e^{\frac{i(ic+p)^2}{4b}} \left( e^{-\frac{i(p^2-c^2)}{2b}} \operatorname{erf}\left(\frac{ic-p+2ibz}{2\sqrt{ib}}\right) + e^{-\frac{i(ic+p)^2}{2b}} \operatorname{erf}\left(\frac{ic+p-2ibz}{2\sqrt{ib}}\right) + \operatorname{erfi}\left(\frac{ic+p+2ibz}{2\sqrt{ib}}\right) + e^{\frac{cp}{b}} \operatorname{erfi}\left(\frac{ic-p-2ibz}{2\sqrt{ib}}\right) \right)$$

01.06.21.1353.01

$$\int e^{pz} \sin(b\sqrt{z}) \sin(cz) dz = \frac{1}{8} \left( \frac{b e^{\frac{ib^2}{4c+4ip}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2(c+ip)\sqrt{z}}{2\sqrt{ic-p}}\right)}{(ic-p)^{3/2}} + \frac{b e^{\frac{ib^2}{4c+4ip}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b-2(c+ip)\sqrt{z}}{2\sqrt{ic-p}}\right)}{(ic-p)^{3/2}} + \frac{b e^{\frac{b^2}{4(ic+p)}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+2(ic+p)\sqrt{z}}{2\sqrt{ic+p}}\right)}{(ic+p)^{3/2}} - \frac{ib e^{\frac{b^2}{4(ic+p)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib-2(ic+p)\sqrt{z}}{2\sqrt{ic+p}}\right)}{(ic+p)^{3/2}} - \frac{4e^{-(ic+p)z} \sin(b\sqrt{z})}{c+ip} - \frac{4e^{(ic+p)z} \sin(b\sqrt{z})}{c-ip} \right)$$

**Involving  $e^{pz^r} \sin(bz^r) \sin(cz)$**

01.06.21.1354.01

$$\int e^{pz^2} \sin(bz^2) \sin(cz) dz = -\frac{\sqrt[4]{-1} e^{\frac{ic^2}{4(b+ip)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(-1)^{3/4}(-c+2bz+2ipz)}{2\sqrt{b+ip}}\right)}{8\sqrt{b+ip}} + \frac{\sqrt[4]{-1} e^{\frac{ic^2}{4(b+ip)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(-1)^{3/4}(c+2bz+2ipz)}{2\sqrt{b+ip}}\right)}{8\sqrt{b+ip}} + \frac{(-1)^{3/4} e^{-\frac{ic^2}{4(b-ip)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(c+2bz-2ipz)}{2\sqrt{b-ip}}\right)}{8\sqrt{b-ip}} - \frac{(-1)^{3/4} e^{-\frac{ic^2}{4(b-ip)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-c+2bz-2ipz)}{2\sqrt{b-ip}}\right)}{8\sqrt{b-ip}}$$

01.06.21.1355.01

$$\int e^{p\sqrt{z}} \sin(b\sqrt{z}) \sin(cz) dz =$$

$$\frac{1}{8c^{3/2}} \left( -2i\sqrt{c} e^{(-ib+p)\sqrt{z}-icz} + 2i\sqrt{c} e^{(ib+p)\sqrt{z}-icz} - 2i\sqrt{c} e^{\sqrt{z}(-ib+p)+icz} + 2i\sqrt{c} e^{\sqrt{z}(ib+p)+icz} + \right.$$

$$(-1)^{3/4} b e^{-\frac{i(b+i)p^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(b+i p-2c\sqrt{z})}{2\sqrt{c}}\right) + (-1)^{3/4} e^{\frac{i(b+i)p^2}{4c}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-ib+p-2ic\sqrt{z})}{2\sqrt{c}}\right) -$$

$$(-1)^{3/4} e^{\frac{i(b-i)p^2}{4c}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(ib+p-2ic\sqrt{z})}{2\sqrt{c}}\right) - \sqrt[4]{-1} e^{-\frac{i(b+i)p^2}{4c}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{(-1)^{3/4}(-ib+p+2ic\sqrt{z})}{2\sqrt{c}}\right) +$$

$$\sqrt[4]{-1} e^{-\frac{i(b-i)p^2}{4c}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{(-1)^{3/4}(ib+p+2ic\sqrt{z})}{2\sqrt{c}}\right) - (-1)^{3/4} b e^{-\frac{i(b-i)p^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(b-i p+2c\sqrt{z})}{2\sqrt{c}}\right) -$$

$$\left. \sqrt[4]{-1} b e^{\frac{i(b-i)p^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(-1)^{3/4}(-b+i p+2c\sqrt{z})}{2\sqrt{c}}\right) - \sqrt[4]{-1} b e^{\frac{i(b+i)p^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(-1)^{3/4}(b+i p+2c\sqrt{z})}{2\sqrt{c}}\right) \right)$$

**Involving  $e^{pZ} \sin(bz^r) \sin(cz^r)$**

01.06.21.1356.01

$$\int e^{pz} \sin(bz^2) \sin(cz^2) dz =$$

$$\frac{1}{8} \sqrt{\pi} \left( \frac{e^{\frac{ip^2}{4c-4b}} \operatorname{erf}\left(\frac{2i(b-c)z-p}{2\sqrt{i(b-c)}}\right)}{\sqrt{i(b-c)}} + \frac{e^{\frac{ip^2}{4b-4c}} \operatorname{erfi}\left(\frac{p+2(b-c)iz}{2\sqrt{i(b-c)}}\right)}{\sqrt{i(b-c)}} - \frac{e^{-\frac{ip^2}{4(b+c)}} \operatorname{erf}\left(\frac{2i(b+c)z-p}{2\sqrt{i(b+c)}}\right)}{\sqrt{i(b+c)}} - \frac{e^{\frac{ip^2}{4(b+c)}} \operatorname{erfi}\left(\frac{p+2(b+c)iz}{2\sqrt{i(b+c)}}\right)}{\sqrt{i(b+c)}} \right)$$

01.06.21.1357.01

$$\int e^{pz} \sin(b\sqrt{z}) \sin(c\sqrt{z}) dz =$$

$$\frac{1}{8} \left( \frac{(b-c) e^{\frac{(b-c)^2}{4p}} \sqrt{\pi} \operatorname{erf}\left(\frac{b-c+2ip\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} + \frac{(b+c) e^{\frac{(b+c)^2}{4p}} \sqrt{\pi} \operatorname{erf}\left(\frac{-b-c-2ip\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} + \frac{(b-c) e^{\frac{(c-b)^2}{4p}} \sqrt{\pi} \operatorname{erf}\left(\frac{b-c-2ip\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} + \right.$$

$$\left. \frac{(b+c) e^{\frac{(b+c)^2}{4p}-2\pi i} i \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+ic+2p\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} + \frac{8 e^{pz} \sin(b\sqrt{z}) \sin(c\sqrt{z})}{p} \right)$$

**Involving  $e^{pZ^r} \sin(bz^r) \sin(cz^r)$**

01.06.21.1358.01

$$\int e^{p z^r} \sin(b z^r) \sin(c z^r) dz = -\frac{z}{4r} \left( \Gamma\left(\frac{1}{r}, i(b-c+ip)z^r\right) (i(b-c+ip)z^r)^{-1/r} - (i(b+c+ip)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i(b+c+ip)z^r\right) + (-i(b-c-ip)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(b-c-ip)z^r\right) - (-i(b+c-ip)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(b+c-ip)z^r\right) \right)$$

01.06.21.1359.01

$$\int e^{p z^2} \sin(b z^2) \sin(c z^2) dz = -\left( \sqrt{\pi} \left( \sqrt{-i(b+c+ip)} \sqrt{ib-ic+p} (-ib+ic+p) \sqrt{ib+ic+p} \operatorname{erfi}\left(\sqrt{-i(b+c+ip)} z\right) - i(b+c+ip) \left( \sqrt{ib-ic+p} \left( (-ib+ic+p) \operatorname{erfi}\left(\sqrt{ib+ic+p} z\right) - \sqrt{-ib+ic+p} \sqrt{ib+ic+p} \operatorname{erfi}\left(\sqrt{-ib+ic+p} z\right) \right) + i \sqrt{ib+ic+p} (b-c+ip) \operatorname{erfi}\left(\sqrt{ib-ic+p} z\right) \right) \right) / \left( 8 \sqrt{ib-ic+p} \sqrt{ib+ic+p} (-b^2 - 2ipb + c^2 + p^2) \right)$$

01.06.21.1360.01

$$\int e^{p \sqrt{z}} \sin(b \sqrt{z}) \sin(c \sqrt{z}) dz = -\frac{1}{2} e^{-i(b+c+ip)\sqrt{z}} \left( \frac{1}{(b+c+ip)^2} + e^{2ic\sqrt{z}} \left( \frac{1}{(-ib+ic+p)^2} - \frac{e^{2ib\sqrt{z}} ((ib+ic+p)\sqrt{z} - 1)}{(b+c-ip)^2} + \frac{i\sqrt{z}}{-b+c-ip} \right) + \frac{e^{2ib\sqrt{z}} (1 - (ib-ic+p)\sqrt{z})}{(ib-ic+p)^2} + \frac{i\sqrt{z}}{b+c+ip} \right)$$

**Involving  $e^{bz^r+e} \sin(az^r + q) \sin(cz^r + g)$**

01.06.21.1361.01

$$\int e^{bz^r+e} \sin(az^r + q) \sin(cz^r + g) dz = -\frac{1}{4r} e^{-i(g+q)z} \left( e^{2ig} \Gamma\left(\frac{1}{r}, i(a-c+ib)z^r\right) (i(a-c+ib)z^r)^{-1/r} + e^{2iq} (-i(a-ib-c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(a-ib-c)z^r\right) - (i(a+c+ib)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, i(a+c+ib)z^r\right) - e^{2i(g+q)} (-i(a-ib+c)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, -i(a-ib+c)z^r\right) \right)$$

01.06.21.1362.01

$$\int e^{bz^2+e} \sin(az^2 + q) \sin(cz^2 + g) dz = \frac{1}{8} e^{-i(g+q)\sqrt{z}} \left( -\frac{\operatorname{erfi}\left(\sqrt{-i(a+c+ib)} z\right)}{\sqrt{-i(a+c+ib)}} + \frac{e^{2ig} \operatorname{erfi}\left(\sqrt{b-ia+ic} z\right)}{\sqrt{b-ia+ic}} + \frac{e^{2iq} \operatorname{erfi}\left(\sqrt{b-ic+ia} z\right)}{\sqrt{b-ic+ia}} - \frac{e^{2i(g+q)} \operatorname{erfi}\left(\sqrt{b+ia+ic} z\right)}{\sqrt{b+ia+ic}} \right)$$



01.06.21.1363.01

$$\int e^{\sqrt{z} b+e} \sin(\sqrt{z} a+q) \sin(\sqrt{z} c+g) dz =$$

$$\frac{1}{2} \left( \frac{e^{\sqrt{z} (b-ic-ia)+e-ig+iq+i\pi} (\sqrt{z} b+(-ia-ic)\sqrt{z}-1)}{(b-ic-ia)^2} + \frac{e^{\sqrt{z} (b-ic+ia)+e-ig+iq} (\sqrt{z} b+(ia-ic)\sqrt{z}-1)}{(b-ic+ia)^2} + \frac{e^{\sqrt{z} (b+ia+ic)+e+ig+iq-i\pi} (\sqrt{z} b-(-ia-ic)\sqrt{z}-1)}{(-b-ic-ia)^2} + \frac{e^{\sqrt{z} (b-ia+ic)+e+ig-iq} (\sqrt{z} b-(ia-ic)\sqrt{z}-1)}{(-b-ic+ia)^2} \right)$$

Involving  $e^{bz^r+dz+e} \sin(az^r + pz + q) \sin(cz^r + fz + g)$

01.06.21.1364.01

$$\int e^{bz^2+dz+e} \sin(az^2 + pz + q) \sin(cz^2 + fz + g) dz = -\frac{1}{8} \sqrt{\pi}$$

$$\left( \frac{e^{-ig-iq-\frac{-d^2+2ifd+2ipd+f^2+p^2+2fp}{4(-b+ia+ic)}} \operatorname{erf}\left(\frac{-d+if+ip-2bz+2iaz+2icz}{2\sqrt{-b+ia+ic}}\right)}{\sqrt{-b+ia+ic}} + \frac{e^{+ig+iq-\frac{d^2+2ifd+2ipd-f^2-p^2-2fp}{4(b+ia+ic)}} \operatorname{erfi}\left(\frac{d+if+ip+2bz+2iaz+2icz}{2\sqrt{b+ia+ic}}\right)}{\sqrt{b+ia+ic}} - \frac{e^{+ig-iq-\frac{-d^2-2ifd+2ipd+f^2+p^2-2fp}{4(-b-ic+ia)}} \operatorname{erf}\left(\frac{-d-if+ip-2bz-2icz+2iaz}{2\sqrt{-b-ic+ia}}\right)}{\sqrt{-b-ic+ia}} - \frac{e^{-ig+iq-\frac{d^2-2ifd+2ipd-f^2-p^2+2fp}{4(b-ic+ia)}} \operatorname{erfi}\left(\frac{d-if+ip+2bz-2icz+2iaz}{2\sqrt{b-ic+ia}}\right)}{\sqrt{b-ic+ia}} \right)$$

01.06.21.1365.01

$$\begin{aligned}
 & \int e^{\sqrt{z} b+d z+e} \sin(\sqrt{z} a+p z+q) \sin(\sqrt{z} c+f z+g) d z = \\
 & -\frac{1}{4} e^{e-i g-i q} \left( -\frac{e^{\sqrt{z}(b-i c+i a)+2 i q+(d-i f+i p) z}}{d-i f+i p} - \frac{e^{\sqrt{z}(b-i a+i c)+2 i g+(d+i f-i p) z}}{d+i f-i p} + \right. \\
 & \left. \frac{e^{\sqrt{z}(b-i c-i a)+(d-i f-i p) z}}{d-i f-i p} + \frac{e^{\sqrt{z}(b+i a+i c)+2 i g+2 i q+(d+i f+i p) z}}{d+i f+i p} \right) + \\
 & \frac{1}{8(d+i f+i p)^{3 / 2}} \left( (b+i a+i c) e^{-\frac{-d^2+2(b+i c) i a+b^2-c^2-4 d e-4 i e f-4 i d g+4 f g+2 i b c-4 i e p+4 g p-4 i d q+4 f q+4 p q}{4(d+i f+i p)}} \right. \\
 & \left. \sqrt{\pi} \operatorname{erfi}\left(\frac{b+i a+i c+2 d \sqrt{z}+2 i f \sqrt{z}+2 i p \sqrt{z}}{2 \sqrt{d+i f+i p}}\right) \right) - \\
 & \frac{1}{8(d-i f+i p)^{3 / 2}} \left( (b-i c+i a) e^{-\frac{-d^2+2(b-i c) i a+b^2-c^2-2 i b c-4 d e+4 f g+4 i e f+4 i d g-4 i e p-4 g p-4 i d q-4 f q+4 p q}{4(d-i f+i p)}} \right. \\
 & \left. \sqrt{\pi} \operatorname{erfi}\left(\frac{b-i c+i a+2 d \sqrt{z}-2 i f \sqrt{z}+2 i p \sqrt{z}}{2 \sqrt{d-i f+i p}}\right) \right) - \\
 & \frac{1}{8(d+i f-i p)^{3 / 2}} \left( (-b-i c+i a) e^{-\frac{-d^2-2 i(b+i c) a+b^2-c^2-4 d e-4 i e f-4 i d g+4 f g+2 i b c-4 g p+4 i e p-4 f q+4 i d q+4 p q}{4(d+i f-i p)}} \right. \\
 & \left. \sqrt{\pi} \operatorname{erfi}\left(\frac{-b-i c+i a-2 d \sqrt{z}-2 i f \sqrt{z}+2 i p \sqrt{z}}{2 \sqrt{d+i f-i p}}\right) \right) + \\
 & \frac{1}{8(d-i f-i p)^{3 / 2}} \left( (-b+i a+i c) e^{-\frac{-d^2-2 i b a-2 c a+b^2-c^2-2 i b c-4 d e+4 f g+4 i e f+4 i d g+4 g p+4 i e p+4 f q+4 i d q+4 p q}{4(-d-i f-i p)}} \right. \\
 & \left. \sqrt{\pi} \operatorname{erfi}\left(\frac{-b+i a+i c-2 d \sqrt{z}+2 i f \sqrt{z}+2 i p \sqrt{z}}{2 \sqrt{d-i f-i p}}\right) \right)
 \end{aligned}$$

Involving products of two direct functions and rational functions of exp

Involving  $\sin(e z) \sin(c z) (a+b e^{d z})^{-n}$

01.06.21.1366.01

$$\int \frac{\sin(ez) \sin(cz)}{(a + b e^{dz})^n} dz =$$

$$-\frac{1}{4} i a^{-n} \left( \frac{e^{-i(c-e)z}}{c-e} \left( e^{2i(c-e)z} {}_2F_1 \left( \frac{i(c-e)}{d}, n; \frac{d-ie+ic}{d}; -\frac{b e^{dz}}{a} \right) - {}_2F_1 \left( -\frac{i(c-e)}{d}, n; \frac{d-ic+ie}{d}; -\frac{b e^{dz}}{a} \right) \right) + \right.$$

$$\left. \frac{e^{-i(c+e)z}}{c+e} \left( {}_2F_1 \left( -\frac{i(c+e)}{d}, n; -\frac{i(c+e+id)}{d}; -\frac{b e^{dz}}{a} \right) - e^{2i(c+e)z} {}_2F_1 \left( \frac{i(c+e)}{d}, n; \frac{d+ic+ie}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) /; n \in \mathbb{N}^+$$

**Involving  $e^{pz} \sin(ez) \sin(cz) (a + b e^{dz})^{-n}$**

01.06.21.1367.01

$$\int \frac{e^{pz} \sin(ez) \sin(cz)}{(a + b e^{dz})^n} dz =$$

$$\frac{1}{4} a^{-n} \left( \frac{1}{c^2 - 2ec + e^2 + p^2} \left( e^{(-ic+ie+p)z} (ic - ie + p) {}_2F_1 \left( \frac{-ic+ie+p}{d}, n; \frac{d-ic+ie+p}{d}; -\frac{b e^{dz}}{a} \right) + \right. \right.$$

$$e^{i(c-ie+p)z} (-ic + ie + p) {}_2F_1 \left( \frac{ic-ie+p}{d}, n; \frac{d-ie+ic+p}{d}; -\frac{b e^{dz}}{a} \right) +$$

$$\frac{i}{c^2 + 2ec + e^2 + p^2} \left( e^{i(c+ie+p)z} (c+e+ip) {}_2F_1 \left( \frac{ic+ie+p}{d}, n; \frac{d+ic+ie+p}{d}; -\frac{b e^{dz}}{a} \right) - \right.$$

$$\left. \left. e^{-i(c+e+ip)z} (c+e-ip) {}_2F_1 \left( -\frac{i(c+e+ip)}{d}, n; \frac{d-ie-ic+p}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) /; n \in \mathbb{N}^+$$

Involving products of two direct functions and algebraic functions of exp

**Involving  $(a + b e^{dz})^\beta \sin(ez) \sin(cz)$**

01.06.21.1368.01

$$\int (a + b e^{dz})^\beta \sin(ez) \sin(cz) dz =$$

$$\frac{i}{4(c-e)(c+e)} e^{-2i(c+e)z} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \left( -(c+e) e^{i(3c+e)z} {}_2F_1 \left( \frac{i(c-e)}{d}, -\beta; \frac{d-ie+ic}{d}; -\frac{b e^{dz}}{a} \right) + \right.$$

$$(c-e) e^{i(c+e)z} \left( e^{2i(c+e)z} {}_2F_1 \left( \frac{i(c+e)}{d}, -\beta; \frac{d+ic+ie}{d}; -\frac{b e^{dz}}{a} \right) - {}_2F_1 \left( -\frac{i(c+e)}{d}, -\beta; -\frac{i(c+e+id)}{d}; -\frac{b e^{dz}}{a} \right) \right) +$$

$$(c+e) e^{i(c+3e)z} {}_2F_1 \left( -\frac{i(c-e)}{d}, -\beta; \frac{d-ic+ie}{d}; -\frac{b e^{dz}}{a} \right) \right)$$

**Involving  $e^{pz} (a + b e^{dz})^\beta \sin(ez) \sin(cz)$**

01.06.21.1369.01

$$\int e^{pz} (a + b e^{dz})^\beta \sin(ez) \sin(cz) dz = \frac{1}{4} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \left( -\frac{1}{c^2 - 2ec + e^2 + p^2} \left( i e^{(ic-ie+p)z} (c - e + ip) {}_2F_1 \left( \frac{ic - ie + p}{d}, -\beta; \frac{d - ie + ic + p}{d}; -\frac{b e^{dz}}{a} \right) - e^{(-ic+ie+p)z} (ic - ie + p) {}_2F_1 \left( \frac{-ic + ie + p}{d}, -\beta; \frac{d - ic + ie + p}{d}; -\frac{b e^{dz}}{a} \right) \right) + \frac{1}{c^2 + 2ec + e^2 + p^2} \left( i e^{(ic+ie+p)z} (c + e + ip) {}_2F_1 \left( \frac{ic + ie + p}{d}, -\beta; \frac{d + ic + ie + p}{d}; -\frac{b e^{dz}}{a} \right) - e^{-i(c+e+ip)z} (c + e - ip) {}_2F_1 \left( -\frac{i(c+e+ip)}{d}, -\beta; \frac{d - ie - ic + p}{d}; -\frac{b e^{dz}}{a} \right) \right) \right)$$

Involving products of several direct functions and exponential function

Involving  $e^{pz} \sin(az) \sin(bz) \sin(cz)$

01.06.21.1370.01

$$\int e^{pz} \sin(az) \sin(bz) \sin(cz) dz = \frac{1}{4} e^{pz} \left( \frac{(a - b - c) \cos((a - b - c)z) - p \sin((a - b - c)z)}{a^2 - 2(b + c)a + b^2 + c^2 + p^2 + 2bc} + \frac{(a + b + c) \cos((a + b + c)z) - p \sin((a + b + c)z)}{(a + b + c - ip)(a + b + c + ip)} - \frac{(a + b - c) \cos((a + b - c)z) - p \sin((a + b - c)z)}{(a + b - c - ip)(a + b - c + ip)} - \frac{(a - b + c) \cos((a - b + c)z) - p \sin((a - b + c)z)}{(a - b + c - ip)(a - b + c + ip)} \right)$$

Involving  $e^{pz} \prod_{k=1}^n \sin(a_k z)$

01.06.21.1371.01

$$\int e^{pz} \prod_{k=1}^n \sin(a_k z) dz = (-2)^{-n} e^{pz} \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \left( \frac{p \cos(\sum_{j=1}^n k_j (z a_j + \frac{\pi}{2})) + \sum_{j=1}^n k_j a_j \sin(\sum_{j=1}^n k_j (z a_j + \frac{\pi}{2}))}{p^2 + (\sum_{j=1}^n k_j a_j)^2} \right)$$

Involving products of powers of two direct functions and exponential function

Involving product of power of the direct function, the direct function and exponential function

Involving  $e^{bz} \sin(cz) \sin^v(az)$

01.06.21.1372.01

$$\int e^{bz} \sin(cz) \sin^v(az) dz = -\frac{1}{2} (1 - e^{-2iaz})^{-v} \sin^v(az) \left( \frac{e^{(-ic+b)z}}{c + ib - av} {}_2F_1 \left( \frac{c + ib - av}{2a}, -v; \frac{-va + 2a + c + ib}{2a}; e^{-2iaz} \right) + \frac{e^{(ic+b)z}}{c - ib + av} {}_2F_1 \left( -\frac{c - ib + av}{2a}, -v; -\frac{c - ib + a(v - 2)}{2a}; e^{-2iaz} \right) \right)$$

01.06.21.1373.01

$$\int e^{bz} \sin(cz) \sin^v(az) dz = (2i)^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{(b+ic-2iak+ia)vz}}{b+ic-2iak+ia} + \frac{e^{(b-ic-2iak+ia)vz}}{-b+ic+2iak-ia} + \frac{e^{i\pi v+(b+ic+2iak-ia)vz}}{b+ic+2iak-ia} + \frac{e^{i\pi v+(b-ic+2iak-ia)vz}}{-b+ic-2iak+ia} \right) + 2^{-v-1} \left( \frac{e^{(b-ic)z}}{b-ic} - \frac{e^{(b+ic)z}}{b+ic} \right) i \binom{v}{\frac{v}{2}} (1-v \bmod 2) ; v \in \mathbb{N}^+$$

### Involving $e^{bz} \sin(cz + d) \sin^v(az)$

01.06.21.1374.01

$$\int e^{bz} \sin(d + cz) \sin^v(az) dz = -\frac{1}{2} e^{-id} (1 - e^{-2iaz})^{-v} \sin^v(az) \left( \frac{e^{(-ic+b)z}}{c+ib-av} {}_2F_1 \left( \frac{c+ib-av}{2a}, -v; \frac{-va+2a+c+ib}{2a}; e^{-2iaz} \right) + \frac{e^{2id+(ic+b)z}}{c-ib+av} {}_2F_1 \left( -\frac{c-ib+av}{2a}, -v; -\frac{c-ib+a(v-2)}{2a}; e^{-2iaz} \right) \right)$$

01.06.21.1375.01

$$\int e^{bz} \sin(d + cz) \sin^v(az) dz = i 2^{-v-1} \left( \frac{e^{-id+(-ic+b)z}}{-ic+b} - \frac{e^{id+(ic+b)z}}{ic+b} \right) \binom{v}{\frac{v}{2}} (1-v \bmod 2) + 2^{-v-1} i^{-v-1} e^{id} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{(ic-2iak+b+ia)vz}}{ic-2iak+b+ia} + \frac{e^{-2id+(-ic-2iak+b+ia)vz}}{ic+2iak-b-ia} + \frac{e^{i\pi v+(ic+2iak+b-ia)vz}}{ic+2iak+b-ia} + \frac{e^{-2id+i\pi v+(-ic+2iak+b-ia)vz}}{ic-2iak-b+ia} \right) ; v \in \mathbb{N}^+$$

### Involving $e^{pz} \sin(cz) \sin^v(az + b)$

01.06.21.1376.01

$$\int e^{pz} \sin(cz) \sin^v(b + az) dz = -\frac{1}{2} (1 - e^{-2i(b+az)})^{-v} \sin^v(b + az) \left( \frac{e^{(-ic+p)z}}{c+ip-av} {}_2F_1 \left( \frac{c+ip-av}{2a}, -v; \frac{-va+2a+c+ip}{2a}; e^{-2i(b+az)} \right) + \frac{e^{(ic+p)z}}{c-ip+av} {}_2F_1 \left( -\frac{c-ip+av}{2a}, -v; -\frac{c-ip+a(v-2)}{2a}; e^{-2i(b+az)} \right) \right)$$

01.06.21.1377.01

$$\int e^{pz} \sin(cz) \sin^v(b + az) dz = i 2^{-v-1} \left( \frac{e^{(-ic+p)z}}{-ic+p} - \frac{e^{(ic+p)z}}{ic+p} \right) \binom{v}{\frac{v}{2}} (1-v \bmod 2) + 2^{-v-1} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{-2ibk-ibv} \left( \frac{e^{2ibv+(ic-2iak+p+ia)vz}}{ic-2iak+p+ia} + \frac{e^{2ibv+(-ic-2iak+p+ia)vz}}{ic+2iak-p-ia} + \frac{e^{4ibk+i\pi v+(ic+2iak+p-ia)vz}}{ic+2iak+p-ia} + \frac{e^{4ibk+i\pi v+(-ic+2iak+p-ia)vz}}{ic-2iak-p+ia} \right) ; v \in \mathbb{N}^+$$

**Involving  $e^{pz} \sin(cz + d) \sin^v(az + b)$**

01.06.21.1378.01

$$\int e^{pz} \sin(d + cz) \sin^v(b + az) dz = -\frac{1}{2} e^{-id} (1 - e^{-2i(b+az)})^{-v} \sin^v(b + az) \left( \frac{e^{(-ic+p)z}}{c + ip - av} {}_2F_1\left(\frac{c + ip - av}{2a}, -v; \frac{-va + 2a + c + ip}{2a}; e^{-2i(b+az)}\right) + \frac{e^{2id+(ic+p)z}}{c - ip + av} {}_2F_1\left(-\frac{c - ip + av}{2a}, -v; -\frac{c - ip + a(v-2)}{2a}; e^{-2i(b+az)}\right) \right)$$

01.06.21.1379.01

$$\int e^{pz} \sin(d + cz) \sin^v(b + az) dz = i 2^{-v-1} \left( \frac{e^{-id+(-ic+p)z}}{-ic+p} - \frac{e^{id+(ic+p)z}}{ic+p} \right) \binom{v}{\frac{v}{2}} (1 - v \bmod 2) + 2^{-v-1} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{id-2ibk-ibv} \left( \frac{e^{2ibv+(ic-2iak+p+ia)v}z}{ic-2iak+p+ia} + \frac{e^{-2id+2ibv+(-ic-2iak+p+ia)v}z}{ic+2iak-p-ia} + \frac{e^{4ibk+i\pi v+(ic+2iak+p-ia)v}z}{ic+2iak+p-ia} + \frac{e^{-2id+4ibk+i\pi v+(-ic+2iak+p-ia)v}z}{ic-2iak-p+ia} \right); v \in \mathbb{N}^+$$

**Involving  $e^{pz} \sin(bz) \sin^v(cz)$**

01.06.21.1380.01

$$\int e^{pz} \sin(bz) \sin^v(cz) dz = -\frac{i 2^{-v-2} e^{\frac{b^2}{4p}} \sqrt{\pi} (1 - v \bmod 2)}{\sqrt{p}} \binom{v}{\frac{v}{2}} \left( \operatorname{erfi}\left(\frac{ib+2pz}{2\sqrt{p}}\right) + \operatorname{erfi}\left(\frac{ib-2pz}{2\sqrt{p}}\right) \right) + \frac{i^{-v-1} 2^{-v-2} \sqrt{\pi}}{\sqrt{p}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{-b^2-2c(2k+v)b-c^2(v-2k)^2}{4p}} \binom{v}{k} \left( e^{-\frac{2bck}{p}} \operatorname{erfi}\left(\frac{ib-2ick+icv+2pz}{2\sqrt{p}}\right) + e^{i\pi v - \frac{bcv}{p}} \operatorname{erfi}\left(\frac{ib+2ick-icv+2pz}{2\sqrt{p}}\right) + e^{i\pi v - \frac{2bck}{p}} \operatorname{erfi}\left(\frac{ib-2ick+icv-2pz}{2\sqrt{p}}\right) + e^{-\frac{bcv}{p}} \operatorname{erfi}\left(\frac{ib+2ick-icv-2pz}{2\sqrt{p}}\right) \right); v \in \mathbb{N}^+$$

01.06.21.1381.01

$$\int e^{p\sqrt{z}} \sin(bz) \sin^v(cz) dz =$$

$$2^{-v} \binom{v}{\frac{v}{2}} \left( -\frac{e^{p\sqrt{z}} \cos(bz)}{b} + \frac{e^{-\frac{ip^2}{4b}} i p \sqrt{\pi} \operatorname{erf}\left(\frac{-p+2ib\sqrt{z}}{2\sqrt{ib}}\right)}{4(ib)^{3/2}} + \frac{e^{\frac{ip^2}{4b}} i p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2ib\sqrt{z}}{2\sqrt{ib}}\right)}{4(ib)^{3/2}} \right) (1-v \bmod 2) +$$

$$2^{-v-2} i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( \frac{2i e^{p\sqrt{z}-i(b+2ck-cv)z}}{b+2ck-cv} - \frac{2i(-1)^v e^{\sqrt{z} p+i(b+2ck-cv)z}}{b+2ck-cv} - \frac{2i(-1)^v e^{p\sqrt{z}-i(b+c(v-2k))z}}{b+c(v-2k)} - \frac{2i e^{\sqrt{z} p+i(b+c(v-2k))z}}{b+c(v-2k)} \right.$$

$$\frac{(-1)^v e^{\frac{ip^2}{4b+8ck-4cv}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2i(b+2ck-cv)\sqrt{z}}{2\sqrt{i(b+2ck-cv)}}\right)}{(i(b+2ck-cv))^{3/2}} - \frac{i e^{-\frac{ip^2}{4b-8ck+4cv}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{i p+2(b+2ck-cv)\sqrt{z}}{2\sqrt{i(b+2ck-cv)}}\right)}{(i(b+2ck-cv))^{3/2}}$$

$$\left. \frac{e^{\frac{ip^2}{4(b+c(v-2k))}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2i(b+c(v-2k))\sqrt{z}}{2\sqrt{i(b+c(v-2k))}}\right)}{(i(b+c(v-2k)))^{3/2}} - \frac{i(-1)^v e^{-\frac{ip^2}{4(b+c(v-2k))}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{i p+2(b+c(v-2k))\sqrt{z}}{2\sqrt{i(b+c(v-2k))}}\right)}{(i(b+c(v-2k)))^{3/2}} \right) /; v \in \mathbb{N}^+$$

**Involving  $e^{pZ} \sin(bz^r) \sin^v(cz)$**

01.06.21.1382.01

$$\int e^{pZ} \sin(bz^2) \sin^v(cz) dz = -\frac{i 2^{-v-2} \sqrt{\pi} \binom{v}{\frac{v}{2}} e^{\frac{ip^2}{4b}} \left( e^{-\frac{ip^2}{2b}} \operatorname{erf}\left(\frac{p-2ibz}{2\sqrt{ib}}\right) + \operatorname{erfi}\left(\frac{p+2ibz}{2\sqrt{ib}}\right) \right) (1-v \bmod 2)}{\sqrt{ib}} +$$

$$\frac{1}{\sqrt{ib}} \left( \left( i^{-v-1} 2^{-v-2} \sqrt{\pi} \right) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{\frac{i(p^2+2ci(2k+v)p-c^2(2k+v)^2)}{4b}} \binom{v}{k} \left( -e^{-\frac{i(-4k^2+v^2)c^2+2ipvc+p^2}{2b}} \operatorname{erf}\left(\frac{2ick-p-icv+2ibz}{2\sqrt{ib}}\right) \right.$$

$$e^{-\frac{i(-4k^2+v^2)c^2+4ikpc+p^2-2b\pi v}{2b}} \operatorname{erf}\left(\frac{-p+ci(v-2k)+2ibz}{2\sqrt{ib}}\right) +$$

$$\left. \left. e^{-\frac{i(-2k^2+ipc-b\pi)v}{b}} \operatorname{erfi}\left(\frac{2ick+p-icv+2ibz}{2\sqrt{ib}}\right) + e^{\frac{2ck(p+icv)}{b}} \operatorname{erfi}\left(\frac{p+ci(v-2k)+2ibz}{2\sqrt{ib}}\right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1383.01

$$\int e^{pz} \sin(b\sqrt{z}) \sin^v(cz) dz = 2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( \frac{b e^{\frac{b^2}{4p}} \sqrt{\pi} \left( \operatorname{erfi}\left(\frac{ib-2p\sqrt{z}}{2\sqrt{p}}\right) - \operatorname{erfi}\left(\frac{ib+2p\sqrt{z}}{2\sqrt{p}}\right) \right)}{4p^{3/2}} + \frac{e^{pz} \sin(b\sqrt{z})}{p} \right) + 2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-ib\sqrt{z} + (-2cik+p+icv)z} (-1 + e^{2ib\sqrt{z}})}{p + ci(v-2k)} + \frac{ib e^{\frac{b^2}{4(-2cik+p+icv)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+4ick\sqrt{z}-2p\sqrt{z}-2icv\sqrt{z}}{2\sqrt{-2cik+p+icv}}\right)}{2(-2cik+p+icv)^{3/2}} + \frac{i(-1)^v b e^{\frac{b^2}{4(2ick+p-icv)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib-4ick\sqrt{z}-2p\sqrt{z}+2icv\sqrt{z}}{2\sqrt{2ick+p-icv}}\right)}{2(2ick+p-icv)^{3/2}} - \frac{ib e^{\frac{b^2}{4(-2cik+p+icv)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib-4ick\sqrt{z}+2p\sqrt{z}+2icv\sqrt{z}}{2\sqrt{-2cik+p+icv}}\right)}{2(-2cik+p+icv)^{3/2}} + \frac{(-1)^v e^{-ib\sqrt{z} + (2ick+p-icv)z} (-1 + e^{2ib\sqrt{z}})}{2ick+p-icv} - \frac{i(-1)^v b e^{\frac{b^2}{4(2ick+p-icv)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+4ick\sqrt{z}+2p\sqrt{z}-2icv\sqrt{z}}{2\sqrt{2ick+p-icv}}\right)}{2(2ick+p-icv)^{3/2}} \right) /; v \in \mathbb{N}^+$$

**Involving  $e^{pz} \sin(bz) \sin^v(cz^r)$**

01.06.21.1384.01

$$\int e^{pz} \sin(bz) \sin^v(cz^2) dz = -i 2^{-v-1} \left( \frac{e^{(ib+p)z}}{ib+p} + \frac{e^{-(ib+p)z}}{ib-p} \right) \binom{v}{\frac{v}{2}} (1 - v \bmod 2) + \frac{2^{-v-2} i^{-v-1} \sqrt{\pi}}{\sqrt{ic}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{(-1)^k}{\sqrt{v-2k}} e^{\frac{-b^2+2ipb+p^2}{4(icv-2ick)}} \binom{v}{k} \left( e^{i\pi v} \operatorname{erf}\left(\frac{-ib-p-4ickz+2icvz}{2\sqrt{ic}\sqrt{v-2k}}\right) - \frac{ibp}{e^{2ick-icv}} + i\pi v \operatorname{erf}\left(\frac{ib-p+2ic(v-2k)z}{2\sqrt{ic}\sqrt{v-2k}}\right) + e^{\frac{(ib+p)^2}{4ick-2icv}} \operatorname{erfi}\left(\frac{ib+p+2ic(v-2k)z}{2\sqrt{ic}\sqrt{v-2k}}\right) + e^{\frac{p^2-b^2}{4ick-2icv}} \operatorname{erfi}\left(\frac{ib-p+4ickz-2icvz}{2\sqrt{ic}\sqrt{v-2k}}\right) \right) /; v \in \mathbb{N}^+$$



01.06.21.1385.01

$$\int e^{pz} \sin(bz) \sin^v(c\sqrt{z}) dz = 2^{-v-1} i \left( \frac{e^{(-ib+p)z}}{-ib+p} - \frac{e^{(ib+p)z}}{ib+p} \right) \left( \frac{v}{2} \right) (1 - v \bmod 2) +$$

$$2^{-v-2} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-\frac{1}{2}i\pi(v-1)} \left( - \frac{i e^{\frac{(2ck-cv)^2}{4(ib+p)}} \sqrt{\pi} (2ck-cv) \operatorname{erf} \left( \frac{2\sqrt{z} (b+ip)+c(2k-v)}{2\sqrt{-ib+p}} \right)}{(-b-ip)\sqrt{-ib+p}} + \right.$$

$$\frac{i e^{\frac{(cv-2ck)^2}{4(ib+p)} + i\pi(v-1)} \sqrt{\pi} (2ck-cv) \operatorname{erf} \left( \frac{2\sqrt{z} (b-ip)+c(2k-v)}{2\sqrt{ib+p}} \right)}{(ip-b)\sqrt{ib+p}} + \frac{2 e^{(-ib+p)z-i(2ck-cv)\sqrt{z}}}{-ib+p} +$$

$$\left. \frac{2 e^{i\pi(v-1)+(ib+p)z+i(2ck-cv)\sqrt{z}}}{ib+p} \right) + e^{\frac{1}{2}i\pi(v+1)} \left( \frac{c e^{\frac{c^2(v-2k)^2}{4(ib+p)} - i\pi(v+1)} \sqrt{\pi} (v-2k) \operatorname{erfi} \left( \frac{2\sqrt{z} (ib+p)+c(v-2k)}{2\sqrt{ib+p}} \right)}{(ip-b)\sqrt{ib+p}} - \right.$$

$$\frac{i c e^{\frac{ic^2(v-2k)^2}{4(b+ip)}} \sqrt{\pi} (v-2k) \operatorname{erf} \left( \frac{2\sqrt{z} (-b-ip)+c(2k-v)}{2\sqrt{-ib+p}} \right)}{(b+ip)\sqrt{-ib+p}} +$$

$$\left. \left. \frac{2 e^{(-ib+p)z-i(cv-2ck)\sqrt{z}}}{-ib+p} + \frac{2 e^{-i\pi(v+1)+(ib+p)z+i(cv-2ck)\sqrt{z}}}{ib+p} \right) \right) /; v \in \mathbb{N}^+$$

### Involving $e^{pz} \sin(bz^r) \sin^v(cz^r)$

01.06.21.1386.01

$$\int e^{pz} \sin(bz^2) \sin^v(cz^2) dz =$$

$$2^{-v-2} \sqrt{\pi} \left( \frac{i \left( e^{-\frac{ip^2}{4b}} \left( \frac{v}{2} \right) \left( \operatorname{erf} \left( \frac{p-2ibz}{2\sqrt{ib}} \right) + e^{\frac{ip^2}{2b}} \operatorname{erfi} \left( \frac{p+2ibz}{2\sqrt{ib}} \right) \right) (v \bmod 2 - 1) \right)}{\sqrt{ib}} + i^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{i(b-2ck+cv)}} \right.$$

$$\left. \left( e^{-\frac{ip^2}{4(b-2ck+cv)}} \left( e^{\frac{ip^2}{2(b-2ck+cv)}} \operatorname{erfi} \left( \frac{p+2i(b-2ck+cv)z}{2\sqrt{i(b-2ck+cv)}} \right) - i e^{i\pi v} \operatorname{erfi} \left( \frac{ip+2(b-2ck+cv)z}{2\sqrt{i(b-2ck+cv)}} \right) \right) \right) -$$

$$\left. \frac{e^{i \left( \frac{p^2}{4b+8ck-4cv} + \pi v \right)} \operatorname{erf} \left( \frac{p+2i(b+2ck-cv)z}{2\sqrt{-i(b+2ck-cv)}} \right) - i e^{-\frac{ip^2}{4b-8ck+4cv}} \operatorname{erfi} \left( \frac{ip+2(b+2ck-cv)z}{2\sqrt{i(b+2ck-cv)}} \right)}{\sqrt{-i(b+2ck-cv)}} - \frac{i e^{-\frac{ip^2}{4b-8ck+4cv}} \operatorname{erfi} \left( \frac{ip+2(b+2ck-cv)z}{2\sqrt{i(b+2ck-cv)}} \right)}{\sqrt{i(b+2ck-cv)}} \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1387.01

$$\int e^{pz} \sin(b\sqrt{z}) \sin^v(c\sqrt{z}) dz =$$

$$2^{-v-2} i \left( \frac{b e^{\frac{b^2}{4p}} i \sqrt{\pi} \operatorname{erfi}\left(\frac{-ib+2p\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} + \frac{4 e^{-\frac{1}{2}(i\pi)+pz} \sin(b\sqrt{z})}{p} - \frac{ib e^{\frac{b^2}{4p}-i\pi} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+2p\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} \right) \left( \frac{v}{2} \right) (1 - v \bmod 2) +$$

$$2^{-v-2} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{4 e^{pz - \frac{1}{2}i\pi(1-v)} \cos\left(\frac{1}{2}\pi(v-1) + (b+2ck-cv)\sqrt{z}\right)}{p} + \right.$$

$$\frac{e^{\frac{(b+2ck-cv)^2}{4p}} \sqrt{\pi} (b+2ck-cv) \operatorname{erf}\left(\frac{b+c(2k-v)+2ip\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} +$$

$$\left. \frac{e^{\frac{(-b-2ck+cv)^2}{4p} + i\pi(v-1)} \sqrt{\pi} (b+2ck-cv) \operatorname{erf}\left(\frac{b+c(2k-v)-2ip\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} \right) +$$

$$e^{\frac{1}{2}i\pi(v+1)} \left( \frac{4 e^{pz - \frac{1}{2}i\pi(v+1)} \cos\left(\frac{1}{2}\pi(v+1) + (-b+2ck-cv)\sqrt{z}\right)}{p} - \right.$$

$$\frac{e^{\frac{(b+c(v-2k))^2}{4p}} \sqrt{\pi} (b+c(v-2k)) \operatorname{erf}\left(\frac{-b+c(2k-v)-2ip\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} -$$

$$\left. \frac{ie^{\frac{(b+c(v-2k))^2}{4p} - i\pi(v+1)} \sqrt{\pi} (b+c(v-2k)) \operatorname{erfi}\left(\frac{ib+ic(v-2k)+2p\sqrt{z}}{2\sqrt{p}}\right)}{p^{3/2}} \right) \Bigg) /; v \in \mathbb{N}^+$$

Involving  $e^{pz} \sin(bz) \sin^v(cz^r)$

01.06.21.1388.01

$$\int e^{p z^2} \sin(b z) \sin^v(c z^2) dz = -\frac{i 2^{-v-2} e^{\frac{b^2}{4p}} \sqrt{\pi} (1-v \bmod 2) \left(\frac{v}{2}\right) \left(\operatorname{erfi}\left(\frac{ib+2pz}{2\sqrt{p}}\right) + \operatorname{erfi}\left(\frac{ib-2pz}{2\sqrt{p}}\right)\right)}{\sqrt{p}} -$$

$$2^{-v-2} i^{-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-\frac{b^2}{8ick-4p-4icv}} \binom{v}{k} \left( e^{i\pi v - \frac{1}{4} b^2 \left(\frac{1}{-2cik+p+icv} + \frac{1}{-2cik-p+icv}\right)} \sqrt{ic(v-2k)-p} \right.$$

$$\left. \sqrt{p+ci(v-2k)} \left( \operatorname{erf}\left(\frac{ib+2(2ick+p-icv)z}{2\sqrt{ic(v-2k)-p}}\right) + \operatorname{erf}\left(\frac{ib-2(2ick+p-icv)z}{2\sqrt{ic(v-2k)-p}}\right) \right) + \right.$$

$$\left. (2ick+p-icv) \left( \operatorname{erfi}\left(\frac{ib+2(-2cik+p+icv)z}{2\sqrt{-2cik+p+icv}}\right) + \operatorname{erfi}\left(\frac{ib+4ickz-2pz-2icvz}{2\sqrt{-2cik+p+icv}}\right) \right) \right) /$$

$$\left( (-2cik-p+icv) \sqrt{p+ci(v-2k)} \right); v \in \mathbb{N}^+$$

01.06.21.1389.01

$$\int e^{p\sqrt{z}} \sin(bz) \sin^v(c\sqrt{z}) dz =$$

$$2^{-v-2} \left( \frac{4 e^{p\sqrt{z}} i \cos(bz)}{b} - \frac{e^{-\frac{ip^2}{4b}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p-2ib\sqrt{z}}{2\sqrt{-ib}}\right)}{(-ib)^{3/2}} - \frac{e^{\frac{ip^2}{4b}-i\pi} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2ib\sqrt{z}}{2\sqrt{ib}}\right)}{(ib)^{3/2}} \right) i \binom{v}{\frac{v}{2}} (1-v \bmod 2) +$$

$$\frac{2^{-v-2}}{b} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-\frac{1}{2}i\pi(v-1)} \left( 2i e^{(p-i(2ck-cv))\sqrt{z}-ibz} - 2i e^{i\pi(v-1)+ibz+(p+i(2ck-cv))\sqrt{z}} - \frac{e^{\frac{i(2ck+ip-cv)^2}{4b}} \sqrt{\pi} (2ck+ip-cv) \operatorname{erfi}\left(\frac{p-i(2\sqrt{z}b+c(2k-v))}{2\sqrt{-ib}}\right)}{\sqrt{-ib}} - \frac{1}{\sqrt{ib}} \left( e^{i\pi(v-1)-\frac{i(-2ck+ip+cv)^2}{4b}} \sqrt{\pi} (2ck-ip-cv) \operatorname{erfi}\left(\frac{p+i(2\sqrt{z}b+c(2k-v))}{2\sqrt{ib}}\right) \right) \right) \right) + e^{\frac{1}{2}i\pi(v+1)} \left( 2i e^{(p-i(cv-2ck))\sqrt{z}-ibz} - 2i e^{-i\pi(v+1)+ibz+(p+i(cv-2ck))\sqrt{z}} - \frac{e^{\frac{i(ip+cv-2k)^2}{4b}} \sqrt{\pi} (ip+cv-2k) \operatorname{erfi}\left(\frac{p+i(c(2k-v)-2b\sqrt{z})}{2\sqrt{-ib}}\right)}{\sqrt{-ib}} - \frac{1}{\sqrt{ib}} \left( e^{\frac{i(p+cv-2k)^2}{4b}-i\pi(v+1)} \sqrt{\pi} (cv-2k-ip) \operatorname{erfi}\left(\frac{p+ic(v-2k)+2ib\sqrt{z}}{2\sqrt{ib}}\right) \right) \right) \right) /; v \in \mathbb{N}^+$$

Involving  $z^n e^{pz'} \sin(bz') \sin^v(cz)$

01.06.21.1390.01

$$\int z^n e^{p z^2} \sin(b z^2) \sin^v(c z) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( ((-i b - p) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-i b - p) z^2\right) - ((i b - p) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b - p) z^2\right) \right) (1 - v \bmod 2) +$$

$$\frac{2^{-v-2} i^{-v-1}}{\sqrt{-i b + p} \sqrt{i b + p}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{\frac{c^2 p (v-2s)^2}{2(-i b + p)(i b + p)}} \binom{v}{s}$$

$$\left( (-1)^v e^{-\frac{c^2 (v-2s)^2}{4(i b + p)}} \sqrt{i b + p} \sum_{q=0}^n 2^{q-n} (-i b + p)^{-n-\frac{1}{2}} (i c (v-2s))^{n-q} (c i (2s-v) + 2(-i b + p) z)^{q+1} \right.$$

$$\left. \left( -\frac{(c i (2s-v) + 2(-i b + p) z)^2}{-i b + p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(c i (2s-v) + 2(-i b + p) z)^2}{4(-i b + p)}\right) + \right.$$

$$e^{-\frac{c^2 (v-2s)^2}{4(i b + p)}} \sqrt{i b + p} \sum_{q=0}^n (-i b + p)^{-n-\frac{1}{2}} \left( i c \left( s - \frac{v}{2} \right) \right)^{n-q} (c i (v-2s) + 2(-i b + p) z)^{q+1}$$

$$\left. \left( -\frac{(c i (v-2s) + 2(-i b + p) z)^2}{-i b + p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(c i (v-2s) + 2(-i b + p) z)^2}{4(-i b + p)}\right) - \right.$$

$$e^{-\frac{c^2 (v-2s)^2}{4(-i b + p)}} \sqrt{-i b + p} \left( (-1)^v \sum_{q=0}^n 2^{q-n} (i b + p)^{-n-\frac{1}{2}} (i c (v-2s))^{n-q} (c i (2s-v) + 2(i b + p) z)^{q+1} \right.$$

$$\left. \left( -\frac{(c i (2s-v) + 2(i b + p) z)^2}{i b + p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(c i (2s-v) + 2(i b + p) z)^2}{4(i b + p)}\right) + \right.$$

$$\left. \sum_{q=0}^n (i b + p)^{-n-\frac{1}{2}} \left( i c \left( s - \frac{v}{2} \right) \right)^{n-q} (c i (v-2s) + 2(i b + p) z)^{q+1} \left( -\frac{(c i (v-2s) + 2(i b + p) z)^2}{i b + p} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(c i (v-2s) + 2(i b + p) z)^2}{4(i b + p)}\right) \right) \right) /; v \in \mathbb{N}^+ \wedge n \in \mathbb{N}$$

01.06.21.1391.01

$$\int z^n e^{p \sqrt{z}} \sin(b \sqrt{z}) \sin^v(c z) dz =$$

$$2^{-v} i z^{n+1} \left(\frac{v}{2}\right) \left( ((-i b - p) \sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (-i b - p) \sqrt{z}) - ((i b - p) \sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (i b - p) \sqrt{z}) \right)$$

$$(1 - v \bmod 2) - i^{1-v} 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v-1} e^{-\frac{i(-i b + p)^2}{4c(v-2s)}} (-i c (v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b + p)^{-h-j+2n} \right.$$

$$\begin{aligned}
 & (-ib+p-2ic(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-ib+p) \\
 & (-ib+p-2ic(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) - 2ic(v-2s) \\
 & \sqrt{-\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) \Bigg) + \\
 & (-1)^v e^{-\frac{i(ib+p)^2}{4c(v-2s)}} (-ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+p)^{-h-j+2n} (ib+p-2ic(v-2s)\sqrt{z})^{h+j} \\
 & \left( -\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (ib+p)(ib+p-2ic(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) - 2ic(v-2s) \right. \\
 & \left. \sqrt{-\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) \right) - \\
 & e^{\frac{i(-ib+p)^2}{4c(v-2s)}} (ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+p)^{-h-j+2n} (-ib+p+2ic(v-2s)\sqrt{z})^{h+j} \\
 & \left( \frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (-ib+p)(-ib+p+2ic(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) + 2ci \right. \\
 & \left. (v-2s) \sqrt{\frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & e^{\frac{i(i b+p)^2}{4 c(v-2 s)}} (i c(v-2 s))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b+p)^{-h-j+2 n} (i b+p+2 i c(v-2 s) \sqrt{z})^{h+j} \\
 & \left( \frac{i(i b+p+2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (i b+p)(i b+p+2 i c(v-2 s) \sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. \frac{i(i b+p+2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)} \right) + 2 c i(v-2 s) \sqrt{\frac{i(i b+p+2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)}} \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+2), \frac{i(i b+p+2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)} \right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $e^{p z^r} \sin(b z^r) \sin^v(c z^r)$

01.06.21.1392.01

$$\int e^{p z^r} \sin(b z^r) \sin^v(c z^r) dz =$$

$$\frac{2^{-v-1} z}{r} \left( i \binom{v}{\frac{v}{2}} \left( ((-i b-p) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, (-i b-p) z^r \right) - (i(b+i p) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, i(b+i p) z^r \right) \right) (1-v \bmod 2) + i^{-v-1} \right.$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \Gamma \left( \frac{1}{r}, i(b+i p-2 c s+c v) z^r \right) (i(b+i p-2 c s+c v) z^r)^{-1/r} - (-i(b-i p-2 c s+c v) z^r)^{-1/r} \right.$$

$$\Gamma \left( \frac{1}{r}, -i(b-i p-2 c s+c v) z^r \right) + (i(b+i p+2 c s-c v) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, i(b+i p+2 c s-c v) z^r \right) -$$

$$\left. (-1)^v (-i(b-i p+2 c s-c v) z^r)^{-1/r} \Gamma \left( \frac{1}{r}, -i(b-i p+2 c s-c v) z^r \right) \right) \Bigg) ; v \in \mathbb{N}^+$$

01.06.21.1393.01

$$\int e^{pz^2} \sin(bz^2) \sin^v(cz^2) dz =$$

$$2^{-v-2} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \left( e^{\frac{1}{2}i\pi(v-1)} \sqrt{ib+p+ic(2k-v)} (-ib+p-ic(2k-v)) \operatorname{erfi}\left(\sqrt{ib+p+ic(2k-v)} z\right) + \right. \right.$$

$$e^{-\frac{1}{2}i\pi(v-1)} (ib+p+ic(2k-v)) \sqrt{-ib+p-ic(2k-v)} \operatorname{erfi}\left(\sqrt{-ib+p-ic(2k-v)} z\right) \Big) /$$

$$\left( (-ib+p-ic(2k-v))(ib+p+ic(2k-v)) \right) + \left( e^{-\frac{1}{2}i\pi(v+1)} \sqrt{ib+p+ic(v-2k)} (-ib+p-ic(v-2k)) \right.$$

$$\operatorname{erfi}\left(\sqrt{ib+p+ic(v-2k)} z\right) + e^{\frac{1}{2}i\pi(v+1)} (ib+p+ic(v-2k)) \sqrt{-ib+p-ic(v-2k)} \operatorname{erfi}\left(\sqrt{-ib+p-ic(v-2k)} z\right) \Big) /$$

$$\left( (-ib+p-ic(v-2k))(ib+p+ic(v-2k)) \right) \Big) -$$

$$\frac{i 2^{-v-2} \sqrt{\pi}}{(-ib+p)(ib+p)} \binom{v}{\frac{v}{2}} \left( (-ib+p) \sqrt{ib+p} \operatorname{erfi}\left(\sqrt{ib+p} z\right) - \sqrt{-ib+p} (ib+p) \operatorname{erfi}\left(\sqrt{-ib+p} z\right) \right)$$

(1 - v mod 2) /; v ∈ ℕ<sup>+</sup>

01.06.21.1394.01

$$\int e^{p\sqrt{z}} \sin(b\sqrt{z}) \sin^v(c\sqrt{z}) dz =$$

$$2^{-v} e^{\frac{i\pi}{2}+(-ib+p)\sqrt{z}} \left( \frac{e^{2\left(-\frac{1}{2}(i\pi+ib\sqrt{z})\right)} (-1+ib\sqrt{z}+p\sqrt{z})}{(ib+p)^2} + \frac{\sqrt{z}}{-ib+p} - \frac{1}{(ib-p)^2} \right) \binom{v}{\frac{v}{2}} (1 - v \bmod 2) +$$

$$2^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{(-ib+p-ic(2k-v))\sqrt{z} - \frac{1}{2}i\pi(v-1)} \left( \frac{e^{2\left(\sqrt{z}(ib+ic(2k-v)) + \frac{1}{2}i\pi(v-1)\right)} (\sqrt{z} p + (ib+ic(2k-v))\sqrt{z} - 1)}{(ib+p+ic(2k-v))^2} + \right. \right.$$

$$\left. \frac{\sqrt{z}}{-ib+p-ic(2k-v)} - \frac{1}{(ib-p+ic(2k-v))^2} \right) +$$

$$e^{\frac{1}{2}i\pi(v+1)+(-ib+p-ic(v-2k))\sqrt{z}} \left( \frac{e^{2\left((ib+ic(v-2k))\sqrt{z} - \frac{1}{2}i\pi(v+1)\right)} (\sqrt{z} p + (ib+ic(v-2k))\sqrt{z} - 1)}{(ib+p+ic(v-2k))^2} + \right.$$

$$\left. \frac{\sqrt{z}}{-ib+p-ic(v-2k)} - \frac{1}{(ib-p+ic(v-2k))^2} \right) \Big) /; v \in \mathbb{N}^+$$

Involving  $e^{bz^r+e} \sin(az^r+q) \sin^v(cz^r+g)$



01.06.21.1395.01

$$\int e^{bz^r+e} \sin(az^r+q) \sin^v(cz^r+g) dz =$$

$$\frac{i 2^{-v-1} z \left(\frac{v}{2}\right)}{r} \left( e^{e+iq} ((-b-ia)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-ia)z^r\right) - e^{e-iq} ((ia-b)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (ia-b)z^r\right) \right) (1-v \bmod 2) +$$

$$\frac{i^{-v-1} 2^{-v-1} z \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{e+iq+2igs-igv} \Gamma\left(\frac{1}{r}, (-b-ia-2ics+icv)z^r\right) ((-b-ia-2ics+icv)z^r)^{-1/r} + \right.$$

$$\left. (-1)^v e^{e-iq+2igs-igv} ((-b+ia-2ics+icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b+ia-2ics+icv)z^r\right) - \right.$$

$$\left. e^{e+iq-2igs+igv} ((-b-ia+2ics-icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-ia+2ics-icv)z^r\right) + \right.$$

$$\left. e^{e-iq-2igs+igv} ((-b+ia+2ics-icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b+ia+2ics-icv)z^r\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1396.01

$$\int e^{bz^2+e} \sin(az^2+q) \sin^v(cz^2+g) dz =$$

$$2^{-v-2} \left( \frac{e^{2\left(\frac{i\pi}{2}-iq\right)} \operatorname{erfi}(\sqrt{b-ia}z)}{\sqrt{b-ia}} + \frac{\operatorname{erfi}(\sqrt{b+ia}z)}{\sqrt{b+ia}} \right) e^{e+iq-\frac{i\pi}{2}} \sqrt{\pi} \left(\frac{v}{2}\right) (1-v \bmod 2) +$$

$$2^{-v-2} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{e-iq-\frac{1}{2}i\pi(v-1)+gi(v-2s)} \left( \frac{\operatorname{erfi}(\sqrt{b-ia+ci(v-2s)}z)}{\sqrt{b-ia+ci(v-2s)}} + \right.$$

$$\left. \frac{e^{2\left(iq+\frac{1}{2}i\pi(v-1)-ig(v-2s)\right)} \operatorname{erfi}(\sqrt{b+ia-ic(v-2s)}z)}{\sqrt{b+ia-ic(v-2s)}} \right) + e^{e+iq-\frac{1}{2}i\pi(v+1)+gi(v-2s)}$$

$$\left. \left( \frac{\operatorname{erfi}(\sqrt{b+ia+ci(v-2s)}z)}{\sqrt{b+ia+ci(v-2s)}} + \frac{e^{2\left(-iq+\frac{1}{2}i\pi(v+1)-ig(v-2s)\right)} \operatorname{erfi}(\sqrt{b-ia-ic(v-2s)}z)}{\sqrt{b-ia-ic(v-2s)}} \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1397.01

$$\int e^{\sqrt{z} b+e} \sin(\sqrt{z} a+q) \sin^v(\sqrt{z} c+g) dz =$$

$$2^{-v} \left( \frac{e^{\sqrt{z} (b+ia)+e+iq-\frac{i\pi}{2}} (\sqrt{z} b+ia\sqrt{z}-1)}{(-b-ia)^2} + \frac{e^{\sqrt{z} (b-ia)+e-iq+\frac{i\pi}{2}} (\sqrt{z} b-ia\sqrt{z}-1)}{(b-ia)^2} \right) \left( \frac{v}{2} \right) (1-v \bmod 2) +$$

$$2^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \left( \left( e^{e+iq+\frac{1}{2}i\pi(v+1)-ig(v-2s)+(b-ia-ic(v-2s))\sqrt{z}} (\sqrt{z} b+(-ia-ic(v-2s))\sqrt{z}-1) \right) / (b-ia-ic(v-2s))^2 + \right.$$

$$\left( e^{e+iq+\frac{1}{2}i\pi(v-1)-ig(v-2s)+(b+ia-ic(v-2s))\sqrt{z}} (\sqrt{z} b+(ia-ic(v-2s))\sqrt{z}-1) \right) / (b+ia-ic(v-2s))^2 +$$

$$\left( e^{e+iq-\frac{1}{2}i\pi(v+1)+gi(v-2s)+(b+ia+ci(v-2s))\sqrt{z}} (\sqrt{z} b-(-ia-ic(v-2s))\sqrt{z}-1) \right) / (-b-ia-ic(v-2s))^2 +$$

$$\left( e^{e+iq-\frac{1}{2}i\pi(v-1)+gi(v-2s)+(b-ia+ci(v-2s))\sqrt{z}} (\sqrt{z} b-(ia-ic(v-2s))\sqrt{z}-1) \right) /$$

$$\left. (-b+ia-ic(v-2s))^2 \right) \binom{v}{s} /; v \in \mathbb{N}^+$$

**Involving  $e^{bz'+dz+e} \sin(az'+pz+q) \sin^v(cz'+fz+g)$**

01.06.21.1398.01

$$\int e^{bz^2+dz+e} \sin(az^2+pz+q) \sin^v(cz^2+fz+g) dz =$$

$$\frac{2^{-v-2} \sqrt{\pi}}{a^2+b^2} \left( \frac{v}{2} \right) (1-v \bmod 2) \left( \sqrt{b-ia} (b+ia) e^{\frac{-(d-ip)^2-2(-a-ib)(-2ie+\pi-2q)}{4(b-ia)}} \operatorname{erfi} \left( \frac{d-ip+2(b-ia)z}{2\sqrt{b-ia}} \right) + \right.$$

$$\left. (b-ia) \sqrt{b+ia} e^{\frac{-(d+ip)^2-2(ib-a)(2ie+\pi-2q)}{4(b+ia)}} \operatorname{erfi} \left( \frac{d+ip+2bz+2iaz}{2\sqrt{b+ia}} \right) \right) + 2^{-v-2} \sqrt{\pi}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \left( e^{\frac{-(d+i(-p+2fs-fv))^2-2(-a+ib-2cs+c v)(-2ie+\pi-2q+4gs-2gv+\pi v)(-a+ib+2cs-cv)}{4(b+i(-a+2cs-cv))}} \operatorname{erfi} \left( \frac{d-ip+fi(2s-v)+2(b-ia+ci(2s-v))z}{2\sqrt{b-ia+ci(2s-v)}} \right) \right) /$$

$$\left( \sqrt{b-ia+ci(2s-v)} \right) + \frac{1}{\sqrt{b+ia+ci(2s-v)}} \left( e^{\frac{-(d+i(p+2fs-fv))^2-2(-a+ib-2cs+c v)(2ie+\pi-2q-4gs+2gv-\pi v)}{4(b-i(-a-2cs+c v))}} \operatorname{erfi} \left( \frac{d+ip+fi(2s-v)+2(b+ia+ci(2s-v))z}{2\sqrt{b+ia+ci(2s-v)}} \right) \right) +$$

$$\left( e^{\frac{-(d+i(-p-2fs+fv))^2-2(-a-ib-2cs+c v)(-2ie+\pi-2q-4gs+2gv-\pi v)}{4(b+i(-a-2cs+c v))}} \operatorname{erfi} \left( \frac{d-ip+fi(v-2s)+2(b-ia+ci(v-2s))z}{2\sqrt{b-ia+ci(v-2s)}} \right) \right) /$$

$$\left( \sqrt{b-ia+ci(v-2s)} \right) + \frac{1}{\sqrt{b+ia+ci(v-2s)}} \left( e^{\frac{-(d+ip+fi(v-2s))^2-2(2ie+\pi-2q+4gs-2gv+\pi v)(-a+ib+2cs-cv)}{4(b+ia+ci(v-2s))}} \operatorname{erfi} \left( \frac{d+ip+fi(v-2s)+2(b+ia+ci(v-2s))z}{2\sqrt{b+ia+ci(v-2s)}} \right) \right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1399.01

$$\int e^{\sqrt{z} b+d z+e} \sin(\sqrt{z} a+p z+q) \sin^v(\sqrt{z} c+f z+g) d z =$$

$$2^{-v-2} e^{-i q+\frac{i \pi}{2}\left(\frac{v}{2}\right)} \left( \frac{(b+i a) e^{-\frac{(b+i a)^2}{4(d+i p)}+2 i q-i \pi} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+i a+2(d+i p) \sqrt{z}}{2 \sqrt{d+i p}}\right)}{(d+i p)^{3 / 2}} + \right.$$

$$\left. \frac{(i a-b) e^{-\frac{(b-i a)^2}{4(d-i p)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b-i a+2(d-i p) \sqrt{z}}{2 \sqrt{d-i p}}\right)}{(d-i p)^{3 / 2}} + \frac{2 e^{\sqrt{z}(b+i a)+2 i q+(d+i p) z-i \pi}}{d+i p} + \frac{2 e^{\sqrt{z}(b-i a)+(d-i p) z}}{d-i p} \right) (1-v \bmod 2) +$$

$$2^{-v-2} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-i q+\frac{1}{2} i \pi(v+1)-i g(v-2 k)} \left( \left( e^{-\frac{(b+i(a+c(v-2 k)))^2}{4(d+i p+f i(v-2 k))}+2 i q-i \pi(v+1)+2 g i(v-2 k)} \sqrt{\pi}(a-i b+c(v-2 k)) \right. \right.$$

$$\left. \left. \operatorname{erfi}\left(\frac{b+i a+c i(v-2 k)+2(d+i p+f i(v-2 k)) \sqrt{z}}{2 \sqrt{d+i p+f i(v-2 k)}}\right) \right) / \left( (i d+2 f k-p-f v) \right. \right.$$

$$\left. \left. \sqrt{d+i p+f i(v-2 k)} \right) + \frac{2 e^{2 i q-i \pi(v+1)+2 g i(v-2 k)+(d+i p+f i(v-2 k)) z+(b+i(a-2 c k+c v)) \sqrt{z}}}{d+i p+f i(v-2 k)} - \right.$$

$$\left. \left( e^{\frac{i(a+i b+c(v-2 k))^2}{4(i d+p+f(v-2 k))}} \sqrt{\pi}(a+i b+c(v-2 k)) \operatorname{erfi}\left(\frac{b+i(-a+c(2 k-v)+2(-i d+2 f k-p-f v) \sqrt{z})}{2 \sqrt{d+i(2 f k-p-f v)}}\right) \right) / \right.$$

$$\left. \left( (i d+p+f(v-2 k)) \sqrt{d+i(2 f k-p-f v)} \right) + \frac{2 e^{\sqrt{z}(b-i(a-2 c k+c v)+(d+i(2 f k-p-f v)) z}}}{d+i(2 f k-p-f v)} \right) +$$

$$e^{-i q-i g(2 k-v)-\frac{1}{2} i \pi(v-1)} \left( \left( e^{\frac{(-a+i b-2 c k+c v)^2}{4(d+i(2 f k+p-f v))}+2 i q+2 g i(2 k-v)+i \pi(v-1)} \sqrt{\pi}(a-i b+2 c k-c v) \right. \right.$$

$$\left. \left. \operatorname{erfi}\left(\frac{b+i(a+c(2 k-v)+2(-i d+2 f k+p-f v) \sqrt{z})}{2 \sqrt{d+i(2 f k+p-f v)}}\right) \right) / \right.$$

$$\left. \left( (i d-2 f k-p+f v) \sqrt{d+i(2 f k+p-f v)} \right) + \left( e^{\frac{(a+i b+2 c k-c v)^2}{4(d-i(2 f k+p-f v))}} \sqrt{\pi}(a+i b+2 c k-c v) \right. \right.$$

$$\left. \left. \operatorname{erfi}\left(\frac{b-i(a+c(2 k-v)+2(i d+2 f k+p-f v) \sqrt{z})}{2 \sqrt{d-i(2 f k+p-f v)}}\right) \right) / \left( (-i d-2 f k-p+f v) \right. \right.$$

$$\left. \left. \sqrt{d-i(2 f k+p-f v)} \right) + \frac{2 e^{2 i q+2 g i(2 k-v)+i \pi(v-1)+(d+i(2 f k+p-f v)) z+(b+i(a+2 c k-c v)) \sqrt{z}}}{d+i(2 f k+p-f v)} + \right.$$

$$\left. \left. 2 e^{\sqrt{z}(b-i(a+2 c k-c v)+(d-i(2 f k+p-f v)) z} \right) \right) \dots \infty+$$

Involving product of power of the direct function, the direct function and rational functions of exp

**Involving  $\sin(ez) \sin^v(cz) (a + b e^{dz})^{-n}$**

01.06.21.1400.01

$$\int \frac{\sin(ez) \sin^v(cz)}{(a + b e^{dz})^n} dz =$$

$$2^{-v-1} a^{-n} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{1}{-ie-2ics+icv} i \cos\left(\frac{\pi v}{2}\right) \left( e^{(-ie-2ics+icv)z} {}_2F_1\left(\frac{-ie-2ics+icv}{d}, n; \frac{d-ie-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right); \right. \right.$$

$$\left. \left. -\frac{b e^{dz}}{a} \right) + e^{(ie+2ics-icv)z} {}_2F_1\left(\frac{ie+2ics-icv}{d}, n; \frac{d+ie+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) +$$

$$\frac{1}{-ie+2ics-icv} i \cos\left(\frac{\pi v}{2}\right) \left( e^{(ie-2ics+icv)z} {}_2F_1\left(\frac{ie-2ics+icv}{d}, n; \frac{d+ie-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) + \right.$$

$$\left. e^{(-ie+2ics-icv)z} {}_2F_1\left(\frac{-ie+2ics-icv}{d}, n; \frac{d-ie+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) -$$

$$\frac{1}{-ie+2ics-icv} \sin\left(\frac{\pi v}{2}\right) \left( e^{(ie+2ics-icv)z} {}_2F_1\left(\frac{-ie+2ics-icv}{d}, n; \frac{d-ie+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) - \right.$$

$$\left. e^{(ie-2ics+icv)z} {}_2F_1\left(\frac{ie-2ics+icv}{d}, n; \frac{d+ie-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) \right) +$$

$$\frac{1}{-ie-2ics+icv} \sin\left(\frac{\pi v}{2}\right) \left( e^{(-ie-2ics+icv)z} {}_2F_1\left(\frac{-ie-2ics+icv}{d}, n; \frac{d-ie-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) - \right.$$

$$\left. e^{(ie+2ics-icv)z} {}_2F_1\left(\frac{ie+2ics-icv}{d}, n; \frac{d+ie+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) -$$

$$\frac{2^{-v-1} a^{-n}}{e} \binom{v}{\frac{v}{2}} \left( e^{+ie z} {}_2F_1\left(\frac{ie}{d}, n; \frac{d+ie}{d}; -\frac{b e^{dz}}{a}\right) + e^{-ie z} {}_2F_1\left(-\frac{ie}{d}, n; \frac{d-ie}{d}; -\frac{b e^{dz}}{a}\right) \right)$$

$(1 - v \bmod 2) / ; n \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$

**Involving  $e^{pz} \sin(ez) \sin^v(cz) (a + b e^{dz})^{-n}$**

01.06.21.1401.01

$$\int \frac{e^{p z} \sin(e z) \sin^v(c z)}{(a + b e^{d z})^n} dz =$$

$$2^{-v-1} a^{-n} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( i \cos\left(\frac{\pi v}{2}\right) \left( e^{(-ie+p-2ics+icv)z} (-ie-p-2ics+icv) {}_2F_1\left(\frac{-ie+p-2ics+icv}{d}, n; \frac{d-ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) + e^{(ie+p+2ics-icv)z} (-ie+p-2ics+icv) {}_2F_1\left(\frac{ie+p+2ics-icv}{d}, n; \frac{d+ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) / \right.$$

$$\left. ((-ie-p-2ics+icv)(-ie+p-2ics+icv)) + i \cos\left(\frac{\pi v}{2}\right) \left( e^{(ie+p+2ics+icv)z} (-ie+p+2ics-icv) {}_2F_1\left(\frac{ie+p+2ics+icv}{d}, n; \frac{d+ie+p+2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) + e^{(-ie+p+2ics-icv)z} (-ie-p+2ics-icv) {}_2F_1\left(\frac{-ie+p+2ics-icv}{d}, n; \frac{d-ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) / \right.$$

$$\left. ((-ie-p+2ics-icv)(-ie+p+2ics-icv)) - \sin\left(\frac{\pi v}{2}\right) \left( e^{(-ie+p+2ics-icv)z} (-ie-p+2ics-icv) {}_2F_1\left(\frac{-ie+p+2ics-icv}{d}, n; \frac{d-ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) - e^{(ie+p-2ics+icv)z} (ie+p-2ics+icv) {}_2F_1\left(\frac{ie+p-2ics+icv}{d}, n; \frac{d+ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) \right) / \right.$$

$$\left. ((-ie-p+2ics-icv)(-ie+p+2ics-icv)) + \sin\left(\frac{\pi v}{2}\right) \left( e^{(-ie+p-2ics+icv)z} (-ie-p-2ics+icv) {}_2F_1\left(\frac{-ie+p-2ics+icv}{d}, n; \frac{d-ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) - e^{(ie+p+2ics-icv)z} (ie+p+2ics-icv) {}_2F_1\left(\frac{ie+p+2ics-icv}{d}, n; \frac{d+ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) \right)$$

$$\left. - \frac{i 2^{-v-1} a^{-n}}{(ie-p)(ie+p)} \binom{v}{\frac{v}{2}} \left( e^{(-ie+p)z} (ie+p) {}_2F_1\left(\frac{-ie+p}{d}, n; \frac{d-ie+p}{d}; -\frac{b e^{dz}}{a}\right) + e^{(ie+p)z} (ie-p) {}_2F_1\left(\frac{ie+p}{d}, n; \frac{d+ie+p}{d}; -\frac{b e^{dz}}{a}\right) \right) (1 - v \bmod 2) ; n \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving product of power of the direct function, the direct function and algebraic functions of exp

### Involving $(a + b e^{dz})^\beta \sin(ez) \sin^v(cz)$

01.06.21.1402.01

$$\int (a + b e^{dz})^\beta \sin(ez) \sin^v(cz) dz = 2^{-v-1} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{1}{-e - 2cs + cv} \left( e^{(-ie-2ics+icv)z} {}_2F_1 \left( \frac{-ie-2ics+icv}{d}, -\beta; \frac{d-ie-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) + e^{(ie+2ics-icv)z} {}_2F_1 \left( \frac{ie+2ics-icv}{d}, -\beta; \frac{d+ie+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \cos\left(\frac{\pi v}{2}\right) + \frac{1}{-e+2cs-cv} \left( e^{(ie-2ics+icv)z} {}_2F_1 \left( \frac{ie-2ics+icv}{d}, -\beta; \frac{d+ie-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) + e^{(-ie+2ics-icv)z} {}_2F_1 \left( \frac{-ie+2ics-icv}{d}, -\beta; \frac{d-ie+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \cos\left(\frac{\pi v}{2}\right) - \frac{1}{-ie+2ics-icv} \left( \sin\left(\frac{v\pi}{2}\right) \left( e^{(-ie+2ics-icv)z} {}_2F_1 \left( \frac{-ie+2ics-icv}{d}, -\beta; \frac{d-ie+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) - e^{(ie-2ics+icv)z} {}_2F_1 \left( \frac{ie-2ics+icv}{d}, -\beta; \frac{d+ie-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) + \frac{1}{-ie-2ics+icv} \left( \left( e^{(-ie-2ics+icv)z} {}_2F_1 \left( \frac{-ie-2ics+icv}{d}, -\beta; \frac{d-ie-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) - e^{(ie+2ics-icv)z} {}_2F_1 \left( \frac{ie+2ics-icv}{d}, -\beta; \frac{d+ie+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \sin\left(\frac{v\pi}{2}\right) \right) \right)$$

$$\frac{2^{-v-1} (a + b e^{dz})^\beta}{e} \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \binom{v}{\frac{v}{2}} \left( e^{ie z} {}_2F_1 \left( \frac{ie}{d}, -\beta; \frac{d+ie}{d}; -\frac{b e^{dz}}{a} \right) + e^{-ie z} {}_2F_1 \left( -\frac{ie}{d}, -\beta; \frac{d-ie}{d}; -\frac{b e^{dz}}{a} \right) \right)$$

$(1 - v \bmod 2) / ; v \in \mathbb{N}^+$

### Involving $e^{pz}(a + b e^{dz})^\beta \sin(ez) \sin^v(cz)$

01.06.21.1403.01

$$\begin{aligned}
 & \int e^{pz} (a + b e^{dz})^\beta \sin(ez) \sin^v(cz) dz = \\
 & 2^{-v-1} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( i \cos\left(\frac{\pi v}{2}\right) \left( e^{(-ie+p-2ics+icv)z} (-ie-p-2ics+icv) \right. \right. \\
 & \quad \left. \left. {}_2F_1\left(\frac{-ie+p-2ics+icv}{d}, -\beta; \frac{d-ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) + e^{(ie+p+2ics-icv)z} \right. \right. \\
 & \quad \left. \left. (-ie+p-2ics+icv) {}_2F_1\left(\frac{ie+p+2ics-icv}{d}, -\beta; \frac{d+ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) \right) / \\
 & \quad \left( (-ie-p-2ics+icv)(-ie+p-2ics+icv) + i \cos\left(\frac{\pi v}{2}\right) \left( e^{(ie+p-2ics+icv)z} (-ie+p+2ics-icv) \right. \right. \\
 & \quad \left. \left. {}_2F_1\left(\frac{ie+p-2ics+icv}{d}, -\beta; \frac{d+ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) + e^{(-ie+p+2ics-icv)z} \right. \right. \\
 & \quad \left. \left. (-ie-p+2ics-icv) {}_2F_1\left(\frac{-ie+p+2ics-icv}{d}, -\beta; \frac{d-ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) \right) / \\
 & \quad \left( (-ie-p+2ics-icv)(-ie+p+2ics-icv) - \sin\left(\frac{\pi v}{2}\right) \left( e^{(-ie+p+2ics-icv)z} (-ie-p+2ics-icv) \right. \right. \\
 & \quad \left. \left. {}_2F_1\left(\frac{-ie+p+2ics-icv}{d}, -\beta; \frac{d-ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) - e^{(ie+p-2ics+icv)z} \right. \right. \\
 & \quad \left. \left. (-ie+p+2ics-icv) {}_2F_1\left(\frac{ie+p-2ics+icv}{d}, -\beta; \frac{d+ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) \right) \right) / \\
 & \quad \left( (-ie-p+2ics-icv)(-ie+p+2ics-icv) + \sin\left(\frac{\pi v}{2}\right) \left( e^{(-ie+p-2ics+icv)z} (-ie-p-2ics+icv) \right. \right. \\
 & \quad \left. \left. {}_2F_1\left(\frac{-ie+p-2ics+icv}{d}, -\beta; \frac{d-ie+p-2ics+icv}{d}; -\frac{b e^{dz}}{a}\right) - e^{(ie+p+2ics-icv)z} \right. \right. \\
 & \quad \left. \left. (-ie+p-2ics+icv) {}_2F_1\left(\frac{ie+p+2ics-icv}{d}, -\beta; \frac{d+ie+p+2ics-icv}{d}; -\frac{b e^{dz}}{a}\right) \right) \right) / \\
 & \quad \left( (-ie-p-2ics+icv)(-ie+p-2ics+icv) \right) - \frac{1}{(ie-p)(ie+p)} \\
 & \left( i \left( 2^{-v-1} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \binom{v}{\frac{v}{2}} \left( e^{(-ie+p)z} (ie+p) {}_2F_1\left(\frac{-ie+p}{d}, -\beta; \frac{d-ie+p}{d}; -\frac{b e^{dz}}{a}\right) + \right. \right. \right. \\
 & \quad \left. \left. \left. e^{(ie+p)z} (ie-p) {}_2F_1\left(\frac{ie+p}{d}, -\beta; \frac{d+ie+p}{d}; -\frac{b e^{dz}}{a}\right) \right) (1-v \bmod 2) \right) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

Involving products of powers of two direct functions and exponential function

Involving  $e^{bz} \sin^\mu(cz) \sin^v(az)$

01.06.21.1404.01

$$\int e^{bz} \sin^\mu(cz) \sin^\nu(az) dz = \frac{2^{-\nu} e^{bz} (1 - e^{2icz})^{-\mu} (\nu \bmod 2 - 1) \sin^\mu(cz) \left(\frac{\nu}{2}\right) {}_2F_1\left(-\frac{ib+c\mu}{2c}, -\mu; \frac{1}{2}\left(2 - \frac{ib}{c} - \mu\right); e^{2icz}\right) + 2^{-\nu} i^{-\nu} (1 - e^{2icz})^{-\mu}}{b - ic\mu} \\ + \sin^\mu(cz) \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{i\pi\nu+(b-ia(v-2k))z}}{b+i(2ak-av-c\mu)} {}_2F_1\left(-\frac{ib-2ak+av+c\mu}{2c}, -\mu; -\frac{ib+a(v-2k)+c(\mu-2)}{2c}; e^{2icz}\right) + \frac{e^{(b+ai(v-2k))z}}{b-i(2ak-av+c\mu)} {}_2F_1\left(-\frac{ib+2ak-av+c\mu}{2c}, -\mu; -\frac{\mu c-2c+ib+2ak-av}{2c}; e^{2icz}\right) \right); \nu \in \mathbb{N}^+$$

01.06.21.1405.01

$$\int e^{bz} \sin^m(cz) \sin^\nu(az) dz = \frac{2^{-m-\nu} e^{bz} (1 - m \bmod 2)(1 - \nu \bmod 2) \binom{m}{\frac{m}{2}} \binom{\nu}{\frac{\nu}{2}}}{b} + 2^{-m-\nu} \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( \frac{e^{\frac{i\pi m}{2}+(b+2ick-icm)z}}{b+2ick-icm} + \frac{e^{(b-2ick+icm)z-\frac{i\pi m}{2}}}{b-2ick+icm} \right) + 2^{-m-\nu} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( \frac{e^{\frac{i\pi\nu}{2}+(b+2iak-ia\nu)z}}{b+2iak-ia\nu} + \frac{e^{(b-2iak+ia\nu)z-\frac{i\pi\nu}{2}}}{b-2iak+ia\nu} \right) + 2^{-m-\nu} i^{-m-\nu} e^{bz} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s e^{(2ick-icm+2ias-ia\nu)z} \binom{\nu}{s} \left( -\frac{e^{i\pi(m+\nu)}}{-b+ci(m-2k)-2ias+ia\nu} + \frac{e^{2i(c(m-2k)+a(v-2s))z}}{b+ci(m-2k)-2ias+ia\nu} + \frac{e^{i\pi\nu+2ci(m-2k)z}}{b+ci(m-2k)+2ias-ia\nu} + \frac{e^{im\pi-2ia(2s-\nu)z}}{b+2ick-icm-2ias+ia\nu} \right); m \in \mathbb{N}^+ \wedge \nu \in \mathbb{N}^+$$

### Involving $e^{pz} \sin^m(cz) \sin^\nu(az + b)$

01.06.21.1406.01

$$\int e^{pz} \sin^\mu(cz) \sin^\nu(az + b) dz = \frac{2^{-\nu} e^{pz} (1 - \nu \bmod 2) \sin^\mu(cz)}{p - ic\mu} (1 - e^{2icz})^{-\mu} \left(\frac{\nu}{2}\right) {}_2F_1\left(-\frac{ip+c\mu}{2c}, -\mu; \frac{1}{2}\left(-\frac{ip}{c} - \mu + 2\right); e^{2icz}\right) + i^{1-\nu} 2^{-\nu} (1 - e^{2icz})^{-\mu} \sin^\mu(cz) \\ + \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k e^{ib(v-2k)} \binom{\nu}{k} \left( \frac{e^{(p+ai(v-2k))z}}{2ak+ip-av+c\mu} {}_2F_1\left(-\frac{2ak+ip-av+c\mu}{2c}, -\mu; -\frac{2ak+ip-av+c(\mu-2)}{2c}; e^{2icz}\right) + \frac{e^{i\pi\nu-2ib(v-2k)+(p-ia(v-2k))z}}{ip+a(v-2k)+c\mu} {}_2F_1\left(-\frac{ip+a(v-2k)+c\mu}{2c}, -\mu; -\frac{-2ak+ip+av+c(\mu-2)}{2c}; e^{2icz}\right) \right); \nu \in \mathbb{N}^+$$



01.06.21.1407.01

$$\int e^{pz} \sin^m(cz) \sin^v(b+az) dz =$$

$$\frac{2^{-m} e^{pz}}{p-ia v} (1 - e^{2i(b+az)})^{-v} \left(\frac{m}{2}\right) {}_2F_1\left(-\frac{ip+av}{2a}, -v; \frac{1}{2}\left(-\frac{ip}{a} - v + 2\right); e^{2i(b+az)}\right) (1 - m \bmod 2) \sin^v(b+az) +$$

$$i^{1-m} 2^{-m} (1 - e^{2i(b+az)})^{-v} \sin^v(b+az)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( \frac{e^{c(i(m-2k)+p)z}}{2ck - cm + ip + av} {}_2F_1\left(-\frac{2ck - cm + ip + av}{2a}, -v; -\frac{2ck - cm + ip + a(v-2)}{2a}; e^{2i(b+az)}\right) + \right.$$

$$\left. \frac{e^{i\pi m + (p-ic(m-2k))z}}{c(m-2k) + ip + av} {}_2F_1\left(-\frac{c(m-2k) + ip + av}{2a}, -v; -\frac{-2ck + cm + ip + a(v-2)}{2a}; e^{2i(b+az)}\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1408.01

$$\int e^{pz} \sin^m(cz) \sin^v(b+az) dz =$$

$$e^{pz} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{i(c(2k-m)z + (2s-v)(b+az))} \left( \frac{i e^{i(m\pi - 2(2s-v)(b+az))}}{c(m-2k) + ip + 2as - av} + \frac{e^{-2i(2bs + 2azs - bv + 2ckz - cmz - avz)}}{ci(m-2k) + p - 2ias + iav} \right. \right.$$

$$\left. \left. + \frac{i e^{i(\pi v + 2c(m-2k)z)}}{2ck - cm + ip - 2as + av} + \frac{i e^{i\pi(m+v)}}{c(m-2k) + ip + a(v-2s)} \right) \binom{v}{s} \right)$$

$$(2i)^{-m-v} + \frac{2^{-m-v} e^{pz} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)}{p} + 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \left( \frac{e^{-\frac{1}{2}i(-2czm + \pi m + 4ckz + 2ipz)}}{-2cik + icm + p} + \frac{e^{\frac{1}{2}i(-2czm + \pi m + 4ckz - 2ipz)}}{ci(2k-m) + p} \right) \binom{m}{k} +$$

$$2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \left( \frac{e^{-\frac{1}{2}i(4bk + 4azk - 2bv + \pi v + 2ipz - 2avz)}}{-2aik + p + iav} + \frac{e^{\frac{1}{2}i(4bk + 4azk - 2bv + \pi v - 2ipz - 2avz)}}{p + ai(2k-v)} \right) \binom{v}{k} /; m \in$$

$$\mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $e^{pz} \sin^\mu(cz + d) \sin^v(az + b)$**

01.06.21.1409.01

$$\int e^{pz} \sin^\mu(d+cz) \sin^v(b+az) dz =$$

$$\frac{1}{p-ic\mu} \left( 2^{-v} e^{pz} (1-e^{2i(d+cz)})^{-\mu} \binom{v}{\frac{v}{2}} {}_2F_1\left(-\frac{ip+c\mu}{2c}, -\mu; \frac{1}{2}\left(-\frac{ip}{c}-\mu+2\right); e^{2i(d+cz)}\right) (1-v \bmod 2) \sin^\mu(d+cz) \right) +$$

$$2^{-v} i^{1-v} (1-e^{2i(d+cz)})^{-\mu} \sin^\mu(d+cz) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{ib(v-2k)} \binom{v}{k} \left( \frac{e^{(p+ai(v-2k))z}}{2ak+ip-av+c\mu} \right.$$

$$\left. {}_2F_1\left(-\frac{2ak+ip-av+c\mu}{2c}, -\mu; -\frac{2ak+ip-av+c(\mu-2)}{2c}; e^{2i(d+cz)}\right) + \frac{e^{i\pi v-2ib(v-2k)+(p-ia(v-2k))z}}{ip+a(v-2k)+c\mu} \right.$$

$$\left. {}_2F_1\left(-\frac{ip+a(v-2k)+c\mu}{2c}, -\mu; -\frac{-2ak+ip+av+c(\mu-2)}{2c}; e^{2i(d+cz)}\right) \right) /; v \in \mathbb{N}^+$$

01.06.21.1410.01

$$\int e^{pz} \sin^m(d+cz) \sin^v(b+az) dz = \frac{2^{-m-v} e^{pz} (1-m \bmod 2) (1-v \bmod 2)}{p} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} +$$

$$2^{-m-v} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( \frac{e^{-\frac{1}{2}i(4dk+4czk-2dm-2cmz+2ipz+m\pi)}}{-2cik+icm+p} + \frac{e^{\frac{1}{2}i(4dk+4czk-2dm-2cmz-2ipz+m\pi)}}{ci(2k-m)+p} \right) +$$

$$2^{-m-v} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{-\frac{1}{2}i(4bk+4azk-2bv+\pi v+2ipz-2avz)}}{-2aik+p+ia v} + \frac{e^{\frac{1}{2}i(4bk+4azk-2bv+\pi v-2ipz-2avz)}}{p+ai(2k-v)} \right) +$$

$$2^{-m-v} i^{-m-v} e^{pz} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} e^{i((2s-v)(b+az)+(2k-m)(d+cz))} \left( \frac{i e^{i(m\pi-2(2s-v)(b+az))}}{c(m-2k)+ip+2as-av} + \frac{e^{-2i(2dk+2czk-dm+2bs-bv-cmz+2asz-avz)}}{ci(m-2k)+p-2ias+ia v} + \right.$$

$$\left. \frac{i e^{i(2d(m-2k)+2cz(m-2k)+\pi v)}}{2ck-cm+ip-2as+av} + \frac{i e^{i\pi(m+v)}}{c(m-2k)+ip+a(v-2s)} \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $e^{pz} \sin^m(bz) \sin^v(cz)$

01.06.21.1411.01

$$\int e^{pz^2} \sin^m(bz) \sin^v(cz) dz =$$

$$\frac{2^{-m-v-1} \sqrt{\pi} (1-m \bmod 2)(1-v \bmod 2)}{\sqrt{p}} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{p} z) + \frac{2^{-m-v-1} \sqrt{\pi}}{\sqrt{p}} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s}$$

$$\left( e^{-\frac{-b^2(m-2s)^2-2\pi i m p}{4p}} \operatorname{erfi}\left(\frac{2pz - ib(m-2s)}{2\sqrt{p}}\right) + e^{-\frac{2\pi i m p - b^2(m-2s)^2}{4p}} \operatorname{erfi}\left(\frac{bi(m-2s) + 2pz}{2\sqrt{p}}\right) \right) + \frac{2^{-m-v-1} \sqrt{\pi}}{\sqrt{p}} \binom{m}{\frac{m}{2}}$$

$$(1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-\frac{-c^2(v-2k)^2-2\pi i p v}{4p}} \operatorname{erfi}\left(\frac{2pz - ic(v-2k)}{2\sqrt{p}}\right) + e^{-\frac{2\pi i p v - c^2(v-2k)^2}{4p}} \operatorname{erfi}\left(\frac{ci(v-2k) + 2pz}{2\sqrt{p}}\right) \right) +$$

$$\frac{2^{-m-v-1} \sqrt{\pi}}{\sqrt{p}} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{-\frac{(bi(m-2s)+ci(2k-v))^2-2i p \pi(v-m)}{4p}} \operatorname{erfi}\left(\frac{bi(m-2s) + ci(2k-v) + 2pz}{2\sqrt{p}}\right) +$$

$$e^{-\frac{(-ib(m-2s)-ic(2k-v))^2+2i p \pi(v-m)}{4p}} \operatorname{erfi}\left(\frac{-ib(m-2s) - ic(2k-v) + 2pz}{2\sqrt{p}}\right) +$$

$$e^{-\frac{(bi(m-2s)+ci(v-2k))^2+2i p \pi(m+v)}{4p}} \operatorname{erfi}\left(\frac{bi(m-2s) + ci(v-2k) + 2pz}{2\sqrt{p}}\right) +$$

$$e^{-\frac{(-ib(m-2s)-ic(v-2k))^2-2i p \pi(m+v)}{4p}} \operatorname{erfi}\left(\frac{-ib(m-2s) - ic(v-2k) + 2pz}{2\sqrt{p}}\right) \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1412.01

$$\int e^{p\sqrt{z}} \sin^m(bz) \sin^v(cz) dz =$$

$$2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s e^{\frac{im\pi}{2}} \binom{m}{s} \left( \frac{2i e^{p\sqrt{z} - ib(m-2s)z}}{b(m-2s)} - \frac{2i e^{-i\pi m + bi(m-2s)z + p\sqrt{z}}}{b(m-2s)} -$$

$$\frac{e^{-\frac{ip^2}{4b(m-2s)}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p-2ib(m-2s)\sqrt{z}}{2\sqrt{-ib(m-2s)}}\right)}{(-ib(m-2s))^{3/2}} - \frac{e^{\frac{ip^2}{4b(m-2s)} - im\pi} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2bi(m-2s)\sqrt{z}}{2\sqrt{ib(m-2s)}}\right)}{(ib(m-2s))^{3/2}} \right) +$$

$$\frac{2^{-m-v+1} e^{p\sqrt{z}} (p\sqrt{z} - 1) (1-m \bmod 2)(1-v \bmod 2)}{p^2} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} + 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{\frac{i\pi v}{2}} \binom{v}{k} \left( \frac{2i e^{p\sqrt{z} - ic(v-2k)z}}{c(v-2k)} - \frac{2i e^{\sqrt{z} p - i\pi v + ci(v-2k)z}}{c(v-2k)} -$$

$$\begin{aligned}
 & \left. \frac{e^{-\frac{ip^2}{4c(v-2k)}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p-2ic(v-2k)\sqrt{z}}{2\sqrt{-ic(v-2k)}}\right) - \frac{e^{\frac{ip^2}{4c(v-2k)}-i\pi v} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2ci(v-2k)\sqrt{z}}{2\sqrt{ic(v-2k)}}\right)}{(-ic(v-2k))^{3/2} - (ic(v-2k))^{3/2}} \right\} + \\
 & 2^{-m-v-1} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{-\frac{1}{2}i\pi(v-m)} \left( \frac{2e^{\sqrt{z} p+i\pi(v-m)+(bi(m-2s)+ci(2k-v))z}}{bi(m-2s)+ci(2k-v)} - \right. \right. \\
 & \left. \left. \left( e^{i\pi(v-m)-\frac{p^2}{4(bi(m-2s)+ci(2k-v))}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2(bi(m-2s)+ci(2k-v))\sqrt{z}}{2\sqrt{bi(m-2s)+ci(2k-v)}}\right) \right) \right) / \\
 & (bi(m-2s)+ci(2k-v))^{3/2} + \frac{2e^{\sqrt{z} p+(-ib(m-2s)-ic(2k-v))z}}{-ib(m-2s)-ic(2k-v)} - \left( e^{-\frac{p^2}{4(-ib(m-2s)-ic(2k-v))}} p \sqrt{\pi} \right. \\
 & \left. \operatorname{erfi}\left(\frac{p+2(-ib(m-2s)-ic(2k-v))\sqrt{z}}{2\sqrt{-ib(m-2s)-ic(2k-v)}}\right) \right) / (-ib(m-2s)-ic(2k-v))^{3/2} \Bigg) + \\
 & e^{\frac{1}{2}i\pi(m+v)} \left( \frac{2e^{\sqrt{z} p-i\pi(m+v)+(bi(m-2s)+ci(v-2k))z}}{bi(m-2s)+ci(v-2k)} - \left( e^{-\frac{p^2}{4(bi(m-2s)+ci(v-2k))}-i\pi(m+v)}} p \sqrt{\pi} \right. \right. \\
 & \left. \left. \operatorname{erfi}\left(\frac{p+2(bi(m-2s)+ci(v-2k))\sqrt{z}}{2\sqrt{bi(m-2s)+ci(v-2k)}}\right) \right) \right) / \\
 & (bi(m-2s)+ci(v-2k))^{3/2} + \frac{2e^{\sqrt{z} p+(-ib(m-2s)-ic(v-2k))z}}{-ib(m-2s)-ic(v-2k)} - \\
 & \left( e^{-\frac{p^2}{4(-ib(m-2s)-ic(v-2k))}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2(-ib(m-2s)-ic(v-2k))\sqrt{z}}{2\sqrt{-ib(m-2s)-ic(v-2k)}}\right) \right) / \\
 & (-ib(m-2s)-ic(v-2k))^{3/2} \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $e^{pz} \sin^m(bz^r) \sin^v(cz)$

01.06.21.1413.01

$$\int e^{pz} \sin^m(bz^2) \sin^v(cz) dz = \frac{2^{-m-v} e^{pz} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{p} +$$

$$2^{-m-v+1} e^{pz} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \left( (-1)^k \binom{v}{k} \left( \cos(c(v-2k)z) \left( p \cos\left(\frac{\pi v}{2}\right) + c(2k-v) \sin\left(\frac{\pi v}{2}\right) \right) - \right. \right.$$

$$\left. \left. \left( c(2k-v) \cos\left(\frac{\pi v}{2}\right) - p \sin\left(\frac{\pi v}{2}\right) \right) \sin(c(v-2k)z) \right) \right) / ((2ick + p - icv)(p + ci(v-2k))) + \frac{1}{b}$$

$$\left( i 2^{-m-v-1} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{m-2s} \left( (-1)^s \binom{m}{s} \left( e^{-\frac{i(p^2-2bm\pi(m-2s))}{4b(m-2s)}} \sqrt{-ib(m-2s)} \operatorname{erfi}\left(\frac{p-2ib(m-2s)z}{2\sqrt{-ib(m-2s)}}\right) - \right. \right. \right.$$

$$\left. \left. \left. e^{\frac{i(p^2-2bm\pi(m-2s))}{4b(m-2s)}} \sqrt{ib(m-2s)} \operatorname{erfi}\left(\frac{p+2bi(m-2s)z}{2\sqrt{ib(m-2s)}}\right) \right) \right) \right) + \frac{1}{b} \left( i 2^{-m-v-1} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \right.$$

$$\left. \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{m-2s} \left( (-1)^{k+s} \binom{v}{k} \left( e^{-\frac{i((p-ic(2k-v))^2+2b\pi(m-2s)(v-m))}{4b(m-2s)}} \sqrt{-ib(m-2s)} \operatorname{erfi}\left(\frac{p-ic(2k-v)-2ib(m-2s)z}{2\sqrt{-ib(m-2s)}}\right) + \right. \right. \right.$$

$$\left. \left. \left. e^{-\frac{i((p-ic(v-2k))^2-2b\pi(m-2s)(m+v))}{4b(m-2s)}} \sqrt{-ib(m-2s)} \operatorname{erfi}\left(\frac{p-ic(v-2k)-2ib(m-2s)z}{2\sqrt{-ib(m-2s)}}\right) - \right. \right. \right.$$

$$\left. \left. \left. e^{\frac{i((p+ci(2k-v))^2+2b\pi(m-2s)(v-m))}{4b(m-2s)}} \sqrt{ib(m-2s)} \operatorname{erfi}\left(\frac{p+ci(2k-v)+2bi(m-2s)z}{2\sqrt{ib(m-2s)}}\right) - \right. \right. \right.$$

$$\left. \left. \left. e^{\frac{i((p+ci(v-2k))^2-2b\pi(m-2s)(m+v))}{4b(m-2s)}} \sqrt{ib(m-2s)} \operatorname{erfi}\left(\frac{p+ci(v-2k)+2bi(m-2s)z}{2\sqrt{ib(m-2s)}}\right) \right) \right) \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1414.01

$$\begin{aligned}
 \int e^{pz} \sin^m(b\sqrt{z}) \sin^v(cz) dz = & \frac{(-1)^m 2^{-m-v} e^{pz} (1-m \bmod 2) (1-v \bmod 2)}{p} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} + \\
 & (-1)^m i^v 2^{-m-v} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{e^{(p-ic(v-2k))z}}{p-ic(v-2k)} + \frac{e^{(p+ci(v-2k))z-i\pi v}}{p+ci(v-2k)} \right) + \\
 & i^{-m} 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s} \left( \frac{i b e^{\frac{b^2(m-2s)^2}{4p}-im\pi} \sqrt{\pi} (m-2s) \operatorname{erfi}\left(\frac{2p\sqrt{z}-ib(m-2s)}{2\sqrt{p}}\right)}{p^{3/2}} + \right. \\
 & \left. \frac{i b e^{\frac{b^2(m-2s)^2}{4p}} \sqrt{\pi} (m-2s) \operatorname{erfi}\left(\frac{-2\sqrt{z}p-ib(m-2s)}{2\sqrt{p}}\right)}{p^{3/2}} + \frac{2 e^{bi\sqrt{z}(m-2s)+pz}}{p} + \frac{2 e^{-i\pi m+pz-ib(m-2s)\sqrt{z}}}{p} \right) + \\
 & (-1)^m 2^{-m-v-1} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{-\frac{1}{2}i\pi(v-m)} \left( \left( i b e^{\frac{b^2(m-2s)^2}{4(p+ci(2k-v))+i\pi(v-m)}} \sqrt{\pi} (m-2s) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{erfi}\left(\frac{2(p+ci(2k-v)\sqrt{z}-ib(m-2s))}{2\sqrt{p+ci(2k-v)}}\right) \right) \right) / (p+ci(2k-v))^{3/2} + \right. \\
 & \left. \left( i b e^{\frac{b^2(m-2s)^2}{4(p-ic(2k-v))}} \sqrt{\pi} (m-2s) \operatorname{erfi}\left(\frac{2(ic(2k-v)-p)\sqrt{z}-ib(m-2s)}{2\sqrt{p-ic(2k-v)}}\right) \right) \right) / (p-ic(2k-v))^{3/2} + \\
 & \left. \frac{2 e^{-ib\sqrt{z}(m-2s)+i\pi(v-m)+(p+ci(2k-v))z}}{p+ci(2k-v)} + \frac{2 e^{bi\sqrt{z}(m-2s)+(p-ic(2k-v))z}}{p-ic(2k-v)} \right) + e^{\frac{1}{2}i\pi(m+v)} \\
 & \left( \left( i b e^{\frac{b^2(m-2s)^2}{4(p+ci(v-2k))-i\pi(m+v)}} \sqrt{\pi} (m-2s) \operatorname{erfi}\left(\frac{2(p+ci(v-2k)\sqrt{z}-ib(m-2s))}{2\sqrt{p+ci(v-2k)}}\right) \right) \right) / (p+ci(v-2k))^{3/2} + \\
 & \left( i b e^{\frac{b^2(m-2s)^2}{4(p-ic(v-2k))}} \sqrt{\pi} (m-2s) \operatorname{erfi}\left(\frac{2(ic(v-2k)-p)\sqrt{z}-ib(m-2s)}{2\sqrt{p-ic(v-2k)}}\right) \right) \right) / (p-ic(v-2k))^{3/2} + \\
 & \left. \frac{2 e^{-ib\sqrt{z}(m-2s)-i\pi(m+v)+(p+ci(v-2k))z}}{p+ci(v-2k)} + \frac{2 e^{bi\sqrt{z}(m-2s)+(p-ic(v-2k))z}}{p-ic(v-2k)} \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $e^{pz} \sin^m(bz) \sin^v(cz)$

01.06.21.1415.01

$$\int e^{p z^2} \sin^m(b z^2) \sin^v(c z) dz = 2^{-m-v-1} \sqrt{\pi} \left(\frac{v}{2}\right) (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{i m \pi}{2}} \sqrt{p-i b(m-2 k)} (b i(m-2 k)+p) \operatorname{erfi}\left(\frac{2 p z-2 i b(m-2 k) z}{2 \sqrt{p-i b(m-2 k)}}\right) + e^{-\frac{i}{2} m \pi} (p-i b(m-2 k)) \right.$$

$$\left. \sqrt{b i(m-2 k)+p} \operatorname{erfi}\left(\sqrt{b i(m-2 k)+p} z\right) \right) / ((p-i b(m-2 k))(b i(m-2 k)+p)) +$$

$$\frac{2^{-m-v-1} \sqrt{\pi} (1-m \bmod 2)(1-v \bmod 2)}{\sqrt{p}} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\sqrt{p} z\right) + \frac{2^{-m-v-1} \sqrt{\pi}}{\sqrt{p}} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{-c^2(v-2 s)^2-2 \pi i p v}{4 p}} \operatorname{erfi}\left(\frac{2 p z-i c(v-2 s)}{2 \sqrt{p}}\right) + e^{-\frac{2 \pi i p v-c^2(v-2 s)^2}{4 p}} \operatorname{erfi}\left(\frac{c i(v-2 s)+2 p z}{2 \sqrt{p}}\right) \right) +$$

$$2^{-m-v-1} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \binom{v}{s} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+s} \binom{m}{k} \left( \left( e^{-\frac{2 i(p-i b(2 k-m)) \pi(m-v)-c^2(v-2 s)^2}{4(p-i b(2 k-m))}} \sqrt{p-i b(2 k-m)} (b i(2 k-m)+p) \right. \right.$$

$$\left. \left. \operatorname{erfi}\left(\frac{-i c(v-2 s)-2 i b(2 k-m) z+2 p z}{2 \sqrt{p-i b(2 k-m)}}\right) + e^{-\frac{-c^2(v-2 s)^2-2 i(b i(2 k-m)+p) \pi(m-v)}{4(b i(2 k-m)+p)}} \right. \right.$$

$$\left. \left. (p-i b(2 k-m)) \sqrt{b i(2 k-m)+p} \operatorname{erfi}\left(\frac{c i(v-2 s)+2(b i(2 k-m)+p) z}{2 \sqrt{b i(2 k-m)+p}}\right) \right) \right) /$$

$$((p-i b(2 k-m))(b i(2 k-m)+p)) + \left( e^{-\frac{-c^2(v-2 s)^2-2 i(p-i b(m-2 k)) \pi(m+v)}{4(p-i b(m-2 k))}} \sqrt{p-i b(m-2 k)} \right.$$

$$(b i(m-2 k)+p) \operatorname{erfi}\left(\frac{-i c(v-2 s)-2 i b(m-2 k) z+2 p z}{2 \sqrt{p-i b(m-2 k)}}\right) + e^{-\frac{2 i(b i(m-2 k)+p) \pi(m+v)-c^2(v-2 s)^2}{4(b i(m-2 k)+p)}}$$

$$(p-i b(m-2 k)) \sqrt{b i(m-2 k)+p} \operatorname{erfi}\left(\frac{c i(v-2 s)+2(b i(m-2 k)+p) z}{2 \sqrt{b i(m-2 k)+p}}\right) \right) /$$

$$((p-i b(m-2 k))(b i(m-2 k)+p)) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1416.01

$$\int e^{p \sqrt{z}} \sin^m(b \sqrt{z}) \sin^v(c z) dz =$$

$$\frac{2^{-m-v+1} e^{p \sqrt{z}} (p \sqrt{z}-1)(1-m \bmod 2)(1-v \bmod 2)}{p^2} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} + i^m 2^{-m-v+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s}$$

$$\begin{aligned}
 & e^{(p-i b(m-2 s)) \sqrt{z}} \left( \frac{e^{2(i b(m-2 s) \sqrt{z}-\frac{i m \pi}{2})}(\sqrt{z} p+b i(m-2 s) \sqrt{z}-1)}{(p+b i(m-2 s))^2} + \frac{\sqrt{z}}{p-i b(m-2 s)} - \frac{1}{(i b(m-2 s)-p)^2} \right) + \\
 & i^v 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{2 i e^{p \sqrt{z}-i c(v-2 k) z}}{c(v-2 k)} - \frac{2 i e^{\sqrt{z} p-i \pi v+c i(v-2 k) z}}{c(v-2 k)} - \right. \\
 & \left. \frac{e^{-\frac{i p^2}{4 c(v-2 k)}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p-2 i c(v-2 k) \sqrt{z}}{2 \sqrt{-i c(v-2 k)}}\right)}{(-i c(v-2 k))^{3 / 2}} - \frac{e^{\frac{i p^2}{4 c(v-2 k)}-i \pi v} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+2 c i(v-2 k) \sqrt{z}}{2 \sqrt{i c(v-2 k)}}\right)}{(i c(v-2 k))^{3 / 2}} \right) + \\
 & 2^{-m-v-1} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{-\frac{1}{2} i \pi(v-m)} \left( \frac{2 i e^{(p-i b(m-2 s)) \sqrt{z}-i c(2 k-v) z}}{c(2 k-v)} - \frac{2 i e^{\sqrt{z}(p+b i(m-2 s))+i \pi(v-m)+c i(2 k-v) z}}{c(2 k-v)} - \right. \right. \\
 & \left. \frac{e^{-\frac{i(p-i b(m-2 s))^2}{4 c(2 k-v)}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p-i b(m-2 s)-2 i c(2 k-v) \sqrt{z}}{2 \sqrt{-i c(2 k-v)}}\right)}{(-i c(2 k-v))^{3 / 2}} - \right. \\
 & \left. \left( i b e^{-\frac{i(p-i b(m-2 s))^2}{4 c(2 k-v)}} \sqrt{\pi}(m-2 s) \operatorname{erfi}\left(\frac{-p+b i(m-2 s)+2 c i(2 k-v) \sqrt{z}}{2 \sqrt{-i c(2 k-v)}}\right) \right) /(-i c(2 k-v))^{3 / 2} - \right. \\
 & \left. \frac{e^{\frac{i(p+b i(m-2 s))^2}{4 c(2 k-v)}+i \pi(v-m)} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+b i(m-2 s)+2 c i(2 k-v) \sqrt{z}}{2 \sqrt{i c(2 k-v)}}\right)}{(i c(2 k-v))^{3 / 2}} - \right. \\
 & \left. \left. \frac{1}{(i c(2 k-v))^{3 / 2}} \left( i b e^{\frac{i(p+b i(m-2 s))^2}{4 c(2 k-v)}+i \pi(v-m)} \sqrt{\pi}(m-2 s) \operatorname{erfi}\left(\frac{p+b i(m-2 s)+2 c i(2 k-v) \sqrt{z}}{2 \sqrt{i c(2 k-v)}}\right) \right) \right) \right) + \\
 & e^{\frac{1}{2} i \pi(m+v)} \left( \frac{2 i e^{(p-i b(m-2 s)) \sqrt{z}-i c(v-2 k) z}}{c(v-2 k)} - \frac{2 i e^{\sqrt{z}(p+b i(m-2 s))-i \pi(m+v)+c i(v-2 k) z}}{c(v-2 k)} - \right. \\
 & \left. \frac{e^{-\frac{i(p-i b(m-2 s))^2}{4 c(v-2 k)}} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p-i b(m-2 s)-2 i c(v-2 k) \sqrt{z}}{2 \sqrt{-i c(v-2 k)}}\right)}{(-i c(v-2 k))^{3 / 2}} \right)
 \end{aligned}$$



$$\left( i b e^{-\frac{i(p-i b(m-2 s))^2}{4 c(v-2 k)}} \sqrt{\pi} (m-2 s) \operatorname{erfi}\left(\frac{-p+b i(m-2 s)+2 c i(v-2 k) \sqrt{z}}{2 \sqrt{-i c(v-2 k)}}\right) \right) / (-i c(v-2 k))^{3/2} -$$

$$\frac{e^{\frac{i(p+b i(m-2 s))^2}{4 c(v-2 k)}-i \pi(m+v)} p \sqrt{\pi} \operatorname{erfi}\left(\frac{p+b i(m-2 s)+2 c i(v-2 k) \sqrt{z}}{2 \sqrt{i c(v-2 k)}}\right)}{(i c(v-2 k))^{3/2}} - \frac{1}{(i c(v-2 k))^{3/2}} \left( i b e^{\frac{i(p+b i(m-2 s))^2}{4 c(v-2 k)}-i \pi(m+v)} \right.$$

$$\left. \left. \left. \sqrt{\pi} (m-2 s) \operatorname{erfi}\left(\frac{p+b i(m-2 s)+2 c i(v-2 k) \sqrt{z}}{2 \sqrt{i c(v-2 k)}}\right) \right) \right) \right) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $e^{p z} \sin^m(b z^r) \sin^v(c z^r)$

01.06.21.1417.01

$$\int e^{pz} \sin^m(bz^2) \sin^v(cz^2) dz = \frac{2^{-m-v} e^{pz} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{p} +$$

$$\frac{1}{b} \left( i 2^{-m-v-1} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{m-2s} \left( (-1)^s \binom{m}{s} \left( e^{-\frac{i(p^2-2b\pi(m-2s))}{4b(m-2s)}} \sqrt{-ib(m-2s)} \operatorname{erfi} \left( \frac{p-2ib(m-2s)z}{2\sqrt{-ib(m-2s)}} \right) - e^{\frac{i(p^2-2b\pi(m-2s))}{4b(m-2s)}} \sqrt{ib(m-2s)} \operatorname{erfi} \left( \frac{p+2bi(m-2s)z}{2\sqrt{ib(m-2s)}} \right) \right) \right) \right) +$$

$$\frac{1}{c} \left( i 2^{-m-v-1} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{v-2k} \left( (-1)^k \binom{v}{k} \left( e^{-\frac{i(p^2-2c\pi v(v-2k))}{4c(v-2k)}} \sqrt{-ic(v-2k)} \operatorname{erfi} \left( \frac{p-2ic(v-2k)z}{2\sqrt{-ic(v-2k)}} \right) - e^{\frac{i(p^2-2c\pi v(v-2k))}{4c(v-2k)}} \sqrt{ic(v-2k)} \operatorname{erfi} \left( \frac{p+2ci(v-2k)z}{2\sqrt{ic(v-2k)}} \right) \right) \right) \right) + 2^{-m-v-1} \sqrt{\pi}$$

$$\sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( \frac{1}{bi(m-2s) + ci(2k-v)} \left( e^{-\frac{p^2-2i\pi(bi(m-2s)+ci(2k-v))(v-m)}{4(bi(m-2s)+ci(2k-v))}} \sqrt{bi(m-2s) + ci(2k-v)} \operatorname{erfi} \left( \frac{p+2(bi(m-2s) + ci(2k-v))z}{2\sqrt{bi(m-2s) + ci(2k-v)}} \right) - e^{-\frac{p^2+2i\pi(-ib(m-2s)-ic(2k-v))(v-m)}{4(-ib(m-2s)-ic(2k-v))}} \sqrt{-ib(m-2s) - ic(2k-v)} \operatorname{erfi} \left( \frac{p-2(bi(m-2s) + ci(2k-v))z}{2\sqrt{-ib(m-2s) - ic(2k-v)}} \right) \right) + \frac{1}{bi(m-2s) + ci(v-2k)} \left( e^{-\frac{p^2+2i\pi(m+v)(bi(m-2s)+ci(v-2k))}{4(bi(m-2s)+ci(v-2k))}} \sqrt{bi(m-2s) + ci(v-2k)} \operatorname{erfi} \left( \frac{p+2(bi(m-2s) + ci(v-2k))z}{2\sqrt{bi(m-2s) + ci(v-2k)}} \right) - e^{-\frac{p^2-2i\pi(m+v)(-ib(m-2s)-ic(v-2k))}{4(-ib(m-2s)-ic(v-2k))}} \sqrt{-ib(m-2s) - ic(v-2k)} \operatorname{erfi} \left( \frac{p-2(bi(m-2s) + ci(v-2k))z}{2\sqrt{-ib(m-2s) - ic(v-2k)}} \right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1418.01

$$\int e^{pz} \sin^m(b\sqrt{z}) \sin^v(c\sqrt{z}) dz = 2^{-m-v-1} \binom{v}{\frac{v}{2}}$$

$$\left( \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s e^{\frac{im\pi}{2}} \binom{m}{s} \left( \frac{4 e^{pz - \frac{im\pi}{2}} \cos\left(\frac{m\pi}{2} - b(m-2s)\sqrt{z}\right)}{p} + \frac{b e^{-\frac{(2ib s - ib m)^2}{4p}} i \sqrt{\pi} (m-2s) \operatorname{erfi} \left( \frac{2p\sqrt{z} - ib(m-2s)}{2\sqrt{p}} \right)}{p^{3/2}} - \frac{ib e^{\frac{b^2(m-2s)^2}{4p} - im\pi} \sqrt{\pi} (m-2s) \operatorname{erfi} \left( \frac{2\sqrt{z} p + bi(m-2s)}{2\sqrt{p}} \right)}{p^{3/2}} \right) \right) (1-v \bmod 2) +$$

$$\begin{aligned}
 & \frac{2^{-m-v} e^{pz} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{p} + 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{\frac{i\pi v}{2}} \binom{v}{k} \left( \frac{4 e^{pz - \frac{i\pi v}{2}} \cos(c\sqrt{z} (2k-v) + \frac{\pi v}{2})}{p} - \right. \\
 & \left. \frac{e^{-\frac{(2ick-icv)^2}{4p}} \sqrt{\pi} (2ick - icv) \operatorname{erfi}\left(\frac{2\sqrt{z} p + ci(2k-v)}{2\sqrt{p}}\right)}{p^{3/2}} - \frac{ic e^{\frac{c^2(v-2k)^2}{4p} - i\pi v} \sqrt{\pi} (v-2k) \operatorname{erfi}\left(\frac{2\sqrt{z} p + ci(v-2k)}{2\sqrt{p}}\right)}{p^{3/2}} \right) + \\
 & 2^{-m-v-1} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{-\frac{1}{2} i\pi(v-m)} \left( \frac{4 e^{pz - \frac{1}{2} i\pi(m-v)} \cos\left(\frac{1}{2} \pi(v-m) + (2ck + bm - 2bs - cv)\sqrt{z}\right)}{p} + \right. \right. \\
 & \left. \frac{1}{p^{3/2}} \left( e^{\frac{(2ck+bm-2bs-cv)^2}{4p}} \sqrt{\pi} (2ck + bm - 2bs - cv) \operatorname{erf}\left(\frac{2i\sqrt{z} p + b(m-2s) + c(2k-v)}{2\sqrt{p}}\right) \right) + \frac{1}{p^{3/2}} \right. \\
 & \left. \left( e^{\frac{(-2ck-bm+2bs+cv)^2}{4p} + i\pi(v-m)} \sqrt{\pi} (2ck + bm - 2bs - cv) \operatorname{erf}\left(\frac{-2i\sqrt{z} p + b(m-2s) + c(2k-v)}{2\sqrt{p}}\right) \right) \right) + \\
 & e^{\frac{1}{2} i\pi(m+v)} \left( \frac{4 e^{pz - \frac{1}{2} i\pi(m+v)} \cos\left(\frac{1}{2} \pi(m+v) + (2ck - bm + 2bs - cv)\sqrt{z}\right)}{p} - \right. \\
 & \left. \frac{1}{p^{3/2}} \left( e^{\frac{(b(m-2s)+c(v-2k))^2}{4p}} \sqrt{\pi} (b(m-2s) + c(v-2k)) \operatorname{erf}\left(\frac{-2i\sqrt{z} p - b(m-2s) + c(2k-v)}{2\sqrt{p}}\right) \right) - \right. \\
 & \left. \frac{1}{p^{3/2}} \left( i e^{\frac{(b(m-2s)+c(v-2k))^2}{4p} - i\pi(m+v)} \sqrt{\pi} (b(m-2s) + c(v-2k)) \operatorname{erfi}\left(\frac{2\sqrt{z} p + bi(m-2s) + ci(v-2k)}{2\sqrt{p}}\right) \right) \right) \Bigg) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $e^{pz'} \sin^m(bz') \sin^v(cz')$

01.06.21.1419.01

$$\begin{aligned}
 \int e^{p z^r} \sin^m(b z^r) \sin^v(c z^r) dz = & -\frac{(-1)^m 2^{-m-v} z (-p z^r)^{-1/r} (1-m \bmod 2) (1-v \bmod 2)}{r} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma\left(\frac{1}{r}, -p z^r\right) - \\
 & \frac{2^{-m-v} i^{-m-v} z}{r} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m e^{\frac{i\pi v}{2}} \Gamma\left(\frac{1}{r}, (-2bik + ibm - p) z^r\right) ((-2bik + ibm - p) z^r)^{-1/r} + \right. \\
 & \left. e^{\frac{i\pi v}{2}} ((2ibk - ibm - p) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm - p) z^r\right) \right) - \\
 & \frac{(-1)^m i^{-v} 2^{-m-v} z}{r} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v \Gamma\left(\frac{1}{r}, (-2cik - p + icv) z^r\right) ((-2cik - p + icv) z^r)^{-1/r} + \right. \\
 & \left. ((2ick - p - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ick - p - icv) z^r\right) \right) - \frac{(-1)^m i^{-m-v} 2^{-m-v} z}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\
 & \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \Gamma\left(\frac{1}{r}, (-2bik + ibm - p - 2ics + icv) z^r\right) ((-2bik + ibm - p - 2ics + icv) z^r)^{-1/r} + \right. \\
 & (-1)^{m+v} ((2ibk - ibm - p - 2ics + icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm - p - 2ics + icv) z^r\right) + \\
 & \left. ((-2bik + ibm - p + 2ics - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-2bik + ibm - p + 2ics - icv) z^r\right) + (-1)^m \right. \\
 & \left. ((2ibk - ibm - p + 2ics - icv) z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (2ibk - ibm - p + 2ics - icv) z^r\right) \right); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1420.01

$$\int e^{p z^2} \sin^m(b z^2) \sin^v(c z^2) dz = 2^{-m-v-1} \sqrt{\pi} \left(\frac{v}{2}\right) (1 - v \bmod 2)$$

$$\begin{aligned} & \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \left( (-1)^s \binom{m}{s} \left( e^{-\frac{1}{2} i m \pi} \sqrt{p + b i (m - 2s)} (p - i b (m - 2s)) \operatorname{erfi}\left(\sqrt{p + b i (m - 2s)} z\right) + e^{\frac{i m \pi}{2}} (p + b i (m - 2s)) \right. \right. \\ & \quad \left. \left. \sqrt{p - i b (m - 2s)} \operatorname{erfi}\left(\sqrt{p - i b (m - 2s)} z\right) \right) \right) / ((p - i b (m - 2s)) (p + b i (m - 2s))) + \\ & \frac{2^{-m-v-1} \sqrt{\pi} (1 - m \bmod 2) (1 - v \bmod 2)}{\sqrt{p}} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\sqrt{p} z\right) + 2^{-m-v-1} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \\ & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \left( (-1)^k \binom{v}{k} \left( e^{-\frac{1}{2} i \pi v} \sqrt{p + c i (v - 2k)} (p - i c (v - 2k)) \operatorname{erfi}\left(\sqrt{p + c i (v - 2k)} z\right) + \right. \right. \\ & \quad \left. \left. e^{\frac{i \pi v}{2}} (p + c i (v - 2k)) \sqrt{p - i c (v - 2k)} \operatorname{erfi}\left(\sqrt{p - i c (v - 2k)} z\right) \right) \right) / ((p - i c (v - 2k)) (p + c i (v - 2k))) + \\ & 2^{-m-v-1} \sqrt{\pi} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( \left( e^{\frac{1}{2} i \pi (v-m)} \sqrt{p + b i (m - 2s) + c i (2k - v)} (p - i b (m - 2s) - i c (2k - v)) \right. \right. \\ & \quad \left. \left. \operatorname{erfi}\left(\sqrt{p + b i (m - 2s) + c i (2k - v)} z\right) + e^{-\frac{1}{2} i \pi (v-m)} (p + b i (m - 2s) + c i (2k - v)) \right. \right. \\ & \quad \left. \left. \sqrt{p - i b (m - 2s) - i c (2k - v)} \operatorname{erfi}\left(\sqrt{p - i b (m - 2s) - i c (2k - v)} z\right) \right) \right) / \\ & \quad ((p - i b (m - 2s) - i c (2k - v)) (p + b i (m - 2s) + c i (2k - v))) + \\ & \quad \left( e^{-\frac{1}{2} i \pi (m+v)} \sqrt{p + b i (m - 2s) + c i (v - 2k)} (p - i b (m - 2s) - i c (v - 2k)) \right. \\ & \quad \left. \operatorname{erfi}\left(\sqrt{p + b i (m - 2s) + c i (v - 2k)} z\right) + e^{\frac{1}{2} i \pi (m+v)} (p + b i (m - 2s) + c i (v - 2k)) \right. \\ & \quad \left. \sqrt{p - i b (m - 2s) - i c (v - 2k)} \operatorname{erfi}\left(\sqrt{p - i b (m - 2s) - i c (v - 2k)} z\right) \right) / \\ & \quad ((p - i b (m - 2s) - i c (v - 2k)) (p + b i (m - 2s) + c i (v - 2k))) \Big); m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1421.01

$$\int e^{p\sqrt{z}} \sin^m(b\sqrt{z}) \sin^v(c\sqrt{z}) dz =$$

$$\frac{2^{-m-v+1} e^{p\sqrt{z}} (p\sqrt{z} - 1) (1 - m \bmod 2) (1 - v \bmod 2)}{p^2} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} + 2^{-m-v+1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s \binom{m}{s}$$

$$e^{\frac{i\pi m}{2} + (p - ib(m-2s))\sqrt{z}} \left( \frac{e^{2(i b(m-2s)\sqrt{z} - \frac{i m \pi}{2})} (\sqrt{z} p + b i(m-2s)\sqrt{z} - 1)}{(p + b i(m-2s))^2} + \frac{\sqrt{z}}{p - i b(m-2s)} - \frac{1}{(i b(m-2s) - p)^2} \right) +$$

$$2^{-m-v+1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{\frac{i\pi v}{2} + (p - ic(v-2k))\sqrt{z}}$$

$$\left( \frac{e^{2(i c(v-2k)\sqrt{z} - \frac{i\pi v}{2})} (\sqrt{z} p + c i(v-2k)\sqrt{z} - 1)}{(p + c i(v-2k))^2} + \frac{\sqrt{z}}{p - i c(v-2k)} - \frac{1}{(i c(v-2k) - p)^2} \right) +$$

$$2^{-m-v+1} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{(p - ib(m-2s) - ic(2k-v))\sqrt{z} - \frac{1}{2} i\pi(v-m)}$$

$$\left( \frac{e^{2(\sqrt{z} (b i(m-2s) + c i(2k-v)) + \frac{1}{2} i\pi(v-m))} (\sqrt{z} p + (b i(m-2s) + c i(2k-v))\sqrt{z} - 1)}{(p + b i(m-2s) + c i(2k-v))^2} + \frac{\sqrt{z}}{p - i b(m-2s) - i c(2k-v)} - \frac{1}{(-p + b i(m-2s) + c i(2k-v))^2} \right) +$$

$$e^{\frac{1}{2} i\pi(m+v) + (p - ib(m-2s) - ic(v-2k))\sqrt{z}} \left( \frac{e^{2((b i(m-2s) + c i(v-2k))\sqrt{z} - \frac{1}{2} i\pi(m+v))} (\sqrt{z} p + (b i(m-2s) + c i(v-2k))\sqrt{z} - 1)}{(p + b i(m-2s) + c i(v-2k))^2} + \frac{\sqrt{z}}{p - i b(m-2s) - i c(v-2k)} - \frac{1}{(-p + b i(m-2s) + c i(v-2k))^2} \right) \Bigg) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

Involving  $e^{bz^r+e} \sin^m(az^r+q) \sin^v(cz^r+g)$

01.06.21.1422.01

$$\int e^{bz^r+e} \sin^m(az^r+q) \sin^v(cz^r+g) dz =$$

$$\frac{(-1)^m 2^{-m-v} e^e z (-bz^r)^{-1/r} (1-m \bmod 2) (1-v \bmod 2)}{r} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) \Gamma\left(\frac{1}{r}, -bz^r\right) - \frac{i^{-m} 2^{-m-v} z \left(\frac{v}{2}\right)}{r}$$

$$(1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m e^{e+2ikq-imq} \Gamma\left(\frac{1}{r}, (-b-2iak+iam)z^r\right) ((-b-2iak+iam)z^r)^{-1/r} + \right.$$

$$\left. e^{e-2ikq+imq} ((-b+2iak-iam)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b+2iak-iam)z^r\right) \right) - \frac{(-1)^m i^{-v} 2^{-m-v} z \left(\frac{m}{2}\right)}{r}$$

$$(1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{e+2igk-igv} \Gamma\left(\frac{1}{r}, (-b-2ick+icv)z^r\right) ((-b-2ick+icv)z^r)^{-1/r} + \right.$$

$$\left. e^{e-2igk+igv} ((-b+2ick-icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b+2ick-icv)z^r\right) \right) -$$

$$\frac{i^{m-v} 2^{-m-v} z}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{e+2ikq-imq+2igs-igv} \Gamma\left(\frac{1}{r}, (-b-2iak+iam-2ics+icv)z^r\right) \right.$$

$$\left. ((-b-2iak+iam-2ics+icv)z^r)^{-1/r} + (-1)^{m+v} e^{e-2ikq+imq+2igs-igv} \right.$$

$$\left. ((-b+2iak-iam-2ics+icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b+2iak-iam-2ics+icv)z^r\right) + \right.$$

$$\left. e^{e+2ikq-imq-2igs+igv} ((-b-2iak+iam+2ics-icv)z^r)^{-1/r} \Gamma\left(\frac{1}{r}, (-b-2iak+iam+2ics-icv) \right. \right.$$

$$\left. \left. z^r\right) + (-1)^m e^{e-2ikq+imq-2igs+igv} ((-b+2iak-iam+2ics-icv)z^r)^{-1/r} \right.$$

$$\left. \Gamma\left(\frac{1}{r}, (-b+2iak-iam+2ics-icv)z^r\right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

01.06.21.1423.01

$$\int e^{bz^2+e} \sin^m(az^2+q) \sin^v(cz^2+g) dz =$$

$$\frac{2^{-m-v-1} e^e \sqrt{\pi} (1-m \bmod 2) (1-v \bmod 2)}{\sqrt{b}} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \operatorname{erfi}(\sqrt{b} z) + 2^{-m-v-1} \sqrt{\pi} \binom{v}{\frac{v}{2}} (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k e^{e+i(m-2k)q-\frac{im\pi}{2}} \binom{m}{k} \left( \frac{\operatorname{erfi}(\sqrt{b+ai(m-2k)} z)}{\sqrt{b+ai(m-2k)}} + \frac{e^{2(\frac{im\pi}{2}-i(m-2k)q)} \operatorname{erfi}(\sqrt{b-ia(m-2k)} z)}{\sqrt{b-ia(m-2k)}} \right) +$$

$$2^{-m-v-1} \sqrt{\pi} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{e+g i(v-2k)-\frac{i\pi v}{2}} \binom{v}{k}$$

$$\left( \frac{\operatorname{erfi}(\sqrt{b+ci(v-2k)} z)}{\sqrt{b+ci(v-2k)}} + \frac{e^{2(\frac{i\pi v}{2}-i g(v-2k))} \operatorname{erfi}(\sqrt{b-ic(v-2k)} z)}{\sqrt{b-ic(v-2k)}} \right) + 2^{-m-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s$$

$$\binom{v}{s} \left( e^{\frac{e}{2}-\frac{1}{2}i\pi(v-m)-i(m-2k)q+g i(v-2s)} \left( \frac{\operatorname{erfi}(\sqrt{b-ia(m-2k)+ci(v-2s)} z)}{\sqrt{b-ia(m-2k)+ci(v-2s)}} + \left( e^{2(\frac{1}{2}i\pi(v-m)+i(m-2k)q-i g(v-2s))} \right. \right. \right.$$

$$\left. \left. \left. \operatorname{erfi}(\sqrt{b+ai(m-2k)-ic(v-2s)} z) \right) \right) / \left( \sqrt{b+ai(m-2k)-ic(v-2s)} \right) \right) +$$

$$e^{e+i(m-2k)q+g i(v-2s)-\frac{1}{2}i\pi(m+v)} \left( \frac{\operatorname{erfi}(\sqrt{b+ai(m-2k)+ci(v-2s)} z)}{\sqrt{b+ai(m-2k)+ci(v-2s)}} + \left( e^{2(-i(m-2k)q-i g(v-2s)+\frac{1}{2}i\pi(m+v))} \operatorname{erfi} \left( \right. \right. \right.$$

$$\left. \left. \left. \sqrt{b-ia(m-2k)-ic(v-2s)} z) \right) \right) / \left( \sqrt{b-ia(m-2k)-ic(v-2s)} \right) \right) \Bigg] ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$



01.06.21.1424.01

$$\int e^{\sqrt{z} b+e} \sin^m(\sqrt{z} a+q) \sin^v(\sqrt{z} c+g) dz = \frac{2^{-m-v+1} e^{\sqrt{z} b+e} (b\sqrt{z}-1) \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2)}{b^2} +$$

$$2^{-m-v+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \left( \frac{e^{e+i(m-2k)q+(b+ai(m-2k))\sqrt{z}-\frac{im\pi}{2}} (\sqrt{z} b+ai(m-2k)\sqrt{z}-1)}{(b-ia(m-2k))^2} + \right.$$

$$\left. \frac{e^{e-i(m-2k)q+(b-ia(m-2k))\sqrt{z}+\frac{im\pi}{2}} (\sqrt{z} b-ia(m-2k)\sqrt{z}-1)}{(b-ia(m-2k))^2} \right) \binom{m}{k} +$$

$$2^{-m-v+1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \left( \frac{e^{e+g+i(v-2k)+(b+ci(v-2k))\sqrt{z}-\frac{iv\pi}{2}} (\sqrt{z} b+ci(v-2k)\sqrt{z}-1)}{(b-ic(v-2k))^2} + \right.$$

$$\left. \frac{e^{e+\frac{iv\pi}{2}-i g(v-2k)+(b-ic(v-2k))\sqrt{z}} (\sqrt{z} b-ic(v-2k)\sqrt{z}-1)}{(b-ic(v-2k))^2} \right) \binom{v}{k} +$$

$$2^{-m-v+1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \left( \left( e^{e-i(m-2k)q+\frac{1}{2}i\pi(m+v)-i g(v-2s)+(b-ia(m-2k)-ic(v-2s))\sqrt{z}} \right. \right.$$

$$\left. \left. (\sqrt{z} b+(-ia(m-2k)-ic(v-2s))\sqrt{z}-1) \right) / (b-ia(m-2k)-ic(v-2s))^2 + \right.$$

$$\left. \left( e^{e+i(m-2k)q+\frac{1}{2}i\pi(v-m)-i g(v-2s)+(b+ai(m-2k)-ic(v-2s))\sqrt{z}} (\sqrt{z} b+(ia(m-2k)-ic(v-2s))\sqrt{z}-1) \right) / \right.$$

$$\left. (b+ai(m-2k)-ic(v-2s))^2 + \left( e^{e+i(m-2k)q-\frac{1}{2}i\pi(m+v)+g i(v-2s)+(b+ai(m-2k)+ci(v-2s))\sqrt{z}} \right. \right.$$

$$\left. \left. (\sqrt{z} b-(-ia(m-2k)-ic(v-2s))\sqrt{z}-1) \right) / (-b-ia(m-2k)-ic(v-2s))^2 + \right.$$

$$\left. \left( e^{e-i(m-2k)q-\frac{1}{2}i\pi(v-m)+g i(v-2s)+(b-ia(m-2k)+ci(v-2s))\sqrt{z}} (\sqrt{z} b-(ia(m-2k)-ic(v-2s))\sqrt{z}-1) \right) / \right.$$

$$\left. (-b+ai(m-2k)-ic(v-2s))^2 \right) \binom{v}{s} /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

**Involving  $e^{bz^r+dz+e} \sin^m(az^r+pz+q) \sin^v(cz^r+fz+g)$**

01.06.21.1425.01

$$\int e^{bz^2+dz+e} \sin^m(az^2+pz+q) \sin^v(cz^2+fz+g) dz =$$

$$\frac{2^{-m-v-1} e^{-\frac{d^2-4be}{4b}} \sqrt{\pi} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \operatorname{erfi}\left(\frac{d+2bz}{2\sqrt{b}}\right) (1-m \bmod 2) (1-v \bmod 2)}{\sqrt{b}} +$$

$$\begin{aligned}
 & 2^{-m-v-1} \sqrt{\pi} \left( \frac{v}{2} \right) \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{b^2 + a^2 (m-2k)^2} \left( (-1)^k \binom{m}{k} \left( e^{-\frac{(d+i(m-2k)p)^2 + 2(i b + 2 a k - a m)(2 i e + m(\pi - 2q) + 4 k q)}{4(b+i(m-2k))}} \sqrt{b + a i (m-2k)} \right. \right. \right. \\
 & \quad (b - i a (m-2k)) \operatorname{erfi} \left( \frac{d + i (m-2k) p + 2 b z + 2 a i (m-2k) z}{2 \sqrt{b + a i (m-2k)}} \right) + e^{-\frac{(d-i(m-2k)p)^2 + 2(-i b + 2 a k - a m)(-2 i e + m(\pi - 2q) + 4 k q)}{4(b-i(m-2k))}} \\
 & \quad \left. \left. \left. (b + a i (m-2k)) \sqrt{b - i a (m-2k)} \operatorname{erfi} \left( \frac{d - i (m-2k) p + 2 (b - i a (m-2k)) z}{2 \sqrt{b - i a (m-2k)}} \right) \right) \right) \right) (1 - v \bmod 2) + \\
 & 2^{-m-v-1} \sqrt{\pi} \left( \frac{m}{2} \right) (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{b^2 + c^2 (v-2k)^2} \left( (-1)^k \binom{v}{k} \left( e^{-\frac{(d+f i (v-2k))^2 + 2(2 i e + 4 g k - 2 g v + \pi v)(i b + 2 c k - c v)}{4(b+c i (v-2k))}} \sqrt{b + c i (v-2k)} \right. \right. \\
 & \quad (b - i c (v-2k)) \operatorname{erfi} \left( \frac{d + f i (v-2k) + 2 b z + 2 c i (v-2k) z}{2 \sqrt{b + c i (v-2k)}} \right) + e^{-\frac{(d-i f (v-2k))^2 + 2(-2 i e + 4 g k - 2 g v + \pi v)(-i b + 2 c k - c v)}{4(b-i c (v-2k))}} \\
 & \quad \left. \left. \left. (b + c i (v-2k)) \sqrt{b - i c (v-2k)} \operatorname{erfi} \left( \frac{d - i f (v-2k) + 2 (b - i c (v-2k)) z}{2 \sqrt{b - i c (v-2k)}} \right) \right) \right) \right) + \\
 & 2^{-m-v-1} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{s} \left( \left( e^{-\frac{(d+i(2k p - m p + 2 f s - f v))^2 + 2(-2 i e + m(\pi - 2q) + 4 k q + 4 g s - 2 g v + \pi v)(-i b + 2 a k - a m + 2 c s - c v)}{4(b+i(2 a k - a m + 2 c s - c v))}} \right. \right. \\
 & \quad \left. \left. \operatorname{erfi} \left( \frac{d + i (2k - m) p + f i (2s - v) + 2 (b + a i (2k - m) + c i (2s - v)) z}{2 \sqrt{b + a i (2k - m) + c i (2s - v)}} \right) \right) \right) / \\
 & \quad \left( \sqrt{b + a i (2k - m) + c i (2s - v)} \right) + \left( e^{-\frac{(d+i(-2k p + m p + 2 f s - f v))^2 + 2(i b + 2 a k - a m - 2 c s + c v)(2 i e + m(\pi - 2q) + 4 k q - 4 g s + 2 g v - \pi v)}{4(b-i(2 a k - a m - 2 c s + c v))}} \right. \\
 & \quad \left. \operatorname{erfi} \left( \frac{d + i (m-2k) p + f i (2s - v) + 2 (b + a i (m-2k) + c i (2s - v)) z}{2 \sqrt{b + a i (m-2k) + c i (2s - v)}} \right) \right) / \\
 & \quad \left( \sqrt{b + a i (m-2k) + c i (2s - v)} \right) + \left( e^{-\frac{(d+i(2k p - m p - 2 f s + f v))^2 + 2(-i b + 2 a k - a m - 2 c s + c v)(-2 i e + m(\pi - 2q) + 4 k q - 4 g s + 2 g v - \pi v)}{4(b+i(2 a k - a m - 2 c s + c v))}} \right. \\
 & \quad \left. \operatorname{erfi} \left( \frac{d + i (2k - m) p + f i (v-2s) + 2 (b + a i (2k - m) + c i (v-2s)) z}{2 \sqrt{b + a i (2k - m) + c i (v-2s)}} \right) \right) / \\
 & \quad \left( \sqrt{b + a i (2k - m) + c i (v-2s)} \right) + \left( e^{-\frac{(d+i(m-2k)p + f i (v-2s))^2 + 2(2 i e + m(\pi - 2q) + 4 k q + 4 g s - 2 g v + \pi v)(i b + 2 a k - a m + 2 c s - c v)}{4(b+a i (m-2k) + c i (v-2s))}} \right. \\
 & \quad \left. \operatorname{erfi} \left( \frac{d + i (m-2k) p + f i (v-2s) + 2 (b + a i (m-2k) + c i (v-2s)) z}{2 \sqrt{b + a i (m-2k) + c i (v-2s)}} \right) \right) / \\
 & \quad \left. \left. \left. \left( \sqrt{b + a i (m-2k) + c i (v-2s)} \right) \right) \right) / ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1426.01

$$\int e^{\sqrt{z} b+d z+e} \sin^m(\sqrt{z} a+p z+q) \sin^v(\sqrt{z} c+f z+g) d z =$$

$$2^{-m-v-2} \left( \frac{4 e^{\sqrt{z} b+d z}}{d} - \frac{2 b e^{-\frac{b^2}{4 d}} \sqrt{\pi} \operatorname{erfi}\left(\frac{b+2 d \sqrt{z}}{2 \sqrt{d}}\right)}{d^{3/2}} \right) e^e \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1-m \bmod 2) (1-v \bmod 2) +$$

$$2^{-m-v-1} \binom{v}{\frac{v}{2}} \left( \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^s e^{-i q(m-2 s)+\frac{i m \pi}{2}} \binom{m}{s} \right.$$

$$\left. \left( \left( e^{-\frac{(b-i a m+2 i a s)^2}{4(d-i m p+2 i p s)}} \sqrt{\pi} (i a(m-2 s)-b) \operatorname{erfi}\left(\frac{b-i a(m-2 s)+2(d-i m p+2 i p s) \sqrt{z}}{2 \sqrt{d-i m p+2 i p s}}\right) \right) / (d-i m p+2 i p s)^{3/2} + \right.$$

$$\frac{2 e^{2 i q m-i \pi m-4 i q s+(d+i p(m-2 s)) z+(b+a i(m-2 s)) \sqrt{z}}}{d+i p(m-2 s)} - \frac{1}{(d+i p(m-2 s))^{3/2}} \left( e^{-\frac{(b+a i(m-2 s))^2+2 i q(m-2 s)-i m \pi}{4(d+i p(m-2 s))}} \sqrt{\pi} \right.$$

$$\left. (b+a i(m-2 s)) \operatorname{erfi}\left(\frac{b+a i(m-2 s)+2(d+i m p-2 i p s) \sqrt{z}}{2 \sqrt{d+i p(m-2 s)}}\right) \right) + \frac{2 e^{\sqrt{z}(b-i a(m-2 s)+(d-i p(m-2 s)) z}}}{d-i p(m-2 s)} \Bigg)$$

$$(1-v \bmod 2) + 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{+\frac{i \pi v}{2}-i g(v-2 k)} \binom{v}{k}$$

$$\left( - \left( e^{-\frac{(b+2 i c k-i c v)^2}{4(d+2 i f k-i f v)}} \sqrt{\pi} (b+2 i c k-i c v) \operatorname{erfi}\left(\frac{b+c i(2 k-v)+2(d+2 i f k-i f v) \sqrt{z}}{2 \sqrt{d+2 i f k-i f v}}\right) \right) / (d+2 i f k-i f v)^{3/2} + \right.$$

$$\frac{2 e^{-4 g i k+2 i g v-i \pi v+(d+f i(v-2 k)) z+(b+c i(v-2 k)) \sqrt{z}}}{d+f i(v-2 k)} - \frac{1}{(d+f i(v-2 k))^{3/2}} \left( e^{-\frac{(b+c i(v-2 k))^2-i \pi v+2 g i(v-2 k)}{4(d+f i(v-2 k))}} \sqrt{\pi} \right.$$

$$\left. (b+c i(v-2 k)) \operatorname{erfi}\left(\frac{b+c i(v-2 k)+2(d-2 i f k+i f v) \sqrt{z}}{2 \sqrt{d+f i(v-2 k)}}\right) \right) + \frac{2 e^{\sqrt{z}(b-i c(v-2 k)+(d-i f(v-2 k)) z}}}{d-i f(v-2 k)} \Bigg) +$$

$$2^{-m-v-1} \sum_{s=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{s} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{k} \left( e^{-i q(m-2 s)-i g(v-2 k)+\frac{1}{2} i \pi(m+v)} \left( \left( e^{-\frac{(b+i(a(m-2 s)+c(v-2 k))^2+2 i q(m-2 s)+2 g i(v-2 k)-i \pi(m+v))}{4(d+i p(m-2 s)+f i(v-2 k))}} \right. \right.$$

$$\left. \left. \sqrt{\pi} (-i b+a(m-2 s)+c(v-2 k)) \operatorname{erfi}\left(\frac{b+a i(m-2 s)+c i(v-2 k)+2(d+i p(m-2 s)+f i(v-2 k)) \sqrt{z}}{2 \sqrt{d+i p(m-2 s)+f i(v-2 k)}}\right) \right) \right) /$$

$$\left( (i d+2 f k-m p+2 p s-f v) \sqrt{d+i p(m-2 s)+f i(v-2 k)} \right) +$$

$$\left( 2 e^{2 i q(m-2 s)+2 g i(v-2 k)-i \pi(m+v)+(d+i p(m-2 s)+f i(v-2 k)) z+(b+i(-2 c k+a m-2 a s+c v)) \sqrt{z}} \right) /$$

$$\begin{aligned}
 & (d + i p (m - 2 s) + f i (v - 2 k)) - \left( e^{\frac{i (i b + a (m - 2 s) + c (v - 2 k))^2}{4 (i d + p (m - 2 s) + f (v - 2 k))}} \sqrt{\pi} (i b + a (m - 2 s) + c (v - 2 k)) \right. \\
 & \operatorname{erfi} \left( \left( b + i (-a (m - 2 s) + c (2 k - v) + 2 (-i d + 2 f k - m p + 2 p s - f v) \sqrt{z}) \right) / \right. \\
 & \left. \left. \left( 2 \sqrt{d + i (2 f k - m p + 2 p s - f v)} \right) \right) \right) / \left( (i d + p (m - 2 s) + f (v - 2 k)) \right. \\
 & \left. \sqrt{d + i (2 f k - m p + 2 p s - f v)} \right) + \frac{2 e^{\sqrt{z} (b - i (-2 c k + a m - 2 a s + c v)) + (d + i (2 f k - m p + 2 p s - f v)) z}}{d + i (2 f k - m p + 2 p s - f v)} \Bigg) + \\
 & e^{-i q (m - 2 s) - i g (2 k - v) - \frac{1}{2} i \pi (v - m)} \left( \left( e^{\frac{(i b - 2 c k - a m + 2 a s + c v)^2}{4 (d + i (2 f k + m p - 2 p s - f v))} + 2 i q (m - 2 s) + 2 g i (2 k - v) + i \pi (v - m)} \sqrt{\pi} (-i b + 2 c k + a m - \right. \right. \\
 & \left. \left. 2 a s - c v) \operatorname{erfi} \left( \left( b + i (a (m - 2 s) + c (2 k - v) + 2 (-i d + 2 f k + m p - 2 p s - f v) \sqrt{z}) \right) / \right. \right. \\
 & \left. \left. \left( 2 \sqrt{d + i (2 f k + m p - 2 p s - f v)} \right) \right) \right) / \\
 & \left( (i d - 2 f k - m p + 2 p s + f v) \sqrt{d + i (2 f k + m p - 2 p s - f v)} \right) + \\
 & \left( e^{\frac{(i b + 2 c k + a m - 2 a s - c v)^2}{4 (d - i (2 f k + m p - 2 p s - f v))}} \sqrt{\pi} (i b + 2 c k + a m - 2 a s - c v) \operatorname{erfi} \left( \left( b - i (a (m - 2 s) + c (2 k - v) + \right. \right. \right. \\
 & \left. \left. \left. 2 (i d + 2 f k + m p - 2 p s - f v) \sqrt{z}) \right) / \left( 2 \sqrt{d - i (2 f k + m p - 2 p s - f v)} \right) \right) \right) / \\
 & \left( (-i d - 2 f k - m p + 2 p s + f v) \sqrt{d - i (2 f k + m p - 2 p s - f v)} \right) + \\
 & \left. \left. \left. \left( 2 e^{2 i q (m - 2 s) + 2 g i (2 k - v) + i \pi (v - m) + (d + i (2 f k + m p - 2 p s - f v)) z + (b + i (2 c k + a m - 2 a s - c v)) \sqrt{z}} \right) / (d + i (2 f k + \right. \right. \right. \\
 & \left. \left. \left. m p - 2 p s - f v)) + \frac{2 e^{\sqrt{z} (b - i (2 c k + a m - 2 a s - c v)) + (d - i (2 f k + m p - 2 p s - f v)) z}}{d - i (2 f k + m p - 2 p s - f v)} \right) \right) / ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving product of powers of two direct functions and rational functions of exp

Involving  $\sin^m(ez) \sin^v(cz) (a + b e^{dz})^{-n}$

01.06.21.1427.01

$$\int \frac{\sin^m(ez) \sin^v(cz)}{(a + b e^{dz})^n} dz =$$

$$\begin{aligned}
 & 2^{-m-v} \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{s} \left( \cos \left( \frac{1}{2} \pi (m+v) \right) \left( e^{2 i e k - i e m + 2 i c s - i c v} z {}_2F_1 \left( \frac{2 i e k - i e m + 2 i c s - i c v}{d}, \right. \right. \right. \right. \\
 & \left. \left. \left. n; \frac{d + 2 i e k - i e m + 2 i c s - i c v}{d}; -\frac{b e^{dz}}{a} \right) - e^{(-2 i e k + i e m - 2 i c s + i c v) z} \right. \right. \\
 & \left. \left. \left. {}_2F_1 \left( \frac{-2 i e k + i e m - 2 i c s + i c v}{d}, n; \frac{d - 2 i e k + i e m - 2 i c s + i c v}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & (2iek - iem + 2ics - icv) + \left( \cos\left(\frac{1}{2}\pi(m-v)\right) \right) \left( e^{(2iek - iem - 2ics + icv)z} \right. \\
 & \quad {}_2F_1\left(\frac{2iek - iem - 2ics + icv}{d}, n; \frac{d + 2iek - iem - 2ics + icv}{d}; -\frac{be^{dz}}{a}\right) - \\
 & \quad e^{(-2eik + iem + 2ics - icv)z} {}_2F_1\left(\frac{-2eik + iem + 2ics - icv}{d}, n; \right. \\
 & \quad \left. \frac{d - 2iek + iem + 2ics - icv}{d}; -\frac{be^{dz}}{a}\right) \Big) / (2iek - iem - 2ics + icv) + \\
 & \left( i \left( e^{(2iek - iem - 2ics + icv)z} {}_2F_1\left(\frac{2iek - iem - 2ics + icv}{d}, n; \frac{d + 2iek - iem - 2ics + icv}{d}; -\frac{be^{dz}}{a}\right) \right. \right. \\
 & \quad e^{(-2eik + iem + 2ics - icv)z} {}_2F_1\left(\frac{-2eik + iem + 2ics - icv}{d}, n; \frac{d - 2iek + iem + 2ics - icv}{d}; \right. \\
 & \quad \left. \left. -\frac{be^{dz}}{a}\right) \sin\left(\frac{1}{2}\pi(m-v)\right) \right) / (2iek - iem - 2ics + icv) + \left( i \left( e^{(-2eik + iem - 2ics + icv)z} \right. \right. \\
 & \quad {}_2F_1\left(\frac{-2eik + iem - 2ics + icv}{d}, n; \frac{d - 2iek + iem - 2ics + icv}{d}; -\frac{be^{dz}}{a}\right) + \\
 & \quad \left. \left. e^{(2iek - iem + 2ics - icv)z} {}_2F_1\left(\frac{2iek - iem + 2ics - icv}{d}, n; \frac{d + 2iek - iem + 2ics - icv}{d}; \right. \right. \right. \\
 & \quad \left. \left. -\frac{be^{dz}}{a}\right) \sin\left(\frac{1}{2}\pi(m+v)\right) \right) / (2iek - iem + 2ics - icv) \Big) \\
 & a^{-n} - \frac{2^{-m-v} b^{-n} e^{-dnz} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} {}_2F_1\left(n, n; n+1; -\frac{ae^{-dz}}{b}\right) (m \bmod 2 - 1) (v \bmod 2 - 1)}{dn} - \\
 & \frac{1}{e} \\
 & \left( i \right. \\
 & \quad 2^{-m-v} \\
 & \quad a^{-n} \\
 & \quad \binom{v}{\frac{v}{2}} \\
 & \quad (1 - v \bmod 2) \\
 & \quad \left. \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{m-2k} (-1)^k \binom{m}{k} \left( e^{ie(m-2k)z - \frac{im\pi}{2}} {}_2F_1\left(\frac{ie(m-2k)}{d}, n; \frac{d + ie(m-2k)}{d}; -\frac{be^{dz}}{a}\right) - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & e^{\frac{i\pi}{2} - i e(m-2k)z} {}_2F_1\left(-\frac{i e(m-2k)}{d}, n; \frac{d - i e(m-2k)}{d}; -\frac{b e^{dz}}{a}\right) \Bigg) - \\
 & \frac{1}{c} \left( i 2^{-m-v} a^{-n} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{v-2s} (-1)^s \binom{v}{s} \left( e^{i c(v-2s)z - \frac{i\pi v}{2}} {}_2F_1\left(\frac{i c(v-2s)}{d}, n; \frac{d + c i(v-2s)}{d}; -\frac{b e^{dz}}{a}\right) - \right. \right. \\
 & \left. \left. e^{\frac{i\pi v}{2} - i c(v-2s)z} {}_2F_1\left(-\frac{i c(v-2s)}{d}, n; \frac{d - i c(v-2s)}{d}; -\frac{b e^{dz}}{a}\right) \right) \Bigg) /; n \in \mathbb{N}^+ \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $e^{pz} \sin^m(ez) \sin^v(cz) (a + b e^{dz})^{-n}$**

01.06.21.1428.01

$$\begin{aligned}
 \int \frac{e^{pz} \sin^m(ez) \sin^v(cz)}{(a + b e^{dz})^n} dz &= 2^{-m-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) a^{-n} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{(e i(m-2k)+p)z - \frac{i\pi m}{2}} (i e(m-2k) - p) {}_2F_1\left(\frac{e i(m-2k) + p}{d}, n; \frac{d + e i(m-2k) + p}{d}; -\frac{b e^{dz}}{a}\right) - \right. \\
 & \left. e^{\frac{i\pi m}{2} + (p - i e(m-2k))z} (e i(m-2k) + p) {}_2F_1\left(\frac{p - i e(m-2k)}{d}, n; \frac{d - i e(m-2k) + p}{d}; -\frac{b e^{dz}}{a}\right) \right) / \\
 & ((i e(m-2k) - p)(e i(m-2k) + p)) + 2^{-m-v} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) a^{-n} \\
 & \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{(p + c i(v-2s))z - \frac{i\pi v}{2}} (i c(v-2s) - p) {}_2F_1\left(\frac{p + c i(v-2s)}{d}, n; \frac{d + p + c i(v-2s)}{d}; -\frac{b e^{dz}}{a}\right) - \right. \\
 & \left. e^{\frac{i\pi v}{2} + (p - i c(v-2s))z} (p + c i(v-2s)) {}_2F_1\left(\frac{p - i c(v-2s)}{d}, n; \frac{d + p - i c(v-2s)}{d}; -\frac{b e^{dz}}{a}\right) \right) / \\
 & ((i c(v-2s) - p)(p + c i(v-2s))) + 2^{-m-v} a^{-n} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{s} \left( \cos\left(\frac{1}{2} \pi(m+v)\right) \left( e^{(2iek - iem + p + 2ics - icv)z} (2iek - iem - p + 2ics - icv) \right. \right. \\
 & \left. {}_2F_1\left(\frac{2iek - iem + p + 2ics - icv}{d}, n; \frac{d + 2iek - iem + p + 2ics - icv}{d}; -\frac{b e^{dz}}{a}\right) - \right. \\
 & \left. e^{(-2iek + iem + p - 2ics + icv)z} (2iek - iem + p + 2ics - icv) \right. \\
 & \left. {}_2F_1\left(\frac{-2iek + iem + p - 2ics + icv}{d}, n; \frac{d - 2iek + iem + p - 2ics + icv}{d}; -\frac{b e^{dz}}{a}\right) \right) / \\
 & ((2iek - iem - p + 2ics - icv)(2iek - iem + p + 2ics - icv)) + \\
 & \left( \cos\left(\frac{1}{2} \pi(m-v)\right) \left( e^{(2iek - iem + p - 2ics + icv)z} (2iek - iem - p - 2ics + icv) \right. \right. \\
 & \left. {}_2F_1\left(\frac{2iek - iem + p - 2ics + icv}{d}, n; \frac{d + 2iek - iem + p - 2ics + icv}{d}; -\frac{b e^{dz}}{a}\right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & e^{(-2iek+iem+p+2ics-icv)z} (2iek-iem+p-2ics+icv) \\
 & {}_2F_1\left(\frac{-2iek+iem+p+2ics-icv}{d}, n; \frac{d-2iek+iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) \Big/ \\
 & ((2iek-iem-p-2ics+icv)(2iek-iem+p-2ics+icv)) + \\
 & \left( i \left( e^{(2iek-iem+p-2ics+icv)z} (2iek-iem-p-2ics+icv) {}_2F_1\left(\frac{2iek-iem+p-2ics+icv}{d}, \right. \right. \right. \\
 & \left. \left. \left. n; \frac{d+2iek-iem+p-2ics+icv}{d}; -\frac{be^{dz}}{a}\right) + e^{(-2iek+iem+p+2ics-icv)z} \right. \right. \\
 & (2iek-iem+p-2ics+icv) {}_2F_1\left(\frac{-2iek+iem+p+2ics-icv}{d}, n; \right. \\
 & \left. \left. \frac{d-2iek+iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) \right) \sin\left(\frac{1}{2}\pi(m-v)\right) \Big/ \\
 & ((2iek-iem-p-2ics+icv)(2iek-iem+p-2ics+icv)) + \\
 & \left( i \left( e^{(-2iek+iem+p-2ics+icv)z} (2iek-iem+p+2ics-icv) {}_2F_1\left(\frac{-2iek+iem+p-2ics+icv}{d}, \right. \right. \right. \\
 & \left. \left. \left. n; \frac{d-2iek+iem+p-2ics+icv}{d}; -\frac{be^{dz}}{a}\right) + e^{(2iek-iem+p+2ics-icv)z} \right. \right. \\
 & (2iek-iem-p+2ics-icv) {}_2F_1\left(\frac{2iek-iem+p+2ics-icv}{d}, n; \right. \\
 & \left. \left. \frac{d+2iek-iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) \right) \sin\left(\frac{1}{2}\pi(m+v)\right) \Big/ \\
 & ((2iek-iem-p+2ics-icv)(2iek-iem+p+2ics-icv)) \Big) + \\
 & \frac{2^{-m-v} a^{-n} e^{pz} (1-m \bmod 2) (1-v \bmod 2)}{p} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \\
 & {}_2F_1\left(\frac{p}{d}, \right. \\
 & \left. n; \frac{d+p}{d}; -\frac{be^{dz}}{a}\right) ; n \in \mathbb{N}^+ \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving product of powers of two direct functions and algebraic functions of exp

Involving  $(a + b e^{dz})^\beta \sin^m(ez) \sin^v(cz)$

01.06.21.1429.01

$$\int (a + b e^{dz})^\beta \sin^m(ez) \sin^v(cz) dz =$$

$$2^{-m-v} (a + b e^{dz})^\beta \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{s} \left( \cos\left(\frac{1}{2} \pi (m+v)\right) \left( e^{(2iek-iem+2ics-icv)z} {}_2F_1\left(\frac{2iek-iem+2ics-icv}{d}, \right. \right. \right. \right.$$

$$\left. \left. \left. -\beta; \frac{d+2iek-iem+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) - e^{(-2eik+iem-2ics+icv)z} \right. \right.$$

$$\left. \left. {}_2F_1\left(\frac{-2eik+iem-2ics+icv}{d}, -\beta; \frac{d-2iek+iem-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) /$$

$$(2iek-iem+2ics-icv) + \left( \cos\left(\frac{1}{2} \pi (m-v)\right) \left( e^{(2iek-iem-2ics+icv)z} \right. \right.$$

$$\left. \left. {}_2F_1\left(\frac{2iek-iem-2ics+icv}{d}, -\beta; \frac{d+2iek-iem-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) - \right. \right.$$

$$\left. \left. e^{(-2eik+iem+2ics-icv)z} {}_2F_1\left(\frac{-2eik+iem+2ics-icv}{d}, -\beta; \right. \right. \right.$$

$$\left. \left. \left. \frac{d-2iek+iem+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) / (2iek-iem-2ics+icv) +$$

$$\left( i \left( e^{(2iek-iem-2ics+icv)z} {}_2F_1\left(\frac{2iek-iem-2ics+icv}{d}, -\beta; \frac{d+2iek-iem-2ics+icv}{d}; \right. \right. \right.$$

$$\left. \left. \left. -\frac{b e^{dz}}{a} \right) + e^{(-2eik+iem+2ics-icv)z} {}_2F_1\left(\frac{-2eik+iem+2ics-icv}{d}, \right. \right. \right.$$

$$\left. \left. \left. -\beta; \frac{d-2iek+iem+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \sin\left(\frac{1}{2} \pi (m-v)\right) \right) /$$

$$(2iek-iem-2ics+icv) + \left( i \left( e^{(-2eik+iem-2ics+icv)z} {}_2F_1\left(\frac{-2eik+iem-2ics+icv}{d}, \right. \right. \right.$$

$$\left. \left. \left. -\beta; \frac{d-2iek+iem-2ics+icv}{d}; -\frac{b e^{dz}}{a} \right) + e^{(2iek-iem+2ics-icv)z} \right. \right.$$

$$\left. \left. {}_2F_1\left(\frac{2iek-iem+2ics-icv}{d}, -\beta; \frac{d+2iek-iem+2ics-icv}{d}; -\frac{b e^{dz}}{a} \right) \right) \right)$$

$$\sin\left(\frac{1}{2} \pi (m+v)\right) \Bigg) / (2iek-iem+2ics-icv) \Bigg) \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} +$$

$$\frac{1}{d \beta} \left( 2^{-m-v} \left( \frac{e^{-dz} a}{b} + 1 \right)^{-\beta} (a + b e^{dz})^\beta \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} {}_2F_1\left(-\beta, -\beta; 1-\beta; -\frac{a e^{-dz}}{b} \right) \right.$$

$$(m \bmod 2 - 1)$$

$$\left. (v \bmod 2 - 1) \right) - \frac{1}{e} i$$



$$\begin{aligned}
 & 2^{-m-v} \\
 & (a + b e^{dz})^\beta \\
 & \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \\
 & \left( \frac{v}{2} \right) \\
 & (1 - v \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \frac{1}{m-2k} \left( (-1)^k \binom{m}{k} \left( e^{i e(m-2k)z - \frac{i m \pi}{2}} {}_2F_1 \left( \frac{i e(m-2k)}{d}, -\beta; \frac{d + e i(m-2k)}{d}; -\frac{b e^{dz}}{a} \right) - \right. \right. \\
 & \left. \left. e^{\frac{i m \pi}{2} - i e(m-2k)z} {}_2F_1 \left( -\frac{i e(m-2k)}{d}, -\beta; \frac{d - i e(m-2k)}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) \\
 & \frac{1}{c} \left( i 2^{-m-v} (a + b e^{dz})^\beta \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \frac{1}{v-2s} \right. \\
 & \left. \left( (-1)^s \binom{v}{s} \left( e^{i c(v-2s)z - \frac{i \pi v}{2}} {}_2F_1 \left( \frac{i c(v-2s)}{d}, -\beta; \frac{d + c i(v-2s)}{d}; -\frac{b e^{dz}}{a} \right) - \right. \right. \\
 & \left. \left. e^{\frac{i \pi v}{2} - i c(v-2s)z} {}_2F_1 \left( -\frac{i c(v-2s)}{d}, -\beta; \frac{d - i c(v-2s)}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $e^{pz}(a + b e^{dz})^\beta \sin^m(ez) \sin^v(cz)$

01.06.21.1430.01

$$\begin{aligned}
 \int e^{pz} (a + b e^{dz})^\beta \sin^m(ez) \sin^v(cz) dz &= 2^{-m-v} (a + b e^{dz})^\beta \left( \frac{v}{2} \right) (1 - v \bmod 2) \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \left( (-1)^k \binom{m}{k} \left( e^{(e i(m-2k)+p)z - \frac{i m \pi}{2}} (i e(m-2k) - p) {}_2F_1 \left( \frac{e i(m-2k) + p}{d}, -\beta; \frac{d + e i(m-2k) + p}{d}; -\frac{b e^{dz}}{a} \right) - \right. \right. \\
 & \left. \left. e^{\frac{i \pi m}{2} + (p - i e(m-2k))z} (e i(m-2k) + p) {}_2F_1 \left( \frac{p - i e(m-2k)}{d}, -\beta; \frac{d - i e(m-2k) + p}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) / \\
 & ((e i(m-2k) - p) (e i(m-2k) + p)) + 2^{-m-v} (a + b e^{dz})^\beta \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \left( \frac{e^{dz} b}{a} + 1 \right)^{-\beta} \\
 & \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} \left( (-1)^s \binom{v}{s} \left( e^{(p + c i(v-2s))z - \frac{i \pi v}{2}} (i c(v-2s) - p) {}_2F_1 \left( \frac{p + c i(v-2s)}{d}, -\beta; \frac{d + p + c i(v-2s)}{d}; -\frac{b e^{dz}}{a} \right) - \right. \right. \\
 & \left. \left. e^{\frac{i \pi v}{2} + (p - i c(v-2s))z} (p + c i(v-2s)) {}_2F_1 \left( \frac{p - i c(v-2s)}{d}, -\beta; \frac{d + p - i c(v-2s)}{d}; -\frac{b e^{dz}}{a} \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & ((ic(v-2s)-p)(p+ci(v-2s))) + 2^{-m-v} (a+be^{dz})^\beta \left(\frac{e^{dz}b}{a} + 1\right)^{-\beta} \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^{k+s} \binom{v}{s} \left( \cos\left(\frac{1}{2}\pi(m+v)\right) \left( e^{2iek-iem+p+2ics-icv} z (2iek-iem-p+2ics-icv) \right. \right. \\
 & \quad {}_2F_1\left(\frac{2iek-iem+p+2ics-icv}{d}, -\beta; \frac{d+2iek-iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) - \\
 & \quad e^{(-2eik+iem+p-2ics+icv)z} (2iek-iem+p+2ics-icv) \\
 & \quad \left. \left. {}_2F_1\left(\frac{-2eik+iem+p-2ics+icv}{d}, -\beta; \frac{d-2iek+iem+p-2ics+icv}{d}; -\frac{be^{dz}}{a}\right) \right) \right) / \\
 & \quad ((2iek-iem-p+2ics-icv)(2iek-iem+p+2ics-icv)) + \\
 & \quad \left( \cos\left(\frac{1}{2}\pi(m-v)\right) \left( e^{2iek-iem+p-2ics+icv} z (2iek-iem-p-2ics+icv) \right. \right. \\
 & \quad \left. \left. {}_2F_1\left(\frac{2iek-iem+p-2ics+icv}{d}, -\beta; \frac{d+2iek-iem+p-2ics+icv}{d}; -\frac{be^{dz}}{a}\right) - \right. \right. \\
 & \quad e^{(-2eik+iem+p+2ics-icv)z} (2iek-iem+p-2ics+icv) \\
 & \quad \left. \left. {}_2F_1\left(\frac{-2eik+iem+p+2ics-icv}{d}, -\beta; \frac{d-2iek+iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) \right) \right) / \\
 & \quad ((2iek-iem-p-2ics+icv)(2iek-iem+p-2ics+icv)) + \\
 & \quad \left( i \left( e^{2iek-iem+p-2ics+icv} z (2iek-iem-p-2ics+icv) {}_2F_1\left(\frac{2iek-iem+p-2ics+icv}{d}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\beta; \frac{d+2iek-iem+p-2ics+icv}{d}; -\frac{be^{dz}}{a}\right) + e^{(-2eik+iem+p+2ics-icv)z} \right. \right. \\
 & \quad \left. \left. (2iek-iem+p-2ics+icv) {}_2F_1\left(\frac{-2eik+iem+p+2ics-icv}{d}, -\beta; \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d-2iek+iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) \right) \sin\left(\frac{1}{2}\pi(m-v)\right) \right) / \\
 & \quad ((2iek-iem-p-2ics+icv)(2iek-iem+p-2ics+icv)) + \\
 & \quad \left( i \left( e^{(-2eik+iem+p-2ics+icv)z} (2iek-iem+p+2ics-icv) {}_2F_1\left(\frac{-2eik+iem+p-2ics+icv}{d}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\beta; \frac{d-2iek+iem+p-2ics+icv}{d}; -\frac{be^{dz}}{a}\right) + e^{(2iek-iem+p+2ics-icv)z} \right. \right. \\
 & \quad \left. \left. (2iek-iem-p+2ics-icv) {}_2F_1\left(\frac{2iek-iem+p+2ics-icv}{d}, -\beta; \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d+2iek-iem+p+2ics-icv}{d}; -\frac{be^{dz}}{a}\right) \right) \sin\left(\frac{1}{2}\pi(m+v)\right) \right) / \\
 & \quad ((2iek-iem-p+2ics-icv)(2iek-iem+p+2ics-icv)) \Big) +
 \end{aligned}$$

$$\frac{2^{-m-v} e^{pz}}{p} (a + b e^{dz})^\beta \left(\frac{e^{dz} b}{a} + 1\right)^{-\beta} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) {}_2F_1\left(\frac{p}{d}, -\beta; \frac{d+p}{d}; -\frac{b e^{dz}}{a}\right)$$

(1 -  
 $m \bmod 2$ ) (1 -  
 $v \bmod 2$ ) /;  $m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$

### Involving rational functions of the direct function and exponential function

Involving exp

Involving  $\frac{e^{pz}}{a+b \sin(cz)}$

01.06.21.1431.01

$$\int \frac{e^{pz}}{a + b \sin(cz)} dz = -\frac{1}{b \sqrt{a^2 - b^2} (c - ip)} e^{(ic+p)z}$$

$$\left( (a + \sqrt{a^2 - b^2}) {}_2F_1\left(1 - \frac{ip}{c}, 1; 2 - \frac{ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}}\right) + (\sqrt{a^2 - b^2} - a) {}_2F_1\left(1 - \frac{ip}{c}, 1; 2 - \frac{ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}}\right) \right)$$

Involving  $e^{pz}(a + b \sin(cz))^{-n}$

01.06.21.1432.01

$$\int \frac{e^{pz}}{(a + b \sin(cz))^2} dz =$$

$$\frac{i e^{(ic+p)z}}{b(a^2 - b^2)^{3/2} (ic + p)} \left( -a(a + \sqrt{a^2 - b^2}) {}_2F_1\left(1 - \frac{ip}{c}, 1; 2 - \frac{ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}}\right) + a(a - \sqrt{a^2 - b^2}) \right.$$

$${}_2F_1\left(1 - \frac{ip}{c}, 1; 2 - \frac{ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}}\right) + (a^2 + \sqrt{a^2 - b^2} a - b^2) {}_2F_1\left(1 - \frac{ip}{c}, 2; 2 - \frac{ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}}\right) +$$

$$\left. (-a^2 + \sqrt{a^2 - b^2} a + b^2) {}_2F_1\left(1 - \frac{ip}{c}, 2; 2 - \frac{ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}}\right) \right)$$

Involving  $\frac{e^{pz}}{a+b \sin^2(cz)}$

01.06.21.1433.01

$$\int \frac{e^{pz}}{a + b \sin^2(cz)} dz = -\frac{1}{\sqrt{a} b \sqrt{a+b} (-2ic+p)} \left( e^{(-2ic+p)z} \left( (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1\left(\frac{ip}{2c}+1, 1; \frac{ip}{2c}+2; \frac{be^{-2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) + (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1\left(\frac{ip}{2c}+1, 1; \frac{ip}{2c}+2; \frac{be^{-2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) \right)$$

**Involving  $e^{pz}(a + b \sin^2(cz))^{-n}$**

01.06.21.1434.01

$$\int \frac{e^{pz}}{(a + b \sin^2(cz))^2} dz = -\frac{1}{2a^{3/2} b (a+b)^{3/2} (2ic+p)} \left( e^{(2ic+p)z} \left( (2a+b) (-2a+2\sqrt{a+b}\sqrt{a}-b) {}_2F_1\left(1-\frac{ip}{2c}, 1; 2-\frac{ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) + (2a+b) (2a+2\sqrt{a+b}\sqrt{a}+b) {}_2F_1\left(1-\frac{ip}{2c}, 1; 2-\frac{ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) + 2\sqrt{a} \left( (2a^{3/2}-2\sqrt{a+b}a+2b\sqrt{a}-b\sqrt{a+b}) {}_2F_1\left(1-\frac{ip}{2c}, 2; 2-\frac{ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) - (2a^{3/2}+2\sqrt{a+b}a+2b\sqrt{a}+b\sqrt{a+b}) {}_2F_1\left(1-\frac{ip}{2c}, 2; 2-\frac{ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) \right) \right)$$

**Involving  $\frac{e^{pz} \sin(dz)}{a+b \sin(cz)}$**

01.06.21.1435.01

$$\int \frac{e^{pz} \sin(dz)}{a + b \sin(cz)} dz = \frac{i}{2b\sqrt{a^2-b^2}} \left( \frac{1}{c+d-ip} e^{(ic+id+p)z} \left( (a+\sqrt{a^2-b^2}) {}_2F_1\left(\frac{c+d-ip}{c}, 1; \frac{2c+d-ip}{c}; \frac{ibe^{icz}}{a-\sqrt{a^2-b^2}}\right) + (\sqrt{a^2-b^2}-a) {}_2F_1\left(\frac{c+d-ip}{c}, 1; \frac{2c+d-ip}{c}; \frac{ibe^{icz}}{a+\sqrt{a^2-b^2}}\right) \right) - \frac{1}{c-d-ip} e^{(ic-id+p)z} \left( (a+\sqrt{a^2-b^2}) {}_2F_1\left(\frac{c-d-ip}{c}, 1; -\frac{-2c+d+ip}{c}; \frac{ibe^{icz}}{a-\sqrt{a^2-b^2}}\right) + (\sqrt{a^2-b^2}-a) {}_2F_1\left(\frac{c-d-ip}{c}, 1; -\frac{-2c+d+ip}{c}; \frac{ibe^{icz}}{a+\sqrt{a^2-b^2}}\right) \right) \right)$$



01.06.21.1437.01

$$\int \frac{e^{pz} \sin(dz)}{a + b \sin^2(cz)} dz = \frac{i}{2\sqrt{a} b \sqrt{a+b}}$$

$$\left( \frac{1}{-2ic + id + p} \left( e^{(-2ic + id + p)z} \left( (-2a + 2\sqrt{a+b} \sqrt{a} - b) {}_2F_1 \left( 1 - \frac{d-ip}{2c}, 1; 2 - \frac{d-ip}{2c}; \frac{b e^{-2icz}}{2a + 2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right. \right.$$

$$\left. \left. \left. (2a + 2\sqrt{a+b} \sqrt{a} + b) {}_2F_1 \left( 1 - \frac{d-ip}{2c}, 1; 2 - \frac{d-ip}{2c}; \frac{b e^{-2icz}}{2a - 2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) - \frac{1}{2c + d + ip}$$

$$\left( i e^{(-2ic - id + p)z} \left( (-2a + 2\sqrt{a+b} \sqrt{a} - b) {}_2F_1 \left( \frac{2c + d + ip}{2c}, 1; \frac{4c + d + ip}{2c}; \frac{b e^{-2icz}}{2a + 2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right.$$

$$\left. \left. \left. (2a + 2\sqrt{a+b} \sqrt{a} + b) {}_2F_1 \left( \frac{2c + d + ip}{2c}, 1; \frac{4c + d + ip}{2c}; \frac{b e^{-2icz}}{2a - 2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) \right)$$

01.06.21.1438.01

$$\int \frac{e^{pz} \sin(cz)}{a + b \sin^2(cz)} dz =$$

$$\frac{i}{2\sqrt{a} b \sqrt{a+b}} \left( \frac{1}{-ic + p} \left( e^{(-ic + p)z} \left( (-2a + 2\sqrt{a+b} \sqrt{a} - b) {}_2F_1 \left( \frac{c + ip}{2c}, 1; \frac{ip}{2c} + \frac{3}{2}; \frac{b e^{-2icz}}{2a + 2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right. \right.$$

$$\left. \left. \left. (2a + 2\sqrt{a+b} \sqrt{a} + b) {}_2F_1 \left( \frac{c + ip}{2c}, 1; \frac{ip}{2c} + \frac{3}{2}; \frac{b e^{-2icz}}{2a - 2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) -$$

$$\frac{1}{-3ic + p} \left( e^{(-3ic + p)z} \left( (-2a + 2\sqrt{a+b} \sqrt{a} - b) {}_2F_1 \left( \frac{ip}{2c} + \frac{3}{2}, 1; \frac{ip}{2c} + \frac{5}{2}; \frac{b e^{-2icz}}{2a + 2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right.$$

$$\left. \left. \left. (2a + 2\sqrt{a+b} \sqrt{a} + b) {}_2F_1 \left( \frac{ip}{2c} + \frac{3}{2}, 1; \frac{ip}{2c} + \frac{5}{2}; \frac{b e^{-2icz}}{2a - 2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) \right)$$

Involving  $e^{pz}(a + b \sin^2(cz))^{-n} \sin(dz)$

01.06.21.1439.01

$$\int \frac{e^{pz} \sin(dz)}{(a+b \sin^2(cz))^2} dz = \frac{i}{4a^{3/2} b(a+b)^{3/2}} \left( \frac{1}{2ic+id+p} e^{(2ic+id+p)z} \right. \\ \left. \left( (2a+b) \left( -2a+2\sqrt{a+b} \sqrt{a-b} \right) {}_2F_1 \left( \frac{2c+d-ip}{2c}, 1; \frac{4c+d-ip}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right. \\ \left. (2a+b) \left( 2a+2\sqrt{a+b} \sqrt{a+b} \right) {}_2F_1 \left( \frac{2c+d-ip}{2c}, 1; \frac{4c+d-ip}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) + 2\sqrt{a} \right. \\ \left. \left( \left( 2a^{3/2} - 2\sqrt{a+b} a + 2b\sqrt{a-b} \sqrt{a+b} \right) {}_2F_1 \left( \frac{2c+d-ip}{2c}, 2; \frac{4c+d-ip}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) - \right. \right. \\ \left. \left( 2a^{3/2} + 2\sqrt{a+b} a + 2b\sqrt{a+b} \sqrt{a+b} \right) \right. \\ \left. \left. {}_2F_1 \left( \frac{2c+d-ip}{2c}, 2; \frac{4c+d-ip}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) - \frac{1}{2ic-id+p} e^{(2ic-id+p)z} \\ \left( (2a+b) \left( -2a+2\sqrt{a+b} \sqrt{a-b} \right) {}_2F_1 \left( 1 - \frac{d+ip}{2c}, 1; 2 - \frac{d+ip}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \\ \left. (2a+b) \left( 2a+2\sqrt{a+b} \sqrt{a+b} \right) {}_2F_1 \left( 1 - \frac{d+ip}{2c}, 1; 2 - \frac{d+ip}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \\ \left. 2\sqrt{a} \left( \left( 2a^{3/2} - 2\sqrt{a+b} a + 2b\sqrt{a-b} \sqrt{a+b} \right) {}_2F_1 \left( 1 - \frac{d+ip}{2c}, 2; 2 - \frac{d+ip}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) - \right. \right. \\ \left. \left. \left( 2a^{3/2} + 2\sqrt{a+b} a + 2b\sqrt{a+b} \sqrt{a+b} \right) {}_2F_1 \left( 1 - \frac{d+ip}{2c}, 2; 2 - \frac{d+ip}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) \right)$$

Involving  $\frac{e^{pz} \sin(ez) \sin(dz)}{a+b \sin(cz)}$

01.06.21.1440.01

$$\int \frac{e^{pz} \sin(ez) \sin(dz)}{a + b \sin(cz)} dz =$$

$$-\frac{1}{4b\sqrt{a^2-b^2}} \left( \frac{1}{c+d-e-ip} \left( e^{i(c+d-e-ip)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d-e-ip}{c}, 1; \frac{2c+d-e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) + \right. \right.$$

$$\left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( \frac{c+d-e-ip}{c}, 1; \frac{2c+d-e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) +$$

$$\frac{1}{c-d+e-ip} \left( e^{i(c-d+e-ip)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c-d+e-ip}{c}, 1; \frac{2c-d+e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) + \right.$$

$$\left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( \frac{c-d+e-ip}{c}, 1; \frac{2c-d+e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) -$$

$$\frac{1}{c+d+e-ip} \left( e^{i(c+d+e-ip)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d+e-ip}{c}, 1; \frac{2c+d+e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) + \right.$$

$$\left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( \frac{c+d+e-ip}{c}, 1; \frac{2c+d+e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) +$$

$$\frac{1}{-c+d+e+ip} \left( e^{i(c-d+e+ip)z} \left( (a + \sqrt{a^2-b^2}) {}_2F_1 \left( -\frac{-c+d+e+ip}{c}, 1; -\frac{-2c+d+e+ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) + \right.$$

$$\left. \left( \sqrt{a^2-b^2} - a \right) {}_2F_1 \left( -\frac{-c+d+e+ip}{c}, 1; -\frac{-2c+d+e+ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) \right) \right)$$

**Involving  $e^{pz} \sin(ez) \sin(dz) (a + b \sin(cz))^{-n}$**

01.06.21.1441.01

$$\int \frac{e^{pz} \sin(ez) \sin(dz)}{(a + b \sin(cz))^2} dz =$$

$$\frac{1}{4b(a^2-b^2)^{3/2}} \left( \frac{1}{c+d-e-ip} \left( e^{i(c+d-e-ip)z} \left( -a(a + \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d-e-ip}{c}, 1; \frac{2c+d-e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) + \right. \right.$$

$$\left. a(a - \sqrt{a^2-b^2}) {}_2F_1 \left( \frac{c+d-e-ip}{c}, 1; \frac{2c+d-e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2-b^2}} \right) \right) +$$

$$\left( a^2 + \sqrt{a^2-b^2} a - b^2 \right) {}_2F_1 \left( \frac{c+d-e-ip}{c}, 2; \frac{2c+d-e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2-b^2}} \right) \right) +$$



$$\begin{aligned}
 & \left( -a^2 + \sqrt{a^2 - b^2} a + b^2 \right) {}_2F_1 \left( \frac{c+d-e-ip}{c}, 2; \frac{2c+d-e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \frac{1}{c-d+e-ip} \left( e^{i(c-d+e-ip)z} \left( -a \left( a + \sqrt{a^2 - b^2} \right) {}_2F_1 \left( \frac{c-d+e-ip}{c}, 1; \frac{2c-d+e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}} \right) \right) + \right. \\
 & \quad a \left( a - \sqrt{a^2 - b^2} \right) {}_2F_1 \left( \frac{c-d+e-ip}{c}, 1; \frac{2c-d+e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \quad \left( a^2 + \sqrt{a^2 - b^2} a - b^2 \right) {}_2F_1 \left( \frac{c-d+e-ip}{c}, 2; \frac{2c-d+e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \quad \left( -a^2 + \sqrt{a^2 - b^2} a + b^2 \right) {}_2F_1 \left( \frac{c-d+e-ip}{c}, 2; \frac{2c-d+e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) \Bigg) - \\
 & \frac{1}{c+d+e-ip} \left( e^{i(c+d+e-ip)z} \left( -a \left( a + \sqrt{a^2 - b^2} \right) {}_2F_1 \left( \frac{c+d+e-ip}{c}, 1; \frac{2c+d+e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}} \right) \right) + \right. \\
 & \quad a \left( a - \sqrt{a^2 - b^2} \right) {}_2F_1 \left( \frac{c+d+e-ip}{c}, 1; \frac{2c+d+e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \quad \left( a^2 + \sqrt{a^2 - b^2} a - b^2 \right) {}_2F_1 \left( \frac{c+d+e-ip}{c}, 2; \frac{2c+d+e-ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \quad \left( -a^2 + \sqrt{a^2 - b^2} a + b^2 \right) {}_2F_1 \left( \frac{c+d+e-ip}{c}, 2; \frac{2c+d+e-ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) \Bigg) + \\
 & \frac{1}{-c+d+e+ip} \left( e^{i(c-i(d+e+ip))z} \left( -a \left( a + \sqrt{a^2 - b^2} \right) {}_2F_1 \left( -\frac{-c+d+e+ip}{c}, 1; -\frac{-2c+d+e+ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}} \right) \right) + \right. \\
 & \quad a \left( a - \sqrt{a^2 - b^2} \right) {}_2F_1 \left( -\frac{-c+d+e+ip}{c}, 1; -\frac{-2c+d+e+ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \quad \left( a^2 + \sqrt{a^2 - b^2} a - b^2 \right) {}_2F_1 \left( -\frac{-c+d+e+ip}{c}, 2; -\frac{-2c+d+e+ip}{c}; \frac{ib e^{icz}}{a - \sqrt{a^2 - b^2}} \right) \Bigg) + \\
 & \quad \left. \left( -a^2 + \sqrt{a^2 - b^2} a + b^2 \right) {}_2F_1 \left( -\frac{-c+d+e+ip}{c}, 2; -\frac{-2c+d+e+ip}{c}; \frac{ib e^{icz}}{a + \sqrt{a^2 - b^2}} \right) \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

**Involving**  $\frac{e^{pz} \sin(ez) \sin(dz)}{a+b \sin^2(cz)}$

01.06.21.1442.01

$$\int \frac{e^{pz} \sin(ez) \sin(dz)}{a+b \sin^2(cz)} dz =$$

$$-\frac{1}{4\sqrt{a} b \sqrt{a+b}} \left( \frac{1}{2c+d-e+ip} \left( i e^{(-2ic-id+ie+p)z} \left( (-2a+2\sqrt{a+b} \sqrt{a}-b) {}_2F_1 \left( \frac{2c+d-e+ip}{2c}, \right. \right. \right. \right.$$

$$\left. \left. \left. 1; \frac{4c+d-e+ip}{2c}; \frac{b e^{-2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + (2a+2\sqrt{a+b} \sqrt{a+b}) \right. \right. \right.$$

$$\left. \left. {}_2F_1 \left( \frac{2c+d-e+ip}{2c}, 1; \frac{4c+d-e+ip}{2c}; \frac{b e^{-2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) + \frac{1}{2c-d+e+ip}$$

$$\left( i e^{(-2ic+id-ie+p)z} \left( (-2a+2\sqrt{a+b} \sqrt{a}-b) {}_2F_1 \left( \frac{2c-d+e+ip}{2c}, 1; \frac{4c-d+e+ip}{2c}; \frac{b e^{-2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right.$$

$$\left. \left. (2a+2\sqrt{a+b} \sqrt{a+b}) {}_2F_1 \left( \frac{2c-d+e+ip}{2c}, 1; \frac{4c-d+e+ip}{2c}; \frac{b e^{-2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) -$$

$$\frac{1}{2c+d+e+ip} \left( i e^{-i(2c+d+e+ip)z} \left( (-2a+2\sqrt{a+b} \sqrt{a}-b) {}_2F_1 \left( \frac{2c+d+e+ip}{2c}, 1; \right. \right. \right.$$

$$\left. \left. \frac{4c+d+e+ip}{2c}; \frac{b e^{-2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + (2a+2\sqrt{a+b} \sqrt{a+b}) \right. \right.$$

$$\left. \left. {}_2F_1 \left( \frac{2c+d+e+ip}{2c}, 1; \frac{4c+d+e+ip}{2c}; \frac{b e^{-2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) - \frac{1}{-2ic+id+ie+p}$$

$$\left( e^{(-2ic+id+ie+p)z} \left( (-2a+2\sqrt{a+b} \sqrt{a}-b) {}_2F_1 \left( 1 - \frac{d+e-ip}{2c}, 1; 2 - \frac{d+e-ip}{2c}; \frac{b e^{-2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + \right. \right.$$

$$\left. \left. (2a+2\sqrt{a+b} \sqrt{a+b}) {}_2F_1 \left( 1 - \frac{d+e-ip}{2c}, 1; 2 - \frac{d+e-ip}{2c}; \frac{b e^{-2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) \right) \right) \right)$$

**Involving**  $e^{pz} \sin(ez) \sin(dz) (a+b \sin^2(cz))^{-n}$

01.06.21.1443.01

$$\int \frac{e^{pz} \sin(ez) \sin(dz)}{(a+b \sin^2(cz))^2} dz =$$

$$\frac{1}{8a^{3/2} b(a+b)^{3/2}} \left( -\frac{1}{2ic+id-ie+p} \left( e^{(2ic+id-ie+p)z} \left( (2a+b) \left( -2a+2\sqrt{a+b} \sqrt{a}-b \right) {}_2F_1 \left( \frac{2c+d-e-ip}{2c}, 1; \right. \right. \right. \right.$$

$$\left. \left. \frac{4c+d-e-ip}{2c}; \frac{b e^{2icz}}{2a+2\sqrt{a+b} \sqrt{a+b}} \right) + (2a+b) \left( 2a+2\sqrt{a+b} \sqrt{a+b} \right) {}_2F_1 \left( \frac{2c+d-e-ip}{2c}, \right. \right.$$

$$\left. \left. 1; \frac{4c+d-e-ip}{2c}; \frac{b e^{2icz}}{2a-2\sqrt{a+b} \sqrt{a+b}} \right) + 2\sqrt{a} \left( \left( 2a^{3/2} - 2\sqrt{a+b} a + 2b\sqrt{a} - b\sqrt{a+b} \right) \right. \right.$$

$$\begin{aligned}
 & {}_2F_1\left(\frac{2c+d-e-ip}{2c}, 2; \frac{4c+d-e-ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) - \left(2a^{3/2} + 2\sqrt{a+b}a + \right. \\
 & \left. 2b\sqrt{a+b}\sqrt{a+b}\right) {}_2F_1\left(\frac{2c+d-e-ip}{2c}, 2; \frac{4c+d-e-ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \Bigg) - \\
 & \frac{1}{2ic-id+ie+p} \left( e^{(2ic-id+ie+p)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a-b} \right) {}_2F_1\left(\frac{2c-d+e-ip}{2c}, \right. \right. \right. \\
 & \left. \left. \left. 1; \frac{4c-d+e-ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) \right) + \right. \\
 & \left. (2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a+b} \right) {}_2F_1\left(\frac{2c-d+e-ip}{2c}, 1; \frac{4c-d+e-ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) + \\
 & 2\sqrt{a} \left( \left( 2a^{3/2} - 2\sqrt{a+b}a + 2b\sqrt{a-b}\sqrt{a+b} \right) {}_2F_1\left(\frac{2c-d+e-ip}{2c}, 2; \frac{4c-d+e-ip}{2c}; \right. \right. \\
 & \left. \left. \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) - \left( 2a^{3/2} + 2\sqrt{a+b}a + 2b\sqrt{a+b}\sqrt{a+b} \right) \right. \\
 & \left. {}_2F_1\left(\frac{2c-d+e-ip}{2c}, 2; \frac{4c-d+e-ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) \Bigg) - \\
 & \frac{1}{2c+d+e-ip} \left( i e^{i(2c+d+e-ip)z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a-b} \right) {}_2F_1\left(\frac{2c+d+e-ip}{2c}, 1; \right. \right. \right. \\
 & \left. \left. \left. \frac{4c+d+e-ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) \right) + \right. \\
 & \left. (2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a+b} \right) {}_2F_1\left(\frac{2c+d+e-ip}{2c}, 1; \frac{4c+d+e-ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) + \\
 & 2\sqrt{a} \left( \left( 2a^{3/2} - 2\sqrt{a+b}a + 2b\sqrt{a-b}\sqrt{a+b} \right) {}_2F_1\left(\frac{2c+d+e-ip}{2c}, 2; \frac{4c+d+e-ip}{2c}; \right. \right. \\
 & \left. \left. \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) - \left( 2a^{3/2} + 2\sqrt{a+b}a + 2b\sqrt{a+b}\sqrt{a+b} \right) \right. \\
 & \left. {}_2F_1\left(\frac{2c+d+e-ip}{2c}, 2; \frac{4c+d+e-ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) \Bigg) + \\
 & \frac{1}{-2c+d+e+ip} \left( i e^{(2ic-i(d+e+ip))z} \left( (2a+b) \left( -2a+2\sqrt{a+b}\sqrt{a-b} \right) {}_2F_1\left(-\frac{-2c+d+e+ip}{2c}, 1; \right. \right. \right. \\
 & \left. \left. \left. -\frac{-4c+d+e+ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}}\right) \right) + (2a+b) \left( 2a+2\sqrt{a+b}\sqrt{a+b} \right) \right. \\
 & \left. {}_2F_1\left(-\frac{-2c+d+e+ip}{2c}, 1; -\frac{-4c+d+e+ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}}\right) \right) +
 \end{aligned}$$

$$2\sqrt{a} \left( \left( 2a^{3/2} - 2\sqrt{a+b} a + 2b\sqrt{a} - b\sqrt{a+b} \right) {}_2F_1 \left( -\frac{-2c+d+e+ip}{2c}, 2; -\frac{-4c+d+e+ip}{2c}; \frac{be^{2icz}}{2a+2\sqrt{a+b}\sqrt{a+b}} \right) - \left( 2a^{3/2} + 2\sqrt{a+b} a + 2b\sqrt{a} + b\sqrt{a+b} \right) {}_2F_1 \left( -\frac{-2c+d+e+ip}{2c}, 2; -\frac{-4c+d+e+ip}{2c}; \frac{be^{2icz}}{2a-2\sqrt{a+b}\sqrt{a+b}} \right) \right)$$

**Involving algebraic functions of the direct function and exponential function**

Involving exp

**Involving  $e^{pz} (a + b \sin(dz))^\beta$**

01.06.21.1444.01

$$\int e^{pz} (a + b \sin(dz))^\beta dz = \frac{e^{pz}}{p - id\beta} \left( 1 - \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right)^{-\beta} \left( 1 - \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}} \right)^{-\beta} (a + b \sin(dz))^\beta F_1 \left( -\frac{ip}{d} - \beta; -\beta, -\beta; -\frac{ip}{d} - \beta + 1; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, -\frac{ib e^{idz}}{\sqrt{a^2 - b^2} - a} \right)$$

**Involving  $e^{pz} (a + b \sin^2(dz))^\beta$**

01.06.21.1445.01

$$\int e^{pz} (a + b \sin^2(dz))^\beta dz = \frac{1}{p - 2id\beta} e^{pz} \left( 1 - \frac{be^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right)^{-\beta} \left( 1 - \frac{be^{2idz}}{2a+b+2\sqrt{a(a+b)}} \right)^{-\beta} \left( a - \frac{1}{4} b e^{-2idz} (-1 + e^{2idz})^2 \right)^\beta F_1 \left( -\frac{ip}{2d} - \beta; -\beta, -\beta; -\frac{ip}{2d} - \beta + 1; \frac{be^{2idz}}{2a+b+2\sqrt{a(a+b)}}, \frac{be^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right)$$

**Involving  $e^{pz} (a + b \sin(dz))^\beta \sin(cz)$**

01.06.21.1446.01

$$\int e^{pz} (a + b \sin(dz))^\beta \sin(cz) dz = i \left( 1 + \frac{ib e^{idz}}{\sqrt{a^2 - b^2} - a} \right)^{-\beta} \left( 1 - \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}} \right)^{-\beta} (a + b \sin(dz))^\beta$$

$$\left( e^{(ic+p)z} i(c + ip + d\beta) F_1 \left( \frac{c - ip - d\beta}{d}; -\beta, -\beta; \frac{c + d - ip - d\beta}{d}; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right) + \right.$$

$$\left. e^{(-ic+p)z} (ic + p - id\beta) F_1 \left( -\frac{c + ip + d\beta}{d}; -\beta, -\beta; -\frac{c + ip + d(\beta - 1)}{d}; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right) \right) / (2$$

$$(c - ip - d\beta)(c + ip + d\beta))$$

**Involving  $e^{pz}(a + b \sin^2(dz))^\beta \sin(cz)$**

01.06.21.1447.01

$$\int e^{pz} (a + b \sin^2(dz))^\beta \sin(cz) dz = \frac{1}{2(c^2 + (p - 2id\beta)^2)} \left( 1 - \frac{b e^{2idz}}{2a + b - 2\sqrt{a(a+b)}} \right)^{-\beta}$$

$$\left( 1 - \frac{b e^{2idz}}{2a + b + 2\sqrt{a(a+b)}} \right)^{-\beta} \left( a - \frac{1}{4} b e^{-2idz} (-1 + e^{2idz})^2 \right)^\beta \left( i e^{(-ic+p)z} (ic + p - 2id\beta) \right.$$

$$F_1 \left( -\frac{c + ip + 2d\beta}{2d}; -\beta, -\beta; -\frac{c + ip + 2d(\beta - 1)}{2d}; \frac{b e^{2idz}}{2a + b + 2\sqrt{a(a+b)}}, \frac{b e^{2idz}}{2a + b - 2\sqrt{a(a+b)}} \right) - e^{(ic+p)z}$$

$$\left. (c + ip + 2d\beta) F_1 \left( \frac{c - ip - 2d\beta}{2d}; -\beta, -\beta; \frac{c + 2d - ip - 2d\beta}{2d}; \frac{b e^{2idz}}{2a + b + 2\sqrt{a(a+b)}}, \frac{b e^{2idz}}{2a + b - 2\sqrt{a(a+b)}} \right) \right)$$

**Involving  $e^{pz} \sin(ez) \sin(cz) (a + b \sin(dz))^\beta$**

01.06.21.1448.01

$$\int e^{pz} \sin(ez) \sin(cz) (a + b \sin(dz))^\beta dz = \frac{1}{4} i \left( 1 + \frac{ib e^{idz}}{\sqrt{a^2 - b^2} - a} \right)^{-\beta} \left( 1 - \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}} \right)^{-\beta} (a + b \sin(dz))^\beta$$

$$\left( \frac{e^{(ic+ie+p)z}}{c+e-ip-d\beta} F_1 \left( \frac{c+e-ip-d\beta}{d}; -\beta, -\beta; \frac{c+d+e-ip-d\beta}{d}; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right) + \right.$$

$$\frac{e^{(-ic+ie+p)z}}{c-e+ip+d\beta} F_1 \left( -\frac{c-e+ip+d\beta}{d}; -\beta, -\beta; -\frac{c+d+e-ip-d\beta}{d}; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right) +$$

$$\frac{e^{(ic-ie+p)z}}{-c+e+ip+d\beta} F_1 \left( -\frac{-c+e+ip+d\beta}{d}; -\beta, -\beta; \frac{c+d-e-ip-d\beta}{d}; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right) -$$

$$\left. \frac{e^{-i(c+e+p)z}}{c+e+ip+d\beta} F_1 \left( -\frac{c+e+ip+d\beta}{d}; -\beta, -\beta; -\frac{c+e+ip+d(\beta-1)}{d}; \frac{ib e^{idz}}{a + \sqrt{a^2 - b^2}}, \frac{ib e^{idz}}{a - \sqrt{a^2 - b^2}} \right) \right)$$

**Involving  $e^{pz} \sin(ez) \sin(cz) (a + b \sin^2(dz))^\beta$**

01.06.21.1449.01

$$\int e^{pz} \sin(ez) \sin(cz) (a + b \sin^2(dz))^\beta dz =$$

$$\frac{1}{4} i \left( 1 - \frac{b e^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right)^{-\beta} \left( 1 - \frac{b e^{2idz}}{2a+b+2\sqrt{a(a+b)}} \right)^{-\beta} \left( a - \frac{1}{4} b e^{-2idz} (-1 + e^{2idz})^2 \right)^\beta$$

$$\left( \frac{e^{(ic+ie+p)z}}{c+e-ip-2d\beta} F_1 \left( \frac{c+e-ip-2d\beta}{2d}; -\beta, -\beta; \frac{c+2d+e-ip-2d\beta}{2d}; \frac{b e^{2idz}}{2a+b+2\sqrt{a(a+b)}}, \right.$$

$$\frac{b e^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right) + \frac{e^{(-ic+ie+p)z}}{c-e+ip+2d\beta} F_1 \left( -\frac{c-e+ip+2d\beta}{2d}; -\beta, -\beta; -\frac{c-e+ip+2d(\beta-1)}{2d}; \right.$$

$$\frac{b e^{2idz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right) - \frac{e^{(ic-ie+p)z}}{c-e-ip-2d\beta} F_1 \left( -\frac{-c+e+ip+2d\beta}{2d}; -\beta, \right.$$

$$\left. -\beta; \frac{c+2d-e-ip-2d\beta}{2d}; \frac{b e^{2idz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right) - \frac{e^{-i(c+e+p)z}}{c+e+ip+2d\beta}$$

$$F_1 \left( -\frac{c+e+ip+2d\beta}{2d}; -\beta, -\beta; -\frac{c+e+ip+2d(\beta-1)}{2d}; \frac{b e^{2idz}}{2a+b+2\sqrt{a(a+b)}}, \frac{b e^{2idz}}{2a+b-2\sqrt{a(a+b)}} \right)$$

**Involving functions of the direct function, exponential and a power functions**

**Involving powers of the direct function, exponential and a power functions**

Involving powers of sin, exp and power

### Involving $z^{\alpha-1} e^{bz} \sin^v(az)$

01.06.21.1450.01

$$\int z^n e^{bz} \sin^v(az) dz = n! e^{bz} \sin^v(az) (1 - e^{2ia z})^{-v}$$

$$\sum_{p=0}^n \frac{(-1)^p z^{n-p}}{(n-p)! (b-ia v)^{p+1}} {}_{p+2}F_{p+1} \left( -\frac{ib+av}{2a}, \dots, -\frac{ib+av}{2a}, -v; 1 - \frac{ib+av}{2a}, \dots, 1 - \frac{ib+av}{2a}; e^{2iaz} \right); n \in \mathbb{N}$$

01.06.21.1451.01

$$\int z^{\alpha-1} e^{bz} \sin^v(az) dz = -2^{-v} \binom{v}{\frac{v}{2}} E_{1-\alpha}(-bz) (1 - v \bmod 2) z^\alpha -$$

$$2^{-v} z^\alpha \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{-\frac{i\pi v}{2}} (E_{1-\alpha}(-(b+ai(v-2k))z) + (-1)^v E_{1-\alpha}(-(b-ia(v-2k))z)); v \in \mathbb{N}$$

01.06.21.1452.01

$$\int z^n e^{pz} \sin^v(az) dz = -2^{-v} \binom{v}{\frac{v}{2}} E_{-n}(-pz) (1 - v \bmod 2) z^{n+1} -$$

$$2^{-v} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-\frac{i\pi v}{2}} \binom{v}{s} ((-1)^v E_{-n}((ia(v-2s)-p)z) + E_{-n}((-p-ia(v-2s))z)); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1453.01

$$\int z^n e^{pz} \sin^v(az) dz = -2^{-v} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) (-p)^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}(pz)}{(-n-1)!} + e^{pz} \sum_{k=0}^n \frac{(-pz)^k}{(n+1)_{k-n}} - e^{pz} \sum_{k=n+1}^{-1} \frac{(-pz)^k}{(n+1)_{k-n}} \right) -$$

$$2^{-v} z^{n+1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \left( \frac{(-1)^{-n} \text{Ei}(-ia(v-2s)-p)z}{(-n-1)!} + e^{-ia(v-2s)-p}z \sum_{k=0}^n \frac{((ia(v-2s)-p)z)^k}{(n+1)_{k-n}} - \right. \right.$$

$$\left. \left. e^{-ia(v-2s)-p}z \sum_{k=n+1}^{-1} \frac{((ia(v-2s)-p)z)^k}{(n+1)_{k-n}} \right) ((ia(v-2s)-p)z)^{-n-1} + \right.$$

$$\left. ((-p-ia(v-2s))z)^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}(-(-p-ia(v-2s))z)}{(-n-1)!} + e^{-(-p-ia(v-2s))z} \sum_{k=0}^n \frac{((-p-ia(v-2s))z)^k}{(n+1)_{k-n}} - \right. \right.$$

$$\left. \left. e^{-(-p-ia(v-2s))z} \sum_{k=n+1}^{-1} \frac{((-p-ia(v-2s))z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1454.01

$$\int z^{n+\frac{1}{2}} e^{pz} \sin^v(az) dz = -2^{-v} \binom{v}{\frac{v}{2}} E_{-n-\frac{1}{2}}(-pz) (1 - v \bmod 2) z^{n+\frac{3}{2}} -$$

$$2^{-v} i^{-v} z^{n+\frac{3}{2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v E_{-n-\frac{1}{2}}((ia(v-2s)-p)z) + E_{-n-\frac{1}{2}}((-p-ia(v-2s))z) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1455.01

$$\int z^{n+\frac{1}{2}} e^{pz} \sin^v(a z) dz =$$

$$-2^{-v} (-p)^{-n-2} z^{-\frac{1}{2}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sqrt{-p z} \left( \operatorname{erfc}(\sqrt{-p z}) \Gamma\left(n + \frac{3}{2}\right) + e^{pz} \sum_{k=0}^n \frac{(-p z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - e^{pz} \sum_{k=n+1}^{-1} \frac{(-p z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) -$$

$$2^{-v} z^{n+\frac{3}{2}} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \left( \operatorname{erfc}(\sqrt{(i a (v-2s) - p) z}) \Gamma\left(n + \frac{3}{2}\right) + e^{-i a (v-2s) - p} z \sum_{k=0}^n \frac{((i a (v-2s) - p) z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - \right.$$

$$\left. e^{-i a (v-2s) - p} z \sum_{k=n+1}^{-1} \frac{((i a (v-2s) - p) z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) ((i a (v-2s) - p) z)^{-n-\frac{3}{2}} +$$

$$((-p - i a (v-2s) z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}(\sqrt{(-p - i a (v-2s) z})} \Gamma\left(n + \frac{3}{2}\right) + e^{-(-p - i a (v-2s) z)} \right.$$

$$\left. \sum_{k=0}^n \frac{((-p - i a (v-2s) z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} - e^{-(-p - i a (v-2s) z)} \sum_{k=n+1}^{-1} \frac{((-p - i a (v-2s) z)^{k+\frac{1}{2}}}{\left(n + \frac{3}{2}\right)_{k-n}} \right) \Bigg) /; n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1456.01

$$\int z e^{bz} \sin^2(a z) dz =$$

$$\frac{1}{2(b^3 + 4a^2 b)^2} \left( e^{bz} \left( -(4(bz + 1)a^2 + b^2(bz - 1)) \cos(2az) b^2 - 2a(4za^2 - 2b + b^2z) \sin(2az) b^2 + (4a^2 + b^2)^2 (bz - 1) \right) \right)$$

### Involving $z^{\alpha-1} e^{bz+e} \sin^v(a z)$

01.06.21.1457.01

$$\int z^n e^{bz+e} \sin^v(a z) dz = n! e^{bz+e} \sin^v(a z) (1 - e^{2i a z})^{-v}$$

$$\sum_{p=0}^n \frac{(-1)^p z^{n-p}}{(n-p)! (b - i a v)^{p+1}} {}_{p+2}F_{p+1} \left( -\frac{i b + a v}{2 a}, \dots, -\frac{i b + a v}{2 a}, -v; 1 - \frac{i b + a v}{2 a}, \dots, 1 - \frac{i b + a v}{2 a}; e^{2i a z} \right) /; n \in \mathbb{N}$$

01.06.21.1458.01

$$\int z^{\alpha-1} e^{e+bz} \sin^v(a z) dz = -2^{-v} e^e \left( \frac{v}{2} \right) E_{1-\alpha}(-b z) (1 - v \bmod 2) z^\alpha -$$

$$2^{-v} z^\alpha \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{-\frac{i \pi v}{2}} (E_{1-\alpha}(-(b + a i (v-2k)) z) + (-1)^v E_{1-\alpha}(-(b - i a (v-2k)) z)) /; v \in \mathbb{N}$$



01.06.21.1459.01

$$\int z^n e^{e+pz} \sin^v(a z) dz = -2^{-v} e^e \left(\frac{v}{2}\right) E_{-n}(-p z) (1 - v \bmod 2) z^{n+1} - 2^{-v} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{e - \frac{i\pi v}{2}} \binom{v}{s} \left( (-1)^v E_{-n}((i a (v - 2 s) - p) z) + E_{-n}((-p - i a (v - 2 s)) z) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1460.01

$$\int z^n e^{p z+e} \sin^v(a z) dz = -2^{-v} e^e \left(\frac{v}{2}\right) (1 - v \bmod 2) (-p)^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}(p z)}{(-n-1)!} + e^{p z} \sum_{k=0}^n \frac{(-p z)^k}{(n+1)_{k-n}} - e^{p z} \sum_{k=n+1}^{-1} \frac{(-p z)^k}{(n+1)_{k-n}} \right) - 2^{-v} z^{n+1} i^{-v} e^e \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \left( \frac{(-1)^{-n} \operatorname{Ei}(-i a (v - 2 s) - p) z}{(-n-1)!} + e^{-i a (v - 2 s) - p} z \sum_{k=0}^n \frac{(i a (v - 2 s) - p) z^k}{(n+1)_{k-n}} - e^{-i a (v - 2 s) - p} z \sum_{k=n+1}^{-1} \frac{(i a (v - 2 s) - p) z^k}{(n+1)_{k-n}} \right) ((i a (v - 2 s) - p) z)^{-n-1} + ((-p - i a (v - 2 s)) z)^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}(-(-p - i a (v - 2 s)) z)}{(-n-1)!} + e^{-(-p - i a (v - 2 s)) z} \sum_{k=0}^n \frac{((-p - i a (v - 2 s)) z)^k}{(n+1)_{k-n}} - e^{-(-p - i a (v - 2 s)) z} \sum_{k=n+1}^{-1} \frac{((-p - i a (v - 2 s)) z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1461.01

$$\int z^{n+\frac{1}{2}} e^{p z+e} \sin^v(a z) dz = -2^{-v} e^e \left(\frac{v}{2}\right) E_{-n-\frac{1}{2}}(-p z) (1 - v \bmod 2) z^{n+\frac{3}{2}} - 2^{-v} i^{-v} z^{n+\frac{3}{2}} e^e \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v E_{-n-\frac{1}{2}}((i a (v - 2 s) - p) z) + E_{-n-\frac{1}{2}}((-p - i a (v - 2 s)) z) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1462.01

$$\int z^{n+\frac{1}{2}} e^{e+pz} \sin^v(a z) dz =$$

$$-2^{-v} e^e (-p)^{-n-2} z^{-\frac{1}{2}} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( \operatorname{erfc}(\sqrt{-p z}) \Gamma\left(n+\frac{3}{2}\right) + e^{p z} \sum_{k=0}^n \frac{(-p z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{p z} \sum_{k=n+1}^{-1} \frac{(-p z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \sqrt{-p z} -$$

$$2^{-v} z^{n+\frac{3}{2}} i^{-v} e^e \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \left( \operatorname{erfc}(\sqrt{(i a (v-2 s)-p) z}) \Gamma\left(n+\frac{3}{2}\right) + e^{-i a (v-2 s)-p} z \sum_{k=0}^n \frac{((i a (v-2 s)-p) z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - \right.$$

$$\left. e^{-i a (v-2 s)-p} z \sum_{k=n+1}^{-1} \frac{((i a (v-2 s)-p) z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) ((i a (v-2 s)-p) z)^{-n-\frac{3}{2}} +$$

$$\left( (-p-i a (v-2 s) z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}(\sqrt{(-p-i a (v-2 s) z)}) \Gamma\left(n+\frac{3}{2}\right) + e^{-(-p-i a (v-2 s) z)} \right. \right.$$

$$\left. \left. \sum_{j=0}^n \frac{((-p-i a (v-2 s) z)^{j+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{j-n}} - e^{-(-p-i a (v-2 s) z)} \sum_{k=n+1}^{-1} \frac{((-p-i a (v-2 s) z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \right) /; n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

### Involving $z^{\alpha-1} e^{p z} \sin^v(a z + b)$

01.06.21.1463.01

$$\int z^n e^{p z} \sin^v(a z + b) dz = n! e^{p z} \sin^v(b + a z) (1 - e^{2i(b+az)})^{-v}$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (p-i a v)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{i p + a v}{2 a}, \dots, -\frac{i p + a v}{2 a}, -v; 1 - \frac{i p + a v}{2 a}, \dots, 1 - \frac{i p + a v}{2 a}; e^{2i(b+az)} \right); n \in \mathbb{N}^+$$

01.06.21.1464.01

$$\int z^{\alpha-1} e^{p z} \sin^v(b + a z) dz = -2^{-v} \binom{v}{\frac{v}{2}} E_{1-\alpha}(-p z) (1-v \bmod 2) z^\alpha -$$

$$2^{-v} z^\alpha \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{-\frac{1}{2} i (\pi v + 2 b (2k+v))} \left( e^{2 i b v} E_{1-\alpha}(-(p + a i (v-2 k)) z) + e^{i (4 b k + \pi v)} E_{1-\alpha}(-(p - i a (v-2 k)) z) \right); v \in \mathbb{N}$$

01.06.21.1465.01

$$\int z^n e^{p z} \sin^v(a z + b) dz = -2^{-v} \binom{v}{\frac{v}{2}} E_{-n}(-p z) (1-v \bmod 2) z^{n+1} - 2^{-v} z^{n+1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-\frac{1}{2} i (\pi v + 2 b (2s+v))} \binom{v}{s} \left( e^{i (4 b s + \pi v)} E_{-n}((i a (v-2 s)-p) z) + e^{2 i b v} E_{-n}((-p-i a (v-2 s)) z) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1466.01

$$\int z^n e^{pz} \sin^v(az+b) dz =$$

$$-2^{-v} (-p)^{-n-1} \left(\frac{v}{2}\right) (1-v \bmod 2) \left( \frac{(-1)^{-n} \operatorname{Ei}(pz)}{(-n-1)!} + e^{pz} \sum_{k=0}^n \frac{(-pz)^k}{(n+1)_{k-n}} - e^{pz} \sum_{k=n+1}^{-1} \frac{(-pz)^k}{(n+1)_{k-n}} \right) - 2^{-v} z^{n+1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-\frac{1}{2}i(\pi v + 2b(2s+v))} \binom{v}{s} \left( e^{i(4bs+\pi v)} \left( \frac{(-1)^{-n} \operatorname{Ei}(-ia(v-2s)-p)z}{(-n-1)!} + e^{-ia(v-2s)-p)z} \sum_{k=0}^n \frac{((ia(v-2s)-p)z)^k}{(n+1)_{k-n}} - \right. \right.$$

$$\left. e^{-ia(v-2s)-p)z} \sum_{k=n+1}^{-1} \frac{((ia(v-2s)-p)z)^k}{(n+1)_{k-n}} \right) ((ia(v-2s)-p)z)^{-n-1} +$$

$$e^{2ibv} ((-p-ia(v-2s))z)^{-n-1} \left( \frac{(-1)^{-n} \operatorname{Ei}(-(-p-ia(v-2s))z)}{(-n-1)!} + e^{-(-p-ia(v-2s))z} \sum_{k=0}^n \frac{((-p-ia(v-2s))z)^k}{(n+1)_{k-n}} - \right.$$

$$\left. e^{-(-p-ia(v-2s))z} \sum_{k=n+1}^{-1} \frac{((-p-ia(v-2s))z)^k}{(n+1)_{k-n}} \right) \Bigg) ; n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1467.01

$$\int z^{n+\frac{1}{2}} e^{pz} \sin^v(az+b) dz = -2^{-v} \binom{v}{\frac{v}{2}} E_{-n-\frac{1}{2}}(-pz) (1-v \bmod 2) z^{n+\frac{3}{2}} -$$

$$2^{-v} z^{n+\frac{3}{2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-\frac{1}{2}i(\pi v + 2b(2s+v))} \binom{v}{s} \left( e^{i(4bs+\pi v)} E_{-n-\frac{1}{2}}((ia(v-2s)-p)z) + e^{2ibv} E_{-n-\frac{1}{2}}((-p-ia(v-2s))z) \right) ; n \in$$

$$\mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1468.01

$$\int z^{n+\frac{1}{2}} e^{pz} \sin^v(az+b) dz =$$

$$-2^{-v} (-p)^{-n-2} z^{\frac{1}{2}} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( \operatorname{erfc}(\sqrt{-pz}) \Gamma\left(n+\frac{3}{2}\right) + e^{pz} \sum_{k=0}^n \frac{(-pz)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{pz} \sum_{k=n+1}^{-1} \frac{(-pz)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \sqrt{-pz} -$$

$$2^{-v} z^{n+\frac{3}{2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{-\frac{1}{2}i(\pi v + 2b(2s+v))} \binom{v}{s} \left( e^{i(4bs+\pi v)} \left( \operatorname{erfc}(\sqrt{(ia(v-2s)-p)z}) \Gamma\left(n+\frac{3}{2}\right) + e^{-ia(v-2s)-p)z} \right. \right.$$

$$\left. \sum_{k=0}^n \frac{((ia(v-2s)-p)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{-ia(v-2s)-p)z} \sum_{k=n+1}^{-1} \frac{((ia(v-2s)-p)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) ((ia(v-2s)-p)z)^{-n-\frac{3}{2}} +$$

$$e^{2ibv} ((-p-ia(v-2s))z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}(\sqrt{(-p-ia(v-2s))z}) \Gamma\left(n+\frac{3}{2}\right) + e^{-(-p-ia(v-2s))z} \right.$$

$$\left. \sum_{k=0}^n \frac{((-p-ia(v-2s))z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{-(-p-ia(v-2s))z} \sum_{k=n+1}^{-1} \frac{((-p-ia(v-2s))z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \Bigg) ; n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

### Involving $z^{\alpha-1} e^{pz+e} \sin^v(az+b)$

01.06.21.1469.01

$$\int z^n e^{pz+e} \sin^v(az+b) dz = n! e^{pz+e} \sin^v(b+az) (1 - e^{2i(b+az)})^{-v}$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (p-ia v)^{j+1}} {}_{j+2}F_{j+1}\left(-\frac{ip+av}{2a}, \dots, -\frac{ip+av}{2a}, -v; 1 - \frac{ip+av}{2a}, \dots, 1 - \frac{ip+av}{2a}; e^{2i(b+az)}\right); n \in \mathbb{N}^+$$

01.06.21.1470.01

$$\int z^{\alpha-1} e^{pz+e} \sin^v(b+az) dz = -2^{-v} e^e \left(\frac{v}{2}\right) E_{1-\alpha}(-pz) (1 - v \bmod 2) z^\alpha -$$

$$2^{-v} z^\alpha \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} e^{e - \frac{1}{2} i(\pi v + 2b(2k+v))} (e^{2ibv} E_{1-\alpha}(-(p+ai(v-2k))z) + e^{i(4bk+\pi v)} E_{1-\alpha}(-(p-ia(v-2k))z)); v \in \mathbb{N}$$

01.06.21.1471.01

$$\int z^n e^{pz+e} \sin^v(az+b) dz = -2^{-v} e^e \left(\frac{v}{2}\right) E_{-n}(-pz) (1 - v \bmod 2) z^{n+1} - 2^{-v} z^{n+1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{e - \frac{1}{2} i(\pi v + 2b(2s+v))} \binom{v}{s} (e^{i(4bs+\pi v)} E_{-n}((ia(v-2s)-p)z) + e^{2ibv} E_{-n}((-p-ia(v-2s))z)); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1472.01

$$\int z^n e^{pz+e} \sin^v(az+b) dz =$$

$$-2^{-v} (-p)^{-n-1} e^e \left(\frac{v}{2}\right) (1 - v \bmod 2) \left( \frac{(-1)^{-n} \text{Ei}(pz)}{(-n-1)!} + e^{pz} \sum_{k=0}^n \frac{(-pz)^k}{(n+1)_{k-n}} - e^{pz} \sum_{k=n+1}^{-1} \frac{(-pz)^k}{(n+1)_{k-n}} \right) - 2^{-v} z^{n+1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{e - \frac{1}{2} i(\pi v + 2b(2s+v))} \binom{v}{s} \left( e^{i(4bs+\pi v)} \left( \frac{(-1)^{-n} \text{Ei}(-ia(v-2s)-pz)}{(-n-1)!} + e^{-ia(v-2s)-pz} \sum_{k=0}^n \frac{((ia(v-2s)-p)z)^k}{(n+1)_{k-n}} - \right. \right.$$

$$\left. \left. e^{-ia(v-2s)-pz} \sum_{k=n+1}^{-1} \frac{((ia(v-2s)-p)z)^k}{(n+1)_{k-n}} \right) ((ia(v-2s)-p)z)^{-n-1} + \right.$$

$$\left. e^{2ibv} ((-p-ia(v-2s))z)^{-n-1} \left( \frac{(-1)^{-n} \text{Ei}(-(-p-ia(v-2s))z)}{(-n-1)!} + e^{-(-p-ia(v-2s))z} \sum_{k=0}^n \frac{((-p-ia(v-2s))z)^k}{(n+1)_{k-n}} - \right. \right.$$

$$\left. \left. e^{-(-p-ia(v-2s))z} \sum_{k=n+1}^{-1} \frac{((-p-ia(v-2s))z)^k}{(n+1)_{k-n}} \right) \right); n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1473.01

$$\int z^{n+\frac{1}{2}} e^{pz+e} \sin^v(az+b) dz = -2^{-v} e^e \left(\frac{v}{2}\right) E_{-n-\frac{1}{2}}(-pz) (1 - v \bmod 2) z^{n+\frac{3}{2}} -$$

$$2^{-v} z^{n+\frac{3}{2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{e - \frac{1}{2} i(\pi v + 2b(2s+v))} \binom{v}{s} \left( e^{i(4bs+\pi v)} E_{-n-\frac{1}{2}}((ia(v-2s)-p)z) + e^{2ibv} E_{-n-\frac{1}{2}}((-p-ia(v-2s))z) \right); n \in$$

$$\mathbb{Z} \wedge v \in \mathbb{N}$$

01.06.21.1474.01

$$\int z^{n+\frac{1}{2}} e^{pz+e} \sin^v(az+b) dz =$$

$$-2^{-v} (-p)^{-n-2} z^{-\frac{1}{2}} e^e \left(\frac{v}{2}\right) (1-v \bmod 2) \left( \operatorname{erfc}(\sqrt{-pz}) \Gamma\left(n+\frac{3}{2}\right) + e^{pz} \sum_{k=0}^n \frac{(-pz)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{pz} \sum_{k=n+1}^{-1} \frac{(-pz)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \sqrt{-pz} -$$

$$2^{-v} z^{n+\frac{3}{2}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{e-\frac{1}{2}i(\pi v+2b(2s+v))} \binom{v}{s} \left( e^{i(4bs+\pi v)} \left( \operatorname{erfc}(\sqrt{(ia(v-2s)-p)z}) \Gamma\left(n+\frac{3}{2}\right) + e^{-(ia(v-2s)-p)z} \right. \right.$$

$$\left. \left. \sum_{k=0}^n \frac{((ia(v-2s)-p)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{-(ia(v-2s)-p)z} \sum_{k=n+1}^{-1} \frac{((ia(v-2s)-p)z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) ((ia(v-2s)-p)z)^{-n-\frac{3}{2}} + \right.$$

$$\left. e^{2ibv} ((-p-ia(v-2s))z)^{-n-\frac{3}{2}} \left( \operatorname{erfc}(\sqrt{(-p-ia(v-2s))z}) \Gamma\left(n+\frac{3}{2}\right) + e^{-(-p-ia(v-2s))z} \right. \right.$$

$$\left. \left. \sum_{k=0}^n \frac{((-p-ia(v-2s))z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} - e^{-(-p-ia(v-2s))z} \sum_{k=n+1}^{-1} \frac{((-p-ia(v-2s))z)^{k+\frac{1}{2}}}{\left(n+\frac{3}{2}\right)_{k-n}} \right) \right) /; n \in \mathbb{Z} \wedge v \in \mathbb{N}$$

### Involving $z^n e^{bz^r} \sin^v(cz)$

01.06.21.1475.01

$$\int z^n e^{bz^2} \sin^v(cz) dz = -i^{-v} 2^{-v-1} b^{-n-1}$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{\frac{c^2(v-2k)^2}{4b}} \binom{v}{k} \left( (-1)^v \sum_{q=0}^n \binom{n}{q} 2^{q-n} (ic(v-2k))^{n-q} (2ick-icv+2bz)^{q+1} \left( -\frac{(2ick-icv+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \Gamma\left(\frac{q+1}{2}, -\frac{(2ick-icv+2bz)^2}{4b}\right) + \sum_{q=0}^n \binom{n}{q} (ic\left(k-\frac{v}{2}\right))^{n-q} \right.$$

$$\left. (ci(v-2k)+2bz)^{q+1} \left( -\frac{(ci(v-2k)+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \Gamma\left(\frac{q+1}{2}, -\frac{(ci(v-2k)+2bz)^2}{4b}\right) \right) -$$

$$2^{-v-1} z^{n+1} (-bz^2)^{\frac{1}{2}(-n-1)} \binom{v}{\frac{v}{2}} \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1476.01

$$\int z^n e^{b\sqrt{z}} \sin^v(cz) dz = i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{\frac{b^2}{8ics-4icv}} (-c^2(v-2s)^2)^{-2n-1} \binom{v}{s}$$

$$\left( (ic(2s-v))^{2n} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2ci(v-2s)\sqrt{z})^{h+k} \left( \frac{i(b+2ci(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2ci(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(b+2ci(v-2s)\sqrt{z})^2}{c(8s-4v)} \right) \right) + \right.$$

$$\left. 2ci \sqrt{-\frac{i(b+2ci(v-2s)\sqrt{z})^2}{c(2s-v)}} (v-2s) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(b+2ci(v-2s)\sqrt{z})^2}{c(8s-4v)} \right) \right) +$$

$$(-1)^v e^{\frac{b^2}{2icv-4ics}} (ic(v-2s))^{2n} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b-2ic(v-2s)\sqrt{z})^{h+k}$$

$$\left( -\frac{i(b-2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k}$$

$$\left( b(b-2ic(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(b-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) - \right.$$

$$\left. \left. 2ic(v-2s) \sqrt{-\frac{i(b-2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(b-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) \right) \right) -$$

$$2^{1-v} b^{-2n-2} \left( \frac{v}{2} \right) \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) /; n \in$$

$\mathbb{N} \wedge$   
 $v \in \mathbb{N}^+$

Involving  $z^n e^{bz^r+e} \sin^v(cz)$

01.06.21.1477.01

$$\int z^n e^{bz^2+e} \sin^v(cz) dz = -2^{-v-1} e^e z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(2ics-icv)^2}{4b}} \left( \sum_{q=0}^n 2^{q-n} (icv-2ics)^{n-q} (2ics-icv+2bz)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(2ics-icv+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ics-icv+2bz)^2}{4b}\right) \right) b^{-n-1} + \right.$$

$$\left. e^{-\frac{(icv-2ics)^2}{4b}} \left( \sum_{q=0}^n 2^{q-n} (2ics-icv)^{n-q} (ci(v-2s)+2bz)^{q+1} \left( -\frac{(ci(v-2s)+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right. \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ci(v-2s)+2bz)^2}{4b}\right) \right) b^{-n-1} \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1478.01

$$\int z^n e^{\sqrt{z} b+e} \sin^v(c z) dz = i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\left( (-1)^v e^{\frac{ib^2}{4c(2s-v)}+e} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2ci(2s-v)\sqrt{z})^{h+k} \left( \frac{i(b+2ci(2s-v)\sqrt{z})^2}{c(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \right. \right. \\ \left. \binom{k}{h} \binom{n}{k} \left( b(b+2ci(2s-v)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{i(b+2ci(2s-v)\sqrt{z})^2}{4c(2s-v)} \right) + 2ci(2s-v) \right. \right. \\ \left. \left. \sqrt{\frac{i(b+2ci(2s-v)\sqrt{z})^2}{c(2s-v)}} \Gamma \left( \frac{1}{2}(h+k+2), \frac{i(b+2ci(2s-v)\sqrt{z})^2}{4c(2s-v)} \right) \right) \right) (ic(2s-v))^{-2n-2} +$$

$$e^{\frac{ib^2}{4c(v-2s)}+e} (ic(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2ci(v-2s)\sqrt{z})^{h+k}$$

$$\left( \frac{i(b+2ci(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k}$$

$$\left( b(b+2ci(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{i(b+2ci(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) + \right.$$

$$\left. 2ci(v-2s) \sqrt{\frac{i(b+2ci(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma \left( \frac{1}{2}(h+k+2), \frac{i(b+2ci(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) \right) -$$

$$2^{1-v} (-b)^{-2(n+1)} e^e \left( \frac{v}{2} \right) \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) /; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

Involving  $z^n e^{bz'+dz} \sin^v(cz)$



01.06.21.1479.01

$$\int z^n e^{b z^2 + d z} \sin^v(c z) dz =$$

$$-2^{-v-1} e^{-\frac{d^2}{4b}} \left(\frac{v}{\frac{v}{2}}\right) (1 - v \bmod 2) b^{-n-1} \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d + 2bz)^{q+1} \left(-\frac{(d + 2bz)^2}{b}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2bz)^2}{4b}\right) -$$

$$i^{-v} 2^{-v-1} b^{-n-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(d+ic(v-2s))^2}{4b}} \sum_{q=0}^n \binom{n}{q} 2^{q-n} (-d + 2ics - icv)^{n-q} (d - 2ics + icv + 2bz)^{q+1} \right.$$

$$\left. \left(-\frac{(d - 2ics + icv + 2bz)^2}{b}\right)^{\frac{1}{2}(-q-1)} \Gamma\left(\frac{q+1}{2}, -\frac{(d - 2ics + icv + 2bz)^2}{4b}\right) + \right.$$

$$\left. (-1)^v e^{-\frac{(d+2ics-icv)^2}{4b}} \sum_{q=0}^n \binom{n}{q} 2^{q-n} (ic(v-2s) - d)^{n-q} (d + 2ics - icv + 2bz)^{q+1} \right.$$

$$\left. \left(-\frac{(d + 2ics - icv + 2bz)^2}{b}\right)^{\frac{1}{2}(-q-1)} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2ics - icv + 2bz)^2}{4b}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1480.01

$$\int z^n e^{\sqrt{z} b + d z} \sin^v(c z) dz = 2^{-2n-v-1} e^{-\frac{b^2}{4d}} \left(\frac{v}{\frac{v}{2}}\right) (1 - v \bmod 2)$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2d\sqrt{z})^{h+k} \left(-\frac{(b + 2d\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} b(b + 2d\sqrt{z}) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + 2d\sqrt{z})^2}{4d}\right) + 2\sqrt{-\frac{(b + 2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b + 2d\sqrt{z})^2}{4d}\right) \right) d^{-2n-2} +$$

$$2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{b^2}{4d-8ics+4icv}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2(d + 2ics - icv)\sqrt{z})^{h+k} \right.$$

$$\left. \left(-\frac{(b + 2(d + 2ics - icv)\sqrt{z})^2}{d + 2ics - icv}\right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} b(b + 2(d + 2ics - icv)\sqrt{z}) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + 2(d + 2ics - icv)\sqrt{z})^2}{4(d + 2ics - icv)}\right) + 2\sqrt{-\frac{(b + 2(d + 2ics - icv)\sqrt{z})^2}{d + 2ics - icv}} \right)$$

$$\begin{aligned}
 & \left. \left. \left. (d + 2ics - icv) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d+2ics-icv)\sqrt{z})^2}{4(d+2ics-icv)} \right) \right) \right) \right) (d+2ics-icv)^{-2(n+1)} + \\
 & e^{-\frac{b^2}{4(d+ic(v-2s))}} (d+ci(v-2s))^{-2(n+1)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d-2ics+icv)\sqrt{z})^{h+k} \\
 & \left( -\frac{(b+2(d-2ics+icv)\sqrt{z})^2}{d+ci(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b+2(d-2ics+icv)\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+k+1), -\frac{(b+2(d-2ics+icv)\sqrt{z})^2}{4(d+ci(v-2s))} \right) + 2 \sqrt{-\frac{(b+2(d-2ics+icv)\sqrt{z})^2}{d+ci(v-2s)}} \right) \\
 & \left. \left. \left. (d+ci(v-2s)) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+2(d-2ics+icv)\sqrt{z})^2}{4(d+ci(v-2s))} \right) \right) \right) \right) \Bigg/ ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n e^{bz^r+dz+e} \sin^v(cz)$**

01.06.21.1481.01

$$\int z^n e^{bz^2+dz+e} \sin^v(cz) dz =$$

$$\begin{aligned}
 & 2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( e^e \left( \frac{v}{2} \right) (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left( -\frac{(d+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d+2bz)^2}{4b} \right) - \right. \\
 & i^{-v} e^{\frac{d^2}{4b}+e} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(d-2ics+icv)^2}{4b}} \sum_{q=0}^n 2^{q-n} (-d+2ics-icv)^{n-q} (d-2ics+icv+2bz)^{q+1} \right. \\
 & \left. \left( -\frac{(d-2ics+icv+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d-2ics+icv+2bz)^2}{4b} \right) + \right. \\
 & \left. (-1)^v e^{-\frac{(d+2ics-icv)^2}{4b}} \sum_{q=0}^n 2^{q-n} (-d-2ics+icv)^{n-q} (d+2ics-icv+2bz)^{q+1} \right. \\
 & \left. \left. \left. \left( -\frac{(d+2ics-icv+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{(d+2ics-icv+2bz)^2}{4b} \right) \right) \right) \right) \Bigg/ ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1482.01

$$\int z^n e^{\sqrt{z} b + dz + e} \sin^v(cz) dz = 2^{-2n-v-1} e^{-\frac{b^2}{4d}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2d\sqrt{z})^{h+k} \left( -\frac{(b + 2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2d\sqrt{z}) \right) \right. \\ \left. \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b + 2d\sqrt{z})^2}{4d} \right) + 2 \sqrt{-\frac{(b + 2d\sqrt{z})^2}{d}} d \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b + 2d\sqrt{z})^2}{4d} \right) \right) d^{-2n-2} +$$

$$2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{b^2}{4(d+ci(v-2s))}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2(d+ci(v-2s))\sqrt{z})^{h+k} \right. \right. \\ \left. \left. \left( -\frac{(b + 2(d+ci(v-2s))\sqrt{z})^2}{d+ci(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2(d+ci(v-2s))\sqrt{z}) \right) \right) \right. \\ \left. \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b + 2(d+ci(v-2s))\sqrt{z})^2}{4(d+ci(v-2s))} \right) + 2 \sqrt{-\frac{(b + 2(d+ci(v-2s))\sqrt{z})^2}{d+ci(v-2s)}} \right) \\ (d+ci(v-2s)) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b + 2(d+ci(v-2s))\sqrt{z})^2}{4(d+ci(v-2s))} \right) \right) (d+ci(v-2s))^{-2n-2} +$$

$$(-1)^v e^{-\frac{b^2}{4(d-ic(v-2s))}} (d-ic(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2(d-ic(v-2s))\sqrt{z})^{h+k}$$

$$\left( -\frac{(b + 2(d-ic(v-2s))\sqrt{z})^2}{d-ic(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2(d-ic(v-2s))\sqrt{z}) \right) \Gamma \left($$

$$\frac{1}{2}(h+k+1), -\frac{(b + 2(d-ic(v-2s))\sqrt{z})^2}{4(d-ic(v-2s))} \right) + 2 \sqrt{-\frac{(b + 2(d-ic(v-2s))\sqrt{z})^2}{d-ic(v-2s)}} \right)$$

$$(d-ic(v-2s)) \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b + 2(d-ic(v-2s))\sqrt{z})^2}{4(d-ic(v-2s))} \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^n e^{bz^r} \sin^v(fz + g)$

01.06.21.1483.01

$$\int z^n e^{bz^2} \sin^v(fz + g) dz = -2^{-v-1} z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1 - v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(2ifs-ifv)^2}{4b} + gi(2s-v)} \left( \sum_{q=0}^n 2^{q-n} (ifv - 2ifs)^{n-q} (2ifs - ifv + 2bz)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(2ifs - ifv + 2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ifs - ifv + 2bz)^2}{4b}\right) \right) b^{-n-1} + \right.$$

$$\left. e^{-\frac{(ifv-2ifs)^2}{4b} + gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (2ifs - ifv)^{n-q} (fi(v-2s) + 2bz)^{q+1} \left( -\frac{(fi(v-2s) + 2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right. \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(fi(v-2s) + 2bz)^2}{4b}\right) \right) b^{-n-1} \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1484.01

$$\int z^n e^{\sqrt{z}} b \sin^v(fz + g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{ib^2}{4f(2s-v)} + g i(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2fi(2s-v)\sqrt{z})^{h+k} \right. \right. \\ \left. \left. \left( \frac{i(b + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2fi(2s-v)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \right. \right. \right. \\ \left. \left. \left. \frac{i(b + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)} \right) + 2fi(2s-v) \sqrt{\frac{i(b + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)}} \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \right. \\ \left. \left. \left. \frac{i(b + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)} \right) \right) \right) \left( (if(2s-v))^{-2n-2} + e^{\frac{ib^2}{4f(v-2s)} + g i(v-2s)} (if(v-2s))^{-2n-2} \right)$$

$$\sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2fi(v-2s)\sqrt{z})^{h+k} \left( \frac{i(b + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \\ \left( \binom{k}{h} \binom{n}{k} \left( b(b + 2fi(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) + \right. \right. \\ \left. \left. 2fi(v-2s) \sqrt{\frac{i(b + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) \right) \right) -$$

$$2^{1-v} (-b)^{-2(n+1)} \left( \frac{v}{2} \right) \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) ; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

Involving  $z^n e^{bz^r+e} \sin^v(fz + g)$

01.06.21.1485.01

$$\int z^n e^{bz^2+e} \sin^v(fz+g) dz = -2^{-v-1} e^e z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(2ifs-ifv)^2}{4b} + e + gi(2s-v)} \left( \sum_{q=0}^n 2^{q-n} (ifv-2ifs)^{n-q} (2ifs-ifv+2bz)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(2ifs-ifv+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ifs-ifv+2bz)^2}{4b}\right) \right) b^{-n-1} + \right.$$

$$\left. e^{-\frac{(ifv-2ifs)^2}{4b} + e + gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (2ifs-ifv)^{n-q} (fi(v-2s)+2bz)^{q+1} \left( -\frac{(fi(v-2s)+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right. \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(fi(v-2s)+2bz)^2}{4b}\right) \right) b^{-n-1} \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1486.01

$$\int z^n e^{\sqrt{z}} b^{+e} \sin^v(fz + g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{ib^2}{4f(2s-v)} + e+g} i(2s-v) \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2fi(2s-v)\sqrt{z})^{h+k} \right. \right. \\ \left. \left. \left( \frac{i(b + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2fi(2s-v)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \right. \right. \right. \\ \left. \left. \left. \frac{i(b + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)} \right) + 2fi(2s-v) \sqrt{\frac{i(b + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)}} \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \right. \\ \left. \left. \left. \frac{i(b + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)} \right) \right) \right) \left( (if(2s-v))^{-2n-2} + e^{\frac{ib^2}{4f(v-2s)} + e+g} i(v-2s) (if(v-2s))^{-2n-2} \right)$$

$$\sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2fi(v-2s)\sqrt{z})^{h+k} \left( \frac{i(b + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \\ \left( \binom{k}{h} \binom{n}{k} \left( b(b + 2fi(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) + \right. \right. \\ \left. \left. 2fi(v-2s) \sqrt{\frac{i(b + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)} \right) \right) \right) -$$

$$2^{1-v} (-b)^{-2(n+1)} e^e \left( \frac{v}{2} \right) \Gamma(2(n+1), -b\sqrt{z}) (1 - v \bmod 2) /; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

Involving  $z^n e^{bz^r+dz} \sin^v(fz + g)$

01.06.21.1487.01

$$\int z^n e^{b z^2 + d z} \sin^v(f z + g) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d + 2 b z)^{q+1} \left( -\frac{(d + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 b z)^2}{4 b}\right) - \right.$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(d+2 i f s - i f v)^2}{4 b} + g i (2 s - v)} \right.$$

$$\left. \left( \sum_{q=0}^n 2^{q-n} (-d - 2 i f s + i f v)^{n-q} (d + 2 i f s - i f v + 2 b z)^{q+1} \left( -\frac{(d + 2 i f s - i f v + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 i f s - i f v + 2 b z)^2}{4 b}\right) \right) b^{-n-1} + e^{-\frac{(d-2 i f s + i f v)^2}{4 b} + g i (v-2 s)} \right.$$

$$\left. \left( \sum_{q=0}^n 2^{q-n} (-d + 2 i f s - i f v)^{n-q} (d + f i (v - 2 s) + 2 b z)^{q+1} \left( -\frac{(d + f i (v - 2 s) + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + f i (v - 2 s) + 2 b z)^2}{4 b}\right) \right) b^{-n-1} \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1488.01

$$\int z^n e^{\sqrt{z} b + d z} \sin^v(f z + g) dz = 2^{-2n-v-1} e^{-\frac{b^2}{4d}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2 d \sqrt{z})^{h+k} \left( -\frac{(b + 2 d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2 d \sqrt{z}) \right. \right.$$

$$\left. \left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) + 2 \sqrt{-\frac{(b + 2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) \right) \right) d^{-2n-2} +$$

$$2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{b^2}{4(d+f i (2 s - v))} + g i (2 s - v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2(d + f i (2 s - v)) \sqrt{z})^{h+k} \right. \right.$$

$$\left. \left. \left( -\frac{(b + 2(d + f i (2 s - v)) \sqrt{z})^2}{d + f i (2 s - v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2(d + f i (2 s - v)) \sqrt{z}) \right. \right.$$



$$\begin{aligned}
 & \left( \frac{1}{2} (h+k+1), -\frac{(b+2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))} \right) + 2 \sqrt{-\frac{(b+2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)}} \\
 & (d+fi(2s-v)) \Gamma \left( \frac{1}{2} (h+k+2), -\frac{(b+2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))} \right) \Bigg) \Bigg) (d+fi(2s-v))^{-2n-2} + \\
 & e^{-\frac{b^2}{4(d+fi(v-2s))} + gi(v-2s)} (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d+fi(v-2s))\sqrt{z})^{h+k} \\
 & \left( -\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b+2(d+fi(v-2s))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2} (h+k+1), -\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} \right) + 2 \sqrt{-\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} \right) \\
 & (d+fi(v-2s)) \Gamma \left( \frac{1}{2} (h+k+2), -\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} \right) \Bigg) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{bz^r+dz+e} \sin^v(fz+g)$

01.06.21.1489.01

$$\int z^n e^{b z^2 + d z + e} \sin^v(f z + g) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( e^e \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d + 2 b z)^{q+1} \left( -\frac{(d + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 b z)^2}{4 b}\right) - \right.$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(d+2if s - i f v)^2}{4b} + e + g i (2s-v)} \right.$$

$$\left. \left( \sum_{q=0}^n 2^{q-n} (-d - 2 i f s + i f v)^{n-q} (d + 2 i f s - i f v + 2 b z)^{q+1} \left( -\frac{(d + 2 i f s - i f v + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 i f s - i f v + 2 b z)^2}{4 b}\right) \right) b^{-n-1} + e^{-\frac{(d-2if s + i f v)^2}{4b} + e + g i (v-2s)} \right.$$

$$\left. \left. \left( \sum_{q=0}^n 2^{q-n} (-d + 2 i f s - i f v)^{n-q} (d + f i (v - 2 s) + 2 b z)^{q+1} \left( -\frac{(d + f i (v - 2 s) + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + f i (v - 2 s) + 2 b z)^2}{4 b}\right) \right) b^{-n-1} \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1490.01

$$\int z^n e^{\sqrt{z} b + d z + e} \sin^v(f z + g) dz = 2^{-2n-v-1} e^{-\frac{b^2}{4d}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2 d \sqrt{z})^{h+k} \left( -\frac{(b + 2 d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2 d \sqrt{z}) \right. \right.$$

$$\left. \left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) + 2 \sqrt{-\frac{(b + 2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) \right) \right) d^{-2n-2} +$$

$$2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{b^2}{4(d+f i (2s-v))} + e + g i (2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2(d + f i (2s-v)) \sqrt{z})^{h+k} \right. \right.$$

$$\left. \left. \left( -\frac{(b + 2(d + f i (2s-v)) \sqrt{z})^2}{d + f i (2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b + 2(d + f i (2s-v)) \sqrt{z}) \right. \right.$$

$$\begin{aligned}
 & \left( \frac{1}{2} (h+k+1), -\frac{(b+2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))} \right) + 2 \sqrt{-\frac{(b+2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)}} \\
 & (d+fi(2s-v)) \Gamma \left( \frac{1}{2} (h+k+2), -\frac{(b+2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))} \right) \Bigg) (d+fi(2s-v))^{-2n-2} + \\
 & e^{-\frac{b^2}{4(d+fi(v-2s))} + e+g i(v-2s)} (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2(d+fi(v-2s))\sqrt{z})^{h+k} \\
 & \left( -\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b+2(d+fi(v-2s))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2} (h+k+1), -\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} \right) + 2 \sqrt{-\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} \right) \\
 & (d+fi(v-2s)) \Gamma \left( \frac{1}{2} (h+k+2), -\frac{(b+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^n e^{bz} \sin^v(cz^r)$

01.06.21.1491.01

$$\begin{aligned}
 \int z^n e^{bz} \sin^v(cz^2) dz &= 2^{-v} \left( (-b)^{-n-1} \binom{v}{\frac{v}{2}} \Gamma(n+1, -bz) (v \bmod 2 - 1) - \right. \\
 & \frac{1}{2} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{b^2}{4icv-8ics}} (ic(2s-v))^{-n-1} \sum_{q=0}^n 2^{q-n} (-b)^{n-q} (b+4icsz-2icvz)^{q+1} \right. \\
 & \left. \left( -\frac{i(b+4icsz-2icvz)^2}{c(v-2s)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{i(b+4icsz-2icvz)^2}{4c(v-2s)} \right) + \right. \\
 & \left. e^{\frac{b^2}{8ics-4icv}} (ic(v-2s))^{-n-1} \sum_{q=0}^n 2^{q-n} (-b)^{n-q} (b+2ci(v-2s)z)^{q+1} \left( \frac{i(b+2ci(v-2s)z)^2}{c(v-2s)} \right)^{\frac{1}{2}(-q-1)} \right. \\
 & \left. \left. \binom{n}{q} \Gamma \left( \frac{q+1}{2}, -\frac{i(b+2ci(v-2s)z)^2}{c(8s-4v)} \right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1492.01

$$\int z^n e^{bz} \sin^v(c\sqrt{z}) dz = i^{-v} 2^{-2n-v-1} b^{-2n-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{\frac{c^2(v-2s)^2}{4b}} \binom{v}{s}$$

$$\left( (-1)^v \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ic(v-2s))^{-h-k+2n} (2b\sqrt{z} - ic(v-2s))^{h+k} \left( -\frac{(2b\sqrt{z} - ic(v-2s))^2}{b} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( 2b \sqrt{-\frac{(2b\sqrt{z} - ic(v-2s))^2}{b}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2b\sqrt{z} - ic(v-2s))^2}{4b}\right) - \right.$$

$$\left. ic(v-2s)(2b\sqrt{z} - ic(v-2s)) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2b\sqrt{z} - ic(v-2s))^2}{4b}\right) \right) +$$

$$\sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(v-2s))^{-h-k+2n} (2\sqrt{z}b + ci(v-2s))^{h+k} \left( -\frac{(2\sqrt{z}b + ci(v-2s))^2}{b} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( ci(v-2s)(2\sqrt{z}b + ci(v-2s)) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}b + ci(v-2s))^2}{4b}\right) + \right.$$

$$\left. \left. 2 \sqrt{-\frac{(2\sqrt{z}b + ci(v-2s))^2}{b}} b \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z}b + ci(v-2s))^2}{4b}\right) \right) \right) -$$

$$2^{-v} (-b)^{-n-1} \left( \frac{v}{2} \right) \Gamma(n+1, -bz) (1-v \bmod 2) ; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

Involving  $z^n e^{bz+e} \sin^v(cz^r)$

01.06.21.1493.01

$$\int z^n e^{bz+e} \sin^v(cz^2) dz = -2^{-v} e^e \left(\frac{v}{2}\right) \Gamma(n+1, -bz) (1-v \bmod 2) (-b)^{-n-1} -$$

$$2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{ib^2}{4c(v-2k)} + e - \frac{i\pi v}{2}} \sum_{q=0}^n 2^{q-n} (-b)^{n-q} (ic(v-2k))^{-n-\frac{1}{2}} (b+2ci(v-2k)z)^{q+1} \right. \right.$$

$$\left. \left. \left( \frac{i(b+2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(b+2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) +$$

$$\frac{1}{\sqrt{-ic(v-2k)}} \left( e^{-\frac{ib^2}{4c(v-2k)} + e + \frac{i\pi v}{2}} \sum_{q=0}^n 2^{q-n} (-b)^{n-q} (-ic(v-2k))^{-n-\frac{1}{2}} (b-2ic(v-2k)z)^{q+1} \right.$$

$$\left. \left. \left( -\frac{i(b-2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(b-2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1494.01

$$\int z^n e^{bz+e} \sin^v(c\sqrt{z}) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2}{4b} + e} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(2s-v))^{-h-k+2n} (2\sqrt{z} b + ci(2s-v))^{h+k} \right. \right. \\ \left. \left. \left( -\frac{(2\sqrt{z} b + ci(2s-v))^2}{b} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \right. \right. \\ \left. \left. \left( ci(2s-v)(2\sqrt{z} b + ci(2s-v)) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} b + ci(2s-v))^2}{4b} \right) + 2 \right. \right. \right. \\ \left. \left. \left. \sqrt{-\frac{(2\sqrt{z} b + ci(2s-v))^2}{b}} b \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} b + ci(2s-v))^2}{4b} \right) \right) \right) \right) b^{-2n-2} + \\ e^{\frac{c^2(v-2s)^2}{4b} + e} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(v-2s))^{-h-k+2n} (2\sqrt{z} b + ci(v-2s))^{h+k} \left( -\frac{(2\sqrt{z} b + ci(v-2s))^2}{b} \right)^{\frac{1}{2}(-h-k-1)} \right. \\ \left. \binom{k}{h} \binom{n}{k} \left( ci(v-2s)(2\sqrt{z} b + ci(v-2s)) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} b + ci(v-2s))^2}{4b} \right) + 2 \right. \right. \\ \left. \left. \left. \sqrt{-\frac{(2\sqrt{z} b + ci(v-2s))^2}{b}} b \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} b + ci(v-2s))^2}{4b} \right) \right) \right) \right) b^{-2n-2} \Bigg) - \\ 2^{-v} (-b)^{-n-1} e^e \left( \frac{v}{2} \right) \Gamma(n+1, -bz) (1-v \bmod 2) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving  $z^{\alpha-1} e^{bz^r} \sin^v(cz^r)$

01.06.21.1495.01

$$\int z^{\alpha-1} e^{b z^r} \sin^v(c z^r) dz = -\frac{2^{-v} z^\alpha (-b z^r)^{-\frac{\alpha}{r}} (1-v \bmod 2)}{r} \left(\frac{v}{2}\right) \Gamma\left(\frac{\alpha}{r}, -b z^r\right) -$$

$$\frac{(2i)^{-v} z^\alpha \sum_{i=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^i \binom{v}{i} \left((-1)^v \Gamma\left(\frac{\alpha}{r}, (ic(v-2i)-b) z^r\right) ((ic(v-2i)-b) z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. ((-b-ic(v-2i)) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ic(v-2i)) z^r\right)\right) /; v \in \mathbb{N}^+$$

01.06.21.1496.01

$$\int z^n e^{b z^2} \sin^v(c z^2) dz = -2^{-v-1} z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -b z^2\right) (1-v \bmod 2) (-b z^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} z^{n+1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left((-1)^v \Gamma\left(\frac{n+1}{2}, (-b-2ics+icv) z^2\right) ((-b-2ics+icv) z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. ((-b-ic(v-2s)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-b-ic(v-2s)) z^2\right)\right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1497.01

$$\int z^n e^{b \sqrt{z}} \sin^v(c \sqrt{z}) dz = -2^{1-v} \left(\frac{v}{2}\right) \Gamma(2(n+1), -b \sqrt{z}) (1-v \bmod 2) (-b)^{-2(n+1)} -$$

$$i^{-v} 2^{1-v} z^{n+1} \sum_{i=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^i \binom{v}{i} \left((-1)^v \Gamma(2(n+1), (ic(v-2i)-b) \sqrt{z}) ((ic(v-2i)-b) \sqrt{z})^{-2(n+1)} + \right.$$

$$\left. ((-b-ic(v-2i)) \sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (-b-ic(v-2i)) \sqrt{z})\right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} e^{b z^r + e} \sin^v(c z^r)$

01.06.21.1498.01

$$\int z^{\alpha-1} e^{b z^r + e} \sin^v(c z^r) dz = -\frac{2^{-v} e^e (1-v \bmod 2)}{r} z^\alpha (-b z^r)^{-\frac{\alpha}{r}} \left(\frac{v}{2}\right) \Gamma\left(\frac{\alpha}{r}, -b z^r\right) -$$

$$\frac{2^{-v} z^\alpha \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left(e^{e+\frac{i\pi v}{2}} \Gamma\left(\frac{\alpha}{r}, (ic(v-2k)-b) z^r\right) ((ic(v-2k)-b) z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. e^{-\frac{i\pi v}{2}} ((-b-ic(v-2k)) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ic(v-2k)) z^r\right)\right) /; v \in \mathbb{N}^+$$

01.06.21.1499.01

$$\int z^n e^{b z^2 + e} \sin^v(c z^2) dz = -2^{-v-1} e^e z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -b z^2\right) (1-v \bmod 2) (-b z^2)^{\frac{1}{2}(-n-1)} -$$

$$2^{-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left(e^{e+\frac{i\pi v}{2}} \Gamma\left(\frac{n+1}{2}, (ic(v-2k)-b) z^2\right) ((ic(v-2k)-b) z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{-\frac{i\pi v}{2}} ((-b-ic(v-2k)) z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-b-ic(v-2k)) z^2\right)\right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1500.01

$$\int z^n e^{\sqrt{z} b + e} \sin^v(c \sqrt{z}) dz = -2^{1-v} e^e \left(\frac{v}{2}\right) \Gamma(2(n+1), -b \sqrt{z}) (1 - v \bmod 2) (-b)^{-2(n+1)} -$$

$$2^{1-v} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{e + \frac{i\pi v}{2}} \Gamma(2(n+1), (ic(v-2k) - b) \sqrt{z}) ((ic(v-2k) - b) \sqrt{z})^{-2(n+1)} + \right.$$

$$\left. e^{e - \frac{i\pi v}{2}} ((-b - ic(v-2k)) \sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (-b - ic(v-2k)) \sqrt{z}) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n e^{bz^r+dz} \sin^v(cz^r)$**

01.06.21.1501.01

$$\int z^n e^{bz^2+dz} \sin^v(cz^2) dz =$$

$$-2^{-v-1} e^{-\frac{d^2}{4b}} \left(\frac{v}{2}\right) (1 - v \bmod 2) b^{-n-1} \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left( -\frac{(d+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz)^2}{4b}\right) -$$

$$2^{-1-v} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( \frac{1}{\sqrt{b+2ics-icv}} \left( (-1)^v e^{-\frac{d^2}{4b-8ics+4icv}} \right. \right.$$

$$\left. \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (b+2ics-icv)^{-n-\frac{1}{2}} (d+2(b+2ics-icv)z)^{q+1} \left( -\frac{(d+2(b+2ics-icv)z)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b+2ics-icv)z)^2}{4(b+2ics-icv)}\right) \right) + \frac{1}{\sqrt{b+ci(v-2s)}} \left( e^{-\frac{d^2}{4(b+ci(v-2s))}} \right.$$

$$\left. \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (b+ci(v-2s))^{-n-\frac{1}{2}} (d+2(b-2ics+icv)z)^{q+1} \left( -\frac{(d+2(b-2ics+icv)z)^2}{b+ci(v-2s)} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b-2ics+icv)z)^2}{4(b+ci(v-2s))}\right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$



01.06.21.1502.01

$$\int z^n e^{\sqrt{z} b+d z} \sin^v(c \sqrt{z}) d z =$$

$$2^{-2 n-v-1} e^{-\frac{b^2}{4 d}}\left(\frac{v}{2}\right)(1-v \bmod 2) d^{-2 n-2} \sum_{k=0}^n \sum_{h=0}^k(-1)^{k-h} 4^k b^{-h-k+2 n}(b+2 d \sqrt{z})^{h+k}\left(-\frac{(b+2 d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)}\binom{k}{h}\binom{n}{k}$$

$$\left(b(b+2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1),-\frac{(b+2 d \sqrt{z})^2}{4 d}\right)+2 \sqrt{-\frac{(b+2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2),-\frac{(b+2 d \sqrt{z})^2}{4 d}\right)\right)+$$

$$2^{-2 n-v-1} i^{-v} d^{-2 n-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor}(-1)^s\binom{v}{s}\left((-1)^v e^{-\frac{(b+c i(2 s-v))^2}{4 d}} \sum_{k=0}^n \sum_{h=0}^k(-1)^{k-h} 4^k(b+c i(2 s-v))^{-h-k+2 n}\right.$$

$$\left.(b+c i(2 s-v)+2 d \sqrt{z})^{h+k}\left(-\frac{(b+c i(2 s-v)+2 d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)}\binom{k}{h}\binom{n}{k}\right.$$

$$\left.\left((b+c i(2 s-v))(b+c i(2 s-v)+2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1),-\frac{(b+c i(2 s-v)+2 d \sqrt{z})^2}{4 d}\right)+\right.\right.$$

$$\left.\left.2 \sqrt{-\frac{(b+c i(2 s-v)+2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2),-\frac{(b+c i(2 s-v)+2 d \sqrt{z})^2}{4 d}\right)\right)\right)+$$

$$e^{-\frac{(b+c i(v-2 s))^2}{4 d}} \sum_{k=0}^n \sum_{h=0}^k(-1)^{k-h} 4^k(b+c i(v-2 s))^{-h-k+2 n}(b+c i(v-2 s)+2 d \sqrt{z})^{h+k}$$

$$\left(-\frac{(b+c i(v-2 s)+2 d \sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)}\binom{k}{h}\binom{n}{k}\left((b+c i(v-2 s))(b+c i(v-2 s)+2 d \sqrt{z}) \Gamma\left(\right.\right.$$

$$\left.\left.\frac{1}{2}(h+k+1),-\frac{(b+c i(v-2 s)+2 d \sqrt{z})^2}{4 d}\right)+2 \sqrt{-\frac{(b+c i(v-2 s)+2 d \sqrt{z})^2}{d}} d \Gamma\left(\right.$$

$$\left.\left.\frac{1}{2}(h+k+2),-\frac{(b+c i(v-2 s)+2 d \sqrt{z})^2}{4 d}\right)\right)\right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^n e^{bz^2+dz+e} \sin^v(cz^r)$

01.06.21.1503.01

$$\int z^n e^{bz^2+dz+e} \sin^v(cz^2) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( e^e \left( \frac{v}{2} \right) (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left( -\frac{(d+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz)^2}{4b}\right) -$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{d^2}{4(b-2ics+icv)}} (b-2ics+icv)^{-n-1} \right.$$

$$\left. \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2(b-2ics+icv)z)^{q+1} \left( -\frac{(d+2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \right.$$

$$\left. \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) + (-1)^v e^{-\frac{d^2}{4(b+2ics-icv)}} (b+2ics-icv)^{-n-1} \right.$$

$$\left. \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz+4icsz-2icvz)^{q+1} \left( -\frac{(d+2bz+4icsz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz+4icsz-2icvz)^2}{4(b+2ics-icv)}\right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1504.01

$$\int z^n e^{\sqrt{z} b+dz+e} \sin^v(c \sqrt{z}) dz =$$

$$2^{-2n-v-1} e^{-\frac{b^2}{4d}} \left(\frac{v}{2}\right) (1-v \bmod 2) d^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2d\sqrt{z})^{h+k} \left(-\frac{(b+2d\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k}$$

$$\left( b(b+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+2d\sqrt{z})^2}{4d}\right) + 2\sqrt{-\frac{(b+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+2d\sqrt{z})^2}{4d}\right) \right) +$$

$$2^{-2n-v-1} i^{-v} d^{-2n-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} \right.$$

$$\left. (b+ci(2s-v)+2d\sqrt{z})^{h+k} \left(-\frac{(b+ci(2s-v)+2d\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \right.$$

$$\left. \left( (b+ci(2s-v))(b+ci(2s-v)+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(2s-v)+2d\sqrt{z})^2}{4d}\right) + \right.$$

$$\left. 2\sqrt{-\frac{(b+ci(2s-v)+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ci(2s-v)+2d\sqrt{z})^2}{4d}\right) \right) +$$

$$e^{-\frac{(b+ci(v-2s))^2}{4d}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n} (b+ci(v-2s)+2d\sqrt{z})^{h+k}$$

$$\left( -\frac{(b+ci(v-2s)+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s)+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(v-2s)+2d\sqrt{z})^2}{4d}\right) + \right.$$

$$\left. 2\sqrt{-\frac{(b+ci(v-2s)+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ci(v-2s)+2d\sqrt{z})^2}{4d}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^n e^{dz} \sin^v(cz^r + g)$

01.06.21.1505.01

$$\int z^n e^{dz} \sin^v(cz^2 + g) dz = -2^{-v} \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1 - v \bmod 2) (-d)^{-n-1} -$$

$$2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{id^2}{4c(v-2k)} + g i^{(v-2k)} - \frac{i\pi v}{2}} \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (ic(v-2k))^{-n-\frac{1}{2}} (d+2ci(v-2k)z)^{q+1} \right. \right.$$

$$\left. \left( \frac{i(d+2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) +$$

$$\frac{1}{\sqrt{-ic(v-2k)}} \left( e^{-\frac{id^2}{4c(v-2k)} + \frac{i\pi v}{2} - ig^{(v-2k)}} \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (-ic(v-2k))^{-n-\frac{1}{2}} (d-2ic(v-2k)z)^{q+1} \right.$$

$$\left. \left( -\frac{i(d-2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1506.01

$$\int z^n e^{dz} \sin^v(\sqrt{z} c + g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2}{4d} + g i(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i c(2s-v))^{-h-k+2n} (2\sqrt{z} d + c i(2s-v))^{h+k} \right. \right. \\ \left. \left. \left( -\frac{(2\sqrt{z} d + c i(2s-v))^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( c i(2s-v) (2\sqrt{z} d + c i(2s-v)) \right. \right. \right. \\ \left. \left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} d + c i(2s-v))^2}{4d}\right) + 2\sqrt{-\frac{(2\sqrt{z} d + c i(2s-v))^2}{d}} \right. \right. \\ \left. \left. \left. \left. d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} d + c i(2s-v))^2}{4d}\right) \right) \right) \right) \right) d^{-2n-2} + e^{\frac{c^2(v-2s)^2}{4d} + g i(v-2s)} \\ \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i c(v-2s))^{-h-k+2n} (2\sqrt{z} d + c i(v-2s))^{h+k} \left( -\frac{(2\sqrt{z} d + c i(v-2s))^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right. \\ \left. \binom{k}{h} \binom{n}{k} \left( c i(v-2s) (2\sqrt{z} d + c i(v-2s)) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} d + c i(v-2s))^2}{4d}\right) + 2 \right. \right. \\ \left. \left. \sqrt{-\frac{(2\sqrt{z} d + c i(v-2s))^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} d + c i(v-2s))^2}{4d}\right) \right) \right) \right) \\ \left. d^{-2n-2} \right) - 2^{-v} (-d)^{-n-1} \binom{v}{\frac{v}{2}} \Gamma(n+1, -dz) (1-v \bmod 2) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving  $z^n e^{dz+e} \sin^v(cz^r + g)$

01.06.21.1507.01

$$\int z^n e^{dz+e} \sin^v(cz^2+g) dz = -2^{-v} e^e \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1-v \bmod 2) (-d)^{-n-1} -$$

$$2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{id^2}{4c(v-2k)}+e+g} i^{(v-2k)-\frac{i\pi v}{2}} \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (ic(v-2k))^{-n-\frac{1}{2}} \right. \right.$$

$$\left. \left. (d+2ci(v-2k)z)^{q+1} \left( \frac{i(d+2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) + \right.$$

$$\left. \frac{1}{\sqrt{-ic(v-2k)}} \left( e^{-\frac{id^2}{4c(v-2k)}+e+\frac{i\pi v}{2}-ig(v-2k)} \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (-ic(v-2k))^{-n-\frac{1}{2}} (d-2ic(v-2k)z)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{i(d-2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1508.01

$$\int z^n e^{dz+e} \sin^v(\sqrt{z} c + g) dz =$$

$$\begin{aligned} & i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2}{4d} + g i(2s-v)+e} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i c(2s-v))^{-h-k+2n} (2\sqrt{z} d + c i(2s-v))^{h+k} \right. \right. \\ & \left. \left. \left( -\frac{(2\sqrt{z} d + c i(2s-v))^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( c i(2s-v) (2\sqrt{z} d + c i(2s-v)) \right. \right. \right. \\ & \left. \left. \Gamma\left( \frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} d + c i(2s-v))^2}{4d} \right) + 2\sqrt{-\frac{(2\sqrt{z} d + c i(2s-v))^2}{d}} \right. \right. \\ & \left. \left. \left. \left. \left. d \Gamma\left( \frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} d + c i(2s-v))^2}{4d} \right) \right) \right) \right) \right) d^{-2n-2} + e^{\frac{c^2(v-2s)^2}{4d} + g i(v-2s)+e} \\ & \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i c(v-2s))^{-h-k+2n} (2\sqrt{z} d + c i(v-2s))^{h+k} \left( -\frac{(2\sqrt{z} d + c i(v-2s))^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right. \\ & \left. \binom{k}{h} \binom{n}{k} \left( c i(v-2s) (2\sqrt{z} d + c i(v-2s)) \Gamma\left( \frac{1}{2}(h+k+1), -\frac{(2\sqrt{z} d + c i(v-2s))^2}{4d} \right) + 2 \right. \right. \\ & \left. \left. \left. \left. \left. \sqrt{-\frac{(2\sqrt{z} d + c i(v-2s))^2}{d}} d \Gamma\left( \frac{1}{2}(h+k+2), -\frac{(2\sqrt{z} d + c i(v-2s))^2}{4d} \right) \right) \right) \right) \right) d^{-2n-2} \left. \right) - \\ & 2^{-v} (-d)^{-n-1} e^e \left( \frac{v}{2} \right) \Gamma(n+1, -dz) (1-v \bmod 2) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+ \end{aligned}$$

Involving  $z^{\alpha-1} e^{bz^r} \sin^v(cz^r + g)$

01.06.21.1509.01

$$\int z^{\alpha-1} e^{bz^r} \sin^v(cz^r + g) dz = -\frac{2^{-v}(1-v \bmod 2)}{r} z^\alpha (-bz^r)^{-\frac{\alpha}{r}} \left(\frac{v}{2}\right) \Gamma\left(\frac{\alpha}{r}, -bz^r\right) -$$

$$\frac{2^{-v} z^\alpha}{r} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i\pi v}{2} - ig(v-2k)} \Gamma\left(\frac{\alpha}{r}, (ic(v-2k) - b)z^r\right) ((ic(v-2k) - b)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. e^{g(v-2k) - \frac{i\pi v}{2}} ((-b - ic(v-2k))z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b - ic(v-2k))z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.1510.01

$$\int z^n e^{bz^2} \sin^v(cz^2 + g) dz = -2^{-v-1} z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$2^{-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i\pi v}{2} - ig(v-2k)} \Gamma\left(\frac{n+1}{2}, (ic(v-2k) - b)z^2\right) ((ic(v-2k) - b)z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{g(v-2k) - \frac{i\pi v}{2}} ((-b - ic(v-2k))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-b - ic(v-2k))z^2\right) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1511.01

$$\int z^n e^{\sqrt{z}^b} \sin^v(\sqrt{z}c + g) dz = -2^{1-v} \left(\frac{v}{2}\right) \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) (-b)^{-2(n+1)} -$$

$$2^{1-v} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i\pi v}{2} - ig(v-2k)} \Gamma(2(n+1), (ic(v-2k) - b)\sqrt{z}) ((ic(v-2k) - b)\sqrt{z})^{-2(n+1)} + \right.$$

$$\left. e^{g(v-2k) - \frac{i\pi v}{2}} ((-b - ic(v-2k))\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (-b - ic(v-2k))\sqrt{z}) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} e^{bz^r+e} \sin^v(cz^r + g)$

01.06.21.1512.01

$$\int z^{\alpha-1} e^{bz^r+e} \sin^v(cz^r + g) dz = -\frac{2^{-v} e^e (1-v \bmod 2)}{r} z^\alpha (-bz^r)^{-\frac{\alpha}{r}} \left(\frac{v}{2}\right) \Gamma\left(\frac{\alpha}{r}, -bz^r\right) -$$

$$\frac{2^{-v} z^\alpha}{r} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{e+\frac{i\pi v}{2} - ig(v-2k)} \Gamma\left(\frac{\alpha}{r}, (ic(v-2k) - b)z^r\right) ((ic(v-2k) - b)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. e^{e+g(v-2k) - \frac{i\pi v}{2}} ((-b - ic(v-2k))z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b - ic(v-2k))z^r\right) \right); v \in \mathbb{N}^+$$

01.06.21.1513.01

$$\int z^n e^{bz^2+e} \sin^v(cz^2 + g) dz = -2^{-v-1} e^e z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$2^{-v-1} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{e+\frac{i\pi v}{2} - ig(v-2k)} \Gamma\left(\frac{n+1}{2}, (ic(v-2k) - b)z^2\right) ((ic(v-2k) - b)z^2)^{\frac{1}{2}(-n-1)} + \right.$$

$$\left. e^{e+g(v-2k) - \frac{i\pi v}{2}} ((-b - ic(v-2k))z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-b - ic(v-2k))z^2\right) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$



01.06.21.1514.01

$$\int z^n e^{\sqrt{z} b+e} \sin^v(\sqrt{z} c+g) dz = -2^{1-v} e^e \left(\frac{v}{2}\right) \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) (-b)^{-2(n+1)} -$$

$$2^{1-v} z^{n+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{e+\frac{i\pi v}{2}-ig(v-2k)} \Gamma(2(n+1), (ic(v-2k)-b)\sqrt{z}) ((ic(v-2k)-b)\sqrt{z})^{-2(n+1)} + \right.$$

$$\left. e^{e+g} i^{(v-2k)-\frac{i\pi v}{2}} ((-b-ic(v-2k))\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (-b-ic(v-2k))\sqrt{z}) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n e^{bz^r+dz} \sin^v(cz^r+g)$**

01.06.21.1515.01

$$\int z^n e^{bz^2+dz} \sin^v(cz^2+g) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left(\frac{v}{2}\right) (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left(-\frac{(d+2bz)^2}{b}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz)^2}{4b}\right) -$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{ig(v-2s)-\frac{d^2}{4(b-2ics+icv)}} \left( \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2(b-2ics+icv)z)^{q+1} \right. \right.$$

$$\left. \left. \left(-\frac{(d+2(b-2ics+icv)z)^2}{b-2ics+icv}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right)$$

$$(b-2ics+icv)^{-n-1} + (-1)^v e^{ig(2s-v)-\frac{d^2}{4(b+2ics-icv)}} (b+2ics-icv)^{-n-1}$$

$$\sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz+4icsz-2icvz)^{q+1} \left(-\frac{(d+2bz+4icsz-2icvz)^2}{b+2ics-icv}\right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz+4icsz-2icvz)^2}{4(b+2ics-icv)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1516.01

$$\int z^n e^{\sqrt{z} b+dz} \sin^v(\sqrt{z} c+g) dz = 2^{-2n-v-1} e^{-\frac{b^2}{4d}} \left(\frac{v}{2}\right) (1-v \bmod 2)$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2d\sqrt{z})^{h+k} \left(-\frac{(b+2d\sqrt{z})^2}{d}\right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b+2d\sqrt{z}) \right. \right.$$

$$\left. \left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+2d\sqrt{z})^2}{4d}\right) + 2\sqrt{-\frac{(b+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+2d\sqrt{z})^2}{4d}\right) \right) \right) d^{-2n-2} +$$

$$\begin{aligned}
 & 2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4d} + gi(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} \right. \right. \\
 & \quad \left. \left. (b+ci(2s-v) + 2d\sqrt{z})^{h+k} \left( -\frac{(b+ci(2s-v) + 2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \right. \right. \\
 & \quad \left. \left. \left( (b+ci(2s-v))(b+ci(2s-v) + 2d\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+ci(2s-v) + 2d\sqrt{z})^2}{4d} \right) + 2 \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{-\frac{(b+ci(2s-v) + 2d\sqrt{z})^2}{d}} d \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+ci(2s-v) + 2d\sqrt{z})^2}{4d} \right) \right) \right) \right) d^{-2n-2} + \\
 & \quad e^{-\frac{(b+ci(v-2s))^2}{4d} + gi(v-2s)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n} (b+ci(v-2s) + 2d\sqrt{z})^{h+k} \right. \\
 & \quad \left. \left( -\frac{(b+ci(v-2s) + 2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s) + 2d\sqrt{z}) \right. \right. \\
 & \quad \left. \left. \Gamma \left( \frac{1}{2}(h+k+1), -\frac{(b+ci(v-2s) + 2d\sqrt{z})^2}{4d} \right) + 2 \sqrt{-\frac{(b+ci(v-2s) + 2d\sqrt{z})^2}{d}} \right. \right. \\
 & \quad \left. \left. \left. d \Gamma \left( \frac{1}{2}(h+k+2), -\frac{(b+ci(v-2s) + 2d\sqrt{z})^2}{4d} \right) \right) \right) \right) d^{-2n-2} \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{bz^r+dz+e} \sin^v(cz^r+g)$

01.06.21.1517.01

$$\int z^n e^{bz^2+dz+e} \sin^v(cz^2+g) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( e^e \left( \frac{v}{2} \right) (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left( -\frac{(d+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz)^2}{4b}\right) - \right.$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{d^2}{4(b-2ics+icv)}+e+gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2(b-2ics+icv)z)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(d+2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right)$$

$$(b-2ics+icv)^{-n-1} + (-1)^v e^{-\frac{d^2}{4(b+2ics-icv)}+e+gi(2s-v)} (b+2ics-icv)^{-n-1}$$

$$\sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz+4icsz-2icvz)^{q+1} \left( -\frac{(d+2bz+4icsz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz+4icsz-2icvz)^2}{4(b+2ics-icv)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1518.01

$$\int z^n e^{\sqrt{z}bz+dz+e} \sin^v(\sqrt{z}c+g) dz = 2^{-2n-v-1} e^{-\frac{b^2}{4d}} \left( \frac{v}{2} \right) (1-v \bmod 2)$$

$$\left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2d\sqrt{z})^{h+k} \left( -\frac{(b+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b(b+2d\sqrt{z}) \right. \right.$$

$$\left. \left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+2d\sqrt{z})^2}{4d}\right) + 2\sqrt{-\frac{(b+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+2d\sqrt{z})^2}{4d}\right) \right) \right) d^{-2n-2} +$$

$$2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4d}+e+gi(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} \right. \right.$$

$$\left. \left. (b+ci(2s-v)+2d\sqrt{z})^{h+k} \left( -\frac{(b+ci(2s-v)+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \right) \right)$$

$$\begin{aligned}
 & \left( (b + ci(2s - v))(b + ci(2s - v) + 2d\sqrt{z}) \Gamma \left( \frac{1}{2}(h + k + 1), -\frac{(b + ci(2s - v) + 2d\sqrt{z})^2}{4d} \right) + 2 \right. \\
 & \left. \sqrt{-\frac{(b + ci(2s - v) + 2d\sqrt{z})^2}{d}} d \Gamma \left( \frac{1}{2}(h + k + 2), -\frac{(b + ci(2s - v) + 2d\sqrt{z})^2}{4d} \right) \right) d^{-2n-2} + \\
 & e^{-\frac{(b+ci(v-2s))^2}{4d} + e+gi(v-2s)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b + ci(v - 2s))^{-h-k+2n} (b + ci(v - 2s) + 2d\sqrt{z})^{h+k} \right. \\
 & \left. \left( -\frac{(b + ci(v - 2s) + 2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} (b + ci(v - 2s))(b + ci(v - 2s) + 2d\sqrt{z}) \right. \\
 & \left. \Gamma \left( \frac{1}{2}(h + k + 1), -\frac{(b + ci(v - 2s) + 2d\sqrt{z})^2}{4d} \right) + 2 \sqrt{-\frac{(b + ci(v - 2s) + 2d\sqrt{z})^2}{d}} \right. \\
 & \left. \left. d \Gamma \left( \frac{1}{2}(h + k + 2), -\frac{(b + ci(v - 2s) + 2d\sqrt{z})^2}{4d} \right) \right) \right) d^{-2n-2} \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{dz} \sin^v(cz^r + fz)$

01.06.21.1519.01

$$\int z^n e^{dz} \sin^v(cz^2 + fz) dz =$$

$$-2^{-v} \binom{v}{\frac{v}{2}} \Gamma(n+1, -dz) (1-v \bmod 2) (-d)^{-n-1} - 2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{i(d+fi(v-2k))^2 - i\pi v}{4c(v-2k)} - \frac{i\pi v}{2}} \right. \right.$$

$$\sum_{q=0}^n 2^{q-n} (ic(v-2k))^{-n-\frac{1}{2}} (-d-ifi(v-2k))^{n-q} (d+fi(v-2k) + 2ci(v-2k)z)^{q+1}$$

$$\left. \left. \left( \frac{i(d+fi(v-2k) + 2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+fi(v-2k) + 2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) +$$

$$\frac{1}{\sqrt{-ic(v-2k)}} \left( e^{\frac{i(d-ifi(v-2k))^2 + i\pi v}{4c(v-2k)} + \frac{i\pi v}{2}} \sum_{q=0}^n 2^{q-n} (-ic(v-2k))^{-n-\frac{1}{2}} (if(v-2k) - d)^{n-q}$$

$$(d-ifi(v-2k) - 2ic(v-2k)z)^{q+1} \left( -\frac{i(d-ifi(v-2k) - 2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-ifi(v-2k) - 2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1520.01

$$\int z^n e^{dz} \sin^v(\sqrt{z}c + fz) dz = i^{-v} 2^{-2n-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2}{4(d+fi(2s-v))}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(2s-v))^{-h-k+2n} (2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^{h+k} \right. \right.$$

$$\left. \left. \left( -\frac{(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^2}{d+fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \right. \right.$$

$$\left. \left. \left( ci(2s-v)(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v)) \right) \Gamma\left(\frac{1}{2}(h+k+1), \right. \right.$$

$$\left. \left. -\frac{(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^2}{4(d+fi(2s-v))} \right) + 2\sqrt{-\frac{(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^2}{d+fi(2s-v)}} \right)$$

$$\begin{aligned}
 & \left. \left. \left. (d + f i (2 s - v)) \Gamma \left( \frac{1}{2} (h + k + 2), - \frac{(2 \sqrt{z} (d + f i (2 s - v)) + c i (2 s - v))^2}{4 (d + f i (2 s - v))} \right) \right) \right) \right) \\
 & (d + f i (2 s - v))^{-2 n - 2} + e^{\frac{c^2 (v - 2 s)^2}{4 (d + f i (v - 2 s))}} (d + f i (v - 2 s))^{-2 n - 2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i c (v - 2 s))^{-h-k+2 n} \\
 & (c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^{h+k} \left( - \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{d + f i (v - 2 s)} \right)^{\frac{1}{2} (-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left( c i (v - 2 s) (c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + k + 1), \right. \right. \\
 & \left. \left. - \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{4 (d + f i (v - 2 s))} \right) + 2 \sqrt{- \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{d + f i (v - 2 s)}} \right) \\
 & \left. \left. \left. (d + f i (v - 2 s)) \Gamma \left( \frac{1}{2} (h + k + 2), - \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{4 (d + f i (v - 2 s))} \right) \right) \right) \right) -
 \end{aligned}$$

$$2^{-v} (-d)^{-n-1} \left( \frac{v}{2} \right) \Gamma(n+1, -dz) (1 - v \bmod 2) ; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

**Involving  $z^n e^{dz+e} \sin^v(cz^r + fz)$**

01.06.21.1521.01

$$\int z^n e^{dz+e} \sin^v(cz^2 + fz) dz =$$

$$-2^{-v} e^e \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1-v \bmod 2) (-d)^{-n-1} - 2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{i(d+fi(v-2k))^2}{4c(v-2k)} + e^{-\frac{i\pi v}{2}}} \right. \right.$$

$$\sum_{q=0}^n 2^{q-n} (ic(v-2k))^{-n-\frac{1}{2}} (-d-ifi(v-2k))^{n-q} (d+fi(v-2k) + 2ci(v-2k)z)^{q+1}$$

$$\left. \left. \left( \frac{i(d+fi(v-2k) + 2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d+fi(v-2k) + 2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) +$$

$$\frac{1}{\sqrt{-ic(v-2k)}} \left( e^{\frac{i(d-ifi(v-2k))^2}{4c(v-2k)} + e^{\frac{i\pi v}{2}}} \sum_{q=0}^n 2^{q-n} (-ic(v-2k))^{-n-\frac{1}{2}} (if(v-2k) - d)^{n-q} \right.$$

$$(d-ifi(v-2k) - 2ic(v-2k)z)^{q+1} \left( -\frac{i(d-ifi(v-2k) - 2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d-ifi(v-2k) - 2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1522.01

$$\int z^n e^{dz+e} \sin^v(\sqrt{z}c + fz) dz = i^{-v} 2^{-2n-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2}{4(d+fi(2s-v))} + e} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(2s-v))^{-h-k+2n} (2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^{h+k} \right. \right.$$

$$\left. \left. \left( \frac{(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^2}{d+fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \right. \right.$$

$$\left. \left. \left( ci(2s-v)(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v)) \right) \Gamma\left(\frac{1}{2}(h+k+1), \right. \right.$$

$$\left. \left. -\frac{(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^2}{4(d+fi(2s-v))} \right) + 2\sqrt{-\frac{(2\sqrt{z}(d+fi(2s-v)) + ci(2s-v))^2}{d+fi(2s-v)}} \right)$$

$$\begin{aligned}
 & \left. \left. \left. (d + f i (2 s - v)) \Gamma \left( \frac{1}{2} (h + k + 2), - \frac{(2 \sqrt{z} (d + f i (2 s - v)) + c i (2 s - v))^2}{4 (d + f i (2 s - v))} \right) \right) \right) \right) \\
 & (d + f i (2 s - v))^{-2 n - 2} + e^{\frac{c^2 (v - 2 s)^2}{4 (d + f i (v - 2 s))} + e} (d + f i (v - 2 s))^{-2 n - 2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i c (v - 2 s))^{-h-k+2 n} \\
 & (c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^{h+k} \left( - \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{d + f i (v - 2 s)} \right)^{\frac{1}{2} (-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left( c i (v - 2 s) (c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + k + 1), \right. \right. \\
 & \left. \left. - \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{4 (d + f i (v - 2 s))} \right) + 2 \sqrt{- \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{d + f i (v - 2 s)}} \right) \\
 & \left. \left. \left. (d + f i (v - 2 s)) \Gamma \left( \frac{1}{2} (h + k + 2), - \frac{(c i (v - 2 s) + 2 (d + f i (v - 2 s)) \sqrt{z})^2}{4 (d + f i (v - 2 s))} \right) \right) \right) \right) -
 \end{aligned}$$

$$2^{-v} (-d)^{-n-1} e^e \left( \frac{v}{2} \right) \Gamma(n + 1, -d z) (1 - v \bmod 2) ; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

**Involving  $z^n e^{bz'} \sin^v(cz' + fz)$**



01.06.21.1523.01

$$\int z^n e^{bz^2} \sin^v(cz^2 + fz) dz = -2^{-v-1} z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(ifv-2ifs)^2}{4(b-2ics+icv)}} \left( \sum_{q=0}^n 2^{q-n} (2ifs-ifv)^{n-q} (fi(v-2s) + 2(b-2ics+icv)z)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(fi(v-2s) + 2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(fi(v-2s) + 2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right)$$

$$(b-2ics+icv)^{-n-1} + (-1)^v e^{-\frac{(2ifs-ifv)^2}{4(b+2ics-icv)}} (b+2ics-icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (ifv-2ifs)^{n-q}$$

$$(2ifs+4icsz-ifv+2bz-2icvz)^{q+1} \left( -\frac{(2ifs+4icsz-ifv+2bz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ifs+4icsz-ifv+2bz-2icvz)^2}{4(b+2ics-icv)}\right) \right) \right); n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1524.01

$$\int z^n e^{\sqrt{z} b} \sin^v(\sqrt{z} c + fz) dz = i^{-v} 2^{-2n-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{i(b+ci(2s-v))^2}{4f(2s-v)}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} (b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^{h+k} \right. \right.$$

$$\left. \left. \left( \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} (b+ci(2s-v)) \right) \right)$$

$$(b+ci(2s-v) + 2fi(2s-v)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right) +$$

$$2fi(2s-v) \sqrt{\frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)}} \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right) \left. \right) \left. \right) \left. \right) \left. \right) (if(2s-v))^{-2n-2} + e^{\frac{i(b+ci(v-2s))^2}{4f(v-2s)}}$$

$$\begin{aligned}
 & (i f(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b + ci(v-2s))^{-h-k+2n} (b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^{h+k} \\
 & \left( \frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b + ci(v-2s)) \right. \\
 & \left. (b + ci(v-2s) + 2fi(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + \right. \\
 & \left. 2fi(v-2s) \sqrt{\frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \left. \left. \frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \right) \Bigg) \Bigg) \Bigg) -
 \end{aligned}$$

$$2^{1-v} (-b)^{-2(n+1)} \left( \frac{v}{2} \right) \Gamma(2(n+1), -b\sqrt{z}) (1 - v \bmod 2) /; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

**Involving  $z^n e^{bz^r+e} \sin^v(cz^r + fz)$**

01.06.21.1525.01

$$\int z^n e^{bz^2+e} \sin^v(cz^2 + fz) dz = -2^{-v-1} e^e z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(ifv-2ifs)^2}{4(b-2ics+icv)}} \left( \sum_{q=0}^n 2^{q-n} (2ifs-ifv)^{n-q} (fi(v-2s) + 2(b-2ics+icv)z)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(fi(v-2s) + 2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(fi(v-2s) + 2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right)$$

$$(b-2ics+icv)^{-n-1} + (-1)^v e^{-\frac{(2ifs-ifv)^2}{4(b+2ics-icv)}} (b+2ics-icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (ifv-2ifs)^{n-q}$$

$$(2ifs+4icsz-ifv+2bz-2icvz)^{q+1} \left( -\frac{(2ifs+4icsz-ifv+2bz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ifs+4icsz-ifv+2bz-2icvz)^2}{4(b+2ics-icv)}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1526.01

$$\int z^n e^{\sqrt{z}bz+e} \sin^v(\sqrt{z}c + fz) dz = i^{-v} 2^{-2n-v-1}$$

$$\sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{i(b+ci(2s-v))^2}{4f(2s-v)}+e} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} (b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^{h+k} \right. \right.$$

$$\left. \left. \left( \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} (b+ci(2s-v)) \right. \right.$$

$$\left. \left. (b+ci(2s-v) + 2fi(2s-v)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right) \right) + \right.$$

$$2fi(2s-v) \sqrt{\frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)}} \Gamma\left(\frac{1}{2}(h+k+2), \right.$$

$$\left. \left. \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)} \right) \right) \left. \right) \left. \right) \left. \right) (if(2s-v))^{-2n-2} + e^{\frac{i(b+ci(v-2s))^2}{4f(v-2s)}+e}$$

$$\begin{aligned}
 & (i f(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b + ci(v-2s))^{-h-k+2n} (b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^{h+k} \\
 & \left( \frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b + ci(v-2s) \right. \\
 & \left. (b + ci(v-2s) + 2fi(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + \right. \\
 & \left. 2fi(v-2s) \sqrt{\frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{f(v-2s)}} \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \left. \left. \frac{i(b + ci(v-2s) + 2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \right) \Bigg) \Bigg) \Bigg) -
 \end{aligned}$$

$$2^{1-\nu} (-b)^{-2(n+1)} e^e \left(\frac{\nu}{2}\right) \Gamma(2(n+1), -b\sqrt{z}) (1-\nu \bmod 2) ; n \in$$

$\mathbb{N} \wedge$   
 $\nu \in$   
 $\mathbb{N}^+$

**Involving  $z^n e^{bz^r+dz+e} \sin^\nu(cz^r + fz)$**

01.06.21.1527.01

$$\int z^n e^{b z^2 + d z} \sin^v(c z^2 + f z) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( \binom{v}{\frac{v}{2}} (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d + 2 b z)^{q+1} \left( -\frac{(d + 2 b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 b z)^2}{4 b}\right) - \right.$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(d-2i f s + i f v)^2}{4(b-2i c s + i c v)}} \left( \sum_{q=0}^n 2^{q-n} (-d + 2 i f s - i f v)^{n-q} \right. \right.$$

$$\left. \left. (d + f i(v - 2 s) + 2(b - 2 i c s + i c v) z)^{q+1} \left( -\frac{(d + f i(v - 2 s) + 2(b - 2 i c s + i c v) z)^2}{b - 2 i c s + i c v} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \right. \right.$$

$$\left. \left. \Gamma\left(\frac{q+1}{2}, -\frac{(d + f i(v - 2 s) + 2(b - 2 i c s + i c v) z)^2}{4(b - 2 i c s + i c v)}\right) \right) (b - 2 i c s + i c v)^{-n-1} + (-1)^v e^{-\frac{(d+2i f s - i f v)^2}{4(b+2i c s - i c v)}} \right.$$

$$\left. (b + 2 i c s - i c v)^{-n-1} \sum_{q=0}^n 2^{q-n} (-d - 2 i f s + i f v)^{n-q} (d + 2 i f s - i f v + 2 b z + 4 i c s z - 2 i c v z)^{q+1} \right.$$

$$\left. \left( -\frac{(d + 2 i f s - i f v + 2 b z + 4 i c s z - 2 i c v z)^2}{b + 2 i c s - i c v} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \right.$$

$$\left. \left. \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2 i f s - i f v + 2 b z + 4 i c s z - 2 i c v z)^2}{4(b + 2 i c s - i c v)}\right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1528.01

$$\int z^n e^{\sqrt{z} b + d z} \sin^v(\sqrt{z} c + f z) dz =$$

$$2^{-2n-v-1} e^{-\frac{b^2}{4d}} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2 d \sqrt{z})^{h+k} \left( -\frac{(b + 2 d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b + 2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) + \right.$$

$$\left. \left. 2 \sqrt{-\frac{(b + 2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) \right) \right) d^{-2n-2} + 2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\begin{aligned}
 & \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4(d+fi(2s-v))}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} (b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^{h+k} \right. \\
 & \quad \left( -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(2s-v))(b+ci(2s-v) + \right. \\
 & \quad \left. 2(d+fi(2s-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) + 2 \right. \\
 & \quad \left. \sqrt{-\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)}} (d+fi(2s-v)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \quad \left. \left. -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) \right) \left. \right) \left( (d+fi(2s-v))^{-2n-2} + e^{-\frac{(b+ci(v-2s))^2}{4(d+fi(v-2s))}} \right. \\
 & \quad \left. (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n} (b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^{h+k} \right. \\
 & \quad \left( -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s) + \right. \\
 & \quad \left. 2(d+fi(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) + \right. \\
 & \quad \left. 2 \sqrt{-\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} (d+fi(v-2s)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \quad \left. \left. -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) \right) \left. \right) \Bigg/ ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{bz^r+dz+e} \sin^v(cz^r+fz)$

01.06.21.1529.01

$$\int z^n e^{bz^2+dz+e} \sin^v(cz^2+fz) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( e^e \left( \frac{v}{2} \right) (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left( -\frac{(d+2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz)^2}{4b}\right) - \right.$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(d-2ifs+ifv)^2}{4(b-2ics+icv)}} \left( \sum_{q=0}^n 2^{q-n} (-d+2ifs-ifv)^{n-q} \right. \right.$$

$$\left. \left. (d+fi(v-2s)+2(b-2ics+icv)z)^{q+1} \left( -\frac{(d+fi(v-2s)+2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \right. \right.$$

$$\left. \left. \Gamma\left(\frac{q+1}{2}, -\frac{(d+fi(v-2s)+2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) (b-2ics+icv)^{-n-1} + (-1)^v e^{-\frac{(d+2ifs-ifv)^2}{4(b+2ics-icv)}} \right.$$

$$\left. (b+2ics-icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (-d-2ifs+ifv)^{n-q} (d+2ifs-ifv+2bz+4icsz-2icvz)^{q+1} \right.$$

$$\left. \left( -\frac{(d+2ifs-ifv+2bz+4icsz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \right.$$

$$\left. \left. \Gamma\left(\frac{q+1}{2}, -\frac{(d+2ifs-ifv+2bz+4icsz-2icvz)^2}{4(b+2ics-icv)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1530.01

$$\int z^n e^{\sqrt{z}bz+dz+e} \sin^v(\sqrt{z}c+fz) dz =$$

$$2^{-2n-v-1} e^{-\frac{b^2}{4d}} \left( \frac{v}{2} \right) (1-v \bmod 2) \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2d\sqrt{z})^{h+k} \left( -\frac{(b+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+2d\sqrt{z})^2}{4d}\right) + \right.$$

$$\left. \left. 2\sqrt{-\frac{(b+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+2d\sqrt{z})^2}{4d}\right) \right) \right) d^{-2n-2} + 2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\begin{aligned}
 & \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4(d+fi(2s-v))}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} (b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^{h+k} \right. \right. \\
 & \left. \left( -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(2s-v))(b+ci(2s-v) + \right. \right. \\
 & \left. \left. 2(d+fi(2s-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) + 2 \right. \right. \\
 & \left. \sqrt{-\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)}} (d+fi(2s-v)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \left. \left. -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) \right) \left. \right) \left( (d+fi(2s-v))^{-2n-2} + e^{-\frac{(b+ci(v-2s))^2}{4(d+fi(v-2s))}} \right. \\
 & (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n} (b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^{h+k} \\
 & \left. \left( -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s) + \right. \right. \\
 & \left. \left. 2(d+fi(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) + \right. \right. \\
 & \left. \left. 2 \sqrt{-\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} (d+fi(v-2s)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \right. \\
 & \left. \left. -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) \right) \right) \left. \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{dz} \sin^v(cz^r + fz + g)$



01.06.21.1531.01

$$\int z^n e^{dz} \sin^v(cz^2 + fz + g) dz = -2^{-v} \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1 - v \bmod 2) (-d)^{-n-1} -$$

$$2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{-ic(v-2k)}} \left( e^{-\frac{i(d-if(v-2k))^2 + i\pi v}{4c(v-2k)} - ig(v-2k)} \sum_{q=0}^n 2^{q-n} (-ic(v-2k))^{-n-\frac{1}{2}} (if(v-2k) - d)^{n-q} \right. \right.$$

$$(d - if(v-2k) - 2ic(v-2k)z)^{q+1} \left( -\frac{i(d - if(v-2k) - 2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d - if(v-2k) - 2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) + \right.$$

$$\frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{i(d+fi(v-2k))^2 + g i(v-2k) - i\pi v}{4c(v-2k)}} \sum_{q=0}^n 2^{q-n} (ic(v-2k))^{-n-\frac{1}{2}} (-d - if(v-2k))^{n-q} \right.$$

$$(d + fi(v-2k) + 2ci(v-2k)z)^{q+1} \left( \frac{i(d + fi(v-2k) + 2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d + fi(v-2k) + 2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1532.01

$$\int z^n e^{dz} \sin^v(\sqrt{z}c + fz + g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2 + g i(2s-v)}{4(d+fi(2s-v))}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(2s-v))^{-h-k+2n} (2\sqrt{z}(d + fi(2s-v)) + \right. \right.$$

$$ci(2s-v))^{h+k} \left( -\frac{(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v))^2}{d + fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( ci(2s-v)(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v)) \Gamma\left(\frac{1}{2}(h+k+1), \right. \right. \right.$$

$$\left. \left. -\frac{(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v))^2}{4(d + fi(2s-v))} \right) + 2(d + fi(2s-v)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right.$$

$$\left. - \frac{(2\sqrt{z}(d+fi(2s-v))+ci(2s-v))^2}{4(d+fi(2s-v))} \right) \sqrt{-\frac{(2\sqrt{z}(d+fi(2s-v))+ci(2s-v))^2}{d+fi(2s-v)}} \Bigg)$$

$$(d+fi(2s-v))^{-2n-2} + e^{\frac{c^2(v-2s)^2}{4(d+fi(v-2s))+gi(v-2s)}+gi(v-2s)} (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(v-2s))^{-h-k+2n}$$

$$(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^{h+k} \left( -\frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( ci(v-2s)(ci(v-2s)+2(d+fi(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1)\right) \right.$$

$$\left. - \frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} + 2(d+fi(v-2s)) \Gamma\left(\frac{1}{2}(h+k+2)\right) \right.$$

$$\left. - \frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} \right) \sqrt{-\frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} \Bigg) -$$

$$2^{-v} (-d)^{-n-1} \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1-v \bmod 2) /; n \in$$

$$\mathbb{N} \wedge$$

$$v \in$$

$$\mathbb{N}^+$$

**Involving  $z^n e^{dz+e} \sin^v(cz^r + fz + g)$**

01.06.21.1533.01

$$\int z^n e^{dz+e} \sin^v(cz^2 + fz + g) dz = -2^{-v} e^e \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1 - v \bmod 2) (-d)^{-n-1} -$$

$$2^{-v-1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{1}{\sqrt{-ic(v-2k)}} \left( e^{-\frac{i(d-if(v-2k))^2}{4c(v-2k)} + e + \frac{i\pi v}{2} - ig(v-2k)} \sum_{q=0}^n 2^{q-n} (-ic(v-2k))^{-n-\frac{1}{2}} (if(v-2k) - d)^{n-q} \right. \right.$$

$$(d - if(v-2k) - 2ic(v-2k)z)^{q+1} \left( -\frac{i(d - if(v-2k) - 2ic(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(d - if(v-2k) - 2ic(v-2k)z)^2}{4c(v-2k)}\right) \right) + \right.$$

$$\frac{1}{\sqrt{ic(v-2k)}} \left( e^{\frac{i(d+fi(v-2k))^2}{4c(v-2k)} + e + g + i(v-2k) - \frac{i\pi v}{2}} \sum_{q=0}^n 2^{q-n} (ic(v-2k))^{-n-\frac{1}{2}} (-d - if(v-2k))^{n-q} \right.$$

$$(d + fi(v-2k) + 2ci(v-2k)z)^{q+1} \left( \frac{i(d + fi(v-2k) + 2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(d + fi(v-2k) + 2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1534.01

$$\int z^n e^{dz+e} \sin^v(\sqrt{z}c + fz + g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{c^2(2s-v)^2}{4(d+fi(2s-v))} + e + g + i(2s-v)} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(2s-v))^{-h-k+2n} \right.$$

$$(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v))^{h+k} \left( -\frac{(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v))^2}{d + fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\left. \binom{k}{h} \binom{n}{k} \left( ci(2s-v)(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v)) \right. \right.$$

$$\left. \left. \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2\sqrt{z}(d + fi(2s-v)) + ci(2s-v))^2}{4(d + fi(2s-v))}\right) + 2(d + fi(2s-v)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right.$$

$$\left. - \frac{(2\sqrt{z}(d+fi(2s-v))+ci(2s-v))^2}{4(d+fi(2s-v))} \right) \sqrt{-\frac{(2\sqrt{z}(d+fi(2s-v))+ci(2s-v))^2}{d+fi(2s-v)}} \Bigg)$$

$$(d+fi(2s-v))^{-2n-2} + e^{\frac{c^2(v-2s)^2}{4(d+fi(v-2s))+g}+gi(v-2s)+e} (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ic(v-2s))^{-h-k+2n}$$

$$(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^{h+k} \left( -\frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( ci(v-2s)(ci(v-2s)+2(d+fi(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1)\right) \right.$$

$$\left. - \frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} + 2(d+fi(v-2s)) \Gamma\left(\frac{1}{2}(h+k+2)\right) \right.$$

$$\left. - \frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))} \right) \sqrt{-\frac{(ci(v-2s)+2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} \Bigg) -$$

$$2^{-v} (-d)^{-n-1} e^e \left(\frac{v}{2}\right) \Gamma(n+1, -dz) (1-v \bmod 2) ; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

**Involving  $z^n e^{bz^r} \sin^v(cz^r + fz + g)$**

01.06.21.1535.01

$$\int z^n e^{bz^2} \sin^v(cz^2 + fz + g) dz = -2^{-v-1} z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(ifv-2ifs)^2}{4(b-2ics+icv)} + gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (2ifs - ifv)^{n-q} (fi(v-2s) + 2(b-2ics+icv)z)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(fi(v-2s) + 2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(fi(v-2s) + 2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right)$$

$$(b-2ics+icv)^{-n-1} + (-1)^v e^{-\frac{(2ifs-ifv)^2}{4(b+2ics-icv)} + gi(2s-v)} (b+2ics-icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (ifv - 2ifs)^{n-q}$$

$$(2ifs + 4iczs - ifv + 2bz - 2icvz)^{q+1} \left( -\frac{(2ifs + 4iczs - ifv + 2bz - 2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ifs + 4iczs - ifv + 2bz - 2icvz)^2}{4(b+2ics-icv)}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1536.01

$$\int z^n e^{\sqrt{z} b} \sin^v(\sqrt{z} c + fz + g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{i(b+ci(2s-v))^2}{4f(2s-v)} + gi(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} \right. \right.$$

$$\left. \left. (b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^{h+k} \left( \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \right) \right)$$

$$\binom{k}{h} \binom{n}{k} \left( (b+ci(2s-v))(b+ci(2s-v) + 2fi(2s-v)\sqrt{z}) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right) + 2 \right.$$

$$\left. fi(2s-v) \sqrt{\frac{i(b+ci(2s-v) + 2fi(2s-v)\sqrt{z})^2}{f(2s-v)}} \right)$$

$$\Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+ci(2s-v)+2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right)\Bigg)\Bigg)\Bigg)(if(2s-v))^{-2n-2} +$$

$$e^{\frac{i(b+ci(v-2s))^2}{4f(v-2s)}+g} i^{i(v-2s)} (if(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n}$$

$$(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^{h+k} \left(\frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{f(v-2s)}\right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s)+2fi(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + 2fi(v-2s) \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \right) \sqrt{\frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{f(v-2s)}}\Bigg)$$

$$2^{1-v} (-b)^{-2(n+1)} \binom{v}{\frac{v}{2}} \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) /; n \in$$

$\mathbb{N} \wedge$   
 $v \in$   
 $\mathbb{N}^+$

Involving  $z^n e^{bz^r+e} \sin^v(cz^r + fz + g)$

01.06.21.1537.01

$$\int z^n e^{bz^2+e} \sin^v(cz^2+fz+g) dz = -2^{-v-1} e^e z^{n+1} \left(\frac{v}{2}\right) \Gamma\left(\frac{n+1}{2}, -bz^2\right) (1-v \bmod 2) (-bz^2)^{\frac{1}{2}(-n-1)} -$$

$$i^{-v} 2^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(ifv-2ifs)^2}{4(b-2ics+icv)}+e+gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (2ifs-ifv)^{n-q} (fi(v-2s)+2(b-2ics+icv)z)^{q+1} \right. \right.$$

$$\left. \left. \left( -\frac{(fi(v-2s)+2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(fi(v-2s)+2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right)$$

$$(b-2ics+icv)^{-n-1} + (-1)^v e^{-\frac{(2ifs-ifv)^2}{4(b+2ics-icv)}+e+gi(2s-v)} (b+2ics-icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (ifv-2ifs)^{n-q}$$

$$(2ifs+4icsz-ifv+2bz-2icvz)^{q+1} \left( -\frac{(2ifs+4icsz-ifv+2bz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(2ifs+4icsz-ifv+2bz-2icvz)^2}{4(b+2ics-icv)}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1538.01

$$\int z^n e^{\sqrt{z}bz+e} \sin^v(\sqrt{z}c+fz+g) dz =$$

$$i^{-v} 2^{-2n-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{i(b+ci(2s-v))^2}{4f(2s-v)}+e+gi(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} \right. \right.$$

$$\left. \left. (b+ci(2s-v)+2fi(2s-v)\sqrt{z})^{h+k} \left( \frac{i(b+ci(2s-v)+2fi(2s-v)\sqrt{z})^2}{f(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \right) \right)$$

$$\binom{k}{h} \binom{n}{k} \left( (b+ci(2s-v))(b+ci(2s-v)+2fi(2s-v)\sqrt{z}) \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+ci(2s-v)+2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right) + 2 \right.$$

$$\left. fi(2s-v) \sqrt{\frac{i(b+ci(2s-v)+2fi(2s-v)\sqrt{z})^2}{f(2s-v)}} \right)$$

$$\Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+ci(2s-v)+2fi(2s-v)\sqrt{z})^2}{4f(2s-v)}\right)\Bigg)\Bigg)\Bigg)(if(2s-v))^{-2n-2} +$$

$$e^{\frac{i(b+ci(v-2s))^2}{4f(v-2s)}+e+g} i^{i(v-2s)} (if(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n}$$

$$(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^{h+k} \left(\frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{f(v-2s)}\right)^{\frac{1}{2}(-h-k-1)}$$

$$\binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s)+2fi(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) + 2fi(v-2s) \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{4f(v-2s)}\right) \right) \sqrt{\frac{i(b+ci(v-2s)+2fi(v-2s)\sqrt{z})^2}{f(v-2s)}} \Bigg)$$

$$2^{1-v} (-b)^{-2(n+1)} e^e \left(\frac{v}{2}\right) \Gamma(2(n+1), -b\sqrt{z}) (1-v \bmod 2) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving  $z^n e^{bz^r+dz} \sin^v(cz^r + fz + g)$



01.06.21.1539.01

$$\int z^n e^{bz^2+dz} \sin^v(cz^2+fz+g) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b} \left(\frac{v}{2}\right)} (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d+2bz)^{q+1} \left(-\frac{(d+2bz)^2}{b}\right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2bz)^2}{4b}\right) -$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}} \left( e^{-\frac{(d-2ifs+ifv)^2}{4(b-2ics+icv)} + gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (-d+2ifs-ifv)^{n-q} \right. \right.$$

$$\left. \left. (d+fi(v-2s)+2(b-2ics+icv)z)^{q+1} \left( -\frac{(d+fi(v-2s)+2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \right. \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+fi(v-2s)+2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) (b-2ics+icv)^{-n-1} + \right.$$

$$\left. (-1)^v e^{-\frac{(d+2ifs-ifv)^2}{4(b+2ics-icv)} + gi(2s-v)} (b+2ics-icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (-d-2ifs+ifv)^{n-q} (d+2ifs- \right.$$

$$\left. ifv+2bz+4icsz-2icvz)^{q+1} \left( -\frac{(d+2ifs-ifv+2bz+4icsz-2icvz)^2}{b+2ics-icv} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d+2ifs-ifv+2bz+4icsz-2icvz)^2}{4(b+2ics-icv)}\right) \right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1540.01

$$\int z^n e^{\sqrt{z}bz+dz} \sin^v(\sqrt{z}c+fz+g) dz =$$

$$2^{-2n-v-1} e^{-\frac{b^2}{4d} \left(\frac{v}{2}\right)} (1-v \bmod 2) \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b+2d\sqrt{z})^{h+k} \left( -\frac{(b+2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \binom{k}{h} \binom{n}{k} \left( b(b+2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+2d\sqrt{z})^2}{4d}\right) + \right. \right.$$

$$\left. \left. 2\sqrt{-\frac{(b+2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+2d\sqrt{z})^2}{4d}\right) \right) \right) d^{-2n-2} + 2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\begin{aligned}
 & \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4(d+fi(2s-v))} + gi(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} (b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^{h+k} \right. \right. \\
 & \left. \left( -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(2s-v))(b+ci(2s-v) + \right. \right. \\
 & \left. \left. 2(d+fi(2s-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) + 2 \right. \right. \\
 & \left. \sqrt{-\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)}} (d+fi(2s-v)) \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) \right) \right) (d+fi(2s-v))^{-2n-2} + \\
 & e^{-\frac{(b+ci(v-2s))^2}{4(d+fi(v-2s))} + gi(v-2s)} (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n} \\
 & (b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^{h+k} \left( -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z}) \Gamma\left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+k+1), -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) + \right. \\
 & \left. 2 \sqrt{-\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} (d+fi(v-2s)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \left. \left. -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) \right) \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^n e^{bz^2+dz+e} \sin^v(cz^r + fz + g)$**

01.06.21.1541.01

$$\int z^n e^{bz^2+dz+e} \sin^v(cz^2 + fz + g) dz =$$

$$2^{-v-1} b^{-n-1} e^{-\frac{d^2}{4b}} \left( e^e \left( \frac{v}{2} \right) (v \bmod 2 - 1) \sum_{q=0}^n 2^{q-n} (-d)^{n-q} (d + 2bz)^{q+1} \left( -\frac{(d + 2bz)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2bz)^2}{4b}\right) -$$

$$i^{-v} b^{n+1} e^{\frac{d^2}{4b}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{(d-2ifs+ifv)^2}{4(b-2ics+icv)} + e+gi(v-2s)} \left( \sum_{q=0}^n 2^{q-n} (-d + 2ifs - ifv)^{n-q} \right. \right.$$

$$\left. \left. (d + fi(v-2s) + 2(b-2ics+icv)z)^{q+1} \left( -\frac{(d + fi(v-2s) + 2(b-2ics+icv)z)^2}{b-2ics+icv} \right)^{\frac{1}{2}(-q-1)} \right. \right.$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + fi(v-2s) + 2(b-2ics+icv)z)^2}{4(b-2ics+icv)}\right) \right) \right) (b-2ics+icv)^{-n-1} +$$

$$(-1)^v e^{-\frac{(d+2ifs-ifv)^2}{4(b+2ics-icv)} + e+gi(2s-v)} (b + 2ics - icv)^{-n-1} \sum_{q=0}^n 2^{q-n} (-d - 2ifs + ifv)^{n-q} (d + 2ifs -$$

$$ifv + 2bz + 4icsz - 2icvz)^{q+1} \left( -\frac{(d + 2ifs - ifv + 2bz + 4icsz - 2icvz)^2}{b + 2ics - icv} \right)^{\frac{1}{2}(-q-1)}$$

$$\left. \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(d + 2ifs - ifv + 2bz + 4icsz - 2icvz)^2}{4(b + 2ics - icv)}\right) \right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1542.01

$$\int z^n e^{\sqrt{z}bz+dz+e} \sin^v(\sqrt{z}c + fz + g) dz =$$

$$2^{-2n-v-1} e^{-\frac{b^2}{4d}} \left( \frac{v}{2} \right) (1 - v \bmod 2) \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k b^{-h-k+2n} (b + 2d\sqrt{z})^{h+k} \left( -\frac{(b + 2d\sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-k-1)} \right.$$

$$\left. \left. \binom{k}{h} \binom{n}{k} \left( b(b + 2d\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b + 2d\sqrt{z})^2}{4d}\right) \right) \right) +$$

$$\left. \left. 2\sqrt{-\frac{(b + 2d\sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b + 2d\sqrt{z})^2}{4d}\right) \right) \right) \Bigg) d^{-2n-2} + 2^{-2n-v-1} i^{-v} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}$$

$$\begin{aligned}
 & \left( (-1)^v e^{-\frac{(b+ci(2s-v))^2}{4(d+fi(2s-v))} + e+gi(2s-v)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(2s-v))^{-h-k+2n} (b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^{h+k} \right. \right. \\
 & \left. \left. \left( -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( (b+ci(2s-v))(b+ci(2s-v) + \right. \right. \right. \\
 & \left. \left. \left. 2(d+fi(2s-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) + 2 \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{d+fi(2s-v)}} (d+fi(2s-v)) \right. \right. \right. \\
 & \left. \left. \left. \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(b+ci(2s-v) + 2(d+fi(2s-v))\sqrt{z})^2}{4(d+fi(2s-v))}\right) \right) \right) \right) (d+fi(2s-v))^{-2n-2} + \\
 & e^{-\frac{(b+ci(v-2s))^2}{4(d+fi(v-2s))} + e+gi(v-2s)} (d+fi(v-2s))^{-2n-2} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (b+ci(v-2s))^{-h-k+2n} \\
 & (b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^{h+k} \left( -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)} \right)^{\frac{1}{2}(-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left( (b+ci(v-2s))(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z}) \Gamma\left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+k+1), -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) + \right. \\
 & \left. 2 \sqrt{-\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{d+fi(v-2s)}} (d+fi(v-2s)) \Gamma\left(\frac{1}{2}(h+k+2), \right. \right. \\
 & \left. \left. -\frac{(b+ci(v-2s) + 2(d+fi(v-2s))\sqrt{z})^2}{4(d+fi(v-2s))}\right) \right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving products of the direct functions, exponential and a power functions

Involving products of two direct functions, exponential and a power functions

#### Involving $z^{\alpha-1} e^{pz} \sin(cz) \sin(az)$

01.06.21.1543.01

$$\int z^{\alpha-1} e^{pz} \sin(cz) \sin(az) dz = -\frac{1}{4} z^{\alpha} (\Gamma(\alpha, (-ia+ic-p)z) ((-ia+ic-p)z)^{-\alpha} - ((ia+ic-p)z)^{-\alpha} \Gamma(\alpha, (ia+ic-p)z) - ((-ia-ic-p)z)^{-\alpha} \Gamma(\alpha, (-ia-ic-p)z) + ((ia-ic-p)z)^{-\alpha} \Gamma(\alpha, (ia-ic-p)z))$$

#### Involving $z^{\alpha-1} e^{pz} \sin(cz) \sin(az+b)$

01.06.21.1544.01

$$\int z^{\alpha-1} e^{pz} \sin(cz) \sin(az+b) dz = -\frac{1}{4} e^{-ib} z^{\alpha} (e^{2ib} \Gamma(\alpha, (-ia+ic-p)z) ((-ia+ic-p)z)^{-\alpha} - ((ia+ic-p)z)^{-\alpha} \Gamma(\alpha, (ia+ic-p)z) - e^{2ib} ((-ia-ic-p)z)^{-\alpha} \Gamma(\alpha, (-ia-ic-p)z) + ((ia-ic-p)z)^{-\alpha} \Gamma(\alpha, (ia-ic-p)z))$$

#### Involving $z^{\alpha-1} e^{pz} \sin(cz+d) \sin(az+b)$

01.06.21.1545.01

$$\int z^{\alpha-1} e^{pz} \sin(d+cz) \sin(b+az) dz = -\frac{1}{4} e^{-ib-id} z^{\alpha} (e^{2ib} \Gamma(\alpha, (-ia+ic-p)z) ((-ia+ic-p)z)^{-\alpha} - ((ia+ic-p)z)^{-\alpha} \Gamma(\alpha, (ia+ic-p)z) + e^{2id} (((ia-ic-p)z)^{-\alpha} \Gamma(\alpha, (ia-ic-p)z) - e^{2ib} ((-ia-ic-p)z)^{-\alpha} \Gamma(\alpha, (-ia-ic-p)z)))$$

#### Involving $z^n e^{pz} \sin(bz) \sin(cz)$

01.06.21.1546.01

$$\int z^n e^{pz^2} \sin(bz) \sin(cz) dz = \frac{1}{8} e^{-\frac{b^2-c^2}{2p}} p^{-n-1} \left( -e^{\frac{(ib+ic)^2}{4p}} \sum_{q=0}^n 2^{q-n} (ib-ic)^{n-q} (-ib+ic+2pz)^{q+1} \left( -\frac{(-ib+ic+2pz)^2}{p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(-ib+ic+2pz)^2}{4p}\right) + e^{\frac{(-ib+ic)^2}{4p}} \sum_{q=0}^n 2^{q-n} (-ib-ic)^{n-q} (ib+ic+2pz)^{q+1} \left( -\frac{(ib+ic+2pz)^2}{p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ib+ic+2pz)^2}{4p}\right) - e^{\frac{(ib+ic)^2}{4p}} \sum_{q=0}^n 2^{q-n} (-ib+ic)^{n-q} (ib-ic+2pz)^{q+1} \left( -\frac{(ib-ic+2pz)^2}{p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ib-ic+2pz)^2}{4p}\right) + e^{\frac{(-ib+ic)^2}{4p}} \sum_{q=0}^n 2^{q-n} (ib+ic)^{n-q} \left( -\frac{(ib+ic-2pz)^2}{p} \right)^{\frac{1}{2}(-q-1)} (-ib-ic+2pz)^{q+1} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ib+ic-2pz)^2}{4p}\right) \right); n \in \mathbb{N}$$

01.06.21.1547.01

$$\int z^n e^{p\sqrt{z}} \sin(bz) \sin(cz) dz = 2^{-2n-3} \left( e^{\frac{p^2}{4ib-4ic}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k p^{-h-k+2n} (2\sqrt{z}(-ib+ic)+p)^{h+k} \left( \frac{(2\sqrt{z}(-ib+ic)+p)^2}{ib-ic} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( p(2\sqrt{z}(-ib+ic)+p) \Gamma\left(\frac{1}{2}(h+k+1), \frac{(2\sqrt{z}(-ib+ic)+p)^2}{4ib-4ic}\right) + 2(-ib+ic) \sqrt{\frac{(2\sqrt{z}(-ib+ic)+p)^2}{ib-ic}} \Gamma\left(\frac{1}{2}(h+k+2), \frac{(2\sqrt{z}(-ib+ic)+p)^2}{4ib-4ic}\right) \right) \right) \right) (-ib+ic)^{-2(n+1)} - (-ib-ic)^{-2(n+1)} e^{\frac{p^2}{4ib+4ic}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k p^{-h-k+2n} (p-2(ib+ic)\sqrt{z})^{h+k} \left( \frac{(p-2(ib+ic)\sqrt{z})^2}{ib+ic} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( p(p-2(ib+ic)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{(p-2(ib+ic)\sqrt{z})^2}{4(ib+ic)}\right) - \right)$$

$$\begin{aligned}
 & 2(i b+i c) \sqrt{\frac{(p-2(i b+i c) \sqrt{z})^2}{i b+i c}} \Gamma\left(\frac{1}{2}(h+k+2), \frac{(p-2(i b+i c) \sqrt{z})^2}{4(i b+i c)}\right) \Bigg| - \\
 & (i b+i c)^{-2(n+1)} e^{-\frac{p^2}{-4 i b-4 i c}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k p^{-h-k+2 n}(2 \sqrt{z}(i b+i c)+p)^{h+k} \left(-\frac{(2 \sqrt{z}(i b+i c)+p)^2}{i b+i c}\right)^{\frac{1}{2}(-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left(p(2 \sqrt{z}(i b+i c)+p) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2 \sqrt{z}(i b+i c)+p)^2}{4(i b+i c)}\right)\right) + \\
 & 2 \sqrt{-\frac{(2 \sqrt{z}(i b+i c)+p)^2}{i b+i c}} (i b+i c) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2 \sqrt{z}(i b+i c)+p)^2}{4(i b+i c)}\right) \Bigg| + \\
 & (i b-i c)^{-2(n+1)} e^{-\frac{p^2}{-4 i b+4 i c}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k p^{-h-k+2 n}(2 \sqrt{z}(i b-i c)+p)^{h+k} \left(-\frac{(2 \sqrt{z}(i b-i c)+p)^2}{i b-i c}\right)^{\frac{1}{2}(-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left(p(2 \sqrt{z}(i b-i c)+p) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(2 \sqrt{z}(i b-i c)+p)^2}{4 i b-4 i c}\right)\right) + \\
 & 2 \sqrt{-\frac{(2 \sqrt{z}(i b-i c)+p)^2}{i b-i c}} (i b-i c) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(2 \sqrt{z}(i b-i c)+p)^2}{4 i b-4 i c}\right) \Bigg| \Bigg| ; n \in \mathbb{N}
 \end{aligned}$$

**Involving  $z^n e^{p z} \sin(b z^r) \sin(c z)$**

01.06.21.1548.01

$$\int z^n e^{p z} \sin(b z^2) \sin(c z) dz = -\frac{1}{8} (i b)^{-n-1} e^{\frac{3 i(i c+p)^2}{4 b}} \left( e^{-\frac{i(-c^2+4 i p c+p^2)}{2 b}} \sum_{q=0}^n 2^{q-n} (i c-p)^{n-q} (-i c+p+2 i b z)^{q+1} \left( \frac{i(-i c+p+2 i b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(-i c+p+2 i b z)^2}{4 b}\right) - e^{-\frac{i(i c+p)^2}{2 b}} \sum_{q=0}^n 2^{q-n} (-i c-p)^{n-q} (i c+p+2 i b z)^{q+1} \left( \frac{i(i c+p+2 i b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{i(i c+p+2 i b z)^2}{4 b}\right) + (-1)^{n-1} \left( e^{-\frac{i(i c+p)^2}{b}} \sum_{q=0}^n 2^{q-n} (-i c-p)^{n-q} (i c+p-2 i b z)^{q+1} \left( -\frac{i(i c+p-2 i b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(i c+p-2 i b z)^2}{4 b}\right) - e^{-\frac{i(-c^2+i p c+p^2)}{b}} \sum_{q=0}^n 2^{q-n} (i c-p)^{n-q} (-i c+p-2 i b z)^{q+1} \left( -\frac{i(i c-p+2 i b z)^2}{b} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{i(i c-p+2 i b z)^2}{4 b}\right) \right) / ; n \in \mathbb{N}$$

01.06.21.1549.01

$$\int z^n e^{p z} \sin(b \sqrt{z}) \sin(c z) dz = 2^{-2 n-3} \left( e^{\frac{b^2}{4(-i c+p)}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (i b)^{-h-k+2 n} (i b+2(-i c+p) \sqrt{z})^{h+k} \left( -\frac{(i b+2(-i c+p) \sqrt{z})^2}{-i c+p} \right)^{\frac{1}{2}(-h-k-1)} \binom{k}{h} \binom{n}{k} \left( b i(i b+2(-i c+p) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(i b+2(-i c+p) \sqrt{z})^2}{4(-i c+p)}\right) + 2 \sqrt{-\frac{(i b+2(-i c+p) \sqrt{z})^2}{-i c+p}} (-i c+p) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(i b+2(-i c+p) \sqrt{z})^2}{4(-i c+p)}\right) \right) \right) (-i c+p)^{-2(n+1)} - e^{\frac{b^2}{4(-i c+p)}} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-i b)^{-h-k+2 n} \left( -\frac{(i b-2(-i c+p) \sqrt{z})^2}{-i c+p} \right)^{\frac{1}{2}(-h-k-1)} (-i b+2(-i c+p) \sqrt{z})^{h+k} \right) \right)$$



$$\begin{aligned}
 & \binom{k}{h} \binom{n}{k} \left( 2(-ic+p) \sqrt{-\frac{(ib-2(-ic+p)\sqrt{z})^2}{-ic+p}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(ib-2(-ic+p)\sqrt{z})^2}{4(-ic+p)}\right) - \right. \\
 & \left. ib(-ib+2(-ic+p)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(ib-2(-ic+p)\sqrt{z})^2}{4(-ic+p)}\right) \right) \left( (-ic+p)^{-2(n+1)} - \right. \\
 & \left. e^{\frac{b^2}{4(ic+p)}} (ic+p)^{-2(n+1)} \left( \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ib)^{-h-k+2n} (ib+2(ic+p)\sqrt{z})^{h+k} \left( -\frac{(ib+2(ic+p)\sqrt{z})^2}{ic+p} \right)^{\frac{1}{2}(-h-k-1)} \right. \right. \\
 & \left. \left. \binom{k}{h} \binom{n}{k} \left( bi(ib+2(ic+p)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(ib+2(ic+p)\sqrt{z})^2}{4(ic+p)}\right) + \right. \right. \\
 & \left. \left. 2\sqrt{-\frac{(ib+2(ic+p)\sqrt{z})^2}{ic+p}} (ic+p) \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(ib+2(ic+p)\sqrt{z})^2}{4(ic+p)}\right) \right) \right) - \right. \\
 & \left. \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ib)^{-h-k+2n} \left( -\frac{(ib-2(ic+p)\sqrt{z})^2}{ic+p} \right)^{\frac{1}{2}(-h-k-1)} (-ib+2(ic+p)\sqrt{z})^{h+k} \right. \\
 & \left. \binom{k}{h} \binom{n}{k} \left( 2(ic+p) \sqrt{-\frac{(ib-2(ic+p)\sqrt{z})^2}{ic+p}} \Gamma\left(\frac{1}{2}(h+k+2), -\frac{(ib-2(ic+p)\sqrt{z})^2}{4(ic+p)}\right) - \right. \right. \\
 & \left. \left. ib(-ib+2(ic+p)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), -\frac{(ib-2(ic+p)\sqrt{z})^2}{4(ic+p)}\right) \right) \right) \Bigg) /; n \in \mathbb{N}
 \end{aligned}$$

Involving  $z^n e^{pz^r} \sin(bz^r) \sin(cz)$

01.06.21.1550.01

$$\int z^n e^{p z^2} \sin(b z^2) \sin(c z) dz = \frac{1}{8} e^{-\frac{c^2 p}{-2b^2-2p^2}} (b^2 + p^2)^{-n-1} \left( e^{-\frac{c^2}{4(ib+p)}} (ib+p)^{n+1} \right. \\ \left. \left( \sum_{q=0}^n 2^{q-n} (ic)^{n-q} \left( \frac{(ic+2(ib-p)z)^2}{ib-p} \right)^{\frac{1}{2}(-q-1)} (-ic-2ibz+2pz)^{q+1} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{(ic+2(ib-p)z)^2}{4(ib-p)}\right) - \right. \right. \\ \left. \left. \sum_{q=0}^n 2^{q-n} (-ic)^{n-q} (ic+2(-ib+p)z)^{q+1} \left( \frac{(ic+2(-ib+p)z)^2}{ib-p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, \frac{(ic+2(-ib+p)z)^2}{4(ib-p)}\right) \right) \right) \\ e^{-\frac{c^2}{-4ib+4p}} (-ib+p)^{n+1} \left( \sum_{q=0}^n 2^{q-n} (ic)^{n-q} \left( -\frac{(ic-2(ib+p)z)^2}{ib+p} \right)^{\frac{1}{2}(-q-1)} (-ic+2(ib+p)z)^{q+1} \right. \\ \left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ic-2(ib+p)z)^2}{4(ib+p)}\right) - \sum_{q=0}^n 2^{q-n} (-ic)^{n-q} (ic+2(ib+p)z)^{q+1} \right. \\ \left. \left. \left( -\frac{(ic+2(ib+p)z)^2}{ib+p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ic+2(ib+p)z)^2}{4(ib+p)}\right) \right) \right) /; n \in \mathbb{N}$$

01.06.21.1551.01

$$\int z^n e^{p \sqrt{z}} \sin(b \sqrt{z}) \sin(c z) dz = 2^{-2n-3} (ic)^{-2(n+1)} e^{\frac{i(-3b^2+2ipb+3p^2)}{4c}} \\ \left( e^{-\frac{i(ib+p)^2}{2c}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ib+p)^{-h-k+2n} (-ib+p+2ic\sqrt{z})^{h+k} \left( \frac{i(-ib+p+2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-h-k-1)} \right. \\ \left. \binom{k}{h} \binom{n}{k} \left( (-ib+p)(-ib+p+2ic\sqrt{z}) \Gamma\left(\frac{1}{2}(h+k+1), \frac{i(-ib+p+2ic\sqrt{z})^2}{4c}\right) + \right. \right. \\ \left. \left. 2 \sqrt{\frac{i(-ib+p+2ic\sqrt{z})^2}{c}} ci \Gamma\left(\frac{1}{2}(h+k+2), \frac{i(-ib+p+2ic\sqrt{z})^2}{4c}\right) \right) \right) - \\ e^{-\frac{i(p^2-b^2)}{2c}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ib+p)^{-h-k+2n} (ib+p+2ic\sqrt{z})^{h+k} \left( \frac{i(ib+p+2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-h-k-1)}$$

$$\begin{aligned}
 & \binom{k}{h} \binom{n}{k} \left( (ib+p)(ib+p+2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), \frac{i(ib+p+2ic\sqrt{z})^2}{4c} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(ib+p+2ic\sqrt{z})^2}{c}} c i \Gamma \left( \frac{1}{2}(h+k+2), \frac{i(ib+p+2ic\sqrt{z})^2}{4c} \right) \right) - \\
 & e^{-\frac{i(p^2-b^2)}{c}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (-ib+p)^{-h-k+2n} (-ib+p-2ic\sqrt{z})^{h+k} \left( -\frac{i(ib-p+2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left( (ib-p)(ib-p+2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(ib-p+2ic\sqrt{z})^2}{4c} \right) - \right. \\
 & \left. 2ic \sqrt{-\frac{i(ib-p+2ic\sqrt{z})^2}{c}} \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(ib-p+2ic\sqrt{z})^2}{4c} \right) \right) + \\
 & e^{-\frac{i(-b^2+ipb+p^2)}{c}} \sum_{k=0}^n \sum_{h=0}^k (-1)^{k-h} 4^k (ib+p)^{-h-k+2n} (ib+p-2ic\sqrt{z})^{h+k} \left( -\frac{i(ib+p-2ic\sqrt{z})^2}{c} \right)^{\frac{1}{2}(-h-k-1)} \\
 & \binom{k}{h} \binom{n}{k} \left( (ib+p)(ib+p-2ic\sqrt{z}) \Gamma \left( \frac{1}{2}(h+k+1), -\frac{i(ib+p-2ic\sqrt{z})^2}{4c} \right) - \right. \\
 & \left. 2ic \sqrt{-\frac{i(ib+p-2ic\sqrt{z})^2}{c}} \Gamma \left( \frac{1}{2}(h+k+2), -\frac{i(ib+p-2ic\sqrt{z})^2}{4c} \right) \right) /; n \in \mathbb{N}
 \end{aligned}$$

Involving  $z^n e^{pZ} \sin(bz^r) \sin(cz^r)$

01.06.21.1552.01

$$\int z^n e^{pz} \sin(bz^2) \sin(cz^2) dz =$$

$$\frac{1}{8} \left( -e^{-\frac{p^2}{4(-ib+ic)}} \left( \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(-ib+ic)z)^{j+1} \left( -\frac{(p+2(-ib+ic)z)^2}{-ib+ic} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(-ib+ic)z)^2}{4(-ib+ic)} \right) \right. \right.$$

$$\left. \left. - \frac{(p+2(-ib+ic)z)^2}{4(-ib+ic)} \right) \right) (-ib+ic)^{-n-1} + (ib+ic)^{-n-1} e^{-\frac{p^2}{4(ib+ic)}}$$

$$\sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(ib+ic)z)^{j+1} \left( -\frac{(p+2(ib+ic)z)^2}{ib+ic} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(ib+ic)z)^2}{4(ib+ic)} \right) +$$

$$(-ib-ic)^{-n-1} e^{-\frac{p^2}{4(-ib-ic)}} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(-ib-ic)z)^{j+1} \left( -\frac{(p+2(-ib-ic)z)^2}{-ib-ic} \right)^{\frac{1}{2}(-j-1)}$$

$$\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(-ib-ic)z)^2}{4(-ib-ic)} \right) - (ib-ic)^{-n-1} e^{-\frac{p^2}{4(ib-ic)}}$$

$$\sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(ib-ic)z)^{j+1} \left( -\frac{(p+2(ib-ic)z)^2}{ib-ic} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(ib-ic)z)^2}{4(ib-ic)} \right) \Big/; n \in \mathbb{N}$$

01.06.21.1553.01

$$\int z^n e^{pz} \sin(b\sqrt{z}) \sin(c\sqrt{z}) dz =$$

$$2^{-2n-3} \left( e^{-\frac{(-ib+ic)^2}{4p}} \left( \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (-ib+ic)^{-h-i+2n} (-ib+ic+2p\sqrt{z})^{h+i} \left( -\frac{(-ib+ic+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-i-1)} \right. \right.$$

$$\left. \binom{i}{h} \binom{n}{i} \left( (-ib+ic)(-ib+ic+2p\sqrt{z}) \Gamma\left(\frac{1}{2}(h+i+1), -\frac{(-ib+ic+2p\sqrt{z})^2}{4p} \right) + \right. \right.$$

$$\left. \left. 2\sqrt{-\frac{(-ib+ic+2p\sqrt{z})^2}{p}} p \Gamma\left(\frac{1}{2}(h+i+2), -\frac{(-ib+ic+2p\sqrt{z})^2}{4p} \right) \right) \right) p^{-2n-2} -$$

$$e^{-\frac{(ib+ic)^2}{4p}} \left( \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (ib+ic)^{-h-i+2n} (ib+ic+2p\sqrt{z})^{h+i} \left( -\frac{(ib+ic+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-i-1)} \right.$$

$$\begin{aligned}
 & \binom{i}{h} \binom{n}{i} \left( (ib+ic)(ib+ic+2p\sqrt{z}) \Gamma \left( \frac{1}{2}(h+i+1), -\frac{(ib+ic+2p\sqrt{z})^2}{4p} \right) + \right. \\
 & \left. 2 \sqrt{-\frac{(ib+ic+2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2}(h+i+2), -\frac{(ib+ic+2p\sqrt{z})^2}{4p} \right) \right) p^{-2n-2} - \\
 & e^{-\frac{(ib-ic)^2}{4p}} \left( \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (-ib-ic)^{-h-i+2n} (-ib-ic+2p\sqrt{z})^{h+i} \left( -\frac{(-ib-ic+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-i-1)} \right. \\
 & \left. \binom{i}{h} \binom{n}{i} \left( (-ib-ic)(-ib-ic+2p\sqrt{z}) \Gamma \left( \frac{1}{2}(h+i+1), -\frac{(-ib-ic+2p\sqrt{z})^2}{4p} \right) + \right. \right. \\
 & \left. \left. 2 \sqrt{-\frac{(-ib-ic+2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2}(h+i+2), -\frac{(-ib-ic+2p\sqrt{z})^2}{4p} \right) \right) \right) p^{-2n-2} + \\
 & e^{-\frac{(ib-ic)^2}{4p}} \left( \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (ib-ic)^{-h-i+2n} (ib-ic+2p\sqrt{z})^{h+i} \left( \frac{(ib-ic+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-i-1)} \right. \\
 & \left. \binom{i}{h} \binom{n}{i} \left( (ib-ic)(ib-ic+2p\sqrt{z}) \Gamma \left( \frac{1}{2}(h+i+1), -\frac{(ib-ic+2p\sqrt{z})^2}{4p} \right) + \right. \right. \\
 & \left. \left. 2 \sqrt{-\frac{(ib-ic+2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2}(h+i+2), -\frac{(ib-ic+2p\sqrt{z})^2}{4p} \right) \right) \right) p^{-2n-2} \Bigg) /; n \in \mathbb{N}
 \end{aligned}$$

Involving  $z^{\alpha-1} e^{pz^r} \sin(bz^r) \sin(cz^r)$

01.06.21.1554.01

$$\int z^{\alpha-1} e^{p z^r} \sin(b z^r) \sin(c z^r) dz =$$

$$\frac{z^\alpha}{4r} \left( -\Gamma\left(\frac{\alpha}{r}, (-ib+ic-p)z^r\right) ((-ib+ic-p)z^r)^{-\frac{\alpha}{r}} + ((ib+ic-p)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib+ic-p)z^r\right) + \right.$$

$$\left. ((-ib-ic-p)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-ib-ic-p)z^r\right) - ((ib-ic-p)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-ic-p)z^r\right) \right)$$

**Involving  $z^{\alpha-1} e^{b z^r + e} \sin(a z^r + q) \sin(c z^r + g)$**

01.06.21.1555.01

$$\int z^{\alpha-1} e^{b z^r + e} \sin(a z^r + q) \sin(c z^r + g) dz =$$

$$\frac{z^\alpha}{4r} \left( -e^{-ig+iq} \Gamma\left(\frac{\alpha}{r}, (-b-ia+ic)z^r\right) ((-b-ia+ic)z^r)^{-\frac{\alpha}{r}} + e^{-ig-iq} ((-b+ia+ic)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+ia+ic)z^r\right) + \right.$$

$$\left. e^{e+ig+iq} ((-b-ic-ia)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ic-ia)z^r\right) - e^{e+ig-iq} ((-b-ic+ia)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ic+ia)z^r\right) \right)$$

**Involving  $z^n e^{b z^r + d z + e} \sin(a z^r + p z + q) \sin(c z^r + f z + g)$**

01.06.21.1556.01

$$\int z^n e^{bz^2+dz+e} \sin(az^2 + pz + q) \sin(cz^2 + fz + g) dz = \frac{1}{8} \left( -e^{-\frac{(d+if-ip)^2}{4(b-ia+ic)} + e+ig-iq} \right. \\ \left. \left( \sum_{j=0}^n 2^{j-n} (-d-if+ip)^{n-j} (d+if-ip+2(b-ia+ic)z)^{j+1} \left( -\frac{(d+if-ip+2(b-ia+ic)z)^2}{b-ia+ic} \right)^{\frac{1}{2}(-j-1)} \right. \right. \\ \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d+if-ip+2(b-ia+ic)z)^2}{4(b-ia+ic)}\right) \right) (b-ia+ic)^{-n-1} + \right. \\ \left. (b+ia+ic)^{-n-1} e^{-\frac{(d+if+ip)^2}{4(b+ia+ic)} + e+ig+iq} \sum_{j=0}^n 2^{j-n} (-d-if-ip)^{n-j} (d+if+ip+2(b+ia+ic)z)^{j+1} \right. \\ \left. \left( -\frac{(d+if+ip+2(b+ia+ic)z)^2}{b+ia+ic} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d+if+ip+2(b+ia+ic)z)^2}{4(b+ia+ic)}\right) \right) + \\ \left. (b-ic-ia)^{-n-1} e^{-\frac{(d-if-ip)^2}{4(b-ic-ia)} + e-ig-iq} \sum_{j=0}^n 2^{j-n} (-d+if+ip)^{n-j} (d-if-ip+2(b-ic-ia)z)^{j+1} \right. \\ \left. \left( -\frac{(d-if-ip+2(b-ic-ia)z)^2}{b-ic-ia} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-if-ip+2(b-ic-ia)z)^2}{4(b-ic-ia)}\right) \right) - \\ \left. (b-ic+ia)^{-n-1} e^{-\frac{(d-if+ip)^2}{4(b-ic+ia)} + e-ig+iq} \sum_{j=0}^n 2^{j-n} (-d+if-ip)^{n-j} (d-if+ip+2(b-ic+ia)z)^{j+1} \right. \\ \left. \left( -\frac{(d-if+ip+2(b-ic+ia)z)^2}{b-ic+ia} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-if+ip+2(b-ic+ia)z)^2}{4(b-ic+ia)}\right) \right) \Bigg) /; n \in \mathbb{N}$$

01.06.21.1557.01

$$\int z^n e^{\sqrt{z}bz+dz+e} \sin(\sqrt{z}a + pz + q) \sin(\sqrt{z}c + fz + g) dz = \\ 2^{-2n-3} \left( -e^{-\frac{(b+ia+ic)^2}{4(d+if+ip)} + e+ig+iq} \left( \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (b+ia+ic)^{-h-i+2n} \right. \right. \\ \left. \left. (b+ia+ic + 2(d+if+ip)\sqrt{z})^{h+i} \left( -\frac{(b+ia+ic + 2(d+if+ip)\sqrt{z})^2}{d+if+ip} \right)^{\frac{1}{2}(-h-i-1)} \right. \right. \\ \left. \left. \binom{i}{h} \binom{n}{i} \right) (b+ia+ic)(b+ia+ic + 2(d+if+ip)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+i+1), \right. \right.$$

$$\begin{aligned}
 & \left. -\frac{(b+ia+ic+2(d+if+ip)\sqrt{z})^2}{4(d+if+ip)} \right) + 2\sqrt{-\frac{(b+ia+ic+2(d+if+ip)\sqrt{z})^2}{d+if+ip}} \\
 & (d+if+ip)\Gamma\left(\frac{1}{2}(h+i+2), -\frac{(b+ia+ic+2(d+if+ip)\sqrt{z})^2}{4(d+if+ip)}\right) \Bigg) \Bigg) (d+if+ip)^{-2n-2} + \\
 & e^{-\frac{(b-ic+ia)^2}{4(d-if+ip)}+e-ig+iq} (d-if+ip)^{-2n-2} \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (b-ic+ia)^{-h-i+2n} (b-ic+ia+2(d-if+ip)\sqrt{z})^{h+i} \\
 & \left( -\frac{(b-ic+ia+2(d-if+ip)\sqrt{z})^2}{d-if+ip} \right)^{\frac{1}{2}(-h-i-1)} \binom{i}{h} \binom{n}{i} \left( (b-ic+ia)(b-ic+ia+2(d-if+ip)\sqrt{z}) \right) \\
 & \Gamma\left(\frac{1}{2}(h+i+1), -\frac{(b-ic+ia+2(d-if+ip)\sqrt{z})^2}{4(d-if+ip)}\right) + 2\sqrt{-\frac{(b-ic+ia+2(d-if+ip)\sqrt{z})^2}{d-if+ip}} \\
 & (d-if+ip)\Gamma\left(\frac{1}{2}(h+i+2), -\frac{(b-ic+ia+2(d-if+ip)\sqrt{z})^2}{4(d-if+ip)}\right) \Bigg) \Bigg) + \\
 & e^{-\frac{(b-ia+ic)^2}{4(d+if-ip)}+e+ig-iq} (d+if-ip)^{-2n-2} \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (b-ia+ic)^{-h-i+2n} (b-ia+ic+2(d+if-ip)\sqrt{z})^{h+i} \\
 & \left( -\frac{(b-ia+ic+2(d+if-ip)\sqrt{z})^2}{d+if-ip} \right)^{\frac{1}{2}(-h-i-1)} \binom{i}{h} \binom{n}{i} \\
 & \left( (b-ia+ic)(b-ia+ic+2(d+if-ip)\sqrt{z}) \right) \Gamma\left(\frac{1}{2}(h+i+1), \right. \\
 & \left. -\frac{(b-ia+ic+2(d+if-ip)\sqrt{z})^2}{4(d+if-ip)}\right) + 2\sqrt{-\frac{(b-ia+ic+2(d+if-ip)\sqrt{z})^2}{d+if-ip}} \\
 & (d+if-ip)\Gamma\left(\frac{1}{2}(h+i+2), -\frac{(b-ia+ic+2(d+if-ip)\sqrt{z})^2}{4(d+if-ip)}\right) \Bigg) \Bigg) -
 \end{aligned}$$



$$e^{-\frac{(b-ic-ia)^2}{4(d-if-ip)}+e-ig-iq} (d-if-ip)^{-2n-2} \sum_{i=0}^n \sum_{h=0}^i (-1)^{i-h} 4^i (b-ic-ia)^{-h-i+2n} (b-ic-ia+2(d-if-ip)\sqrt{z})^{h+i}$$

$$\left( -\frac{(b-ic-ia+2(d-if-ip)\sqrt{z})^2}{d-if-ip} \right)^{\frac{1}{2}(-h-i-1)} \binom{i}{h} \binom{n}{i} \left( (b-ic-ia)(b-ic-ia+2(d-if-ip)\sqrt{z}) \right)$$

$$\Gamma \left( \frac{1}{2}(h+i+1), -\frac{(b-ic-ia+2(d-if-ip)\sqrt{z})^2}{4(d-if-ip)} \right) + 2 \sqrt{-\frac{(b-ic-ia+2(d-if-ip)\sqrt{z})^2}{d-if-ip}}$$

$$(d-if-ip) \Gamma \left( \frac{1}{2}(h+i+2), -\frac{(b-ic-ia+2(d-if-ip)\sqrt{z})^2}{4(d-if-ip)} \right) \Bigg) ; n \in \mathbb{N}$$

Involving products of several direct functions, exponential and a power functions

**Involving  $z^{\alpha-1} e^{pz} \sin(az) \sin(bz) \sin(cz)$**

01.06.21.1558.01

$$\int z^{\alpha-1} e^{pz} \sin(az) \sin(bz) \sin(cz) dz =$$

$$\frac{1}{8} i z^\alpha \left( -\Gamma(\alpha, -(i(a-b-c)+p)z) (-i(a-b-c)+p)z^{-\alpha} + (-i(a+b-c)+p)z^{-\alpha} \Gamma(\alpha, -(i(a+b-c)+p)z) + \right.$$

$$\left. (-i(a-b+c)+p)z^{-\alpha} \Gamma(\alpha, -(i(a-b+c)+p)z) - (-i(a+b+c)+p)z^{-\alpha} \Gamma(\alpha, -(i(a+b+c)+p)z) + \right.$$

$$\left. (i(a-b-c+ip)z)^{-\alpha} \Gamma(\alpha, i(a-b-c+ip)z) - (i(a+b-c+ip)z)^{-\alpha} \Gamma(\alpha, i(a+b-c+ip)z) - \right.$$

$$\left. (i(a-b+c+ip)z)^{-\alpha} \Gamma(\alpha, i(a-b+c+ip)z) + (i(a+b+c+ip)z)^{-\alpha} \Gamma(\alpha, i(a+b+c+ip)z) \right)$$

**Involving  $z^{\alpha-1} e^{pz} \prod_{k=1}^n \sin(a_k z)$**

01.06.21.1559.01

$$\int z^{\alpha-1} e^{pz} \prod_{k=1}^n \sin(a_k z) dz =$$

$$(-2)^{-n-1} z^\alpha \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \left( e^{\frac{1}{2}(-\pi i) \sum_{j=1}^n k_j} \Gamma \left( \alpha, \left( i \sum_{j=1}^n (k_j a_j) - p \right) z \right) \left( \left( i \sum_{j=1}^n (k_j a_j) - p \right) z \right)^{-\alpha} + e^{\frac{1}{2}(\pi i) \sum_{j=1}^n k_j} \right.$$

$$\left. \Gamma \left( \alpha, -\left( i \sum_{j=1}^n (k_j a_j) + p \right) z \right) \left( -\left( i \sum_{j=1}^n (k_j a_j) + p \right) z \right)^{-\alpha} \right)$$

01.06.21.1560.01

$$\int \frac{1}{z} e^{pz} \prod_{k=1}^n \sin(a_k z) dz = \frac{(-1)^n}{2^{n+1}} \sum_{\substack{k_1=-1 \\ \Delta k_1=2}}^1 \sum_{\substack{k_2=-1 \\ \Delta k_2=2}}^1 \dots \sum_{\substack{k_n=-1 \\ \Delta k_n=2}}^1 \left( e^{\frac{1}{2}(\pi i) \sum_{j=1}^n k_j} \text{Ei} \left( \left( p + i \sum_{j=1}^n k_j a_j \right) z \right) + e^{\frac{1}{2}(-\pi i) \sum_{j=1}^n k_j} \text{Ei} \left( \left( p - i \sum_{j=1}^n k_j a_j \right) z \right) \right)$$

### Involving products of powers of the direct function, exponential and a power functions

Involving product of power of the direct function, the direct function, exponential and a power functions

#### Involving $z^{\alpha-1} e^{bz} \sin(cz) \sin^v(az)$

$$\begin{aligned}
 & \int z^{\alpha-1} e^{bz} \sin(cz) \sin^v(az) dz = \\
 & -2^{-1-v} i z^\alpha \left( i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} (-\Gamma(\alpha, -(b+i(c-2ak+av))z)) (-b+i(c-2ak+av))z)^{-\alpha} + \right. \\
 & \quad (-1)^v (-b-i(c-2ak+av))z)^{-\alpha} \Gamma(\alpha, -(b-i(c-2ak+av))z) - (-1)^v (-b+i(c+2ak-av))z)^{-\alpha} \\
 & \quad \Gamma(\alpha, -(b+i(c+2ak-av))z) + (-b-i(c+2ak-av))z)^{-\alpha} \Gamma(\alpha, -(b-i(c+2ak-av))z) + \\
 & \quad \left. \binom{v}{\frac{v}{2}} \left( (-b-ic)z)^{-\alpha} \Gamma(\alpha, icz-bz) - (-b+ic)z)^{-\alpha} \Gamma(\alpha, -(b+ic)z) \right) (1-v \bmod 2) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

$$\begin{aligned}
 & \int z^n e^{bz} \sin(cz) \sin^v(az) dz = \\
 & -\frac{i}{2} (1 - e^{2iaz})^{-v} n! \sin^v(az) \left( e^{(b+ic)z} \sum_{p=0}^n \frac{(-1)^p z^{n-p} (b+i c - i a v)^{-p-1}}{(n-p)!} {}_{p+2}F_{p+1} \left( \frac{-ib+c-av}{2a}, \dots, \frac{-ib+c-av}{2a}, -v; \right. \right. \\
 & \quad \left. \left. 1 + \frac{-ib+c-av}{2a}, \dots, 1 + \frac{-ib+c-av}{2a}; e^{2iaz} \right) - e^{(b-ic)z} \sum_{p=0}^n \frac{(-1)^p z^{n-p} (b-i c - i a v)^{-p-1}}{(n-p)!} \right. \\
 & \quad \left. {}_{p+2}F_{p+1} \left( -\frac{ib+c+av}{2a}, \dots, -\frac{ib+c+av}{2a}, -v; 1 - \frac{ib+c+av}{2a}, \dots, 1 - \frac{ib+c+av}{2a}; e^{2iaz} \right) \right) /; n \in \mathbb{N}
 \end{aligned}$$

#### Involving $z^n e^{bz} \sin(cz+d) \sin^v(az)$

$$\begin{aligned}
 & \int z^{\alpha-1} e^{bz} \sin(d+cz) \sin^v(az) dz = \\
 & -2^{-v-1} i z^\alpha \left( e^{-id} \binom{v}{\frac{v}{2}} \left( (i(c+ib)z)^{-\alpha} \Gamma(\alpha, icz-bz) - e^{2id} ((-b-ic)z)^{-\alpha} \Gamma(\alpha, -bz-icz) \right) (1-v \bmod 2) + i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \right. \\
 & \quad e^{-id} \binom{v}{k} \left( e^{i\pi v} \Gamma(\alpha, i(c+ib-2ak+av)z) (i(c+ib-2ak+av)z)^{-\alpha} - e^{2id} (-i(c-ib-2ak+av)z)^{-\alpha} \right. \\
 & \quad \Gamma(\alpha, -i(c-ib-2ak+av)z) + (i(c+ib+2ak-av)z)^{-\alpha} \Gamma(\alpha, i(c+ib+2ak-av)z) - \\
 & \quad \left. \left. e^{i(2d+\pi v)} (-i(c-ib+2ak-av)z)^{-\alpha} \Gamma(\alpha, -i(c-ib+2ak-av)z) \right) \right) /; v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1564.01

$$\int z^n e^{bz} \sin(cz + d) \sin^v(az) dz =$$

$$-\frac{1}{2} n! \sin^v(az) (1 - e^{2iaz})^{-v} \left( e^{id+(b+ic)z} \sum_{p=0}^n \frac{((-1)^p z^{n-p})}{(n-p)! (b+ic-ia)^{p+1}} {}_{p+2}F_{p+1} \left( \frac{-ib+c-av}{2a}, \dots, \frac{-ib+c-av}{2a}, -v; \right.$$

$$\left. \frac{-ib+c-av}{2a} + 1, \dots, \frac{-ib+c-av}{2a} + 1; e^{2iaz} \right) - e^{-id+(b-ic)z} \sum_{p=0}^n \frac{((-1)^p z^{n-p})}{(n-p)! (b-ic-ia)^{p+1}}$$

$${}_{p+2}F_{p+1} \left( -\frac{ib+c+av}{2a}, \dots, -\frac{ib+c+av}{2a}, -v; 1 - \frac{ib+c+av}{2a}, \dots, 1 - \frac{ib+c+av}{2a}; e^{2iaz} \right) \Big/; n \in \mathbb{N}$$

**Involving  $z^{\alpha-1} e^{pz} \sin(cz) \sin^v(az + b)$**

01.06.21.1565.01

$$\int z^{\alpha-1} e^{pz} \sin(cz) \sin^v(b+az) dz =$$

$$-2^{-v-1} i z^\alpha \left( \binom{v}{\frac{v}{2}} \left( (i(c+ip)z)^{-\alpha} \Gamma(\alpha, icz-pz) - ((-ic-p)z)^{-\alpha} \Gamma(\alpha, -icz-pz) \right) (1-v \bmod 2) + i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-ib(2k+v)} \right.$$

$$\left. \binom{v}{k} \left( e^{i(4bk+\pi v)} \Gamma(\alpha, i(c-2ak+ip+av)z) (i(c-2ak+ip+av)z)^{-\alpha} - e^{2ibv} (-i(c-2ak-ip+av)z)^{-\alpha} \right. \right.$$

$$\left. \Gamma(\alpha, -i(c-2ak-ip+av)z) + e^{2ibv} (i(c+2ak+ip-av)z)^{-\alpha} \Gamma(\alpha, i(c+2ak+ip-av)z) - \right.$$

$$\left. e^{i(4bk+\pi v)} (-i(c+2ak-ip-av)z)^{-\alpha} \Gamma(\alpha, -i(c+2ak-ip-av)z) \right) \Big/; v \in \mathbb{N}^+$$

01.06.21.1566.01

$$\int z^n e^{pz} \sin(cz) \sin^v(b+az) dz =$$

$$\frac{1}{2} i (1 - e^{2i(b+az)})^{-v} n! \sin^v(b+az) \left( e^{(-ic+p)z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ic+p-ia)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{c+ip+av}{2a}, \dots, -\frac{c+ip+av}{2a}, \right. \right.$$

$$\left. -v; 1 - \frac{c+ip+av}{2a}, \dots, 1 - \frac{c+ip+av}{2a}; e^{2i(b+az)} \right) - e^{(ic+p)z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ic+p-ia)^{-j-1}}{(n-j)!}$$

$${}_{j+2}F_{j+1} \left( -\frac{-c+ip+av}{2a}, \dots, -\frac{-c+ip+av}{2a}, -v; 1 - \frac{-c+ip+av}{2a}, \dots, 1 - \frac{-c+ip+av}{2a}; e^{2i(b+az)} \right) \Big/; n \in \mathbb{N}$$

**Involving  $z^{\alpha-1} e^{pz} \sin(cz + d) \sin^v(az + b)$**

01.06.21.1567.01

$$\int z^{\alpha-1} e^{pz} \sin(d+cz) \sin^v(b+az) dz =$$

$$-2^{-v-1} i z^\alpha \left( e^{-id} \binom{v}{\frac{v}{2}} \left( (i(c+ip)z)^{-\alpha} \Gamma(\alpha, icz-pz) - e^{2id} ((-ic-p)z)^{-\alpha} \Gamma(\alpha, -icz-pz) \right) (1-v \bmod 2) + \right.$$

$$i^{-v} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k e^{-i(d+b(2k+v))} \binom{v}{k} \left( e^{i(4bk+\pi v)} \Gamma(\alpha, i(c-2ak+ip+av)z) (i(c-2ak+ip+av)z)^{-\alpha} - \right.$$

$$e^{2i(d+bv)} (-i(c-2ak-ip+av)z)^{-\alpha} \Gamma(\alpha, -i(c-2ak-ip+av)z) +$$

$$e^{2ibv} (i(c+2ak+ip-av)z)^{-\alpha} \Gamma(\alpha, i(c+2ak+ip-av)z) -$$

$$\left. e^{i(2d+4bk+\pi v)} (-i(c+2ak-ip-av)z)^{-\alpha} \Gamma(\alpha, -i(c+2ak-ip-av)z) \right) /; v \in \mathbb{N}^+$$

01.06.21.1568.01

$$\int z^n e^{pz} \sin(d+cz) \sin^v(b+az) dz =$$

$$\frac{1}{2} i (1 - e^{2i(b+az)})^{-v} n! \sin^v(b+az) \left( e^{-id+(-ic+p)z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-ic+p-ia v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \right.$$

$$\left( -\frac{c+ip+av}{2a}, \dots, -\frac{c+ip+av}{2a}, -v; 1 - \frac{c+ip+av}{2a}, \dots, 1 - \frac{c+ip+av}{2a}; e^{2i(b+az)} \right) -$$

$$e^{id+(ic+p)z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (ic+p-ia v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{-c+ip+av}{2a}, \dots, -\frac{-c+ip+av}{2a}, \right.$$

$$\left. -v; 1 - \frac{-c+ip+av}{2a}, \dots, 1 - \frac{-c+ip+av}{2a}; e^{2i(b+az)} \right) /; n \in \mathbb{N}$$

**Involving  $z^n e^{pz} \sin(bz) \sin^v(cz)$**

01.06.21.1569.01

$$\int z^n e^{p z^2} \sin(b z) \sin^v(c z) dz =$$

$$i 2^{-v-2} p^{-n-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( e^{\frac{b^2}{4p}} \sum_{j=0}^n 2^{j-n} (-i b)^{n-j} (i b + 2 p z)^{j+1} \left( -\frac{(i b + 2 p z)^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(i b + 2 p z)^2}{4 p}\right) - \right.$$

$$e^{\frac{b^2}{4p}} \sum_{j=0}^n 2^{j-n} (i b)^{n-j} (-i b + 2 p z)^{j+1} \left( -\frac{(-i b + 2 p z)^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-i b + 2 p z)^2}{4 p}\right) \Bigg) +$$

$$i^{-v-1} 2^{-v-2} p^{-n-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(-i b + i c(2s-v))^2}{4p}} \sum_{j=0}^n 2^{j-n} (i b - i c(2s-v))^{n-j} (-i b + i c(2s-v) + 2 p z)^{j+1} \right.$$

$$\left( -\frac{(-i b + i c(2s-v) + 2 p z)^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-i b + i c(2s-v) + 2 p z)^2}{4 p}\right) -$$

$$(-1)^v e^{-\frac{(i b + i c(2s-v))^2}{4p}} \sum_{j=0}^n 2^{j-n} (-i b - i c(2s-v))^{n-j} (i b + i c(2s-v) + 2 p z)^{j+1}$$

$$\left( -\frac{(i b + i c(2s-v) + 2 p z)^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(i b + i c(2s-v) + 2 p z)^2}{4 p}\right) + e^{-\frac{(-i b + i c(v-2s))^2}{4p}}$$

$$\sum_{j=0}^n 2^{j-n} (i b - i c(v-2s))^{n-j} (-i b + i c(v-2s) + 2 p z)^{j+1} \left( -\frac{(-i b + i c(v-2s) + 2 p z)^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-i b + i c(v-2s) + 2 p z)^2}{4 p}\right) -$$

$$\left. \frac{(-i b + i c(v-2s) + 2 p z)^2}{4 p} \right) - e^{-\frac{(i b + i c(v-2s))^2}{4p}} \sum_{j=0}^n 2^{j-n} (-i b - i c(v-2s))^{n-j} (i b + i c(v-2s) + 2 p z)^{j+1}$$

$$\left( -\frac{(i b + i c(v-2s) + 2 p z)^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(i b + i c(v-2s) + 2 p z)^2}{4 p}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1570.01

$$\int z^n e^{p \sqrt{z}} \sin(b z) \sin^v(c z) dz =$$

$$i 2^{-2n-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( (-i b)^{-2n-2} e^{-\frac{i p^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p - 2 i b \sqrt{z})^{h+j} \left( -\frac{i(p - 2 i b \sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( p(p - 2 i b \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(p - 2 i b \sqrt{z})^2}{4 b}\right) \right) \right)$$

$$\begin{aligned}
 & 2ib \sqrt{-\frac{i(p-2ib\sqrt{z})^2}{b}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(p-2ib\sqrt{z})^2}{4b}\right) - \\
 & (ib)^{-2n-2} e^{\frac{ip^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2ib\sqrt{z})^{h+j} \left(\frac{i(p+2ib\sqrt{z})^2}{b}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left(p(p+2ib\sqrt{z})\right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(p+2ib\sqrt{z})^2}{4b}\right) + 2\sqrt{\frac{i(p+2ib\sqrt{z})^2}{b}} bi \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(p+2ib\sqrt{z})^2}{4b}\right)\right) + \\
 & 2^{-2n-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{p^2}{4(-ib+ic(2s-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2(-ib+ic(2s-v))\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(p+2(-ib+ic(2s-v))\sqrt{z})^2}{-ib+ic(2s-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( p(p+2(-ib+ic(2s-v))\sqrt{z}) \right. \right. \right. \\
 & \left. \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(p+2(-ib+ic(2s-v))\sqrt{z})^2}{4(-ib+ic(2s-v))}\right) + 2\sqrt{-\frac{(p+2(-ib+ic(2s-v))\sqrt{z})^2}{-ib+ic(2s-v)}} \right. \right. \right. \\
 & \left. \left. \left. (-ib+ic(2s-v)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(p+2(-ib+ic(2s-v))\sqrt{z})^2}{4(-ib+ic(2s-v))}\right) \right) \right) \right) \\
 & (-ib+ic(2s-v))^{-2n-2} + (-1)^v e^{-\frac{p^2}{4(ib+ic(2s-v))}} (ib+ic(2s-v))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2(ib+ic(2s-v))\sqrt{z})^{h+j} \left( -\frac{(p+2(ib+ic(2s-v))\sqrt{z})^2}{ib+ic(2s-v)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( p(p+2(ib+ic(2s-v))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(p+2(ib+ic(2s-v))\sqrt{z})^2}{4(ib+ic(2s-v))}\right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2\sqrt{-\frac{(p+2(ib+ic(2s-v))\sqrt{z})^2}{ib+ic(2s-v)}} (ib+ic(2s-v))\Gamma\left(\frac{1}{2}(h+j+2), -\frac{(p+2(ib+ic(2s-v))\sqrt{z})^2}{4(ib+ic(2s-v))}\right) \\
 & e^{-\frac{p^2}{4(-ib+ic(v-2s))}} (-ib+ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2(-ib+ic(v-2s))\sqrt{z})^{h+j} \\
 & \left(-\frac{(p+2(-ib+ic(v-2s))\sqrt{z})^2}{-ib+ic(v-2s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left(p(p+2(-ib+ic(v-2s))\sqrt{z})\Gamma\left(\frac{1}{2}(h+j+1), -\frac{(p+2(-ib+ic(v-2s))\sqrt{z})^2}{4(-ib+ic(v-2s))}\right) + 2\sqrt{-\frac{(p+2(-ib+ic(v-2s))\sqrt{z})^2}{-ib+ic(v-2s)}}\right) \\
 & (-ib+ic(v-2s))\Gamma\left(\frac{1}{2}(h+j+2), -\frac{(p+2(-ib+ic(v-2s))\sqrt{z})^2}{4(-ib+ic(v-2s))}\right) \Bigg) + \\
 & e^{-\frac{p^2}{4(ib+ic(v-2s))}} (ib+ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2(ib+ic(v-2s))\sqrt{z})^{h+j} \\
 & \left(-\frac{(p+2(ib+ic(v-2s))\sqrt{z})^2}{ib+ic(v-2s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left(p(p+2(ib+ic(v-2s))\sqrt{z})\Gamma\left(\frac{1}{2}(h+j+1), -\frac{(p+2(ib+ic(v-2s))\sqrt{z})^2}{4(ib+ic(v-2s))}\right) + 2\sqrt{-\frac{(p+2(ib+ic(v-2s))\sqrt{z})^2}{ib+ic(v-2s)}}\right) \\
 & (ib+ic(v-2s))\Gamma\left(\frac{1}{2}(h+j+2), -\frac{(p+2(ib+ic(v-2s))\sqrt{z})^2}{4(ib+ic(v-2s))}\right) \Bigg) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{pZ} \sin(bz^r) \sin^v(cz)$

01.06.21.1571.01

$$\int z^n e^{p z} \sin(b z^2) \sin^v(c z) dz = i 2^{-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( (i b)^{-n-1} e^{\frac{i p^2}{4 b}} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p + 2 i b z)^{j+1} \left( \frac{i(p + 2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(p + 2 i b z)^2}{4 b}\right) - \right.$$

$$\left. (-i b)^{-n-1} e^{-\frac{i p^2}{4 b}} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p - 2 i b z)^{j+1} \left( -\frac{i(p - 2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p - 2 i b z)^2}{4 b}\right) \right) -$$

$$2^{-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v-1} e^{-\frac{i(p+c i(2s-v))^2}{4 b}} (-i b)^{-n-1} \sum_{j=0}^n 2^{j-n} (-p - i c(2s-v))^{n-j} (p + c i(2s-v) - 2 i b z)^{j+1} \right.$$

$$\left. \left( -\frac{i(p + c i(2s-v) - 2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p + c i(2s-v) - 2 i b z)^2}{4 b}\right) - \right.$$

$$\left. e^{-\frac{i(p+c i(v-2s))^2}{4 b}} (-i b)^{-n-1} \sum_{j=0}^n 2^{j-n} (-p - i c(v-2s))^{n-j} (p + c i(v-2s) - 2 i b z)^{j+1} \right.$$

$$\left. \left( -\frac{i(p + c i(v-2s) - 2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p + c i(v-2s) - 2 i b z)^2}{4 b}\right) + \right.$$

$$\left. (-1)^v (i b)^{-n-1} e^{\frac{i(p+c i(2s-v))^2}{4 b}} \sum_{j=0}^n 2^{j-n} (-p - i c(2s-v))^{n-j} (p + c i(2s-v) + 2 i b z)^{j+1} \right.$$

$$\left. \left( \frac{i(p + c i(2s-v) + 2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(p + c i(2s-v) + 2 i b z)^2}{4 b}\right) + \right.$$

$$\left. (i b)^{-n-1} e^{\frac{i(p+c i(v-2s))^2}{4 b}} \sum_{j=0}^n 2^{j-n} (-p - i c(v-2s))^{n-j} (p + c i(v-2s) + 2 i b z)^{j+1} \right.$$

$$\left. \left( \frac{i(p + c i(v-2s) + 2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(p + c i(v-2s) + 2 i b z)^2}{4 b}\right) \right) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1572.01

$$\int z^n e^{p z} \sin(b \sqrt{z}) \sin^v(c z) dz = i^{-v-1} 2^{-2n-v-2} e^{\frac{b^2}{4 p} + \frac{i \pi v}{2}} p^{-2n-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i b)^{-h-j+2n} (i b + 2 p \sqrt{z})^{h+j} \left( -\frac{(i b + 2 p \sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right) b i (i b + 2 p \sqrt{z})$$



$$\begin{aligned}
 & \left. \Gamma \left( \frac{1}{2} (h+j+1), -\frac{(ib+2p\sqrt{z})^2}{4p} \right) + 2 \sqrt{-\frac{(ib+2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2} (h+j+2), -\frac{(ib+2p\sqrt{z})^2}{4p} \right) \right) - \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2p\sqrt{z})^{h+j} \left( -\frac{(-ib+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( 2p \sqrt{-\frac{(-ib+2p\sqrt{z})^2}{p}} \Gamma \left( \frac{1}{2} (h+j+2), -\frac{(-ib+2p\sqrt{z})^2}{4p} \right) - \right. \\
 & \left. ib(-ib+2p\sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{(-ib+2p\sqrt{z})^2}{4p} \right) \right) \Bigg) + \\
 & 2^{-2n-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{b^2}{4(p+ci(2s-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2(p+ci(2s-v))\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(-ib+2(p+ci(2s-v))\sqrt{z})^2}{p+ci(2s-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2(p+ci(2s-v)) \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-\frac{(-ib+2(p+ci(2s-v))\sqrt{z})^2}{p+ci(2s-v)}} \Gamma \left( \frac{1}{2} (h+j+2), -\frac{(-ib+2(p+ci(2s-v))\sqrt{z})^2}{4(p+ci(2s-v))} \right) - i \right. \right. \right. \\
 & \left. \left. \left. b(-ib+2(p+ci(2s-v))\sqrt{z}) \Gamma \left( \frac{1}{2} (h+j+1), -\frac{(-ib+2(p+ci(2s-v))\sqrt{z})^2}{4(p+ci(2s-v))} \right) \right) \right) \right) \Bigg) \\
 & (p+ci(2s-v))^{-2n-2} + (-1)^v e^{\frac{b^2}{4(p+ci(2s-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(p+ci(2s-v))\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{(ib+2(p+ci(2s-v))\sqrt{z})^2}{p+ci(2s-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2(p+ci(2s-v))\sqrt{z}) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ib+2(p+ci(2s-v))\sqrt{z})^2}{4(p+ci(2s-v))}\right) + 2\sqrt{-\frac{(ib+2(p+ci(2s-v))\sqrt{z})^2}{p+ci(2s-v)}} \right. \\
 & \left. (p+ci(2s-v)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ib+2(p+ci(2s-v))\sqrt{z})^2}{4(p+ci(2s-v))}\right) \right) \Bigg) (p+ci(2s-v))^{-2n-2} - \\
 & e^{\frac{b^2}{4(p+ci(v-2s))}} (p+ci(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib)^{-h-j+2n} (-ib+2(p+ci(v-2s))\sqrt{z})^{h+j} \\
 & \left( -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{p+ci(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( 2(p+ci(v-2s)) \right. \\
 & \left. \sqrt{-\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{p+ci(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{4(p+ci(v-2s))}\right) - \right. \\
 & \left. ib(-ib+2(p+ci(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{4(p+ci(v-2s))}\right) \right) \Bigg) + \\
 & e^{\frac{b^2}{4(p+ci(v-2s))}} (p+ci(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2(p+ci(v-2s))\sqrt{z})^{h+j} \\
 & \left( -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{p+ci(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( bi(ib+2(p+ci(v-2s))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{4(p+ci(v-2s))}\right) \right. \\
 & \left. + \frac{1}{2}(h+j+1), -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{4(p+ci(v-2s))}\right) + 2\sqrt{-\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{p+ci(v-2s)}} \\
 & \left. (p+ci(v-2s)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ib+2(p+ci(v-2s))\sqrt{z})^2}{4(p+ci(v-2s))}\right) \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

Involving  $z^n e^{pz} \sin(bz) \sin^v(cz^r)$

01.06.21.1573.01

$$\int z^n e^{p z} \sin(b z) \sin^v(c z^2) dz =$$

$$i 2^{-v-1} z^{n+1} \binom{v}{\frac{v}{2}} \left( (-i b - p) z \right)^{-n-1} \Gamma(n+1, (-i b - p) z) - \left( (i b - p) z \right)^{-n-1} \Gamma(n+1, (i b - p) z) (1 - v \bmod 2) -$$

$$2^{-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{i(-i b+p)^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (i b - p)^{n-j} (-i b + p + 2 i c (2 s - v) z)^{j+1} \right. \right.$$

$$\left. \left. \left( \frac{i(-i b + p + 2 i c (2 s - v) z)^2}{c(2 s - v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-i b + p + 2 i c (2 s - v) z)^2}{4 c(2 s - v)}\right) \right) (i c(2 s - v))^{-n-1} + \right.$$

$$\left. (-1)^v e^{\frac{i(i b+p)^2}{4c(2s-v)}} \left( \sum_{j=0}^n 2^{j-n} (-i b - p)^{n-j} (i b + p + 2 i c (2 s - v) z)^{j+1} \left( \frac{i(i b + p + 2 i c (2 s - v) z)^2}{c(2 s - v)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(i b + p + 2 i c (2 s - v) z)^2}{4 c(2 s - v)}\right) \right) (i c(2 s - v))^{-n-1} - \right.$$

$$e^{\frac{i(-i b+p)^2}{4c(v-2s)}} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (i b - p)^{n-j} (-i b + p + 2 i c (v - 2 s) z)^{j+1}$$

$$\left( \frac{i(-i b + p + 2 i c (v - 2 s) z)^2}{c(v - 2 s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(-i b + p + 2 i c (v - 2 s) z)^2}{4 c(v - 2 s)}\right) +$$

$$e^{\frac{i(i b+p)^2}{4c(v-2s)}} (i c(v-2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-i b - p)^{n-j} (i b + p + 2 i c (v - 2 s) z)^{j+1}$$

$$\left( \frac{i(i b + p + 2 i c (v - 2 s) z)^2}{c(v - 2 s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(i b + p + 2 i c (v - 2 s) z)^2}{4 c(v - 2 s)}\right) \Big/; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1574.01

$$\int z^n e^{p z} \sin(b z) \sin^v(c \sqrt{z}) dz =$$

$$-2^{-v-1} i \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( -(-i b + p) \right)^{-n-1} \Gamma(n+1, -(-i b + p) z) - \left( -(i b + p) \right)^{-n-1} \Gamma(n+1, -(i b + p) z) +$$

$$i^{-v-1} 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{\frac{c^2(2s-v)^2}{4(-i b+p)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c(2 s - v))^{-h-j+2n} (2 \sqrt{z} (-i b + p) + c i(2 s - v))^{h+j} \right. \right.$$

$$\left. \left. \left( \frac{(2 \sqrt{z} (-i b + p) + c i(2 s - v))^2}{-i b + p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right) c i(2 s - v) (2 \sqrt{z} (-i b + p) + c i(2 s - v)) \right)$$

$$\begin{aligned}
 & \left( \Gamma \left[ \frac{1}{2} (h+j+1), -\frac{(2\sqrt{z}(-ib+p)+ci(2s-v))^2}{4(-ib+p)} \right] + 2\sqrt{-\frac{(2\sqrt{z}(-ib+p)+ci(2s-v))^2}{-ib+p}} \right. \\
 & \left. (-ib+p) \Gamma \left[ \frac{1}{2} (h+j+2), -\frac{(2\sqrt{z}(-ib+p)+ci(2s-v))^2}{4(-ib+p)} \right] \right) \Bigg) (-ib+p)^{-2n-2} - \\
 & e^{\frac{c^2(v-2s)^2}{4(-ib+p)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (2\sqrt{z}(-ib+p)+ci(v-2s))^{h+j} \right. \\
 & \left. \left( -\frac{(2\sqrt{z}(-ib+p)+ci(v-2s))^2}{-ib+p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(2\sqrt{z}(-ib+p)+ci(v-2s)) \right. \right. \\
 & \left. \left. \Gamma \left[ \frac{1}{2} (h+j+1), -\frac{(2\sqrt{z}(-ib+p)+ci(v-2s))^2}{4(-ib+p)} \right] + 2\sqrt{-\frac{(2\sqrt{z}(-ib+p)+ci(v-2s))^2}{-ib+p}} \right] \right. \\
 & \left. \left. (-ib+p) \Gamma \left[ \frac{1}{2} (h+j+2), -\frac{(2\sqrt{z}(-ib+p)+ci(v-2s))^2}{4(-ib+p)} \right] \right) \right) \Bigg) (-ib+p)^{-2n-2} + \\
 & (-1)^v e^{\frac{c^2(2s-v)^2}{4(ib+p)}} (ib+p)^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2s-v))^{-h-j+2n} (2\sqrt{z}(ib+p)+ci(2s-v))^{h+j} \\
 & \left( -\frac{(2\sqrt{z}(ib+p)+ci(2s-v))^2}{ib+p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( ci(2s-v)(2\sqrt{z}(ib+p)+ci(2s-v)) \Gamma \left[ \frac{1}{2} (h+j+1), -\frac{(2\sqrt{z}(ib+p)+ci(2s-v))^2}{4(ib+p)} \right] + \right. \\
 & \left. 2\sqrt{-\frac{(2\sqrt{z}(ib+p)+ci(2s-v))^2}{ib+p}} (ib+p) \Gamma \left[ \frac{1}{2} (h+j+2), -\frac{(2\sqrt{z}(ib+p)+ci(2s-v))^2}{4(ib+p)} \right] \right) \Bigg) + \\
 & e^{\frac{c^2(v-2s)^2}{4(ib+p)}} (ib+p)^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(v-2s))^{-h-j+2n} (2\sqrt{z}(ib+p)+ci(v-2s))^{h+j}
 \end{aligned}$$

$$\left( -\frac{(2\sqrt{z}(ib+p) + ci(v-2s))^2}{ib+p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( ci(v-2s)(2\sqrt{z}(ib+p) + ci(v-2s)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(2\sqrt{z}(ib+p) + ci(v-2s))^2}{4(ib+p)} \right) + 2\sqrt{-\frac{(2\sqrt{z}(ib+p) + ci(v-2s))^2}{ib+p}} \right) (ib+p) \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(2\sqrt{z}(ib+p) + ci(v-2s))^2}{4(ib+p)} \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

**Involving  $z^n e^{pz} \sin(bz^r) \sin^v(cz^r)$**

01.06.21.1575.01

$$\int z^n e^{p z} \sin(b z^2) \sin^v(c z^2) dz = i 2^{-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\left( (i b)^{-n-1} e^{\frac{i p^2}{4 b}} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2 i b z)^{j+1} \left( \frac{i(p+2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(p+2 i b z)^2}{4 b}\right) - (-i b)^{-n-1} e^{-\frac{i p^2}{4 b}} \right.$$

$$\left. \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p-2 i b z)^{j+1} \left( -\frac{i(p-2 i b z)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p-2 i b z)^2}{4 b}\right) \right) - 2^{-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s$$

$$\binom{v}{s} \left( (-1)^{v+1} e^{-\frac{p^2}{4(-i b+i c(2 s-v))}} \left( \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(-i b+i c(2 s-v)) z)^{j+1} \left( -\frac{(p+2(-i b+i c(2 s-v)) z)^2}{-i b+i c(2 s-v)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(-i b+i c(2 s-v)) z)^2}{4(-i b+i c(2 s-v))}\right) \right) (-i b+i c(2 s-v))^{-n-1} +$$

$$(-1)^v e^{-\frac{p^2}{4(i b+i c(2 s-v))}} (i b+i c(2 s-v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(i b+i c(2 s-v)) z)^{j+1}$$

$$\left( -\frac{(p+2(i b+i c(2 s-v)) z)^2}{i b+i c(2 s-v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(i b+i c(2 s-v)) z)^2}{4(i b+i c(2 s-v))}\right) -$$

$$e^{-\frac{p^2}{4(-i b+i c(v-2 s))}} (-i b+i c(v-2 s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(-i b+i c(v-2 s)) z)^{j+1}$$

$$\left( -\frac{(p+2(-i b+i c(v-2 s)) z)^2}{-i b+i c(v-2 s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(-i b+i c(v-2 s)) z)^2}{4(-i b+i c(v-2 s))}\right) +$$

$$e^{-\frac{p^2}{4(i b+i c(v-2 s))}} (i b+i c(v-2 s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(i b+i c(v-2 s)) z)^{j+1}$$

$$\left( -\frac{(p+2(i b+i c(v-2 s)) z)^2}{i b+i c(v-2 s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(i b+i c(v-2 s)) z)^2}{4(i b+i c(v-2 s))}\right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1576.01

$$\int z^n e^{p z} \sin(b \sqrt{z}) \sin^v(c \sqrt{z}) dz =$$

$$i 2^{-2 n-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( e^{\frac{b^2}{4 p}} p^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b)^{-h-j+2 n} (-i b+2 p \sqrt{z})^{h+j} \left( -\frac{(-i b+2 p \sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \right)$$

$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( 2p \sqrt{-\frac{(-ib+2p\sqrt{z})^2}{p}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+2p\sqrt{z})^2}{4p}\right) - \right. \\
 & \left. ib(-ib+2p\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+2p\sqrt{z})^2}{4p}\right) \right) - \\
 & e^{\frac{b^2}{4p}} p^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib)^{-h-j+2n} (ib+2p\sqrt{z})^{h+j} \left( -\frac{(ib+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( b i (ib+2p\sqrt{z}) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(ib+2p\sqrt{z})^2}{4p}\right) + 2 \sqrt{-\frac{(ib+2p\sqrt{z})^2}{p}} p \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(ib+2p\sqrt{z})^2}{4p}\right) \right) + \\
 & i^{-v-1} 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{(-ib+ic(2s-v))^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(2s-v))^{-h-j+2n} \right. \right. \\
 & \left. \left. (-ib+ic(2s-v)+2p\sqrt{z})^{h+j} \left( -\frac{(-ib+ic(2s-v)+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right. \\
 & \left. \left. \left( (-ib+ic(2s-v))(-ib+ic(2s-v)+2p\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(-ib+ic(2s-v)+2p\sqrt{z})^2}{4p}\right) + \right. \right. \right. \\
 & \left. \left. \left. 2 \sqrt{-\frac{(-ib+ic(2s-v)+2p\sqrt{z})^2}{p}} p \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(-ib+ic(2s-v)+2p\sqrt{z})^2}{4p}\right) \right) \right) \right) \\
 & p^{-2n-2} + (-1)^v e^{-\frac{(ib+ic(2s-v))^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(2s-v))^{-h-j+2n} (ib+ic(2s-v)+2p\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{(ib+ic(2s-v)+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (ib+ic(2s-v))(ib+ic(2s-v)+2p\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+ic(2s-v)+2p\sqrt{z})^2}{4p} \right) + 2 \right. \\
 & \left. \sqrt{-\frac{(ib+ic(2s-v)+2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+ic(2s-v)+2p\sqrt{z})^2}{4p} \right) \right) p^{-2n-2} - \\
 & e^{-\frac{(-ib+ic(v-2s))^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+ic(v-2s))^{-h-j+2n} (-ib+ic(v-2s)+2p\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{(-ib+ic(v-2s)+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (-ib+ic(v-2s))(-ib+ic(v-2s)+2p\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(-ib+ic(v-2s)+2p\sqrt{z})^2}{4p} \right) + \right. \right. \\
 & \left. \left. 2 \sqrt{-\frac{(-ib+ic(v-2s)+2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(-ib+ic(v-2s)+2p\sqrt{z})^2}{4p} \right) \right) \right) \\
 & p^{-2n-2} + e^{-\frac{(ib+ic(v-2s))^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+ic(v-2s))^{-h-j+2n} (ib+ic(v-2s)+2p\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{(ib+ic(v-2s)+2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (ib+ic(v-2s))(ib+ic(v-2s)+2p\sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(ib+ic(v-2s)+2p\sqrt{z})^2}{4p} \right) + 2 \sqrt{-\frac{(ib+ic(v-2s)+2p\sqrt{z})^2}{p}} \right. \right. \\
 & \left. \left. p \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(ib+ic(v-2s)+2p\sqrt{z})^2}{4p} \right) \right) \right) p^{-2n-2} \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$



### Involving $z^n e^{pz} \sin(bz) \sin^v(cz)$

01.06.21.1577.01

$$\int z^n e^{pz} \sin(bz) \sin^v(cz) dz =$$

$$i 2^{-v-2} e^{\frac{b^2}{4p}} p^{-n-1} \left(\frac{v}{2}\right) (1 - v \bmod 2) \left( \sum_{j=0}^n 2^{j-n} (-ib)^{n-j} (ib + 2pz)^{j+1} \left(-\frac{(ib + 2pz)^2}{p}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(ib + 2pz)^2}{4p}\right) - \right.$$

$$\left. \sum_{j=0}^n 2^{j-n} (ib)^{n-j} (-ib + 2pz)^{j+1} \left(-\frac{(-ib + 2pz)^2}{p}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-ib + 2pz)^2}{4p}\right) \right) - 2^{-v-2} i^{-v-1}$$

$$\sum_{h=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^h \binom{v}{h} \left( -e^{\frac{b^2}{4(p+ci(v-2h))}} \left( \sum_{j=0}^n 2^{j-n} (ib)^{n-j} (-ib + 2(p+ci(v-2h))z)^{j+1} \left(-\frac{(-ib + 2(p+ci(v-2h))z)^2}{p+ci(v-2h)}\right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-ib + 2(p+ci(v-2h))z)^2}{4(p+ci(v-2h))}\right) \right) (p+ci(v-2h))^{-n-1} +$$

$$e^{\frac{b^2}{4(p+ci(v-2h))}} \left( \sum_{j=0}^n 2^{j-n} (-ib)^{n-j} (ib + 2(p+ci(v-2h))z)^{j+1} \left(-\frac{(ib + 2(p+ci(v-2h))z)^2}{p+ci(v-2h)}\right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(ib + 2(p+ci(v-2h))z)^2}{4(p+ci(v-2h))}\right) \right) (p+ci(v-2h))^{-n-1} +$$

$$(-1)^{v+1} e^{\frac{b^2}{4(p-ic(v-2h))}} (p-ic(v-2h))^{-n-1} \sum_{j=0}^n 2^{j-n} (ib)^{n-j} (-ib + 2(p-ic(v-2h))z)^{j+1}$$

$$\left(-\frac{(-ib + 2(p-ic(v-2h))z)^2}{p-ic(v-2h)}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-ib + 2(p-ic(v-2h))z)^2}{4(p-ic(v-2h))}\right) +$$

$$(-1)^v e^{\frac{b^2}{4(p-ic(v-2h))}} (p-ic(v-2h))^{-n-1} \sum_{j=0}^n 2^{j-n} (-ib)^{n-j} (ib + 2(p-ic(v-2h))z)^{j+1}$$

$$\left(-\frac{(ib + 2(p-ic(v-2h))z)^2}{p-ic(v-2h)}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(ib + 2(p-ic(v-2h))z)^2}{4(p-ic(v-2h))}\right) \Big/; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1578.01

$$\int z^n e^{p\sqrt{z}} \sin(bz) \sin^v(c\sqrt{z}) dz =$$

$$i 2^{-2n-v-2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( (-ib)^{-2n-2} e^{-\frac{ip^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p-2ib\sqrt{z})^{h+j} \left( -\frac{i(p-2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \right. \\ \left. \binom{j}{h} \binom{n}{j} \left( p(p-2ib\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(p-2ib\sqrt{z})^2}{4b} \right) - \right. \right. \\ \left. \left. 2ib \sqrt{-\frac{i(p-2ib\sqrt{z})^2}{b}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(p-2ib\sqrt{z})^2}{4b} \right) \right) \right) - \\ (ib)^{-2n-2} e^{\frac{ip^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2ib\sqrt{z})^{h+j} \left( \frac{i(p+2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( p(p+2ib\sqrt{z}) \right. \\ \left. \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(p+2ib\sqrt{z})^2}{4b} \right) + 2 \sqrt{\frac{i(p+2ib\sqrt{z})^2}{b}} bi \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(p+2ib\sqrt{z})^2}{4b} \right) \right) \Bigg) + \\ i^{-v-1} 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{i(p+ic(2s-v))^2}{4b}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (p+ic(2s-v))^{-h-j+2n} \right. \right. \\ \left. \left. (p+ic(2s-v)-2ib\sqrt{z})^{h+j} \left( -\frac{i(p+ic(2s-v)-2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right. \\ \left. \left. \left( (p+ic(2s-v))(p+ic(2s-v)-2ib\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(p+ic(2s-v)-2ib\sqrt{z})^2}{4b} \right) - 2 \right. \right. \right. \\ \left. \left. \left. ib \sqrt{-\frac{i(p+ic(2s-v)-2ib\sqrt{z})^2}{b}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(p+ic(2s-v)-2ib\sqrt{z})^2}{4b} \right) \right) \right) \right) \Bigg)$$

$$\begin{aligned}
 & (-i b)^{-2n-2} - e^{-\frac{i(p+ci(v-2s))^2}{4b}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (p+ci(v-2s))^{-h-j+2n} (p+ic(v-2s)-2ib\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(p+ic(v-2s)-2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \\
 & \left. \left( (p+ci(v-2s))(p+ic(v-2s)-2ib\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(p+ic(v-2s)-2ib\sqrt{z})^2}{4b} \right) - 2 \right. \right. \\
 & \left. \left. i b \sqrt{-\frac{i(p+ic(v-2s)-2ib\sqrt{z})^2}{b}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(p+ic(v-2s)-2ib\sqrt{z})^2}{4b} \right) \right) \right) \\
 & (-i b)^{-2n-2} + (-1)^v (i b)^{-2n-2} e^{\frac{i(p+ci(2s-v))^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (p+ci(2s-v))^{-h-j+2n} \\
 & (p+ic(2s-v)+2ib\sqrt{z})^{h+j} \left( \frac{i(p+ic(2s-v)+2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (p+ci(2s-v))(p+ic(2s-v)+2ib\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(p+ic(2s-v)+2ib\sqrt{z})^2}{4b} \right) + \right. \\
 & \left. 2 \sqrt{\frac{i(p+ic(2s-v)+2ib\sqrt{z})^2}{b}} b i \Gamma \left( \frac{1}{2}(h+j+2), \frac{i(p+ic(2s-v)+2ib\sqrt{z})^2}{4b} \right) \right) + \\
 & (i b)^{-2n-2} e^{\frac{i(p+ci(v-2s))^2}{4b}} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (p+ci(v-2s))^{-h-j+2n} (p+ic(v-2s)+2ib\sqrt{z})^{h+j} \\
 & \left( \frac{i(p+ic(v-2s)+2ib\sqrt{z})^2}{b} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (p+ci(v-2s))(p+ic(v-2s)+2ib\sqrt{z}) \Gamma \left( \right. \right. \\
 & \left. \left. \frac{1}{2}(h+j+1), \frac{i(p+ic(v-2s)+2ib\sqrt{z})^2}{4b} \right) + 2 \sqrt{\frac{i(p+ic(v-2s)+2ib\sqrt{z})^2}{b}} b i \Gamma \left( \right. \right.
 \end{aligned}$$

### Involving $z^n e^{pz^r} \sin(bz^r) \sin^v(cz)$

01.06.21.1579.01

$$\int z^n e^{pz^2} \sin(bz^2) \sin^v(cz) dz =$$

$$i 2^{-v-2} z^{n+1} \left(\frac{v}{2}\right) \left( ((-ib-p)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (-ib-p)z^2\right) - ((ib-p)z^2)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (ib-p)z^2\right) \right) (1-v \bmod 2) +$$

$$\frac{2^{-v-2} i^{-v-1}}{\sqrt{-ib+p} \sqrt{ib+p}} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s e^{\frac{c^2 p(v-2s)^2}{2(-ib+p)(ib+p)}} \binom{v}{s}$$

$$\left( (-1)^v e^{-\frac{c^2(v-2s)^2}{4(ib+p)}} \sqrt{ib+p} \sum_{q=0}^n 2^{q-n} (-ib+p)^{-n-\frac{1}{2}} (ic(v-2s))^{n-q} (ci(2s-v) + 2(-ib+p)z)^{q+1} \right.$$

$$\left. \left( -\frac{(ci(2s-v) + 2(-ib+p)z)^2}{-ib+p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ci(2s-v) + 2(-ib+p)z)^2}{4(-ib+p)}\right) + \right.$$

$$e^{-\frac{c^2(v-2s)^2}{4(ib+p)}} \sqrt{ib+p} \sum_{q=0}^n (-ib+p)^{-n-\frac{1}{2}} \left( ic\left(s - \frac{v}{2}\right) \right)^{n-q} (ci(v-2s) + 2(-ib+p)z)^{q+1}$$

$$\left( -\frac{(ci(v-2s) + 2(-ib+p)z)^2}{-ib+p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ci(v-2s) + 2(-ib+p)z)^2}{4(-ib+p)}\right) -$$

$$e^{-\frac{c^2(v-2s)^2}{4(-ib+p)}} \sqrt{-ib+p} \left( (-1)^v \sum_{q=0}^n 2^{q-n} (ib+p)^{-n-\frac{1}{2}} (ic(v-2s))^{n-q} (ci(2s-v) + 2(ib+p)z)^{q+1} \right.$$

$$\left. \left( -\frac{(ci(2s-v) + 2(ib+p)z)^2}{ib+p} \right)^{\frac{1}{2}(-q-1)} \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ci(2s-v) + 2(ib+p)z)^2}{4(ib+p)}\right) + \right.$$

$$\left. \sum_{q=0}^n (ib+p)^{-n-\frac{1}{2}} \left( ic\left(s - \frac{v}{2}\right) \right)^{n-q} (ci(v-2s) + 2(ib+p)z)^{q+1} \left( -\frac{(ci(v-2s) + 2(ib+p)z)^2}{ib+p} \right)^{\frac{1}{2}(-q-1)} \right.$$

$$\left. \binom{n}{q} \Gamma\left(\frac{q+1}{2}, -\frac{(ci(v-2s) + 2(ib+p)z)^2}{4(ib+p)}\right) \right) \Bigg| ; v \in \mathbb{N}^+ \wedge n \in \mathbb{N}$$

01.06.21.1580.01

$$\int z^n e^{p\sqrt{z}} \sin(b\sqrt{z}) \sin^v(cz) dz =$$

$$2^{-v} i z^{n+1} \left(\frac{v}{2}\right) \left( ((-ib-p)\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (-ib-p)\sqrt{z}) - ((ib-p)\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (ib-p)\sqrt{z}) \right)$$

$$\begin{aligned}
 & (1 - v \bmod 2) - i^{1-v} 2^{-2n-v-2} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v-1} e^{-\frac{i(-ib+p)^2}{4c(v-2s)}} (-ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+p)^{-h-j+2n} \right. \\
 & \quad (-ib+p-2ic(v-2s)\sqrt{z})^{h+j} \left( -\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (-ib+p) \\
 & \quad (-ib+p-2ic(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) - 2ic(v-2s) \\
 & \quad \left. \sqrt{-\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(-ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) \right) + \\
 & \quad (-1)^v e^{-\frac{i(ib+p)^2}{4c(v-2s)}} (-ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+p)^{-h-j+2n} (ib+p-2ic(v-2s)\sqrt{z})^{h+j} \\
 & \quad \left( -\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad (ib+p)(ib+p-2ic(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) - 2ic(v-2s) \\
 & \quad \left. \sqrt{-\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{i(ib+p-2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) \right) - \\
 & \quad e^{\frac{i(-ib+p)^2}{4c(v-2s)}} (ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib+p)^{-h-j+2n} (-ib+p+2ic(v-2s)\sqrt{z})^{h+j} \\
 & \quad \left( \frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{c(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \quad (-ib+p)(-ib+p+2ic(v-2s)\sqrt{z}) \Gamma \left( \frac{1}{2}(h+j+1), \frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)} \right) + 2ci
 \end{aligned}$$

$$\begin{aligned}
 & (v-2s) \sqrt{\frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(-ib+p+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) + \\
 & e^{\frac{i(ib+p)^2}{4c(v-2s)}} (ic(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ib+p)^{-h-j+2n} (ib+p+2ic(v-2s)\sqrt{z})^{h+j} \\
 & \left(\frac{i(ib+p+2ic(v-2s)\sqrt{z})^2}{c(v-2s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (ib+p)(ib+p+2ic(v-2s)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. \frac{i(ib+p+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) + 2ci(v-2s) \sqrt{\frac{i(ib+p+2ic(v-2s)\sqrt{z})^2}{c(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. \frac{i(ib+p+2ic(v-2s)\sqrt{z})^2}{4c(v-2s)}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^{\alpha-1} e^{pz^r} \sin(bz^r) \sin^v(cz^r)$**

01.06.21.1581.01

$$\begin{aligned}
 & \int z^{\alpha-1} e^{pz^r} \sin(bz^r) \sin^v(cz^r) dz = \\
 & \frac{1}{r} \left( 2^{-v-1} z^\alpha i \binom{v}{\frac{v}{2}} \left( ((-ib-p)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-ib-p)z^r\right) - ((ib-p)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-p)z^r\right) \right) (1-v \bmod 2) \right) + \\
 & \frac{2^{-v-1} z^\alpha i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} \Gamma\left(\frac{\alpha}{r}, (-ib-p-2ics+icv)z^r\right) ((-ib-p-2ics+icv)z^r)^{-\frac{\alpha}{r}} + \right. \\
 & \left. (-1)^v ((ib-p-2ics+icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-p-2ics+icv)z^r\right) - ((-ib-p+2ics-icv)z^r)^{-\frac{\alpha}{r}} \right. \\
 & \left. \Gamma\left(\frac{\alpha}{r}, (-ib-p+2ics-icv)z^r\right) + ((ib-p+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ib-p+2ics-icv)z^r\right) \right) ; v \in \mathbb{N}^+
 \end{aligned}$$

**Involving  $z^{\alpha-1} e^{bz^r+e} \sin(az^r+q) \sin^v(cz^r+g)$**

01.06.21.1582.01

$$\int z^{\alpha-1} e^{bz^r+e} \sin(az^r+q) \sin^v(cz^r+g) dz =$$

$$\frac{i 2^{-v-1} z^\alpha}{r} \left(\frac{v}{\frac{v}{2}}\right) \left( e^{e+iq} ((-b-ia)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ia)z^r\right) - e^{-iq} ((ia-b)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (ia-b)z^r\right) \right) (1-v \bmod 2) +$$

$$\frac{2^{-v-1} z^\alpha i^{-v-1}}{r} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{e+iq+2igs-igv} \Gamma\left(\frac{\alpha}{r}, (-b-ia-2ics+icv)z^r\right) ((-b-ia-2ics+icv)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. (-1)^v e^{-iq+2igs-igv} ((-b+ia-2ics+icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+ia-2ics+icv)z^r\right) - \right.$$

$$\left. e^{e+iq-2igs+igv} ((-b-ia+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b-ia+2ics-icv)z^r\right) + \right.$$

$$\left. e^{-iq-2igs+igv} ((-b+ia+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+ia+2ics-icv)z^r\right) \right); v \in \mathbb{N}^+$$

**Involving  $z^n e^{bz^r+dz+e} \sin(az^r+pz+q) \sin^v(cz^r+fz+g)$**

01.06.21.1583.01

$$\int z^n e^{bz^2+dz+e} \sin(az^2+pz+q) \sin^v(cz^2+fz+g) dz =$$

$$i 2^{-v-2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \left( (b+ia)^{-n-1} e^{-\frac{(d+ip)^2}{4(b+ia)}+e+iq} \sum_{j=0}^n 2^{j-n} (-d-ip)^{n-j} (d+ip+2(b+ia)z)^{j+1} \right.$$

$$\left. \left( -\frac{(d+ip+2(b+ia)z)^2}{b+ia} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d+ip+2(b+ia)z)^2}{4(b+ia)}\right) - \right.$$

$$\left. (b-ia)^{-n-1} e^{-\frac{(d-ip)^2}{4(b-ia)}+e-iq} \sum_{j=0}^n 2^{j-n} (ip-d)^{n-j} (d-ip+2(b-ia)z)^{j+1} \left( -\frac{(d-ip+2(b-ia)z)^2}{b-ia} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-ip+2(b-ia)z)^2}{4(b-ia)}\right) \right) -$$

$$2^{-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^{v+1} e^{-\frac{(d-ip+fi(2s-v))^2}{4(b-ia+ci(2s-v))}+e-iq+gi(2s-v)} \left( \sum_{j=0}^n 2^{j-n} (-d+ip-fi(2s-v))^{n-j} (d-ip+fi(2s-v) + \right. \right.$$

$$\left. \left. 2(b-ia+ci(2s-v))z \right)^{j+1} \left( -\frac{(d-ip+fi(2s-v)+2(b-ia+ci(2s-v))z)^2}{b-ia+ci(2s-v)} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-ip+fi(2s-v)+2(b-ia+ci(2s-v))z)^2}{4(b-ia+ci(2s-v))} \right) \right)$$

$$(b-ia+ci(2s-v))^{-n-1} + (-1)^v e^{-\frac{(d+ip+fi(2s-v))^2}{4(b+ia+ci(2s-v))}+e+iq+gi(2s-v)} (b+ia+ci(2s-v))^{-n-1}$$

$$\begin{aligned}
 & \sum_{j=0}^n 2^{j-n} (-d - ip - if(2s - v))^{n-j} (d + ip + fi(2s - v) + 2(b + ia + ci(2s - v))z)^{j+1} \\
 & \left( -\frac{(d + ip + fi(2s - v) + 2(b + ia + ci(2s - v))z)^2}{b + ia + ci(2s - v)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(d + ip + fi(2s - v) + 2(b + ia + ci(2s - v))z)^2}{4(b + ia + ci(2s - v))}\right) - \\
 & e^{-\frac{(d-ip+fi(v-2s))^2}{4(b-ia+ci(v-2s))} + e-iq+gi(v-2s)} (b - ia + ci(v - 2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-d + ip - if(v - 2s))^{n-j} \\
 & (d - ip + fi(v - 2s) + 2(b - ia + ci(v - 2s))z)^{j+1} \\
 & \left( -\frac{(d - ip + fi(v - 2s) + 2(b - ia + ci(v - 2s))z)^2}{b - ia + ci(v - 2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(d - ip + fi(v - 2s) + 2(b - ia + ci(v - 2s))z)^2}{4(b - ia + ci(v - 2s))}\right) + \\
 & e^{-\frac{(d+ip+fi(v-2s))^2}{4(b+ia+ci(v-2s))} + e+iq+gi(v-2s)} (b + ia + ci(v - 2s))^{-n-1} \sum_{j=0}^n 2^{j-n} (-d - ip - if(v - 2s))^{n-j} \\
 & (d + ip + fi(v - 2s) + 2(b + ia + ci(v - 2s))z)^{j+1} \\
 & \left( -\frac{(d + ip + fi(v - 2s) + 2(b + ia + ci(v - 2s))z)^2}{b + ia + ci(v - 2s)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \\
 & \Gamma\left(\frac{j+1}{2}, -\frac{(d + ip + fi(v - 2s) + 2(b + ia + ci(v - 2s))z)^2}{4(b + ia + ci(v - 2s))}\right) \Bigg] ; n \in \mathbb{N} \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1584.01

$$\begin{aligned}
 & \int z^n e^{\sqrt{z} b + dz + e} \sin(\sqrt{z} a + pz + q) \sin^v(\sqrt{z} c + fz + g) dz = \\
 & i 2^{-2n-v-2} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \left( e^{-\frac{(b-ia)^2}{4(d-ip)} + e-iq} (d - ip)^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b - ia)^{-h-j+2n} (b - ia + 2(d - ip)\sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{(b - ia + 2(d - ip)\sqrt{z})^2}{d - ip} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (b - ia)(b - ia + 2(d - ip)\sqrt{z}) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{(b - ia + 2(d - ip)\sqrt{z})^2}{4(d - ip)}\right) + 2\sqrt{-\frac{(b - ia + 2(d - ip)\sqrt{z})^2}{d - ip}} \right)
 \end{aligned}$$



$$\begin{aligned}
 & (d - i p) \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{(b - i a + 2(d - i p) \sqrt{z})^2}{4(d - i p)} \right) \left. - e^{-\frac{(b + i a)^2}{4(d + i p)} + e + i q} (d + i p)^{-2n - 2} \right. \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b + i a)^{-h-j+2n} (b + i a + 2(d + i p) \sqrt{z})^{h+j} \left( -\frac{(b + i a + 2(d + i p) \sqrt{z})^2}{d + i p} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b + i a)(b + i a + 2(d + i p) \sqrt{z}) \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{(b + i a + 2(d + i p) \sqrt{z})^2}{4(d + i p)} \right) + \right. \\
 & \left. 2 \sqrt{-\frac{(b + i a + 2(d + i p) \sqrt{z})^2}{d + i p}} (d + i p) \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{(b + i a + 2(d + i p) \sqrt{z})^2}{4(d + i p)} \right) \right) \Bigg) + \\
 & 2^{-2n-v-2} i^{-v-1} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(b + i a + c i(2s-v))^2}{4(d + i p + f i(2s-v))} + e + i q + g i(2s-v)} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b + i a + c i(2s-v))^{-h-j+2n} \right. \right. \\
 & \left. \left. (b + i a + c i(2s-v) + 2(d + i p + f i(2s-v)) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(b + i a + c i(2s-v) + 2(d + i p + f i(2s-v)) \sqrt{z})^2}{d + i p + f i(2s-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right. \right. \\
 & \left. \left. \left( (b + i a + c i(2s-v))(b + i a + c i(2s-v) + 2(d + i p + f i(2s-v)) \sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h + j + 1), -(b + i a + c i(2s-v) + 2(d + i p + f i(2s-v)) \sqrt{z})^2 \right) / \right. \right. \\
 & \left. \left. (4(d + i p + f i(2s-v))) + 2(d + i p + f i(2s-v)) \Gamma \left( \frac{1}{2} (h + j + 2), \right. \right. \right. \\
 & \left. \left. \left. -(b + i a + c i(2s-v) + 2(d + i p + f i(2s-v)) \sqrt{z})^2 / (4(d + i p + f i(2s-v))) \right) \right) \right) \Bigg) \\
 & \left. \sqrt{\left( -(b + i a + c i(2s-v) + 2(d + i p + f i(2s-v)) \sqrt{z})^2 / (d + i p + f i(2s-v)) \right)} \right) \Bigg) \\
 & (d + i p + f i(2s-v))^{-2n-2} + (-1)^{v+1} e^{-\frac{(b - i a + c i(2s-v))^2}{4(d - i p + f i(2s-v))} + e - i q + g i(2s-v)} (d - i p + f i(2s-v))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b - i a + c i(2s-v))^{-h-j+2n} (b - i a + c i(2s-v) + 2(d - i p + f i(2s-v)) \sqrt{z})^{h+j}
 \end{aligned}$$

$$\begin{aligned}
 & \left( -(b - ia + ci(2s - v) + 2(d - ip + fi(2s - v))\sqrt{z})^2 / (d - ip + fi(2s - v)) \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( (b - ia + ci(2s - v))(b - ia + ci(2s - v) + 2(d - ip + fi(2s - v))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \quad \left. \left. \frac{1}{2}(h + j + 1), -(b - ia + ci(2s - v) + 2(d - ip + fi(2s - v))\sqrt{z})^2 / \right. \right. \\
 & \quad \left. \left. (4(d - ip + fi(2s - v))) \right) + 2(d - ip + fi(2s - v)) \Gamma \left( \frac{1}{2}(h + j + 2), \right. \right. \\
 & \quad \left. \left. -(b - ia + ci(2s - v) + 2(d - ip + fi(2s - v))\sqrt{z})^2 / (4(d - ip + fi(2s - v))) \right) \right) \\
 & \left. \sqrt{-(b - ia + ci(2s - v) + 2(d - ip + fi(2s - v))\sqrt{z})^2 / (d - ip + fi(2s - v))} \right) + \\
 & e^{-\frac{(b+ia+ci(v-2s))^2}{4(d+ip+fi(v-2s))} + e+iq+gi(v-2s)} (d + ip + fi(v - 2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b + ia + ci(v - 2s))^{-h-j+2n} \\
 & (b + ia + ci(v - 2s) + 2(d + ip + fi(v - 2s))\sqrt{z})^{h+j} \\
 & \left( -\frac{(b + ia + ci(v - 2s) + 2(d + ip + fi(v - 2s))\sqrt{z})^2}{d + ip + fi(v - 2s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \\
 & \left( (b + ia + ci(v - 2s))(b + ia + ci(v - 2s) + 2(d + ip + fi(v - 2s))\sqrt{z}) \Gamma \left( \right. \right. \\
 & \quad \left. \left. \frac{1}{2}(h + j + 1), -\frac{(b + ia + ci(v - 2s) + 2(d + ip + fi(v - 2s))\sqrt{z})^2}{4(d + ip + fi(v - 2s))} \right) + \right. \\
 & \quad \left. 2(d + ip + fi(v - 2s)) \Gamma \left( \frac{1}{2}(h + j + 2), -\frac{(b + ia + ci(v - 2s) + 2(d + ip + fi(v - 2s))\sqrt{z})^2}{4(d + ip + fi(v - 2s))} \right) \right) \\
 & \left. \sqrt{-(b + ia + ci(v - 2s) + 2(d + ip + fi(v - 2s))\sqrt{z})^2 / (d + ip + fi(v - 2s))} \right) - \\
 & e^{-\frac{(b-ia+ci(v-2s))^2}{4(d-ip+fi(v-2s))} + e-iq+gi(v-2s)} (d - ip + fi(v - 2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b - ia + ci(v - 2s))^{-h-j+2n} \\
 & (b - ia + ci(v - 2s) + 2(d - ip + fi(v - 2s))\sqrt{z})^{h+j} \\
 & \left( -(b - ia + ci(v - 2s) + 2(d - ip + fi(v - 2s))\sqrt{z})^2 / (d - ip + fi(v - 2s)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \\
 & \binom{n}{j} \left( (b - ia + ci(v - 2s))(b - ia + ci(v - 2s) + 2(d - ip + fi(v - 2s))\sqrt{z}) \Gamma \left( \frac{1}{2}(h + j + 1), \right. \right. \\
 & \quad \left. \left. -(b - ia + ci(v - 2s) + 2(d - ip + fi(v - 2s))\sqrt{z})^2 / (4(d - ip + fi(v - 2s))) \right) + \right.
 \end{aligned}$$

$$\left. \begin{aligned} &2(d - ip + fi(v - 2s)) \Gamma\left(\frac{1}{2}(h + j + 2), -(b - ia + ci(v - 2s) + 2(d - ip + fi(v - 2s))\sqrt{z})^2\right) / \\ &(4(d - ip + fi(v - 2s))) \sqrt{-(b - ia + ci(v - 2s) + 2(d - ip + fi(v - 2s))\sqrt{z})^2} / \\ &(d - ip + fi(v - 2s)) \end{aligned} \right) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

Involving product of powers of two direct functions, exponential and a power functions

**Involving  $z^{\alpha-1} e^{bz} \sin^\mu(cz) \sin^\nu(az)$**

01.06.21.1585.01

$$\begin{aligned} \int z^{\alpha-1} e^{bz} \sin^m(cz) \sin^\nu(az) dz = &(-1)^{m-1} 2^{-m-\nu} z^\alpha (-bz)^{-\alpha} \binom{m}{\frac{m}{2}} \binom{\nu}{\frac{\nu}{2}} \Gamma(\alpha, -bz) (1 - m \bmod 2) (1 - \nu \bmod 2) - \\ &2^{-m-\nu} i^{-m-\nu} z^\alpha \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^{k+m} e^{\frac{i\pi\nu}{2}} \binom{m}{k} \\ &(e^{im\pi} \Gamma(\alpha, (-b + 2ick - icm)z) ((-b + 2ick - icm)z)^{-\alpha} + (ic(m - 2k) - b)z)^{-\alpha} \Gamma(\alpha, (ic(m - 2k) - b)z) - \\ &(-1)^m i^{-\nu} 2^{-m-\nu} z^\alpha \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^s \binom{\nu}{s} (e^{i\pi\nu} \Gamma(\alpha, (-b - 2ias + iav)z) ((-b - 2ias + iav)z)^{-\alpha} + \\ &((-b - ia(v - 2s))z)^{-\alpha} \Gamma(\alpha, (-b - ia(v - 2s))z) + 2^{-m-\nu} i^{-m-\nu} z^\alpha \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\ &\sum_{s=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^{m+s} \binom{\nu}{s} (-e^{i\pi\nu} \Gamma(\alpha, (-b - 2ick + icm - 2ias + iav)z) ((-b - 2ick + icm - 2ias + iav)z)^{-\alpha} - \\ &e^{i\pi m + i\pi\nu} ((-b + 2ick - icm - 2ias + iav)z)^{-\alpha} \Gamma(\alpha, (-b + 2ick - icm - 2ias + iav)z) - \\ &((-b - 2ick + icm + 2ias - iav)z)^{-\alpha} \Gamma(\alpha, (-b - 2ick + icm + 2ias - iav)z) - \\ &e^{im\pi} ((-b + 2ick - icm + 2ias - iav)z)^{-\alpha} \Gamma(\alpha, (-b + 2ick - icm + 2ias - iav)z) /; m \in \mathbb{N}^+ \wedge \nu \in \mathbb{N}^+ \end{aligned}$$

01.06.21.1586.01

$$\int z^n e^{bz} \sin^\mu(cz) \sin^v(az) dz = 2^{-v} e^{bz} \left(\frac{v}{2}\right) n! (1 - v \bmod 2) \sin^\mu(cz)$$

$$\left( \sum_{p=0}^n \frac{(-1)^p z^{n-p} (b - ic\mu)^{-p-1}}{(n-p)!} {}_{p+2}F_{p+1} \left( -\frac{ib+c\mu}{2c}, \dots, -\frac{ib+c\mu}{2c}, -\mu; 1 - \frac{ib+c\mu}{2c}, \dots, 1 - \frac{ib+c\mu}{2c}; e^{2icz} \right) \right)$$

$$(1 - e^{2icz})^{-\mu} + 2^{-v} n! \sin^\mu(cz)$$

$$\left( \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( i^v e^{(b-ia(v-2k))z} \sum_{p=0}^n \frac{(-1)^p z^{n-p} (b - ia(v-2k) - ic\mu)^{-p-1}}{(n-p)!} {}_{p+2}F_{p+1} \left( -\frac{ib-2ak+av+c\mu}{2c}, \dots, \right. \right. \right.$$

$$\left. \left. -\frac{ib-2ak+av+c\mu}{2c}, -\mu; 1 - \frac{ib-2ak+av+c\mu}{2c}, \dots, 1 - \frac{ib-2ak+av+c\mu}{2c}; e^{2icz} \right) + \right.$$

$$\left. i^{-v} e^{(b+ai(v-2k))z} \sum_{p=0}^n \frac{(-1)^p z^{n-p} (b + ai(v-2k) - ic\mu)^{-p-1}}{(n-p)!} {}_{p+2}F_{p+1} \left( -\frac{ib+2ak-av+c\mu}{2c}, \right. \right.$$

$$\left. \dots, -\frac{ib+2ak-av+c\mu}{2c}, -\mu; 1 - \frac{ib+2ak-av+c\mu}{2c}, \dots, \right.$$

$$\left. \left. 1 - \frac{ib+2ak-av+c\mu}{2c}; e^{2icz} \right) \right) (1 - e^{2icz})^{-\mu} /; v \in \mathbb{N} \wedge n \in \mathbb{N}$$

Involving  $z^{\alpha-1} e^{pz} \sin^m(cz) \sin^v(az + b)$

01.06.21.1587.01

$$\begin{aligned}
 \int z^{\alpha-1} e^{pz} \sin^m(cz) \sin^v(b+az) dz = & -2^{-m-v} z^\alpha \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma(\alpha, -pz) (1-m \bmod 2) (1-v \bmod 2) (-pz)^{-\alpha} - \\
 & 2^{-m-v} z^\alpha \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k ((-ic(m-2k)-p)z)^{-\alpha} ((ic(m-2k)-p)z)^{-\alpha} \binom{m}{k} \\
 & \left( e^{\frac{im\pi}{2}} \Gamma(\alpha, (ic(m-2k)-p)z) ((-ic(m-2k)-p)z)^\alpha + e^{-\frac{1}{2}im\pi} ((ic(m-2k)-p)z)^\alpha \Gamma(\alpha, (-ic(m-2k)-p)z) \right) - \\
 & 2^{-m-v} z^\alpha \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s ((-p-ia(v-2s))z)^{-\alpha} ((ia(v-2s)-p)z)^{-\alpha} \binom{v}{s} \left( e^{-i(2bs-bv+\frac{\pi v}{2})} \Gamma(\alpha, \right. \\
 & \left. (-p-ia(v-2s))z) ((ia(v-2s)-p)z)^\alpha + e^{i(2bs-bv+\frac{\pi v}{2})} ((-p-ia(v-2s))z)^\alpha \Gamma(\alpha, (ia(v-2s)-p)z) \right) - \\
 & 2^{-m-v} z^\alpha \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s (i(2ck-cm+ip-2as+av)z)^{-\alpha} ((-p-i(2ck-cm+2as-av))z)^{-\alpha} \\
 & ((-p-i(2ck-cm-2as+av))z)^{-\alpha} ((-p-i(c(m-2k)+a(v-2s)))z)^{-\alpha} \binom{v}{s} \\
 & \left( \left( e^{-i(2bs-bv+\frac{\pi v}{2})} \left( e^{-\frac{1}{2}im\pi} \Gamma(\alpha, (-p-i(c(m-2k)+a(v-2s)))z) ((-p-i(2ck-cm-2as+av))z)^\alpha + \right. \right. \right. \\
 & \left. \left. e^{\frac{im\pi}{2}} ((-p-i(c(m-2k)+a(v-2s)))z)^\alpha \Gamma(\alpha, (-p-i(2ck-cm-2as+av))z) \right) \right. \\
 & \left. (i(2ck-cm+ip-2as+av)z)^\alpha + e^{-\frac{1}{2}i(\pi m-4bs+2bv-\pi v)} ((-p-i(2ck-cm-2as+av))z)^\alpha \right. \\
 & \left. ((-p-i(c(m-2k)+a(v-2s)))z)^\alpha \Gamma(\alpha, (-p-i(-2ck+cm+2as-av))z) \right) \\
 & ((-p-i(2ck-cm+2as-av))z)^\alpha + e^{\frac{1}{2}i(\pi m+4bs-2bv+\pi v)} (i(2ck-cm+ip-2as+av)z)^\alpha \\
 & ((-p-i(2ck-cm-2as+av))z)^\alpha ((-p-i(c(m-2k)+a(v-2s)))z)^\alpha \\
 & \left. \Gamma(\alpha, (-p-i(2ck-cm+2as-av))z) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1588.01

$$\int z^n e^{p z} \sin^\mu(c z) \sin^v(a z + b) dz = 2^{-v} e^{p z} \binom{v}{\frac{v}{2}} n! (1 - v \bmod 2) \sin^\mu(c z) (1 - e^{2 i c z})^{-\mu}$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (p - i c \mu)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{i p + c \mu}{2 c}, \dots, -\frac{i p + c \mu}{2 c}, -\mu; 1 - \frac{i p + c \mu}{2 c}, \dots, 1 - \frac{i p + c \mu}{2 c}; e^{2 i c z} \right) +$$

$$2^{-v} n! \sin^\mu(c z) (1 - e^{2 i c z})^{-\mu} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{\frac{i \pi v}{2} - i b (v-2k) + (p - i a (v-2k)) z} \right.$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j} (p - i a (v-2k) - i c \mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{i p + a (-2k+v) + c \mu}{2 c}, \dots, -\frac{i p + a (-2k+v) + c \mu}{2 c}, \right.$$

$$\left. -\mu; 1 - \frac{i p + a (-2k+v) + c \mu}{2 c}, \dots, 1 - \frac{i p + a (-2k+v) + c \mu}{2 c}; e^{2 i c z} \right) + e^{-\frac{1}{2} i \pi v + b i (v-2k) + (p + a i (v-2k)) z}$$

$$\sum_{j=0}^n \frac{(-1)^j z^{n-j} (p + a i (v-2k) - i c \mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{i p - a (-2k+v) + c \mu}{2 c}, \dots, -\frac{i p - a (-2k+v) + c \mu}{2 c}, \right.$$

$$\left. -\mu; 1 - \frac{i p - a (-2k+v) + c \mu}{2 c}, \dots, 1 - \frac{i p - a (-2k+v) + c \mu}{2 c}; e^{2 i c z} \right) \Bigg) /; n \in \mathbb{N} \wedge v \in \mathbb{N}^+$$

01.06.21.1589.01

$$\int z^n e^{p z} \sin^m(c z) \sin^v(b + a z) dz = 2^{-m} e^{p z} \binom{m}{\frac{m}{2}} n! (1 - m \bmod 2) \sin^v(b + a z)$$

$$\left( \sum_{j=0}^n \frac{(-1)^j z^{n-j} (p - i a v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{i p + a v}{2 a}, \dots, -\frac{i p + a v}{2 a}, -v; 1 - \frac{i p + a v}{2 a}, \dots, 1 - \frac{i p + a v}{2 a}; e^{2 i (b+a z)} \right) \right)$$

$$(1 - e^{2 i (b+a z)})^{-v} + 2^{-m} n! \sin^v(b + a z)$$

$$\left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{c i (m-2k) + p} z^{-\frac{i m \pi}{2}} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (c i (m-2k) + p - i a v)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{-c (m-2k) + i p + a v}{2 a}, \dots, \right. \right.$$

$$\left. -\frac{-c (m-2k) + i p + a v}{2 a}, -v; 1 - \frac{-c (m-2k) + i p + a v}{2 a}, \dots, 1 - \frac{-c (m-2k) + i p + a v}{2 a}; \right.$$

$$\left. e^{2 i (b+a z)} \right) + e^{\frac{i \pi m}{2} + (p - i c (m-2k)) z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (-i c (m-2k) + p - i a v)^{-j-1}}{(n-j)!}$$

$${}_{j+2}F_{j+1} \left( -\frac{c (m-2k) + i p + a v}{2 a}, \dots, -\frac{c (m-2k) + i p + a v}{2 a}, -v; 1 - \frac{c (m-2k) + i p + a v}{2 a}, \right.$$

$$\left. \dots, 1 - \frac{c (m-2k) + i p + a v}{2 a}; e^{2 i (b+a z)} \right) \Bigg) \Bigg) (1 - e^{2 i (b+a z)})^{-v} /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+$$

Involving  $z^{\alpha-1} e^{p z} \sin^m(c z + d) \sin^v(a z + b)$

01.06.21.1590.01

$$\begin{aligned}
 & \int z^{\alpha-1} e^{pz} \sin^m(d+cz) \sin^v(b+az) dz = \\
 & -2^{-m-v} z^\alpha \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) \Gamma(\alpha, -pz) (1-m \bmod 2) (1-v \bmod 2) (-pz)^{-\alpha} - 2^{-m-v} z^\alpha \left(\frac{v}{2}\right) (1-v \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} (-p-ic(m-2k)z)^{-\alpha} (-ci(m-2k)+p)z^{-\alpha} \left( e^{-i(2dk-dm+\frac{m\pi}{2})} \Gamma(\alpha, -(ci(m-2k)+p)z) \right. \\
 & \quad \left. - (p-ic(m-2k)z)^\alpha + e^{i(2dk-dm+\frac{m\pi}{2})} (-ci(m-2k)+p)z^\alpha \Gamma(\alpha, -(p-ic(m-2k)z)) \right) - \\
 & 2^{-m-v} z^\alpha \left(\frac{m}{2}\right) (1-m \bmod 2) \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} (-p-ia(v-2s)z)^{-\alpha} (-p+ai(v-2s)z)^{-\alpha} \\
 & \left( e^{i(2bs-bv+\frac{\pi v}{2})} \Gamma(\alpha, -(p-ia(v-2s)z)) (-p+ai(v-2s)z)^\alpha + \right. \\
 & \quad \left. e^{-i(2bs-bv+\frac{\pi v}{2})} (-p-ia(v-2s)z)^\alpha \Gamma(\alpha, -(p+ai(v-2s)z)) \right) - \\
 & 2^{-m-v} z^\alpha \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} (i(2ck-cm+ip-2as+av)z)^{-\alpha} (-p+i(2ck-cm+2as-av)z)^{-\alpha} \\
 & \left( -(p+i(2ck-cm-2as+av)z)^{-\alpha} (-p+i(c(m-2k)+a(v-2s))z)^{-\alpha} \right. \\
 & \quad \left( \left( e^{-i(2bs-bv+\frac{\pi v}{2})} \left( e^{-i(2dk-dm+\frac{m\pi}{2})} \Gamma(\alpha, -(p+i(c(m-2k)+a(v-2s))z)) (-p+i(2ck-cm-2as+av)z)^\alpha + \right. \right. \right. \\
 & \quad \left. \left. \left. e^{i(2dk-dm+\frac{m\pi}{2})} (-p+i(c(m-2k)+a(v-2s))z)^\alpha \Gamma(\alpha, -(p+i(2ck-cm-2as+av)z)) \right) \right) \right. \\
 & \quad \left. (i(2ck-cm+ip-2as+av)z)^\alpha + e^{-i\frac{1}{2}(4dk-2dm-4bs+2bv-\pi v+m\pi)} \right. \\
 & \quad \left. (-p+i(2ck-cm-2as+av)z)^\alpha (-p+i(c(m-2k)+a(v-2s))z)^\alpha \right. \\
 & \quad \left. \Gamma(\alpha, -(p+i(-2ck+cm+2as-av)z)) \right) (-p+i(2ck-cm+2as-av)z)^\alpha + \\
 & \left. e^{\frac{1}{2}i(4dk-2dm+4bs-2bv+\pi v+m\pi)} (i(2ck-cm+ip-2as+av)z)^\alpha (-p+i(2ck-cm-2as+av)z)^\alpha \right. \\
 & \quad \left. (-p+i(c(m-2k)+a(v-2s))z)^\alpha \Gamma(\alpha, -(p+i(2ck-cm+2as-av)z)) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

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$$\int z^n e^{p z} \sin^\mu(c z + d) \sin^\nu(a z + b) dz = 2^{-\nu} e^{p z} \binom{\nu}{\frac{\nu}{2}} n! (1 - \nu \bmod 2) \sin^\mu(d + c z) (1 - e^{2i(d+cz)})^{-\mu}$$

$$+ \sum_{j=0}^n \frac{(-1)^j z^{n-j}}{(n-j)! (p - ic\mu)^{j+1}} {}_{j+2}F_{j+1} \left( -\frac{ip+c\mu}{2c}, \dots, -\frac{ip+c\mu}{2c}, -\mu; 1 - \frac{ip+c\mu}{2c}, \dots, 1 - \frac{ip+c\mu}{2c}; e^{2i(d+cz)} \right) +$$

$$2^{-\nu} n! \sin^\mu(d + cz) (1 - e^{2i(d+cz)})^{-\mu} \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k}$$

$$\left( e^{\frac{i\pi\nu}{2} - ib(v-2k) + (p-ia(v-2k))z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (p - ia(v-2k) - ic\mu)^{-j-1}}{(n-j)!} {}_{j+2}F_{j+1} \left( -\frac{ip+a(-2k+v)+c\mu}{2c}, \dots, \right. \right.$$

$$\left. -\frac{ip+a(-2k+v)+c\mu}{2c}, -\mu; 1 - \frac{ip+a(-2k+v)+c\mu}{2c}, \dots, 1 - \frac{ip+a(-2k+v)+c\mu}{2c}; e^{2i(d+cz)} \right) +$$

$$e^{-\frac{1}{2}i\pi\nu + bi(v-2k) + (p+ai(v-2k))z} \sum_{j=0}^n \frac{(-1)^j z^{n-j} (p + ai(v-2k) - ic\mu)^{-j-1}}{(n-j)!}$$

$${}_{j+2}F_{j+1} \left( -\frac{ip-a(-2k+v)+c\mu}{2c}, \dots, -\frac{ip-a(-2k+v)+c\mu}{2c}, -\mu; 1 - \frac{ip-a(-2k+v)+c\mu}{2c}, \dots, \right.$$

$$\left. \dots, 1 - \frac{ip-a(-2k+v)+c\mu}{2c}; e^{2i(d+cz)} \right) \Bigg/ ; n \in \mathbb{N} \wedge \nu \in \mathbb{N}^+$$

### Involving $z^n e^{p z} \sin^m(b z) \sin^\nu(c z)$

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$$\int z^n e^{p z} \sin^m(b z) \sin^\nu(c z) dz =$$

$$-(-1)^m 2^{-m-\nu-1} \binom{\nu}{\frac{\nu}{2}} (1 - \nu \bmod 2) \left( \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{b^2(2k-m)^2}{4p} + \frac{im\pi}{2}} \sum_{j=0}^n 2^{j-n} (ib(2k-m))^{n-j} (2pz - ib(2k-m))^{j+1} \right. \right.$$

$$\left. \left( -\frac{(2pz - ib(2k-m))^2}{p} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{(2pz - ib(2k-m))^2}{4p} \right) + \right.$$

$$e^{\frac{b^2(m-2k)^2}{4p} - \frac{im\pi}{2}} \sum_{j=0}^n 2^{j-n} (ib(m-2k))^{n-j} (2pz - ib(m-2k))^{j+1} \left( -\frac{(2pz - ib(m-2k))^2}{p} \right)^{\frac{1}{2}(-j-1)}$$

$$\left. \left. \binom{n}{j} \Gamma \left( \frac{j+1}{2}, -\frac{(2pz - ib(m-2k))^2}{4p} \right) \right) \right) p^{-n-1} - (-1)^m i^{-\nu} 2^{-m-\nu-1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2)$$

$$\left( \sum_{k=0}^{\lfloor \frac{\nu-1}{2} \rfloor} (-1)^k \binom{\nu}{k} \left( (-1)^{\nu} e^{\frac{c^2(2k-\nu)^2}{4p}} \sum_{j=0}^n 2^{j-n} (-ic(2k-\nu))^{n-j} (ci(2k-\nu) + 2pz)^{j+1} \left( -\frac{(ci(2k-\nu) + 2pz)^2}{p} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$



$$\begin{aligned}
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{c i (2 k - v) + 2 p z)^2}{4 p}\right) + e^{\frac{c^2 (v-2 k)^2}{4 p}} \sum_{j=0}^n 2^{j-n} (-i c (v-2 k))^{n-j} (c i (v-2 k) + 2 p z)^{j+1} \\
 & \left(-\frac{(c i (v-2 k) + 2 p z)^2}{p}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(c i (v-2 k) + 2 p z)^2}{4 p}\right) \Bigg) p^{-n-1} - \\
 & (-1)^m i^{-v} 2^{-m-v-1} \left(\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s}\right) \left((-1)^v e^{\frac{i m \pi}{2} - \frac{(i c (2 s - v) - i b (2 k - m))^2}{4 p}} \sum_{j=0}^n 2^{j-n} (i b (2 k - m) - i c (2 s - v))^{n-j}\right. \\
 & \left.(-i b (2 k - m) + c i (2 s - v) + 2 p z)^{j+1} \left(-\frac{(-i b (2 k - m) + c i (2 s - v) + 2 p z)^2}{p}\right)^{\frac{1}{2}(-j-1)}\right. \\
 & \left.\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-i b (2 k - m) + c i (2 s - v) + 2 p z)^2}{4 p}\right) + \right. \\
 & \left.(-1)^v e^{-\frac{(i c (2 s - v) - i b (m - 2 k))^2}{4 p} - \frac{i m \pi}{2}} \sum_{j=0}^n 2^{j-n} (i b (m - 2 k) - i c (2 s - v))^{n-j}\right. \\
 & \left.(-i b (m - 2 k) + c i (2 s - v) + 2 p z)^{j+1} \left(-\frac{(-i b (m - 2 k) + c i (2 s - v) + 2 p z)^2}{p}\right)^{\frac{1}{2}(-j-1)}\right. \\
 & \left.\binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(-i b (m - 2 k) + c i (2 s - v) + 2 p z)^2}{4 p}\right) + \right. \\
 & \left. e^{\frac{i m \pi}{2} - \frac{(i c (v-2 s) - i b (2 k - m))^2}{4 p}} \sum_{j=0}^n 2^{j-n} (i b (2 k - m) - i c (v - 2 s))^{n-j} (-i b (2 k - m) + c i (v - 2 s) + 2 p z)^{j+1}\right. \\
 & \left. \left(-\frac{(-i b (2 k - m) + c i (v - 2 s) + 2 p z)^2}{p}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j}\right. \\
 & \left. \Gamma\left(\frac{j+1}{2}, -\frac{(-i b (2 k - m) + c i (v - 2 s) + 2 p z)^2}{4 p}\right) + \right. \\
 & \left. e^{-\frac{(i c (v-2 s) - i b (m - 2 k))^2}{4 p} - \frac{i m \pi}{2}} \sum_{j=0}^n 2^{j-n} (i b (m - 2 k) - i c (v - 2 s))^{n-j} (-i b (m - 2 k) + c i (v - 2 s) + 2 p z)^{j+1}\right. \\
 & \left. \left(-\frac{(-i b (m - 2 k) + c i (v - 2 s) + 2 p z)^2}{p}\right)^{\frac{1}{2}(-j-1)} \binom{n}{j}\right. \\
 & \left. \Gamma\left(\frac{j+1}{2}, -\frac{(-i b (m - 2 k) + c i (v - 2 s) + 2 p z)^2}{4 p}\right) \Bigg) \Bigg) \right) \\
 & p^{-n-1} + (-1)^{m-1} 2^{-m-v-1} z^{n+1} (-p z^2)^{\frac{1}{2}(-n-1)} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma\left(\frac{n+1}{2}, -p z^2\right) (1 - m \bmod 2) \\
 & (1 -
 \end{aligned}$$

$m \bmod 2) k, n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$

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$$\int z^n e^{p\sqrt{z}} \sin^m(bz) \sin^v(cz) dz =$$

$$(-1)^{m-1} 2^{-m-v+1} (-p\sqrt{z})^{-2(n+1)} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma(2(n+1), -p\sqrt{z}) (1-m \bmod 2) (1-v \bmod 2) +$$

$$i^{-m} 2^{-m-2n-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k}$$

$$\left( e^{-\frac{ip^2}{4b(2k-m)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p-2ib(2k-m)\sqrt{z})^{h+j} \left( -\frac{i(p-2ib(2k-m)\sqrt{z})^2}{b(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \right. \right.$$

$$\left. \binom{n}{j} \left( p(p-2ib(2k-m)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(p-2ib(2k-m)\sqrt{z})^2}{4b(2k-m)}\right) - 2ib(2k-m) \right. \right.$$

$$\left. \left. \sqrt{-\frac{i(p-2ib(2k-m)\sqrt{z})^2}{b(2k-m)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(p-2ib(2k-m)\sqrt{z})^2}{4b(2k-m)}\right) \right) \right)$$

$$(-ib(2k-m))^{-2n-2} + (-1)^m e^{-\frac{ip^2}{4b(m-2k)}} (-ib(m-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n}$$

$$(p-2ib(m-2k)\sqrt{z})^{h+j} \left( -\frac{i(p-2ib(m-2k)\sqrt{z})^2}{b(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j}$$

$$\left( p(p-2ib(m-2k)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(p-2ib(m-2k)\sqrt{z})^2}{4b(m-2k)}\right) - \right.$$

$$\left. \left. 2ib(m-2k) \sqrt{-\frac{i(p-2ib(m-2k)\sqrt{z})^2}{b(m-2k)}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(p-2ib(m-2k)\sqrt{z})^2}{4b(m-2k)}\right) \right) \right) +$$

$$(-1)^m i^{-v} 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{\frac{ip^2}{4c(2k-v)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} \right. \right.$$

$$\begin{aligned}
 & (p + 2ci(2k - v)\sqrt{z})^{h+j} \left( \frac{i(p + 2ci(2k - v)\sqrt{z})^2}{c(2k - v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( p(p + 2ci(2k - v)\sqrt{z}) \right. \\
 & \left. \Gamma\left(\frac{1}{2}(h + j + 1), \frac{i(p + 2ci(2k - v)\sqrt{z})^2}{4c(2k - v)}\right) + 2ci(2k - v) \sqrt{\frac{i(p + 2ci(2k - v)\sqrt{z})^2}{c(2k - v)}} \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h + j + 2), \frac{i(p + 2ci(2k - v)\sqrt{z})^2}{4c(2k - v)}\right) \right) \right) \left( ic(2k - v) \right)^{-2n-2} + e^{\frac{ip^2}{4c(v-2k)}} (ic(v - 2k))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p + 2ci(v - 2k)\sqrt{z})^{h+j} \left( \frac{i(p + 2ci(v - 2k)\sqrt{z})^2}{c(v - 2k)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( p(p + 2ci(v - 2k)\sqrt{z}) \Gamma\left(\frac{1}{2}(h + j + 1), \frac{i(p + 2ci(v - 2k)\sqrt{z})^2}{4c(v - 2k)}\right) + \right. \\
 & \left. 2ci(v - 2k) \sqrt{\frac{i(p + 2ci(v - 2k)\sqrt{z})^2}{c(v - 2k)}} \Gamma\left(\frac{1}{2}(h + j + 2), \frac{i(p + 2ci(v - 2k)\sqrt{z})^2}{4c(v - 2k)}\right) \right) \right) + \\
 & i^{-m-v} 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{p^2}{4(ic(2s-v)-ib(2k-m))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} \right. \right. \\
 & \left. \left. (p + 2(ic(2s - v) - ib(2k - m))\sqrt{z}) \right)^{h+j} \left( -\frac{(p + 2(ic(2s - v) - ib(2k - m))\sqrt{z})^2}{ic(2s - v) - ib(2k - m)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( p(p + 2(ic(2s - v) - ib(2k - m))\sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{(p + 2(ic(2s - v) - ib(2k - m))\sqrt{z})^2}{4(ic(2s - v) - ib(2k - m))}\right) + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \sqrt{-\frac{(p+2(ic(2s-v)-ib(2k-m))\sqrt{z})^2}{ic(2s-v)-ib(2k-m)}} (ic(2s-v)-ib(2k-m)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \\
 & \left. -\frac{(p+2(ic(2s-v)-ib(2k-m))\sqrt{z})^2}{4(ic(2s-v)-ib(2k-m))}\right) \Bigg) (ic(2s-v)-ib(2k-m))^{-2n-2} + \\
 & (-1)^{m+v} e^{-\frac{p^2}{4(ic(2s-v)-ib(m-2k))}} (ic(2s-v)-ib(m-2k))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} \\
 & (p+2(ic(2s-v)-ib(m-2k))\sqrt{z})^{h+j} \left( -\frac{(p+2(ic(2s-v)-ib(m-2k))\sqrt{z})^2}{ic(2s-v)-ib(m-2k)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( p(p+2(ic(2s-v)-ib(m-2k))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(p+2(ic(2s-v)-ib(m-2k))\sqrt{z})^2}{4(ic(2s-v)-ib(m-2k))}\right) + 2 \sqrt{-\frac{(p+2(ic(2s-v)-ib(m-2k))\sqrt{z})^2}{ic(2s-v)-ib(m-2k)}} \right. \\
 & \left. (ic(2s-v)-ib(m-2k)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(p+2(ic(2s-v)-ib(m-2k))\sqrt{z})^2}{4(ic(2s-v)-ib(m-2k))}\right) \right) \Bigg) + \\
 & e^{-\frac{p^2}{4(ic(v-2s)-ib(2k-m))}} (ic(v-2s)-ib(2k-m))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} \\
 & (p+2(ic(v-2s)-ib(2k-m))\sqrt{z})^{h+j} \left( -\frac{(p+2(ic(v-2s)-ib(2k-m))\sqrt{z})^2}{ic(v-2s)-ib(2k-m)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( p(p+2(ic(v-2s)-ib(2k-m))\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \left. \left. -\frac{(p+2(ic(v-2s)-ib(2k-m))\sqrt{z})^2}{4(ic(v-2s)-ib(2k-m))}\right) + 2 \sqrt{-\frac{(p+2(ic(v-2s)-ib(2k-m))\sqrt{z})^2}{ic(v-2s)-ib(2k-m)}} \right. \\
 & \left. (ic(v-2s)-ib(2k-m)) \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(p+2(ic(v-2s)-ib(2k-m))\sqrt{z})^2}{4(ic(v-2s)-ib(2k-m))}\right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. (i c (v - 2 s) - i b (2 k - m)) \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{(p + 2 (i c (v - 2 s) - i b (2 k - m)) \sqrt{z})^2}{4 (i c (v - 2 s) - i b (2 k - m))} \right) \right) + \\
 & (-1)^m e^{-\frac{p^2}{4 (i c (v - 2 s) - i b (m - 2 k))}} (i c (v - 2 s) - i b (m - 2 k))^{-2 n - 2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2 n} \\
 & (p + 2 (i c (v - 2 s) - i b (m - 2 k)) \sqrt{z})^{h+j} \left( -\frac{(p + 2 (i c (v - 2 s) - i b (m - 2 k)) \sqrt{z})^2}{i c (v - 2 s) - i b (m - 2 k)} \right)^{\frac{1}{2} (-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( p (p + 2 (i c (v - 2 s) - i b (m - 2 k)) \sqrt{z}) \right. \\
 & \left. \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{(p + 2 (i c (v - 2 s) - i b (m - 2 k)) \sqrt{z})^2}{4 (i c (v - 2 s) - i b (m - 2 k))} \right) + \right. \\
 & \left. 2 \sqrt{-\frac{(p + 2 (i c (v - 2 s) - i b (m - 2 k)) \sqrt{z})^2}{i c (v - 2 s) - i b (m - 2 k)}} (i c (v - 2 s) - i b (m - 2 k)) \right. \\
 & \left. \left. \Gamma \left( \frac{1}{2} (h + j + 2), -\frac{(p + 2 (i c (v - 2 s) - i b (m - 2 k)) \sqrt{z})^2}{4 (i c (v - 2 s) - i b (m - 2 k))} \right) \right) \right) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^n e^{p z} \sin^m(b z^r) \sin^v(c z)$

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$$\begin{aligned}
 \int z^n e^{p z} \sin^m(b z^2) \sin^v(c z) dz &= (-1)^{m-1} 2^{-m-v} (-p)^{-n-1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma(n+1, -p z) (1 - m \bmod 2) (1 - v \bmod 2) - \\
 & (-1)^m i^{-v} 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} ((-1)^v \Gamma(n+1, (-2 c i k - p + i c v) z) ((-2 c i k - p + i c v) z)^{-n-1} + \\
 & ((-p - i c (v - 2 k)) z)^{-n-1} \Gamma(n+1, (-p - i c (v - 2 k)) z) - i^{-m} 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{i p^2}{4 b (2 k - m)}} \left( \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p - 2 i b (2 k - m) z)^{j+1} \left( -\frac{i (p - 2 i b (2 k - m) z)^2}{b (2 k - m)} \right)^{\frac{1}{2} (-j-1)} \binom{n}{j} \Gamma \left( \frac{j+1}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. - \frac{i(p-2ib(2k-m)z)^2}{4b(2k-m)} \right) (-ib(2k-m))^{-n-1} + (-1)^m e^{-\frac{ip^2}{4b(m-2k)}} (-ib(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} \\
 & (p-2ib(m-2k)z)^{j+1} \left( -\frac{i(p-2ib(m-2k)z)^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p-2ib(m-2k)z)^2}{4b(m-2k)}\right) \Bigg) - \\
 & (-1)^m 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( e^{-\frac{i(p+ci(2s-v))^2}{4b(2k-m)} + \frac{i\pi v}{2} + \frac{im\pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (-p-ic(2s-v))^{n-j} \right. \right. \\
 & \left. \left. (p+ci(2s-v)-2ib(2k-m)z)^{j+1} \left( -\frac{i(p+ci(2s-v)-2ib(2k-m)z)^2}{b(2k-m)} \right)^{\frac{1}{2}(-j-1)} \right. \right. \\
 & \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p+ci(2s-v)-2ib(2k-m)z)^2}{4b(2k-m)}\right) \right) \right) (-ib(2k-m))^{-n-1} + \\
 & e^{-\frac{i(p+ci(v-2s))^2}{4b(2k-m)} - \frac{i\pi v}{2} + \frac{im\pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (-p-ic(v-2s))^{n-j} (p+ci(v-2s)-2ib(2k-m)z)^{j+1} \right. \\
 & \left. \left( -\frac{i(p+ci(v-2s)-2ib(2k-m)z)^2}{b(2k-m)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \right. \\
 & \left. \Gamma\left(\frac{j+1}{2}, -\frac{i(p+ci(v-2s)-2ib(2k-m)z)^2}{4b(2k-m)}\right) \right) \Bigg) (-ib(2k-m))^{-n-1} + \\
 & e^{-\frac{i(p+ci(2s-v))^2}{4b(m-2k)} + \frac{i\pi v}{2} + \frac{im\pi}{2}} (-ib(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p-ic(2s-v))^{n-j} \\
 & (p+ci(2s-v)-2ib(m-2k)z)^{j+1} \left( -\frac{i(p+ci(2s-v)-2ib(m-2k)z)^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p+ci(2s-v)-2ib(m-2k)z)^2}{4b(m-2k)}\right) \Bigg) + \\
 & e^{-\frac{i(p+ci(v-2s))^2}{4b(m-2k)} - \frac{i\pi v}{2} + \frac{im\pi}{2}} (-ib(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p-ic(v-2s))^{n-j} \\
 & (p+ci(v-2s)-2ib(m-2k)z)^{j+1} \left( -\frac{i(p+ci(v-2s)-2ib(m-2k)z)^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p+ci(v-2s)-2ib(m-2k)z)^2}{4b(m-2k)}\right) \Bigg) /; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

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$$\int z^n e^{p z} \sin^m(b \sqrt{z}) \sin^v(c z) dz =$$

$$(-1)^{m-1} 2^{-m-v} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma(n+1, -p z) (1-m \bmod 2) (1-v \bmod 2) (-p)^{-n-1} - (-1)^m i^{-v} 2^{-m-v} z^{n+1} \binom{m}{\frac{m}{2}} (1-m \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} (-1)^v \Gamma(n+1, (-2c i k - p + i c v) z) ((-2c i k - p + i c v) z)^{-n-1} + ((-p - i c (v - 2k)) z)^{-n-1}$$

$$\Gamma(n+1, (-p - i c (v - 2k)) z) + 2^{-m-2n-v-1} i^{-m-v} p^{-2n-2} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{b^2(2k-m)^2}{4p} + \frac{i\pi v}{2}} \right.$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b (2k-m))^{-h-j+2n} (2p \sqrt{z} - i b (2k-m))^{h+j} \left( -\frac{(2p \sqrt{z} - i b (2k-m))^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h}$$

$$\binom{n}{j} \left( 2p \sqrt{-\frac{(2p \sqrt{z} - i b (2k-m))^2}{p}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(2p \sqrt{z} - i b (2k-m))^2}{4p}\right) - i b (2k-m) \right.$$

$$\left. (2p \sqrt{z} - i b (2k-m)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2p \sqrt{z} - i b (2k-m))^2}{4p}\right) \right) + (-1)^m e^{\frac{b^2(m-2k)^2}{4p} + \frac{i\pi v}{2}}$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b (m-2k))^{-h-j+2n} (2p \sqrt{z} - i b (m-2k))^{h+j} \left( -\frac{(2p \sqrt{z} - i b (m-2k))^2}{p} \right)^{\frac{1}{2}(-h-j-1)}$$

$$\binom{j}{h} \binom{n}{j} \left( 2p \sqrt{-\frac{(2p \sqrt{z} - i b (m-2k))^2}{p}} \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(2p \sqrt{z} - i b (m-2k))^2}{4p}\right) - \right.$$

$$\left. i b (m-2k) (2p \sqrt{z} - i b (m-2k)) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2p \sqrt{z} - i b (m-2k))^2}{4p}\right) \right) \right) +$$

$$2^{-m-2n-v-1} i^{-m-v} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{\frac{b^2(2k-m)^2}{4(p+ic(2s-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b (2k-m))^{-h-j+2n} \right. \right.$$

$$\begin{aligned}
 & (2(p + ci(2s - v))\sqrt{z} - ib(2k - m))^{h+j} \left( -\frac{(2(p + ci(2s - v))\sqrt{z} - ib(2k - m))^2}{p + ci(2s - v)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(p + ci(2s - v)) \sqrt{-\frac{(2(p + ci(2s - v))\sqrt{z} - ib(2k - m))^2}{p + ci(2s - v)}} \Gamma\left(\frac{1}{2}(h + j + 2), \right. \right. \\
 & \left. \left. -\frac{(2(p + ci(2s - v))\sqrt{z} - ib(2k - m))^2}{4(p + ci(2s - v))} \right) - ib(2k - m)(2(p + ci(2s - v))\sqrt{z} - \right. \\
 & \left. \left. ib(2k - m)) \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{(2(p + ci(2s - v))\sqrt{z} - ib(2k - m))^2}{4(p + ci(2s - v))} \right) \right) \right) \\
 & (p + ci(2s - v))^{-2n-2} + (-1)^{m+v} e^{\frac{b^2(m-2k)^2}{4(p+ci(2s-v))}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib(m-2k))^{-h-j+2n} \right. \\
 & \left. (2(p + ci(2s - v))\sqrt{z} - ib(m - 2k))^{h+j} \left( -\frac{(2(p + ci(2s - v))\sqrt{z} - ib(m - 2k))^2}{p + ci(2s - v)} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \left. \binom{j}{h} \binom{n}{j} \left( 2(p + ci(2s - v)) \sqrt{-\frac{(2(p + ci(2s - v))\sqrt{z} - ib(m - 2k))^2}{p + ci(2s - v)}} \Gamma\left(\frac{1}{2}(h + j + 2), \right. \right. \right. \\
 & \left. \left. -\frac{(2(p + ci(2s - v))\sqrt{z} - ib(m - 2k))^2}{4(p + ci(2s - v))} \right) - ib(m - 2k)(2(p + ci(2s - v))\sqrt{z} - \right. \\
 & \left. \left. ib(m - 2k)) \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{(2(p + ci(2s - v))\sqrt{z} - ib(m - 2k))^2}{4(p + ci(2s - v))} \right) \right) \right) \right) \\
 & (p + ci(2s - v))^{-2n-2} + e^{\frac{b^2(2k-m)^2}{4(p+ci(v-2s))}} (p + ci(v - 2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib(2k - m))^{-h-j+2n} \\
 & (2(p + ci(v - 2s))\sqrt{z} - ib(2k - m))^{h+j} \left( -\frac{(2(p + ci(v - 2s))\sqrt{z} - ib(2k - m))^2}{p + ci(v - 2s)} \right)^{\frac{1}{2}(-h-j-1)}
 \end{aligned}$$



$$\begin{aligned}
 & \binom{j}{h} \binom{n}{j} \left( 2(p+ci(v-2s)) \sqrt{-\frac{(2(p+ci(v-2s))\sqrt{z}-ib(2k-m))^2}{p+ci(v-2s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \quad \left. \left. -\frac{(2(p+ci(v-2s))\sqrt{z}-ib(2k-m))^2}{4(p+ci(v-2s))}\right) - ib(2k-m)(2(p+ci(v-2s))\sqrt{z}- \right. \\
 & \quad \left. \left. ib(2k-m)\right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(2(p+ci(v-2s))\sqrt{z}-ib(2k-m))^2}{4(p+ci(v-2s))}\right) \right) + \\
 & (-1)^m e^{\frac{b^2(m-2k)^2}{4(p+ci(v-2s))}} (p+ci(v-2s))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-ib(m-2k))^{-h-j+2n} \\
 & \quad (2(p+ci(v-2s))\sqrt{z}-ib(m-2k))^{h+j} \left( -\frac{(2(p+ci(v-2s))\sqrt{z}-ib(m-2k))^2}{p+ci(v-2s)} \right)^{\frac{1}{2}(-h-j-1)} \\
 & \binom{j}{h} \binom{n}{j} \left( 2(p+ci(v-2s)) \sqrt{-\frac{(2(p+ci(v-2s))\sqrt{z}-ib(m-2k))^2}{p+ci(v-2s)}} \right. \\
 & \quad \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(2(p+ci(v-2s))\sqrt{z}-ib(m-2k))^2}{4(p+ci(v-2s))}\right) - \right. \\
 & \quad \left. ib(m-2k)(2(p+ci(v-2s))\sqrt{z}-ib(m-2k)) \Gamma\left(\frac{1}{2}(h+j+1), \right. \right. \\
 & \quad \left. \left. -\frac{(2(p+ci(v-2s))\sqrt{z}-ib(m-2k))^2}{4(p+ci(v-2s))}\right) \right) \Bigg) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

### Involving $z^n e^{pz^r} \sin^m(bz^r) \sin^v(cz)$

01.06.21.1596.01

$$\begin{aligned}
 \int z^n e^{pz^2} \sin^m(bz^2) \sin^v(cz) dz = & (-1)^{m-1} 2^{-m-v-1} z^{n+1} (-pz^2)^{\frac{1}{2}(-n-1)} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma\left(\frac{n+1}{2}, -pz^2\right) (1-m \bmod 2) (1-v \bmod 2) - \\
 & i^m 2^{-m-v-1} z^{n+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m \Gamma\left(\frac{n+1}{2}, (2ibk-ibm-p)z^2\right) ((2ibk-ibm-p)z^2)^{\frac{1}{2}(-n-1)} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (i b (m - 2 k) - p) z^2 \right)^{\frac{1}{2}(-n-1)} \Gamma\left(\frac{n+1}{2}, (i b (m - 2 k) - p) z^2\right) - (-1)^m i^{-v} 2^{-m-v-1} p^{-n-1} \left(\frac{m}{2}\right) (1 - m \bmod 2) \\
 & \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{\frac{c^2(v-2k)^2}{4p}} \sum_{h=0}^n 2^{h-n} (i c (v-2k))^{n-h} (2 p z - i c (v-2k))^{h+1} \left( -\frac{(2 p z - i c (v-2k))^2}{p} \right)^{\frac{1}{2}(-h-1)} \right. \\
 & \quad \left. \binom{n}{h} \Gamma\left(\frac{h+1}{2}, -\frac{(2 p z - i c (v-2k))^2}{4 p}\right) + e^{\frac{c^2(v-2k)^2}{4p}} \sum_{h=0}^n 2^{h-n} (-i c (v-2k))^{n-h} \right. \\
 & \quad \left. (c i (v-2k) + 2 p z)^{h+1} \left( -\frac{(c i (v-2k) + 2 p z)^2}{p} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \Gamma\left(\frac{h+1}{2}, -\frac{(c i (v-2k) + 2 p z)^2}{4 p}\right) \right) - \\
 & (-1)^m i^{-v} 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{j=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^j \binom{v}{j} \left( e^{\frac{c^2(v-2j)^2}{4(p-i b(m-2k))} + i \pi v - \frac{i m \pi}{2}} \sum_{h=0}^n 2^{h-n} (i c (v-2j))^{n-h} \right. \\
 & \quad \left. (2(p-i b(m-2k))z - i c(v-2j))^{h+1} \left( -\frac{(2(p-i b(m-2k))z - i c(v-2j))^2}{p-i b(m-2k)} \right)^{\frac{1}{2}(-h-1)} \right. \\
 & \quad \left. \binom{n}{h} \Gamma\left(\frac{h+1}{2}, -\frac{(2(p-i b(m-2k))z - i c(v-2j))^2}{4(p-i b(m-2k))}\right) \right) (p-i b(m-2k))^{-n-1} + \\
 & \quad e^{\frac{c^2(v-2j)^2}{4(p-i b(m-2k))} - \frac{i m \pi}{2}} \sum_{h=0}^n 2^{h-n} (-i c(v-2j))^{n-h} (c i (v-2j) + 2(p-i b(m-2k))z)^{h+1} \\
 & \quad \left( -\frac{(c i (v-2j) + 2(p-i b(m-2k))z)^2}{p-i b(m-2k)} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \\
 & \quad \left. \Gamma\left(\frac{h+1}{2}, -\frac{(c i (v-2j) + 2(p-i b(m-2k))z)^2}{4(p-i b(m-2k))}\right) \right) (p-i b(m-2k))^{-n-1} + \\
 & \quad e^{\frac{c^2(v-2j)^2}{4(b i(m-2k)+p)} + i \pi v + \frac{i m \pi}{2}} (b i(m-2k) + p)^{-n-1} \sum_{h=0}^n 2^{h-n} (i c(v-2j))^{n-h} (2(b i(m-2k) + p)z - i c(v-2j))^{h+1} \\
 & \quad \left( -\frac{(2(b i(m-2k) + p)z - i c(v-2j))^2}{b i(m-2k) + p} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \\
 & \quad \left. \Gamma\left(\frac{h+1}{2}, -\frac{(2(b i(m-2k) + p)z - i c(v-2j))^2}{4(b i(m-2k) + p)}\right) \right) +
 \end{aligned}$$

$$e^{\frac{c^2(v-2j)^2}{4(bi(m-2k)+p)} + \frac{im\pi}{2}} (bi(m-2k)+p)^{-n-1} \sum_{h=0}^n 2^{h-n} (-ic(v-2j))^{n-h} (ci(v-2j)+2(bi(m-2k)+p)z)^{h+1} \left( -\frac{(ci(v-2j)+2(bi(m-2k)+p)z)^2}{bi(m-2k)+p} \right)^{\frac{1}{2}(-h-1)} \binom{n}{h} \Gamma\left(\frac{h+1}{2}, -\frac{(ci(v-2j)+2(bi(m-2k)+p)z)^2}{4(bi(m-2k)+p)}\right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+ \wedge n \in \mathbb{N}$$

01.06.21.1597.01

$$\int z^n e^{p\sqrt{z}} \sin^m(b\sqrt{z}) \sin^v(cz) dz =$$

$$(-1)^{m-1} 2^{-m-v+1} (-p\sqrt{z})^{-2(n+1)} z^{n+1} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma(2(n+1), -p\sqrt{z}) (1-m \bmod 2) (1-v \bmod 2) -$$

$$i^{-m} 2^{-m-v+1} z^{n+1} \binom{v}{\frac{v}{2}} (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( \Gamma(2(n+1), (2ibk - ibm - p)\sqrt{z}) ((2ibk - ibm - p)\sqrt{z})^{-2(n+1)} + (-1)^m ((ib(m-2k) - p)\sqrt{z})^{-2(n+1)} \Gamma(2(n+1), (ib(m-2k) - p)\sqrt{z}) \right) +$$

$$(-1)^m i^{-v} 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{-\frac{ip^2}{4c(v-2k)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} \right. \right.$$

$$\left. (p-2ic(v-2k)\sqrt{z})^{h+j} \left( -\frac{i(p-2ic(v-2k)\sqrt{z})^2}{c(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( p(p-2ic(v-2k)\sqrt{z}) \right. \right.$$

$$\left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(p-2ic(v-2k)\sqrt{z})^2}{4c(v-2k)}\right) - 2ic(v-2k) \sqrt{-\frac{i(p-2ic(v-2k)\sqrt{z})^2}{c(v-2k)}} \right.$$

$$\left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{i(p-2ic(v-2k)\sqrt{z})^2}{4c(v-2k)}\right) \right) \right) \left( (-ic(v-2k))^{-2n-2} + e^{\frac{ip^2}{4c(v-2k)}} (ic(v-2k))^{-2n-2} \right.$$

$$\left. \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j p^{-h-j+2n} (p+2ci(v-2k)\sqrt{z})^{h+j} \left( \frac{i(p+2ci(v-2k)\sqrt{z})^2}{c(v-2k)} \right)^{\frac{1}{2}(-h-j-1)} \right.$$

$$\left. \binom{j}{h} \binom{n}{j} \left( p(p+2ci(v-2k)\sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(p+2ci(v-2k)\sqrt{z})^2}{4c(v-2k)}\right) \right) + \right.$$

$$\begin{aligned}
 & 2 c i (v-2 k) \sqrt{\frac{i(p+2 c i(v-2 k) \sqrt{z})^2}{c(v-2 k)}} \Gamma\left(\frac{1}{2}(h+j+2), \frac{i(p+2 c i(v-2 k) \sqrt{z})^2}{4 c(v-2 k)}\right) \Bigg) + \\
 & (-1)^m i^{-\nu} 2^{-m-2 n-\nu-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^\nu e^{-\frac{i(p-i b(m-2 k))^2}{4 c(v-2 s)}-\frac{i m \pi}{2}} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (p-i b(m-2 k))^{-h-j+2 n} (-i b(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{i(-i b(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (p-i b(m-2 k))(-i b(m-2 k)+ \right. \right. \right. \\
 & \left. \left. \left. p-2 i c(v-2 s) \sqrt{z}\right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(-i b(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right) - \right. \right. \\
 & \left. \left. 2 i c(v-2 s) \sqrt{-\frac{i(-i b(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \left. \left. \left. -\frac{i(-i b(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right) \right) \right) \Bigg) (-i c(v-2 s))^{-2 n-2} + \\
 & (-1)^\nu e^{\frac{i m \pi}{2}-\frac{i(b i(m-2 k)+p)^2}{4 c(v-2 s)}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b i(m-2 k)+p)^{-h-j+2 n} (b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^{h+j} \right. \\
 & \left. \left( -\frac{i(b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b i(m-2 k)+p)(b i(m-2 k)+ \right. \right. \\
 & \left. \left. p-2 i c(v-2 s) \sqrt{z}\right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{i(b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right) - \right. \\
 & \left. 2 i c(v-2 s) \sqrt{-\frac{i(b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -\frac{i(b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right) \right) \Bigg) (-i c(v-2 s))^{-2 n-2} +
 \end{aligned}$$

$$\begin{aligned}
 & 2 i c (v-2 s) \sqrt{-\frac{i(b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{c(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left. -\frac{i(b i(m-2 k)+p-2 i c(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right) \Bigg) \Bigg) \Bigg) (-i c(v-2 s))^{-2 n-2} + e^{\frac{i(p-i b(m-2 k))^2}{4 c(v-2 s)}-\frac{i m \pi}{2}} \\
 & (i c(v-2 s))^{-2 n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (p-i b(m-2 k))^{-h-j+2 n} (-i b(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^{h+j} \\
 & \left(\frac{i(-i b(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{c(v-2 s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left((p-i b(m-2 k))(-i b(m-2 k)+\right. \\
 & \left. p+2 c i(v-2 s) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(-i b(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right)\right) + \\
 & 2 c i(v-2 s) \sqrt{\frac{i(-i b(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{c(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left. \frac{i(-i b(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right) \Bigg) \Bigg) + e^{\frac{i(b i(m-2 k)+p)^2}{4 c(v-2 s)}+\frac{i m \pi}{2}} (i c(v-2 s))^{-2 n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b i(m-2 k)+p)^{-h-j+2 n} (b i(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^{h+j} \\
 & \left(\frac{i(b i(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{c(v-2 s)}\right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left((b i(m-2 k)+p)(b i(m-2 k)+\right. \\
 & \left. p+2 c i(v-2 s) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), \frac{i(b i(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{4 c(v-2 s)}\right)\right) + \\
 & 2 c i(v-2 s) \sqrt{\frac{i(b i(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2}{c(v-2 s)}} \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left. i(b i(m-2 k)+p+2 c i(v-2 s) \sqrt{z})^2\right) \Bigg) \Bigg) \Bigg) \dots
 \end{aligned}$$

### Involving $z^n e^{pz} \sin^m(bz^r) \sin^v(cz^r)$

01.06.21.1598.01

$$\int z^n e^{pz} \sin^m(bz^2) \sin^v(cz^2) dz =$$

$$(-1)^{m-1} 2^{-m-v} (-p)^{-n-1} \left(\frac{m}{2}\right) \binom{v}{\frac{v}{2}} \Gamma(n+1, -pz) (1-m \bmod 2) (1-v \bmod 2) - i^{-m} 2^{-m-v-1} \binom{v}{\frac{v}{2}} (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{ip^2}{4b(2k-m)}} \left( \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p-2ib(2k-m)z)^{j+1} \left( -\frac{i(p-2ib(2k-m)z)^2}{b(2k-m)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p-2ib(2k-m)z)^2}{4b(2k-m)}\right) \right) (-ib(2k-m))^{-n-1} + \right.$$

$$\left. (-1)^m e^{-\frac{ip^2}{4b(m-2k)}} (-ib(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p-2ib(m-2k)z)^{j+1} \left( -\frac{i(p-2ib(m-2k)z)^2}{b(m-2k)} \right)^{\frac{1}{2}(-j-1)} \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{i(p-2ib(m-2k)z)^2}{4b(m-2k)}\right) \right) - (-1)^m i^{-v} 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \right.$$

$$\sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{\frac{ip^2}{4c(2k-v)}} \left( \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2ci(2k-v)z)^{j+1} \left( \frac{i(p+2ci(2k-v)z)^2}{c(2k-v)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(p+2ci(2k-v)z)^2}{4c(2k-v)}\right) \right) (ic(2k-v))^{-n-1} + e^{\frac{ip^2}{4c(v-2k)}} (ic(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} \right.$$

$$\left. \left. (p+2ci(v-2k)z)^{j+1} \left( \frac{i(p+2ci(v-2k)z)^2}{c(v-2k)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \frac{i(p+2ci(v-2k)z)^2}{4c(v-2k)}\right) \right) - \right.$$

$$i^{-m-v} 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{p^2}{4(ic(2s-v)-ib(2k-m))}} \right.$$

$$\left. \left. \left( \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p+2(ic(2s-v)-ib(2k-m))z)^{j+1} \left( -\frac{(p+2(ic(2s-v)-ib(2k-m))z)^2}{ic(2s-v)-ib(2k-m)} \right)^{\frac{1}{2}(-j-1)} \right. \right.$$

$$\left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p+2(ic(2s-v)-ib(2k-m))z)^2}{4(ic(2s-v)-ib(2k-m))}\right) \right) \right)$$

$$(ic(2s-v)-ib(2k-m))^{-n-1} + (-1)^{m+v} e^{-\frac{p^2}{4(ic(2s-v)-ib(m-2k))}} (ic(2s-v)-ib(m-2k))^{-n-1}$$

$$\begin{aligned}
 & \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p + 2(i c (2s - v) - i b (m - 2k)) z)^{j+1} \left( -\frac{(p + 2(i c (2s - v) - i b (m - 2k)) z)^2}{i c (2s - v) - i b (m - 2k)} \right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p + 2(i c (2s - v) - i b (m - 2k)) z)^2}{4(i c (2s - v) - i b (m - 2k))}\right) + \\
 & e^{-\frac{p^2}{4(i c (v-2s) - i b (2k-m))}} (i c (v - 2s) - i b (2k - m))^{-n-1} \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p + 2(i c (v - 2s) - i b (2k - m)) z)^{j+1} \\
 & \left( -\frac{(p + 2(i c (v - 2s) - i b (2k - m)) z)^2}{i c (v - 2s) - i b (2k - m)} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, \right. \\
 & \left. -\frac{(p + 2(i c (v - 2s) - i b (2k - m)) z)^2}{4(i c (v - 2s) - i b (2k - m))}\right) + (-1)^m e^{-\frac{p^2}{4(i c (v-2s) - i b (m-2k))}} (i c (v - 2s) - i b (m - 2k))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (-p)^{n-j} (p + 2(i c (v - 2s) - i b (m - 2k)) z)^{j+1} \left( -\frac{(p + 2(i c (v - 2s) - i b (m - 2k)) z)^2}{i c (v - 2s) - i b (m - 2k)} \right)^{\frac{1}{2}(-j-1)} \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(p + 2(i c (v - 2s) - i b (m - 2k)) z)^2}{4(i c (v - 2s) - i b (m - 2k))}\right) \right) ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

01.06.21.1599.01

$$\int z^n e^{p z} \sin^m(b \sqrt{z}) \sin^v(c \sqrt{z}) dz =$$

$$(-1)^{m+n} 2^{-m-v} p^{-1-n} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2) \Gamma(n + 1, -p z) + i^{-m} 2^{-m-2n-v-1} \binom{v}{\frac{v}{2}} (1 - v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{\frac{b^2(2k-m)^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b (2k - m))^{-h-j+2n} (2p \sqrt{z} - i b (2k - m))^{h+j} \right. \right.$$

$$\left. \left( -\frac{(2p \sqrt{z} - i b (2k - m))^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \right)$$

$$\left( 2p \sqrt{-\frac{(2p \sqrt{z} - i b (2k - m))^2}{p}} \Gamma\left(\frac{1}{2}(h + j + 2), -\frac{(2p \sqrt{z} - i b (2k - m))^2}{4p}\right) - i b (2k - m) \right)$$

$$\left. \left. \left. (2p \sqrt{z} - i b (2k - m)) \Gamma\left(\frac{1}{2}(h + j + 1), -\frac{(2p \sqrt{z} - i b (2k - m))^2}{4p}\right) \right) \right) \right) p^{-2n-2} + (-1)^m e^{\frac{b^2(m-2k)^2}{4p}}$$

$$\begin{aligned}
 & \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (-i b (m-2k))^{-h-j+2n} (2p\sqrt{z} - i b (m-2k))^{h+j} \left( -\frac{(2p\sqrt{z} - i b (m-2k))^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \quad \left( \frac{j}{h} \right) \binom{n}{j} \left( 2p\sqrt{-\frac{(2p\sqrt{z} - i b (m-2k))^2}{p}} \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(2p\sqrt{z} - i b (m-2k))^2}{4p} \right) - i b \right. \\
 & \quad \left. \left. (m-2k)(2p\sqrt{z} - i b (m-2k)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(2p\sqrt{z} - i b (m-2k))^2}{4p} \right) \right) \right) p^{-2n-2} \Bigg) + \\
 & i^{-m-v} 2^{-m-2n-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{\frac{c^2(2k-v)^2 - im\pi}{4p} - \frac{im\pi}{2}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c (2k-v))^{-h-j+2n} \right. \right. \\
 & \quad \left. \left. (2\sqrt{z} p + c i (2k-v))^{h+j} \left( -\frac{(2\sqrt{z} p + c i (2k-v))^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \right) \binom{j}{h} \binom{n}{j} \left( c i (2k-v) (2\sqrt{z} p + \right. \right. \\
 & \quad \left. \left. c i (2k-v)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(2\sqrt{z} p + c i (2k-v))^2}{4p} \right) + 2\sqrt{-\frac{(2\sqrt{z} p + c i (2k-v))^2}{p}} \right) \right. \\
 & \quad \left. \left. p \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(2\sqrt{z} p + c i (2k-v))^2}{4p} \right) \right) \right) p^{-2n-2} + e^{\frac{c^2(v-2k)^2 - im\pi}{4p} - \frac{im\pi}{2}} \\
 & \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (i c (v-2k))^{-h-j+2n} (2\sqrt{z} p + c i (v-2k))^{h+j} \left( -\frac{(2\sqrt{z} p + c i (v-2k))^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \quad \left( \frac{j}{h} \right) \binom{n}{j} \left( c i (v-2k) (2\sqrt{z} p + c i (v-2k)) \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(2\sqrt{z} p + c i (v-2k))^2}{4p} \right) + 2 \right. \\
 & \quad \left. \left. \sqrt{-\frac{(2\sqrt{z} p + c i (v-2k))^2}{p}} p \Gamma \left( \frac{1}{2}(h+j+2), -\frac{(2\sqrt{z} p + c i (v-2k))^2}{4p} \right) \right) \right) p^{-2n-2} \Bigg) + i^{-m-v}
 \end{aligned}$$



$$\begin{aligned}
 & 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(ic(2s-v)-ib(2k-m))^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2s-v) - ib(2k-m))^{-h-j+2n} \right. \right. \\
 & \quad \left. \left. (-ib(2k-m) + ci(2s-v) + 2p\sqrt{z})^{h+j} \left( -\frac{(-ib(2k-m) + ci(2s-v) + 2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \right. \right. \\
 & \quad \left. \left. \binom{j}{h} \binom{n}{j} \left( ic(2s-v) - ib(2k-m) \right) (-ib(2k-m) + ci(2s-v) + 2p\sqrt{z}) \right. \right. \\
 & \quad \left. \left. \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(-ib(2k-m) + ci(2s-v) + 2p\sqrt{z})^2}{4p} \right) + \right. \right. \\
 & \quad \left. \left. 2\sqrt{-\frac{(-ib(2k-m) + ci(2s-v) + 2p\sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2}(h+j+2), \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{(-ib(2k-m) + ci(2s-v) + 2p\sqrt{z})^2}{4p} \right) \right) \right) \right) p^{-2n-2} + \\
 & \quad (-1)^{m+v} e^{-\frac{(ic(2s-v)-ib(m-2k))^2}{4p}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (ic(2s-v) - ib(m-2k))^{-h-j+2n} \right. \\
 & \quad \left. (-ib(m-2k) + ci(2s-v) + 2p\sqrt{z})^{h+j} \left( -\frac{(-ib(m-2k) + ci(2s-v) + 2p\sqrt{z})^2}{p} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \quad \left. \binom{j}{h} \binom{n}{j} \left( ic(2s-v) - ib(m-2k) \right) (-ib(m-2k) + ci(2s-v) + 2p\sqrt{z}) \right. \\
 & \quad \left. \Gamma \left( \frac{1}{2}(h+j+1), -\frac{(-ib(m-2k) + ci(2s-v) + 2p\sqrt{z})^2}{4p} \right) + \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2 \sqrt{-\frac{(-i b(m-2 k)+c i(2 s-v)+2 p \sqrt{z})^2}{p}} p \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left. -\frac{(-i b(m-2 k)+c i(2 s-v)+2 p \sqrt{z})^2}{4 p}\right) \Bigg) \Bigg) p^{-2 n-2}+e^{-\frac{(i c(v-2 s)-i b(2 k-m))^2}{4 p}} \\
 & \left(\sum_{j=0}^n \sum_{h=0}^j(-1)^{j-h} 4^j(i c(v-2 s)-i b(2 k-m))^{-h-j+2 n}(-i b(2 k-m)+c i(v-2 s)+2 p \sqrt{z})^{h+j}\right. \\
 & \left.\left(-\frac{(-i b(2 k-m)+c i(v-2 s)+2 p \sqrt{z})^2}{p}\right)^{\frac{1}{2}(-h-j-1)}\binom{j}{h}\binom{n}{j}\right. \\
 & \left.\left(i c(v-2 s)-i b(2 k-m)\right)(-i b(2 k-m)+c i(v-2 s)+2 p \sqrt{z})\right. \\
 & \left.\Gamma\left(\frac{1}{2}(h+j+1),-\frac{(-i b(2 k-m)+c i(v-2 s)+2 p \sqrt{z})^2}{4 p}\right)\right)+ \\
 & 2 \sqrt{-\frac{(-i b(2 k-m)+c i(v-2 s)+2 p \sqrt{z})^2}{p}} p \Gamma\left(\frac{1}{2}(h+j+2),\right. \\
 & \left. -\frac{(-i b(2 k-m)+c i(v-2 s)+2 p \sqrt{z})^2}{4 p}\right) \Bigg) \Bigg) p^{-2 n-2}+ \\
 & (-1)^m e^{-\frac{(i c(v-2 s)-i b(m-2 k))^2}{4 p}}\left(\sum_{j=0}^n \sum_{h=0}^j(-1)^{j-h} 4^j(i c(v-2 s)-i b(m-2 k))^{-h-j+2 n}\right. \\
 & \left.(-i b(m-2 k)+c i(v-2 s)+2 p \sqrt{z})^{h+j}\left(-\frac{(-i b(m-2 k)+c i(v-2 s)+2 p \sqrt{z})^2}{p}\right)^{\frac{1}{2}(-h-j-1)}\right)
 \end{aligned}$$

$$\binom{j}{h} \binom{n}{j} \left( (i c (v - 2 s) - i b (m - 2 k)) (-i b (m - 2 k) + c i (v - 2 s) + 2 p \sqrt{z}) \right. \\ \left. \Gamma \left( \frac{1}{2} (h + j + 1), -\frac{(-i b (m - 2 k) + c i (v - 2 s) + 2 p \sqrt{z})^2}{4 p} \right) + \right. \\ \left. 2 \sqrt{-\frac{(-i b (m - 2 k) + c i (v - 2 s) + 2 p \sqrt{z})^2}{p}} p \Gamma \left( \frac{1}{2} (h + j + 2), \right. \right. \\ \left. \left. -\frac{(-i b (m - 2 k) + c i (v - 2 s) + 2 p \sqrt{z})^2}{4 p} \right) \right) p^{-2 n - 2} ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} e^{p z^r} \sin^m(b z^r) \sin^v(c z^r)$

01.06.21.1600.01

$$\int z^{\alpha-1} e^{p z^r} \sin^m(b z^r) \sin^v(c z^r) dz = \frac{(-1)^{m-1} 2^{-m-v} z^\alpha (-p z^r)^{-\frac{\alpha}{r}} (1 - m \bmod 2) (1 - v \bmod 2)}{r} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} \Gamma\left(\frac{\alpha}{r}, -p z^r\right) - \\ \frac{(2i)^{-m-v} z^\alpha}{r} \binom{v}{\frac{v}{2}} (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m e^{\frac{i\pi v}{2}} \Gamma\left(\frac{\alpha}{r}, (-2bik + ibm - p) z^r\right) ((-2bik + ibm - p) z^r)^{-\frac{\alpha}{r}} + \right. \\ \left. e^{\frac{i\pi v}{2}} ((2ibk - ibm - p) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ibk - ibm - p) z^r\right) \right) - \\ \frac{(-1)^m i^{-v} 2^{-m-v} z^\alpha}{r} \binom{m}{\frac{m}{2}} (1 - m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v \Gamma\left(\frac{\alpha}{r}, (-2cik - p + icv) z^r\right) ((-2cik - p + icv) z^r)^{-\frac{\alpha}{r}} + \right. \\ \left. ((2ick - p - icv) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ick - p - icv) z^r\right) \right) - \frac{i^{m-v} 2^{-m-v} z^\alpha}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \\ \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v \Gamma\left(\frac{\alpha}{r}, (-2bik + ibm - p - 2ics + icv) z^r\right) ((-2bik + ibm - p - 2ics + icv) z^r)^{-\frac{\alpha}{r}} + \right. \\ \left. (-1)^{m+v} ((2ibk - ibm - p - 2ics + icv) z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ibk - ibm - p - 2ics + icv) z^r\right) \right) + \\ \left( (-2bik + ibm - p + 2ics - icv) z^r \right)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-2bik + ibm - p + 2ics - icv) z^r\right) + (-1)^m \\ \left( (2ibk - ibm - p + 2ics - icv) z^r \right)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (2ibk - ibm - p + 2ics - icv) z^r\right) \Big) ; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^{\alpha-1} e^{bz^r+e} \sin^m(az^r+q) \sin^v(cz^r+g)$

01.06.21.1601.01

$$\int z^{\alpha-1} e^{bz^r+e} \sin^m(az^r+q) \sin^v(cz^r+g) dz =$$

$$\frac{(-1)^{m-1} 2^{-m-v} e^e z^\alpha (-bz^r)^{-\frac{\alpha}{r}} (1-m \bmod 2) (1-v \bmod 2)}{r} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) \Gamma\left(\frac{\alpha}{r}, -bz^r\right) - \frac{(2i)^{-m-v} z^\alpha}{r} \left(\frac{v}{2}\right) (1-v \bmod 2)$$

$$\sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( (-1)^m e^{e+2ikq-imq+\frac{i\pi v}{2}} \Gamma\left(\frac{\alpha}{r}, (-b-2iak+iam)z^r\right) ((-b-2iak+iam)z^r)^{-\frac{\alpha}{r}} + \right.$$

$$\left. e^{e-2ikq+imq+\frac{i\pi v}{2}} ((-b+2iak-iam)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+2iak-iam)z^r\right) \right) -$$

$$\frac{(-1)^m i^{-v} 2^{-m-v} z^\alpha}{r} \left(\frac{m}{2}\right) (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{e+2igk-igv} \Gamma\left(\frac{\alpha}{r}, (-b-2ick+icv)z^r\right) \right.$$

$$\left. ((-b-2ick+icv)z^r)^{-\frac{\alpha}{r}} + e^{e-2igk+igv} ((-b+2ick-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+2ick-icv)z^r\right) \right) -$$

$$\frac{i^{m-v} 2^{-m-v} z^\alpha}{r} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{e+2ikq-imq+2igs-igv} \Gamma\left(\frac{\alpha}{r}, (-b-2iak+iam-2ics+icv)z^r\right) \right.$$

$$\left. ((-b-2iak+iam-2ics+icv)z^r)^{-\frac{\alpha}{r}} + (-1)^{m+v} e^{e-2ikq+imq+2igs-igv} \right.$$

$$\left. ((-b+2iak-iam-2ics+icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+2iak-iam-2ics+icv)z^r\right) + \right.$$

$$\left. e^{e+2ikq-imq-2igs+igv} ((-b-2iak+iam+2ics-icv)z^r)^{-\frac{\alpha}{r}} \right.$$

$$\left. \Gamma\left(\frac{\alpha}{r}, (-b-2iak+iam+2ics-icv)z^r\right) + (-1)^m e^{e-2ikq+imq-2igs+igv} \right.$$

$$\left. ((-b+2iak-iam+2ics-icv)z^r)^{-\frac{\alpha}{r}} \Gamma\left(\frac{\alpha}{r}, (-b+2iak-iam+2ics-icv)z^r\right) \right) /; m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+$$

### Involving $z^n e^{bz^r+dz+e} \sin^m(az^r+pz+q) \sin^v(cz^r+fz+g)$

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$$\int z^n e^{bz^r+dz+e} \sin^m(az^r+pz+q) \sin^v(cz^r+fz+g) dz = (-1)^{m-1} 2^{-m-v-1} b^{-n-1} e^{e-\frac{d^2}{4b}} \left(\frac{m}{2}\right) \left(\frac{v}{2}\right) (1-m \bmod 2)$$

$$(1-v \bmod 2) \sum_{j=0}^n 2^{j-n} (-d)^{n-j} (d+2bz)^{j+1} \left( -\frac{(d+2bz)^2}{b} \right)^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d+2bz)^2}{4b}\right) -$$

$$i^{-m} 2^{-m-v-1} \left(\frac{v}{2}\right) (1-v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{(d-i(2k-m)p)^2}{4(b-ia(2k-m))}+e-i(2k-m)q} \left( \sum_{j=0}^n 2^{j-n} (i(2k-m)p-d)^{n-j} \right. \right.$$

$$\left. (d-i(2k-m)p+2(b-ia(2k-m))z)^{j+1} \left( -\frac{(d-i(2k-m)p+2(b-ia(2k-m))z)^2}{b-ia(2k-m)} \right)^{\frac{1}{2}(-j-1)} \right)$$

$$\begin{aligned}
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-i(2k-m)p+2(b-ia(2k-m))z)^2}{4(b-ia(2k-m))}\right) (b-ia(2k-m))^{-n-1} + \\
 & (-1)^m e^{-\frac{(d-i(m-2k)p)^2}{4(b-ia(m-2k))}+e-i(m-2k)q} (b-ia(m-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (i(m-2k)p-d)^{n-j} \\
 & (d-i(m-2k)p+2(b-ia(m-2k))z)^{j+1} \left(-\frac{(d-i(m-2k)p+2(b-ia(m-2k))z)^2}{b-ia(m-2k)}\right)^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-i(m-2k)p+2(b-ia(m-2k))z)^2}{4(b-ia(m-2k))}\right) - \\
 & i^{-m-v} 2^{-m-v-1} \binom{m}{\frac{m}{2}} (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{-\frac{(d+fi(2k-v))^2}{4(b+ci(2k-v))}+e+gi(2k-v)-\frac{im\pi}{2}} \left( \sum_{j=0}^n 2^{j-n} (-d-ifi(2k-v))^{n-j} \right. \right. \\
 & \left. \left. (d+fi(2k-v)+2(b+ci(2k-v))z)^{j+1} \left(-\frac{(d+fi(2k-v)+2(b+ci(2k-v))z)^2}{b+ci(2k-v)}\right)^{\frac{1}{2}(-j-1)} \right. \right. \\
 & \left. \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d+fi(2k-v)+2(b+ci(2k-v))z)^2}{4(b+ci(2k-v))}\right) \right) (b+ci(2k-v))^{-n-1} + \right. \\
 & \left. e^{-\frac{(d+fi(v-2k))^2}{4(b+ci(v-2k))}+e+gi(v-2k)-\frac{im\pi}{2}} (b+ci(v-2k))^{-n-1} \sum_{j=0}^n 2^{j-n} (-d-ifi(v-2k))^{n-j} \right. \\
 & \left. (d+fi(v-2k)+2(b+ci(v-2k))z)^{j+1} \left(-\frac{(d+fi(v-2k)+2(b+ci(v-2k))z)^2}{b+ci(v-2k)}\right)^{\frac{1}{2}(-j-1)} \right. \\
 & \left. \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d+fi(v-2k)+2(b+ci(v-2k))z)^2}{4(b+ci(v-2k))}\right) \right) - \\
 & i^{-m-v} 2^{-m-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(d-i(2k-m)p+fi(2s-v))^2}{4(b-ia(2k-m)+ci(2s-v))}+e-i(2k-m)q+gi(2s-v)} \right. \\
 & \left. \left( \sum_{j=0}^n 2^{j-n} (-d+i(2k-m)p-ifi(2s-v))^{n-j} (d-i(2k-m)p+fi(2s-v)+2(b-ia(2k-m)+ci(2s-v))z)^{j+1} \right. \right. \\
 & \left. \left. (-d-i(2k-m)p+fi(2s-v)+2(b-ia(2k-m)+ci(2s-v))z)^2 / \right. \right. \\
 & \left. \left. (b-ia(2k-m)+ci(2s-v))^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -\frac{(d-i(2k-m)p+fi(2s-v)+2(b-ia(2k-m)+ci(2s-v))z)^2}{4(b-ia(2k-m)+ci(2s-v))}\right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & (b - i a (2 k - m) + c i (2 s - v))^{-n-1} + (-1)^{m+v} e^{-\frac{(d-i(m-2k)p+fi(2s-v))^2}{4(b-ia(m-2k)+ci(2s-v))} + e-i(m-2k)q+gi(2s-v)} \\
 & (b - i a (m - 2 k) + c i (2 s - v))^{-n-1} \sum_{j=0}^n 2^{j-n} (-d + i (m - 2 k) p - i f (2 s - v))^{n-j} \\
 & (d - i (m - 2 k) p + f i (2 s - v) + 2 (b - i a (m - 2 k) + c i (2 s - v)) z)^{j+1} \\
 & (-d - i (m - 2 k) p + f i (2 s - v) + 2 (b - i a (m - 2 k) + c i (2 s - v)) z)^2 / \\
 & (b - i a (m - 2 k) + c i (2 s - v))^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(d - i (m - 2 k) p + f i (2 s - v) + \right. \\
 & \left. 2 (b - i a (m - 2 k) + c i (2 s - v)) z)^2 / (4 (b - i a (m - 2 k) + c i (2 s - v)))\right) + \\
 & e^{-\frac{(d-i(2k-m)p+fi(v-2s))^2}{4(b-ia(2k-m)+ci(v-2s))} + e-i(2k-m)q+gi(v-2s)} (b - i a (2 k - m) + c i (v - 2 s))^{-n-1} \sum_{j=0}^n 2^{j-n} \\
 & (-d + i (2 k - m) p - i f (v - 2 s))^{n-j} (d - i (2 k - m) p + f i (v - 2 s) + 2 (b - i a (2 k - m) + c i (v - 2 s)) \\
 & z)^{j+1} (-d - i (2 k - m) p + f i (v - 2 s) + 2 (b - i a (2 k - m) + c i (v - 2 s)) z)^2 / \\
 & (b - i a (2 k - m) + c i (v - 2 s))^{\frac{1}{2}(-j-1)} \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(d - i (2 k - m) p + f i (v - 2 s) + \right. \\
 & \left. 2 (b - i a (2 k - m) + c i (v - 2 s)) z)^2 / (4 (b - i a (2 k - m) + c i (v - 2 s)))\right) + \\
 & (-1)^m e^{-\frac{(d-i(m-2k)p+fi(v-2s))^2}{4(b-ia(m-2k)+ci(v-2s))} + e-i(m-2k)q+gi(v-2s)} (b - i a (m - 2 k) + c i (v - 2 s))^{-n-1} \\
 & \sum_{j=0}^n 2^{j-n} (-d + i (m - 2 k) p - i f (v - 2 s))^{n-j} (d - i (m - 2 k) p + f i (v - 2 s) + \\
 & 2 (b - i a (m - 2 k) + c i (v - 2 s)) z)^{j+1} (-d - i (m - 2 k) p + f i (v - 2 s) + \\
 & 2 (b - i a (m - 2 k) + c i (v - 2 s)) z)^2 / (b - i a (m - 2 k) + c i (v - 2 s))^{\frac{1}{2}(-j-1)} \\
 & \binom{n}{j} \Gamma\left(\frac{j+1}{2}, -(d - i (m - 2 k) p + f i (v - 2 s) + 2 (b - i a (m - 2 k) + c i (v - 2 s)) z)^2 / \right. \\
 & \left. (4 (b - i a (m - 2 k) + c i (v - 2 s)))\right) \Bigg) / ; n \in \mathbb{N} \wedge m \in \mathbb{N}^+ \wedge v \in \mathbb{N}^+
 \end{aligned}$$

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$$\int z^n e^{\sqrt{z} b + d z + e} \sin^m(\sqrt{z} a + p z + q) \sin^v(\sqrt{z} c + f z + g) dz =$$

$$(-1)^m 2^{-m-2n-v-1} d^{-2n-2} e^{\frac{b^2}{4d}} \binom{m}{\frac{m}{2}} \binom{v}{\frac{v}{2}} (1 - m \bmod 2) (1 - v \bmod 2)$$

$$\sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j b^{-h-j+2n} (b + 2 d \sqrt{z})^{h+j} \left( -\frac{(b + 2 d \sqrt{z})^2}{d} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( b (b + 2 d \sqrt{z}) \Gamma\left(\frac{1}{2}(h + j + 1), \right. \right.$$

$$\left. -\frac{(b + 2 d \sqrt{z})^2}{4 d} \right) + 2 \sqrt{-\frac{(b + 2 d \sqrt{z})^2}{d}} d \Gamma\left(\frac{1}{2}(h + j + 2), -\frac{(b + 2 d \sqrt{z})^2}{4 d}\right) \Bigg) + i^{-m} 2^{-m-2n-v-1} \binom{v}{\frac{v}{2}}$$

$$\begin{aligned}
 & (1 - v \bmod 2) \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \left( e^{-\frac{(b-ia(2k-m))^2}{4(d-i(2k-m)p)} + e^{-i(2k-m)q}} \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b-ia(2k-m))^{-h-j+2n} (b-ia(2k-m) + \right. \right. \\
 & \qquad \qquad \qquad \left. \left. 2(d-i(2k-m)p)\sqrt{z}\right)^{h+j} \left( -\frac{(b-ia(2k-m) + 2(d-i(2k-m)p)\sqrt{z})^2}{d-i(2k-m)p} \right)^{\frac{1}{2}(-h-j-1)} \right. \\
 & \qquad \qquad \qquad \left. \binom{j}{h} \binom{n}{j} \left( (b-ia(2k-m))(b-ia(2k-m) + 2(d-i(2k-m)p)\sqrt{z}) \right. \right. \\
 & \qquad \qquad \qquad \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(b-ia(2k-m) + 2(d-i(2k-m)p)\sqrt{z})^2}{4(d-i(2k-m)p)}\right) + 2 \right. \right. \\
 & \qquad \qquad \qquad \left. \sqrt{-\frac{(b-ia(2k-m) + 2(d-i(2k-m)p)\sqrt{z})^2}{d-i(2k-m)p}} (d-i(2k-m)p) \right. \\
 & \qquad \qquad \qquad \left. \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(b-ia(2k-m) + 2(d-i(2k-m)p)\sqrt{z})^2}{4(d-i(2k-m)p)}\right) \right) \right) \right) \\
 & (d-i(2k-m)p)^{-2n-2} + (-1)^m e^{-\frac{(b-ia(m-2k))^2}{4(d-i(m-2k)p)} + e^{-i(m-2k)q}} (d-i(m-2k)p)^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b-ia(m-2k))^{-h-j+2n} (b-ia(m-2k) + 2(d-i(m-2k)p)\sqrt{z})^{h+j} \\
 & \left( -\frac{(b-ia(m-2k) + 2(d-i(m-2k)p)\sqrt{z})^2}{d-i(m-2k)p} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b-ia(m-2k))(b-ia(m-2k) + \right. \\
 & \qquad \qquad \qquad \left. 2(d-i(m-2k)p)\sqrt{z}\right) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(b-ia(m-2k) + 2(d-i(m-2k)p)\sqrt{z})^2}{4(d-i(m-2k)p)}\right) + \\
 & \qquad \qquad \qquad 2\sqrt{-\frac{(b-ia(m-2k) + 2(d-i(m-2k)p)\sqrt{z})^2}{d-i(m-2k)p}} (d-i(m-2k)p) \left( \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{1}{2} (h+j+2), -\frac{(b-i a(m-2 k)+2(d-i(m-2 k) p) \sqrt{z})^2}{4(d-i(m-2 k) p)} \right) \right) \right) + \\
 & i^{-m-v} 2^{-m-2 n-v-1} \left( \frac{m}{2} \right) (1-m \bmod 2) \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( (-1)^v e^{-\frac{(b+c i(2 k-v))^2}{4(d+f i(2 k-v))+e+g i(2 k-v)}-\frac{i m \pi}{2}} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b+c i(2 k-v))^{-h-j+2 n} (b+c i(2 k-v)+2(d+f i(2 k-v)) \sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -\frac{(b+c i(2 k-v)+2(d+f i(2 k-v)) \sqrt{z})^2}{d+f i(2 k-v)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (b+c i(2 k-v))(b+c i(2 k-v)+ \right. \right. \\
 & \left. \left. 2(d+f i(2 k-v)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(b+c i(2 k-v)+2(d+f i(2 k-v)) \sqrt{z})^2}{4(d+f i(2 k-v))}\right) + 2 \right. \right. \\
 & \left. \left. \sqrt{-\frac{(b+c i(2 k-v)+2(d+f i(2 k-v)) \sqrt{z})^2}{d+f i(2 k-v)}} (d+f i(2 k-v)) \right. \right. \\
 & \left. \left. \left. \Gamma\left(\frac{1}{2}(h+j+2), -\frac{(b+c i(2 k-v)+2(d+f i(2 k-v)) \sqrt{z})^2}{4(d+f i(2 k-v))}\right) \right) \right) \right) \\
 & (d+f i(2 k-v))^{-2 n-2} + e^{-\frac{(b+c i(v-2 k))^2}{4(d+f i(v-2 k))+e+g i(v-2 k)}-\frac{i m \pi}{2}} (d+f i(v-2 k))^{-2 n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b+c i(v-2 k))^{-h-j+2 n} (b+c i(v-2 k)+2(d+f i(v-2 k)) \sqrt{z})^{h+j} \\
 & \left( -\frac{(b+c i(v-2 k)+2(d+f i(v-2 k)) \sqrt{z})^2}{d+f i(v-2 k)} \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (b+c i(v-2 k))(b+c i(v-2 k)+ \\
 & 2(d+f i(v-2 k)) \sqrt{z}) \Gamma\left(\frac{1}{2}(h+j+1), -\frac{(b+c i(v-2 k)+2(d+f i(v-2 k)) \sqrt{z})^2}{4(d+f i(v-2 k))}\right) +
 \end{aligned}$$



$$\begin{aligned}
 & 2\sqrt{-\frac{(b+ci(v-2k)+2(d+fi(v-2k))\sqrt{z})^2}{d+fi(v-2k)}}(d+fi(v-2k))\Gamma\left(\frac{1}{2}(h+j+2), -\frac{(b+ci(v-2k)+2(d+fi(v-2k))\sqrt{z})^2}{4(d+fi(v-2k))}\right) \Bigg) + \\
 & i^{-m-v} 2^{-m-2n-v-1} \sum_{k=0}^{\lfloor \frac{m-1}{2} \rfloor} (-1)^k \binom{m}{k} \sum_{s=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^s \binom{v}{s} \left( (-1)^v e^{-\frac{(b-ia(2k-m)+ci(2s-v))^2}{4(d-i(2k-m)p+fi(2s-v))} + e^{-i(2k-m)q+gi(2s-v)}} \right. \\
 & \left. \left( \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b-ia(2k-m)+ci(2s-v))^{-h-j+2n} \right. \right. \\
 & \left. \left. (b-ia(2k-m)+ci(2s-v)+2(d-i(2k-m)p+fi(2s-v))\sqrt{z})^{h+j} \right. \right. \\
 & \left. \left. \left( -(b-ia(2k-m)+ci(2s-v)+2(d-i(2k-m)p+fi(2s-v))\sqrt{z})^2 \right) \right. \right. \\
 & \left. \left. (d-i(2k-m)p+fi(2s-v))^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (b-ia(2k-m)+ci(2s-v)) \right. \right. \\
 & \left. \left. (b-ia(2k-m)+ci(2s-v)+2(d-i(2k-m)p+fi(2s-v))\sqrt{z}) \right. \right. \\
 & \left. \left. \Gamma\left(\frac{1}{2}(h+j+1), -(b-ia(2k-m)+ci(2s-v)+2(d-i(2k-m)p+fi(2s-v))\sqrt{z})^2 \right) \right. \right. \\
 & \left. \left. (4(d-i(2k-m)p+fi(2s-v))) \right) + 2(d-i(2k-m)p+fi(2s-v)) \Gamma\left(\frac{1}{2}(h+j+2), \right. \right. \\
 & \left. \left. -(b-ia(2k-m)+ci(2s-v)+2(d-i(2k-m)p+fi(2s-v))\sqrt{z})^2 \right) \right. \right. \\
 & \left. \left. (4(d-i(2k-m)p+fi(2s-v))) \right) \sqrt{\left( -(b-ia(2k-m)+ci(2s-v)+ \right. \right. \\
 & \left. \left. 2(d-i(2k-m)p+fi(2s-v))\sqrt{z})^2 \right) / (d-i(2k-m)p+fi(2s-v)) \right) \Bigg) \\
 & (d-i(2k-m)p+fi(2s-v))^{-2n-2} + (-1)^{m+v} e^{-\frac{(b-ia(m-2k)+ci(2s-v))^2}{4(d-i(m-2k)p+fi(2s-v))} + e^{-i(m-2k)q+gi(2s-v)}} \\
 & (d-i(m-2k)p+fi(2s-v))^{-2n-2} \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b-ia(m-2k)+ci(2s-v))^{-h-j+2n} \\
 & (b-ia(m-2k)+ci(2s-v)+2(d-i(m-2k)p+fi(2s-v))\sqrt{z})^{h+j} \\
 & \left( -(b-ia(m-2k)+ci(2s-v)+2(d-i(m-2k)p+fi(2s-v))\sqrt{z})^2 \right) / \\
 & (d-i(m-2k)p+fi(2s-v))^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} (b-ia(m-2k)+ci(2s-v)) \\
 & (b-ia(m-2k)+ci(2s-v)+2(d-i(m-2k)p+fi(2s-v))\sqrt{z}) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(b-ia(m-2k)+ci(2s-v)+2(d-i(m-2k)p+fi(2s-v))\sqrt{z})^2 \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left. (4(d-i(m-2k)p+fi(2s-v))) \right) + 2(d-i(m-2k)p+fi(2s-v)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(b-ia(m-2k)+ci(2s-v)+2(d-i(m-2k)p+fi(2s-v))\sqrt{z})^2 \right) / \\
 & \left. (4(d-i(m-2k)p+fi(2s-v))) \right) \sqrt{\left( -(b-ia(m-2k)+ci(2s-v)+ \right. \\
 & \left. 2(d-i(m-2k)p+fi(2s-v))\sqrt{z})^2 / (d-i(m-2k)p+fi(2s-v)) \right)} \Bigg) + \\
 & e^{-\frac{(b-ia(2k-m)+ci(v-2s))^2}{4(d-i(2k-m)p+fi(v-2s))} + e^{-i(2k-m)q+gi(v-2s)}} (d-i(2k-m)p+fi(v-2s))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b-ia(2k-m)+ci(v-2s))^{-h-j+2n} \\
 & \left. (b-ia(2k-m)+ci(v-2s)+2(d-i(2k-m)p+fi(v-2s))\sqrt{z})^{h+j} \right) \\
 & \left. \left( -(b-ia(2k-m)+ci(v-2s)+2(d-i(2k-m)p+fi(v-2s))\sqrt{z})^2 \right) / \right. \\
 & \left. (d-i(2k-m)p+fi(v-2s)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b-ia(2k-m)+ci(v-2s)) \right. \\
 & \left. (b-ia(2k-m)+ci(v-2s)+2(d-i(2k-m)p+fi(v-2s))\sqrt{z}) \right) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(b-ia(2k-m)+ci(v-2s)+2(d-i(2k-m)p+fi(v-2s))\sqrt{z})^2 \right) / \\
 & \left. (4(d-i(2k-m)p+fi(v-2s))) \right) + 2(d-i(2k-m)p+fi(v-2s)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(b-ia(2k-m)+ci(v-2s)+2(d-i(2k-m)p+fi(v-2s))\sqrt{z})^2 \right) / \\
 & \left. (4(d-i(2k-m)p+fi(v-2s))) \right) \sqrt{\left( -(b-ia(2k-m)+ci(v-2s)+ \right. \\
 & \left. 2(d-i(2k-m)p+fi(v-2s))\sqrt{z})^2 / (d-i(2k-m)p+fi(v-2s)) \right)} \Bigg) + \\
 & (-1)^m e^{-\frac{(b-ia(m-2k)+ci(v-2s))^2}{4(d-i(m-2k)p+fi(v-2s))} + e^{-i(m-2k)q+gi(v-2s)}} (d-i(m-2k)p+fi(v-2s))^{-2n-2} \\
 & \sum_{j=0}^n \sum_{h=0}^j (-1)^{j-h} 4^j (b-ia(m-2k)+ci(v-2s))^{-h-j+2n} \\
 & \left. (b-ia(m-2k)+ci(v-2s)+2(d-i(m-2k)p+fi(v-2s))\sqrt{z})^{h+j} \right) \\
 & \left. \left( -(b-ia(m-2k)+ci(v-2s)+2(d-i(m-2k)p+fi(v-2s))\sqrt{z})^2 \right) / \right. \\
 & \left. (d-i(m-2k)p+fi(v-2s)) \right)^{\frac{1}{2}(-h-j-1)} \binom{j}{h} \binom{n}{j} \left( (b-ia(m-2k)+ci(v-2s)) \right. \\
 & \left. (b-ia(m-2k)+ci(v-2s)+2(d-i(m-2k)p+fi(v-2s))\sqrt{z}) \right) \\
 & \Gamma\left(\frac{1}{2}(h+j+1), -(b-ia(m-2k)+ci(v-2s)+2(d-i(m-2k)p+fi(v-2s))\sqrt{z})^2 \right) / \\
 & \left. (4(d-i(m-2k)p+fi(v-2s))) \right) + 2(d-i(m-2k)p+fi(v-2s)) \\
 & \Gamma\left(\frac{1}{2}(h+j+2), -(b-ia(m-2k)+ci(v-2s)+2(d-i(m-2k)p+fi(v-2s))\sqrt{z})^2 \right) /
 \end{aligned}$$



01.06.21.1605.01

$$\int (az+b)^\beta d^z \sin^v(cz+e) dz =$$

$$-\frac{1}{a} 2^{-v} (b+az)^{\beta+1} d^{-\frac{b}{a}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-i\left(-\frac{bc(2k-v)}{a} + \frac{\pi v}{2} - e(v-2k)\right)} E_{-\beta} \left( \frac{i(b+az)(c(2k-v) + i \log(d))}{a} \right) + \right.$$

$$\left. e^{i\left(-\frac{bc(2k-v)}{a} + \frac{\pi v}{2} - e(v-2k)\right)} E_{-\beta} \left( -\frac{i(b+az)(c(2k-v) - i \log(d))}{a} \right) \right) -$$

$$\frac{2^{-v}(1-v \bmod 2)}{a} d^{-\frac{b}{a}} (b+az)^{\beta+1} E_{-\beta} \left( -\frac{(b+az) \log(d)}{a} \right) \binom{v}{\frac{v}{2}} ; v \in \mathbb{N}$$

01.06.21.1606.01

$$\int (az+b)^\beta e^{pz} \sin^v(cz+e) dz =$$

$$-\frac{1}{a} 2^{-v} e^{-\frac{pb}{a}} (b+az)^{\beta+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( e^{-i\left(-\frac{bc(2k-v)}{a} + \frac{\pi v}{2} - e(v-2k)\right)} E_{-\beta} \left( \frac{i(b+az)(ip+c(2k-v))}{a} \right) + e^{i\left(-\frac{bc(2k-v)}{a} + \frac{\pi v}{2} - e(v-2k)\right)} \right.$$

$$\left. E_{-\beta} \left( -\frac{i(b+az)(c(2k-v) - ip)}{a} \right) \right) - \frac{2^{-v}(1-v \bmod 2)}{a} e^{-\frac{pb}{a}} (b+az)^{\beta+1} E_{-\beta} \left( -\frac{(b+az)p}{a} \right) \binom{v}{\frac{v}{2}} ; v \in \mathbb{N}$$

01.06.21.1607.01

$$\int (az+b)^\beta d^z \sin^v(cz) dz = -\frac{1}{a} 2^{-v} (b+az)^{\beta+1} d^{-\frac{b}{a}} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k}$$

$$\left( e^{-i\left(-\frac{bc(2k-v)}{a} + \frac{\pi v}{2}\right)} E_{-\beta} \left( \frac{i(b+az)(c(2k-v) + i \log(d))}{a} \right) + e^{i\left(-\frac{bc(2k-v)}{a} + \frac{\pi v}{2}\right)} E_{-\beta} \left( -\frac{i(b+az)(c(2k-v) - i \log(d))}{a} \right) \right) -$$

$$\frac{2^{-v}(1-v \bmod 2)}{a} d^{-\frac{b}{a}} (b+az)^{\beta+1} E_{-\beta} \left( -\frac{(b+az) \log(d)}{a} \right) \binom{v}{\frac{v}{2}} ; v \in \mathbb{N}$$

01.06.21.1608.01

$$\int (b+az)^\beta e^{pz} \sin^v(cz) dz = \frac{2^{-v}(1-v \bmod 2)}{p} e^{-\frac{bp}{a}} (b+az)^\beta \left( -\frac{p(b+az)}{a} \right)^{-\beta} \binom{v}{\frac{v}{2}} \Gamma \left( \beta+1, -\frac{p(b+az)}{a} \right) - \frac{1}{a} 2^{-v}$$

$$(b+az)^{\beta+1} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( i^v e^{-\frac{b(p-ic(v-2k))}{a}} \left( -\frac{(p-ic(v-2k))(b+az)}{a} \right)^{-\beta-1} \Gamma \left( \beta+1, -\frac{(p-ic(v-2k))(b+az)}{a} \right) + \right.$$

$$\left. i^{-v} e^{-\frac{b(p+ci(v-2k))}{a}} \left( -\frac{(p+ci(v-2k))(b+az)}{a} \right)^{-\beta-1} \Gamma \left( \beta+1, -\frac{(p+ci(v-2k))(b+az)}{a} \right) \right) ; v \in \mathbb{N}$$

01.06.21.1609.01

$$\int \frac{e^{pz} \sin^v(cz)}{\sqrt{az+b}} dz = \frac{2^{-v} e^{-\frac{bp}{a}} \sqrt{\pi} (1-v \bmod 2) \left(\frac{v}{2}\right) \operatorname{erfi}\left(\sqrt{\frac{p}{a}} \sqrt{b+az}\right) + \frac{2^{-v} \sqrt{\pi}}{a} \sum_{k=0}^{\lfloor \frac{v-1}{2} \rfloor} (-1)^k \binom{v}{k} \left( \frac{i^v}{\sqrt{\frac{p-ic(v-2k)}{a}}} e^{-\frac{b(p-ic(v-2k))}{a}} \operatorname{erfi}\left(\sqrt{\frac{p-ic(v-2k)}{a}} \sqrt{b+az}\right) + \frac{i^{-v}}{\sqrt{\frac{p+ci(v-2k)}{a}}} e^{-\frac{b(p+ci(v-2k))}{a}} \operatorname{erfi}\left(\sqrt{\frac{p+ci(v-2k)}{a}} \sqrt{b+az}\right) \right)}{; v \in \mathbb{N}}$$

01.06.21.1610.01

$$\int \frac{e^{pz} \sin^2(cz)}{\sqrt{az+b}} dz = \frac{\sqrt{\pi}}{4a} \left( \frac{e^{-\frac{b(-2ic+p)}{a}} \operatorname{erfi}\left(\sqrt{\frac{-2ic+p}{a}} \sqrt{b+az}\right)}{\sqrt{\frac{-2ic+p}{a}}} - \frac{e^{-\frac{b(2ic+p)}{a}} \operatorname{erfi}\left(\sqrt{\frac{2ic+p}{a}} \sqrt{b+az}\right)}{\sqrt{\frac{2ic+p}{a}}} \right) + \frac{e^{-\frac{bp}{a}} \sqrt{\pi}}{2a \sqrt{\frac{p}{a}}} \operatorname{erfi}\left(\sqrt{\frac{p}{a}} \sqrt{b+az}\right)$$

**Involving products of the direct function, exponential and algebraic functions**

Involving products of sin, exp and algebraic functions

**Involving  $(az + b)^\beta d^z \sin(cz) \sin(ez)$**

01.06.21.1611.01

$$\int (a + bz)^\beta d^z \sin(cz) \sin(ez) dz = -\frac{1}{4} i d^{-\frac{a}{b}} (a + bz)^\beta$$

$$\left( -\frac{1}{b} \left( i (a + bz) \Gamma\left(\beta + 1, \frac{i(a + bz)(c - e + i \log(d))}{b}\right) \left(\frac{i(a + bz)(c - e + i \log(d))}{b}\right)^{-\beta-1} \left(\cos\left(\frac{a(c - e)}{b}\right) + i \sin\left(\frac{a(c - e)}{b}\right)\right) \right) + \right.$$

$$\frac{1}{c - e - i \log(d)}$$

$$\left. \left( \Gamma\left(\beta + 1, -\frac{i(a + bz)(c - e - i \log(d))}{b}\right) \left(-\frac{i(a + bz)(c - e - i \log(d))}{b}\right)^{-\beta} \left(\cos\left(\frac{a(c - e)}{b}\right) - i \sin\left(\frac{a(c - e)}{b}\right)\right) \right) + \right.$$

$$\frac{\Gamma\left(\beta + 1, \frac{i(a + bz)(c + e + i \log(d))}{b}\right) \left(\frac{i(a + bz)(c + e + i \log(d))}{b}\right)^{-\beta} \left(\cos\left(\frac{a(c + e)}{b}\right) + i \sin\left(\frac{a(c + e)}{b}\right)\right)}{c + e + i \log(d)} - \frac{1}{c + e - i \log(d)}$$

$$\left. \left( \Gamma\left(\beta + 1, -\frac{i(a + bz)(c + e - i \log(d))}{b}\right) \left(-\frac{i(a + bz)(c + e - i \log(d))}{b}\right)^{-\beta} \left(\cos\left(\frac{a(c + e)}{b}\right) - i \sin\left(\frac{a(c + e)}{b}\right)\right) \right) \right)$$

### Definite integration

For the direct function itself

01.06.21.0014.01

$$\int_0^\infty \frac{\sin(t)}{t} dt = \frac{\pi}{2}$$

01.06.21.0015.01

$$\int_0^\infty \frac{\sin(at)}{t} dt = \frac{\pi}{2} \operatorname{sgn}(a) \quad ; a \in \mathbb{R}$$

01.06.21.0016.01

$$\int_0^\infty \sin(t^2) dt = \frac{1}{2} \sqrt{\frac{\pi}{2}}$$

01.06.21.0017.01

$$\int_0^\infty t^k \sin(t) dt = \cos\left(\frac{k\pi}{2}\right) \Gamma(k + 1) \quad ; -2 < \operatorname{Re}(k) < 0$$

01.06.21.0018.01

$$\int_0^\infty t^{-z} \sin(at) dt = \frac{\pi a^{z-1}}{2 \Gamma(z) \sin\left(\frac{\pi z}{2}\right)} \quad ; 0 < \operatorname{Re}(z) < 2 \wedge a \in \mathbb{R}$$

01.06.21.1612.01

$$\int_0^\infty \left(\frac{\sin(x)}{x}\right)^n dx = 2^{1-2n} \sqrt{\pi} \frac{\Gamma\left(\frac{1}{4}(-2n - (-1)^n + 3)\right)}{\Gamma\left(\frac{1}{4}(2n - (-1)^n + 1)\right)} \sum_{j=0}^{\lfloor \frac{n-1}{2} \rfloor} \frac{(-1)^{j+\lfloor \frac{n}{2} \rfloor} (n-2j)^{n-1} n!}{j!(n-j)!} \quad ; n \in \mathbb{N}^+$$

01.06.21.1613.01

$$\int_0^\infty \sin(ax^4) \sin(bx^2) dx = -\frac{1}{4} \pi \sqrt{\frac{b}{2a}} \sin\left(\frac{b^2}{8a} - \frac{3\pi}{8}\right) J_{\frac{1}{4}}\left(\frac{b^2}{8a}\right); a \in \mathbb{R} \wedge b \in \mathbb{R}$$

**Involving the direct function**

01.06.21.0019.01

$$\int_0^{2\pi} \sin(nt) \sin(mt) dt = \frac{-m \sin(2\pi m + 2n\pi) + n \sin(2\pi m + 2n\pi) + m \sin(2m\pi - 2n\pi) + n \sin(2m\pi - 2n\pi)}{2(m-n)(m+n)}$$

01.06.21.0020.01

$$\int_0^{2\pi} \sin^2(nt) dt = \pi - \frac{\sin(4n\pi)}{4n}$$

01.06.21.1618.01

$$\int_0^z \sin^{2n}(t) dt = \frac{\left(\frac{1}{2}\right)_n}{n!} \left( z - \frac{1}{2} \cot(z) \sum_{k=1}^n \frac{(k-1)! \sin^{2k}(z)}{\left(\frac{1}{2}\right)_k} \right); n \in \mathbb{N}$$

01.06.21.0021.01

$$\int_0^\pi \frac{1}{\sin\left(\frac{t}{2}\right)} \sin\left(\left(n + \frac{1}{2}\right)t\right) dt = \pi; n \in \mathbb{N}$$

**Dirichlet lemma**

01.06.21.1619.01

$$\int_{\pi k + \csc^{-1}(\sqrt{m})}^{\pi k + \frac{\pi}{2}} \sqrt{1 - m \sin^2(t)} dt = (2k+1)E(m) - E\left(\pi k + \csc^{-1}(\sqrt{m}) \mid m\right); k \in \mathbb{Z}$$

**Dirichlet lemma**

01.06.21.1620.01

$$\int_{k\pi - \csc^{-1}(\sqrt{m})}^{k\pi + \frac{\pi}{2}} \frac{1}{\sqrt{1 - m \sin^2(t)}} dt = (2k+1)K(m) - F\left(k\pi - \csc^{-1}(\sqrt{m}) \mid m\right); k \in \mathbb{Z}$$

**Dirichlet lemma**

01.06.21.1621.01

$$\int_{\pi k + \csc^{-1}(\sqrt{m})}^{\pi k + \frac{\pi}{2}} \frac{1}{(1 - n \sin^2(t)) \sqrt{1 - m \sin^2(t)}} dt = (2k+1)\Pi(n \mid m) - \Pi\left(n; \pi k + \csc^{-1}(\sqrt{m}) \mid m\right); k \in \mathbb{Z}$$

**Dirichlet lemma**

**Involving related functions**

01.06.21.0022.01

$$\int_0^{2\pi} \cos(nt) \sin(mt) dt = \frac{m \cos(2\pi m + 2n\pi) - n \cos(2\pi m + 2n\pi) + m \cos(2m\pi - 2n\pi) + n \cos(2m\pi - 2n\pi)}{2(n-m)(m+n)} - \frac{m}{(n-m)(m+n)}$$

01.06.21.0023.01

$$\int_0^{\frac{\pi}{2}} \log(\sin(t)) dt = -\frac{\pi}{2} \log(2)$$

## Integral transforms

### Fourier exp transforms

01.06.22.0001.01

$$\mathcal{F}_t[\sin(at)](x) = i\sqrt{\frac{\pi}{2}} \delta(x-a) - i\sqrt{\frac{\pi}{2}} \delta(a+x) \quad ; \quad a \in \mathbb{R}$$

### Inverse Fourier exp transforms

01.06.22.0002.01

$$\mathcal{F}_t^{-1}[\sin(t)](z) = -i\sqrt{\frac{\pi}{2}} \delta(z-1) + i\sqrt{\frac{\pi}{2}} \delta(z+1)$$

### Fourier cos transforms

01.06.22.0003.01

$$\mathcal{F}_{C_t}[\sin(at)](z) = \sqrt{\frac{2}{\pi}} \frac{a}{a^2 - z^2} \quad ; \quad a \in \mathbb{R}$$

### Fourier sin transforms

01.06.22.0004.01

$$\mathcal{F}_{S_t}[\sin(at)](z) = \sqrt{\frac{\pi}{2}} (\delta(a-z) - \delta(a+z)) \quad ; \quad a \in \mathbb{R}$$

### Laplace transforms

01.06.22.0005.01

$$\mathcal{L}_t[\sin(t)](z) = \frac{1}{z^2 + 1}$$

### Mellin transforms

01.06.22.0006.01

$$\mathcal{M}_t[\sin(t)](z) = \Gamma(z) \sin\left(\frac{\pi z}{2}\right) \quad ; \quad -1 < \operatorname{Re}(z) < 1$$

### Hankel transforms

01.06.22.0007.01

$$\mathcal{H}_{r,\nu}[t^{\alpha-1} \sin(t)](z) = -\frac{1}{\Gamma(\nu+1)} \left( 2^{-\nu} z^{\nu+\frac{1}{2}} \cos\left(\frac{1}{4}\pi(2\alpha+2\nu+3)\right) \Gamma\left(\alpha+\nu+\frac{1}{2}\right) {}_2F_1\left(\frac{1}{4}(2\alpha+2\nu+1), \frac{1}{4}(2\alpha+2\nu+3); \nu+1; z^2\right) \right) \quad ;$$

$$\operatorname{Re}(\alpha+\nu) > -\frac{3}{2} \wedge \operatorname{Re}(\alpha) < 1$$



## Hilbert transforms

01.06.22.0008.01

$$\mathcal{H}_t[\sin(t)](x) = \cos(x)$$

## Summation

### Finite summation

01.06.23.0001.01

$$\sum_{k=0}^n \sin(ak) = \csc\left(\frac{a}{2}\right) \sin\left(\frac{1}{2} a (n+1)\right) \sin\left(\frac{an}{2}\right)$$

01.06.23.0002.01

$$\sum_{k=0}^n (-1)^k \sin(ak) = \cos\left(\frac{1}{2} (a+n(a+\pi))\right) \sec\left(\frac{a}{2}\right) \sin\left(\frac{1}{2} n(a+\pi)\right)$$

01.06.23.0003.01

$$\sum_{k=0}^n \sin(ak+z) = \csc\left(\frac{a}{2}\right) \sin\left(\frac{1}{2} a (n+1)\right) \sin\left(\frac{an}{2} + z\right)$$

01.06.23.0004.01

$$\sum_{k=0}^n (-1)^k \sin(ak+z) = \cos\left(\frac{1}{2} (a+n(a+\pi))\right) \sec\left(\frac{a}{2}\right) \sin\left(\frac{1}{2} n(a+\pi) + z\right)$$

01.06.23.0005.01

$$\sum_{k=1}^n \sin((2k-1)a) = \csc(a) \sin^2(an)$$

01.06.23.0006.01

$$\sum_{k=1}^n (-1)^k \sin((2k-1)a) = \frac{1}{2} \sec(a) \sin(n(2a-\pi))$$

01.06.23.0007.01

$$\sum_{k=1}^n k \sin(ka) = \frac{1}{4} \csc^2\left(\frac{a}{2}\right) ((n+1) \sin(na) - n \sin((n+1)a))$$

01.06.23.0008.01

$$\sum_{k=1}^n z^k \sin(ka) = \frac{z((z \sin(an) - \sin(a(n+1)))z^n + \sin(a))}{z^2 - 2 \cos(a)z + 1}$$

### Infinite summation

01.06.23.0009.01

$$\sum_{k=1}^{\infty} \frac{\sin(kx)}{k} = \frac{\pi-x}{2} \quad ; 0 < \operatorname{Re}(x) < 2\pi$$

01.06.23.0010.01

$$\sum_{k=1}^{\infty} \frac{(-1)^{k-1} \sin(kx)}{k} = \frac{x}{2} \quad ; |\operatorname{Re}(x)| < \pi$$

01.06.23.0011.01

$$\sum_{k=1}^{\infty} \frac{\sin(kx)}{k^3} = \frac{x^3}{12} - \frac{\pi x^2}{4} + \frac{\pi^2 x}{6} \quad ; 0 \leq \operatorname{Re}(x) \leq 2\pi$$

01.06.23.0012.01

$$\sum_{k=1}^{\infty} \frac{k \sin(kx)}{a^2 + k^2} = \frac{\pi \sinh((\pi - x)a)}{2 \sinh(\pi a)} \quad ; 0 < \operatorname{Re}(x) < 2\pi$$

01.06.23.0013.01

$$\sum_{k=1}^{\infty} \frac{(-1)^{k-1} k \sin(kx)}{a^2 + k^2} = \frac{\pi \sinh(xa)}{2 \sinh(\pi a)} \quad ; |\operatorname{Re}(x)| < \pi$$

01.06.23.0014.01

$$\sum_{k=1}^{\infty} e^{-ka} \sin(kx) = \frac{\sin(x)}{2(\cosh(a) - \cos(x))} \quad ; \operatorname{Re}(a) > 0$$

01.06.23.0015.01

$$\sum_{k=1}^{\infty} z^k \sin(kx) = \frac{z \sin(x)}{z^2 - 2 \cos(x)z + 1} \quad ; |z| < 1$$

01.06.23.0016.01

$$\sum_{k=1}^{\infty} \frac{z^k \sin(kx)}{k} = \tan^{-1} \left( \frac{z \sin(x)}{1 - z \cos(x)} \right) \quad ; 0 < \operatorname{Re}(x) < 2\pi \wedge |z| < 1$$

01.06.23.0017.01

$$\sum_{k=1}^{\infty} \frac{\sin(kx)}{k!} = e^{\cos(x)} \sin(\sin(x))$$

01.06.23.0018.01

$$\sum_{k=1}^{\infty} \frac{z^k \sin(kx)}{k!} = e^{z \cos(x)} \sin(z \sin(x))$$

01.06.23.0019.01

$$\sum_{k=1}^{\infty} \sin(kx) = \frac{1}{2} \cot\left(\frac{x}{2}\right) \quad ; x \in \mathbb{R}$$

Above relation holds in a distributional sense for  $x \in \mathbb{R}$ .

01.06.23.0020.01

$$\sum_{k=1}^{\infty} k \sin(kx) = -\frac{1}{2} \frac{\partial \operatorname{DiracComb}\left(\frac{x}{2\pi}\right)}{\partial x} \quad ; x \in \mathbb{R}$$

Above relation holds in a distributional sense for  $x \in \mathbb{R}$ .

01.06.23.0021.01

$$\sum_{k=1}^{\infty} k^{2m+1} \sin(kx) = \frac{1}{2} (-1)^{m-1} \frac{\partial^{2m+1} \operatorname{DiracComb}\left(\frac{x}{2\pi}\right)}{\partial x^{2m+1}} \quad ; x \in \mathbb{R} \wedge m \in \mathbb{N}$$

Above relation holds in a distributional sense for  $x \in \mathbb{R}$ .

01.06.23.0022.01

$$\sum_{k=1}^{\infty} k^{2m} \sin(kx) = -\frac{\delta_m i}{2} + \frac{1}{2} \left( \cot\left(\frac{z}{2}\right) + i \right) \sum_{k=0}^{2m} \frac{(-1)^k k!}{2^k} \mathcal{S}_{2m}^{(k)} \left( i \cot\left(\frac{z}{2}\right) + 1 \right)^k ; x \in \mathbb{R} \wedge m \in \mathbb{N}$$

Above relation holds in a distributional sense for  $x \in \mathbb{R}$ .

## Products

### Finite products

01.06.24.0001.01

$$\prod_{k=1}^{n-1} \sin\left(\frac{k\pi}{n}\right) = \frac{n}{2^{n-1}} ; n \in \mathbb{N}^+$$

01.06.24.0002.01

$$\prod_{k=1}^{n-1} \sin\left(\frac{\pi k}{n} + z\right) = \frac{2^{1-n} \sin(nz)}{\sin(z)} ; n \in \mathbb{N}^+$$

01.06.24.0003.01

$$\prod_{k=1}^{n-1} \sin\left(\frac{2\pi k}{n} + z\right) = (-2)^{1-n} \csc(z) \left( \cos\left(nz - \frac{\pi n}{2}\right) - \cos\left(\frac{n\pi}{2}\right) \right) ; n \in \mathbb{N}^+$$

01.06.24.0004.01

$$\prod_{k=1}^{\lfloor \frac{n-1}{2} \rfloor} \sin\left(\frac{\pi k}{n}\right) = 2^{\frac{1-n}{2}} \sqrt{n} ; n \in \mathbb{N}^+$$

01.06.24.0005.01

$$\prod_{k=1}^{\lfloor \frac{n-1}{2} \rfloor} \sin\left(\frac{(2k+1)\pi}{2n}\right) = 2^{\frac{1-n}{2}} \csc\left(\frac{\pi}{2n}\right) ; n \in \mathbb{N}^+$$

### Infinite products

01.06.24.0006.01

$$\prod_{k=1}^{\infty} \left( 1 - \frac{4}{3} \sin^2\left(\frac{z}{3^k}\right) \right) = \frac{\sin(z)}{z}$$

## Representations through more general functions

### Through hypergeometric functions

#### Involving ${}_0F_1$

01.06.26.0001.01

$$\sin(z) = z {}_0F_1\left(\frac{3}{2}; -\frac{z^2}{4}\right)$$

01.06.26.0002.01

$$\sin(z) = {}_0F_1\left(\frac{1}{2}; -\frac{1}{4}\left(z - \frac{\pi}{2}\right)^2\right)$$

01.06.26.0004.01

$$\sin^2(z) = \frac{1}{2} {}_0F_1\left(\frac{1}{2}; -\left(z - \frac{\pi}{2}\right)^2\right) + \frac{1}{2}$$

01.06.26.0005.01

$$\sin^3(z) = \frac{3}{4} {}_0F_1\left(\frac{1}{2}; -\frac{1}{4}\left(z - \frac{\pi}{2}\right)^2\right) + \frac{1}{4} {}_0F_1\left(\frac{1}{2}; -\frac{9}{4}\left(z - \frac{\pi}{2}\right)^2\right)$$

**Involving  ${}_pF_q$**

01.06.26.0101.01

$$\sin(z) = z {}_3F_2\left(\frac{z}{\pi}, \frac{z}{\pi}, \frac{z}{\pi}; 1, 1; -1\right) - \frac{2z^3}{\pi^2} {}_3F_2\left(\frac{z}{\pi} + 1, \frac{z}{\pi} + 1, \frac{z}{\pi} + 1; 2, 2; -1\right)$$

Brychkov Yu.A. (2005)

01.06.26.0003.01

$$\sin^2(z) = z^2 {}_1F_2\left(1; 2, \frac{3}{2}; -z^2\right)$$

**Through Meijer G**

**Classical cases for the direct function itself**

01.06.26.0006.01

$$\sin(z) = \frac{\sqrt{\pi}}{2} z G_{0,2}^{1,0}\left(\frac{z^2}{4} \middle| 0, -\frac{1}{2}\right)$$

01.06.26.0007.01

$$\sin(z) = \frac{\sqrt{\pi} z^2}{z} G_{0,2}^{1,0}\left(\frac{z^2}{4} \middle| \frac{1}{2}, 0\right)$$

01.06.26.0008.01

$$\sin(z) = \sqrt{\pi} G_{0,2}^{1,0}\left(\frac{z^2}{4} \middle| \frac{1}{2}, 0\right); \operatorname{Re}(z) > 0$$

01.06.26.0009.01

$$\sin\left(a + \sqrt{z}\right) = \sqrt{\pi} G_{1,3}^{2,0}\left(\frac{z}{4} \middle| 0, \frac{1}{2}, \frac{a}{\pi}\right)$$

**Classical cases for powers of sin**

01.06.26.0010.01

$$\sin^n(\sqrt{z}) = 2^{-n-1} ((-1)^n + 1) \binom{n}{\frac{n}{2}} + 2^{1-n} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^{\lfloor \frac{n}{2} \rfloor - k} \binom{n}{k} G_{0,2}^{1,0}\left(\frac{1}{4} z (n-2k)^2 \middle| \frac{1}{4} (1 - (-1)^n), \frac{1}{4} (1 + (-1)^n)\right); n \in \mathbb{N}^+$$

**Classical cases involving exp**

01.06.26.0095.01

$$e^{-\frac{\sqrt[3]{z}}{\sqrt{3}}} \sin(\sqrt[3]{z}) = \frac{1}{2} \sqrt{3} G_{0,3}^{2,0} \left( \frac{8z}{81\sqrt{3}} \left| \begin{matrix} \frac{1}{3}, \frac{2}{3}, 0 \end{matrix} \right. \right)$$

01.06.26.0102.01

$$e^{-\sqrt[4]{z}} \sin(\sqrt[4]{z}) = \frac{1}{\sqrt{2\pi}} G_{0,4}^{3,0} \left( \frac{z}{64} \left| \begin{matrix} \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 0 \end{matrix} \right. \right)$$

01.06.26.0096.01

$$e^{-\sqrt[6]{z}} \sin(\sqrt[6]{z}) = \frac{\sqrt{3}}{4\pi^{3/2}} G_{0,6}^{5,0} \left( \frac{z}{729} \left| \begin{matrix} \frac{1}{6}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{5}{6}, 0 \end{matrix} \right. \right)$$

**Classical cases involving sinh**

01.06.26.0097.01

$$\sin(\sqrt[4]{z}) \sinh(\sqrt[4]{z}) = \sqrt{2} \pi^{3/2} G_{0,4}^{1,0} \left( \frac{z}{64} \left| \begin{matrix} \frac{1}{2}, 0, \frac{1}{4}, \frac{3}{4} \end{matrix} \right. \right)$$

**Classical cases involving cosh**

01.06.26.0098.01

$$\sin(\sqrt[4]{z}) \cosh(\sqrt[4]{z}) = \sqrt{2} \pi^{3/2} G_{1,5}^{2,0} \left( \frac{z}{64} \left| \begin{matrix} \frac{1}{2} \\ \frac{1}{4}, \frac{3}{4}, 0, \frac{1}{2}, \frac{1}{2} \end{matrix} \right. \right)$$

**Classical cases involving cos, Ci, Si**

01.06.26.0011.01

$$\cos(\sqrt{z}) \text{Ci}(\sqrt{z}) + \sin(\sqrt{z}) \text{Si}(\sqrt{z}) = -\frac{1}{2} \pi^{3/2} G_{2,4}^{2,1} \left( \frac{z}{4} \left| \begin{matrix} 0, \frac{1}{2} \\ 0, 0, \frac{1}{2}, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0012.01

$$\cos(\sqrt{z}) \text{Ci}(\sqrt{z}) + \sin(\sqrt{z}) \left( \text{Si}(\sqrt{z}) - \frac{\pi}{2} \right) = -\frac{1}{2\sqrt{\pi}} G_{1,3}^{3,1} \left( \frac{z}{4} \left| \begin{matrix} 0 \\ 0, 0, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0013.01

$$\sin(\sqrt{z}) \text{Ci}(\sqrt{z}) - \cos(\sqrt{z}) \text{Si}(\sqrt{z}) = -\frac{1}{2} \pi^{3/2} G_{2,4}^{2,1} \left( \frac{z}{4} \left| \begin{matrix} \frac{1}{2}, 1 \\ \frac{1}{2}, \frac{1}{2}, 1, 0 \end{matrix} \right. \right)$$

01.06.26.0014.01

$$\sin(\sqrt{z}) \text{Ci}(\sqrt{z}) - \cos(\sqrt{z}) \left( \text{Si}(\sqrt{z}) - \frac{\pi}{2} \right) = \frac{1}{2\sqrt{\pi}} G_{1,3}^{3,1} \left( \frac{z}{4} \left| \begin{matrix} \frac{1}{2} \\ 0, \frac{1}{2}, \frac{1}{2} \end{matrix} \right. \right)$$

**Classical cases involving  $\cos^{-1}$  in the arguments and unit step  $\theta$**

01.06.26.0015.01

$$\theta(1 - |z|) \sin\left(\nu \cos^{-1}(\sqrt{z})\right) = \frac{\sqrt{\pi} \nu}{2} G_{2,2}^{2,0} \left( z \left| \begin{matrix} 1 - \frac{\nu}{2}, \frac{\nu+2}{2} \\ 0, \frac{1}{2} \end{matrix} \right. \right) /; z \notin (-1, 0)$$

**Classical cases involving  $\tan^{-1}$  in the arguments**

01.06.26.0016.01

$$(z+1)^{\nu/2} \sin\left(\nu \tan^{-1}(\sqrt{z})\right) = -\frac{2^{-\nu-1}}{\Gamma(-\nu)} G_{2,2}^{1,2}\left(z \left| \begin{matrix} \frac{\nu}{2} + 1, \frac{\nu+1}{2} \\ \frac{1}{2}, 0 \end{matrix} \right. \right)$$

**Classical cases involving  $\cot^{-1}$  in the arguments**

01.06.26.0017.01

$$(z+1)^{\nu/2} \sin\left(\nu \cot^{-1}(\sqrt{z})\right) = -\frac{2^{-\nu-1}}{\Gamma(-\nu)} G_{2,2}^{2,1}\left(z \left| \begin{matrix} \frac{\nu+1}{2}, \frac{\nu}{2} + 1 \\ 0, \frac{1}{2} \end{matrix} \right. \right); z \notin (-1, 0)$$

**Classical cases involving  $\sec^{-1}$  in the arguments and unit step  $\theta$**

01.06.26.0018.01

$$\theta(|z|-1) \sin\left(\nu \sec^{-1}(\sqrt{z})\right) = \frac{\sqrt{\pi} \nu}{2} G_{2,2}^{0,2}\left(z \left| \begin{matrix} \frac{1}{2}, 1 \\ -\frac{\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

**Classical cases involving Bessel  $J$**

01.06.26.0019.01

$$\sin(\sqrt{z}) J_{\nu}(\sqrt{z}) = \frac{1}{\sqrt{2}} G_{2,4}^{1,2}\left(z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{\nu+1}{2}, -\frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0020.01

$$\sin\left(a + \sqrt{z}\right) J_{\nu}(\sqrt{z}) = \frac{1}{\sqrt{2}} G_{3,5}^{2,2}\left(z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, \frac{a}{\pi} + \frac{\nu}{2} \\ \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2}, \frac{1-\nu}{2}, \frac{a}{\pi} + \frac{\nu}{2} \end{matrix} \right. \right)$$

**Classical cases involving cos and Bessel  $J$**

01.06.26.0021.01

$$\cos(\sqrt{z}) J_{-\nu}(\sqrt{z}) + \sin(\sqrt{z}) J_{\nu}(\sqrt{z}) = -\sqrt{2} \sin\left(\frac{1}{4} (2\nu - 1)\pi\right) G_{2,4}^{2,1}\left(z \left| \begin{matrix} \frac{3}{4}, \frac{1}{4} \\ -\frac{\nu}{2}, \frac{\nu+1}{2}, \frac{\nu}{2}, \frac{1-\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0022.01

$$\cos(\sqrt{z}) J_{-\nu}(\sqrt{z}) - \sin(\sqrt{z}) J_{\nu}(\sqrt{z}) = \sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu + 1)\right) G_{2,4}^{2,1}\left(z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ -\frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0103.01

$$J_{\nu}(\sqrt{z}) \cos(\sqrt{z}) + J_{-\nu}(\sqrt{z}) \sin(\sqrt{z}) = \sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu + 1)\right) G_{2,4}^{2,1}\left(z \left| \begin{matrix} \frac{3}{4}, \frac{1}{4} \\ \frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0104.01

$$\sin(\sqrt{z}) J_{-\nu}(\sqrt{z}) - \cos(\sqrt{z}) J_{\nu}(\sqrt{z}) = \sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu - 1)\right) G_{2,4}^{2,1}\left(z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

**Classical cases involving Bessel  $Y$**

01.06.26.0023.01

$$\sin(\sqrt{z}) Y_\nu(\sqrt{z}) = \frac{1}{\sqrt{2}} G_{3,5}^{2,2} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, -\frac{\nu}{2} \\ \frac{\nu+1}{2}, \frac{1-\nu}{2}, -\frac{\nu}{2}, -\frac{\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

**Classical cases involving cos and Bessel J, Y**

01.06.26.0024.01

$$\cos(\sqrt{z}) Y_\nu(\sqrt{z}) + \sin(\sqrt{z}) J_\nu(\sqrt{z}) = -\sqrt{2} G_{2,4}^{3,0} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0025.01

$$\sin(\sqrt{z}) Y_\nu(\sqrt{z}) - \cos(\sqrt{z}) J_\nu(\sqrt{z}) = -\sqrt{2} G_{2,4}^{3,0} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{1-\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0026.01

$$\cos(\sqrt{z}) Y_\nu(\sqrt{z}) - \sin(\sqrt{z}) J_\nu(\sqrt{z}) = -\frac{\cos(\nu\pi)}{\pi^2 \sqrt{2}} G_{2,4}^{3,2} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0027.01

$$\sin(\sqrt{z}) Y_\nu(\sqrt{z}) + \cos(\sqrt{z}) J_\nu(\sqrt{z}) = \frac{\cos(\nu\pi)}{\pi^2 \sqrt{2}} G_{2,4}^{3,2} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{1-\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0028.01

$$\sin(a + \sqrt{z}) J_\nu(\sqrt{z}) - \cos(a + \sqrt{z}) Y_\nu(\sqrt{z}) = \frac{\cos(\pi\nu)}{\pi^2 \sqrt{2}} G_{3,5}^{4,2} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, \frac{1-\nu}{2} - \frac{a}{\pi} \\ -\frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2} - \frac{a}{\pi} \end{matrix} \right. \right)$$

01.06.26.0105.01

$$\cos(a + \sqrt{z}) J_\nu(\sqrt{z}) + \sin(a + \sqrt{z}) Y_\nu(\sqrt{z}) = \frac{\cos(\pi\nu)}{\sqrt{2} \pi^2} G_{3,5}^{4,2} \left( z \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, -\frac{a}{\pi} - \frac{\nu}{2} \\ \frac{1-\nu}{2}, -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{a}{\pi} - \frac{\nu}{2} \end{matrix} \right. \right)$$

**Classical cases involving  ${}_0F_1$**

01.06.26.0029.01

$$\sin(z) {}_0F_1 \left( ; b; -\frac{z^2}{4} \right) = 2^{b-\frac{3}{2}} \Gamma(b) G_{2,4}^{1,2} \left( z^2 \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4} \\ \frac{1}{2}, 0, 1-b, \frac{3}{2}-b \end{matrix} \right. \right); -\frac{\pi}{2} < \arg(z) \leq \frac{\pi}{2}$$

01.06.26.0106.01

$$\sin(z) {}_0F_1 \left( ; b; -\frac{z^2}{4} \right) = \frac{2^{b-\frac{3}{2}} \Gamma(b)}{z} G_{2,4}^{1,2} \left( z^2 \left| \begin{matrix} \frac{5}{4} - \frac{b}{2}, \frac{7}{4} - \frac{b}{2} \\ 1, \frac{1}{2}, \frac{3}{2} - b, 2 - b \end{matrix} \right. \right)$$

01.06.26.0031.01

$$\sin(a + z) {}_0F_1 \left( ; b; -\frac{z^2}{4} \right) = -2^{b-\frac{3}{2}} \Gamma(b) G_{3,5}^{2,2} \left( z^2 \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4}, \frac{a}{\pi} + 1 \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b, \frac{a}{\pi} + 1 \end{matrix} \right. \right); -\frac{\pi}{2} < \arg(z) \leq \frac{\pi}{2}$$

01.06.26.0107.01

$$\sin(a+z) {}_0F_1\left(; b; -\frac{z^2}{4}\right) = 2^{b-\frac{3}{2}} \Gamma(b) \left( \frac{\cos(a)}{z} G_{2,4}^{1,2}\left(z^2 \left| \begin{matrix} \frac{5}{4} - \frac{b}{2}, \frac{7}{4} - \frac{b}{2} \\ 1, \frac{1}{2}, \frac{3}{2} - b, 2 - b \end{matrix} \right. \right) + \sin(a) G_{2,4}^{1,2}\left(z^2 \left| \begin{matrix} \frac{1}{4}(3-2b), \frac{1}{4}(5-2b) \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b \end{matrix} \right. \right) \right)$$

01.06.26.0030.01

$$\sin(2\sqrt{z}) {}_0F_1(; b; -z) = 2^{b-\frac{3}{2}} \Gamma(b) G_{2,4}^{1,2}\left(4z \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4} \\ \frac{1}{2}, 0, 1-b, \frac{3}{2}-b \end{matrix} \right. \right)$$

01.06.26.0032.01

$$\sin(a+2\sqrt{z}) {}_0F_1(; b; -z) = -2^{b-\frac{3}{2}} \Gamma(b) G_{3,5}^{2,2}\left(4z \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4}, \frac{a}{\pi} + 1 \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b, \frac{a}{\pi} + 1 \end{matrix} \right. \right)$$

**Classical cases involving  ${}_0\tilde{F}_1$**

01.06.26.0033.01

$$\sin(z) {}_0\tilde{F}_1\left(; b; -\frac{z^2}{4}\right) = 2^{b-\frac{3}{2}} G_{2,4}^{1,2}\left(z^2 \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4} \\ \frac{1}{2}, 0, 1-b, \frac{3}{2}-b \end{matrix} \right. \right) /; -\frac{\pi}{2} < \arg(z) \leq \frac{\pi}{2}$$

01.06.26.0108.01

$$\sin(z) {}_0\tilde{F}_1\left(; b; -\frac{z^2}{4}\right) = \frac{2^{b-\frac{3}{2}}}{z} G_{2,4}^{1,2}\left(z^2 \left| \begin{matrix} \frac{5}{4} - \frac{b}{2}, \frac{7}{4} - \frac{b}{2} \\ 1, \frac{1}{2}, \frac{3}{2} - b, 2 - b \end{matrix} \right. \right)$$

01.06.26.0035.01

$$\sin(a+z) {}_0\tilde{F}_1\left(; b; -\frac{z^2}{4}\right) = -2^{b-\frac{3}{2}} G_{3,5}^{2,2}\left(z^2 \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4}, \frac{a}{\pi} + 1 \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b, \frac{a}{\pi} + 1 \end{matrix} \right. \right) /; -\frac{\pi}{2} < \arg[z] \leq \frac{\pi}{2}$$

01.06.26.0109.01

$$\sin(a+z) {}_0\tilde{F}_1\left(; b; -\frac{z^2}{4}\right) = 2^{b-\frac{3}{2}} \left( \frac{\cos(a)}{z} G_{2,4}^{1,2}\left(z^2 \left| \begin{matrix} \frac{5}{4} - \frac{b}{2}, \frac{7}{4} - \frac{b}{2} \\ 1, \frac{1}{2}, \frac{3}{2} - b, 2 - b \end{matrix} \right. \right) + \sin(a) G_{2,4}^{1,2}\left(z^2 \left| \begin{matrix} \frac{1}{4}(3-2b), \frac{1}{4}(5-2b) \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b \end{matrix} \right. \right) \right)$$

01.06.26.0034.01

$$\sin(2\sqrt{z}) {}_0\tilde{F}_1(; b; -z) = 2^{b-\frac{3}{2}} G_{2,4}^{1,2}\left(4z \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4} \\ \frac{1}{2}, 0, 1-b, \frac{3}{2}-b \end{matrix} \right. \right)$$

01.06.26.0036.01

$$\sin(a+2\sqrt{z}) {}_0\tilde{F}_1(; b; -z) = -2^{b-\frac{3}{2}} G_{3,5}^{2,2}\left(4z \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4}, \frac{a}{\pi} + 1 \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b, \frac{a}{\pi} + 1 \end{matrix} \right. \right)$$

**Generalized cases for the direct function itself**

01.06.26.0037.01

$$\sin(z) = \sqrt{\pi} G_{0,2}^{1,0}\left(\frac{z}{2}, \frac{1}{2} \left| \frac{1}{2}, 0\right.\right)$$

01.06.26.0038.01

$$\sin(a+z) = \sqrt{\pi} G_{1,3}^{2,0}\left(\frac{z}{2}, \frac{1}{2} \left| \begin{matrix} \frac{a}{\pi} \\ 0, \frac{1}{2}, \frac{a}{\pi} \end{matrix} \right.\right)$$



**Generalized cases for powers of sin**

01.06.26.0039.01

$$\sin^n(z) = 2^{-n-1} ((-1)^n + 1) \binom{n}{\frac{n}{2}} + 2^{1-n} \sqrt{\pi} \sum_{k=0}^{\lfloor \frac{n-1}{2} \rfloor} (-1)^{\lfloor \frac{n}{2} \rfloor - k} \binom{n}{k} G_{0,2}^{1,0} \left( \frac{1}{2} z (n - 2k), \frac{1}{2} \left| \frac{1}{4} (1 - (-1)^n), \frac{1}{4} (1 + (-1)^n) \right. \right); n \in \mathbb{N}^+$$

01.06.26.0099.01

$$\sin^{2n}(z) = \sqrt{\pi} 2^{1-2n} \sum_{k=0}^{n-1} (-1)^{-k+n-1} \binom{2n}{k} G_{1,3}^{1,1} \left( (n-k)z, \frac{1}{2} \left| 1, 0, \frac{1}{2} \right. \right); n \in \mathbb{N}^+$$

**Generalized cases involving exp**

01.06.26.0040.01

$$e^{-z} \sin(z) = \frac{1}{\sqrt{2\pi}} G_{0,4}^{3,0} \left( \frac{z}{2\sqrt{2}}, \frac{1}{4} \left| \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 0 \right. \right)$$

01.06.26.0041.01

$$e^{-\frac{z}{\sqrt{3}}} \sin(z) = \frac{1}{2} \sqrt{3} G_{0,3}^{2,0} \left( \frac{2z}{3\sqrt{3}}, \frac{1}{3} \left| \frac{1}{3}, \frac{2}{3}, 0 \right. \right)$$

01.06.26.0042.01

$$e^{-\sqrt{3}z} \sin(z) = \frac{\sqrt{3}}{4\pi^{3/2}} G_{0,6}^{5,0} \left( \frac{z}{3}, \frac{1}{6} \left| \frac{1}{6}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{5}{6}, 0 \right. \right)$$

**Generalized cases involving cosh**

01.06.26.0043.01

$$\sin(z) \cosh(z) = \sqrt{2} \pi^{3/2} G_{1,5}^{2,0} \left( \frac{z}{2\sqrt{2}}, \frac{1}{4} \left| \frac{1}{4}, \frac{3}{4}, 0, \frac{1}{2}, \frac{1}{2} \right. \right)$$

**Generalized cases involving sinh**

01.06.26.0044.01

$$\sin(z) \sinh(z) = \sqrt{2} \pi^{3/2} G_{0,4}^{1,0} \left( \frac{z}{2\sqrt{2}}, \frac{1}{4} \left| \frac{1}{2}, 0, \frac{1}{4}, \frac{3}{4} \right. \right)$$

**Generalized cases involving cos, Ci, Si**

01.06.26.0045.01

$$\cos(z) \text{Ci}(z) + \sin(z) \text{Si}(z) = -\frac{1}{2} \pi^{3/2} G_{2,4}^{2,1} \left( \frac{z}{2}, \frac{1}{2} \left| 0, \frac{1}{2} \right. \right)$$

01.06.26.0046.01

$$\cos(z) \text{Ci}(z) + \sin(z) \left( \text{Si}(z) - \frac{\pi}{2} \right) = -\frac{1}{2\sqrt{\pi}} G_{1,3}^{3,1} \left( \frac{z}{2}, \frac{1}{2} \left| 0, 0, \frac{1}{2} \right. \right)$$

01.06.26.0047.01

$$\sin(z) \text{Ci}(z) - \cos(z) \text{Si}(z) = -\frac{1}{2} \pi^{3/2} G_{2,4}^{2,1} \left( \frac{z}{2}, \frac{1}{2} \left| \frac{1}{2}, 1 \right. \right)$$

01.06.26.0048.01

$$\sin(z) \operatorname{Ci}(z) - \cos(z) \left( \operatorname{Si}(z) - \frac{\pi}{2} \right) = \frac{1}{2\sqrt{\pi}} G_{1,3}^{3,1} \left( \frac{z}{2}, \frac{1}{2} \left| \begin{matrix} \frac{1}{2} \\ 0, \frac{1}{2}, \frac{1}{2} \end{matrix} \right. \right)$$

**Generalized cases involving cos and Fresnel C, S**

01.06.26.0049.01

$$\cos(z) C \left( \sqrt{\frac{2z}{\pi}} \right) + \sin(z) S \left( \sqrt{\frac{2z}{\pi}} \right) = \sqrt{\frac{\pi}{2}} G_{1,3}^{1,1} \left( \frac{z}{2}, \frac{1}{2} \left| \begin{matrix} \frac{1}{4} \\ \frac{1}{4}, 0, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0050.01

$$\cos(z) S \left( \sqrt{\frac{2z}{\pi}} \right) - \sin(z) C \left( \sqrt{\frac{2z}{\pi}} \right) = -\sqrt{\frac{\pi}{2}} G_{1,3}^{1,1} \left( \frac{z}{2}, \frac{1}{2} \left| \begin{matrix} \frac{3}{4} \\ \frac{3}{4}, 0, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0051.01

$$\cos(z) \left( \frac{1}{2} - C \left( \sqrt{\frac{2z}{\pi}} \right) \right) + \sin(z) \left( \frac{1}{2} - S \left( \sqrt{\frac{2z}{\pi}} \right) \right) = (2\pi)^{-3/2} G_{1,3}^{3,1} \left( \frac{z}{2}, \frac{1}{2} \left| \begin{matrix} \frac{1}{4} \\ 0, \frac{1}{4}, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0052.01

$$\cos(z) \left( \frac{1}{2} - S \left( \sqrt{\frac{2z}{\pi}} \right) \right) - \sin(z) \left( \frac{1}{2} - C \left( \sqrt{\frac{2z}{\pi}} \right) \right) = (2\pi)^{-3/2} G_{1,3}^{3,1} \left( \frac{z}{2}, \frac{1}{2} \left| \begin{matrix} \frac{3}{4} \\ 0, \frac{1}{2}, \frac{3}{4} \end{matrix} \right. \right)$$

01.06.26.0110.01

$$\cos \left( \frac{\pi z^2}{2} \right) C(z) + \sin \left( \frac{\pi z^2}{2} \right) S(z) = \sqrt{\frac{\pi}{2}} G_{1,3}^{1,1} \left( \frac{\sqrt{\pi} z}{2}, \frac{1}{4} \left| \begin{matrix} \frac{1}{4} \\ \frac{1}{4}, 0, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0111.01

$$\cos \left( \frac{\pi z^2}{2} \right) S(z) - \sin \left( \frac{\pi z^2}{2} \right) C(z) = -\sqrt{\frac{\pi}{2}} G_{1,3}^{1,1} \left( \frac{\sqrt{\pi} z}{2}, \frac{1}{4} \left| \begin{matrix} \frac{3}{4} \\ \frac{3}{4}, 0, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0112.01

$$\cos \left( \frac{\pi z^2}{2} \right) \left( \frac{1}{2} - C(z) \right) + \sin \left( \frac{\pi z^2}{2} \right) \left( \frac{1}{2} - S(z) \right) = (2\pi)^{-3/2} G_{1,3}^{3,1} \left( \frac{\sqrt{\pi} z}{2}, \frac{1}{4} \left| \begin{matrix} \frac{1}{4} \\ 0, \frac{1}{4}, \frac{1}{2} \end{matrix} \right. \right)$$

01.06.26.0113.01

$$\cos \left( \frac{\pi z^2}{2} \right) \left( \frac{1}{2} - C(z) \right) - \sin \left( \frac{\pi z^2}{2} \right) \left( \frac{1}{2} - S(z) \right) = (2\pi)^{-3/2} G_{1,3}^{3,1} \left( \frac{\sqrt{\pi} z}{2}, \frac{1}{4} \left| \begin{matrix} \frac{3}{4} \\ 0, \frac{1}{2}, \frac{3}{4} \end{matrix} \right. \right)$$

**Generalized cases involving  $\cos^{-1}$  in the arguments and unit step  $\theta$**

01.06.26.0053.01

$$\theta(1 - |z|) \sin(\nu \cos^{-1}(z)) = \frac{\sqrt{\pi} \nu}{2} G_{2,2}^{2,0} \left( z, \frac{1}{2} \left| \begin{matrix} 1 - \frac{\nu}{2}, \frac{\nu+2}{2} \\ 0, \frac{1}{2} \end{matrix} \right. \right)$$

**Generalized cases involving  $\tan^{-1}$  in the arguments**

01.06.26.0054.01

$$(z^2 + 1)^{\nu/2} \sin(\nu \tan^{-1}(z)) = -\frac{2^{-\nu-1}}{\Gamma(-\nu)} G_{2,2}^{1,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{\nu}{2} + 1, \frac{\nu+1}{2} \\ \frac{1}{2}, 0 \end{matrix} \right. \right)$$

**Generalized cases involving  $\cot^{-1}$  in the arguments**

01.06.26.0055.01

$$(z^2 + 1)^{\nu/2} \sin(\nu \cot^{-1}(z)) = -\frac{2^{-\nu-1}}{\Gamma(-\nu)} G_{2,2}^{0,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{\nu+1}{2}, \frac{\nu}{2} + 1 \\ 0, \frac{1}{2} \end{matrix} \right. \right) /; \operatorname{Re}(z) > 0$$

**Generalized cases involving  $\sec^{-1}$  in the arguments and unit step  $\theta$**

01.06.26.0056.01

$$\theta(|z| - 1) \sin(\nu \sec^{-1}(z)) = \frac{\sqrt{\pi} \nu}{2} G_{2,2}^{0,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{2}, 1 \\ -\frac{\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

**Generalized cases involving Bessel  $J$**

01.06.26.0057.01

$$\sin(z) J_\nu(z) = \frac{1}{\sqrt{2}} G_{2,4}^{1,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{\nu+1}{2}, -\frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0058.01

$$\sin(a+z) J_\nu(z) = \frac{1}{\sqrt{2}} G_{3,5}^{2,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, \frac{a}{\pi} + \frac{\nu}{2} \\ \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2}, \frac{1-\nu}{2}, \frac{a}{\pi} + \frac{\nu}{2} \end{matrix} \right. \right)$$

**Generalized cases involving cos and Bessel  $J$**

01.06.26.0059.01

$$\cos(z) J_{-\nu}(z) + \sin(z) J_\nu(z) = -\sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu - 1)\right) G_{2,4}^{2,1} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{3}{4}, \frac{1}{4} \\ -\frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0060.01

$$\cos(z) J_{-\nu}(z) - \sin(z) J_\nu(z) = \sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu + 1)\right) G_{2,4}^{2,1} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ -\frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0114.01

$$\sin(z) J_{-\nu}(z) + \cos(z) J_\nu(z) = \sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu + 1)\right) G_{2,4}^{2,1} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{3}{4}, \frac{1}{4} \\ \frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0115.01

$$\sin(z) J_{-\nu}(z) - \cos(z) J_\nu(z) = \sqrt{2} \sin\left(\frac{1}{4} \pi (2\nu - 1)\right) G_{2,4}^{2,1} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

**Generalized cases involving Bessel  $Y$**

01.06.26.0061.01

$$\sin(z) Y_\nu(z) = \frac{1}{\sqrt{2}} G_{3,5}^{2,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, -\frac{\nu}{2} \\ \frac{\nu+1}{2}, \frac{1-\nu}{2}, -\frac{\nu}{2}, -\frac{\nu}{2}, \frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0100.01

$$\sin(a+z) Y_\nu(z) = \frac{\cos(\pi\nu)}{\sqrt{2} \pi^2} G_{3,5}^{4,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, -\frac{a}{\pi} - \frac{\nu}{2} \\ \frac{1-\nu}{2}, -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{a}{\pi} - \frac{\nu}{2} \end{matrix} \right. \right) - \frac{1}{\sqrt{2}} G_{3,5}^{2,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, \frac{1}{2} \left( \frac{2a}{\pi} + \nu + 1 \right) \\ \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2}, -\frac{\nu}{2}, \frac{1}{2} \left( \frac{2a}{\pi} + \nu + 1 \right) \end{matrix} \right. \right)$$

**Generalized cases involving cos and Bessel J, Y**

01.06.26.0062.01

$$\sin(z) J_\nu(z) + \cos(z) Y_\nu(z) = -\sqrt{2} G_{2,4}^{3,0} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0063.01

$$\cos(z) J_\nu(z) - \sin(z) Y_\nu(z) = \sqrt{2} G_{2,4}^{3,0} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{1-\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0064.01

$$\sin(z) J_\nu(z) - \cos(z) Y_\nu(z) = \frac{\cos(\nu\pi)}{\pi^2 \sqrt{2}} G_{2,4}^{3,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0065.01

$$\cos(z) J_\nu(z) + \sin(z) Y_\nu(z) = \frac{\cos(\nu\pi)}{\pi^2 \sqrt{2}} G_{2,4}^{3,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4} \\ \frac{1-\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{\nu}{2} \end{matrix} \right. \right)$$

01.06.26.0066.01

$$\sin(a+z) J_\nu(z) - \cos(a+z) Y_\nu(z) = \frac{\cos(\pi\nu)}{\pi^2 \sqrt{2}} G_{3,5}^{4,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, \frac{1-\nu}{2} - \frac{a}{\pi} \\ -\frac{\nu}{2}, \frac{1-\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, \frac{1-\nu}{2} - \frac{a}{\pi} \end{matrix} \right. \right)$$

01.06.26.0116.01

$$\cos(a+z) J_\nu(z) + \sin(a+z) Y_\nu(z) = \frac{\cos(\pi\nu)}{\sqrt{2} \pi^2} G_{3,5}^{4,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}, \frac{3}{4}, -\frac{a}{\pi} - \frac{\nu}{2} \\ \frac{1-\nu}{2}, -\frac{\nu}{2}, \frac{\nu}{2}, \frac{\nu+1}{2}, -\frac{a}{\pi} - \frac{\nu}{2} \end{matrix} \right. \right)$$

**Generalized cases involving  ${}_0F_1$**

01.06.26.0117.01

$$\sin(z) {}_0F_1 \left( ; b; -\frac{z^2}{4} \right) = 2^{b-\frac{3}{2}} \Gamma(b) G_{2,4}^{1,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{3-2b}{4}, \frac{5-2b}{4} \\ \frac{1}{2}, 0, 1-b, \frac{3}{2}-b \end{matrix} \right. \right)$$

01.06.26.0118.01

$$\sin(a+z) {}_0F_1 \left( ; b; -\frac{z^2}{4} \right) = 2^{b-\frac{3}{2}} \Gamma(b) G_{3,5}^{2,2} \left( z, \frac{1}{2} \left| \begin{matrix} \frac{3}{4} - \frac{b}{2}, \frac{5}{4} - \frac{b}{2}, \frac{a}{\pi} \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b, \frac{a}{\pi} \end{matrix} \right. \right)$$

**Generalized cases involving  ${}_0\tilde{F}_1$**

01.06.26.0119.01

$$\sin(z) {}_0\tilde{F}_1\left(; b; -\frac{z^2}{4}\right) = 2^{b-\frac{3}{2}} G_{2,4}^{1,2}\left(z, \frac{1}{2} \left| \begin{matrix} \frac{1}{4}(3-2b), \frac{1}{4}(5-2b) \\ \frac{1}{2}, 0, 1-b, \frac{3}{2}-b \end{matrix} \right. \right)$$

01.06.26.0120.01

$$\sin(a+z) {}_0\tilde{F}_1\left(; b; -\frac{z^2}{4}\right) = 2^{b-\frac{3}{2}} G_{3,5}^{2,2}\left(z, \frac{1}{2} \left| \begin{matrix} \frac{3}{4}-\frac{b}{2}, \frac{5}{4}-\frac{b}{2}, \frac{a}{\pi} \\ 0, \frac{1}{2}, 1-b, \frac{3}{2}-b, \frac{a}{\pi} \end{matrix} \right. \right)$$

## Through other functions

### Involving Bessel functions

01.06.26.0067.01

$$\sin(z) = \sqrt{\frac{\pi z}{2}} J_{\frac{1}{2}}(z)$$

01.06.26.0068.01

$$\sin(z) = -i \sqrt{\frac{\pi i z}{2}} I_{\frac{1}{2}}(i z)$$

01.06.26.0069.01

$$\sin(z) = \sqrt{\frac{\pi z}{2}} Y_{-\frac{1}{2}}(z)$$

01.06.26.0070.01

$$\sin(z) = \frac{i}{\sqrt{2\pi}} \left( \sqrt{i z} K_{\frac{1}{2}}(i z) - \sqrt{-i z} K_{\frac{1}{2}}(-i z) \right)$$

### Involving Jacobi functions

01.06.26.0071.01

$$\sin(z) = \operatorname{cd}\left(\frac{\pi}{2} - z \mid 0\right)$$

01.06.26.0072.01

$$\sin(z) = \operatorname{cn}\left(\frac{\pi}{2} - z \mid 0\right)$$

01.06.26.0073.01

$$\sin(z) = \frac{1}{\operatorname{cn}\left(\frac{\pi i}{2} - i z \mid 1\right)}$$

01.06.26.0074.01

$$\sin(z) = -\frac{i}{\operatorname{cs}(i z \mid 1)}$$

01.06.26.0075.01

$$\sin(z) = \frac{1}{\operatorname{dc}\left(\frac{\pi}{2} - z \mid 0\right)}$$

$$\sin(z) = \frac{1}{\operatorname{dn}\left(\frac{\pi i}{2} - iz \mid 1\right)}$$

$$\sin(z) = \frac{1}{\operatorname{ds}(z \mid 0)}$$

$$\sin(z) = -\frac{i}{\operatorname{ds}(iz \mid 1)}$$

$$\sin(z) = \frac{1}{\operatorname{nc}\left(\frac{\pi}{2} - z \mid 0\right)}$$

$$\sin(z) = \operatorname{nc}\left(\frac{\pi i}{2} - iz \mid 1\right)$$

$$\sin(z) = \operatorname{nd}\left(\frac{\pi i}{2} - iz \mid 1\right)$$

$$\sin(z) = \frac{1}{\operatorname{ns}(z \mid 0)}$$

$$\sin(z) = -i \operatorname{sc}(iz \mid 1)$$

$$\sin(z) = -i \operatorname{sd}(iz \mid 1)$$

$$\sin(z) = \operatorname{sd}(z \mid 0)$$

$$\sin(z) = \operatorname{sn}(z \mid 0)$$

### Involving Mathieu functions

$$\sin(\sqrt{a} z) = \operatorname{Se}(a, 0, z)$$

$$\sin(\sqrt{a} z) = -\frac{1}{\sqrt{a}} \operatorname{Ce}_z(a, 0, z)$$

### Involving some elliptic-type functions

$$\sin(z) = E(z \mid 1) \text{ ; } |\operatorname{Re}(z)| \leq \frac{\pi}{2}$$

01.06.26.0090.01

$$\sin(z) = \sqrt{\frac{3}{2}} e^{-\frac{z^2}{6}} \sigma\left(\sqrt{\frac{2}{3}} z; 3, 1\right)$$

**Involving some hypergeometric-type functions**

01.06.26.0091.01

$$\sin(\pi z) = \frac{\pi}{\Gamma(z)\Gamma(1-z)}$$

01.06.26.0092.01

$$\sin(z) = \sqrt{\frac{\pi z}{2}} H_{-\frac{1}{2}}(z)$$

01.06.26.0093.01

$$\sin(z) = -i \sqrt{\frac{\pi i z}{2}} L_{-\frac{1}{2}}(i z)$$

01.06.26.0094.01

$$\sin(n z) = \sin(z) U_{n-1}(\cos(z))$$

**Representations through equivalent functions**

**With inverse function**

01.06.27.0001.01

$$\sin(\sin^{-1}(z)) = z$$

01.06.27.0002.02

$$\sin^{-1}(\sin(z)) = z /; -\frac{\pi}{2} < \operatorname{Re}(z) < \frac{\pi}{2} \bigvee \operatorname{Re}(z) = -\frac{\pi}{2} \bigwedge \operatorname{Im}(z) \geq 0 \bigvee \operatorname{Re}(z) = \frac{\pi}{2} \bigwedge \operatorname{Im}(z) \leq 0$$

01.06.27.0065.01

$$\sin^{-1}(\sin(z)) = -z - \pi /; -\frac{3\pi}{2} < \operatorname{Re}(z) < -\frac{\pi}{2} \bigvee \operatorname{Re}(z) = -\frac{3\pi}{2} \bigwedge \operatorname{Im}(z) \geq 0 \bigvee \operatorname{Re}(z) = -\frac{\pi}{2} \bigwedge \operatorname{Im}(z) \leq 0$$

01.06.27.0066.01

$$\sin^{-1}(\sin(z)) = \pi - z /; \frac{\pi}{2} < \operatorname{Re}(z) < \frac{3\pi}{2} \bigvee \operatorname{Re}(z) = \frac{\pi}{2} \bigwedge \operatorname{Im}(z) \geq 0 \bigvee \operatorname{Re}(z) = \frac{3\pi}{2} \bigwedge \operatorname{Im}(z) \leq 0$$

01.06.27.0067.01

$$\sin^{-1}(\sin(z)) = (-1)^k (z - \pi k) /; \left(k\pi - \frac{\pi}{2} < \operatorname{Re}(z) < \pi k + \frac{\pi}{2} \bigvee \operatorname{Re}(z) = k\pi - \frac{\pi}{2} \bigwedge \operatorname{Im}(z) \geq 0 \bigvee \operatorname{Re}(z) = \pi k + \frac{\pi}{2} \bigwedge \operatorname{Im}(z) \leq 0\right) \bigwedge k \in \mathbb{Z}$$

01.06.27.0003.01

$$\sin^{-1}(\sin(z)) = (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} - \frac{1}{2} \rfloor} \left( \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} + \frac{1}{2} \rfloor - \lceil \frac{\operatorname{Re}(z)}{\pi} + \frac{1}{2} \rceil} \right) \theta(-\operatorname{Im}(z)) - 1 \right) \left( z - \pi \left\lfloor \frac{\operatorname{Re}(z)}{\pi} - \frac{1}{2} \right\rfloor + \frac{\pi}{2} \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} + \frac{1}{2} \rfloor - \lceil \frac{\operatorname{Re}(z)}{\pi} + \frac{1}{2} \rceil} \right) \theta(-\operatorname{Im}(z)) - \pi \right)$$

01.06.27.0068.01

$$\sin^{-1}(\sin(z)) = \begin{cases} (-1)^{\lfloor \frac{2\operatorname{Re}(z)+\pi}{2\pi} \rfloor} \left( \pi \lfloor \frac{2\operatorname{Re}(z)-\pi}{2\pi} \rfloor - z \right) & \frac{2\operatorname{Re}(z)+\pi}{2\pi} \in \mathbb{Z} \wedge \operatorname{Im}(z) \leq 0 \\ (-1)^{\lfloor \frac{2\operatorname{Re}(z)+\pi}{2\pi} \rfloor} \left( z - \pi \lfloor \frac{2\operatorname{Re}(z)+\pi}{2\pi} \rfloor \right) & \text{True} \end{cases}$$

## With related functions

### Involving exp

01.06.27.0004.01

$$\sin(z) = \frac{e^{iz} - e^{-iz}}{2i}$$

### Involving cos

01.06.27.0005.01

$$\sin(z) = \cos\left(\frac{\pi}{2} - z\right)$$

01.06.27.0006.01

$$\sin(z) = -\cos\left(\frac{\pi}{2} + z\right)$$

01.06.27.0007.01

$$\sin(z) = -\frac{\sqrt{-z^2}}{z} \sqrt{\frac{\cos(2z) - 1}{2}} \quad ; \operatorname{Im}(z) \neq 0 \wedge |\operatorname{Re}(z)| < \frac{\pi}{2}$$

01.06.27.0008.01

$$\sin(z) = \frac{\sqrt{z^2}}{z} \sqrt{\frac{1 - \cos(2z)}{2}} \quad ; |\operatorname{Re}(z)| < \pi$$

01.06.27.0009.01

$$\sin(z) = \sqrt{\frac{1 - \cos(2z)}{2}} \quad ; 0 < \operatorname{Re}(z) < \pi$$

01.06.27.0010.01

$$\sin(z) = (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor} \sqrt{\frac{1 - \cos(2z)}{2}} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor + \lfloor \frac{-\operatorname{Re}(z)}{\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right)$$

01.06.27.0011.01

$$\sin(z) = -\frac{\sqrt{-z^2}}{z} \sqrt{\cos^2(z) - 1} \quad ; \operatorname{Im}(z) \neq 0 \wedge |\operatorname{Re}(z)| < \frac{\pi}{2}$$

01.06.27.0012.01

$$\sin(z) = \frac{\sqrt{z^2}}{z} \sqrt{1 - \cos^2(z)} \quad ; |\operatorname{Re}(z)| < \pi$$

01.06.27.0013.01

$$\sin(z) = \sqrt{1 - \cos^2(z)} \quad ; 0 < \operatorname{Re}(z) < \pi \vee \operatorname{Re}(z) = 0 \wedge \operatorname{Im}(z) \geq 0 \vee \operatorname{Re}(z) = \pi \wedge \operatorname{Im}(z) \leq 0$$

01.06.27.0014.01

$$\sin(z) = \sqrt{1 - \cos^2(z)} (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor + \lfloor \frac{-\operatorname{Re}(z)}{\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right)$$



$$\sin^2(z) = \frac{1 - \cos(2z)}{2}$$

$$\sin^2(z) = 1 - \cos^2(z)$$

$$\sin^2(z) + \cos^2(z) = 1$$

$$\sin^2(z) - \cos^2(z) = -\cos(2z)$$

$$\sin(z) + i \cos(z) = i e^{-iz}$$

$$\sin(z) - i \cos(z) = -i e^{iz}$$

$$\sin(z) + \cos(z) = \sqrt{2} \sin\left(z + \frac{\pi}{4}\right)$$

$$\sin(z) - \cos(z) = \sqrt{2} \sin\left(z - \frac{\pi}{4}\right)$$

$$a \sin(z) + b \cos(z) = \sqrt{\frac{a^2}{b^2} + 1} b \cos\left(z - \tan^{-1}\left(\frac{a}{b}\right)\right)$$

$$\sin\left(\frac{\pi}{2} + z\right) = \cos(z)$$

$$\sin\left(\frac{\pi}{2} - z\right) = \cos(z)$$

### Involving tan

$$\sin(z) = \frac{2 \tan\left(\frac{z}{2}\right)}{\tan^2\left(\frac{z}{2}\right) + 1}$$

$$\sin(z) = \frac{\tan(z)}{\sqrt{\tan^2(z) + 1}} \quad ; \quad |\operatorname{Re}(z)| < \frac{\pi}{2}$$

$$\sin(z) = \frac{\tan(z)}{\sqrt{\tan^2(z) + 1}} (-1)^{\lfloor \frac{1}{2} - \frac{\operatorname{Re}(z)}{\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} - \frac{1}{2} \rfloor + \lfloor \frac{1}{2} - \frac{\operatorname{Re}(z)}{\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right)$$

01.06.27.0029.01

$$\sin^2(z) = \frac{\tan^2(z)}{\tan^2(z) + 1}$$

### Involving cot

01.06.27.0030.01

$$\sin(z) = \frac{2 \cot\left(\frac{z}{2}\right)}{\cot^2\left(\frac{z}{2}\right) + 1}$$

01.06.27.0031.01

$$\sin(z) = \frac{1}{\sqrt{1 + \cot^2(z)}} \quad ; \quad 0 < \operatorname{Re}(z) < \pi$$

01.06.27.0032.01

$$\sin(z) = \frac{1}{\sqrt{1 + \cot^2(z)}} (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor + \lfloor -\frac{\operatorname{Re}(z)}{\pi} \rfloor \right) \theta(\operatorname{Im}(z)) \right)$$

01.06.27.0033.01

$$\sin^2(z) = \frac{1}{\cot^2(z) + 1}$$

### Involving csc

01.06.27.0034.01

$$\sin(z) = \frac{1}{\operatorname{csc}(z)}$$

### Involving sec

01.06.27.0035.01

$$\sin(z) = \frac{1}{\sec\left(\frac{\pi}{2} - z\right)}$$

01.06.27.0036.01

$$\sin(z) = -\frac{1}{\sec\left(\frac{\pi}{2} + z\right)}$$

01.06.27.0037.01

$$\sin(z) = \frac{\sqrt{z^2} \sqrt{\sec^2(z) - 1}}{z \sec(z)} \quad ; \quad |\operatorname{Re}(z)| < \frac{\pi}{2}$$

01.06.27.0038.01

$$\sin(z) = z \sqrt{-\frac{1}{z^2} \frac{\sqrt{1 - \sec^2(z)}}{\sec(z)}} \quad ; \quad \operatorname{Im}(z) \neq 0$$

01.06.27.0039.01

$$\sin^2(z) = \frac{\sec^2(z) - 1}{\sec^2(z)}$$

### Involving sinh

01.06.27.0040.01

$$\sin(z) = -i \sinh(iz)$$

01.06.27.0041.01

$$\sin(iz) = i \sinh(z)$$

### Involving cosh

01.06.27.0042.01

$$\sin(z) = \cosh\left(\frac{\pi i}{2} - iz\right)$$

01.06.27.0043.01

$$\sin(z) = -\cosh\left(\frac{\pi i}{2} + iz\right)$$

01.06.27.0044.01

$$\sin(z) = \frac{\sqrt{z^2}}{z} \sqrt{\frac{1 - \cosh(2iz)}{2}} \quad ; |\operatorname{Re}(z)| < \pi$$

01.06.27.0045.01

$$\sin(z) = \sqrt{\frac{1 - \cosh(2iz)}{2}} \quad ; 0 < \operatorname{Re}(z) < \pi$$

01.06.27.0046.01

$$\sin(z) = \sqrt{\frac{1 - \cosh(2iz)}{2}} (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor + \lfloor -\frac{\operatorname{Re}(z)}{\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right)$$

01.06.27.0047.01

$$\sin(z) = \frac{\sqrt{z^2}}{z} \sqrt{1 - \cosh^2(iz)} \quad ; |\operatorname{Re}(z)| < \pi$$

01.06.27.0048.01

$$\sin(z) = \sqrt{1 - \cosh^2(iz)} \quad ; 0 < \operatorname{Re}(z) < \pi$$

01.06.27.0049.01

$$\sin(z) = \sqrt{1 - \cosh^2(iz)} (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor + \lfloor -\frac{\operatorname{Re}(z)}{\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right)$$

01.06.27.0050.01

$$\sin^2(z) = 1 - \cosh^2(iz)$$

### Involving tanh

01.06.27.0051.01

$$\sin(z) = \frac{2i \tanh\left(\frac{z}{2}\right)}{\tanh^2\left(\frac{z}{2}\right) - 1}$$

01.06.27.0052.01

$$\sin(z) = -\frac{i \tanh(iz)}{\sqrt{1 - \tanh^2(iz)}} \quad ; |\operatorname{Re}(z)| < \frac{\pi}{2}$$

01.06.27.0053.01

$$\sin(z) = \frac{i \tanh(iz)}{\sqrt{1 - \tanh^2(iz)}} (-1)^{\lfloor \frac{1 - \operatorname{Re}(z)}{2\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} - \frac{1}{2} \rfloor + \lfloor \frac{1 - \operatorname{Re}(z)}{2\pi} \rfloor} \right) \theta(-\operatorname{Im}(z)) \right)$$

01.06.27.0054.01

$$\sin^2(z) = \frac{\tanh^2(iz)}{\tanh^2(iz) - 1}$$

### Involving coth

01.06.27.0055.01

$$\sin(z) = \frac{2i \coth\left(\frac{iz}{2}\right)}{1 - \coth^2\left(\frac{iz}{2}\right)}$$

01.06.27.0056.01

$$\sin(z) = \frac{1}{\sqrt{1 - \coth^2(iz)}} \quad ; 0 < \operatorname{Re}(z) < \pi$$

01.06.27.0057.01

$$\sin(z) = \frac{1}{\sqrt{1 - \coth^2(iz)}} (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor} \left( 1 - \left( 1 + (-1)^{\lfloor \frac{\operatorname{Re}(z)}{\pi} \rfloor + \lfloor -\frac{\operatorname{Re}(z)}{\pi} \rfloor} \right) \theta(\operatorname{Im}(z)) \right)$$

01.06.27.0058.01

$$\sin^2(z) = \frac{1}{1 - \coth^2(iz)}$$

### Involving csch

01.06.27.0059.01

$$\sin(z) = -\frac{i}{\operatorname{csch}(iz)}$$

### Involving sech

01.06.27.0060.01

$$\sin(z) = \frac{1}{\operatorname{sech}\left(\frac{\pi i}{2} - iz\right)}$$

01.06.27.0061.01

$$\sin(z) = -\frac{1}{\operatorname{sech}\left(\frac{\pi i}{2} + iz\right)}$$

01.06.27.0062.01

$$\sin(z) = \frac{\sqrt{z^2} \sqrt{\operatorname{sech}^2(iz) - 1}}{z \operatorname{sech}(iz)} \quad ; |\operatorname{Re}(z)| < \frac{\pi}{2}$$

01.06.27.0063.01

$$\sin(z) = -\frac{\sqrt{-z^2} \sqrt{1 - \operatorname{sech}^2(iz)}}{z \operatorname{sech}(iz)} \quad ; \operatorname{Im}(z) \neq 0$$

$$\sin^2(z) = \frac{\operatorname{sech}^2(iz) - 1}{\operatorname{sech}^2(iz)}$$

## Inequalities

$$\frac{\sin(x)}{x} > \frac{2}{\pi} /; -\frac{\pi}{2} < x < \frac{\pi}{2}$$

$$\sin(x) \leq x /; x \geq 0$$

$$\sin(x) > x \cos(x) /; 0 < x < 4.493409$$

$$\sin(x) \geq x \left(1 - \frac{x}{\pi}\right) /; 0 \leq x \leq \pi$$

$$\sin(x) \leq \frac{4x}{\pi} \left(1 - \frac{x}{\pi}\right) /; 0 \leq x \leq \pi$$

$$|\sin(x)| \leq 1 /; x \in \mathbb{R}$$

$$|\sin(x)| \leq |x| /; x \in \mathbb{R}$$

$$|\sin(z)| \leq \sinh(|z|)$$

$$|\sin(z)| \leq \cosh(\operatorname{Im}(z))$$

$$|\sin(z)| \geq |\sinh(\operatorname{Im}(z))|$$

$$\frac{x(\pi - x)}{\pi} < \sin(x) < x \frac{(\pi - x)(2\pi - x)}{\pi^2} /; x \in \mathbb{R} \wedge 0 < x < \pi$$

## Zeros

$$\sin(z) = 0 /; z = \pi k \wedge k \in \mathbb{Z}$$

## Theorems

### Fourier sin transforms

$$\hat{f}(y) = \int_0^\infty f(x) \sin(xy) dx \Leftrightarrow f(x) = \frac{2}{\pi} \int_0^\infty \hat{f}(y) \sin(xy) dy.$$

**Fourier series**

$$f(x) \sim \frac{a_0}{2} + \sum_{k=1}^\infty a_k \cos\left(\frac{\pi k x}{r}\right) + b_k \sin\left(\frac{\pi k x}{r}\right); a_k = \frac{1}{r} \int_{-r}^r f(t) \cos\left(\frac{\pi k t}{r}\right) dt \wedge b_k = \frac{1}{r} \int_{-r}^r f(t) \sin\left(\frac{\pi k t}{r}\right) dt$$

**De Moivre's theorem**

$$(\cos(z) + i \sin(z))^n = \cos(nz) + i \sin(nz); n \in \mathbb{N}$$

**The law of sines**

For a triangle in the Euclidean plane with edges  $a, b, c$  and opposite angles  $\alpha, \beta, \gamma$ , the following holds:

$$\frac{\sin(\alpha)}{a} = \frac{\sin(\beta)}{b} = \frac{\sin(\gamma)}{c}.$$

**Logistic equation solution**

$y_n = \sin^2((c 2^n \bmod 1) \pi)$  is a closed form for the chaos-exhibiting logistic equation  $y_{n+1} = 4 y_n(1 - y_n)$ .

**Weierstrass-Riemann function  $\Omega(x)$**

Weierstrass-Riemann function  $\Omega(x)$ , which is continuous everywhere but not differentiable at a dense set of points, has the following representation:

$$\Omega(x) = \sum_{k=1}^\infty \frac{\sin(k^2 \pi x)}{k^2 \pi} = \frac{\pi}{4 q^2} \sum_{k=1}^{q-1} \sin\left(\frac{k^2 p \pi}{q}\right) / \sin^2\left(\frac{k \pi}{2 q}\right); x = \frac{p}{q} \wedge p, q \in \mathbb{N} \wedge \gcd(p, q) = 1.$$

**Coriolis force**

The closed form solution of the vector equation  $\frac{\partial^2 \mathbf{r}(t)}{\partial t^2} = \mathbf{g} - 2 \boldsymbol{\omega} \times \frac{\partial \mathbf{r}(t)}{\partial t}$ , describing the movement of a mass point  $\mathbf{r}(t)$  under the gravitational force  $m \mathbf{g}$  and the Coriolis force  $2 m \boldsymbol{\omega} \times \frac{\partial \mathbf{r}(t)}{\partial t}$  and initial conditions  $\mathbf{r}(t) = \mathbf{r}_0$  and  $\partial \mathbf{r}(t) / \partial t |_{t=0} = \mathbf{v}_0$ , is given by

$$\mathbf{r}(t) = \mathbf{r}_0 + \mathbf{v}_0 t + \mathbf{g} \frac{t^2}{2} - \boldsymbol{\omega} \times \left( \frac{2 \sin^2(\omega t)}{2 \omega^2} \mathbf{v}_0 + \frac{2 \omega t - \sin(2 \omega t)}{4 \omega^3} \mathbf{g} \right) + \boldsymbol{\omega} \times \left( \boldsymbol{\omega} \times \left( \frac{2 \omega t - \sin(2 \omega t)}{2 \omega^3} \mathbf{v}_0 + \frac{2 \omega^2 t^2 - 2 \sin^2(\omega t)}{4 \omega^4} \mathbf{g} \right) \right).$$

**Other information**

**Value properties**

01.06.33.0001.01

$$(x \in \mathbb{Q} \wedge \sin(x^\circ) \in \mathbb{Q}) \Rightarrow \left( \sin(x) = 0 \vee \sin(x) = \frac{1}{2} \vee \sin(x) = -\frac{1}{2} \vee \sin(x) = 1 \vee \sin(x) = -1 \right)$$

## History

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- K. Ptolemaeus
- Brahmagupta (c. 630)
- R. de Chesters (1140) translated Abu Ja'far Muhammed ibn Musa al-Khwarizme's works and used the word "sine" (in Latin, "sinus"; al-Khwarizme's name is the source of the word "algorithm")
- J. M. Regiomontanus (1464) and A. Dürer (1525)
- F. Maurolyco (1555) used the notation "sinus"
- E. Gunter (1624) used the notation "sin"
- I. Newton (1665) found a series expansion for sin
- L. Euler (1734) found a product representation
- T. Simpson (1750)

The function sin is encountered often in mathematics and the natural sciences.

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